Several recent projects have demonstrated the safety of a program characterizes the internals of the next component. For example, the network communication stack, such as TCP/IP; the operating-system kernel that implements (e.g.) virtual-memory protection and process preemption; the network communication stack, such as TCP/IP; crypto primitives, such as AES or RSA; crypto protocols built atop these primitives; compilers that translate all of the above to machine language; RTL (register-transfer language) implementations of that machine language; netlist (logic gates) implementations of the RTL.

The systems we use today are built in a modular way from components, software/hardware processes, and layers such as I describe. An engineer working or an expert analyzing at one of these layers (or in one of these components) will not want to know much, will not be able to know much, about the internals of the next component. For example, the network-stack experts don't want to be optimizing-compiler experts, who don't want to be cryptographers. That fractioning of knowledge is essential, otherwise we could not put together the big and capable systems that we enjoy today.

But how can we come to trust such a big system built from diverse components? Must there inevitably be bugs and vulnerabilities, so that the hacker or the Nation-State Attacker can always get in?

I will argue that:
1) We can gain a substantial basis for trust—we can substantially improve the security of our systems—by using end-to-end, modular, deductive program verification of all of these components.
2) The verifications must be done in different domains: program logic or program refinement to prove that concrete programs correctly implement abstract algorithms; application-domain reasoning to prove that abstract algorithms accomplish our goals.
3) A higher-order pure functional programming language is a particularly effective way of expressing functional specifications for modular program verification.
4) One can connect these different styles of verification together with no specification gaps, by embedding all of the different verification methods into a single general-purpose logic.

I. INTRODUCTION

Computer systems are built from numerous software and hardware components. These components may be buggy or malicious, so it is standard practice to have a trusted kernel that enforces protection mechanisms, to guarantee that bugs (or maliciousness) of one component cannot propagate to others.

But a trusted kernel itself may be very large. It may include
1) the operating-system kernel that implements (e.g.) virtual-memory protection and process preemption;
2) the network communication stack, such as TCP/IP;
3) crypto primitives, such as AES or RSA;
4) crypto protocols built atop these primitives;
5) compilers that translate all of the above to machine language;
6) RTL (register-transfer language) implementations of that machine language;
7) netlist (logic gates) implementations of the RTL.

II. STATIC ANALYSIS VS. FUNCTIONAL CORRECTNESS

Many static analysis tools—commercially available or in academic/industrial research—check safety or liveness properties of programs. Some are sound (if they assert a safety property then every execution of the program must indeed be safe), some are unsound. Such tools can be very useful in the software engineering process to reduce the bug count and increase reliability. Especially the sound tools have application in computer security: for example, the Java typechecker (bytecode verifier) or a software fault isolator (SFI) can guarantee that untrusted code cannot escape its sandbox even in the absence of hardware memory protection.\(^1\) Sound static analysis tools are one kind of formal-methods verification.

Should we static-analyze the OS kernel, crypto library, bytecode verifier? Perhaps, but it’s not enough. These protection mechanisms exist to separate client programs from each other, and to protect system code from client programs. To do this, the protection mechanisms must be not only safe but also correct. It is not enough that the OS kernel or crypto library has no buffer overruns: it must also compute the right answer. Therefore, an important application of formal machine-checked functional-correctness verification is for systems code that implements protection mechanisms.

III. FUNCTIONAL SPECIFICATIONS IN FUNCTIONAL LANGUAGES?

A functional specification of a program characterizes the program’s observable behavior. In this section I will discuss

\(^1\)One can even do machine-checked verification of the soundness of a type-based [1] or SFI-based [17] sandboxer.
two different approaches to functional specs: mathematical relations, and functional programs. Consider this C program,

```c
int minimum(int a[], int n) {
    int i, min;
    min = a[0];
    for (i = 0; i < n; i++)
        if (a[i] < min) min = a[i];
    return min;
}
```

with these three different functional specifications. The notation array $a \sigma$ means, “program variable $a$ is an array whose current contents are the sequence $\sigma$.”

**Specification A:**

$\forall \sigma : \text{list}(\mathbb{Z}).$

precondition : $\{ \sigma | n > 0 \land \text{array } a \sigma \}$

postcondition : $\{ \forall j. 0 \leq j < n \rightarrow \text{ret} \leq \sigma_j \}$

**Specification B:**

$\forall \sigma : \text{list}(\mathbb{Z}).$

precondition : $\{ \sigma | n > 0 \land \text{array } a \sigma \}$

postcondition : $\{ \exists i. 0 \leq i < n \land \text{ret} = \sigma_i \land \forall j. 0 \leq j < n \rightarrow \text{ret} \leq \sigma_j \}$

**Specification C:**

function fold $(f : \alpha \rightarrow \beta \rightarrow \beta)$ $(b : \beta)$ $(a : \text{list}(\alpha)) : \beta =$

match al with nil $\Rightarrow$ b | a::ar $\Rightarrow$ f a (fold $f$ b ar) end

function min $(i : \mathbb{Z})$ $(j : \mathbb{Z}) : \mathbb{Z} =$

if $i < j$ then i else j

function hd $(d : \alpha)$ $(a : \text{list}(\alpha)) : \alpha =$

match al with nil $\Rightarrow$ d | a::ar $\Rightarrow$ a end

IN

$\forall \sigma : \text{list}(\mathbb{Z}).$

precondition : $\{ \sigma | n > 0 \land \text{array } a \sigma \}$

postcondition : $\{ \text{ret} = \text{fold min} (\text{hd } 0 \sigma) \}$

Specs A and B characterize some mathematical relations between the input and the output. You might notice that Spec B is stronger. Spec A just ensures the return value is $\leq$ all elements of the array, without necessarily being one of the elements. Does that mean Spec B is better than Spec A? Perhaps not; perhaps property A is all that the client needs.

Spec C says, “the program computes exactly this function.” Now, any program that satisfies Spec C will also satisfy Specs A and B; that’s straightforward to prove, using the simple semantics of the ML-like functional language in which fold, min, and hd are written.

That is, Spec C is at least as strong as A or B. In fact, any specification written in this style must have a strongest-possible postcondition. That’s because the functional language we use is deterministic and total—if it typechecks then it can’t go wrong and must compute a single unique result.

Is that a good thing? One might think, not necessarily:

- Perhaps property A is all the client needs; are B and C overkill?
- Specification C looks verbose.
- What if my program doesn’t have a deterministic semantics?

Even so, experience in many projects has shown that writing functional specs in functional languages is very effective indeed. These projects use a three-level approach:

- domain-specific properties
- pure functional program
- refinement proof
- imperative program
- compiler-correctness proof
- machine-language program

The reason this strategy often works so well is that it modularizes the proof effort. The refinement proof can focus on programming, the relation between some clumsy low-level language (such as C, Java, or assembly language) and how it implements a given function. In this proof, domain knowledge about the mathematics of the application domain is often not necessary; all the domain knowledge can go in the high-level proof about properties of the functional program.

With this method, it’s crucial to have a functional language that’s easy to reason about formally, i.e., a language with a clean proof theory. Successful examples are,

- Gallina, the functional language embedded in the CiC logic of the Coq proof assistant.
- HOL-fun, (the name I will use to refer to) the pure functional language embedded in the higher-order logic of the Isabelle/HOL proof assistant.\(^2\)
- ACL, Applicative Common Lisp, the pure functional Lisp used in ACL2 (A Computational Logic for Applicative Common Lisp).

Later (§VI) I will argue that first-order logics such as ACL2 are insufficiently modular.

### IV. Examples

Researchers around the world have accomplished full functional correctness verifications of protection mechanisms, employing principles of end-to-end, modular, deductive program verification with respect to functional specifications. The results I list here all use a functional program as a refinement layer in the proof.

**CertikOS:** Hypervisor kernel, implemented in C and proved correct in Coq, by multilayer contextual refinement proofs between Gallina functional specifications and C operational semantics [14]. Then the Gallina specs are shown to enjoy correctness properties: process (VM) isolation [10], VM liveness, OS availability, and correct

\(^2\)“The language doesn’t have a name. We speak of Isabelle/HOL’s function definition facility/command.” Tobias Nipkow, e-mail of April 11, 2016.
The essence of data abstraction is that the private representation of an abstract data type (ADT) can be modeled by execution of guest processes (they execute as if running solo on the bare machine).

**HMAC:** OpenSSL SHA-256 and HMAC, implemented in C and proved correct in Coq [8]. Proved by Separation Logic proofs between C and Gallina functional specifications. The Gallina specs are direct transcriptions of the FIPS 180 and FIPS 198 standards for SHA and HMAC respectively. Then the Gallina specs are shown to enjoy the correctness property that a computationally limited adversary not in possession of the session key cannot distinguish the HMAC from a PRF (pseudorandom function). That proof is by reasoning in a computational monad of probability distributions.

**L4.verified:** The sel4 operating-system kernel, implemented in C and proved correct in Isabelle/HOL [16]. Proved by operational refinement proofs between the C program and an “abstract functional specification,” that is, a program in HOL-fun. Then the functional program is shown to enjoy correctness properties such as integrity and confidentiality.

**Raft:** The Raft consensus protocol, implemented as a state machine translated by the Verdi system (in Coq) to Gallina for extraction to OCaml [28]. Correctness properties proved in Coq include: state machine safety, election safety, log matching, leader completeness, and linearizability. The relation between the Gallina spec and the low-level imperative program (assembly language) is by compilation in OCaml; this part is not proved correct.

In this short paper I cannot possibly survey all the excellent results in related areas; I pick just these few to illustrate some principles of their construction.

**V. Fun with functional program specs**

The advantage of a two-level verification—low-level implementation to functional program, then functional program to domain-specific mathematical/relational properties—is that functional programs are easy to reason about. I will use our HMAC verification as an example.

SHA-2 (Secure Hash Algorithm) is an iterated block compression: in 256-bit mode, a 512-bit block is mixed with a 256-bit hash yielding a new 256-bit hash. Blocks can be chained together, and odd-length strings are handled by a padding+length suffix.

In 1996, Bellare et al. [7] described the HMAC algorithm for symmetric-keyed cryptographic authentication based on any (good-enough) iterated block compression (such as SHA). They proved that it provides cryptographic security: in particular, a polynomial-time adversary who lacks the session key cannot distinguish HMAC from a random function.3 (In short, HMAC is a PRF, a pseudorandom function.)

In 2002 the FIPS 180-2 standard for SHA-2 was promulgated, and in 2008 the FIPS 198 standard for HMAC.

Bellare’s proof is not about a program, but about a mathematical presentation (in English and \(\text{H}\)\(\text{E}\)\(\text{X}\) math) of an algorithm. FIPS 180-2 and FIPS 198 comprise a similar but not identical English+\(\text{H}\)\(\text{E}\)\(\text{X}\) presentation of an algorithm that should be an instance of what Bellare et al. describe.

In 2015 we proved, with machine-checked proofs in Coq, that OpenSSL’s SHA+HMAC, as actually compiled to assembly language, is cryptographically secure (is a keyed PRF) [8]. The four authors of our paper worked on modularly separable tasks, with little communication except at specification interfaces. The specification interfaces are written in Coq, typically in the form of functional programs in Gallina.

- Appel proved the OpenSSL SHA-256 C program implements (our Coq formalization of) FIPS 180.
- Beringer proved the OpenSSL HMAC C program implements (our Coq formalization of) FIPS 198.
- Petcher implemented in Coq the Bellare et al. proof that (our Coq formalization of) Bellare et al.’s presentation of HMAC/SHA is a keyed PRF.
- Ye proved that (our Coq formalization of) FIPS 180 + FIPS 198 is equivalent to (our Coq formalization of) Bellare et al.’s presentation of HMAC/SHA.

Our SHA/HMAC proof would have been impractical without a modular separation of concerns. In particular, Petcher’s proof has no interaction with the C language or with techniques for proving correctness of C programs. Appel’s and Beringer’s proofs have no interaction with Petcher’s computational monad over probability distributions, or with techniques for proving correctness of probabilistic programs, or with crypto proof techniques about distinguishability by computationally limited adversaries. Ye’s proof concerned neither the C language nor the probabilistic techniques.

This proof of a cryptographic primitive is just one example. The OS kernel proofs cited above also enjoy this modularity—the separation of concerns between implementation in C and properties of the algorithm—by using a functional-language specification interface between these two levels.

**VI. Program modules and data abstraction**

SHA-256 and HMAC really are functions: given an input (message + key) there is a unique output. So it’s easy to see how a C program can implement a functional spec written in a pure functional language. But an operating system, or one module of an operating system or of any large software system, is not simply a function from an input to an output. A module has internal state, and interface operations (methods) that operate on the external state. No problem! We can represent this in the functional language as a dependent record of a representation type, a value of that type that represents the “current internal state,” and a series of pure functions that take the representation type and other inputs, and produce the representation type and other outputs [14].

3This proof was subject to the hypothesis that the underlying block-compression function (e.g., the core of SHA-256) is a PRF; a more precise characterization of the assumption is in footnote 12 of Appel [5]. No one knows how to prove this assumption about SHA, but it is generally accepted as a “true enough” property of SHA.
existential quantification [22]. Not only the type of the private variables, but the representation invariant (a predicate), must be quantified over. Let’s do an example:

```c
#include "Counter.h"

struct counter;

Counter.h

// deliberately baroque */
struct counter * make(void);

Counter.c

void inc(struct counter *p);

int get(struct counter *p);

struct counter {
    int x3;
    int x2;
};

# define deliberately baroque */

struct counter *p = (struct counter *)malloc(sizeof(*p));

p->>x3 = 0; p->>x2=0;

return p;

} void inc (struct counter *p) {
    p->>x3+=3; p->>x2+=2;
}

int get (struct counter *p) {
    return p->>x3 - p->>x2;
}
```

Part of the module-interface’s specification is (and don’t be intimidated by the notation, just read on),

\[
Σ(τ : Type),Σ(φ : τ → Prop).
\]

\[
(1 \rightarrow Σ(x : τ),φ(x)), \text{ make}
\]

\[
Π(x : τ).φ(x) \rightarrow Σ(y : τ),φ(y), \text{ inc}
\]

\[
Π(x : τ).φ(x) \rightarrow Σ(x : τ),φ(y)) \text{ get}
\]

This says there is a hidden representation whose type is \( τ \) (in the example implementation, \( τ = \mathbb{Z} \times \mathbb{Z} \), a pair of integers representing the \( x3 \) and \( x2 \) fields of the struct). Then, \( φ \) is a representation invariant (in the example, \( φ(x_3, x_2) = 3i \cdot x_3 = 3i \land x_2 = 2i \)). Then, within the scope of the existential quantification of \( τ \) and \( φ \), there are characterizations of the three interface functions. For example, \( inc \) takes input \( x \) of type \( τ \) such that \( φ(x) \), and produces output \( y \) such that \( φ(y) \).

Both the “deliberately baroque” implementation shown above, and the obvious straightforward implementation, are instances of this representation-hiding specification.

There is more to this specification: I haven’t shown that \( x \) is actually represented as a C struct, and I haven’t shown how we represent the claim that \( inc \) actually increments rather than decrements (or adds 6). But the point I want to make is: quantification over types (\( τ \)) and predicates (\( φ \)) is essential to data abstraction, that is, reasoning about program modules with private data representations.

Therefore, when doing large compositional proofs about modular programs (such as CertiKOS), it’s important to have a higher-order logic, which permits quantification over predicates. Thus I focus on HOL and Coq/Gallina, and it’s not surprising that the OS kernel verifications L4.verified [16] and CertiKOS [14] were done in these (respective) logics rather than a first-order logic such as ACL2.

VII. PROGRAM SYNTHESIS

Instead of (laboriously, interactively) proving the correctness of a C program w.r.t. a functional specification, one might wish to compile the functional spec directly to an imperative (C, or assembly language) program. That is, replace the box labeled refinement proof with one labeled synthesize or compile. In that case, one would need a formally verified functional-language compiler. Several approaches have been demonstrated.

One could compile the ML-like language used in the logic (such as Gallina or HOL-fun) using standard techniques for ML compilation (with heap-allocated data structures and function closures), but with a compiler verified with a machine-checked proof. CakeML is such a compiler, proved correct w.r.t. formalized operational semantics of (a variant of) Standard ML source language and (x86-64) machine language [18]. It is written in (HOL4’s version of) HOL-fun, proved correct in HOL4, and translated through CakeML itself (with careful attention to bootstrapping the proof so this is not too circular).

CertiCoq is an ongoing project at Princeton and Cornell to write, in Gallina, a proved-correct compiler from Gallina to CompCert C light. In the Raft example cited in §IV, CertiCoq+CompCert could be used to obtain formally verified compile layers.

A disadvantage of that approach is that heap-allocated data and closures require garbage collection. Some kinds of low-level security-relevant software, such as OS kernels and crypto primitives, cannot easily tolerate garbage collection.

But most software can tolerate garbage collection—just consider the huge amount of code written in Java, Perl, Python, Ruby, Go, and so on. If this software is insecure, it is not because of garbage collection! In fact, just the opposite, since explicit malloc/free is the source of many bugs and security vulnerabilities. Probably most software—even most operating-system and crypto-protocol software—should be written in garbage-collected languages. For example, Mirage OS kernels (written in garbage-collected OCaml) are layered over the Xen hypervisor (written in C) [21].

But still, can the Gallina or HOL-fun functional specification be automatically translated to an “imperative style” non-garbage-collected low-level program?

Cogent is a linear-typed polymorphic first-order pure functional language. It is not as general as ML (or Gallina or HOL-fun), but it is at least sufficient for implementing (verified functionally correct) file systems [3]. From a Cogent program, the compiler generates a HOL-fun program, a C program, and a refinement proof that the C program implements the HOL-fun program [23]. The linear types ensure that malloc/free can be used instead of garbage collection.

VIII. COMPILER CORRECTNESS

To show correctness of the SHA/HMAC assembly language programs that result from compilation, we rely on two more self-contained modular proofs in Coq:
• Leroy’s proof [19] that the CompCert C compiler is correct with respect to the operational semantics of C and of x86 assembly language (both formalized as small-step operational semantics).
• Appel et al.’s proof [6] that our Verifiable C program logic (used in the SHA and HMAC proofs above) is sound with respect to Leroy’s operational semantics for C.

There is not much overlap between these two proofs. However, there has been much work (2006–2016) on the specification interface between them, that is the Coq presentation of a memory model and operational semantics for CompCert C light [20], [9].

Similarly, CertiKOS enjoys an end-to-end connection between its contextual refinement proofs (about C programs) and the CompCert compiler-correctness proof.

In connecting to a verified compiler, it is advisable to bypass the compiler’s lexer and parser to connect directly via abstract syntax tree (AST) representations of parsers. The high-level tools (such as Verifiable C or CertiKOS’s Certified Abstraction Layers) can reason directly on ASTs, using the formal operational semantics as a reasoning principle. The compiler semantics phases can reason on the same ASTs, using the same operational semantics, in the same logic. There is no need to reason formally about parsing and pretty-printing.

IX. TOOL LINKAGE

The pretty picture repeated at right can get rather messy, depending on how one specifies and proves compiler correctness. What works well is to have concrete abstract-syntax tree (AST) data structures as the specification interface for compiler correctness. This is how the HMAC (Verifiable C) and CertiKOS proofs connect to the CompCert proofs.

L4.verified, the correctness proof in Isabelle/HOL of the seL4 kernel, connects to its compiler using a somewhat weaker semantic specification. It was built originally using an untrusted “C parser” that generates a (partly) shallowly embedded functional semantics, and compiled using gcc, an unverified compiler. Certainly at the time the L4 verified project started (in 2005 or so [13]) there was no available verified C compiler, nor any trustworthy formal specification of an operational semantics for C.

By 2012, CompCert did exist; so why not connect it to the L4.verified proofs? The seL4 team tried this but unfortunately,

“We have used [CompCert] on the verified C source of the seL4 microkernel, but in this case found the result unsatisfactory: There is a remaining chance of a mismatch between CompCert’s interpretation of the C standard in the theorem prover Coq and the interpretation of the C standard the seL4 verification uses in the theorem prover Isabelle/HOL, esp. in cases where the standard is purposely violated to implement machine-dependent, low-level operating system (OS) functionality. Reconciling these two semantics is non-trivial. Firstly the logics of Coq and Isabelle/HOL are not directly compatible. Secondly, since the seL4 semantics is largely shallowly embedded, an equivalence proof would have to be performed for each program, ...” [26]

Instead they take a different approach: they use ad-hoc translation validation of a gcc compilation. Proof checking now relies on two proof assistants (Isabelle/HOL and HOL4) and two SMT solvers (Z3 and SONOLAR). The validation processes uses both tactical proof search and SMT solving. The primary specification interface is the control-flow graph. From the C program there is refinement-based proof search down to the graph; from the ARM binary there is heuristic-based decompilation (with proof) up to the graph; then SMT-based proof is used to match the two graphs.

Unlike a standard deeply embedded SOS, the partly shallow embedding obstructs some kinds of reasoning about the syntactic C program in the proof assistant. In particular, one cannot reason in the logic about transformation functions from one program to another—that is, compilers or domain-specific language processors.

So therefore: L4.verified does indeed use machine-checked formal verification to connect the functional spec to the C program and thence to the machine-language program. That’s good. But their system has several disadvantages. The trusted base is huge; validation is slow and must be done on every recompile of the C program; it’s hard to reason generally about program transformers.

This case study illustrates several issues regarding the specification interface to the compiler:

• Abstract syntax trees and structural operational semantics are good. The programming-languages research community has 35 years experience formalizing them for use as interfaces between compilers and programmers [25]. Failing to use this abstraction layer is a missed opportunity for modularity. Not only for direct refinement proofs on C programs one at a time: ASTs + SOS permit cleaner specifications and proof of domain-specific languages that target C. Perhaps the Cogent compiler [23] would be simpler if it could have targeted an AST rather than heuristic-based decompilation.

4-[The C-parser uses Norbert Schirmer’s Simpl language, which is deeply embedded with respect to statements, but just uses HOL functions (with lambdas) for expressions. The parser also produces types in Isabelle which match input types from C, e.g. an Isabelle record for struct in the C source. All of this is designed to produce an AST which the user can manipulate conveniently like it was the C program.

“However, for automatic or reflected methods, this is a headache. Because the expressions are just state transformers, you can write a VCG or other proof method, but you can’t write a translator to another language (in HOL). You can write a translator at the ML level, but then the translator has to be validating rather than validated, e.g. AutoCorres. [Another reason the translator has to be validating rather than validated is:] Because some of the types are unknown until the parser runs, you can’t obviously use the AST as a target language for some conversion...”

[Thomas Sewell, e-mail of April 23, 2016.]
• Compilation is complete, decompilation is incomplete. Programming languages such as C are designed so that there is an algorithm for translating a legal source program to a target program. (It almost goes without saying.) Sewell et al.’s decompilation heuristics must be tuned to each application; for example, they do not handle nested loops, because these were unnecessary for sel4.

• Reflection. Sewell et al.’s refinement from C to control-flow graphs, and decompilation from machine-language to graphs, is driven by tactical proof search, which is slow. CompCert’s translation from C to assembly language is simply the execution of an ML-like functional program; within an order of magnitude, it is approximately as fast as running gcc. That is, CompCert takes advantage of proof by reflection, the ability to write a functional program inside the logic, prove it correct, then use it in further proofs. CompCert is proved, once and for all in Coq, to preserve observable behavior between source program and target program. Each time a C program is compiled, it is not necessary to do a tactical translation-validation proof.

• When possible, one should connect proof modules together at specification interfaces in the same logic and proof system. Then we don’t have to worry whether the program proof and the compiler proof interpret the operators of the language semantics in the same way: they both import the same specification in logic, and that’s the end of it.

Still, formal top-to-bottom functional correctness verification is much better than top-to-middle verification. Both CertIKOS and L4.verified guarantee that the next bug to show up in gcc cannot undetectedly compromise the security of their operating systems. Neither can the next misunderstanding of the C semantics (see the next section), since the top-to-middle proof connects at the specification interface with the middle-to-bottom proof. If that specification in the middle is not exactly “C,” no matter; the proofs still compose.

X. THE RISE OF THE C LANGUAGE LAWYERS

In the first decades of the 21st century, the discussions leading up to (and past) the C11 standard made the semantic definition of C more precise. This definition is still in natural language and “litmus tests,” rather than in formal mechanized logic. Even so, the characterization of undefined behavior is clearer than before, as is the understanding that compilers are responsible only for the defined behavior of the C language.

This increased precision had an unexpected and paradoxical effect. The language lawyers, who write the optimizing compilers are “taking advantage” of legalisms in order to make programs misbehave! Wang et al. explain this with two examples [27].

5From Wikipedia (Rules lawyers): A rules lawyer is a participant in a rules-based environment who attempts to use the letter of the law without reference to the spirit, usually in order to gain an advantage within that environment. [Shared Fantasy, by Gary Alan Fine, University of Chicago Press, 2002, pp. 109–115.] The term “language lawyer” is used to describe those who are excessively familiar with the details of programming language syntax and semantics. [The Jargon File ed, by Eric S. Raymond, v.4.4.8, October 2004.]

6Wang et al. [27] propose a different solution: a static analysis to detect C code that behaves differently when the compiler does or does not optimize based on undefined behavior.
These examples support my thesis rather than disprove it: it’s useful to have a functional program as one of the specification layers. In the diagram, (+proof?) indicates that Coq’s extractor/compiler is not proved correct; in HOL with CakeML or (eventually) Coq with CertiCoq this phase will be proved.

These examples do show the importance of reasoning in a logic that supports higher-order reasoning about inductive relations. Proving compiler-correctness in a first-order (SMT-compatible) logic can be done for toy examples [11], but I am not aware of attempts to do it at scale.

**Randomness.** Consider a program that is nondeterministic, or that explicitly uses randomness. For example, a quick-sort implementation may use a random-number generation to choose a pivot element. We would like to reason about both the correctness and the average-case complexity of the program.

We could model this as a deterministic program that consumes an input from an external stream of random numbers. Then we could model the program as a simple pure function. But it is not a very natural model. In particular, in what order does the function consume coin-flips from the external stream? Really it should not matter; but the determined program is considered a different function if we reorder the two recursive calls to quicksort. And this determined program, which threads the random stream explicitly through the recursive calls, is difficult to parallelize.

Perhaps this is an application domain where a pure functional program does not serve well as a functional specification. Instead, perhaps some sort of probabilistic Hoare logic [12] is appropriate.

**Graph algorithms.** Imperative programs with pointer data structures with mutation can be refinements of pure functional programs. Our Verifiable C program logic (in which we did HMAC) uses separation logic for such proofs. But when the data structures go beyond lists and trees, to graphs with dynamic patterns of sharing, the going gets rough even in separation logic: “Programs manipulating mutable data structures with intrinsic sharing present a challenge for modular verification.” [15] Graph algorithms are not trivial to model with functional programs, especially concurrent algorithms.

So perhaps my thesis of “functional programs are a good specification layer” applies only to easy domains like compilers, operating systems, and cryptography.

**XII. LIMITATIONS**

In the Introduction I talked about the software/hardware stack all the way down past the ISA (instruction-set architecture) to the RTL (register-transfer language) and netlist. Indeed, from the RTL to the netlist, formal machine-checked functional-equivalence verification (FEV) tools are heavily used in industry. But there is a big gap between the ISA and the RTL: ISA specifications have not been heavily formalized, especially in industry and especially in details such as their cache coherence models [4]. Closing this verification gap is an interesting question, in which there is active academic research; but it is beyond the scope of this paper. However, I will remark that the operational-semantic description of the ISA, along with an axiomatic description of the cache coherence model [2], should be an excellent kind of modular specification interface between the software and the hardware.

Functional correctness is a practical necessity for those system components that implement protection mechanisms: OS kernels, file systems, crypto libraries. Program testing, even of the most organized and principled variety, cannot catch all the bugs that a clever and determined attacker will be looking for. The corollaries of functional correctness are important too, including immunity to buffer-overrun vulnerabilities and general absence of undefined behaviors.

Still, functional correctness does not automatically imply freedom from timing channels or resilience in the presence of hardware faults. Formal machine-checked program analyses of such properties would be useful in conjunction with the methods I have described in this paper.

And what about the bootloader, did it actually install our verified components? And does the chip actually implement that netlist, or were there fab-level hardware trojans? A proof of functional correctness does not make an entire security assurance case! But known cases of deliberate trojans installed by insiders are rare: most rootkits are installed by outsiders exploiting unintentional functional-incorrectness vulnerabilities. Therefore, functional-correctness verification would yield significant improvements in security.

**XIII. CONCLUSION**

Modular machine-checked functional-correctness verification of significant system security components is practical now. I recommend three important modularity principles:

1. Use a functional specification written as a functional program, to separate domain-specific reasoning from low-level program verification.
2. Use operational semantics of the low-level programming language (such as C or assembly) to separate program verification from compiler verification (or machine-architecture verification).
3. To verify modular

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7 An inductive data type is a type associated with a finite set of constructors. The constructors build instances, possibly recursively, and also permit traversal (“parsing”) of the data. Examples are lists (with constructors nil and cons), trees with (internal node and leaf). Direct support for inductive data types is found in some languages (such as ML and Haskell) and logics (such as Coq and some implementations of HOL, higher-order logic). Inductive data types are a bit like context-free grammars, and they work very well to express abstract-syntax trees (AST) that represent programs inside compilers.

8 Functions in Gallina or HOL-fun have direct semantic meaning, as functions, in their respective logics (CiC and HOL); such a program is called shallowly embedded. In contrast, the AST representation of a program is just syntax—it doesn’t mean anything by itself except a static tree. Such a program is called deeply embedded. Structural operational semantics (SOS) is a way of giving meaning to deep embeddings by means of inference rules, showing the transformations on ASTs that can “calculate” the results of program execution. These inference rules are also a kind of inductive construction, but they construct logical propositions rather than data; they are an example of an inductive relation.

All of this is described in standard textbooks such as Pierce [24]. The point here is that in modular layered proofs about the correctness of security-kernel implementations, it is very useful to work in a logic capable of expressive reasoning about inductive relations.

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8 Thanks to my student Qinxiang Cao for this observation.
programs, use a higher-order logic that permits abstraction by quantification over predicates.

Finally, to minimize semantic gaps at specification interfaces, it is helpful if all the verifications can be done (and tools can be embedded) in a common framework—such as a general-purpose higher-order logic proof assistant.

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