# Enhancing Geographic Greedy Routing in Sparse LDACS Air-to-Air Networks through k-Hop Neighborhood Exploitation

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Abstract—The emergence of the L-band Digital Aeronautical Communications System (LDACS) presents a significant opportunity for enabling Air-to-Air (A2A) communication to accommodate the growing number of aircraft. However, it requires overcoming significant Medium Access Control (MAC) delays and enhancing connectivity in sparse networks. Geographic greedy routing, commonly used in Aeronautical Ad-hoc networks, utilizes position information to eliminate the need for topology discovery. Yet, its efficacy declines as network density decreases. With the gradual introduction of aircraft equipped with LDACS, it becomes crucial to improve greedy forwarding performance. This research investigates Greedy-k, a greedy forwarding variant using k-hop neighborhood information, to boost sparse network performance. We introduce a method to minimize beacon size by transmitting a subset of k-hop neighborhood data that fits within an LDACS time slot. We derived the subset size analytically and evaluated the performance through simulations benchmarked against the conventional Greedy-1. Our results indicate that the proposed approach achieves up to 13% higher Packet Delivery Ratio (PDR) than Greedy-1, while capturing additionally 70.1% and **34.6**% of 2<sup>nd</sup> and 3<sup>rd</sup> order neighbors, respectively.

Index Terms—geographic routing, greedy forwarding, A2A, LDACS

## I. INTRODUCTION

By the year 2050, the European Organisation for the Safety of Air Navigation (EUROCONTROL) forecasts a 44% increase in flight numbers compared to 2019, necessitating advanced communication technologies for safety, data rate, and reliability [1]. The *L*-band Digital Aeronautical Communications System (LDACS), currently under standardization, is proposed as a solution for Air-to-Ground (A2G) communication within the Future Communications Infrastructure (FCI), potentially enhancing data rates by up to 200% [2]. It is also proposed to be extended for Air-to-Air (A2A) communication [3].

Recently, the Multi-Channel Self-Organized Time-Division Multiple Access (MCSOTDMA) protocol has been proposed as a viable Medium Access Control (MAC) layer for LDACS A2A communications [4]. This protocol utilizes a Shared (SH) channel for broadcasting beacons and multiple Point-to-Point (PP) channels for unicast packets, ensuring deterministic delays. Geographic routing, the state-of-the-art routing protocol for A2A communication [5], uses beacons to transmit positional information and routes packets greedily towards their destination. If a packet reaches a dead-end, it is dropped or requires a backup mechanism to continue. In deploying LDACS for A2A communications, we identify two key challenges.

*Challenge 1:* The practical implementation of LDACS for A2A links is expected to be a long process, starting by integrating the technology into newly built aircraft. The airspace will include both legacy and LDACS-equipped aircraft until full LDACS deployment is achieved. This situation raises concerns about LDACS A2A performance in sparse networks, particularly regarding the coexistence with legacy aircraft over the coming decades.

*Challenge II:* In the SH channel, a Randomized Slotted ALOHA (RS-ALOHA) is used [6]. This results in a MAC delay that increases linearly with the number of neighboring aircraft. Using a high communication range increases the number of direct neighbors, resulting in significant MAC delays affecting both SH and PP links. To accommodate future growth in airspace, reducing the communication range while ensuring high connectivity with ground stations can mitigate these delays. However, this reduction requires improvements in greedy routing to ensure routes are found when they exist topologically.

This paper proposes a solution that can cope with both difficulties. Greedy forwarding, a main component of geographic routing, while effective in dense airspace [7], struggles with frequent dead-ends in sparse networks as shown in Figure 5. Greedy-k, is proposed as an enhancement in such environments by using extended k-hop neighborhood information [8], [9]. However, this approach results in beacons that exceed the capacity of an LDACS A2A slot in the SH channel. Therefore, we introduce a method that optimizes the beacon size by including only a subset of the neighborhood, facilitating more efficient and scalable Greedy-k implementation in sparse network scenarios.

Our main contributions are:

- We analytically derive an optimal fixed subset size to improve Greedy-1 forwarding performance.
- We propose three subset selection methods (*Random*, *Farthest First (FF)* traversal, and *Extended Farthest First (EFF)* traversal) and introduce a geographic greedy routing protocol that uses this information.
- We evaluate our proposed routing protocol and selection methods over the French airspace with varying equipage fractions, reflecting initial and extended use of LDACS-equipped aircraft in the future.

The organization of the paper is as follows: The required subset size is discussed in Section II. The proposed geographic routing protocol is introduced in Section III. The simulation setup is outlined in Section IV. Our results and discussions are detailed in Section V. Related work is discussed in Section VI. The conclusion and further insights on future directions are given in Section VII.

## II. THE SUBSET SIZE OF THE K-HOP NEIGHBORHOOD

To optimize Greedy-2 routing performance, a node requires a subset of its 1-hop neighborhood, denoted as  $S_{a_i}^1$ , from the full set  $\mathcal{N}_{a_i}^1$  where  $\mathcal{N}_{a_i}^1$  are 1<sup>st</sup> order neighbors of  $a_i$  in network  $\mathcal{A}$ . The challenge lies in determining the optimal subset size  $m = |S_{a_i}^1|$  that maximizes coverage while minimizing redundancy.

Coverage is modeled in Two-dimensional (2D) space using a Unit Disc Graph (UDG). Although aircraft operate in Three-dimensional (3D) space, the altitude variation is minor compared to their communication range r. We consider an infinite set  $\mathcal{N}_{a_i}^1$ , uniformly distributed within the communication range. To maximize diversity, we ensure that m selected nodes are maximally distant from each other and from node  $a_i$ . We analyze various m values, assessing their impact on coverage and overlap, where coverage is the area beyond  $a_i$ 's range relative to the 2<sup>nd</sup> order neighbor area  $(3\pi r^2)$ , and overlap is the area shared between the nodes' coverage. The case for m = 4, 6 is demonstrated in Figure 1, where the Coverage is depicted by the grey hashed area (75.72%, 88.41%) and Overlap by the dark grey hashed area (5.41%, 33.28%) respectively.



Fig. 1: Coverage and overlap for subset sizes m = 4 and m = 6, where the node  $a_i$  is depicted in red.

Furthermore, we analyzed various m values to assess their effects on coverage, overlap, the rate of change of coverage ( $\Delta$ Coverage) and the rate of change of overlap ( $\Delta$ Overlap), as depicted in Figure 2. Here, increasing menhances coverage, yet  $\Delta$ Coverage decreases after m = 3as overlap among nodes starts. When m > 4, we see that  $\Delta$ Coverage  $< \Delta$ Overlap, which means the redundancy among selected nodes increases faster than the increase in coverage. In this study, we establish  $m = |S_{a_i}^1| = 4$ to optimally distribute coverage around  $a_i$ , maintaining  $\Delta$ Coverage  $> \Delta$ Overlap.



Fig. 2: Illustration of coverage (Coverage) and overlap (Overlap) areas, along with their rates of change ( $\Delta$ Coverage and  $\Delta$ Overlap), for different subset sizes m.

## III. GEOGRAPHIC GREEDY ROUTING WITH A SUBSET OF K-HOP NEIGHBORHOOD

#### A. System Model

Within the routing algorithm,  $a_c$  denotes the current node. Each node  $a_c \in \mathcal{A}$  receives beacons  $B_{a_s}$  from beacon senders  $a_s \in \mathcal{N}_{a_c}^1$ . Beacons include the sender's address  $a_s$ , position  $p_{a_s}$ , sequence number seq<sub>as</sub>, and neighbor subset information. For each neighbor  $a_i$  in this subset, its address, position  $p_{a_i}$ , hop count  $h_{a_i}$ , and sequence number seq<sub>ai</sub> are in  $B_{a_s}$ . A beacon entry occupies 12 B, 4 B for the node address (1 B prefix plus 24 bit International Civil Aviation Organization (ICAO) ID), 6 B for the position in Compact Position Reporting (CPR) format, 1 B for hop count, and 1 B for the sequence number. Sequence numbers, incremented by each node  $a_c \in \mathcal{A}$  upon  $\mathcal{N}_{a_c}^1$  changes, track direct neighbor additions or removals.

Nodes maintain a position table  $\mathcal{T}_{a_c}$ , contains all neighbors  $\mathcal{N}_{a_c}$  known through received beacons. Each entry  $a_i \in \mathcal{T}_{a_c}$  includes  $a_i$ 's address, position  $p_{a_i}$ , hops to  $a_i h_{a_i}$ , sequence number seq<sub>a<sub>i</sub></sub>, via address via<sub>a<sub>i</sub></sub> (indicating the beacon's sender) and validity time  $t_{a_i}$ , calculated as:

$$t_{a_i} = t_{B_{a_s}} + t_{validity},\tag{1}$$

where  $t_{B_{a_s}}$  is the beacon reception time and  $t_{validity}$  is a pre-defined beacon interval. An example of a node's position table is shown in Table I.

TABLE I: Position Table of  $a_c$  ( $\mathcal{T}_{a_c}$ )

$\mathbf{a}_i$	$\mathbf{p}_{\mathbf{a_i}}$	$\mathbf{h}_{\mathbf{a_i}}$	seq <sub>ai</sub>	via <sub>ai</sub>	$t_{a_i}$
$a_1$	$(x_1, y_1, z_1)$	2	22	$a_2$	$20.5\mathrm{s}$
$a_2$	$(x_2, y_2, z_2)$	1	34	$a_2$	$24\mathrm{s}$

# B. Neighbor Selection Mechanism

In this section, we describe three methods for selecting a subset  $S_{a_c}^k \subseteq \mathcal{N}_{a_c}^k$ , where each neighbor is exactly k-hop away from node  $a_c$ . The first method, *Random*, randomly selects neighbors to form a subset of size m. This serves as a baseline strategy.

The second method, the *FF* algorithm, starts by randomly picking an initial node and then iteratively adds the node farthest from those already selected, until *m* nodes are chosen or all potential nodes are exhausted. This strategy optimizes spatial diversity among the selected nodes and functions as a standard farthest-first selection. The *FF* algorithm can also incorporate a set of preselected elements  $S_{a_c}^{\text{pre}}$ , where it starts from this set instead of from a random element. Then the preselected nodes are removed in later steps. The notation  $FF(\mathcal{N}_{a_c}^k, m, \mathcal{S}_{a_c}^{\text{pre}} = \emptyset)$  represents the *FF* algorithm when used without  $S_{a_c}^{\text{pre}}$ .

The *EFF* method, denoted by  $\text{EFF}(\mathcal{N}_{a_c}^k, m, d_{\text{thr}}, d_{\text{thr},c})$ , enhances the FF strategy by integrating a distance threshold,  $d_{\text{thr}}$ , and a distance to current node,  $d_{\text{thr},c}$ . The threshold ensures that no two nodes within the subset are closer than the specified distance, reducing redundancy. For a subset size of m = 4, optimal for 1<sup>st</sup> order neighbors,  $d_{\text{thr}}$  is set to  $\frac{1}{\sqrt{2}} \cdot r$ . This value ensures that nodes diagonally positioned within a square remain outside each other's communication range, effectively minimizing overlap. Similarly,  $d_{\text{thr},c}$  is established at  $\frac{1}{2} \cdot r$ , corresponding to the radius of the circle in which the square, centered at  $a_c$  with its diagonal nodes at the edge of each other's communication range, is inscribed. Applying the thresholds  $d_{\text{thr}}$  and  $d_{\text{thr},c}$  might result in selecting fewer than m nodes due to the spatial arrangement of neighbors. This approach allows us to extend our selection to  $k + 1^{\text{th}}$ order neighbors  $\mathcal{N}_{a_c}^{k+1}$ , as will be discussed in Section III-C.

# C. Beaconing Mechanism

The proposed routing protocol uses beacons to disseminate information about a subset of the local *k*-hop neighborhood of a node, as detailed in Section III-B. Initially, each beacon contains only the node's information but gradually accumulates and broadcasts additional neighborhood details received from other beacons.

Each node broadcasts a new beacon at intervals defined by the beacon interval parameter. The beacon includes the sender's address  $a_s$ , position  $p_{a_s}$ , and sequence number seq<sub> $a_s$ </sub>. Each node knows its position, and the sequence number helps mitigate routing loops when a node is removed from the position table. When sending a beacon,  $a_s$  extracts  $\mathcal{N}_{a_s}^1$  and  $\mathcal{N}_{a_s}^2$ . Using the *Random* or *FF* methods, a node selects up to *m* neighbors from  $\mathcal{N}_{a_s}^1$ . With *EFF*, a subset of  $\mathcal{N}_{a_s}^1$  is chosen using  $d_{\text{thr}}$ . If fewer than *m* neighbors are selected from  $\mathcal{N}_{a_s}^1$ , the remainder is selected from  $\mathcal{N}_{a_s}^2$  using the *FF* method with  $\mathcal{S}_{a_c}^1$  as the preselected list  $\mathcal{S}_{a_c}^{\text{pre}}$ . Each selected neighbor's sequence number and hop count from  $\mathcal{T}_{a_s}$  are added to the beacon.

When a beacon  $B_{a_s}$  is received, the current node  $a_c$ updates its position table  $\mathcal{T}_{a_c}$  by removing entries added via  $a_s$  that are no longer in  $B_{a_s}$  or have expired. This ensures  $\mathcal{T}_{a_c}$  is current, reflecting the latest network topology. The validity interval,  $t_{validity}$ , is set to twice the beacon interval, allowing quick response to link loss. For each neighbor  $a_i$  in  $B_{a_s}$ , the algorithm checks if  $a_i$  is already in  $\mathcal{T}_{a_c}$  and updates  $a_i$ 's information if the beacon provides a more recent sequence number or a shorter hop count with an equal or fresher sequence. If  $a_i$  is not found, it is added as a new entry, with  $a_s$  set as the via address.

## D. Forwarding Mechanism

Let  $a_d$  denote the destination node. When a node  $a_c$  sends a packet to  $a_d$ , it is assumed the position of  $a_d$  is known. For forwarding,  $a_c$  selects the neighbor  $a_{\text{best}}$  from its position table  $\mathcal{T}_{a_c}$  that offers the best advancement towards  $a_d$ . The packet is directed to  $a_j = \text{via}_{a_{\text{best}}}$ , a 1<sup>st</sup> order neighbor, ensuring maximal progress towards  $a_d$ . This process is illustrated in Figure 3. To mitigate issues from



Fig. 3: The packet forwarding process, directing the packet towards  $via_{a_{best}}$ , the node through which  $a_{best}$  is reachable.

delayed or lost beacons, a range reduction parameter  $\varepsilon$  is introduced. This parameter restricts selection to 1<sup>st</sup> order neighbors within a radius of  $r - \varepsilon$  to ensure reliability, filtering usable neighbors as illustrated in dotted red in Figure 3. The selection of  $\varepsilon$  considers nodes at the edge of the communication range moving in opposite directions as a worst-case, defined as:

$$\varepsilon = 2 \cdot \text{beacon interval} \cdot \text{average speed.}$$
 (2)

# IV. SIMULATION SETUP

This study evaluates greedy routing using subsets of the k-hop neighborhood with three selection methods: Greedy-Random, Greedy-FF, and Greedy-EFF.

## A. Mobility Model

The French airspace, spanning  $1\,000\,000\,\mathrm{km}^2$ , is modeled as a  $1250\,\mathrm{km} \times 800\,\mathrm{km}$  rectangle (Figure 4). Aircraft can be at altitudes from  $0\,\mathrm{km}$  to  $11\,\mathrm{km}$ , representing various



Fig. 4: The French airspace where the red outline shows the simulation boundary (generated using [10]).

flight phases. The simulation includes an average of 500 aircraft [11] and one ground station, depicted as a green triangle in Figure 4. Each aircraft selects a random position within the simulation area and moves in a straight line in a random direction. The LDACS communication range of 370.4 km is applied for A2G communication. We use an A2A communication range of 100 km, as evaluated in [11], achieving an approximate ground station connectivity ratio of 100%.

# B. Network Model

1) Data Application: Aircraft employ Automatic Dependent Surveillance-Contract (ADS-C) technology to send their Four-dimensional (4D) positions (latitude, longitude, altitude, and time) every minute, with each packet being 34 B. This capability is essential for the safety and efficient management of future airspace [12]. The first packet of an aircraft is randomly transmitted within [0 s, 60 s].

2) Data Link Layer: We implemented an abstract version of the MCSOTDMA, the proposed LDACS MAC layer, as specified in [4]. This implementation supports one LDACS transmitter and two receivers per aircraft, using the SH channel for beacon broadcasting and the PP channels for unicast packet transmission. The number of available PP channels adjusts dynamically based on the location, with up to 50 usable channels in this simulation [13]. Our model results in a linear increase in MAC delay on the SH channel, proportional to the number of direct neighbors, mirroring MCSOTDMA behavior [6]. As a simplification, we assume an entity with global node knowledge for optimal scheduling of transmissions. Considering MAC headers as described in [4], each beacon can accommodate up to 6 neighbor entries, each of 12 B. Hence, we evaluated subset sizes m = 4 and m = 6 for the SH channel, identifying m = 4 as optimal in Section II.

3) *Physical Layer:* Our simulation employs a UDG radio model, assuming a uniform communication range across all

aircraft and no channel errors. Two nodes can communicate successfully if within the defined range.

The simulation parameters are summarized in Table II.

Simulation Time Limit (s)	1800	
Number of Simulation Runs	50, with 95% CIs	
A2G Communication Range (km)	370.4	
A2A Communication Range (km)	100	
Number of Aircraft	500	
Aircraft Speed (km/h)	800	
Simulation Area (km <sup>2</sup> )	1 000 000	
Beacon Interval (s)	5	
Slot Size (s)	0.024	
Packet Size (B)	34	
Application Sending Rate (pkts/node/min)	1	
Aircraft Density ( $\times 10^{-4}$ nodes/km <sup>2</sup> )	2.5, 3, 3.5, 4, 4.5	
	and 5	
LDACS Equipage Fraction $\rho$	0.5, 0.6, 0.7, 0.8,	
	0.9 and 1	
Subset Size m	4 and 6	

## V. RESULTS AND DISCUSSION

In this experiment, we vary the equipage fraction,  $\rho$ , representing the proportion of aircraft equipped with LDACS. We evaluate Greedy-Random, Greedy-FF, and Greedy-EFF algorithms at different equipage fractions, measuring their performance in terms of average Packet Delivery Ratio (PDR) and hop count. We compare their performance against Greedy-1 and Greedy-2. Although Greedy-2 includes the full neighborhood in the beacon, which exceeds the LDACS A2A slot capacity, it serves as a benchmark. The Dijkstra's algorithm is also used to demonstrate the maximum achievable PDR and minimum hop counts for each equipage fraction, despite its infeasibility here. Simulations are conducted using OMNeT++ with a communication range of 100 km and a range reduction parameter of  $\varepsilon = 2.5$  km.

Greedy-Random, Greedy-FF, and Greedy-EFF improve the PDR by 1% compared to Greedy-1 at  $\rho = 1$ , when all aircraft are LDACS equipped as in Figure 5. At  $\rho = 0.5$ ,



Fig. 5: Average PDR with varying equipage fraction.

these improvements increase to 11.5% for m = 4 and 13% for m = 6. Additionally, Greedy-EFF marginally

outperforms Greedy-FF on average in scenarios with lower equipage fractions due to its access to 3-hop neighborhood information. All methods with subset sizes m = 4 and m = 6 achieve performance gains comparable to Greedy-2. Despite achieving higher PDR over Greedy-1, a performance gap of at least 10% compared to Dijkstra persists at  $\rho = 0.5$  due to the lack of a fallback mechanism to navigate through dead-ends, leading to packet drops.

The average hop count results over different equipage fractions are shown in Figure 6. At  $\rho = 1$ , Greedy-EFF,



Fig. 6: Average hop count with varying equipage fraction.

which employs a 3-hop neighborhood information, exhibits slightly higher hop counts compared to its 2-hop counterparts. This increase is attributable to the broader search horizon, which may not always optimize for the maximum advancement per hop, potentially leading to longer routes. As  $\rho$ decreases, the difference in hop counts diminishes. Overall, the hop counts for all methods, including Greedy-EFF, are comparable to those of Greedy-2 and are on average up to 0.82 hops higher than those achieved by Dijkstra at  $\rho = 1$ .

Following the previous analysis, we now evaluate the *Random*, *FF*, and *EFF* algorithms in terms of selecting  $k^{\text{th}}$ order neighbors. We define the Capture Ratio as the ratio of unique  $k^{\text{th}}$  order neighbors identified by each method against the actual total, averaging this across all nodes. Our simulations involve 50 random mobility snapshots conducted in an area large enough to mitigate edge effects, reflecting the density and equipage fractions from the previous scenario. Using a subset size of m = 4 achieves a balance of coverage gain over overlap, as shown in Figure 5. We present how this subset size influences the average capture ratio of 2<sup>nd</sup> and 3<sup>rd</sup> order neighbors. The results in Figure 7 indicate that at a node density of  $5 \times 10^{-4}$  nodes/km<sup>2</sup> and with m = 4, the FF method achieves a capture ratio of 0.6 for 2<sup>nd</sup> order neighbors, compared to 0.52 by Random, marking a 15.4% improvement. Random selection becomes less effective at higher densities due to an enlarged selection pool. At  $2.5 \times 10^{-4}$  nodes/km<sup>2</sup>, the FF method achieves a capture ratio of 0.7, compared to 0.64 by Random, reflecting a 9.3% improvement. With an average of 7.6 first-order



Fig. 7: Average  $k^{\text{th}}$  order neighbors capture ratio for 100 km communication range with subset size m = 4.

neighbors, selecting just four means Random's performance remains effective. Additionally, at this density, *EFF* achieves the same performance as *Random* by strategically sacrificing some  $2^{nd}$  order neighbors to capture 15% of  $3^{rd}$  order neighbors, a capability not present in *FF* or *Random*. At a higher density of  $5 \times 10^{-4}$  nodes/km<sup>2</sup>, despite selecting fewer  $1^{st}$  order neighbors than *Random*, *EFF* achieves a  $2^{nd}$ order neighbor capture ratio of 0.582, compared to 0.52 by Random, marking a 12% improvement, and it also captures 5.1% of  $3^{rd}$  order neighbors. As density increases, *EFF*'s performance is expected to align more closely with *FF* due to the minimal effect of the distance threshold.

With m = 6, the average  $2^{nd}$  order neighbors capture ratios for *FF*, *EFF*, and *Random* range between [0.84, 0.7], [0.70, 0.61], and [0.83, 0.67] respectively (Figure 8). Additionally, *EFF* captured 34.6% of  $3^{rd}$  order neighbors at  $2.5 \times 10^{-4}$  nodes/km<sup>2</sup> and 25.8% at  $5 \times 10^{-4}$  nodes/km<sup>2</sup>.



Fig. 8: Average  $k^{\text{th}}$  order neighbors capture ratio for 100 km communication range with subset size m = 6.

## VI. RELATED WORK

Sparse networks exacerbate dead-end situations, leading to the exploration of greedy forwarding strategies that include 2-hop or 3-hop neighborhood information [9], [14]. However, The performance gain from Greedy-2 is higher than from Greedy-3 [14]. While this approach mitigates routing inefficiencies, it significantly increases beacon size, an issue not fully addressed in previous studies. The slot-based MAC protocol in LDACS A2A communications complicates beacon size management within strict slot durations. Studies like [8], [15] show that including direct neighbors in the beacon doubles the overhead ratio compared to Greedy-1, without considering the necessary beacon size reduction for slot duration compliance.

Addressing the beacon size challenge, existing literature aimed to reduce message counts for capturing 2-hop neighborhood information using O(n) messages of  $O(\log n)$  bits each, where n is the number of nodes in the network [16]. However, this approach focuses on message efficiency rather than direct beacon size reduction. Further advancements used probabilistic structures like Bloom filters to compress the neighbor list [17]–[19]. These methods efficiently encapsulate all direct neighbors and can accommodate khop neighborhoods, enhancing broadcasting protocols but lacking the positional information required for geographic Greedy-k routing.

Our investigation proposes a solution addressing both the need for a fixed maximum beacon size including a subset of direct neighbors with positional information and the constraints of LDACS A2A MAC, which accommodates approximately an additional 72 B in the beacon after headers. This constraint influences the feasible number of neighbors in a beacon, based on entry size, e.g., 12 B in our case as specified in Section III-A. Our method aims to select nodes within this subset to optimally enhance performance, achieving Greedy-2 forwarding gains within LDACS A2A communication slot durations. To the best of our knowledge, our approach is the first to reduce beacon size by selecting a subset of the neighborhood and including both MAC addresses and positional information in the beacon, offering a novel contribution to the field.

# VII. CONCLUSION

We presented a novel approach to enhance greedy forwarding in sparse networks by leveraging 3-hop neighborhood information. We proposed three methods for selecting subsets of  $k^{\text{th}}$  order neighbors: *Random*, *FF*, and *EFF*, and derived an optimal fixed subset size for performance improvements with Greedy-2 forwarding. We found that a subset size of 4 is optimal, balancing coverage and overlap.

Our simulation study evaluated the proposed routing protocol and selection methods over the French airspace with varying equipage fractions. We assessed average PDR, hop count, and capture ratio of  $k^{\text{th}}$  order neighbors. Our methods outperform Greedy-1, especially in improving PDR in sparse scenarios prone to dead-ends. All proposed methods enhance PDR by up to 13% relative to Greedy-1, achieving Greedy-2 performance gain. Additionally, Greedy-FF captures more  $2^{nd}$  order neighbors on average than Greedy-Random and Greedy-EFF, while Greedy-EFF can capture up to 34.6% of  $3^{rd}$  order neighbors. All models were implemented using OMNeT++ and Python, with details available as open-source for the research community in [20].

This approach offers potential benefits for geographical routing beyond aeronautical communication, especially in low-density large networks where greedy forwarding often hits dead-ends. Enhanced neighborhood awareness can be applied in load balancing by capturing the load status of  $2^{nd}$  and  $3^{rd}$  order neighbors. Furthermore, our method's partial *k*-hop neighborhood awareness lays the groundwork for developing effective strategies when a *k*-hop neighborhood is insufficient, and can be adapted for *k*-hop neighborhoods and 3D networks by adjusting the subset size *m*.

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