Full-Duplex Cloud Radio Access Network: Stochastic Design and Analysis

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Abstract—Full-duplex (FD) wireless has emerged as a disruptive communications paradigm for enhancing the achievable spectral efficiency (SE), thanks to the recent major breakthroughs in self-interference (SI) mitigation. The FD versus half-duplex (HD) SE gain, in cellular networks, is however largely limited by the mutual-interference (MI) between the downlink (DL) and the uplink (UL). A potential remedy for tackling the MI bottleneck is through cooperative communications. This paper provides a stochastic design and analysis of FD enabled cloud radio access network (C-RAN) under the Poisson point process (PPP)-based abstraction model of multi-antenna radio units (RUs) and user equipments (UEs). We consider different network- and user-centric approaches towards the formation of finite clusters in the C-RAN. Contrary to most existing studies, we explicitly take into consideration non-isotropic fading channel conditions and finite-capacity fronthaul links. Accordingly, upper-bound expressions for the C-RAN DL and UL SEs, involving the statistics of all intended and interfering signals, are derived. The performance of the FD C-RAN is investigated through the proposed theoretical framework and Monte-Carlo (MC) simulations. According to state-of-the-art system parameters, significant FD versus HD C-RAN SE gains can be achieved in the presence of advanced interference cancellation capabilities and sufficient-capacity fronthaul links.

Index Terms—Cloud radio access network (C-RAN), full-duplex (FD) wireless, multiple-input multiple-output (MIMO), cooperative zero-forcing (ZF) beamforming, spectral efficiency (SE), network-centric clustering, user-centric clustering, non-isotropic fading channels, mutual-interference (MI), successive interference cancellation (SIC), residual self-interference (SI), capacity-limited fronthaul links, system-level analysis.

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I. INTRODUCTION

Full-duplex (FD) communications, that is simultaneous transmission and reception of wireless signals, has emerged as a disruptive solution for enhancing the achievable spectral efficiency (SE) [1]–[3]. In the past, operating in FD mode was deemed unfeasible, due to the overwhelming self-interference (SI) which arises from the bi-directional wireless functionality. In recent years, significant technological advances have been made towards tackling the SI directly in FD mode, using any combination of passive suppression and active cancellation in analog and/or digital domains, see, e.g., [4]–[7]. In point of fact, several protocols and prototypes for FD radios have been successfully implemented in practice, achieving near two-fold increase in SE versus the conventional half-duplex (HD) radios [8]–[10]. On the other hand, it has been shown that the large-scale FD functionality, in the context of cellular networks, is largely limited by the mutual-interference (MI) between the downlink (DL) and the uplink (UL) [11]–[13]. A potential remedy for tackling the MI bottleneck, and hence unlocking the end-to-end benefits of FD operation in cellular networks, may be through cooperative communications.

Cloud radio access network (C-RAN) is a novel cellular network architecture in which the base station (BS) baseband processing and radio-frequency functionalities are decoupled [14], [15]. C-RAN facilitates cooperative wireless communications on a large-scale basis [16], with central processors (CPs) handling the baseband processing and, with the aid of fronthaul links, exchanging information with distributed radio units (RUs), which in turn, provide (for the most part) radio-frequency functionalities. C-RAN has received a great deal of attention in recent years thanks to its ability to address the inter-cell interference phenomenon, and in turn, allowing for higher SE and energy efficiency (EE) performance to be achieved [17]–[19]. In addition, the use of cloud-computing-powered CPs and small-sized low-power RUs is shown to result in significant improvements in terms of deployment cost versus the conventional long-term-evolution (LTE) networks [20], [21]. At the present time, a particular attention is placed on content caching strategies in C-RAN such to further improve the underlying performance measures, such as delay, backhauling, and quality-of-experience (QoE) [22], [23].

A fundamental question hence arises, namely, what is the underlying FD versus HD SE gain in the context of cooperative wireless communications systems, and in particular, C-RAN? This paper takes a step in this direction by providing a stochastic design and analysis of such systems.
A. Related Works

The performance of C-RAN has been analyzed in the literature. In [24], the C-RAN outage probability in the DL was characterized considering a Poisson point process (PPP)-based RU deployment, and the minimum spatial density of RUs required for meeting a target SE was studied. Analytical expressions for the C-RAN outage probability and throughput in the DL were derived considering Matérn Hard-Core point process (MHCPP)-based RU deployment in [25]. In particular, different RU selection schemes, under linear zero-forcing (ZF) precoding, were modeled and compared with one another. Other performance metrics for C-RAN, namely, physical (PHY)-layer security and EE, in the DL, were studied using the PPP-based abstraction model of BSs and RUs in [26]. In particular, it was shown that the integration of massive multiple-input multiple-output (MIMO) assisted macro-cells with C-RAN can greatly improve the secrecy capacity and network EE. Recently in [27], the authors derived explicit expressions for the coverage and rate in DL C-RAN with finite clustering and limited channel knowledge. In particular, the promising potential of C-RAN, even in the presence of finite cooperative clusters and partial feedback, was further confirmed. It is also important to highlight the earlier information-theoretic works on cooperative wireless communications such as [28]–[33].

Several studies on the performance of FD enabled cooperative wireless systems have also been reported in the literature. In [34], an information-theoretic analysis of C-RAN with FD RUs based on the classical Wyner cellular model was provided. In particular, the authors investigated the FD C-RAN DL and UL SEs (versus single-cell processing), considering capacity-limited fronthaul links, successive interference cancellation (SIC) capability at the user equipment (UE) side, and perfect SI cancellation capability at the RU side. In addition, in [35], the authors considered a FD enabled multi-cell network MIMO paradigm, and utilized spatial interference-alignment (IA) towards tackling the MI from the UL operation on the DL performance. In particular, the scaling multiplexing gain of FD versus HD operation in multi-cell network MIMO was characterized in closed-form. On the other hand, the authors in [36], considered a C-RAN scenario in which a single FD UE simultaneously communicates with randomly-deployed HD multi-antenna RUs in the DL and UL directions. The results indicated that with appropriate beamforming and RU association, significant FD versus HD SE gains can be achieved for this particular case, subject to residual SI power being low.

B. Contributions

In this work, we aim to investigate the potential SE gain of FD versus HD operation in the context of C-RAN. To this end, we provide a stochastic design analysis of large-scale cooperative cellular networks using the PPP-based abstraction model of multi-antenna BSs and UEs. To the best of our knowledge, this is the first work that, with the aid of stochastic geometry theory, studies the C-RAN SE performance with FD RUs (relays), equipped with multiple transmit and receive antennas. Apart from the immediately apparent new challenges posed by the FD operation in our setup, our proposed framework differs from the theoretical models (for HD C-RAN) in the existing literature on multiple fronts, as is highlighted below, and throughout this paper.

Here, we consider different network- and user-centric approaches towards the formation of finite clusters in the C-RAN. In the former, the C-RAN comprises fixed non-overlapping clusters, whereas in the latter, (potentially overlapping) clusters are formed around every scheduled UE, respectively. Within any finite cluster, a CP is considered to orchestrate cooperative communications between the RUs and UEs. To our knowledge, this work, as well as the recent contribution in [27] for HD C-RAN, may be viewed as the only stochastic geometry-based models for C-RAN which take into account the impact of inter-cluster interference due to finite clustering. Many related works, on the other hand, consider perfect coordination across all clusters, which is not feasible due to the practical constraints (such as propagation delay).

In this work, in contrast to the existing theoretical studies for C-RAN (e.g., [24]–[27], [34], [36]), we explicitly take into consideration the non-isotropic nature of wireless channels, which inherently arises as a result of cooperative communications. For example, in the context of C-RAN, in each cluster, the channels between the multi-antenna RUs and UEs (which follow from independent PPPs) involve different distance-dependent path-loss parameters. Hence, with cooperative beamforming, the intended and interfering channels, involve non-identically distributed elements. Here, building on the results from [37]–[40], we utilize the Gamma moment-matching technique in order to characterize the distributions of all intended and interfering signals with cooperative ZF beamforming in the FD multi-cluster multi-user C-RAN under consideration.

Cooperative beamforming and resource allocation problems under different fronthaul strategies and constraints in C-RAN have been extensively studied in the optimization-related literature (see, e.g., [16], [41]–[44]). On the other hand, the consideration of finite fronthaul capacity, for the most part, is missing from the existing theoretical C-RAN models (besides the work in [34], for a Wyner-based topology). In this work, we incorporate the impact of capacity-limited fronthaul links in the proposed theoretical framework using cut-set bounds on the achievable capacity [45]. Accordingly, we derive upper-bound expressions for the FD C-RAN DL and UL SEs, in particular, as a main technical contribution of this work, fully accounting for the DL MI (i.e., UE-UE interference), the UL MI (i.e., BS-BS interference), and the post-processing SI.

The validity of the theoretical findings is confirmed through Monte-Carlo (MC) simulations based on state-of-the-art settings of system parameters. The corresponding numerical results highlight the promising potential of FD versus HD operation with regards to the C-RAN SE performance in the presence of advanced interference cancellation capabilities and sufficient-capacity fronthaul links. Our results further show that the underlying SE gains of FD versus HD C-RAN, compared to that in conventional cellular systems, can be significantly higher due to the inherent capabilities of cooperative beamforming in alleviating the network interference.
C. Organization

The remainder of this paper is organized as follows. In Section II, the C-RAN model and operation under consideration is described. The analysis of the C-RAN SE is given in Section III. Numerical results are provided in Section IV. Finally, conclusions are drawn in Section V.

D. Notation

The following notation is used throughout this paper. $X$ is a matrix with $(i,j)$-th element $\{x\}_{i,j}$; $x$ is a vector with $k$-th element $\{x\}_k$; $T$, $\dagger$, and $+$ are the transpose, Hermitian, and pseudo-inverse operations; $j$ is the imaginary unit; $\text{Im}()$ is the imaginary part; $\mathbb{E}_X\{\cdot\}$ is the expectation; $\mathcal{P}(\cdot)$ is the probability; $\mathcal{F}_X(\cdot)$ is the cumulative distribution function (CDF); $\mathcal{P}_X(\cdot)$ is the probability density function (PDF); $\mathcal{M}_X(\cdot)$ is the moment-generating function (MGF); $[x]$ is the modulus; $\|x\|$ is the Euclidean norm; $\mathcal{H}(\cdot)$ is the Heaviside step function; $\delta(\cdot)$ is the Delta function; $\mathbf{I}_{m\times n}$ is the identity matrix; $\text{Null}(\cdot)$ is a nullspace; $\mathcal{CN}(\mu, \sigma^2)$ is the circularly-symmetric complex Gaussian distribution with mean $\mu$ and variance $\sigma^2$; $\Gamma(\cdot)$ and $\Gamma(\cdot, \cdot)$ are the Gamma and incomplete (upper) Gamma functions; $\gamma(k, \theta)$ is the Gamma distribution with shape parameter $k$ and scale parameter $\theta$; and $\text{2F}_1(\cdot, \cdot; \cdot; \cdot)$ is the Gauss hypergeometric function, respectively.

II. System Description

A. Network Topology

In this work, we consider a multi-cluster multi-user C-RAN in which the RUs and UEs are deployed on the two-dimensional (2D) Euclidean space according to independent stationary PPPs $\Phi(d)$ and $\Phi(u)$ with spatial densities $\lambda_d$ and $\lambda_u$, respectively. In the FD C-RAN, each FD RU, equipped with $N(d)$ transmit and $N(u)$ receive antennas, is considered to be serving $K_d(\leq N(d))$ HD DL UEs and $K_u(\leq N(u))$ HD UL UEs, all equipped with single antennas, per resource block. On the other hand, in HD C-RAN, the DL and UL occur over different resource blocks. In what follows, we provide a description for the FD C-RAN. With apparent adjustments, the HD C-RAN model and operation can be depicted. It should be noted the assumption of HD UEs is made due to the inherent restrictions of legacy devices, and the high cost of equipping FD functionality at the UEs, at least in the foreseeable future [46]. Otherwise, the proposed framework can be readily modified to account for FD enabled UEs. It is important to highlight that for the sake of simplicity, in this work, we consider the network nodes to be always-transmitting (i.e., fully-loaded scenario). The results presented in this paper hence correspond to a worst-case scenario in terms of network interference severity. Note that the proposed analytical framework may be extended to account for the impact of the inherent spatial correlations that exist between the network nodes using the methodology from our previous work in [47]. This is however postponed to future work.

B. Finite Clustering

In this work, we consider different network- and user-centric approaches for the formation of the finite clusters in the C-RAN. In the former, the C-RAN comprises disjoint non-overlapping clusters, whereas in the latter, clusters are formed around each scheduled UE. In the case of network-centric clustering, the cooperative RUs jointly serve all UEs in the cluster coverage area (for example, hexagonal-shaped cells). In this sense, the performances of the different UEs, for example one that is located at the cluster-center, versus one that is located at the cluster-edge, are inherently different, i.e., the latter are susceptible to higher out-of-cluster interference versus the former. In the case of user-centric clustering, each UE is served by a subset of its neighboring cooperative RUs (typically BSs with strongest channel strengths). The user-centric clustering approach can hence be viewed as a remedy for tackling the poor performance at the cell-edges. However, the different clusters may be overlapping under the user-centric approach, hence, giving rise to intra-cluster interference. In practice, the user-centric architecture further increases the computational complexity and signaling overhead versus the network-centric approach. Within any finite cluster, a CP is considered to orchestrate cooperative communications between the RUs and UEs.

C. Channel Model

We proceed by defining the different channels. Note that the letters “$g, g, G$” and “$h, h, H$” are accordingly used to distinguish between the effective DL and UL channels, respectively. Moreover, the letters “$f, f, F$” correspond to small-scale channel attenuation, whereas large-scale fading effects are represented using the letter $\beta$. In this work, we consider the residual SI (small-scale) channels are subject to Rician fading with elements distributed according to $\mathcal{CN}(\mu, \xi^2)$. Note that the parameters $\mu$ and $\xi^2$ can be tuned by design or through measurements to capture arbitrary SI cancellation capability [48]. All other (small-scale) fading channels are considered to be Rayleigh distributed with elements following from $\mathcal{CN}(0, 1)$. Moreover, large-scale fading effects are taken into account using the unbounded path-loss model with exponent $\alpha$ ($> 2$), i.e., $\beta_{a,b} = r_{a,b}^{-\alpha}$, where $r_{a,b}$ denotes the Euclidean distance between the nodes $a$ and $b$. Note that the number of cooperative RUs in a cluster $c$ is denoted with $L_c$. The transmit powers of the multi-antenna RUs and UEs are set as $p(d)$ (per-user) and $p(u)$, respectively.

Let $g_{m_1,c_k} = \sqrt{\beta_{m_1,c_k}} f_{m_1,c_k}$, where $f_{m_1,c_k} \in C^1 \times N(d)$ denote the DL channel from the RU $l$ in the cluster $m$ to the UE $k$ in the cluster $c$. The combined DL channel from the $L_m$ cooperative RUs in the cluster $m$ to the UE $k$ in the cluster $c$ is represented using $g_{m,c_k} = [g_{m_1,c_k}]_{1 \leq l \leq L_m} \in C^1 \times N(d)$. The cross-mode channel from the RU $j$ to the RU $b$ in the cluster $c$ is given by $G_{c_j,c_b} = \sqrt{\beta_{c_j,c_b}} F_{c_j,c_b}$, where $F_{c_j,c_b} \in C^{N(u) \times N(d)}$. The residual SI channel of the RU $j$ in the cluster $c$ is denoted with $G_{c_j,c_j} = F_{c_j,c_j} \in C^{N(u) \times N(d)}$ (considering all SI large-scale fading coefficients are equal to one). The channel from the RU $j$ in the cluster $c$ with respect to the cooperating RUs receive antennas in the cluster.
\[ y^{(d)} = \sqrt{p^{(d)}} g_{c,c,c} v_{c,c,c} s_{c,c,c} + \sqrt{p^{(d)}} \sum_{c_k \in \Psi \setminus \{c\}} v_{c,c,c} s_{c,c,c} + \sqrt{p^{(d)}} \sum_{m \in \Psi \setminus \{c\}} g_{m,c,c} V_m s_m \]
\[ \text{intended signal} \]
\[ + \sqrt{p^{(u)}} \sum_{m \in \Psi \setminus \{c\}} h_{m,c,c} s_{m,k} + \eta^{(d)} \]
\[ \text{intra-cluster interference} \]
\[ + \sqrt{p^{(u)}} \sum_{m \in \Psi \setminus \{c\}} h_{m,c,c} s_{m,k} + \eta^{(u)} \]
\[ \text{inter-cluster interference} \]
\[ \text{mutual-interference} \]
\[ y^{(u)} = \sqrt{p^{(u)}} w_{c,c,c} h_{c,c,c} s_{c,c,c} + \sqrt{p^{(u)}} \sum_{c_k \in \Psi \setminus \{c\}} w_{c,c,c} h_{c,c,c} s_{c,c,c} + \sqrt{p^{(u)}} \sum_{m \in \Psi \setminus \{c\}} w_{c,c,c} h_{m,c,c} s_{m,k} \]
\[ \text{intended signal} \]
\[ + \sqrt{p^{(d)}} \sum_{m \in \Psi \setminus \{c\}} w_{c,c,c} G_m V_m s_m + \sqrt{p^{(d)}} w_{c,c,c} G_m V_m s_m + \sqrt{p^{(d)}} w_{c,c,c} \eta^{(u)} \]
\[ \text{intra-cluster interference} \]
\[ \text{residual self-interference} \]
\[ \text{scaled noise} \]
\[ \text{mutual-interference} \]

Here, \( G_{c,c,c} \) represents the channel from the cooperative RUs to the active DL UEs in the cluster \( c \). The combined channel between the cooperating RUs in the cluster \( c \) can be expressed as \( G_{c,c,c} = (G_{c,c,c})_{1 \leq j,k \leq L_c} \in \mathbb{C}^{L_c \times N^{(a)} \times N^{(d)}} \). On the other hand, the cross-mode channel from the RU \( k \) to the cluster \( m \) to the RU \( b \) in the cluster \( c \) is given by \( G_{m,c,b} = \sqrt{\beta_{m,c,b}} F_{m,c,b} \), where \( F_{m,c,b} \in \mathbb{C}^{N^{(a)} \times N^{(d)}} \). We can then express the channel from the RU \( k \) to the cooperative RUs in the cluster \( c \) using \( G_{m,c,c} = (G_{m,c,c})_{1 \leq j,k \leq L_c} \in \mathbb{C}^{L_c \times N^{(a)} \times N^{(d)}} \). Denote the channel from the cooperating RUs in the cluster \( m \) to the cooperating RUs in the cluster \( c \) using \( G_{m,c,c} = (G_{m,c,c})_{1 \leq j,k \leq L_m} \in \mathbb{C}^{L_m \times N^{(a)} \times N^{(d)}} \).

Moreover, we use \( h_{c,k,m} = \sqrt{\beta_{c,k,m}} f_{c,k,m} \), where \( f_{c,k,m} \in \mathbb{C}^{N^{(a)} \times 1} \), to denote the UL channel from the UE \( k \) in the cluster \( c \) to the RU \( m \) in the cluster \( m \). The combined UL channels to the cooperative RUs in the cluster \( m \) to the UE \( k \) in the cluster \( c \) is given by \( h_{c,k,m} = [h_{c,k,m}]_{1 \leq j \leq L_m} \in \mathbb{C}^{L_m \times N^{(a)} \times 1} \). The cross-mode channel from the UL UE \( k \) in the cluster \( m \) to the DL UE \( o \) in the cluster \( c \) is denoted with \( h_{m,k,c} = \sqrt{\beta_{m,k,c}} f_{m,k,c} \).

**D. Baseband Signals**

Let \( G_c = [g_{c,c,k}]_{1 \leq k \leq L_c \times K(d)} \in \mathbb{C}^{L_c \times K(d) \times L_c \times K(d)} \) denote the combined DL channels from the cooperative RUs to the active DL UEs in the cluster \( c \). Moreover, \( s_c = [s_{c,c,k}]_{1 \leq k \leq L_c \times K(d)} \in \mathbb{C}^{L_c \times K(d) \times 1} \), \( \|s_{c,c,k}\|^2 = 1 \), denotes the DL complex symbol vector from the cooperative RUs to the active DL UEs in the cluster \( c \). The normalized linear precoding matrix at the cluster \( c \) is expressed as \( V_c = [v_{c,c,k}]_{1 \leq k \leq L_c \times K(d)} \in \mathbb{C}^{L_c \times N^{(a)} \times L_c \times K(d)} \), \( \|v_{c,c,k}\|^2 = 1 \). The DL received signal for the reference DL active UE \( c_o \) in the cluster \( c \) is given by (1), as shown at the top of this page, where \( \Psi \) is the set of all clusters, \( \Psi^{(d)} \) is the set of active DL UEs in the cluster \( c \), \( \Psi^{(a)} \) is the set of active UL UEs in the cluster \( m \), \( s_{m,k} \) is the information symbol transmitted from active UL UE \( k \) in cluster \( m \), and \( \eta^{(d)} \) is the zero-mean complex additive white Gaussian noise (AWGN) with variance \( \nu^{(d)} \), respectively.

On the other hand, let \( H_e = [h_{c,c,k}]_{1 \leq k \leq L_c \times K(e)} \in \mathbb{C}^{L_c \times N^{(e)} \times L_c \times K(e)} \) represent the collective UL channel from the active UL UEs at the cooperative RUs in the cluster \( c \). The normalized linear decoding matrix at the CP in the cluster \( c \) is given by \( W_e = [w_{c,c,k}]_{1 \leq k \leq L_c \times K(e)} \in \mathbb{C}^{L_c \times K(e) \times L_c \times K(e)} \), \( \|w_{c,c,k}\|^2 = 1 \). The post-processing UL received signal from the reference active UL UE \( c_i \) in the cluster \( c \) is given by (2), as shown at the top of this page, where \( \eta^{(u)} \in \mathbb{C}^{L_c \times N^{(e)} \times 1} \) is the circularly-symmetric zero-mean complex AWGN vector with covariance matrix \( \nu^{(u)}I_{L_c \times N^{(e)}} \).

**E. Cooperative Beamforming**

In the DL, we adopt a cooperative ZF precoder for suppressing intra-cluster interference. The baseband processing is carried out at the CP in each cluster, and the corresponding information is forwarded via fronthaul links to the cooperative RUs. Specifically, in the cluster \( c \), the cooperative ZF beamformer \( V_c \) is set equal to the normalized columns of \( G_c^+ = G_c^T(G_cG_c^T)^{-1} \in \mathbb{C}^{L_c \times N^{(d)} \times L_c \times K(d)} \). Further, in the UL, the signals received at the cooperative RUs from the active UL UEs are compressed, and forwarded via fronthaul links to the CP. The CP, in turn, performs joint decoding. Here, we consider the case where the CP applies a cooperative ZF decoder for suppressing intra-cluster interference in the UL. Specifically, in the cluster \( c \), the normalized rows of \( H_e^+ = (H_e^T H_e)^{-1} H_e^T \) are set equal to the row vectors of \( W_e \).

**F. Interference Cancellation**

In the UL of the FD C-RAN, the RUs may apply SI cancellation, and then forward the received signals to the CP. Prior to performing joint decoding, the CP is considered to cancel the intra-cluster MI in the UL (BS-BS interference) given the DL signals are known to the CP [34]. In the state-of-the-art literature [34], [35], the post-processing SI is considered to have a negligible impact on the FD C-RAN UL SE performance. In this work, we explicitly account for the impact of residual SI with cooperative linear beamforming over multi-user MIMO Rician fading channels. As will later
be shown using numerical examples, the self-interference cancelation capability plays a vital role on the FD C-RAN UL SE performance, thus highlighting the crucial need for a rigorous characterization of the residual SI. Intuitively, without self-interference cancellation, the SI overpowers the UL signals, as a result, the FD operation would not be feasible in practice [5]. Here, we further consider the scenario where the DL UEs may be capable of performing SIC towards mitigating the intra-cluster MI caused by the neighboring UL UEs. The different interference cancellation solutions under consideration hence allow us to focus on the potential benefits of the FD operation.

G. Signals Distributions

We proceed by defining the signal-to-interference-plus-noise ratios (SINRs) in the FD C-RAN under consideration.

The received SINR at the reference active DL UE \( o \) in the cluster \( c \) can be expressed as

\[
\gamma^{(d)} = \frac{\mathcal{X}^{(d)}}{\mathcal{I}^{(d)} + CM\mathcal{I}^{(d)} + \nu^{(d)}}
\]

where \( \mathcal{X}^{(d)} = p^{(d)} \| g_{m,c_o} V_m \|^2 \), \( \mathcal{I}^{(d)} = p^{(u)} \sum_{m \in \Psi} \| g_{m,c_o} V_m \|^2 \), and \( CM\mathcal{I}^{(d)} = p^{(u)} \sum_{m \in \Psi, m_k \in \Psi} \| h_{m_k,c_o} \|^2 \).

On the other hand, in the cluster \( c \), the received UL SINR for the reference active UL UE \( i \) at the CP is given by

\[
\gamma^{(u)} = \frac{\mathcal{X}^{(u)}}{\mathcal{I}^{(u)} + CM\mathcal{I}^{(u)} + RST^{(u)} + \nu^{(u)}}
\]

where \( \mathcal{X}^{(u)} = p^{(u)} \| w_{c_i,c}^H h_{c_i,c} \|^2 \), \( CM\mathcal{I}^{(u)} = p^{(d)} \sum_{m \in \Phi(c)} \| w_{c_i,c}^H G_{m,c} V_m \|^2 \), and \( RST^{(u)} = p^{(d)} \| w_{c_i,c}^H G_{m,c} V_m \|^2 \).

In the case of cooperative beamforming, for example in the C-RAN under consideration, the channels are non-isotropic in nature, given that the links between randomly-located RUs and active UEs involve different path-loss parameters. As a result, it is not possible to derive the exact distributions of the different intended and interfering channel power gains. It has been shown, e.g., in [40], that the Gamma moment-matching technique can be invoked in order to derive approximate expressions for the intended and interfering channel power gains in the case of HD network MIMO. In what follows, we also apply the moment-matching technique to characterize the different channel power gains in the context of FD C-RAN with finite clustering. Note that the average number of cooperating RUs per cluster is denoted with \( L \).

Proposition 1. The DL and UL intended channel power gains with cooperative ZF beamforming in the FD C-RAN under consideration are respectively given by

\[
\| g_{c_i,c_o} V_{c_i,c_o} \|^2 \approx \sum_{c_j \in \Phi(c)} \beta_{c_j,c_o} \psi_{c_j,c_o},
\]

\[
\psi_{c_j,c_o} \sim G \left( N^{(d)} - K^{(d)} + \frac{1}{L}, 1 \right)
\]

and

\[
\| w_{c_i,c}^H h_{c_i,c} \|^2 \approx \sum_{c_j \in \Phi(c)} \beta_{c_j,c} \psi_{c_j,c},
\]

\[
\psi_{c_j,c} \sim G \left( N^{(u)} - K^{(u)} + \frac{1}{L}, 1 \right).
\]

Proposition 2. The DL and UL inter-cluster interference channel power gains with cooperative ZF beamforming in the FD C-RAN under consideration are respectively given by

\[
\| g_{m,c_o} V_m \|^2 \approx \sum_{m_j \in \Phi(c)} \beta_{m_j,c_o} \psi_{m_j,c_o},
\]

\[
\psi_{m_j,c_o} \sim G \left( K^{(d)}, 1 \right)
\]

and

\[
\| w_{c_i,c}^H h_{m_k,c} \|^2 \approx \sum_{c_j \in \Phi(c)} \beta_{m_k,c} \psi_{m_k,c_j},
\]

\[
\psi_{m_k,c_j} \sim G \left( \frac{1}{L}, 1 \right).
\]

Proposition 3. The DL and UL cross-mode interference channel power gains with cooperative ZF beamforming in the FD C-RAN under consideration are respectively given by

\[
| h_{m_k,c_o} |^2 = \beta_{m_k,c_o} \psi_{m_k,c_o}, \quad \psi_{m_k,c_o} \sim G(1, 1)
\]

and

\[
| w_{c_i,c}^H G_{m,c} V_m |^2 \approx \sum_{m_j \in \Phi(c)} \sum_{c_j \in \Phi(c)} \beta_{m_j,c_j} \psi_{m_j,c_j},
\]

\[
\psi_{m_j,c_j} \sim G \left( \frac{K^{(d)}}{L}, 1 \right).
\]

Proposition 4. The UL residual self-interference channel power gain with arbitrary cooperative linear beamforming in the FD C-RAN under consideration is given by

\[
| w_{c_i,c}^H G_{c_i,c} V_{c_i} |^2 \approx \sum_{c_j \in \Phi(c)} \psi_{c_j,c_j}, \quad \psi_{c_j,c_j} \sim G(\kappa, \theta)
\]

where (12) and (13), as shown at the top of the next page.

Proof: See Appendix A.

In general, bounds on the maximum error in the probability distribution obtained through the Gamma moment-matching technique exist [49]. The tightness of the proposed approximate expressions in the paper versus the empirical data however depends on the particular set of system parameters. Nevertheless, it is important to note that the Gamma moment-matching approximation always outperforms the commonly-used isotropic model in terms of goodness of fit versus the empirical non-isotropic fading distribution - while the drawback lies in the more involved analysis due to a certain loss in tractability. In this sense, it may be argued that the Gamma moment-matching approximation provides a reasonable compromise between accuracy and complexity [50]. In Section IV, we will numerically assess the tightness of the proposed approximate expressions versus the empirical data (obtained through MC simulations).
III. C-RAN ANALYSIS

A. Unified Framework

The C-RAN performance depends on the processing and relaying strategies under the finite-capacity fronthaul links. In general, the fronthaul constraint limits the information exchange between the CP and the cooperative RUs. The particular impact, however, significantly varies depending on the fronthaul technology (fiber optic or wireless), communications direction (DL versus UL), etc. For example, in the DL C-RAN, the CP may adopt data-sharing or compression-based relaying strategies. In the former, the fronthaul constraint restricts the cluster size (number of cooperative RUs), whereas in the latter, the capacity-limited fronthaul induces certain compression noise. Similarly, in the UL C-RAN, the impact of fronthaul largely depends on the infrastructure and choice of relaying strategy (e.g., compress-forward versus decode-forward) [16].

In any case, in the context of C-RAN, the achievable information rate between the CP and the RU under a finite-capacity fronthaul link can be upper-bounded according to the information-theoretic cut-set bound [45]. Specifically, the cut-set bound states that the spectral efficiency cannot exceed the minimum of the fronthaul normalized capacity and of the Shannon limit under ideal fronthaul [51]. Considering these bounds are not achievable in general, the study of how close one can get to the cut-set bound in practice would be relevant and interesting. For example, by utilizing distributed source coding-based compression strategies which exploit signal correlation [16]. This is however beyond the scope of this work.

In this work, we consider the case where there exists a per-cell capacity-constrained fronthaul link between the CP and the RU for the relaying of the DL and the UL signals. With equal allocation of normalized (with respect to the available bandwidth) fronthaul capacity among the DL and the UL UEs in the cell, the per-user DL and UL SEs of the fronthaul links between the CP to each cooperative RU in the respective cluster are denoted with $C^{(d)}$ and $C^{(u)}$ (in nat/s/Hz), respectively. Note that $\log(1 + \gamma^{(d)})$ and $\log(1 + \gamma^{(u)})$ respectively denote the C-RAN instantaneous DL and UL per-user SEs (in nat/s/Hz). Hence, we can characterize the C-RAN DL and UL SE upper-bounds in the presence of capacity-limited fronthaul links. Note that $C^{(d)}, C^{(u)} \rightarrow +\infty$ corresponds to the case with unlimited-capacity fronthaul link.

**Theorem 1.** In the FD C-RAN under capacity-limited fronthaul links, the achievable per-user DL and UL SEs (in nat/s/Hz) can be respectively upper-bounded by the cut-set theorem as

$$S^{(d)} \leq \mathbb{E}\left\{ \min \left( \log \left(1 + \gamma^{(d)}\right), C^{(d)} \right) \right\}$$

\begin{equation}
= \int_{0}^{C^{(d)}} \frac{1}{1 + x} \left(1 - F_{\gamma^{(d)}}(x)\right) \, dx \tag{14}
\end{equation}

and

$$S^{(u)} \leq \mathbb{E}\left\{ \min \left( \log \left(1 + \gamma^{(u)}\right), C^{(u)} \right) \right\}$$

\begin{equation}
= \int_{0}^{C^{(u)}} \frac{1}{1 + x} \left(1 - F_{\gamma^{(u)}}(x)\right) \, dx. \tag{15}
\end{equation}

**Proof:** See Appendix B.

The FD C-RAN SE upper-bound expressions under the fronthaul constraint involve the CDFs of the SINRs. In the case of multi-antenna communications over isotropic Rayleigh fading channels, the coverage probability can be calculated in a number of ways, see, e.g., [52]–[54] (the reader is referred to [55] for multi-stream coverage performance analysis). On the other hand, no prior work has derived the SINR distributions in the case of cooperative multi-antenna communications with non-isotropic channels. In this work, we incorporate the Gil-Pelaez inversion theorem to derive, for the first time, explicit expressions for the FD C-RAN DL and UL coverage probabilities over non-isotropic fading channels.

**Theorem 2.** The CDFs of the DL and UL SINRs in the FD C-RAN under consideration are given by

$$F_{\gamma^{(d)}}(x) = \frac{1}{2} - \frac{1}{\pi} \int_{0}^{\infty} \frac{1}{s} \text{Im} \left( \mathcal{M}_{\Theta^{(d)}}(js) \exp(js\nu^{(d)}) \right) \, ds$$

\begin{equation}
= \frac{1}{2} - \frac{1}{\pi} \int_{0}^{\infty} \frac{1}{s} \text{Im} \left( \mathcal{M}_{\Theta^{(d)}}(js) \exp(js\nu^{(u)}) \right) \, ds \tag{16}
\end{equation}

where

$$\mathcal{M}_{\Theta^{(d)}}(js) = \mathcal{M}_{\mathcal{I}^{(d)}}(js) \mathcal{M}_{\mathcal{C}^{(d)}}(js) \mathcal{M}_{\mathcal{X}^{(d)}}(-\frac{js}{x})$$

\begin{equation}
(18)
\end{equation}

and

$$\mathcal{M}_{\Theta^{(u)}}(js) = \mathcal{M}_{\mathcal{I}^{(u)}}(js) \mathcal{M}_{\mathcal{C}^{(u)}}(js) \mathcal{M}_{\mathcal{R}^{(u)}}(js) \times \mathcal{M}_{\mathcal{X}^{(u)}}(-\frac{js}{x}). \tag{19}
\end{equation}

**Proof:** See Appendix C.

Note that in the case of infinite-capacity fronthaul links
(C^{(d)}, C^{(u)} \to +\infty), the C-RAN DL and UL SEs can be obtained by utilizing the computationally-efficient non-direct MGF-based approach from [56], which avoids the need for the computation of the coverage probabilities. This method is highlighted below.

**Theorem 3.** In the FD C-RAN without constraint on the fronthaul capacity, the achievable per-user DL and UL SEs (in nats/Hz) can be respectively expressed as

\[
S^{(d)} = \int_0^\infty \int_0^\infty \frac{1}{1 + x} \left( \frac{1}{2} + \frac{1}{\pi} \int_0^\infty \frac{1}{s} \text{Im} \left( M^{\text{nc}}_{\text{CMZ}^{(d)}}(js) M^{\text{nc}}_{\text{ICZ}^{(d)}}(js) \right) \exp \left( -\frac{js}{x} \right) \text{d}s \right) 2d \text{d}x \text{d}d
\]

and

\[
S^{(u)} = \int_0^\infty \int_0^\infty \frac{1}{1 + x} \left( \frac{1}{2} + \frac{1}{\pi} \int_0^\infty \frac{1}{s} \text{Im} \left( M^{\text{nc}}_{\text{CMZ}^{(d)}}(js) M^{\text{nc}}_{\text{ICZ}^{(d)}}(js) \right) \exp \left( -\frac{js}{x} \right) \text{d}s \right) \frac{2d}{R^2} \text{d}x \text{d}d
\]

**B. Disjoint vs. User-Centric Clustering**

Now we are ready to provide explicit expressions for the FD C-RAN DL and UL per-user SEs under different network- and user-centric clustering approaches. Note that the parameters with superscripts “n/c” and “u/c” correspond to the former and latter cases, respectively. Here, we approximate the disjoint (hexagonal) cluster by a circular region of radius $\mathcal{R}$ with the PDF of the arbitrary distance $r \geq 0$ of the reference user to the cluster center given by $P_r(d) = \frac{2d}{\mathcal{R}^2}$. In the case of user-centric clustering, each scheduled UE is located at the cluster center.

In regards to the FD operation, we characterize the DL MI considering the UEs may be capable of performing SIC. In order to capture performance for general cases, we consider an exclusion region of radius $\mathcal{E}$ when modeling the UE-UE interference. Some special cases include (i) $\mathcal{E} = 0$, a worst-case scenario, without any interference cancellation capability, and (ii) $\mathcal{E} = \mathcal{R}$, a best-case scenario, where the UL intra-cluster signals are successively decoded and suppressed prior to the processing of the DL intended signals. Further, the UL MI (i.e., BS-BS interference) is characterized considering the sum interference from every inter-cluster RU with respect to each intra-cluster RU, all located randomly accordingly to the PPP-based abstraction model.

We proceed by defining the following functions which are subsequently used in the analysis

\[
\Xi(y, \theta, \mathcal{R}) = \sqrt{\mathcal{R}^2 - y^2 \cos^2(\theta)} + y \sin(\theta) \tag{22}
\]

with

\[
S^{(d)} \leq \int_0^\mathcal{R} \int_0^\mathcal{R} \left( \frac{1}{2} + \frac{1}{\pi} \int_0^\infty \frac{1}{s} \text{Im} \left( M^{\text{nc}}_{\text{CMZ}^{(d)}}(js) M^{\text{nc}}_{\text{ICZ}^{(d)}}(js) \right) \exp \left( -\frac{js}{x} \right) \text{d}s \right) 2d \text{d}x \text{d}d
\]

\[
S^{(u)} \leq \int_0^\mathcal{R} \int_0^\mathcal{R} \left( \frac{1}{2} + \frac{1}{\pi} \int_0^\infty \frac{1}{s} \text{Im} \left( M^{\text{nc}}_{\text{CMZ}^{(d)}}(js) M^{\text{nc}}_{\text{ICZ}^{(d)}}(js) \right) \exp \left( -\frac{js}{x} \right) \text{d}s \right) \frac{2d}{\mathcal{R}^2} \text{d}x \text{d}d
\]
Theorem 4 and 5 provide complete solutions for the computation of the FD C-RAN DL and UL SE upper-bounds under different network- and user-centric clustering approaches. In particular, the finite fronthaul capacities, $C^{(d)}$ and $C^{(u)}$, appear as limits of integration in the SE upper-bound expressions in (25), (26), (34), and (35) according to the cut-set theorem. Note that the exclusion region radius $E$ in the UE-UE interference expression in (31) and (40) can be tuned by design or measurements to capture the SIC capability at the reference UE. Further, the UL MI (i.e., BS-BS interference) is explicitly accounted for in (32) and (41). In this work, we have also explicitly accounted for the impact of residual SI on the FD C-RAN UL SE via (33) and (42) with arbitrary Rician fading statistics allowing for the capturing of performance under generalized self-interference cancellation capabilities.

IV. NUMERICAL RESULTS

In this section, we present some numerical examples in order to draw insights into the performance of FD versus HD C-RAN under different settings of system parameters. The density of the RUs is set to be $\lambda^{(d)} = \frac{4}{\pi}$ per km$^2$. The total system bandwidth is $W = 10$ MHz. The corresponding noise variance is set as $\nu^{(d)} = \nu^{(u)} = -174 + 10 \log_{10}(W) = -104$ dBm. The DL (per user) and UL transmit powers are set as 23 dBm and 20 dBm, respectively. The results of the MC simulations are obtained based on 20000 trials in a circular
A. Impact of Interference Cancellation Capability

We study the SE performance of FD and HD C-RANs under different SIC and residual SI cancellation capabilities in Fig. 1. In the DL, we capture the FD C-RAN SE performance of a typical UE under decoding and suppression of different number of intra-cluster UL signals through SIC. In the UL, we consider the case in which the FD RUs experience different post-processing SI channel attenuation. It can be observed that the interference cancellation capability plays a crucial role on the FD C-RAN SE performance. It is however very important to note that the underlying impact largely depends on the particular set of system settings. For example, from Fig. 1, under SIC of one UL stream (out of a possible four), the DL SE performance of FD and HD C-RANs with network-centric clustering are roughly the same. Whereas in the case of a single UE served per RU in the UL, under the same system settings, the FD C-RAN achieves a 84.6% DL SE gain over its HD counterpart. Moreover, from Fig. 1, it can be seen that any significant improvement in FD versus HD C-RAN UL SE occurs for residual SI cancellation of above region of radius 50 km. In order to facilitate comparison between the FD and HD C-RAN paradigms, we consider the SE performance of typical DL and UL HD UEs over two resource blocks. In the HD C-RAN, the DL and the UL occur over different resource blocks, whereas in the FD C-RAN, the DL and the UL run simultaneously over both resource blocks. Note that all results correspond to a chain conserved scenario, where the FD and HD RUs have the same number of transmit and receive radio-frequency (RF) chains.

B. Impact of Cooperation (Cluster Size)

We investigate the impact of cooperation on the FD and HD C-RAN SE gains under different clustering approaches and interference cancellation capabilities in Fig. 2. In the DL, the SE always improves with larger cluster size (L). Furthermore, the FD over HD C-RAN DL SE gain increases in L with SIC capability (successful decoding and cancellation of the UL UE signal). A similar trend can be observed in the UL, where the SE of the HD and FD C-RAN improves as the number of cooperative RUs is increased. Here, the corresponding FD over HD C-RAN UL SE gain improves with increased cooperation (with self-interference mitigation). The highest FD versus HD C-RAN DL and UL SE gains recorded here are 86.4% and 45.1% (with $L = 8$), respectively. It can be observed that the user-centric architecture outperforms the network-centric clustering approach in terms of both DL and UL C-RAN SEs. This is because of enhanced signal strengths and reduced out-of-cluster interference in the former compared to the latter on an average basis. Note that the MC results confirm the validity of the proposed theoretical framework, with the gap in performance mostly stemming from the random per-cluster number of RUs in the MC simulations (versus the average number used in the theoretical analysis).
Fig. 2: Impact of the number of cooperative RUs per cluster on the C-RAN SE performance. System parameters are: $\lambda^{(d)} = \frac{4}{\pi} \text{RU{s}/km}^2$, $\lambda^{(u)} = K^{(u)} \lambda^{(d)} \text{UE{s}/km}^2$, $N^{(d)} = 8$, $N^{(u)} = 8$, $K^{(d)} = 1$, $K^{(u)} = 1$, $p^{(d)} = 0.2 \text{ W}$, $p^{(u)} = 0.1 \text{ W}$, $\nu^{(d)} = \nu^{(u)} = -104 \text{ dBm}$, $\alpha = 4$.

Fig. 3: Impact of the RUs number of antennas on the C-RAN SE performance. System parameters are: $\lambda^{(d)} = \frac{4}{\pi} \text{RU{s}/km}^2$, $\lambda^{(u)} = K^{(u)} \lambda^{(d)} \text{UE{s}/km}^2$, $L = 3$, $K^{(d)} = 1$, $K^{(u)} = 1$, $p^{(d)} = 0.2 \text{ W}$, $p^{(u)} = 0.1 \text{ W}$, $\nu^{(d)} = \nu^{(u)} = -104 \text{ dBm}$, $\alpha = 4$.

C. Impact of the Number of Antennas and Users

Next, we study the FD and HD C-RAN SE performances under different number of transmit/receive antennas at the RUs and number of DL/UL UEs. We capture performance under both network- and user-centric clustering approaches.

In the case of FD C-RAN, we consider the case with SIC and self-interference cancellation capabilities. We can observe, based on the results from Fig. 3, that with higher number of transmit/receive antennas at the RUs, a higher SE can be achieved. Furthermore, the FD over HD SE gain in both DL and UL directions of communications increases in the number
of antennas at the RUs. On the other hand, the FD and HD C-RAN SE performance in the presence of different number of DL/UL users is shown in Fig. 4. It can be observed that the (per-user) SE performance degrades in the number of active users. Furthermore, the FD over HD SE gain in both the DL and the UL is reduced as we increase the number of users served per resource block.

D. Impact of Fronthaul Link SE

We investigate the impact of capacity-limited fronthaul on the FD and HD C-RAN performance in Fig. 5. In the case of HD C-RAN, the fronthaul links are dedicated to either the DL or the UL operation per resource block, whereas in the case of FD C-RAN, the fronthaul capacity is divided equally between the DL and UL operations per resource block. As expected, increasing the fronthaul capacity enhances the C-RAN SE upper-bound performance. Furthermore, the FD over HD C-RAN SE upper-bound gain in both DL and UL increases with greater fronthaul capacity. The capacity of fronthaul links in practice are anticipated to be one or more orders of magnitude greater than the DL or the UL SE [34]. The results from Fig. 5 illustrate that in such cases both FD and HD SE values converge, hence, with sufficient-capacity fronthaul, significant SE gains can be achieved through the FD operation at the RU side. It is important to note that the SE curves under the fronthaul constraint capture the upper-bound performance based on the cut-set theorem. In practice, the achievable SE, depending on the relaying strategy, is further impacted by other factors arising from the finite-capacity fronthaul links (such as compression noise). A rigorous investigation of this aspect is left for future work.

V. CONCLUSIONS

This paper provided a stochastic design and analysis of large-scale C-RAN with FD enabled RUs. Different network- and user-centric approaches for the formation of the finite clusters were considered. We incorporated the notion of non-isotropic fading channels in characterizing the distribution of the different intended and interfering signals power gains. Upper-bound expressions of the C-RAN SE were accordingly derived, in particular, accounting for the impact of finite-capacity fronthaul links, the MI between the DL and the UL, and the residual SI at the FD RUs. Under state-of-the-art system parameters, we showed that in the presence of advanced interference cancellation strategies and sufficient-capacity fronthaul links, the FD over HD SE gain can be enhanced considerably through cooperative communications capabilities of C-RAN.

APPENDIX A

The DL and UL intended channels strengths in the FD C-RAN can be respectively expressed as $\|g_{c,i,c}\|^2 = \sum_{i \in \Phi} \beta_{c,i,c} \|f_{c,i,c}\|^2$ and $\|h_{c,i,c}\|^2 = \sum_{i \in \Phi} \beta_{c,i,c} \|f_{c,i,c}\|^2$. Through applying the Gamma moment-matching technique [40], we can respectively obtain $\|g_{c,i,c}\|^2 \approx \gamma(\kappa_{c,i,c},\theta_{c,i,c})$ and $\|h_{c,i,c}\|^2 \approx \gamma(\kappa_{c,i,c},\theta_{c,i,c})$ where $\kappa_{c,i,c} \triangleq N(\theta_{c,i,c})/\sum_{i \in \Phi} \beta_{c,i,c}$, $\theta_{c,i,c} = (\sum_{i \in \Phi} \beta_{c,i,c}^2)/(\sum_{i \in \Phi} \beta_{c,i,c})$, $\kappa_{c,i,c} \triangleq N(\theta_{c,i,c})/\sum_{i \in \Phi} \beta_{c,i,c}$, and $\theta_{c,i,c} \triangleq (\sum_{i \in \Phi} \beta_{c,i,c}^2)/(\sum_{i \in \Phi} \beta_{c,i,c})$. Next, by invoking the approach from [57], we assume that the DL and UL intended channels are isotropic with
approximate distributions $g_{c,c_o} \approx \mathcal{G}(0, \theta_{c,c_o} I_{L_c N(v)})$ and $h_{c,c} \approx \mathcal{G}(0, \theta_{c,c} I_{L_c N(v)})$, respectively. It can be shown that the DL and UL cooperative ZF beamforming spaces in the cluster $c$ are respectively $L_c(N^{(d)} - \kappa^{(d)}) + 1$ and $L_c(N^{(u)} - \kappa^{(u)}) + 1$ dimensional [58]. Hence, when projecting the intended DL and UL channels onto the cooperative ZF precoding and decoding subspaces, we consider each spatial dimension (i.e., antenna) respectively adds $\frac{x_{c,c_o}}{L_c N(v)}(L_c(N^{(d)} - \kappa^{(d)}) + 1)$ and $\frac{x_{c,c}}{L_c N(v)}(L_c(N^{(u)} - \kappa^{(u)}) + 1)$ to the corresponding Gamma distributed channel power gains. Hence, we can approximate the DL and UL channel power gains using equivalent distributions $|g_{c,c_o} \nu_{c,c_o}|^2 \approx \sum_{c_j \in \psi_{c_o}} \beta_{c,c_o} \psi_{c,c_o} \sim \mathcal{G}(N^{(d)} - \kappa^{(d)} + \frac{1}{L_c}, 1)$ and $|h_{c,c} \nu_{c,c}|^2 \approx \sum_{c_j \in \psi_{c}} \beta_{c,c} \psi_{c,c} \sim \mathcal{G}(N^{(u)} - \kappa^{(u)} + \frac{1}{L_c}, 1)$, respectively. To facilitate stochastic performance analysis, we further approximate the DL and UL intended channel power gains based on the average number of cooperating RUs in each cluster, $L$.

The channel power gain for the DL inter-cluster interference is derived using a similar approach to that described above. We characterize the DL inter-cluster interference channel strength using Gamma moment-matching. Then, the corresponding channel, approximated via an isotropic distribution, is projected onto the one-dimensional interference vector space. Furthermore, under the assumption of inter-cluster precoding matrices having independent column vectors [59], we approximate the respective channel power gain using the Gamma distribution, with each aggregate inter-cluster channel contributing $\kappa^{(d)}$ to the shape parameter. The channel power gain of the UL inter-cluster interference can be readily derived using the same approach, with each link between the UL UE interferer to a cooperating RU in the reference cluster contributing $\frac{1}{L}$ to the corresponding Gamma distributed channel power gain shape parameter.

The cross-mode channels between the UL and DL UEs in the FD C-RAN are isotropic in nature, as there is no coordination among the UEs. Hence, we can readily express the corresponding channel power gains by separating the small- and large-scale fading effects as in (9). On the other hand, the cross-mode channels between the RUs, involve the squa red norm of a vector with each element being a sum of non-identically distributed random variables, i.e., in the form $\|wGV\|^2$, where $w$, $G$, and $V$ denote the decoding vector, MIMO fading channel, and precoding matrix, respectively. In a recent contribution in [48], we provided a unified approximate expression for the distribution of $\|wGV\|^2$, considering arbitrary linear beamforming design, and isotropic MIMO channels. By invoking the assumption that the precoding matrices have independent columns, and using a similar moment-matching technique described previously, we can approximate the cross-mode interference channel power gain between two clusters. The corresponding Gamma distribution is from the aggregation of the power of each link between a RU (from an interfering cluster) transmit antennas to a RU receive antennas (in the reference cluster). Hence, we can arrive at the expression in (10).

The post-processing SI can be characterized using a similar approach to that described above. The main difference, here, lies in the fact that the residual SI MIMO channel at each RU is Rician distributed with arbitrary statistics (which can
be tuned by design or measurement to capture different self-interference cancellation capabilities \([48]\)). Considering that the CP can remove the intra-cluster BS-BS interference prior to performing joint decoding (given the DL signals are known to the CP), the residual SI channel power gain from the cooperative RUs can be formulated as in (11).

Hence, we arrive at Propositions 1-4.

**APPENDIX B**

Consider \(\mathbb{E}\{\min(\log(1 + \gamma), C)\}\), where \(C\) is a non-negative constant constraint (e.g., backhaul or fronthaul SE) on the achievable capacity. This expectation can be equivalently expressed using the complimentary CDF of the SINR as

\[
\mathbb{E}\{\min(\log(1 + \gamma), C)\} \overset{(i)}{=} \int_0^\infty \left(1 - F_{\min(\log(1 + \gamma), C)}(\tau)\right) d\tau
\]

\[
= \int_0^\infty \left(1 - F_{\log(1 + \gamma)}(\tau - C) + F_{\log(1 + \gamma)}(C, \tau, \tau')\right) d\tau
\]

\[
= \int_0^C \mathcal{F}(\log(1 + \gamma) > \tau) d\tau \overset{(v)}{=} \int_0^C \frac{1}{1 + x} \mathcal{F}(\gamma > x) \ dx
\]

where (i) follows from expressing the average of a non-negative continuous random variable using its complementary CDF, i.e., \(\mathbb{E}\{X\} = \int_0^\infty \mathcal{F}(X > x) \ dx\); (ii) is written using the well-known expression \(F_{\log(1 + \gamma)}(\tau - C) = F_{\log(1 + \gamma)}(C, \tau, \tau')\) where \(Z = \min(X, Y)\); (iii) is obtained considering the constant parameter \(C\) has a CDF of \(F_C(\tau) = \mathcal{H}(\tau - C)\); (iv) holds since \(\mathcal{H}(\tau - C) = 0\) for \(\tau < C\) and \(\mathcal{H}(\tau - C) = 1\) for \(\tau \geq C\); and finally we arrive at (v) using a substitution of variables with \(x = \exp(\tau) - 1\).

Hence, we arrive at Theorem 1.

**APPENDIX C**

Consider the general SINR expression \(\gamma = \sum_i \frac{X}{I_i + \nu}\). The CDF of \(\gamma\) can hence be formulated as

\[
F_\gamma(x) = \mathcal{F}(\gamma \leq x) = \mathcal{F}\left(\sum_i \frac{X}{I_i + \nu} \geq x\right)
\]

\[
\overset{(i)}{=} \mathcal{F}\left(\Theta \geq -\nu\right) \quad (C.1)
\]

where \(\Theta \triangleq \sum_i \frac{X}{I_i} - \frac{X}{\nu}\). By applying the Gil-Pelaez inversion theorem \([60]\)

\[
\mathcal{F}(\Theta \geq -\nu) = \frac{1}{2} - \frac{1}{\pi} \int_0^{+\infty} \frac{1}{s} \text{Im} \left(\mathcal{M}_\Theta(js) \exp(js\nu)\right) ds.
\]

\[(C.2)\]

Using the above result, and with the MGF of \(\Theta\), in the case that \(X, \forall I_i\) are independent, we arrive at Theorem 2.

**APPENDIX D**

In the case of network-centric clustering, a typical user location is a random variable following a uniform distribution in the corresponding cluster area. The statistics of the DL intended signal in the FD C-RAN under network-centric clustering can be derived as

\[
\mathcal{M}_{\lambda^{(\text{d})}}^{\text{wc}}(z) = \mathbb{E}\left\{\exp(-z\lambda^{(\text{d})})\right\}
\]

\[
= \mathbb{E}\left\{\exp(-zp^{(\text{d})} |g_{c,e}v_{c,e}|^2)\right\}
\]

\[\overset{(i)}{=} \mathbb{E}\left\{\exp(-zp^{(\text{d})} \sum_{c_j \in \Phi^{(\text{d})}} \beta_{c_j,e} \psi_{c_j,e}^2)\right\}
\]

\[\overset{(ii)}{=} \prod_{c_j \in \Phi^{(\text{d})}} \mathbb{E}_{\psi_{c_j,e}} \left\{\exp(-zp^{(\text{d})} \beta_{c_j,e} \psi_{c_j,e}^2)\right\}
\]

\[\overset{(iii)}{=} \prod_{c_j \in \Phi^{(\text{d})}} \left(1 + zp^{(\text{d})} \beta_{c_j,e}\right)^{-\left(N^{(\text{d})} - K^{(\text{d})} + \frac{1}{z}\right)}
\]

\[\overset{(iv)}{=} \exp\left(-\lambda^{(\text{d})} \int_0^{2\pi} \int_0^{\pi} \mathcal{F}^{(y, \theta)}(1 - \left(1 + zp^{(\text{d})} \rho^{-a}\right)^{-\left(N^{(\text{d})} - K^{(\text{d})} + \frac{1}{z}\right)}) \ dr \ d\theta\right)
\]

\[(D.1)\]

where (i) follows from Proposition 1; (ii) is from the independence property of PPP and uncorrelated channel conditions; (iii) is obtained through the MGF a Gamma random variable, i.e., for \(X \sim \mathcal{G}(P, Q)\), we have \(\mathbb{E}_X\{\exp(-zX)\} = (1 + zQ)^{-P}\); (iv) is written using the probability generating functional (PGFL), i.e., for a stationary PPP \(\Phi\) with density \(\lambda\), we have \(\mathbb{E}_\Phi\{\prod_{x \in \Phi} f(x)\} = \exp(-\lambda \int_{\mathbb{R}^2} (1 - f(x)) \ dx)\), and converting from Cartesian to polar coordinates (with Jacobian \(r\)), where considering a circular cluster of radius \(R\), the distance between a typical RU-UE pair with an angle \(\theta\) range from zero to \(\Xi(y, \theta) \triangleq \sqrt{R^2 - y^2 \cos^2(\theta) + y \sin(\theta)}\); and finally, we arrive at (27) by adopting the integral identity \(\int_{\Xi(y, \theta)} \left(1 - (1 + zp^{(\text{d})} \rho^{-a})^Q\right)^{-P} \ dr \ d\theta = \frac{2\pi}{T} \left(1 - \frac{2}{\pi^{2/2}} \left(\frac{T^{2}}{T^{2} + 1}\right)^{P} \right) 2F_1\left(1, P + \frac{a}{2}; P + \frac{a}{2} + 1; \frac{T^2}{T^2 + 1}\right)\).

Using the same methodology, the statistics of the UL intended signal is given by

\[
\mathcal{M}_{\lambda^{(\text{a})}}^{\text{wc}}(z) = \mathbb{E}\left\{\exp(-z\lambda^{(\text{a})})\right\}
\]

\[
= \mathbb{E}\left\{\exp(-zp^{(\text{a})} |w_{c,e}h_{c,e}|^2)\right\} = (28).
\]

**APPENDIX E**

Moreover, the DL ICI in the FD C-RAN under network-centric clustering is given by

\[
\mathcal{M}_{\mathcal{I}^{(\text{d})}}^{\text{wc}}(z) = \mathbb{E}\left\{\exp(-z\mathcal{I}^{(\text{d})})\right\}
\]

\[
= \mathbb{E}\left\{\exp(-zp^{(\text{d})} \sum_{m \in \Phi(\text{d})} ||g_{m,e}v_{m,e}||^2)\right\}
\]

\[\overset{(i)}{=} \mathbb{E}\left\{\exp(-zp^{(\text{d})} \sum_{m \in \Phi(\text{d})} \sum_{j \in \Phi(\text{d})} \beta_{mj,e} \psi_{mj,e}^2)\right\}
\]
where (i) holds under Proposition 2; (ii) follows from the aggregate interference from inter-cluster RUs being equivalent in distribution to the total interference generated by PPP-based RUs that are independently transmitting outside the circular ball \(B(\mathcal{R})\) of radius \(\mathcal{R}\); and (29) is obtained by using the integral identity \(\mathcal{F}_2(z, p, \alpha, \mathcal{P}, Q, T) \triangleq \int_T^{\infty} \left(1 - (1 + z p r^{-\alpha})^{-\mathcal{P}}\right) r \, dr = \frac{1}{2} T^2 \left(2 F_3 - \frac{2}{\mathcal{P}} \mathcal{P} - 1; 1 - 2; -\frac{T^2}{\mathcal{P}}\right)\).

The UL ICI statistics in the FD C-RAN under network-centric clustering is given by

\[
\mathcal{M}^{\text{IC}}_{\text{IC}c}(z) \triangleq \mathbb{E} \left\{ \exp \left(-z \mathcal{I} \mathcal{C}(u) \right) \right\} \\
= \mathbb{E} \left\{ \exp \left(-z p(u) \sum_{m \in \Psi(u)} \sum_{c_m \in \Psi_m(u)} |\mathbf{w}_{c_m}^T \mathbf{h}_{m_c,c}|^2 \right) \right\} \\
\approx \mathbb{E} \left\{ \exp \left(-z p(u) \sum_{c_l \in \Phi(u)} \sum_{c_k \in \Phi(c_l)} \beta_{k,c_l} \psi_{k,c_l} \right) \right\} \\
= \mathbb{E} \left\{ \prod_{c_l \in \Phi(u)} \mathbb{E}_{\psi_{c_l}} \left\{ \prod_{k \in \Phi(u)} \frac{\mathbb{E}_{\psi_{c_l},c_k} \left\{ \exp \left(-z p(u) \beta_{k,c_l} \psi_{k,c_l} \right) \right\} }{\exp \left(-z p(u) \beta_{k,c_l} \psi_{k,c_l} \right) \right\} \right\} \right\} \\
= \mathbb{E} \left\{ \prod_{c_l \in \Phi(u)} \mathbb{E}_{\psi_{c_l}} \left\{ \prod_{k \in \Phi(u)} \frac{\mathbb{E}_{\psi_{c_l},c_k} \left\{ \exp \left(-z p(u) \beta_{k,c_l} \psi_{k,c_l} \right) \right\} }{\exp \left(-z p(u) \beta_{k,c_l} \psi_{k,c_l} \right) \right\} \right\} \right\} \\
= \mathbb{E} \left\{ \exp \left(-2 \pi \lambda(u) \int_0^{\infty} \left(1 - (1 + z p r^{-\alpha})^{-\mathcal{P}}\right) r \, dr \right) \right\} \\
= \mathbb{E} \left\{ \exp \left(-z p(u) \sum_{m \in \Psi(u)} \sum_{c_m \in \Psi_m(u)} \beta_{m,c,m} \psi_{m,c,c} \right) \right\} \\
= \mathbb{E} \left\{ \exp \left(-z p(u) \sum_{c_l \in \Phi(u)} \sum_{c_k \in \Phi(c_l)} \beta_{k,c_l} \psi_{k,c_l} \right) \right\} \\
= \mathbb{E} \left\{ \prod_{c_l \in \Phi(u)} \mathbb{E}_{\psi_{c_l}} \left\{ \prod_{k \in \Phi(u)} \frac{\mathbb{E}_{\psi_{c_l},c_k} \left\{ \exp \left(-z p(u) \beta_{k,c_l} \psi_{k,c_l} \right) \right\} }{\exp \left(-z p(u) \beta_{k,c_l} \psi_{k,c_l} \right) \right\} \right\} \right\} \\
= \mathbb{E} \left\{ \exp \left(-2 \pi \lambda(u) \int_0^{\infty} \left(1 - (1 + z p r^{-\alpha})^{-\mathcal{P}}\right) r \, dr \right) \right\} \\
= \mathbb{E} \left\{ \exp \left(-z p(u) \sum_{m \in \Psi(u)} \sum_{c_m \in \Psi_m(u)} \beta_{m,c,m} \psi_{m,c,c} \right) \right\} \\
= \mathbb{E} \left\{ \exp \left(-z p(u) \sum_{c_l \in \Phi(u)} \sum_{c_k \in \Phi(c_l)} \beta_{k,c_l} \psi_{k,c_l} \right) \right\} \\
= \mathbb{E} \left\{ \prod_{c_l \in \Phi(u)} \mathbb{E}_{\psi_{c_l}} \left\{ \prod_{k \in \Phi(u)} \frac{\mathbb{E}_{\psi_{c_l},c_k} \left\{ \exp \left(-z p(u) \beta_{k,c_l} \psi_{k,c_l} \right) \right\} }{\exp \left(-z p(u) \beta_{k,c_l} \psi_{k,c_l} \right) \right\} \right\} \right\} \\
= \mathbb{E} \left\{ \exp \left(-2 \pi \lambda(u) \int_0^{\infty} \left(1 - (1 + z p r^{-\alpha})^{-\mathcal{P}}\right) r \, dr \right) \right\} \\
= \mathbb{E} \left\{ \exp \left(-z p(u) \sum_{m \in \Psi(u)} \sum_{c_m \in \Psi_m(u)} \beta_{m,c,m} \psi_{m,c,c} \right) \right\} \\
= \mathbb{E} \left\{ \exp \left(-z p(u) \sum_{c_l \in \Phi(u)} \sum_{c_k \in \Phi(c_l)} \beta_{k,c_l} \psi_{k,c_l} \right) \right\} \\
= \mathbb{E} \left\{ \prod_{c_l \in \Phi(u)} \mathbb{E}_{\psi_{c_l}} \left\{ \prod_{k \in \Phi(u)} \frac{\mathbb{E}_{\psi_{c_l},c_k} \left\{ \exp \left(-z p(u) \beta_{k,c_l} \psi_{k,c_l} \right) \right\} }{\exp \left(-z p(u) \beta_{k,c_l} \psi_{k,c_l} \right) \right\} \right\} \right\} \\
= \mathbb{E} \left\{ \exp \left(-2 \pi \lambda(u) \int_0^{\infty} \left(1 - (1 + z p r^{-\alpha})^{-\mathcal{P}}\right) r \, dr \right) \right\} \\
= \mathbb{E} \left\{ \exp \left(-z p(u) \sum_{m \in \Psi(u)} \sum_{c_m \in \Psi_m(u)} \beta_{m,c,m} \psi_{m,c,c} \right) \right\} \\
= \mathbb{E} \left\{ \exp \left(-z p(u) \sum_{c_l \in \Phi(u)} \sum_{c_k \in \Phi(c_l)} \beta_{k,c_l} \psi_{k,c_l} \right) \right\} \\
= \mathbb{E} \left\{ \prod_{c_l \in \Phi(u)} \mathbb{E}_{\psi_{c_l}} \left\{ \prod_{k \in \Phi(u)} \frac{\mathbb{E}_{\psi_{c_l},c_k} \left\{ \exp \left(-z p(u) \beta_{k,c_l} \psi_{k,c_l} \right) \right\} }{\exp \left(-z p(u) \beta_{k,c_l} \psi_{k,c_l} \right) \right\} \right\} \right\} \\
= \mathbb{E} \left\{ \exp \left(-2 \pi \lambda(u) \int_0^{\infty} \left(1 - (1 + z p r^{-\alpha})^{-\mathcal{P}}\right) r \, dr \right) \right\} \\
= \mathbb{E} \left\{ \exp \left(-z p(u) \sum_{m \in \Psi(u)} \sum_{c_m \in \Psi_m(u)} \beta_{m,c,m} \psi_{m,c,c} \right) \right\} \\
= \mathbb{E} \left\{ \exp \left(-z p(u) \sum_{c_l \in \Phi(u)} \sum_{c_k \in \Phi(c_l)} \beta_{k,c_l} \psi_{k,c_l} \right) \right\} \\
Hence, we have (39), (40), (41), and (42).

Moreover, the DL ICI in the FD C-RAN under user-centric clustering can be obtained as

\[
\mathcal{M}^{UC}_{ICL} (z) = E \left\{ \exp \left( -z ICL^{(u)} \right) \right\} = E \left\{ \exp \left( -z p^{(d)} \left\| g_{m,c} V_m \right\|^2 \right) \right\} \approx \exp \left( -\pi \lambda (d) \int_{\mathcal{R}} \left( 1 - (1 + z p^{(d)} r^{-\alpha}) - \mathcal{K}^{(d)} \right) r \, dr \right) = (38). \tag{E.3}
\]

The above should be viewed as an upper-bound approximation given that under user-centric clustering, the cooperative RU's may be serving different UEs, hence, there may exist certain intra-cluster interference.

It can be shown that the DL cross-mode interference as well as the different UL interference terms are equivalent in distribution under network- and user-centric clustering approaches. Hence, we have (39), (40), (41), and (42).

Hence, we arrive at Theorem 5. ■

### References


