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# **RESEARCH ARTICLE**

# Feature Enhanced Ensemble Modeling With Voting Optimization for Credit Risk Assessment

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**ABSTRACT** Machine learning methods have gained widespread utilization in small and micro enterprise credit risk assessment. However, the practical application of these methods encounters a conundrum involving accuracy and interpretability. In this study, a multi-stage ensemble model is proposed to enhance the model's interpretability. To strengthen predictive portraits, a multi-feature enhancement method is proposed to integrate non-financial behavioral information and soft information on credit rating into the annual loan ledger data, thereby bolstering the explanatory capacity of the features. To rectify the issue of data imbalance and avoid information loss, a new bagging-based oversampling method is proposed to oversample the minority class samples in multiple parallelized subsets divided by the bagging strategy. To unleash the performance potential of base classifiers, a new voting-weight optimization method is proposed to optimize the soft voting weights of the candidate base classifiers. The experiment results of an annual loan ledger dataset of a commercial bank in China (with an accuracy of 97.9%, an area under the curve of 0.97, a logistic loss of 0.07, a Brier score of 0.01, and a Kolmogorov-Smirnov statistic of 0.38) and the other five public datasets indicating excellent model fit. By focusing on the widespread soft information and data structures characteristic of SME loan risk assessment data, an additional SHAP model explanation method enhances interpretability. This method reveals that the enhanced 'debt-to-income ratio,' along with non-financial behavioral information and features derived from soft information, are essential for predicting loan defaults. Such enhancements help to alleviate the issue of information asymmetry in SME loan risk assessment.

**INDEX TERMS** Credit risk, ensemble modeling, feature enhancement, model interpretability, voting optimization.

## **I. INTRODUCTION**

For Small and Medium-sized Enterprises (SMEs), the challenge in credit risk assessment lies in the identification of default characteristics. SMEs often lack effective financial information and have weaker risk resistance capabilities, which adds to the complexity of the assessment. Traditional banking and financial features may lack specificity when assessing the credit risk of SMEs [\[1\]. Le](#page-11-0)vine et al. highlighted that the primary assessment for SME loans is based on unquantifiable ''soft information'' provided by account managers [\[2\]. Th](#page-11-1)erefore, the credit risk assessment for SMEs should transcend traditional financial information

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and take into account the financial status of the business owners as well as external data sources (non-financial and soft information) to provide a comprehensive reflection of their creditworthiness.

<span id="page-0-2"></span><span id="page-0-0"></span>Furthermore, with the increasing demand for SME loans, the development of new credit characteristics and rating methods has become urgent. Given the significant similarity between corporate bankruptcy prediction and credit scoring, incorporating features from credit scoring approaches [\[3\],](#page-11-2) Features from credit scoring approaches, such as the debt-toincome ratio that is effective in credit scoring, can enhance the identification of default characteristics in the credit risk assessment for SMEs.

Another issue arises due to the data imbalance in the corporate loan dataset, where non-defaulted SMEs (majority

class samples) far outnumber defaulted SMEs (minority class samples), and the dataset size is relatively small [\[4\]. C](#page-11-3)onsequently, this results in a scarcity of default samples in the corporate loan dataset and a highly imbalanced data distribution. Applying undersampling methods to address data imbalances would result in the removal of a substantial amount of information, aggravating the scarcity of an already limited sample size [\[5\]. Th](#page-11-4)erefore, one of the main objectives of this study is to develop an oversampling method that can effectively generate minority class samples to alleviate the data imbalance issue.

<span id="page-1-2"></span>Traditional linear models may exhibit limitations in accuracy when dealing with highly complex credit risk assessment problems [\[3\]. E](#page-11-2)nsemble learning algorithms have been demonstrated to provide higher accuracy compared to traditional models across various datasets [\[4\]. In](#page-11-3) the era of big data, credit risk assessment models are required to handle vast amounts of data with complex features, as is the case with the experimental dataset adopted in this study. Ensemble methods can combine the predictive results of multiple models, enhancing the understanding of data complexity and capturing nonlinear relationships within the data. Furthermore, ensemble learning algorithms generally possess better generalization capabilities. By combining multiple weak learners, they can mitigate the risk of overfitting and offer more accu-rate predictions on unseen data [\[6\]. Th](#page-11-5)ese models leverage their robust predictive capabilities, which are typically constructed using ensemble methods such as classifiers adopted in this study, i.e., gradient boosting decision tree (GBDT) [\[7\], ra](#page-11-6)ndom forest (RF) [\[8\], ad](#page-11-7)aptive boosting (AdaBoost) [\[9\], ex](#page-11-8)treme gradient boosting (XGBoost) [\[10\], e](#page-11-9)xtremely randomized trees (ExtraTree) [\[11\],](#page-11-10) bootstrap aggregating (Bagging) [\[12\], a](#page-11-11)nd light gradient-boosting machine (Light-GBM) [\[13\]. H](#page-11-12)owever, ensemble-based models have been criticized for their lack of interpretability compared to traditional linear models. Simply providing accurate predictions is inadequate to support practical applications. Therefore, this study aims to unveil and improve the transparency of machine learning models by deconstructing their ''black box'' nature.

<span id="page-1-10"></span><span id="page-1-9"></span><span id="page-1-6"></span><span id="page-1-4"></span>This study presents a novel multi-stage ensemble model for assessing the risk of SME loans. First, a multi-feature enhancement method is proposed to incorporate external data sources (e.g., external legal risk features) and soft information (e.g., expert credit evaluations) about SME loans. This integration aims to enhance the explanatory capability of the features and generate a feature-enhanced training set. Subsequently, a new bagging-based oversampling method is proposed to partition the feature-enhanced training set into multiple parallelized subsets through the bagging strategy. This method overcomes imbalances in the minority class samples through the use of Synthetic Minority Over-sampling Technique (SMOTE) [\[14\], l](#page-11-13)eading to a balanced training set. Furthermore, a new voting-weight optimization method is proposed for optimizing the soft voting weights of the candidate base classifiers in the classifier ensemble, utilizing the L-BFGS-B algorithm [\[15\]](#page-11-14) for constructing

<span id="page-1-14"></span><span id="page-1-13"></span><span id="page-1-1"></span>the stacking-based model. Finally, the SHapley Additive exPlanations (SHAP) explanation method is employed to evaluate the default features in the proposed model from the perspective of machine learning interpretability. Empirical findings demonstrate  $[16]$ ,  $[17]$  the exceptional performance of the SHAP explanation method in assigning feature importance. The SHAP explanation method indicates that, beyond loan information, financial information, and non-financial basic information included in the annual loan ledger data, the enhanced features (e.g., the enhanced ''debt-to-income ratio,'' non-financial behavioral information, and soft information on credit rating) are effective features of SMEs credit risk assessment.

The main contributions of this paper are highlighted below:

(1) The external data sources and soft information are integrated to enhance credit risk models for SMEs. By incorporating these elements, the model captures a comprehensive view of SME creditworthiness, addressing limitations in traditional financial metrics.

(2) The soft voting weights of the classifier ensemble are optimized adaptively by the L-BFGS-B algorithm, which enhances the performance of the ensemble model, ensuring more accurate and reliable credit risk predictions.

<span id="page-1-3"></span>(3) The SHAP method is employed to evaluate feature importance and enhance the interpretability of the model, which provides insights into key features affecting credit risk, such as the debt-to-income ratio and non-financial behavioral information, making the model more transparent and trustworthy for practical applications.

<span id="page-1-8"></span><span id="page-1-7"></span><span id="page-1-5"></span>The remainder of this study is organized as follows: Section [II](#page-1-0) reviews relevant literature on the proposed model. Section [III](#page-4-0) provides detailed explanations of the model. Section [IV](#page-5-0) introduces the experimental settings. Section [V](#page-6-0) analyzes the experimental results. Section [VI](#page-10-0) concludes this study and discusses future research directions.

#### <span id="page-1-0"></span>**II. RELATED WORK**

# A. FEATURE ENHANCEMENT

The rapid advancement of big data and artificial intelligence technology in recent years has prompted a growing interest in using external data sources as supplementary and expansive resources to traditional data within the financial industry and academic community. For instance, researchers have investigated the utilization of social media data, geographical data, and online behavior data for evaluating borrowers' credit risks [\[18\]. M](#page-11-17)oreover, studies have examined the practical applications of mobile phone and email data [\[19\]. T](#page-12-0)hese data sources provide innovative insights and perspectives for credit risk assessment, empowering financial institutions to conduct thorough and precise credit evaluations and risk control [\[20\].](#page-12-1)

<span id="page-1-18"></span><span id="page-1-17"></span><span id="page-1-16"></span><span id="page-1-15"></span><span id="page-1-12"></span><span id="page-1-11"></span>However, in the credit risk assessment of SMEs, risks from legal proceedings would greatly affect business oper-ations [\[21\]. M](#page-12-2)oreover, the business model of commercial banks assigns a certain level of importance to expert credit

<span id="page-2-1"></span><span id="page-2-0"></span>evaluations of SMEs [\[22\]. C](#page-12-3)onsequently, credit risk assessment for SMEs should encompass not only their loan information and financial data but also take into account external data sources such as non-financial basic information, non-financial behavioral information, and soft information on credit rating. The previous study demonstrated that derived features from outlier algorithms could improve the interpretability of the dataset [\[23\]. I](#page-12-4)n this study, a multi-feature enhancement method was proposed to extend the work [\[23\]](#page-12-4) by integrating external data sources and soft information in the credit risk assessment of SMEs. To incorporate the legal and compliance aspects of SME business operations, the relevant legal case information was included in the dataset. Additionally, to account for the influence of soft information, the ''account manager's evaluation of customer credit'' data was enhanced in the dataset. These feature enhancements play a crucial role in constructing a more comprehensive and informative training set.

While there has been interest in the use of external data sources for credit risk assessment within the financial industry and academic community, the systematic integration of these sources into a multi-feature enhancement method tailored for SMEs has been lacking. The multi-feature enhancement method goes beyond traditional financial data, which is often limited in scope, particularly for SMEs that may lack comprehensive financial records. These enhancements are expected to result in a more comprehensive and informative training set, thereby improving the accuracy and reliability of credit risk assessments for SMEs. By proposing the multi-feature enhancement method that integrates these diverse data sources, including soft information and legal case data, the study seeks to fill the existing gap and provide a more holistic approach to credit risk assessment for SMEs.

#### B. BALANCED SAMPLING

Assessing the credit risk of SMEs is a vital undertaking for financial institutions, as it enables them to determine the creditworthiness and potential default risks associated with providing loans to these enterprises. There has been considerable focus on using oversampling methods as a viable approach to handling the imbalanced nature of corporate loan datasets, where the number of default samples is often significantly smaller than that of non-default samples.

In many practical applications, the minority class may contain critical information. Oversampling methods aim to mitigate the issue of data imbalance by artificially increasing the representation of samples from the minority class [\[24\].](#page-12-5) These techniques encompass synthetic oversampling methods, like the SMOTE, which generate synthetic instances by interpolating between neighboring samples of the minority class, thereby aiding the model in better learning the characteristics of the minority class [\[14\].](#page-11-13)

By balancing the dataset, SMOTE helps to enhance the model's recognition capability for the minority class, potentially improving overall classification accuracy, recall, and F1

<span id="page-2-3"></span>scores [\[25\]. B](#page-12-6)esides, SMOTE does not require a large number of minority class samples, which is particularly useful in this study when the cost of obtaining additional samples is high or impractical.

Applying SMOTE methods to SME credit risk assessment can help address the imbalanced distribution of default and non-default samples, leading to improved model performance in predicting loan defaults. Nevertheless, it is essential to consider the potential drawbacks and challenges associated with oversampling methods, including the heightened computational complexity. Therefore, in this study, a new bagging-based oversampling method is proposed to partition the feature-enhanced training set into multiple parallelized subsets through the bagging strategy. The subsets are balanced using the SMOTE and subsequently merged into a balanced training set. This method plays a pivotal role in enhancing the learning capability of classifiers and reducing time overhead, ultimately leading to a more effective assessment of credit risk for SMEs.

Building upon the related work, this study identifies a research gap where traditional oversampling methods, despite their benefits, may introduce computational complexity. To bridge this gap, the study introduces an innovative bagging-based oversampling method. This approach segments the feature-enhanced training set into multiple subsets, which are then independently balanced using SMOTE and merged to form a balanced dataset. This methodology is designed to bolster the classifiers' learning capabilities and to curtail computational overhead, thereby facilitating a more precise and efficient credit risk assessment for SMEs. The integration of this method into the existing body of knowledge advances the field by offering a practical solution to the prevalent issue of data imbalance, enhancing model performance in predicting loan defaults for SMEs.

# C. ENSEMBLE MODELING & INTERPRETABILITY

<span id="page-2-4"></span>Ensemble modeling has replaced logistic regression as the dominant approach in credit risk assessment due to its superior performance and adaptability to large-scale data, with stacking [\[26\]](#page-12-7) being a representative method. Stacking is based on the premise that combining diverse models can outperform a single model by capturing various aspects of the underlying data distribution through the hard and soft voting mechanisms, supporting multiple aggregation choices for single-classifier predictions [\[25\].](#page-12-6)

<span id="page-2-2"></span>However, the enhanced accuracy and performance achieved through ensemble modeling often come at the cost of interpretability due to its significantly more complex structure compared to logistic regression. Interpretability pertains to the capacity to comprehend and elucidate a model's decision-making process, specifically regarding the contribution and significance of each feature. The ensemble models can make it challenging to differentiate individual feature contributions and comprehend the underlying rationale behind predictions.

<span id="page-3-0"></span>

<span id="page-3-1"></span>**FIGURE 1.** Framework of the proposed model.

Researchers have dedicated considerable efforts to resolving the trade-off between interpretability and accuracy in ensemble modeling. Methods such as SHapley Additive exPlanations (SHAP) [\[27\]](#page-12-8) and feature importance measures have been proposed to quantify the influence of features in ensemble models. However, the pursuit of both high accuracy and interpretability remains an ongoing research challenge.

This study extends prior research by aiming to improve the performance of the ensemble model through the optimization of the soft voting decision weight for the classifier ensemble. The principle is as follows: the soft voting mechanism assumes equal decision weights predicted by different base classifiers, implying that the prediction bias of base classifiers uniformly influences the overall model performance. Therefore, a more effective approach is to adaptively adjust the soft voting weights of the base classifiers in a classifier ensemble based on different data sources and prediction performance. This adaptation reduces the decision weight of the base classifier with poor performance, thereby mitigating excessive degradation in model performance. In this study, a new voting-weight optimization method was proposed to optimize the soft voting weights of base classifiers in the classifier ensemble using the L-BFGS-B algorithm for adaptive optimization. Furthermore, a stacking-based heterogeneous ensemble model was constructed with optimized weights for the classifiers.

This study advances the field by extending prior research through the optimization of soft voting decision weights in ensemble models. The traditional soft voting mechanism assumes equal decision weights from base classifiers, which implies that the prediction bias of each base classifier uniformly affects the overall performance. Challenging this assumption, the study proposes an adaptive adjustment of soft voting weights based on the performance of each base classifier. This optimization aims to diminish the impact of poorly performing base classifiers, thus preventing a significant decline in overall model performance. By addressing the need for performance optimization and interpretability in ensemble models, this study contributes to resolving the persistent challenges in the field and offers a pathway

toward more effective and transparent credit risk assessment models.

# <span id="page-4-0"></span>**III. PROPOSED MODEL**

This study proposes a novel multi-stage ensemble model that assesses the risk of SME loans. The framework is illustrated in Figure [1.](#page-3-0) The proposed model comprises three main stages: multi-feature enhancement, bagging-based oversampling, and voting-weight optimization. Details of these three stages are presented in the following subsections.

# A. MULTI-FEATURE ENHANCEMENT METHOD

<span id="page-4-7"></span><span id="page-4-5"></span><span id="page-4-4"></span>The loan default status of small and medium-sized enterprises (SMEs) is not solely reliant on their financial situation [\[28\].](#page-12-9) External data sources [\[29\],](#page-12-10) [\[30\]](#page-12-11) and soft information [\[31\],](#page-12-12) [\[32\]](#page-12-13) have demonstrated their effectiveness in providing predictive information. Therefore, a multi-feature enhancement method was proposed to integrate various external data sources, including non-financial behavioral information and soft information on credit rating, with the financial information, loan information, and non-financial basic information found in the annual loan ledger data, as illustrated in Figure [2.](#page-4-1) This integration aims to enhance the explanatory power of the features. Firstly, the debt-to-income ratio was enhanced as a financial information feature due to its high similarity to corporate bankruptcy prediction and credit scoring. Next, relevant legal case information (the number of plaintiff/accused cases), which includes external legal risk features that influence daily business operations, was enhanced as non-financial behavioral information in the dataset. Additionally, the expert's credit evaluations were enhanced with soft information on credit ratings provided by account managers who deeply understand their clients. To incorporate qualitative soft information, a discretization approach was employed to transform soft information into multiple graded labels, enabling its quantitative integration into the model. These feature enhancements are merged into the annual loan ledger data of SMEs to create the feature-enhanced training set.

<span id="page-4-1"></span>

**FIGURE 2.** Schematic of the multi-feature enhancement method.

# B. BAGGING-BASED OVERSAMPLING METHOD

<span id="page-4-8"></span>In the scenario of assessing credit risk for SMEs, special attention is given to defaulted SMEs that provide critical and valuable default information, which are considered minority class samples in the dataset [\[33\]. S](#page-12-14)ince the number of defaulted SMEs is relatively small in real business, the dataset is severely imbalanced. Therefore, employing an oversampling method is crucial to effectively expanding and extracting intrinsic information while minimizing the risk of losing important data. To address the issue of high time overhead associated with the oversampling method, a bagging-based oversampling technique is proposed, leveraging the time-saving characteristic of the bagging strategy. As illustrated in Figure [3,](#page-4-2) the method involves dividing the feature-enhanced training set into multiple parallelized subsets using the bagging strategy. To ensure balance, the minority class samples are oversampled using the SMOTE technique until their size matches that of the majority class samples. Finally, the balanced subsets are combined into a balanced training set.

<span id="page-4-6"></span><span id="page-4-3"></span><span id="page-4-2"></span>

**FIGURE 3.** Schematic of the bagging-based oversampling method.

# C. VOTING-WEIGHT OPTIMIZATION METHOD

<span id="page-4-9"></span>The balanced training set was used to train the base classifiers, and their performance was assessed by calculating the area under the receiver operating characteristic curve (AUC) [\[34\]. A](#page-12-15)s depicted in Figure [4,](#page-5-1) the selected base classifiers (i.e.,  $Clf$  1,  $Clf$  2, ...,  $Clf$  *n*) were selected to constitute the candidate classifier pool for subsequent ensemble modeling using the soft voting mechanism. To optimize the capabilities of the selected base classifiers, the soft voting weights  $(i.e., W_{C}V_{C} \mid 1, W_{C}V_{C} \mid 2, \ldots, W_{C}V_{C} \mid n)$  of the candidate base classifiers were fine-tuned utilizing the L-BFGS-B algorithm.

Consequently, the weight-optimized base classifiers (i.e., *Oclf* 1, *Oclf* 2, . . . , *Oclf n*) were obtained to create the optimized classifier pool for the stacking integration process. This formed the basis for constructing the stacking model, which was further applied to predict the test set and derive the final result.

<span id="page-5-1"></span>

**FIGURE 4.** Schematic of the voting-weight optimization method.

#### <span id="page-5-0"></span>**IV. MATERIALS AND METHODS**

#### A. DATASET DESCRIPTION AND DATA PREPROCESSING

This study utilizes the annual loan ledger data obtained from a commercial bank located in Jiangsu Province, China, which is called ChinaZJB and is presented in Table [1.](#page-6-1) The ChinaZJB dataset consists of 1,329 valid samples of SMEs after merging the non-financial behavioral information and soft information on credit rating with the financial information, loan information, and non-financial basic information found in the annual loan ledger data. Among them, 108 SMEs have default records, while 1,221 SMEs have no default records, resulting in an imbalanced ratio of approximately 1:11.

To check the robustness of the proposed model, five datasets from the UC Irvine (UCI) machine-learning repository, that is, the Polish 1, Polish 2, Polish 3 [\[35\], A](#page-12-16)ustralian, and Taiwan credit datasets [\[36\], w](#page-12-17)ere used for robustness checks in this study. The details of these datasets are presented in Table [2.](#page-6-2)

In this study, basic data preprocessing approaches, including standardization and normalization, were applied to process the raw datasets. Binary variables are represented as 0-1 variables for data processing. For categorical variables with multiple categories, one-hot encoding is utilized to convert each category into a binary feature. This approach ensures that the distances between categories are equal, thereby enhancing the characterization of variable relationships. The dataset contains a few missing values, which are addressed through a combination of case-by-case verification and mean

imputation. To test for multicollinearity, the variance inflation factor (VIF) method is employed. The VIF serves as an index for assessing the issue of multicollinearity within a regression model. Multicollinearity refers to a high degree of linear association among the independent variables of the model, which may lead to imprecise estimation of regression coefficients. Consequently, the standard errors may be underestimated, thereby affecting the statistical inference of the model. For the  $i$  th independent variable  $X_i$ , the calculation formula for the VIF is given by Equation [\(1\).](#page-5-2)

<span id="page-5-2"></span>
$$
VIF_i = \frac{1}{1 - R_i^2}.\tag{1}
$$

Here,  $R_i^2$  represents the coefficient of determination (R-squared) obtained from a linear regression model that includes  $X_i$  as the dependent variable and all other independent variables as predictors. In essence, a regression of *X<sup>i</sup>* on the other independent variables yields  $R_i^2$ , which is then utilized in the aforementioned formula to compute the VIF. It indicates that the VIF values, which are less than 5, demonstrate weak multicollinearity among the enhanced features.

#### B. EVALUATION METRICS

<span id="page-5-8"></span><span id="page-5-7"></span>In this study, five evaluation metrics were used: accuracy (ACC) [\[37\], a](#page-12-18)rea under the curve (AUC), logistic loss (Loss) [\[38\], B](#page-12-19)rier score [\[39\], a](#page-12-20)nd Kolmogorov-Smirnov (KS) [\[40\].](#page-12-21) These metrics were determined based on the true positive (TP), true negative (TN), false positive (FP), and false negative (FN) values. Predictive accuracy is defined by Equation [\(2\).](#page-5-3)

<span id="page-5-10"></span><span id="page-5-9"></span><span id="page-5-3"></span>
$$
Accuracy = \frac{TP + TN}{TP + FP + TN + FN}
$$
 (2)

The AUC is a widely used metric in binary classification tasks. It represents the area under the ROC curve and the coordinate axis. The value for this area was less than one. A higher AUC indicates a better classification ability compared to a lower AUC value.

Logistic loss is a measure of loss for the classification model. As is depicted in Equation [\(3\),](#page-5-4) *i* represents the sequence number of the predicted sample and  $i \in$  $\{1, 2, \ldots, n\}$ , *n* represents the number of samples,  $y_i$  and  $p_i$ represent the real value and probability prediction, respectively, and  $y_i \in \{0, 1\}$ . The performance of the model is better when the log loss is lower.

<span id="page-5-6"></span><span id="page-5-5"></span><span id="page-5-4"></span>
$$
L_{logistic} = -\frac{1}{n} \sum_{i=1}^{n} (y_i \times Log(p_i) + (1 - y_i) \times Log(1 - p_i))
$$
\n(3)

The Brier score quantifies the mean squared difference between the predicted probability and the actual label. It can be considered as a loss function. A lower Brier score indicates better model performance.

The KS rate is used to measure the ability of a binary classification model to classify positive and negative samples. A higher KS value corresponds to better model performance.

#### <span id="page-6-1"></span>**TABLE 1.** Data description.



#### <span id="page-6-2"></span>**TABLE 2.** Description of the datasets.



# C. ALGORITHMS

In this study, seven base classifiers (XGBoost, GBDT, Adaboost, RF, LightGBM, Bagging, and ExtraTree) were evaluated, and five evaluation metrics (ACC, AUC, Loss, Brier score, and KS) were adopted to evaluate the performances of the base classifiers and ensemble models. The raw datasets were divided into a training set and a test set using five-fold cross-validation  $[41]$ , repeated 50 times to calculate the mean performance. Five-fold cross-validation is a technique for evaluating a model's generalization capability, dividing the dataset into five parts, using four for training and one for validation in each iteration. Unlike setting aside a separate test set, cross-validation ensures all data is used for both training and validation, which is especially important when data is limited. By training and validating the model on multiple subsets of data, five-fold cross-validation helps detect if the model is overfitting to specific data subsets.

# <span id="page-6-0"></span>**V. EXPERIMENT**

# A. EXPERIMENT SETUP

Data preprocessing approaches and the base classifiers GBDT, Adaboost, RF, Bagging, and ExtraTree were

implemented using the Python module ''sklearn.'' The SMOTE algorithm was imported from the Python module ''imblearn.'' The base classifier XGBoost was imported from the Python module ''xgboost,'' and the base classifier Light-GBM was imported from the Python module ''lightgbm.'' The L-BFGS-B algorithm was imported from the Python module ''SciPy.'' The approaches and algorithms mentioned above are imported with default parameters. All experiments were executed on a laptop running Python Version 3.9 with a 12th Gen Intel Core i7-12700H processor, 16 GB of RAM, and the Microsoft Windows 11 operating system. The soft-ware and hardware requirements are presented in Table [3.](#page-7-0)

# B. BASELINE RESULTS

<span id="page-6-3"></span>The performance of the proposed model was verified by evaluating the baseline results using five metrics. As listed in Table [4,](#page-7-1) seven base classifiers were applied.

# C. PERFORMANCE EVALUATION OF THE MULTI-FEATURE ENHANCEMENT METHOD

The multi-feature enhancement method integrates various external data sources, including non-financial behavioral information and soft information on credit rating, into the ChinaZJB dataset. This did not apply to the other five UCI datasets (Polish 1, Polish 2, Polish 3, Australian, and Taiwan). So the effectiveness of the multi-feature enhancement method was evaluated only on the ChinaZJB dataset using five metrics, as outlined in Table [5.](#page-8-0) The values of the evaluation metrics are highlighted in bold if the base classifiers performed the same or better after applying the multi-feature enhancement method. This observation



#### <span id="page-7-0"></span>**TABLE 3.** Software and hardware requirements.



#### <span id="page-7-1"></span>**TABLE 4.** Baseline results.



indicates an improvement in the performance of most evaluation metrics. In particular, the KS indicator has been greatly improved, which shows that the multi-feature enhancement method would help the proposed model perform better in dealing with data in real business scenarios, providing evidence for the effectiveness of the integrated various external data sources.

# D. PERFORMANCE EVALUATION OF THE BAGGING-BASED OVERSAMPLING METHOD

The effectiveness of the proposed bagging-based oversampling method is outlined in Table [6.](#page-8-1) In Table [6,](#page-8-1) the performance evaluation of the ChinaZJB dataset was compared to Table [5,](#page-8-0) and the performance evaluation of five UCI datasets (Polish 1, Polish 2, Polish 3, Australian, and Taiwan) was

# <span id="page-8-0"></span>**TABLE 5.** Performance evaluation of the multi-feature enhancement method.



Note: significant values were boldfaced.

#### <span id="page-8-1"></span>**TABLE 6.** Performance evaluation of the bagging-based oversampling method.



Note: significant values were boldfaced.

compared to Table [4.](#page-7-1) The values of the evaluation metrics are highlighted in bold if the base classifiers achieved equal or improved performance after applying the bagging-based oversampling method. This observation indicates an overall improvement in the performance of most evaluation metrics on six datasets, which indicates that the oversampled samples generated by the proposed bagging-based oversampling method help increase the sample information in the data and improve the training effect of the classifier.

# E. PERFORMANCE EVALUATION OF THE VOTING-WEIGHT OPTIMIZATION METHOD

After multi-feature enhancement and bagging-based oversampling, base classifiers were selected to form a candidate

<span id="page-9-0"></span>

Dataset	The proposed model	XGBoost	GBDT	AdaBoost	RF	LightGBM	<b>Bagging</b>	ExtraTree
ChinaZJB	Eclf 1							
Polish 1	Eclf2							
Polish 2	Eclf3							
Polish 3	Eclf 4							
Australian	Eclf 5							
Taiwan	Eclf 6							

<span id="page-9-1"></span>**TABLE 8.** Final performance of the proposed model.



classifier pool. Subsequently, the soft voting weights of the candidate classifiers were optimized using the L-BFGS-B algorithm and then used for classifier permutations and combinations to form classifier ensembles. Classifier ensembles that performed better on the AUC indicator for each dataset were selected as the best-performing classifier ensembles. As the performance of Bagging and ExtraTree are relatively weak in the experiment, they are not contained in the best-performing classifier ensemble. As listed in Table [7,](#page-9-0) the best-performing classifier ensembles corresponding to the six datasets are *Eclf* 1, *Eclf* 2, *Eclf* 3, *Eclf* 4, *Eclf* 5, and *Eclf* 6, respectively. For example, *Eclf* 1 is an ensemble of XGBoost, AdaBoost, and LightGBM.

The final performance of the proposed ensemble model is presented in Table [8.](#page-9-1) In Table [8,](#page-9-1) the values of the evaluation metrics are highlighted in bold if the proposed ensemble model outperforms or achieves equal performance compared to the base classifiers after both the multi-feature enhancement and bagging-based oversampling methods. The evaluation indicators show that the performance of the proposed ensemble model has been improved to varying degrees in most indicators after the voting-weight optimization method is used, indicating that the modeling idea of the voting-weight optimization method, i.e., the optimization of soft voting decision weights in ensemble models aims to diminish the impact of poorly performing base classifiers, thus preventing a significant decline in overall model performance is effective.

# F. PERFORMANCE EVALUATION OF THE SHAP EXPLANATION METHOD

An essential challenge encountered in the practical application of machine learning models in business domains is the lack of transparency compared to linear regression [\[42\].](#page-12-23) This lack of transparency makes it difficult for operators to understand the crucial features at play, leading to a potential lack of trustworthiness in the process, despite its reliable results. To address this issue in model interpretation, the study introduces the SHAP explanation method to explore the ChinaZJB dataset.

The core idea of SHAP explanations is to compute the Shapley values of each feature over all possible combinations of feature values. These values can be used to explain individual prediction results or the overall behavior of the model on a dataset. For a feature *j*, its SHAP value  $\phi_i$  can be calculated using the Equation [\(4\):](#page-9-2)

<span id="page-9-2"></span>
$$
\phi_j = \sum_{S \subseteq \{1, \dots, M\} \setminus \{j\}} \frac{|S|!(M - |S| - 1)!}{M!}
$$
  
 
$$
\times [f(x_S \cup \setminus \{j\}) - f(x_S)] \tag{4}
$$

where *M* is the total number of features, *S* is a subset of features not containing feature  $j$ ,  $x<sub>S</sub>$  represents the feature values for the subset *S*,  $f(x_S \cup j)$  is the model output for the feature set including  $j, f(x<sub>S</sub>)$  is the model output for the feature set not including *j*.

Figure [5](#page-10-1) is the feature importance bar graph to illustrate the global significance of the top 20 features in the credit risk assessment of SMEs. This significance is based on the average of absolute SHAP values per feature across the dataset. The features are ranked in descending order, and a red color indicates a positive correlation with failure prediction, while a blue color indicates a negative correlation. Figure  $6$  is the beeswarm plot to display an information-dense summary of how the top 20 features impact the model's output. The features are ranked in descending order. On the x-axis, the signs of the effect on business failure prediction are depicted, and the color of the dots reflects the magnitude of their effect. Blue indicates a low effect, while red indicates a high effect.

<span id="page-9-3"></span>Apart from loan information and financial data, which have consistently demonstrated their significance, it has been discovered that non-financial basic information plays a pivotal role in assessing the likelihood of default among SMEs. Among these features of the ChinaZJB dataset, ''business duration'' ranks first, surpassing other features in identifying defaults. The longer the lifespan of an SME, the more experienced its managers become, enabling them to better

resist external risks and increasing the likelihood of stable operations. Consequently, this strengthens the SME's ability to repay debts. Non-financial behavioral information also serves as valuable explanatory features. Ranking third, the ''number of accused cases'' reflects whether an SME has violated laws or regulations. This highlights the substantial impact of an SME's adherence to legal and compliant business behavior during the loan period on loan quality. Additionally, this feature also provides insight into an SME's credit risk management and operational capabilities.

<span id="page-10-1"></span>

**FIGURE 5.** Feature importance bar graph for global interpretability of the ChinaZJB dataset.

<span id="page-10-2"></span>

**FIGURE 6.** Beeswarm plot for global interpretability of the ChinaZJB dataset.

The ''debt-to-income ratio'' derived from credit scoring, has also proven to be an effective feature. This feature represents the extent to which the SME's ''operating income''

covers its ''total borrowing'' with higher ratios indicating lower default risks. The key to credit risk assessment is effectively measuring the SME's capacity to repay, willingness to repay, and total borrowing (typically consisting of loans from various financial institutions). An SME's funds and loans are different in terms of capacity to repay and willingness to repay. Therefore, ''total borrowing'' is important because it revises estimates of SMEs' capacity and willingness to repay so that the ''debt-to-income ratio'' is important as well.

The integration of the SHAP explanation method within the context of this study offers a transformative perspective for financial institutions and practitioners engaged in credit risk assessment for SMEs. By demystifying the complexities of machine learning models, this approach provides financial institutions and practitioners with a transparent and actionable framework to dissect the contributions of various features impacting creditworthiness. The practical upshot of this transparency is a more nuanced understanding of the risk profiles of SME borrowers, which can lead to the refinement of lending policies that are not only robust but also responsive to the multifaceted nature of business operations.

The identification of ''business duration'' as a pivotal feature points to the value of longevity and experience in business management, suggesting that longer-established SMEs may present lower credit risks due to their managers' enhanced ability to navigate external challenges. This insight could prompt financial institutions to reassess their lending criteria, potentially extending favorable terms to businesses with proven track records of stability.

Moreover, the significance of the ''number of accused cases'' as a feature underscores the imperative of legal compliance in financial health. For practitioners, this indicates that SMEs with a cleaner legal slate may be more reliable borrowers, influencing the development of risk assessment models that factor in legal and regulatory adherence.

The study's findings also highlight the ''debt-to-income ratio'' as a critical quantitative indicator, providing a straightforward yet effective measure for financial institutions to gauge an SME's capacity to service debt. This metric can be instrumental in formulating lending decisions that are underpinned by a clear assessment of the borrower's financial capacity.

Lastly, the study's exploration of ''soft information'' challenges the traditional dichotomy between relationship and transaction lending, demonstrating that qualitative assessments such as credit rating perceptions hold substantial sway even in the transactional sphere. This realization can encourage financial institutions to broaden their evaluative scope to include non-traditional data sources, thereby enriching their risk management strategies.

# <span id="page-10-0"></span>**VI. CONCLUSION AND FUTURE WORK**

The imperative to reconcile the precision of predictions with the clarity of explanations constitutes an essential research frontier, pivotal for instilling trust, transparency, and accountability in the deployment of ensemble models within practical

domains. In this study, we introduce a new multi-stage ensemble model designed to amplify the interpretability of features, thereby addressing the quintessential challenge of balancing accuracy with comprehensibility. The efficacy of our model is rigorously appraised through a quintet of evaluative metrics: accuracy (ACC), area under the curve (AUC), loss, Brier score, and Kolmogorov-Smirnov (KS) statistic. The empirical evidence garnered from our experiments substantiates the model's superior performance, underscoring its efficacy.

Harnessing annual loan ledger data from a commercial bank, we engage the SHAP explanation method to distill and elucidate the significance of pivotal features, unveiling the mechanisms at play. This approach not only underscores the SHAP method's preeminence in bestowing interpretability upon machine learning models but also accentuates the indispensable role of non-traditional data in risk assessment. In particular, we demonstrate that non-financial attributes, such as legal compliance records, the longevity of enterprises, and the seasoned insights of account managers, are paramount in identifying SME default risk.

This study transcends the conventional boundaries by offering financial institutions a novel lens through which to assess borrowers' credit risks and repayment capacities in credit loans. It equips banks with the means to achieve precise outcomes using contemporary machine learning models and adeptly navigates the potential pitfalls of over-reliance on data-driven algorithms. The insights and methodologies proffered by this study are poised to invigorate the financial sector's approach to credit risk evaluation, fostering a more discerning and nuanced appraisal of borrower profiles.

Despite the innovative approach presented in this study through a multi-stage ensemble model for assessing SME loan risk, several limitations remain. The model's effectiveness depends on the availability and quality of external data sources, such as external legal risk features and expert credit evaluations. Variability in these data sources could adversely impact the model's performance and generalizability. Although the SHAP explanation method offers valuable insights into feature importance, it relies on the completeness and relevance of the selected features. Misrepresentation or omission of key variables could lead to biased interpretations of feature significance.

Future research could expand upon these findings in several ways. For example, conducting rigorous external validation across diverse SME loan datasets from different geographic and economic contexts is essential to enhance the generalizability of the proposed model and to ensure its robustness beyond specific datasets. This effort might involve integrating real-time data and continuously updating the model to maintain accuracy and relevance. Moreover, exploring advanced interpretability techniques beyond SHAP, such as model-agnostic methods or visualization tools, could provide deeper insights into decision-making processes, thereby improving stakeholder and regulatory trust and facilitating broader adoption of the model in practical applications.

#### **DECLARATION OF COMPETING INTERESTS**

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

# **DATA AVAILABILITY AND ACCESS**

The raw datasets for this study called ChinaZJB and the UCI datasets Polish 1, Polish 2, Polish 3, Australian, and Taiwan credit datasets were uploaded to IEEE DataPort (https://dx.doi.org/10.21227/n048-7q52).

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