LS-SVM Inverse System Decoupling Control Strategy of a Bearingless Induction Motor Considering Stator Current Dynamics

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ABSTRACT The bearingless induction motor (BL-IM) is a multivariable, nonlinear and strongly coupled object, in order to achieve its dynamic decoupling control with high performance, on the basis of the least square support vector machine (LS-SVM) principle, a novel LS-SVM inverse system decoupling control strategy is proposed. Firstly, under the conditions of taking the stator current dynamics of torque windings into account, the state equations of the BL-IM system are established. Secondly, based on the approximation and identification fitting ability of the LS-SVM to arbitrary nonlinear function, the inverse system mathematical model of the BL-IM system considering the stator current dynamics is trained and obtained. After that, according to the decoupling principle of inverse system, the BL-IM system is decoupled into four second-order pseudo-linear integral subsystems, include a motor speed subsystem, a rotor flux-linkage subsystem and two radial displacement component subsystems. At the end, the comprehensive simulation analysis of the LS-SVM inverse decoupling control system are carried out. From the simulation results, it can be known that the dynamic decoupling control among the motor speed, rotor flux-linkage and two radial displacement components can be realized, meanwhile after considering the dynamics of the stator current, the LS-SVM inverse decoupling control system of BL-IM has the characteristics of fast response and strong anti-interference ability.

INDEX TERMS Bearingless Induction Motor System; Dynamics of Stator Current; LS-SVM; Inverse System Decoupling

I. INTRODUCTION
The AC motor supported by magnetic bearing has been widely used in the high speed drive field [1-4], but it still has some disadvantages, such as the higher magnetic suspension power consumption, the difficulty to over speed, etc. [5-8]. The bearingless motor is a new type of AC motor that is proposed based on the similarity of stator structure between ordinary AC motor and magnetic bearing [9-10]. Normally, there are two sets of windings in the stator slots of bearingless motor, one is the torque windings with current angular frequency \( \omega_1 \) and pole-pair number \( p_1 \), another is the suspension windings with current angular frequency \( \omega_2 \) and pole-pair number \( p_2 \) [5, 10]. The magnetic field produced by the suspension windings breaks the balance and symmetry of the motor magnetic field, and results in the magnetic field enhancement in some air-gap area, and the magnetic field weakening in the symmetrical air-gap area in space [5, 10]. When the pole-pair numbers of two sets of stator windings and their current angular frequencies meet the “\( p_2 = p_1 \pm 1 \), \( \omega_2 = \omega_1 \)” conditions [5, 11-13], a stable resultant force in radial direction can be generated that is controllable both in amplitude and in direction, and then the suspension motion of the bearingless rotor can be freely controlled. The controllable resultant force in radial direction is called controllable magnetic suspension force. The generation principle of the controllable magnetic suspension force is shown in Figure 1 [10], where the pole-pair numbers \( p_1 \) and \( p_2 \) equal to 2 and 1 respectively.
Compared with the AC motor that is supported by magnetic bearings, the shaft of the bearingless motor is shorter, the critical speed of the bearingless rotor is higher, and then the bearingless motor is more suitable for the high-speed rotary drive application [5, 10, 15-17]. Now, in aerospace, advanced manufacturing, semiconductor processing, chemical industry, life sciences and biopharmaceutical fields, an urgent requirement has been proposed for the bearingless motor technology. The bearingless motor technology can be applied to various AC motors, and among them, because of a series of advantages, such as a robust structure, a larger force/current ratio and the convenience for weakening magnetic, the bearingless induction motor (BL-IM) has attracted wide attention [18-23].

![FIGURE 1 Suspension force generation schematic diagram](image)

Inside the BL-IM, there exists complex electromagnetic coupling relationship [18-20]. In order to achieve its dynamic control with high performance, the dynamic decoupling among relevant controlled variables should be achieved[21-22]. The inverse system method is an effective linearization method based on nonlinear feedback [22-24], its physical concepts is clear and intuitive, and it can be used for the dynamic decoupling of all kinds of bearingless motors.

In the analytical inverse system method, the derived analytical inverse system model of the controlled object is always very complicated; meanwhile, the model accuracy is unavoidably affected by the modeling deviation and time-varying parameters, this will inevitably affect the decoupling performance of the BL-IM system [10, 22], and then it is inconvenient for practical application. Utilizing the neural network, the nonlinear inverse model of a BL-IM system can be identified [21, 22]. But the problems of neural network itself, such as the slower convergence rate, the easiness to fall into local minima and the more dependence on the expert knowledge, have limited its application scope to a certain extent [25]. The support vector machine (SVM) is a novel machine learning method that is based on the statistical learning theory [26], it can effectively minimize the dependence on the expert knowledge. In addition, the SVM also has some other excellent characteristics, such as the small sample self-learning ability, the stronger generalization ability, the global optimization ability and the relatively fixed topological structure, etc.[25], and then it is very suitable for the parameter estimation and model identification. The least squares support vector machine (LS-SVM) is a further expansion of the SVM [25, 27], it changes the inequality constraint of traditional SVM to an equivalent equality constraint, it converts the problem of solving the quadratic programming to that of solving linearization equations[25], it effectively simplifies the computation process [25, 28, 29], and then it is applicable to the nonlinear modeling of the bearingless motor system [25, 29]. About the decoupling control strategies of BL-IM system based on the LS-SVM, there have been some research processes. But in the existing researches [30-32], the stator current components are selected as the control inputs of the original system, therefore the dynamics of stator current are not taken into account, and as a result, the identified inverse model of the BL-IM system is not accurate enough [29-32], which inevitably limits the improvement of the dynamic decoupling control performance of the BL-IM system to a certain extent.

In order to control the BL-IM with high-performance, this paper proposes a LS-SVM inverse decoupling control strategy for the BL-IM system. Firstly, taking the current dynamic link of torque windings into account, and on the basis of the rotor flux-linkage orientation of the torque system, the state equations of a BL-IM system are established firstly[22]. And then, on the basis of the reversibility analysis, the LS-LVM inverse system model of a BL-IM system is trained and established, by way of the inverse system method, the BL-IM system is decoupled into four second-order pseudo-linear integral subsystems [22], meanwhile the analysis and synthesis are made for each subsystem. At the end, the proposed LS-SVM inverse decoupling control strategy is simulated and verified in detail.

II. Mathematical Model of a BL-IM system

A. Mathematical Model of the Torque System

During the normal operation of a BL-IM system, because the rotor’s eccentricity is very small, the influence of the suspension control magnetic field on the torque windings can be neglected. And then, the mathematical model of torque system is basically the same as that of the ordinary induction motor system.

Defining \(d-q\) is the coordinate system oriented by the rotor flux-linkage of torque system[22, 24]. Then, considering the dynamic differential equations of the stator current components, and taking the constraint conditions \(\psi_{ld} = \psi_{ld} = 0\), \(\psi_{1} = \psi_{1d}\) into account, the dynamic mathematical model of the torque system can be obtained as follows[24]:

\[\ldots\]
\[
\begin{align*}
\frac{di_{id}}{dt} &= -R_{s1}i_{id} + R_{r1}i_{iq} + \frac{L_{m1}}{\sigma L_{r1}}\psi_{r1} + \frac{1}{\sigma L_{r1}}u_{id}, \\
\frac{di_{iq}}{dt} &= -R_{s1}i_{iq} - R_{r1}i_{id} - \frac{L_{r1}}{\sigma L_{r1}}\omega\psi_{r1} + \frac{1}{\sigma L_{r1}}u_{iq}.
\end{align*}
\]

where, the expression of the synchronous angular speed \( \omega_1 \) is as follows:

\[
\omega_1 = p_s\omega_T + \frac{L_{m1}i_{iq}}{T_L\psi_{r1}}.
\]

In (1) and (2): \( \psi, u, i, R \) represent the flux-linkage, voltage, current and resistance respectively; the subscripts \( s1 \) and \( r1 \) represent the stator and rotor of torque system respectively; \( \omega_1 \) is the rotation angular velocity of the bearingless rotor; the subscripts \( d \) and \( q \) represent the corresponding components in \( d-q \) coordinate system; \( L_{r1}, L_{s1} \) and \( L_{m1} \) represent the stator self-inductance, the rotor self-inductance and the mutual inductance respectively; \( L_{r1} \) and \( L_{s1} \) are the stator- and rotor-leakage inductance respectively; \( T_L \) is the load torque variable; \( T_T \) is the time constant of rotor windings.

B. Mathematical Model of magnetic suspension System

Defining \( \alpha-\beta \) is the stationary coordinate system whose coordinate origin is set on the stator axis. Then the components of controllable magnetic suspension force in the \( \alpha-\beta \) coordinate system can be expressed as follows [24]:

\[
\begin{align*}
F_{\alpha} &= K_m(i_{2d}\psi_{r1} + i_{2q}\psi_{r1}) \\
F_{\beta} &= K_m(i_{2q}\psi_{r1} - i_{2d}\psi_{r1})
\end{align*}
\]

where, \( K_m \) is the stiffness coefficient of magnetic suspension force that is determined by the BL-IM structure; the expression of coefficient \( K_m \) is as follow:

\[
K_m = \pi L_{m1} l (4\mu_0 l r N_1 N_2)
\]

In (3) and (4): \( F_{\alpha} \) and \( F_{\beta} \) are the components of controllable magnetic suspension force in the \( \alpha-\beta \) coordinate system[24, 25]; \( i_{2d} \) and \( i_{2q} \) are the components of magnetic suspension control current in the \( d-q \) coordinate system; \( \mu_0 \) is the air-gap permeability; \( l \) is the length of stator core; \( r \) is the inner diameter of stator core; \( L_{m2} \) is the excitation inductance per phase of the three-phase suspension windings; \( N_1 \) is the effective turn number in series per phase of the three-phase concentrated torque windings, \( N_2 \) is that of the three-phase concentrated suspension windings [22]; \( \psi_{r1} \) and \( \psi_{i1} \) are the air-gap flux-linkage components of the torque system in the \( d-q \) coordinate system [24, 25].

From (3), it can be known that the components of controllable magnetic suspension force is related to the components \( \psi_{r1} \) and \( \psi_{i1} \) of the air-gap flux-linkage. The required \( \psi_{r1} \) and \( \psi_{i1} \) components can be expressed as follows:

\[
\psi_{r1} = \frac{L_{r1}}{L_{s1}}(\psi_{r1} + L_{r1}\dot{i}_{id}), \quad \psi_{i1} = \frac{L_{m1}}{L_{r1}}L_{s1}\dot{i}_{iq}
\]

From the principle of mechanical dynamics, the suspension motion equation of bearingless rotor can be expressed as follow [22]:

\[
m\ddot{x} = F_u + F_{la}, \quad m\ddot{\beta} = F_{\beta} + f_{fa} + f_{fb}
\]

In (6): \( m \) is the mass of bearingless rotor; in the \( \alpha-\beta \) coordinate system, \( F_{la} \) and \( F_{lb} \) are the corresponding components of external radial force, \( f_{fa} \) and \( f_{fb} \) are the corresponding components of unilateral electromagnetic pull. Here, the expressions of \( f_{fa} \) and \( f_{fb} \) components are as follows:

\[
f_{fa} = k_z\alpha, \quad f_{fb} = k_z\beta
\]

Where, \( k_z \) is the stiffness coefficient of radial displacement [22], its expression is “\( k_z = \pi r l B^2 / 2\mu_0\delta_0 \)”, \( \delta_0 \) is the average length of air-gap, \( B \) is the amplitude of air-gap flux density of the torque system.

C. State equation of a BL-IM system

Taking the current dynamics of the torque system into account, the input-, state- and output-variable of the BL-IM system are defined as follows:

\[
\begin{align*}
u &= (u_{1d}, u_{1q}, i_{2d}, i_{2q})^T \\
x &= (x_1, x_2, x_3, x_4, x_5, x_6, x_7, x_8)^T \\
y &= (y_1, y_2, y_3, y_4)^T
\end{align*}
\]

After substituting equations (8) ~ (10) into equations (1) ~ (6), an eight-order state equation of the BL-IM system can be obtained, as shown in equation (11).

\[
\begin{align*}
\dot{x}_1 &= x_3 \\
\dot{x}_2 &= x_4 \\
\dot{x}_3 &= \frac{K_m}{m}\frac{L_{m1}}{L_{r1}}[(x_7 + L_{s1}x_8)u_3 + L_{r1}x_6u_4] + (k_z + F_{la})/m \\
\dot{x}_4 &= \frac{K_m}{m}\frac{L_{m1}}{L_{r1}}[L_{s1}u_3 - (x_5 + L_{s1}x_6)u_4] + (k_z + F_{la})/m \\
\dot{x}_5 &= -(\gamma - \delta)x_5 + (p_1x_3 + L_{m1}\delta x_6 / x_7)x_3 + \xi_1 x_5 + \xi_2 x_6 + \xi_3 x_7 + \xi_4 x_8 \\
\dot{x}_6 &= -(\gamma - \delta)x_6 + (p_1x_4 + L_{m1}\delta x_6 / x_7)x_3 + \xi_1 x_5 + \xi_2 x_6 + \xi_3 x_7 + \xi_4 x_8 \\
\dot{x}_7 &= L_{m1}\delta x_5 - \dot{x}_5 \\
\dot{x}_8 &= \mu x_6 x_7 - T_{L} / J
\end{align*}
\]
In (11), the related parameters are expressed as follows:

\[
\gamma = \frac{R_{r1}}{\sigma L_{l1}} + \frac{R_{s1}}{\sigma L_{l1}}, \quad \sigma = 1 - \frac{L_{m1}}{L_{r1} L_{l1}}, \quad \delta = \frac{R_{m}}{L_{r1}}
\]

\[
\xi = \frac{1}{\sigma L_{l1}}, \quad \mu = \frac{p}{\sigma L_{l1}}, \quad \eta = \frac{L_{m1}}{L_{l1}}.
\]

### III. Reversibility Analysis of the BL-IM system

The invertibility of BL-IM system can be analyzed by Interactor algorithm. Here, each output variable \( y_i \) \((i=1, 2, 3 \text{ and } 4)\) would be asked derivative to time gradually, until one or more input variables \( u_i \) \((j=1, 2, 3 \text{ and } 4)\) are obviously included in the derivative functions [22]. The solving steps can be summarized as follows:

\[
\dot{y}_1 = x_3
\]  
\[
\dot{y}_2 = \frac{K_m}{m} L_{m1} [(x_7 + L_{r1} x_3) u_3 + L_{s1} x_6 u_2] + (k_m x_1 + F_{ld}) / m
\]  
\[
\dot{y}_3 = \frac{K_m}{m} L_{m1} [L_{r1} x_1 u_3 - (x_7 + L_{r1} x_3) u_4] + (k_m x_1 + F_{ld}) / m
\]  
\[
\dot{y}_4 = \mu x_6 x_7 - T_i / J
\]

From (13), (15), (17), (19), it can be known that there is a serious non-linear relationship between the input variable and output variable of BL-IM system, i.e. the inverse system model described by (23) appears serious nonlinearity. In addition, the uncertainty of the BL-IM system, and some other unknown non-linear factors would inevitably affect the decoupling control performance of the analytic inverse system. And then in this paper, in order to overcome the mentioned shortcomings of the analytic inverse system method, utilizing the stronger self-learning and generalization ability of the LS-SVM, the LS-SVM inverse model of a BL-IM system that takes the current dynamics of torque system into account can be expressed as follow:

\[
U = [u_1, u_2, u_3, u_4]^T = \xi^T (\tilde{y}_1, \tilde{y}_1, \tilde{y}_2, \tilde{y}_2, \tilde{y}_3, \tilde{y}_3, \tilde{y}_4, \tilde{y}_4)
\]  
\[
\Sigma \alpha = 8 = n, \text{ then the BL-IM system is reversible}[22].
\]

### IV. LS-SVM inverse system decoupling control strategy of the BL-IM system

#### A. Regression Principle of LS-SVM

For training data sets \( \{(x_i, y_i)\}_{i=1}^N \), where \( N \) is the number of training samples, \( x_i \) is the input data, \( x_i \in R^r \), \( y_i \) is the corresponding output data and \( y_i \in R \), utilizing the non-linear mapping relationship \( \varphi(\cdot) \), the input space is mapped to a feature space with high dimension. And then the optimal linear regression should be performed. The linear function of the high-dimensional feature space is as follows:

\[
y(x) = w^T \varphi(x) + b
\]

In (24): \( w \) is the weight vector[25], \( b \) is the offset value. Defining the "2-norms of error" as the loss function of the LS-SVM, then the optimization problem of the LS-SVM regression algorithms can be expressed as follows:

\[
\min J(w, \xi) = \frac{1}{2} w^T w + \gamma \frac{1}{2} \sum_{i=1}^N \xi_i^2
\]  
\[s.t. \quad y_i = w^T \varphi(x_i) + b + \xi_i, i = 1, 2, ..., N
\]

Where: \( \gamma \) is the regularization parameter(or the penalty factor), and it is a compromise parameter between the model generalization ability and the identification accuracy, \( \gamma > 0 \); \( \xi \) is the relaxation factor of the insensitive loss function.
From (25), defining a Lagrange function as follow:
\[
L(w, b, \xi, \alpha) = J(w, \xi) - \sum_{i=1}^{N} \alpha_i \left\{ w^T \varphi(x_i) + b + \xi_i - y_i \right\}
\] (26)

In (26), \(\alpha_i\) is the nonnegative Lagrange multiplier.

From the Karush-Kuhn-Tuck (KKT) condition, making the partial derivatives of the Lagrange function to the parameters \(w, b, \xi_i\) and \(\alpha_i\), and taking the obtained partial derivatives as zero [24]. Then and:
\[
\begin{align*}
\frac{\partial L}{\partial w} &= 0 \Rightarrow w = \sum_{i=1}^{N} \alpha_i \varphi(x_i), \\
\frac{\partial L}{\partial b} &= 0 \Rightarrow \sum_{i=1}^{N} \alpha_i = 0, \\
\frac{\partial L}{\partial \xi_i} &= 0 \Rightarrow \alpha_i = y_i - \frac{1}{\sigma^2} \varphi(x_i) + b + \xi_i - y_i = 0, \\
\frac{\partial L}{\partial \alpha_i} &= 0 \Rightarrow \alpha_i \geq 0, \quad i = 1, 2, \ldots, N \\
\end{align*}
\] (27)

After eliminating the parameters \(w\) and \(\xi\), following matrix equation can be derived:
\[
\begin{bmatrix} 0 & T^T \\ T & \Omega + \gamma^{-1} I \end{bmatrix} \begin{bmatrix} b \\ \alpha \end{bmatrix} = \begin{bmatrix} y \\ 0 \end{bmatrix}
\] (28)

Where: \(\alpha = [\alpha_1; \ldots; \alpha_N]\), \(y = [y_1; \ldots; y_N]\) and \(\Omega = \{\Omega_{ij}\}_{N \times N}\) are \(N \times N\) dimensional functional matrix; \(\Omega_{ij} = \varphi^T(x_i) \cdot \varphi(x_j)\), and \(i, j = 1, 2, \ldots, N\); \(T = [1, 1, \ldots, 1]^T\).

\[K(x_i, x_j) = \exp[-\frac{1}{2} \left\| x_i - x_j \right\|^2/(2\sigma^2)]\] (29)

Where \(\sigma\) is the kernel width.

Calculating the parameters \(\alpha\) and \(b\) in (28) by the least square method, substituting (27), (29) into (24), then the regression function of the LS-SVM can be derived as follow:
\[
y(x) = \sum_{i=1}^{N} \alpha_i K(x_i, x) + b
\] (30)

Figure 2 gives the LS-SVM topology that takes the \(d\)-axis voltage component \(u_{id}\) of torque windings as the output variable[22]. The LS-SVM topology that takes other variable as the output variable is similar with this, and no further details will be given here.

B. LS-SVM inverse system decoupling control

In this paper, the inverse model of a BL-IM system is realized by way of the LS-SVM and some additional integrators. The schematic diagram of the composite system is shown in Figure 3, which is composed of the trained LS-SVM inverse system and the original BL-IM system. Because a LS-SVM can only be used to approximate a "single output function", then aiming at each output variable, the corresponding LS-SVM inverse model should be constructed firstly. After that, the LS-SVM inverse system should be connected in series before the original BL-IM system, as shown in Figure 3, then the BL-IM system would be decoupled into four independent second-order pseudo-linear subsystems. At the end, adopting the linear system synthesis method, the controllers for each subsystem can be designed separately, and the dynamic decoupling control among the motor speed, the rotor flux-linkage and the two radial displacement components can be realized. The specific implementation steps can be summarized as follows:

1) ACQUISITION OF TRAINING SAMPLE

In this paper, the training sample set is obtained in the precise analytic inverse control system of a four-pole BL-IM. Taking the random signal with normal distribution in the range of 0.45Wb ~ 0.9Wb as the given rotor flux-linkage, taking the random signal with normal distribution in the range of 0 ~ 3000 r/min as the given speed, and taking the random signal with normal distribution in the range of -0.1mm ~ 0.1mm as the given radial displacement component. The whole excitation time is 3.0 seconds, and the sampling step size is set as 0.001 seconds.

The sampled data includes \(\psi_{r1}, \omega_{r}, \alpha, \beta, u_{sid}, u_{sid}, l_{12d}, l_{12q}\). After the sampled data are smoothed and filtered, adopting the "high precision five-point numerical differential algorithm", the first and second derivatives of the radial displacement components, rotor flux- linkage and motor speed are obtained. And then, the training sample set of the LS-SVM, i.e. \{ \(\alpha, \alpha, \beta, \beta, \beta, \psi_{r1}, \psi_{r1}, \tilde{\omega}_{r}, \tilde{\omega}_{r}, \omega_{r}\) \} and \{ \(l_{12d}, l_{12q}, u_{sid}, u_{sid}\) \} are constructed. From the obtained data, selecting 2000 groups at equal intervals as the training set, and the rest data are used as the test set.
FIGURE 3 LS-SVM inverse system decoupling Schematic diagram of a BL-IM

FIGURE 4 Considering the current dynamics of torque windings, the trained LS-SVM inverse model is corrected in front of original BL-IM system, the BL-IM system is decoupled into four second-order subsystems, the PD regulator with a first-order inertia link is used as the regulator of each subsystem, then the LS-SVM inverse decoupling control system a BL-IM is constructed

2) TRAINING LS-SVM INVERSE SYSTEM MODEL

After the training sample set is determined, taking the \( u = [\ddot{\alpha}, \dot{\alpha}, \alpha, \beta, \dot{\beta}, \psi, \dot{\psi}, \omega, \dot{\omega}] \) as the training inputs, using \( i_{\alpha2d}, i_{\beta2d}, u_{\alpha1d} \) and \( u_{\beta1d} \) as the training outputs. Aiming at each of the training output variable, the offline training of LS-SVM inverse model is made. There are four learning machines that are established to train the LS-SVM. In the training process of LS-SVM, the regularization parameter \( \gamma \), and the kernel width parameter \( \sigma \) of the radial basis function determine the training accuracy and complexity of the LS-SVM [25]. Here, the grid search method is used to obtain the best regularization parameter and the kernel width [25], and then the LS-SVM inverse model with a higher training accuracy is obtained.

3) CONTROL SYSTEM SYNTHESIS

After the off-line trained LS-SVM inverse system is combined with the original BL-IM system, the BL-IM system is decoupled into four pseudo-linear second-order integral subsystems, include a motor speed subsystem, a rotor flux-linkage subsystem and two radial displacement component subsystems [22]. In order to obtain excellent static- and dynamic-characteristics, and improve the anti-interference ability, a closed-loop regulator is added to each subsystem. Then the linearized decoupling controller of the BL-IM system is composed of the closed-loop regulators and the LS-SVM inverse system obtained by training. Here, the PD regulator with a first-order inertia link is used as the closed-loop regulator of each subsystem, its transfer function is \( G(s) = K_{\text{PD}} (\tau_1 s + 1) / (\tau_2 s + 1) \), where \( \tau_1 \) and \( \tau_2 \) are the differential- and inertial-time constants respectively. Then the decoupled subsystem is corrected as a “Typical-II” subsystem, its open loop transfer function is as follow:

\[
G_o(s) = \frac{K_{\text{PD}} (\tau_1 s + 1)}{s^2 (\tau_2 s + 1)}
\]  

Figure 4 shows the LS-SVM inverse decoupling control system block diagram of a BL-IM. Compared with the existing LS-SVM inverse decoupling control system [29]-[30],
the advantage is that in the identified LS-SVM inverse system model, because the stator current dynamics of the torque system has been taken into account, the closed-loop current regulator of the torque windings can be omitted naturally, and then the overall control system structure of the BL-IM could be simplified to a certain extent.

V. System simulation verification and analysis

According to the control system structure shown in Figure 4, the system simulation analysis and verification are carried out, Table 1 presents the specific parameters of a BL-IM.

<table>
<thead>
<tr>
<th>Parameters</th>
<th>Description</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>( r )</td>
<td>Inner diameter of stator (mm)</td>
<td>62</td>
</tr>
<tr>
<td>( l )</td>
<td>effective core length (mm)</td>
<td>82</td>
</tr>
<tr>
<td>( \delta )</td>
<td>Air-gap of the auxiliary bearing (mm)</td>
<td>0.2</td>
</tr>
<tr>
<td>( P )</td>
<td>Power of the motor (kW)</td>
<td>2.2</td>
</tr>
<tr>
<td>( R_c )</td>
<td>Resistance of the torque windings (Ω)</td>
<td>1.6</td>
</tr>
<tr>
<td>( R_r )</td>
<td>Resistance of the rotor windings (Ω)</td>
<td>1.423</td>
</tr>
<tr>
<td>( L_{l1} )</td>
<td>leakage inductance of the torque windings (H)</td>
<td>0.0043</td>
</tr>
<tr>
<td>( L_{r1} )</td>
<td>Leakage-inductance of the rotor windings (H)</td>
<td>0.0043</td>
</tr>
<tr>
<td>( L_m )</td>
<td>mutual inductance of the torque system (H)</td>
<td>0.0859</td>
</tr>
<tr>
<td>( J )</td>
<td>rotation inertia (kg.m²)</td>
<td>0.024</td>
</tr>
<tr>
<td>( R_s2 )</td>
<td>Resistance of the suspension windings</td>
<td>2.7</td>
</tr>
<tr>
<td>( L_{s2l} )</td>
<td>leakage inductance of suspension windings (H)</td>
<td>0.00398</td>
</tr>
<tr>
<td>( L_{m2} )</td>
<td>mutual inductance of the suspension system (H)</td>
<td>0.230</td>
</tr>
</tbody>
</table>

Simulation conditions: setting the initial radial displacement components \( \alpha_0 = -0.1 \) mm, \( \beta_0 = -0.12 \) mm; the given rotor flux-linkage \( \psi^* = 0.85 \) Wb, the given motor speed \( n^* = 1500 \) r/min, the given radial displacement components \( \alpha^* \) and \( \beta^* \) equal to zero; the system starts with no load.

Figure 5 shows the response waveforms of the proposed LS-SVM inverse decoupling control system. In order to facilitate the comparative analysis, under the same simulation conditions, the comparative response waveforms of the analytic inverse decoupling control of the analytic inverse decoupling control system are given in Figure 6.

From the Figure 5 and Figure 6, the specific comparative results can be summarized as follows:

1) In the no-load start-up process: based on the proposed LS-SVM inverse decoupling control method, the motor speed overshoot is only about 2%, the \( \alpha \) - and \( \beta \) -displacement components can reach their given values quickly with almost no overshoots, the overshoot of rotor flux-linkage is about 4.7%; but when the analytical inverse decoupling control method is adopted, the motor speed overshoot is about 6%, the overshoot of flux-linkage is about 20%, the overshoots of the \( \alpha \) - and \( \beta \) -displacement components are about 0.01 mm. The simulation results have shown that when the proposed LS-SVM inverse decoupling control method is adopted, a better starting performance can be achieved.
From Figure 5, it can be seen that when one controlled variable changes, the other controlled variables don't change significantly. The simulation results have shown that the LS-SVM inverse system method can realize the dynamic decoupling control among the rotor flux-linkage, motor speed and two radial displacement components.

Comparing Figure 5 with Figure 6, it can be seen that for the LS-SVM inverse decoupling control system, during the transition process of variable mutation, the overshoot of the rotor flux-linkage is no more than 0.04Wb, as for the motor speed, $\alpha$- and $\beta$-displacement components, there are almost no overshoots. While for the analytical inverse decoupling control system, during the transition process of variable mutation, the overshoot of the rotor flux-linkage is about 0.1Wb, the overshoot of the motor speed is about 50r/min, the overshoots of $\alpha$- and $\beta$-displacement components are about 0.01mm. The simulation results have shown that comparing with the analytical inverse decoupling control system, during the transition process of variable mutation, the LS-SVM inverse decoupling control system has smaller overshoot and shorter adjustment time, and then it has better tracking control performance.

3) In order to verify the anti-disturbance ability, the load torque of 8.4N.m is suddenly added at 1.5s. Comparing Figure 5(b) with Figure 6(b), it can be seen that for the LS-SVM inverse decoupling control system, the motor speed decreases by only about 0.5% under the sudden load, and it can be restored to the set value in a very short time; while for the analytical inverse decoupling system, the motor speed decreases by about 1.0%. The simulation results have shown that based on the LS-SVM inverse system
decoupling control method, the BL-IM system owns stronger robustness and stronger anti-disturbance ability. In addition, in the process of sudden loading and unloading, the two radial displacement components in Figure 5(c) and Figure 5(d) are almost unaffected or very little affected, the good dynamic decoupling control performance between torque system and suspension system is verified again.

VI. Conclusion

The bearingless induction motor (BL-IM) is a nonlinear, multivariable and strongly coupled object. In order to improve its dynamic control performance, under the conditions of considering the dynamic characteristics of the stator current of torque system, an inverse system decoupling control strategy based on LS-SVM is proposed, and the system simulation and verification analysis are carried out. The specific research conclusions are summarized as follows:

1) After considering the stator current dynamics of torque system, the BL-IM system oriented by the rotor flux-linkage, is an eight-order nonlinear and strongly coupled complex system that has four input variables and four output variables, the BL-IM system is reversible. In addition, since the components of stator voltage are selected as the input variables of the original torque system, the current closed-loop of the torque windings can be eliminated, and the overall control system structure of the BL-IM can be effectively simplified.

2) Based on the approximation and identification fitting ability of the LS-SVM, the inverse system model can be obtained by off-line learning, and then the dependence of the traditional analytical inverse system method on the accurate model of the BL-IM system can be effectively overcome.

3) Adopting the proposed LS-SVM inverse system decoupling control method, the dynamic decoupling control between the motor speed, rotor flux-linkage and two radial displacement components can be realized. Comparing with the traditional analytical inverse system of BL-IM, the proposed LS-SVM inverse decoupling control system of BL-IM has many advantages, such as smaller overshoot, better tracking performance and stronger robustness.

Reference


