

## RESEARCH ARTICLE

# A Certificate-Based Ring Signcryption Scheme for Securing UAV-Enabled Private Edge Computing Systems

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**ABSTRACT** The evolving paradigm of private edge computing seamlessly incorporates the more extensive functionalities of cloud computing with localized processing. This paradigm eliminates the requirement for unmanned aerial vehicles (UAVs) to transmit large volumes of data to a centralized cloud, thereby reducing response times. UAVs' dynamic nature and dependency on unsecured and publicly accessible wireless channels make secure communication between a private edge cloud and a UAV difficult. Therefore, private edge computing-enabled UAV networks require additional security measures to protect the network and users' data. This research article introduces a certificate-based ring signcryption scheme that mitigates security concerns by utilizing the concept of hyperelliptic curve cryptography (HECC). By combining digital signature and encryption into a single operation, the proposed method takes advantage of the most advantageous characteristic of HECC (the ability to use a short key, such as 80 bits) while maintaining the same level of security as RSA and ECC. The security properties of the proposed scheme are validated by implementing a formal security evaluation method known as the random oracle model (ROM), in addition to informal security analysis. Furthermore, the computation and communication costs of the proposed scheme are evaluated and compared to those of relevant existing schemes. The performance and security analysis demonstrate that the proposed scheme enhances efficiency and security.

**INDEX TERMS** Cloud computing security, private edge computing, unmanned aerial vehicles, cryptography, hyperelliptic curve cryptography, ring signcryption, computational efficiency.

## I. INTRODUCTION

Unmanned aerial vehicles (UAVs) are expected to find widespread adaptation in diverse civilian, commercial, and military applications in the coming years due to their manoeuvrability in three-dimensional (3D) space, simplicity in control mechanisms and high precision in positioning [1], [2], [3]. In addition, the ability to perform beyond

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line-of-sight (BLOS) operations is an extra benefit, which adds to their rising popularity. To meet the increasing demand for UAV-related services in diverse applications, wireless networks beyond 5G (B5G) have additionally encouraged the development of several supporting technologies [4], [5], [6], [7]. These technologies include multi-access edge computing (MEC), software-defined networking (SDN), network function virtualization (NFV), and network slicing (NS) [8]. The UAVs will benefit from these technologies in a way that NFV will facilitate scalability and the

rapid deployment of new services by decoupling network functions from the underlying hardware. On the other hand, SDN enables the automated and programmed configuration and monitoring of UAV networks, thereby contributing to the holistic and global management of the entire infrastructure. NS enhances service customization and resource segregation by building several logical UAV networks on the same physical infrastructure. Through MEC, resource-restricted UAVs can access cloud computing services to execute various computing, storage and processing-related functions [9], [10].

A new concept has emerged under MEC, which proposes using private edge cloud systems as a potential alternative to publicly accessible edge computing solutions [11]. The primary goal of these systems is to more comprehensively address latency, security, and privacy issues while optimizing bandwidth utilization and improving the performance of resource-constrained devices. A private edge cloud system will facilitate UAVs to store, retrieve, and compute information locally while performing operations, as shown in Fig. 1. This facility will reduce the full-time dependence on centralized cloud servers for frequent data transmission, thus opening up the possibility of better response time in various applications. However, this raises security concerns since UAVs typically rely on wireless communication channels to transfer data to and from private edge cloud systems. The importance of secure key management and effective encryption and digital signature mechanisms is thus evident from the fact that these security methods address threats that compromise confidentiality and data integrity. Moreover, authentication and authorization concerns may also arise, emphasizing the importance of implementing identity verification and strict access control mechanisms. Ensuring device security includes implementing adequate security measures, adopting hardening procedures, and enabling regular updates. To proactively address potential security threats, it is crucial to prevent unauthorized access, eavesdropping and potential intrusion [12]. Similarly, high scalability, device diversity and mobility must be considered when designing security schemes for private edge computing systems operated by UAVs [13]. Additionally, in many UAV-assisted communication scenarios, the trajectory plays a crucial role, which is pivotal in ensuring the security and efficiency of UAV operations [14]. Furthermore, in mission planning for UAVs, greater emphasis should be placed on addressing the task assignment problem, as this directly impacts security considerations and operational effectiveness [15].

The motivation of this article is summed up as follows. First, UAVs are configured as smart devices with limited computing resources. Second, UAVs collect real-time data and transmit it to private edge computing over insecure channels (public channels). Consequently, there is the possibility of potential threats. Confidentiality and authentication are two essential features of every security protocol [16]. Encryption and digital signatures offer answers

for confidentiality and authenticity, respectively [17]. For devices with low resources, such as UAVs, when both features are required simultaneously and in a single logical step, signcryption is preferable. As an extra benefit, signcryption can be employed in ring settings, a method referred to as ring signcryption that can offer favorable security properties such as anonymity, spontaneity, flexibility, and equal membership.

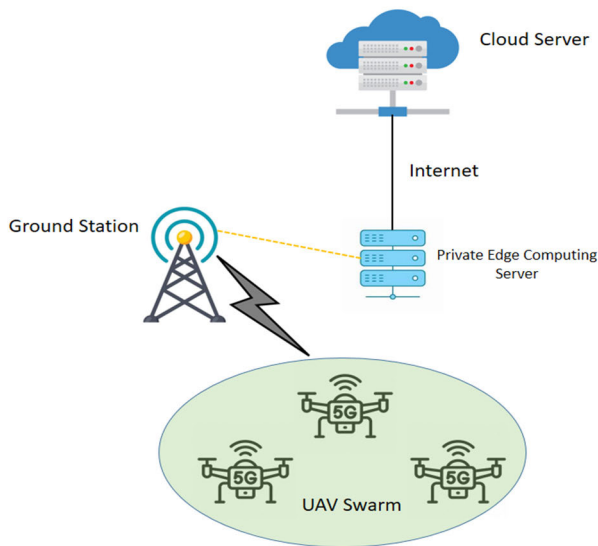
In the literature, the security and efficiency of ring signcryption schemes are typically tested with computationally challenging problems, such as RivestShamir-Adleman (RSA), bilinear pairing (BP), and elliptic curve cryptography (ECC) [18], [19]. However, the high computational and communication costs, complexity, and large-scale mathematical operations associated with the methods above make their implementation on UAVs impractical under normal conditions. As a result, we introduce a novel architecture by integrating a private edge computing capability to a UAV network by deploying a ringsigncryption scheme. Hyperelliptic curve cryptography (HECC) and certificate-based cryptography concepts are used to construct the proposed scheme. With security equivalent to RSA, BP, and ECC, HECC uses a key size of 80 bits. The main contributions made by the proposed research are summarized below:

- We present a certificate-based ring signcryption for UAV-enabled private edge computing systems utilizing HECC to provide security equivalent to RSA, BP, and ECC with a key size of only 80 bits.
- The proposed scheme performs encryption and digital signature in a one-step operation to anonymously signcrypt data.
- The security analysis of the proposed scheme is performed using the random oracle model (ROM), a formal security tool, and an informal security analysis against several known and unknown attacks to verify the security robustness of the proposed scheme.
- Finally, the proposed scheme's effectiveness is assessed by a thorough comparative analysis. The results demonstrate that the proposed scheme outperforms comparable schemes in terms of computation and communication costs.

The rest of the article is organized as follows: Section II discusses related work. Section III covers preliminaries, which detail the hyperelliptic curve, network model and structure of the proposed scheme. A security analysis of the proposed scheme is presented in Section VI. In Section V, we provide the performance analysis. Finally, Section VI comprises the conclusion.

## II. RELATED WORK

During communication, malicious attackers can get the identity and location information of UAV-enabled private edge computing. Several privacy-preserving ring signcryption schemes have been proposed in recent years to address security and privacy problems. Ring signcryption combines



**FIGURE 1.** An overview of the main entities within the UAV network and a potential cyber-attack scenario.

ring signature with encryption in a single logical step that requires minimal computation and communication costs. Moreover, ring signcryption concurrently accomplishes confidentiality, message authentication, and the complete anonymity of the signcryptor. Guo and Deng [20] developed and validated a certificateless ring signcryption (CLRSC) secure approach under the ROM. The proposed method requires just one BP operation for signcryption but three BP operations to decrypt the message. On the other hand, BP is a mathematically challenging task for a UAV to do ring signcryption. The proposed method has significant consequences for computation and communication costs.

Cai et al. [21] presented a unique solution for conditional privacy protection based on ring signcryption that combines identity-based cryptosystems with ring signatures to offer conditional privacy. However, the approach provided by Cai et al. [21] only allows for one-to-one communication. Moreover, the proposed approach was based on bilinear mapping involving computationally intensive processes. Likewise, Lai et al. [22] proposed a method based on certificateless ring signcryption that permits anonymous authentication and secure communication. If a disagreement arises, the system may also provide a tracking function for vehicles of concern. Gupta and Kumar [23] integrated a ring signature scheme with a signcryption method to provide the anonymity feature for the signcryption scheme, and they addressed the security characteristics. The proposed method is based on the ECC operation, which is somewhat more costly than HECC and uses a key size twice as large as HECC to conduct ring signature and signcryption.

Cui et al. [24] proposed a conditional privacy protection scheme for VANETs based on blockchain and ring signcryption. The scheme offers optional privacy protection for vehicle identification and location. In addition, the scheme

employs blockchain technology to eliminate the single point of failure. It immediately distributes the public keys of vehicles, contributing to constructing a ring list. However, the scheme has a high computation cost, and autonomous vehicle tracking of trusted vehicles is not considered. Guo et al. [25] proposed a similar method termed ring signcryption scheme with a conditional privacy-preserving approach based on ECC. The authors also added a tracking mark in the safety message, allowing the trusted party to distinguish malicious vehicles from the member list of the ring. A security analysis using elliptic curve discrete logarithm and elliptic curve computational Diffie-hellman assumptions in the ROM validated the security of this solution.

The scheme we intend to present in this article differs from existing ones. Our certificate-based ring signcryption scheme is based on the concept of hyperelliptic curve cryptography (HECC) for UAV-enabled private edge computing environments, which combines encryption and digital signature in a single step and takes use of HECC's smaller key size for higher security than RSA, BP, and ECC. The HECC is the best option for drones, which are typically resourceconstrained. Furthermore, to our knowledge, HECC has never been employed with ring signcryption in the literature. Tab.1 provides a summary of the existing work and the proposed scheme.

### III. PRELIMINARIES

This section details the hyperelliptic curve, network model and structure of the proposed scheme to describe its functioning and implementation. Tab.2 provides details of the notions used in the proposed scheme's algorithm.

#### A. HYPERELLIPTIC CURVE

Suppose  $F^q$  represents a finite field in which the hyperelliptic curve (HEC) is defined over it and  $q$  is the order of that field, so we can define  $HEC$  by using the following equation  $HEC : \lambda^2 + h(\alpha)\lambda = f(\alpha)$ , where  $h(\alpha) \in F^q(\alpha)$  with the degree of polynomial of  $\delta$ ,  $h(\alpha) \in F^q(\alpha)$  utilized the degree like  $2\delta + 1$  and indicates that it is a monic polynomial. Here, the main objective is to derive a Jacobian group ( $JCB(F^q)$ ) and the divisor  $\mathcal{D}$  with a value of 80 bits must be the generator of  $JCB(F^q)$ .

- Hyperelliptic curve discrete logarithm problem  
Here, we consider ( $Z = \mathcal{J}.\mathcal{D}$ ) to be the instance of the hyperelliptic curve and the goal of the challenger ( $C^A$ ) is to find  $\mathcal{J}$  from  $Z$  with the help of  $F^A$  with the advantage of  $\omega^{C^A}$  which would be called hyperelliptic curve discrete logarithm problem for  $C^A$ .
- Hyperelliptic diffie-hellman problem  
Here, we consider ( $Z = Y.\mathcal{J}.\mathcal{D}$ ) to be the instance of hyperelliptic curve discrete logarithm problem and the goal of the challenger ( $C^B$ ) is to find  $\mathcal{J}$  and  $Y$  from  $Z$  with the help of  $A^B$  with the advantage of  $\omega^{C^B}$  which would be called hyperelliptic curve diffie-hellman problem for  $C^A$ .

TABLE 1. Summary of existing work.

Work	Description	Strengths	Weaknesses
Guo and Deng [20]	Proposed a certificateless ring signcryption scheme from pairings.	The proposed scheme requires only one BP operation for signcryption and is proven to be secure under the ROM.	Performing BP is a mathematically complex task for a UAV when executing ring signcryption operation.
Cai <i>et al.</i> [21]	Presented a unique solution for conditional privacy protection based on ring signcryption.	The proposed scheme combines identity-based cryptosystems with ring signatures to offer conditional privacy.	Allowing for one-to-one communication. Moreover, the proposed approach is based on bilinear mapping operation that involves computationally intensive processes.
Lai <i>et al.</i> [22]	Proposed a method based on certificateless ring signcryption that permits anonymous authentication and secure communication.	The proposed scheme provides a tracking function for vehicles of concern in case a disagreement arises.	Incurs high computation and communication costs, making it impractical for resource-constrained UAV systems.
Gupta and Kumar [23]	Proposed an integrated method of a ring signature scheme with a signcryption.	The proposed scheme provides the anonymity feature for the signcryption scheme and addresses most of the security characteristics.	Uses a key size twice as large as HECC to conduct ring signature and signcryption .
Cui <i>et al.</i> [24]	Proposed a conditional privacy protection scheme based on blockchain and ring signcryption.	The proposed scheme offers optional privacy protection for vehicle identification and location. In addition, the scheme employs blockchain technology to eliminate the single point of failure.	Incurs high computation and communication costs. Moreover, the autonomous vehicle tracking of trusted vehicles is not considered.
Guo <i>et al.</i> [25]	Proposed a method termed ring signcryption scheme with a conditional privacy-preserving approach based on ECC.	The proposed scheme provides a tracking mark in the safety message, allowing the trusted party to distinguish malicious vehicles from the member list of the ring.	Incurs high computation and communication costs, making it impractical for resource-constrained UAV systems.
Our Scheme	We proposed a certificate-based ring signcryption scheme, based on the concept of HECC for UAV-enabled private edge computing environments.	The proposed scheme combines encryption and digital signature in a single step and takes use of HECC's smaller key size for higher security and efficiency than RSA, BP, and ECC.	Fails to address vulnerabilities posed by machine learning-based and quantum attacks.

TABLE 2. Notation guide.

S.No	Symbol	Description
1	TA	used to signify the trusted authority
2	$\chi$	identifies a received hyperelliptic curve security parameter
3	$F^q$	identifies a finite field of hyperelliptic curve with order $q$
4	$q$	identifies several hyperelliptic curves and their values as $q = 80$ bits
5	$MPB$	master public key of TA
6	$\sigma$	secret key of TA
7	$\mathcal{D}$	divisor on the hyperelliptic curve with a value of $\mathcal{D} = 80$ bits
8	$HEC$	used to signify a genus 2 hyperelliptic curve
9	$H_A, H_B, H_C, H_D$	identifies four irreversible, collision resistant, and one-way hash function from SHA family
10	$ID_{Act}$	each actor identity
11	$A_i$	each joining actor
12	$C_i$	each actor certificate
13	$C_r$	receiver actor certificate
14	$C_{SAct}$	sender actor certificate, which belongs to a sending group
15	$D_R$	encryption of plain text through a secret key $R$
16	$ID_{SAct}$	sender actor identity which belongs to a sender group
17	$ID_r$	receiver actor identity
18	$CIPR$	ciphertext
19	$D_R$	decryption of encrypted text through a secret key $R$
20	$R$	secret key, which is used for decryption and encryption encrypted and plain text
21	$M$	plain text

## B. NETWORK MODEL

The network model of the proposed scheme comprises the entities, which include an unmanned aerial vehicle (UAV), a ground station (GS), private edge computing (PEC), and cloud computing as illustrated in Fig.1. UAVs, the primary entity of the proposed scheme, have the potential to play a key role in performing a variety of tasks, including parcel delivery, surveillance, etc. The UAVs have essential equipment such as a camera, inertial measurement unit (IMU), sensors, global positioning system (GPS) unit, and flight controller. A wireless connection is established between the UAV and the PEC server via the ground station, which delegates and plans computational duties to the PEC to facilitate rapid processing and local data storage. A certificate request is initiated as the initial step, functioning as the trusted authority (TA). The TA will issue a certificate for the designated UAV and transmit it via an open channel upon receipt of such a request. Before transmitting a message from TA's certificate to PEC, UAV encrypts it with a ring signcryption using the services of GS. When a receiver UAV eventually needs to decrypt the ring-signcrypted message, it will transmit a certificate request

to the PEC, which functions as the TA. The TA will then generate a certificate for the requesting UAV and send it to it over an open channel. UAV first produces TA's private key when it receives a certificate and then verifies the signcrypted text.

## C. CONSTRUCTION OF THE PROPOSED SCHEME

This section explains the certificate-based ring signcryption scheme for UAV-enabled private edge computing systems. The key notations and definitions used in the proposed scheme are listed in Tab.1. The proposed scheme consists of five phases: setup, key and certificate generation, certificate-based ring signcryption, and certificate-based ring unsigncryption. The following are descriptions of each phase.

1. *Setup*: When a trusted authority (TA) receives the hyperelliptic curve security parameter  $\chi$ , it executes the setup algorithm to make the secret key and public parameters set that are followed: it chooses  $\sigma$  randomly from  $F^q$  and computes  $\mathcal{D}$ . TA sets  $MPB$  as his/her master public key and  $\sigma$  as a secret key. Then, TA chooses four irreversible, collision-resistant, and one-way hash functions ( $H_A, H_B, H_C, H_D$ ) from the SHA family. Finally, TA set  $\lambda = \{MPB, HEC, \mathcal{D}, F^q, H_A, H_B, H_C, H_D\}$  as a public parameter set.
2. *Key and certificate generation*: Given the actor's  $A_i$  identity  $ID_{Act}$ , TA and  $A_i$  together execute this phase for making the private key, public key, and certificate. For this process,  $A_i$  first, choose  $\mathcal{G}_i$  randomly from  $F^q$  and compute  $\varphi_i = \mathcal{G}_i \cdot \mathcal{D}$ , then send  $(\varphi_i, ID_{Act})$  to TA. When TA receives  $(\varphi_i, ID_{Act})$ , it computes  $C_i = \varphi_i + \ell_i \cdot \mathcal{D}$ , where  $\ell_i$  is picked randomly by TA from  $F^q$ ,  $E_i = H_A(\sigma \cdot \varphi_i) + \ell_i + \sigma \cdot H_B(C_i, ID_{Act}, MPB)$ , and send  $C_i$  and  $E_i$  to  $A_i$  by using an open network. When  $(C_i, E_i)$  received to  $A_i$ , it computes  $\alpha_i = E_i - H_A(\mathcal{G}_i \cdot MPB)$ ,  $\beta_i = \alpha_i + \mathcal{G}_i$ , and compare  $\beta_i \cdot \mathcal{D} = C_i + H_B(C_i, ID_{Act}, MPB) \cdot MPB$  if this equation is satisfied, then it accepts the certificate.
3. *Certificate-based ring signcryption*: Suppose  $M$  is a message to be delivered,  $ID_{SAct}$  belongs to  $\mathcal{J} = \{ID_{SAct1}, ID_{SAct2}, ID_{SAct3}, \dots, ID_{SActm}\}$ ,  $C_{SAct}$  belongs to  $\mathcal{Q} = \{C_{SAct1}, C_{SAct2}, C_{SAct3}, \dots, C_{SActm}\}$ , and  $\lambda = \{MPB, HEC, \mathcal{D}, F^q, H_A, H_B, H_C, H_D\}$  will be taken as input, and then the following computation can be made in the proposed algorithm:
  - The sender with  $ID_{SAct}$  and  $C_{SAct}$  can choose  $\mathcal{K}$  randomly from  $F^q$  and compute  $\mathcal{E} = \mathcal{K} \cdot \mathcal{D}$ .
  - Compute  $\Omega = \mathcal{K} \cdot (C_r + H_B(C_r, ID_r, MPB) \cdot MPB)$  and  $R = H_C(\Omega)$ .
  - Compute  $CIPR = E_R(M)$  and  $S = \mathcal{K} + \beta_{SAct} \cdot v$  where  $v = H_D(C_{SAct}, ID_{SAct}, \mathcal{E}, CIPR)$ ,  $\beta_{SAct}$  belongs to  $PRTS = \{\beta_{SAct1}, \beta_{SAct2}, \beta_{SAct3}, \dots, \beta_{SActm}\}$ , which is the private key of one of the senders from the group.
  - Finally, it sends  $(S, CIPR, \mathcal{E})$  to the receiver.
4. *Certificate-based ring unsigncryption*: When  $(S, CIPR, \mathcal{E})$  is received, the receiver does the following for unsigncryption executions.

- Compute  $\Omega = \beta_r \cdot \mathcal{E}$  and  $R = H_C(\Omega)$
- Compute  $M = D_{\mathbb{R}}(CIPR)$  and do for testing the equality of the following equation:  
 $S \cdot \mathcal{D} = \mathcal{E} + C_{SAct} \cdot H_D(C_{SAct}, ID_{SAct}, \mathcal{E}, CIPR) + (C_{SAct}, ID_{SAct}, \mathcal{E}, CIPR) \cdot H_B(C_{SAct}, ID_{SAct}, MPB)$   
 $MPB$  if it is held, then the receiver accepts the triple of ring signcryption.

OR

- It sets  $H_D(C_{SAct}, ID_{SAct}, \mathcal{E}, CIPR) = r$  and  $H_B(C_{SAct}, ID_{SAct}, MPB) = z$ .  
 It computes  $S \cdot \mathcal{D} = \mathcal{E} + r \cdot C_{SAct} + z \cdot MPB$ , if it is held, the receiver accepts the triple ring signcryption.

5. *New device/actor adding phase:* Given the new actor's  $A_{newi}$  identity  $ID_{newi}$ , TA and  $A_{newi}$  together execute this phase for making the private key, public key, and certificate. For this process,  $A_{newi}$  first, chooses  $\mathcal{G}_{newi}$  randomly from  $F^q$  and then computes  $\varphi_{newi} = \mathcal{G}_{newi} \cdot \mathcal{D}$ , sends  $(\varphi_{newi}, ID_{newi})$  to TA. When TA receives  $(\varphi_{newi}, ID_{newi})$ , it first computes  $C_{newi} = \varphi_{newi} + \ell_{newi} \cdot \mathcal{D}$ , where  $\ell_{newi}$  is picked randomly by TA from  $F^q$ ,  $E_{newi} = H_A(\sigma \cdot \varphi_{newi}) + \ell_{newi} + \sigma \cdot H_B(C_{newi}, ID_{newi}, MPB)$ , and send  $C_{newi}$  and  $E_{newi}$  to  $A_{newi}$  by using an open network. When  $(C_{newi}, E_{newi})$  received to  $A_{newi}$ , it computes  $\alpha_{newi} = E_{newi} - H_A(\mathcal{G}_{newi} \cdot MPB)$ ,  $\beta_{newi} = \alpha_{newi} + \mathcal{G}_{newi}$ , and compare  $\beta_{newi} \cdot \mathcal{D} = C_{newi} + H_B(C_{newi}, ID_{newi}, MPB) \cdot MPB$  if this equation is satisfied, then it accepts the certificate.

#### D. CORRECTNESS

When  $(S, CIPR, \mathcal{E})$  is received, the receiver does unsigncryption and verifies the equality of the equation by performing the following operation:

$$\begin{aligned}
 S \cdot \mathcal{D} &= \mathcal{E} + r \cdot C_{SAct} + r \cdot z \cdot MPB \\
 &= (\mathcal{K} + \beta_{SAct} \cdot H_D(C_{SAct}, ID_{SAct}, \mathcal{E}, CIPR)) \cdot \mathcal{D} \\
 &= (\mathcal{K} \cdot \mathcal{D} + \beta_{SAct} \cdot H_D(C_{SAct}, ID_{SAct}, \mathcal{E}, CIPR) \cdot \mathcal{D}) \\
 &= (\mathcal{E} + \beta_{SAct} \cdot H_D(C_{SAct}, ID_{SAct}, \mathcal{E}, CIPR) \cdot \mathcal{D}) \\
 &= (\mathcal{E} + \beta_{SAct} \cdot \mathcal{D} \cdot H_D(C_{SAct}, ID_{SAct}, \mathcal{E}, CIPR)) \\
 &= (\mathcal{E} + (C_{SAct} \\
 &\quad + H_B(C_{SAct}, ID_{SAct}, MPB) \cdot MPB) \\
 &\quad \cdot H_D(C_{SAct}, ID_{SAct}, \mathcal{E}, CIPR)) \\
 &= (\mathcal{E} + (C_{SAct} \cdot H_D(C_{SAct}, ID_{SAct}, \mathcal{E}, CIPR) \\
 &\quad + H_D(C_{SAct}, ID_{SAct}, \mathcal{E}, CIPR) \\
 &\quad \cdot H_B(C_{SAct}, ID_{SAct}, MPB) \cdot MPB)) \\
 &= (\mathcal{E} + (C_{SAct} \cdot r + z \cdot MPB))
 \end{aligned}$$

Also, compute  $\Omega = \beta_r \cdot \mathcal{E}$  as  $\beta_r \cdot \mathcal{E} = (\alpha_r + \mathcal{G}_r) \cdot \mathcal{E} = (E_i - H_A(\sigma \cdot \varphi_i) + \mathcal{G}_r) \cdot \mathcal{E} = (E_i - H_A(\sigma \cdot \varphi_i) + \mathcal{G}_r) \cdot \mathcal{K} \cdot \mathcal{D} = (E_i \cdot \mathcal{D} - H_A(\sigma \cdot \varphi_i) \cdot \mathcal{D} + \mathcal{G}_r \cdot \mathcal{D}) \cdot \mathcal{K}$ .

#### IV. SECURITY ANALYSIS

This section presents formal and informal security analyses, details of which are provided in the following subsections.

#### A. FORMAL SECURITY ANALYSIS

We consider the following theorems: unforgeability against type 1 forger ( $F^A$ ), unforgeability against type 2 forger ( $F^B$ ), confidentiality against type 1 adversary ( $A^A$ ), and confidentiality against type 2 adversary ( $A^B$ ), respectively.  $F^A$  and  $A^A$  can act as an outside adversary and forger, respectively, with the ability to change the user's public key without having access to the master secret key. Next,  $F^B$  and  $A^B$  can act as an insider forger and an enemy, respectively, with the ability to steal the master secret key but not the user's public key. With the help of the following theorems, we may thus perform security proofs.

*Theorem 1 (Confidentiality Against  $A^A$ ):* Here, we consider  $(Z = Y \cdot \mathcal{J} \cdot \mathcal{D})$  is the instance of hyperelliptic curve discrete logarithm problem and the goal of the challenger ( $C^A$ ) is to find  $\mathcal{J}$  and  $Y$  from  $Z$  with the help of  $A^A$  with the advantage of  $\omega^{C^A}$ . We also consider  $\omega^{A^A}$  of type 1 adversary ( $A^A$ ) advantages. To prove this theorem, the following query will correspond between  $CA$  and the setup phase. The possible probability is as follows:

$$\omega^{C^A} = \frac{1}{\text{Query}_{H_B}} \left( 1 - \frac{1}{\text{Query}_{H_B}} \right)^{\text{Query}_{PKQ} + \text{Query}_{CRQ} + \text{Query}_{U_{signQ}}} \left( 1 - \frac{\text{Query}_{H_B}}{\text{Query}} \right) \text{Query}_{SignQ} \omega^{A^A}$$

*Setup:* On the response of  $PB = \sigma \cdot \mathcal{D}$  and  $\lambda = \{MPB, H_{EC}, \mathcal{D}, F^q, H_A, H_B, H_C, H_D\}$ ,  $A^A$  send the target identity ( $ID_{Acti}^*$ ) to  $C^A$ .

*Query $_{H_A}$ :* Given  $\gamma_{Acti}$ ,  $C^A$  check-in  $L_{H_A}$ , if  $L_{H_A}$  contains  $(\gamma_{Acti}, \rho_{Acti})$  then it will send  $\rho_{Acti}$  to  $A^A$ , otherwise, it picks  $\rho_{Acti}$  randomly, including  $(\gamma_{Acti}, \rho_{Acti})$  into  $L_{H_A}$ , and send  $\rho_{Acti}$  to  $A^A$ .

*Query $_{H_B}$ :* Given  $(C_{Acti}, ID_{Acti}, MPB)$ ,  $C^A$  checks in  $L_{H_B}$ , if  $L_{H_B}$  contains  $(C_{Acti}, ID_{Acti}, MPB, \pi_{Acti})$  then it will send  $\pi_{Acti}$  to  $A^A$ , otherwise, it picks  $\pi_{Acti}$  randomly, include  $(C_{Acti}, ID_{Acti}, MPB, \pi_{Acti})$  into  $L_{H_B}$ , and send  $\pi_{Acti}$  to  $A^A$ .

*Query $_{H_C}$ :* Given  $(R_{Acti})$ ,  $C^A$  check in  $L_{H_C}$ , if  $L_{H_C}$  contain  $(R_{Acti}, \Delta_{Acti})$  then it will send  $\Delta_{Acti}$  to  $A^A$ , otherwise, it picks  $\Delta_{Acti}$  randomly, including  $(R_{Acti}, \Delta_{Acti})$  into  $L_{H_C}$ , and send  $\Delta_{Acti}$  to  $A^A$ .

*Query $_{H_D}$ :* Given  $(C_{SActi}, ID_{SActi}, \mathcal{E}, CIPR)$ ,  $C^A$  check in  $L_{H_D}$ , if  $L_{H_D}$  contain  $(C_{SActi}, ID_{SActi}, \mathcal{E}, CIPR, \partial_{Acti})$  then it will send  $\partial_{Acti}$  to  $A^A$ , otherwise, it picks  $\partial_{Acti}$  randomly, including  $(C_{SActi}, ID_{SActi}, \mathcal{E}, CIPR)$  into  $L_{H_D}$ , and send  $\partial_{Acti}$  to  $A^A$ .

*Query $_{C_{UQ}}$ :* In the create user query ( $Query_{C_{UQ}}$ ), when  $C^A$  received a request from  $A^A$ , it can check if  $ID_{Acti}^* = ID_{Acti}$ , when it is satisfied, then  $C^A$  choose  $\mathcal{G}_{Acti}$  and  $\ell_{Acti}$  randomly.  $C^A$  compute  $\varphi_{Acti} = \mathcal{G}_{Acti} \cdot \mathcal{D}$ ,  $\Gamma_{Acti} = \ell_{Acti} \cdot \mathcal{D}$ ,  $C_{Acti} = \Gamma_{Acti} + \varphi_{Acti}$ , and include  $(\Gamma_{Acti}, \varphi_{Acti}, \mathcal{G}_{Acti}, C_{Acti}, \ell_{Acti}, \perp)$  into  $L_{C_{UQ}}$  and send  $\ell_{Acti}$  to  $A^A$ . Otherwise,  $C^A$  choose  $\mathcal{G}_{Acti}$  and  $\alpha_{Acti}$  randomly, perform  $Query_{H_C}$  to get  $\Delta_{Acti}$  and compute  $\varphi_{Acti} = \mathcal{G}_{Acti} \cdot \mathcal{D}$ ,  $\Gamma_{Acti} = \alpha_{Acti} \cdot \mathcal{D} - \Delta_{Acti} \cdot MPB$ ,  $C_{Acti} = \Gamma_{Acti} + \varphi_{Acti}$ , and  $\beta_{Acti} = \alpha_{Acti} + \mathcal{G}_{Acti}$ .

Then,  $C^A$  include  $(\Gamma_{Acti}, \varphi_{Acti}, \mathcal{G}_{Acti}, C_{Acti}, \ell_{Acti}, \beta_{Acti})$  into  $L_{C_{UQ}}$  and send  $\beta_{Acti}$  to  $A^A$ .

*Query $_{P_{UQ}}$* : In the private value query ( $Query_{P_{UQ}}$ ), when  $C^A$  received a request from  $A^A$ , it can check if  $\mathcal{G}_{Acti}$  is existed in  $L_{P_{UQ}}$ , then  $C^A$  send  $\mathcal{G}_{Acti}$  to  $C^A$ . Otherwise,  $C^A$  performs a create user query ( $Query_{C_{UQ}}$ ) and sends  $\mathcal{G}_{Acti}$  to  $A^A$ .

*Query $_{P_{KQ}}$* : In the private key query ( $Query_{P_{KQ}}$ ), when  $C^A$  received a request from  $AA$ , it can check if  $ID_{Acti}^* = ID_{Acti}$  when it is satisfied then  $CA$  will quite, otherwise  $CA$  can check if  $\beta_{Acti}$  exists in  $L_{P_{KQ}}$ , then  $C^A$  send  $\beta_{Acti}$  to  $C^A$ . Else,  $C^A$  performs a create user query ( $Query_{C_{UQ}}$ ) and sends  $\beta_{Acti}$  to  $A^A$ .

*Query $_{C_{RQ}}$* : In the certificate generation query ( $Query_{C_{RQ}}$ ), when  $C^A$  received a request from  $AA$ , it can check if  $C_{Acti}$  exists in  $L_{P_{UQ}}$ , then  $C^A$  send  $C_{Acti}$  to  $C^A$ . Otherwise,  $C^A$  performs a create user query ( $Query_{C_{UQ}}$ ) and send  $C_{Acti}$  to  $A^A$ .

*Query $_{R_{PBQ}}$* : In the replaced public key query ( $Query_{C_{RQ}}$ ), given  $ID_{Acti}$  and  $\varphi_{Acti}$ , it can check if  $ID_{Acti}^* = ID_{Acti}$  when it is satisfied then  $C^A$  will quite, otherwise  $C^A$  can replace  $\varphi_{Acti}$  on  $\varphi_{Acti}$  and  $C_{Acti}$  on  $C_{Acti}$ .

*Query $_{S_{ignQ}}$* : Suppose  $M$  be a message to be delivered,  $ID_{Acti}$  belongs to  $\mathcal{J} = \{ID_{SAct1}, ID_{SAct2}, ID_{SAct3}, \dots, ID_{SActm}\}$ ,  $C_{SActi}$  belongs to  $\mathcal{Q} = \{C_{SAct1}, C_{SAct2}, C_{SAct3}, \dots, C_{SActm}\}$ , and  $\mathcal{A} = \{MPB, HEC, \mathcal{D}, F^q, H_A, H_B, H_C, H_D\}$  will be taken is input, if  $ID_{Acti}^* = ID_{Acti}$ . If yes,  $C^A$  perform  $Query_{C_{RQ}}$  on  $ID_{Acti}$  to get  $C_{Acti}$  and execute  $Query_{H_B}$  on  $(C_{Acti}, ID_{Acti}, MPB)$  to get  $\pi_{Acti}$ . Further,  $C^A$  choose  $\partial_{Acti}$  and  $S_{Acti}$  randomly from  $F^q$  and compute  $\mathcal{E}_{Acti} = S_{Acti} \cdot \mathcal{D} - \partial_{Acti} \cdot C_{Acti} - \pi_{Acti} \cdot \partial_{Acti} \cdot \mathcal{L} \cdot \mathcal{D}$ . It also computes  $\Omega_{Acti} = \beta_{Acti} \cdot \mathcal{E}_{Acti}$  on  $ID_{Acti}$  and compute  $CIPR = E_{\Delta_{Acti}}(M)$ . Then, send  $(S_{Acti}, CIPR, \mathcal{E}_{Acti})$  to  $A^A$ .

*Query $_{U_{signQ}}$* : Suppose  $(S_{Acti}, CIPR, \mathcal{E}_{Acti})$ , one of the sender's identity  $ID_{SAct}$  belongs to  $\mathcal{J} = \{ID_{SAct1}, ID_{SAct2}, ID_{SAct3}, \dots, ID_{SActm}\}$ , and receiver identity  $ID_{RAct}$ , if  $ID_{RAct} = ID_{Acti}^*$ . If yes,  $C^A$  quit; otherwise, it performs the typical un-Signcryption algorithm to get  $M$  and dispatch it to  $A^A$ .

*Challenge*:  $A^A$  can choose and transmit two same nature and different size plaintext  $(M^{1*}, M^{2*})$  to  $C^A$ . So,  $C^A$  can execute  $Query_{C_{UQ}}$  on  $ID_{RAct}$  and  $ID_{Acti}^*$ , Private Value Query ( $Query_{P_{UQ}}$ ) on  $ID_{RAct}$  and  $ID_{Acti}^*$ ,  $Query_{C_{RQ}}$  on  $ID_{RAct}$  and  $ID_{Acti}^*$ , and get the value of hash queries. According to the processed queries, choose  $\rho \in \{0, 1\}$  randomly and perform the execution process to make the signcrypted tuple  $(S_{Acti}^*, CIPR^*, \mathcal{E}_{Acti}^*)$  and transmit it to  $A^A$ .

*Guess*:  $A^A$  guesses  $\rho^A \in \{0, 1\}$ . If  $\rho^A = \rho$ ,  $C^A$  wins, other he will fail.

*Probability analysis*: Suppose  $A^A$  performs all Hash Queries  $Query_{H_i}$  ( $i = A, B, C, D$ ), Create User Query ( $Query_{C_{UQ}}$ ), Private Value Query ( $Query_{P_{UQ}}$ ), Private Key Query ( $Query_{P_{KQ}}$ ), Certificate Generation Query ( $Query_{C_{RQ}}$ ), Replaced Public Key Query ( $Query_{C_{RQ}}$ ), Signcryption Query ( $Query_{S_{ignQ}}$ ), and Un-Signcryption Query ( $Query_{U_{signQ}}$ ). Ultimately, we can ensure the availability of the following three events.

1. In the event 1 ( $E_1$ ),  $C^A$  never quite in  $Query_{P_{KQ}}$ ,  $Query_{C_{RQ}}$ ,  $Query_{S_{ignQ}}$ , and  $Query_{U_{signQ}}$
  2. In the event 2 ( $E_2$ ),  $C^A$  generates a valid signature or cipher text
  3. In the event 3 ( $E_3$ ),  $ID_{Acti}^* = ID_{SAct}$
- The probability for event 1 ( $E_1$ ) is defined as  $Pr(E_1) = (1 - 1/Query_{H_B})^{Query_{P_{KQ}} + Query_{C_{RQ}} + Query_{U_{signQ}}}$  ( $1 - Query_{H_B}/Query$ )  $Query_{S_{ignQ}}$ , the probability for event 1 and event 2 as  $Pr(E_1|E_2) \geq \omega^{A^A}$ , the probability for event 1, event 2, and event 3 as  $Pr(E_1|E_2 \wedge E_3) \geq 1/Query_{H_B}$ . The combined probability of the above events is as follows:

$$\omega^{C^A} = \frac{1}{Query_{H_B}} \left( 1 - \frac{1}{Query_{H_B}} \right)^{Query_{P_{KQ}} + Query_{C_{RQ}} + Query_{U_{signQ}}} \left( 1 - \frac{Query_{H_B}}{Query} \right) Query_{S_{ignQ}} \omega^{A^A}$$

Notice that under the above theorem, the adversary and challenger must discover a solution for hyperelliptic curve discrete logarithm to decrypt an encrypted message. If we examine the proposed scheme, we see that the message is encrypted using a secret key  $R = H_C(\Omega)$ , where  $\Omega = \mathcal{H} \cdot (C_r + H_B(C_r, ID_r, MPB) \cdot MPB)$  in which the attacker failed to get  $R$ . This is because finding the value  $\mathcal{H}$  from  $\Omega$  is impractical and will result in a hyperelliptic curve discrete logarithm.

*Theorem 2 (Confidentiality Against  $A^B$ )*: Here, we consider  $(Z = Y \cdot \mathcal{J} \cdot \mathcal{D})$  is the instance of hyperelliptic curve discrete logarithm problem and the goal of the challenger ( $C^B$ ) is to find  $\mathcal{J}$  and  $Y$  from  $Z$  with the help of  $A^B$  with the advantage of  $\omega^{C^B}$ . We also consider  $\omega^{A^B}$  of type 2 adversary ( $A^B$ ) advantages. So, for the proof of this theorem, the following query will correspond to  $C^B$  and  $A^B$  after the setup phase. The combined probability of the above events is as follows:

$$\omega^{C^B} = \frac{1}{Query_{H_B}} \left( 1 - \frac{1}{Query_{H_B}} \right)^{Query_{P_{KQ}} + Query_{C_{RQ}} + Query_{U_{signQ}}} \left( 1 - \frac{Query_{H_B}}{Query} \right) Query_{S_{ignQ}} \omega^{A^B}$$

*Setup*: On the response of  $PB = \sigma \cdot \mathcal{D}$ ,  $\sigma$  and  $\lambda = \{MPB, HEC, \mathcal{D}, F^q, H_A, H_B, H_C, H_D\}$ ,  $A^B$  send the target identity  $(ID_{Acti}^*)$  to  $C^B$ .

*Queries*: The queries such as Hash Queries  $Query_{H_i}$  ( $i = A, B, C, D$ ), Create User Query ( $Query_{C_{UQ}}$ ), Private Value Query ( $Query_{P_{UQ}}$ ), Private Key Query ( $Query_{P_{KQ}}$ ), Certificate Generation Query ( $Query_{C_{RQ}}$ ), and Signcryption Query ( $Query_{S_{ignQ}}$ ) that will perform in this Theorem as same as used in Theorem 1.

*Query $_{U_{signQ}}$* : Suppose  $(S_{Acti}, CIPR, \mathcal{E}_{Acti})$ , one of the sender's identity  $ID_{SAct}$  belongs to  $\mathcal{J} = \{ID_{SAct1}, ID_{SAct2}, ID_{SAct3}, \dots, ID_{SActm}\}$ , and receiver identity  $ID_{RAct}$ , if  $ID_{RAct} = ID_{Acti}^*$ . If yes,  $C^B$  quiet; otherwise, it performs the normal un-signcryption algorithm to get  $M$  and dispatch it to  $A^B$ .

**Challenge:**  $A^B$  can choose and transmit two same nature and different size plaintext ( $M^{1*}, M^{2*}$ ) to  $C^B$ . So,  $C^B$  can execute  $Query_{CUQ}$  on  $ID_{RAct}$  and  $ID_{Acti}^*$ , *Private Value Query* ( $Query_{PUQ}$ ) on  $ID_{RAct}$  and  $ID_{Acti}^*$ ,  $Query_{CRQ}$  on  $ID_{RAct}$  and  $ID_{Acti}^*$ , and get the value of hash queries. According to the processed queries, choose  $\rho \in \{0, 1\}$  randomly and perform the execution process to make the signcrypted tuple ( $S_{Acti}^*$ ,  $CIPR^*$ ,  $\mathcal{E}_{Acti}^*$ ) and transmit it to  $A^B$ .

**Guess:**  $A^B$  guesses  $\rho^B \in \{0, 1\}$ . If  $\rho^B = \rho$ ,  $C^B$  wins, other he will fail.

**Probability Analysis:** Suppose  $A^B$  performs all Hash Queries  $Query_{H_i}$  ( $i = A, B, C, D$ ), *Create User Query* ( $Query_{CUQ}$ ), *Private Value Query* ( $Query_{PUQ}$ ), *Private Key Query* ( $Query_{PKQ}$ ), *Certificate Generation Query* ( $Query_{CRQ}$ ), *Signcryption Query* ( $Query_{SignQ}$ ), and *Un-Signcryption Query* ( $Query_{U_{signQ}}$ ). Ultimately, we can ensure the availability of the following three events.

1. In the event 1 ( $E_1$ ),  $C^A$  never quite in  $Query_{PKQ}$ ,  $Query_{SignQ}$ , and  $Query_{U_{signQ}}$
2. In the event 2 ( $E_2$ ),  $C^A$  generates a valid signature or cipher text
3. In the event 3 ( $E_3$ ),  $ID_{Acti}^* = ID_{SAct}$

The probability for event 1 ( $E_1$ ) is defined as  $Pr(E_1) = (1 - 1/Query_{HB})^{Query_{PKQ} + Query_{U_{signQ}}}$  ( $1 - Query_{HB}/Query$ )  $Query_{SignQ}$ , the probability for event 1 and event 2 as  $Pr(E_1|E_2) \geq \omega^{A^B}$ , the probability for event 1, event 2, and event 3 as  $Pr(E_1|E_2 \wedge E_3) \geq 1/Query_{HB}$ . The combined probability of the above events is as follows:

$$\omega^{C^B} = \frac{1}{Query_{HB}} \left( 1 - \frac{1}{Query_{HB}} \right)^{Query_{PKQ} + Query_{CRQ} + Query_{U_{signQ}}} \left( 1 - \frac{Query_{HB}}{Query} \right) Query_{SignQ} \omega^{A^B}$$

To decrypt an encrypted message, an adversary or a challenger must solve a hyperelliptic curve discrete logarithm, as shown in the theorem above. If we examine the proposed scheme, we will see that the message has been decrypted using a secret key  $R = H_C(\Omega)$ , where  $\Omega = \beta_r$ .  $\mathcal{E}$  in which the attacker failed to get  $R$ , because finding the value  $\beta_r$  from  $\Omega$  is infeasible and will result in hyperelliptic curve discrete logarithm.

**Theorem 3 (Unforgeability Against  $F^A$ ):** Here, we consider ( $Z = \mathcal{J} \cdot \mathcal{D}$ ) is the instance of hyperelliptic curve discrete logarithm problem and the goal of the challenger ( $C^A$ ) is to find  $\mathcal{J}$  from  $Z$  with the help of  $F^A$  with the advantage of  $\omega^{C^A}$ . We also consider  $\omega^{F^A}$  of type 1 forger ( $F^A$ ) advantages. So, to prove this theorem, the following query will correspond between  $C^A$  and  $F^A$  after the setup phase.

**Setup:** On the response of  $PB = \sigma \cdot \mathcal{D}$  and  $\lambda = \{MPB, HEC, \mathcal{D}, F^q, H_A, H_B, H_C, H_D\}$ ,  $F^A$  send the target identity ( $ID_{Acti}^*$ ) to  $C^A$ .

**Query $_{HA}$ :** Given  $\gamma_{Acti}$ ,  $C^A$  check in  $L_{HA}$ , if  $L_{HA}$  contain ( $\gamma_{Acti}, \rho_{Acti}$ ) then it will send  $\rho_{Acti}$  to  $F^A$ , otherwise, it pick  $\rho_{Acti}$  randomly, include ( $\gamma_{Acti}, \rho_{Acti}$ ) into  $L_{HA}$ , and send  $\rho_{Acti}$  to  $F^A$ .

**Query $_{HB}$ :** Given ( $C_{Acti}, ID_{Acti}, MPB$ ),  $C^A$  check in  $L_{HB}$ , if  $L_{HB}$  contain ( $C_{Acti}, ID_{Acti}, MPB, \pi_{Acti}$ ) then it will send  $\pi_{Acti}$  to  $F^A$ , otherwise, it pick  $\pi_{Acti}$  randomly, include ( $C_{Acti}, ID_{Acti}, MPB, \pi_{Acti}$ ) into  $L_{HB}$ , and send  $\pi_{Acti}$  to  $F^A$ .

**Query $_{HC}$ :** Given ( $R_{Acti}$ ),  $C^A$  check in  $L_{HC}$ , if  $L_{HC}$  contain ( $R_{Acti}, \Delta_{Acti}$ ) then it will send  $\Delta_{Acti}$  to  $F^A$ , otherwise, it picks  $\Delta_{Acti}$  randomly, include ( $R_{Acti}, \Delta_{Acti}$ ) into  $L_{HC}$ , and send  $\Delta_{Acti}$  to  $F^A$ .

**Query $_{HD}$ :** Given ( $C_{SActi}, ID_{SActi}, \mathcal{E}, CIPR$ ),  $C^A$  check in  $L_{HD}$ , if  $L_{HD}$  contain ( $C_{SActi}, ID_{SActi}, \mathcal{E}, CIPR, \partial_{Acti}$ ) then it will send  $\partial_{Acti}$  to  $F^A$ , otherwise, it picks  $\partial_{Acti}$  randomly, include ( $C_{SActi}, ID_{SActi}, \mathcal{E}, CIPR$ ) into  $L_{HD}$ , and send  $\partial_{Acti}$  to  $F^A$ .

**Query $_{CUQ}$ :** In the create user query ( $Query_{CUQ}$ ), when  $C^A$  received a request from  $F^A$ , it can check if  $ID_{Acti}^* = ID_{Acti}$  when it is satisfied, then  $C^A$  choose  $\mathcal{G}_{Acti}$  and  $\ell_{Acti}$  randomly.  $C^A$  compute  $\varphi_{Acti} = \mathcal{G}_{Acti} \cdot \mathcal{D}$ ,  $\Gamma_{Acti} = \ell_{Acti} \cdot \mathcal{D}$ ,  $C_{Acti} = \Gamma_{Acti} + \varphi_{Acti}$ , and include ( $\Gamma_{Acti}, \varphi_{Acti}, \mathcal{G}_{Acti}, C_{Acti}, \ell_{Acti}, \perp$ ) into  $L_{CUQ}$  and send  $\ell_{Acti}$  to  $F^A$ . Otherwise,  $C^A$  choose  $\mathcal{G}_{Acti}$  and  $\alpha_{Acti}$  randomly, perform  $Query_{HC}$  to get  $\Delta_{Acti}$  and compute  $\varphi_{Acti} = \mathcal{G}_{Acti} \cdot \mathcal{D}$ ,  $\Gamma_{Acti} = \alpha_{Acti} \cdot \mathcal{D} - \Delta_{Acti} \cdot MPB$ ,  $C_{Acti} = \Gamma_{Acti} + \varphi_{Acti}$ , and  $\beta_{Acti} = \alpha_{Acti} + \mathcal{G}_{Acti}$ . Then,  $C^A$  include ( $\Gamma_{Acti}, \varphi_{Acti}, \mathcal{G}_{Acti}, C_{Acti}, \ell_{Acti}, \beta_{Acti}$ ) into  $L_{CUQ}$  and send  $\beta_{Acti}$  to  $F^A$ .

**Query $_{PUQ}$ :** In the private value query ( $Query_{PUQ}$ ), when  $C^A$  received a request from  $F^A$ , it can check if  $\mathcal{G}_{Acti}$  exists in  $L_{PUQ}$ , then  $C^A$  send  $\mathcal{G}_{Acti}$  to  $C^A$ . Otherwise,  $C^A$  performs a create user query ( $Query_{CUQ}$ ) and sends  $\mathcal{G}_{Acti}$  to  $F^A$ .

**Query $_{PKQ}$ :** In the private key query ( $Query_{PKQ}$ ), when  $C^A$  received a request from  $F^A$ , it can check if  $ID_{Acti}^* = ID_{Acti}$  when it is satisfied then  $C^A$  will quite, otherwise  $C^A$  can check if  $\beta_{Acti}$  exists in  $L_{PKQ}$ , then  $C^A$  send  $\beta_{Acti}$  to  $C^A$ . Else,  $C^A$  performs a create user query ( $Query_{CUQ}$ ) and sends  $\beta_{Acti}$  to  $F^A$ .

**Query $_{CRQ}$ :** In the certificate generation query ( $Query_{CRQ}$ ), when  $C^A$  received a request from  $F^A$ , it can check if  $C_{Acti}$  exists in  $L_{PUQ}$ , then  $C^A$  send  $C_{Acti}$  to  $C^A$ . Otherwise,  $C^A$  performs a create user query ( $Query_{CUQ}$ ) and sends  $C_{Acti}$  to  $F^A$ .

**Query $_{RPBQ}$ :** In the replaced public key query ( $Query_{CRQ}$ ), given  $ID_{Acti}$  and  $\varphi_{Acti}'$ , it can check if  $ID_{Acti}^* = ID_{Acti}$  when it is satisfied then  $C^A$  will quite, otherwise  $C^A$  can replace  $\varphi_{Acti}$  on  $\varphi_{Acti}'$  and  $C_{Acti}$  on  $C_{Acti}'$ .

**Query $_{SignQ}$ :** Suppose  $M$  be a message to be delivered,  $ID_{Acti}$  belongs to  $\mathcal{J} = \{ID_{SAct1}, ID_{SAct2}, ID_{SAct3}, \dots, ID_{SActm}\}$ ,  $C_{SActi}$  belongs to  $\mathcal{Q} = \{C_{SAct11}, C_{SAct2}, C_{SAct3}, \dots, C_{SActm}\}$ , and  $\lambda = \{MPB, HEC, \mathcal{D}, F^q, H_A, H_B, H_C, H_D\}$  will be taken is input, if  $ID_{Acti}^* = ID_{Acti}$ . If yes,  $C^A$  perform  $Query_{CRQ}$  on  $ID_{Acti}$  to get  $C_{Acti}$  and execute  $Query_{HB}$  on ( $C_{Acti}, ID_{Acti}, MPB$ ) to get  $\pi_{Acti}$ . Further,  $C^A$  choose  $\partial_{Acti}$  and  $S_{Acti}$  randomly from  $F^q$  and compute  $\varepsilon_{Acti} = S_{Acti} \cdot \mathcal{D} - \partial_{Acti} \cdot C_{Acti} - \pi_{Acti} \cdot \partial_{Acti} \cdot \mathcal{J} \cdot \mathcal{D}$ . It also computes  $\Omega_{Acti} = \beta_{Acti} \cdot \mathcal{E}_{Acti}$  on  $ID_{Acti}$  and compute  $CIPR = E_{\Delta_{Acti}}(M)$ . Then, send ( $S_{Acti}, CIPR, \mathcal{E}_{Acti}$ ) to  $F^A$ .



*Query<sub>U<sub>signQ</sub></sub>*: Suppose  $(S_{Acti}, CIPR, \mathcal{E}_{Acti})$ , one of the sender identity  $ID_{SAct}$  belongs to  $\mathcal{J} = \{ID_{SAct1}, ID_{SAct2}, ID_{SAct3}, \dots, ID_{SActm}\}$ , and receiver identity  $ID_{RAct}$ , if  $ID_{RAct} = ID_{Acti}^*$ . If yes,  $C^A$  perform *Query<sub>CRQ</sub>* on  $ID_{Acti}$  to get  $C_{Acti}$  and execute *Query<sub>HB</sub>* on  $(C_{Acti}, ID_{Acti}, MPB)$  to get  $\pi_{Acti}$ . Further,  $C^A$  choose  $\partial_{Acti}$  randomly from  $F^q$  and verify  $S_{Acti} \cdot \mathcal{D} = \mathcal{E}_{Acti} + \partial_{Acti} \cdot C_{Acti} - \pi_{Acti} \cdot \partial_{Acti} MPB$  if holds. If it is holds,  $C^A$  access  $\Delta_{Acti}$  from, recover the plaintext, and send  $\Delta_{Acti}$  to  $F^A$ .

*Forgery*: on a message  $M^*$  under one of the sender's identities  $ID_{SAct}$  belongs to  $\mathcal{J} = \{ID_{SAct1}, ID_{SAct2}, ID_{SAct3}, \dots, ID_{SActm}\}$  and receiver identity  $ID_{RAct}$ ,  $F^A$  computes a forged signature  $(S_{Acti}^*, CIPR^*, \mathcal{E}_{Acti}^*)$ . According to forking lemma,  $C^A$  can also compute the genuine signature  $(S_{Acti}^{**}, CIPR^{**}, \mathcal{E}_{Acti}^{**})$ . At the end, the solution obtained by  $C^A$  as followed:  $\mathcal{J} = \frac{(S_{Acti}^* - S_{Acti}^{**})(\pi_{Acti}^* - \pi_{Acti}^{**})}{\partial_{Acti}^*}$ .

*Probability Analysis*: Suppose  $F^A$  performs all *Hash Queries Query<sub>H<sub>i</sub></sub>* ( $i = A, B, C, D$ ), *Create User Query (Query<sub>CUQ</sub>)*, *Private Value Query (Query<sub>PVQ</sub>)*, *Private Key Query (Query<sub>PKQ</sub>)*, *Certificate Generation Query (Query<sub>CRQ</sub>)*, *Replaced Public Key Query (Query<sub>CRQ</sub>)*, *Signcryption Query (Query<sub>S<sub>ignQ</sub></sub>)*, and *Un-Signcryption Query (Query<sub>U<sub>signQ</sub></sub>)*. Ultimately, we can ensure the availability of the following three events.

1. In the event 1 ( $E_1$ ),  $C^A$  never quite in *Query<sub>PKQ</sub>*, *Query<sub>CRQ</sub>*, *Query<sub>S<sub>ignQ</sub></sub>*, and *Query<sub>U<sub>signQ</sub></sub>*
2. In the event 2 ( $E_2$ ),  $C^A$  generates a valid signature or cipher text
3. In the event 3 ( $E_2$ ),  $ID_{Acti}^* = ID_{SAct}^*$

The probability for event 1 ( $E_1$ ) is define as  $Pr(E_1) = (1 - 1/Query_{HB})^{inQuery_{PKQ} + Query_{CRQ} + Query_{U_{signQ}}}$  probability for event 1 and event 2 as  $Pr(E_1|E_2) \geq \omega^{F^A}$ , probability for event 1, event 2, and event 3 as  $Pr(E_1|E_2 \wedge E_3) \geq 1/Query_{HB}$ . So, the combined probability from the above events as:

$$\omega^{C^A} = \frac{1}{Query_{HB}} \left(1 - \frac{1}{Query_{HB}}\right)^{Query_{PKQ} + Query_{CRQ} + Query_{U_{signQ}}} \left(1 - \frac{Query_{HB}}{Query}\right) Query_{S_{ignQ}} \omega^{F^A}$$

As mentioned in the above theorem, an adversary or a challenger must first find the solution of a hyperelliptic curve discrete logarithm to forge a signature. The signature, if we examine the proposed scheme, has been generated as  $S = \mathcal{K} + \beta_{SAct} \cdot H_D(C_{SAct}, ID_{SAct}, \mathcal{E}, CIPR)$  in which the attacker failed to generate  $S$ . This is because finding the values of  $\mathcal{K}$ ,  $\beta_{SAct}$  is impossible since it would require solving twotimes hyperelliptic curve discrete logarithm, which is a very challenging task.

*Theorem 4 (Unforgeability Against  $F^B$ )*: Suppose  $(Z = \mathcal{J} \cdot \mathcal{D})$  is a hyperelliptic curve discrete logarithm problem and the objective of the challenger ( $C^B$ ) is to compute  $\mathcal{J}$  from  $Z$  using  $F^B$  with the advantage of  $(C^B)$ . We also analyze the

$(F^B)$  advantages of type 1 forger  $F^B$ . After the setup step, to prove this theorem,  $C^B$  and  $F^B$  will exchange the following query.

*Setup*: On the response of  $PB = \sigma \cdot \mathcal{D}$ ,  $\sigma$ , and  $\lambda = \{MPB, HEC, \mathcal{D}, F^q, H_A, H_B, H_C, H_D\}$ ,  $F^B$  sends the target identity ( $ID_{Acti}^*$ ) to  $C^B$ .

*Hash Queries*: All the hash queries performed in this Theorem are the same as Theorem 3.

*Query<sub>CUQ</sub>*: When  $C^A$  receives a request from  $F^B$ , it can check if  $ID_{Acti}^* = ID_{Acti}$ . If this condition is satisfied,  $C^B$  will then select  $\mathcal{G}_{Acti}$  and  $\ell_{Acti}$  at random. Then,  $C^B$  ( $\Gamma_{Acti}, \varphi_{Acti}, \mathcal{G}_{Acti}, C_{Acti}, \ell_{Acti}, \perp$ ) into  $LC_{UQ}$  and send  $\ell_{Acti}$  to  $F^B$ .  $C^B$  computes  $\varphi_{Acti} = \mathcal{G}_{Acti} \cdot \mathcal{D}$ ,  $\Gamma_{Acti} = \ell_{Acti} \cdot \mathcal{D}$ ,  $C_{Acti} = \Gamma_{Acti} + \varphi_{Acti}$ . If not,  $C^B$  will randomly select  $\mathcal{G}_{Acti}$  and  $\alpha_{Acti}$ , run *Query<sub>HC</sub>* to obtain  $\Delta_{Acti}$ , and then compute  $\varphi_{Acti} = \mathcal{G}_{Acti} \cdot \mathcal{D}$ ,  $\Gamma_{Acti} = \alpha_{Acti} \cdot \mathcal{D} - \Delta_{Acti} \cdot MPB$ ,  $C_{Acti} = \Gamma_{Acti} + \varphi_{Acti}$ , and  $\beta_{Acti} = \alpha_{Acti} + \mathcal{G}_{Acti}$ . After that,  $C^B$  adds  $(\Gamma_{Acti}, \varphi_{Acti}, \mathcal{G}_{Acti}, C_{Acti}, \ell_{Acti}, \beta_{Acti})$  to  $LC_{UQ}$  and send  $\beta_{Acti}$  to  $F^B$ .

*Query<sub>PVQ</sub>*: In the private value query (*Query<sub>PVQ</sub>*), when  $C^B$  received request from  $F^B$ , it can check if  $\mathcal{G}_{Acti}$  is exist in  $LP_{UQ}$ , then  $C^B$  send  $\mathcal{G}_{Acti}$  to  $C^A$ . Otherwise,  $C^B$  perform a create user query (*Query<sub>CUQ</sub>*) and send  $\mathcal{G}_{Acti}$  to  $F^B$ .

*Query<sub>PKQ</sub>*: This query will perform in this Theorem is the same as *Theorem 1*.

*Query<sub>CRQ</sub>*: This query that will performed in this *Theorem* is same as *Theorem 1*.

*Query<sub>S<sub>ignQ</sub></sub>*: Suppose  $M$  be a message to be delivered,  $ID_{Acti}$  belongs to  $\mathcal{J} = \{ID_{SAct1}, ID_{SAct2}, ID_{SAct3}, \dots, ID_{SActm}\}$ ,  $C_{SActi}$  belongs to  $\mathcal{Q} = \{C_{SAct1}, C_{SAct2}, C_{SAct3}, \dots, C_{SActm}\}$ , and  $\lambda = \{MPB, HEC, \mathcal{D}, F^q, H_A, H_B, H_C, H_D\}$  will be taken is an input, if  $ID_{Acti}^* = ID_{Acti}$ . If yes,  $C^A$  perform *Query<sub>CRQ</sub>* on  $ID_{Acti}$  to get  $C_{Acti}$  and execute *Query<sub>HB</sub>* on  $(C_{Acti}, ID_{Acti}, MPB)$  to get  $\pi_{Acti}$ . Further,  $C^A$  choose  $\partial_{Acti}$  and  $S_{Acti}$  randomly from  $F^q$  and compute  $\mathcal{E}_{Acti} = S_{Acti} \cdot \mathcal{D} - \partial_{Acti} \cdot C_{Acti} - \pi_{Acti} \cdot \partial_{Acti} \mathcal{J} \cdot \mathcal{D}$ . It also computes  $\Omega_{Acti} = \beta_{Acti} \cdot \mathcal{E}_{Acti}$  on  $ID_{Acti}$  and compute  $CIPR = E_{\Delta_{Acti}}(M)$ . Then, send  $(S_{Acti}, CIPR, \mathcal{E}_{Acti})$  to  $F^A$ .

*Query<sub>U<sub>signQ</sub></sub>*: Suppose  $(S_{Acti}, CIPR, \mathcal{E}_{Acti})$ , one of the sender identity  $ID_{SAct}$  belongs to  $\mathcal{J} = \{ID_{SAct1}, ID_{SAct2}, ID_{SAct3}, \dots, ID_{SActm}\}$ , and receiver identity  $ID_{RAct}$ , if  $ID_{RAct} = ID_{Acti}^*$ . If yes,  $C^A$  perform *Query<sub>CRQ</sub>* on  $ID_{Acti}$  to get  $C_{Acti}$  and execute *Query<sub>HB</sub>* on  $(C_{Acti}, ID_{Acti}, MPB)$  to get  $\pi_{Acti}$ . Further,  $C^A$  choose  $\partial_{Acti}$  randomly from  $F^q$  and verify  $S_{Acti} \cdot \mathcal{D} = \mathcal{E}_{Acti} + \partial_{Acti} \cdot C_{Acti} - \pi_{Acti} \cdot \partial_{Acti} MPB$  if holds. If it is holds,  $C^A$  access  $\Delta_{Acti}$  from, recover the plaintext, and send  $\Delta_{Acti}$  to  $F^A$ .

*Forgery*: On a message  $M^*$  under one of the sender identity  $ID_{SAct}$  belongs to  $\mathcal{J} = \{ID_{SAct1}, ID_{SAct2}, ID_{SAct3}, \dots, ID_{SActm}\}$  and receiver identity  $ID_{RAct}$ ,  $F^A$  compute a forged signature  $(S_{Acti}^*, CIPR^*, \mathcal{E}_{Acti}^*)$ . According to the forking lemma,  $C^A$  can also compute the genuine signature  $(S_{Acti}^{**}, CIPR^{**}, \mathcal{E}_{Acti}^{**})$ . At the end, the solution obtained by  $C^A$  as followed:  $\mathcal{J} = \frac{(S_{Acti}^* - S_{Acti}^{**})(\pi_{Acti}^* - \pi_{Acti}^{**})}{\partial_{Acti}^*}$ .

*Probability Analysis*: Suppose  $F^A$  performs all *Hash Queries Query<sub>H<sub>i</sub></sub>* ( $i = A, B, C, D$ ), *Create User Query*

( $Query_{C_{UQ}}$ ), Private Value Query ( $Query_{P_{UQ}}$ ), Private Key Query ( $Query_{P_{KQ}}$ ), Certificate Generation Query ( $Query_{C_{RQ}}$ ), Replaced Public Key Query ( $Query_{C_{RQ}}$ ), Signcryption Query ( $Query_{S_{ignQ}}$ ), and Un-Signcryption Query ( $Query_{U_{signQ}}$ ). At the end, we can ensure the availability of the following three events.

1. In the event 1 ( $E_1$ ),  $C^A$  never quite in  $Query_{P_{KQ}}$ ,  $Query_{C_{RQ}}$ ,  $Query_{S_{ignQ}}$ , and  $Query_{U_{signQ}}$
2. In the event 2 ( $E_2$ ),  $C^A$  generates a valid signature or cipher text
3. In the event 3 ( $E_3$ ),  $ID_{Acti}^* = ID_{SAct}^*$   
The probability for event 1 ( $E_1$ ) is defined as  $\Pr(E_1) = \frac{1}{(1 - 1/Query_{H_B})^{inQuery_{P_{KQ}} + Query_{C_{RQ}} + Query_{U_{signQ}}}}$ , probability for event 1 and event 2 as  $\Pr(E_1 | E_2) \geq \omega^{FA}$ , probability for event 1, event 2, and event 3 as  $\Pr(E_1 | E_2 \wedge E_3) \geq 1/Query_{H_B}$ . The combined probability of the above events is as follows:

$$\omega^{C^A} = \frac{1}{Query_{H_B} \left(1 - \frac{1}{Query_{H_B}}\right)^{Query_{P_{KQ}} + Query_{C_{RQ}} + Query_{U_{signQ}}} \left(1 - \frac{Query_{H_B}}{Query}\right) Query_{S_{ignQ}} \omega^{FA}}$$

Notice that in the preceding theorem, the adversary and the challenger must seek a solution for the discrete logarithm hyperelliptic curve to generate a forgery signature. If we examine the proposed method, we have already generated the signature as  $S = \ell + \beta_{SAct} \cdot H_D(C_{SAct}, ID_{SAct}, \mathcal{E}, C_{IPR})$ , in which the attacker failed to generate  $S$  because finding the value  $\ell$ ,  $\beta_{SAct}$  is infeasible and it will result in solving two times hyperelliptic curve discrete logarithm.

## B. INFORMAL SECURITY ANALYSIS

The formal security analysis verifies that the proposed scheme is robust against the security criteria of confidentiality and unforgeability and provides the additional security capabilities of message integrity, authentication, non-repudiation, and forward secrecy. These considerations are detailed in further depth below.

**Integrity:** To check integrity, on the sender side, we calculated  $v = H_D(C_{SAct}, ID_{SAct}, \mathcal{E}, C_{IPR})$ , and on the receiver side, we computed  $H_D(C_{SAct}, ID_{SAct}, \mathcal{E}, C_{IPR}) = r$ . If the receiver wishes to determine if the message has been changed, he/she will compare  $v = H_D(C_{SAct}, ID_{SAct}, \mathcal{E}, C_{IPR}) = H_D(C_{SAct}, ID_{SAct}, \mathcal{E}, C_{IPR}) = r$ ; if this condition is fulfilled, the proposed scheme will ensure the message's integrity.

**Authentication:** We computed the signature as  $S = \ell + \beta_{SAct} \cdot v$ , and sent it to the receiver to verify authentication under the proposed scheme. The receiver can verify the signature as  $S \cdot \mathcal{D} = \mathcal{E} + C_{SAct} \cdot H_D(C_{SAct}, ID_{SAct}, \mathcal{E}, C_{IPR}) + (C_{SAct}, ID_{SAct}, \mathcal{E}, C_{IPR}) \cdot H_B(C_{SAct}, ID_{SAct}, MPB) \cdot MPB$ . If it holds, the receiver will accept the signature and the authentication will be confirmed. The alternate method of authentication sets  $H_D(C_{SAct}, ID_{SAct}, \mathcal{E}, C_{IPR}) = r$  and

$H_B(C_{SAct}, ID_{SAct}, MPB) = z$ . It computes  $S \cdot \mathcal{D} = \mathcal{E} + r \cdot C_{SAct} + r \cdot z \cdot MPB$ . If it holds, the receiver will accept the signature, and authentication will be confirmed.

**Non-repudiation:** We calculated the signature as  $S = \ell + \beta_{SAct} \cdot v$ , where  $\beta_{SAct}$  is the private key of sender and sent to the receiver. The receiver can verify the signature as  $S \cdot \mathcal{D} = \mathcal{E} + C_{SAct} \cdot H_D(C_{SAct}, ID_{SAct}, \mathcal{E}, C_{IPR}) + (C_{SAct}, ID_{SAct}, \mathcal{E}, C_{IPR}) \cdot H_B(C_{SAct}, ID_{SAct}, MPB) \cdot MPB$ . If it holds, the receiver will accept the signature and authentication will be confirmed. The alternate way is that it sets  $H_D(C_{SAct}, ID_{SAct}, \mathcal{E}, C_{IPR}) = r$  and  $H_B(C_{SAct}, ID_{SAct}, MPB) = z$ . It computes  $S \cdot \mathcal{D} = \mathcal{E} + r \cdot C_{SAct} + r \cdot z \cdot MPB$ . If it holds then the receiver accepts signature and authentication will be confirmed. In the above two verification equations, we have included  $C_{SAct}$  as the public key of the sender; thus, if the sender denies sending the signature, we can simply prove that the sender sent the signature since the public key is directly related to the sender's private key. Thus, according to the proposed scheme, the sender cannot refute his delivered signature.

**Forward secrecy:** Even if the proposed scheme's private key is compromised, the ciphertext will remain secure since encryption and decryption were performed using the secret key. If the attacker wishes to compromise the security of the cipher text, they must satisfy the two requirements outlined below.

1. We encrypted the message through the secret key as  $R = H_C(\Omega)$ , where  $\Omega = \ell \cdot (C_r + H_B(C_r, ID_r, MPB) \cdot MPB)$  and the attacker fails to get  $R$  because finding the value  $\ell$  from  $\Omega$  is infeasible, leading to solving the hyperelliptic curve discrete logarithm, which is very challenging.
2. We decrypted the message through the secret key as  $R = H_C(\Omega)$ , where  $\Omega = \beta_r \cdot \mathcal{E}$ , and the attacker failed to get  $R$  because finding the value  $\beta_r$  from  $\Omega$  is infeasible, leading to the hyperelliptic curve discrete logarithm.

## C. SECURITY VERIFICATION USING THE AVISPA TOOL

This section performs the simulation of the proposed using the AVISPA tool [26], a formal security verification method to determine the cryptographic scheme resilience against replay and man-in-the-middle (MitM) attacks. The security characteristics are simulated using an expressive and modular formal language in the AVISPA with the assistance of the high-level protocol specification language (HLPSL). We used a Haier Win8.1 PC workstation with an Intel (R) Core (TM) i3-4010U CPU @ 1.70-GHz and a 64-bit operating system to execute the simulations of the proposed certificate-based ring signcryption scheme. Moreover, Oracle VM Virtual Box (version: 5.2.0.118431) and SPAN (version: SPAN-Ubuntu-10.10-light 1) make up the software portion of the simulation setup. The OFMC and CL-AtSe are executed at the back ends for the vulnerability tests. We have not considered the results of SATMC and TA4SP are not included in the simulation results due to the bitwise XOR operations, which are incompatible with SATMC and TA4SP. The

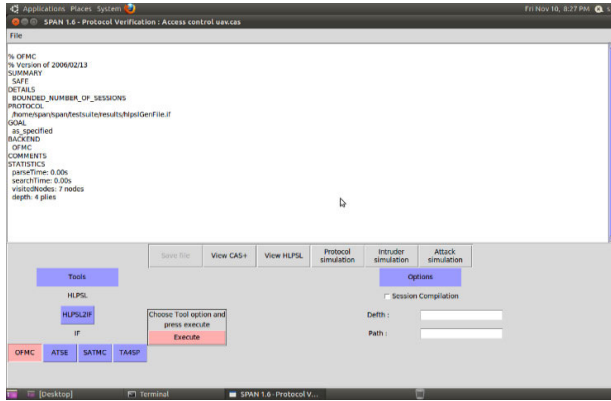


FIGURE 2. Simulation results for OFMC.

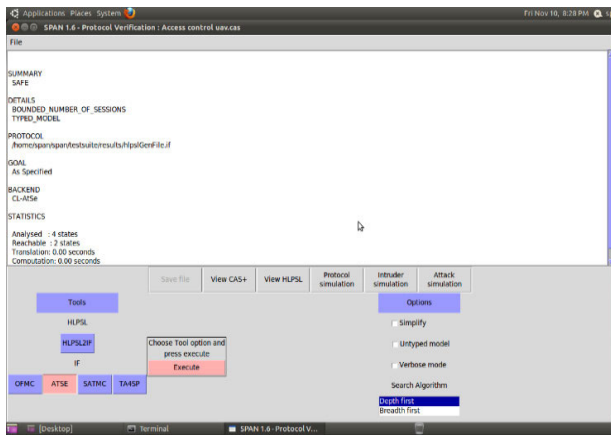


FIGURE 3. Simulation results for ATSE.

proposed scheme is also simulated using the well-known web tool known as specific protocol animator (SPAN) The findings collected from OFMC and AtSe as illustrated in Fig. 2 and 3 authenticate the effectiveness against replay and MitM attacks.

**V. PERFORMANCE ANALYSIS**

This analysis examines the proposed scheme’s efficiency based on its computation and communication costs. It does this by comparing it to other comparable schemes.

**A. COMPUTATION COST**

Based on the major operations such as elliptic curve scalar addition, hyperelliptic curve scalar addition, elliptic curve scalar multiplication, hyperelliptic curve divisor multiplication, modular exponentiation, pairing multiplication operation, and bilinear pairing, the proposed scheme is compared to those proposed by Guo and Deng [20], Cai et al. [21], Gupta and Kumar [23], Cui et al. [24], and Guo et al. [25]. In Tab. 3, the symbols *ESA*, *HESA*, *ESM*, *HEDM*, *MEN*, *PMO*, and *BP* represent the time needed for elliptic curve scalar addition, hyperelliptic curve scalar addition, elliptic curve scalar multiplication, hyperelliptic curve divisor multiplication, modular exponentiation, pairing multiplication

TABLE 3. Major operation costs.

Symbol	Operation	Running time (ms)
<i>ESA</i>	Time required for a single elliptic curve scalar addition	0.002
<i>HESA</i>	Time required for a single hyper elliptic curve scalar addition	0.001
<i>ESM</i>	Time required for a single elliptic curve scalar multiplication	0.341
<i>HEDM</i>	Time required for a single hyper elliptic curve divisor multiplication	0.1705
<i>MEN</i>	Time required for a single modular exponentiation	1.915
<i>PMO</i>	Time required for a single pairing multiplication	0.788
<i>BP</i>	Time required for single bilinear pairing	4.669

TABLE 4. Computation costs.

Schemes	Ring Signcryption	Ring Unsigncryption	Total
[20]	10 <i>PMO</i> + 1 <i>BP</i>	4 <i>PMO</i> + 2 <i>BP</i>	14 <i>PMO</i> + 3 <i>BP</i>
[21]	7 <i>PMO</i> + 1 <i>BP</i>	5 <i>PMO</i> + 3 <i>BP</i>	12 <i>PMO</i> + 4 <i>BP</i>
[23]	6 <i>ESM</i> + 1 <i>ESA</i>	9 <i>ESM</i> + 3 <i>ESA</i>	15 <i>ESM</i> + 4 <i>ESA</i>
[24]	6 <i>PMO</i> + 1 <i>MEN</i> + 1 <i>BP</i>	6 <i>BP</i> + 3 <i>PMO</i>	9 <i>PMO</i> + 1 <i>MEN</i> + 7 <i>BP</i>
[25]	14 <i>ESM</i> + 10 <i>ESA</i>	9 <i>ESM</i> + 9 <i>ESA</i>	23 <i>ESM</i> + 19 <i>ESA</i>
Ours	3 <i>HEDM</i> + 2 <i>HESA</i>	5 <i>HEDM</i> + 2 <i>HESA</i>	8 <i>HEDM</i> + 4 <i>HESA</i>

operation, and bilinear pairing. The computation cost is mainly determined by the amount of computation involved for the signcryption algorithm and decryption verification calculation.

According to Ref. [27], the time required for these operations is listed in Tab.4 is considered. For this experiment, the following execution environment was utilized: CPU: Intel Core i7-6700 @ 3.40GHz; RAM: 8GB; OS: Ubuntu 16.04; MIRACL library. As is well-known, HECC needs half the key size of ECC to provide the same degree of security. Tab. 3 compares the computation performance of the proposed scheme to that of the schemes proposed by Guo and Deng [20], Cai et al. [21], Gupta and Kumar [23], Cui et al. [24], and Guo et al. [25] based on the key operations. As shown in Tab. 5 and illustrated in Fig.4, the proposed scheme is more efficient than its counterpart in terms of computation costs measured in milliseconds, supporting the scheme’s feasibility in the UAV-enabled private edge computing environment.

TABLE 5. Computation costs (in ms).

Schemes	Ring Signcryption	Ring Unsigncryption	Total (ms)
[20]	12.55	12.49	25.04
[21]	10.18	17.95	28.12
[23]	2.048	3.075	5.123
[24]	11.312	30.348	41.66
[25]	4.794	3.087	7.88
Ours	0.5135	0.8545	1.368

TABLE 6. Communication cost.

Schemes	[20]	[21]	[23]	[24]	[25]	Ours
Comm. cost	$ M  + 6 G $	$2 M  + 5 G $	$ M  + 4 Q $	$ M  + 8 G  + 7 Q $	$ M  + 7 Q $	$ M  + 2 N $

TABLE 7. Communication cost (in bits).

Schemes	[20]	[21]	[23]	[24]	[25]	Ours
Comm. cost	7168	7168	1664	9216	2144	1184

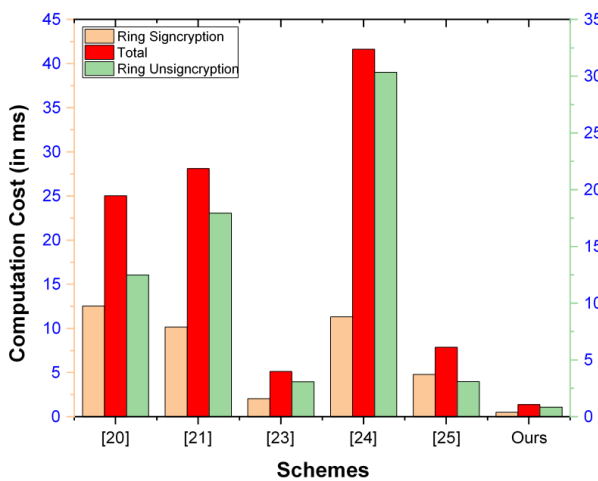


FIGURE 4. Comparative analysis based on computation cost (in ms).

B. COMMUNICATION COST

Communication costs refer to the number of bits that must be transferred in addition to the cipher text or message during the transmission session. Extra bits are often counted as elliptic curve parameter size, hyperelliptic curve parameter size, and bilinear pairing parameter size when calculating the communication cost. Tab.5 provides a comparison of the communication cost between the schemes proposed by Guo and Deng [20], Cai et al. [21], Gupta and Kumar [23], Cui et al. [24], and Guo et al. [25] based on the main operations. Communication costs equal the number of extra bits In Tab.6, The symbols  $|M|$ ,  $|N|$ ,  $|G|$ , and  $|Q|$  stand for the size of the message/cipher text, the size of the hyperelliptic curve parameter, the size of the bilinear pairing parameter, and elliptic curve parameter, and they use 1024 bits, 80 bits, 1024 bits, and 180 bits, respectively.

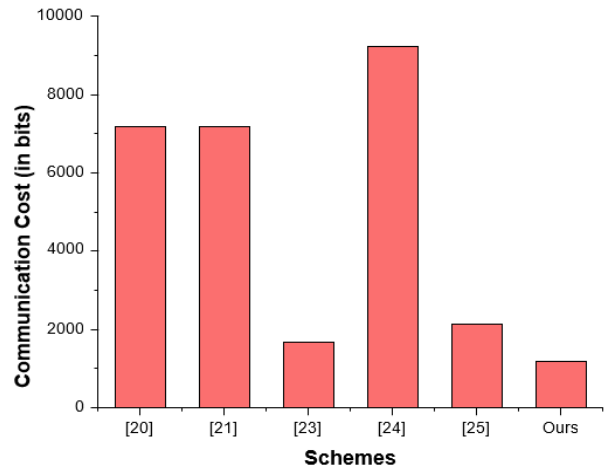


FIGURE 5. Comparative analysis based on communication cost (in bits).

Tab.7 and Fig. 5 compare communication costs in bits, which reveals that the proposed scheme has lower communication costs.

VI. CONCLUSION

UAV-enabled private edge computing systems involve the integration of UAVs into a private edge computing infrastructure. In this system, UAVs are outfitted with a variety of data-collecting sensors and devices within this system; the data is processed locally on an edge computing server. The open wireless channel, nevertheless, renders these systems susceptible to security threats. Threats to UAV-enabled private edge computing systems’s security and privacy can be categorized as either violation threats, deliberate threats, or accidental threats. Similarly, while designing security measures for these systems, high scalability, device diversity, and mobility must be considered. Keeping these vulnerabilities in mind, ring signcryption, which provides advantageous characteristics such as anonymity, spontaneity, flexibility, and equal membership, is the most appropriate cryptographic technique. In this article, we proposed a certificate-based ring signcryption method based on HECC that combines encryption and digital signature in a single step and uses the lower key size of HECC to provide more security than RSA, BP, and ECC. The computation and communication costs of the proposed scheme is 1.368(in ms) and 1184 (in bits) respectively, which is significantly less than by the relevant existing schemes. All of these outcomes indicate the practicality of the proposed scheme. In the future work, integrating blockchain or federated learning to the proposed scheme can further enhance the security of UAV-enabled private edge computing systems.

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