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Secrecy Performance Analysis of RIS-Aided Smart Grid Communications

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4 Abstract—A smart grid (SG) is an advanced electrical 5 grid that enhances the efficiency and reliability of traditional power grids. Reconfigurable intelligent surfaces 6 7 (RISs) have been recently proposed to enhance communication performance in the SG. However, the communi-8 cation links between different SG components could suf-9 10 fer from eavesdropping and unauthorized access, which makes physical layer security (PLS) a promising solution 11 12 for addressing these concerns. In this article, we focus 13 on exploring the effect of applying RIS on enhancing the 14 PLS performance of SG communications. Specifically, we consider an RIS with reflecting elements besides a smart 15 meter, a neighborhood gateway (NG), and an eavesdropper 16 17 to develop a smart environment in the SG to improve PLS 18 performance in terms of secrecy outage probability (SOP) and average secrecy capacity (ASC). For this purpose, we 19 first derive a probability density function and a cumulative 20 21 distribution function for the signal-to-noise ratio (SNR) at both the NG and the eavesdropper. Then, we derive closed-22 23 form expressions of SOP and ASC to evaluate the impact of various system parameters on the secrecy performance of 24 25 RIS-aided SG communications. Furthermore, considering the significance of system behavior under high-SNR con-26 27 ditions, we conduct an asymptotic analysis of the SOP and ASC. Finally, we apply the Monte Carlo simulation to vali-28 date the analytical results. Our results indicate that using 29 the RIS can significantly enhance the secrecy performance 30 of SG communications compared to the conventional SG 31 scenarios without the RIS. 32

Index Terms—Average secrecy capacity (ASC), physical layer security (PLS), reconfigurable intelligent surfaces
 (RISs), secrecy outage probability (SOP), smart grid (SG).

I. INTRODUCTION

SMART grid (SG) is an advanced electrical grid system that uses modern information and communication
technology (ICT) to enable two-way information flow besides
two-way power flow to improve the efficiency, reliability, and
sustainability of the traditional power grid [1]. By employing

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ICT, the SG can significantly contribute to the current power42grid by introducing numerous improvements such as advanced43monitoring and control, sound integration of renewable energy44resources, enhanced reliability and resiliency, increased flexibil-45ity, better energy distribution and customization, and decreasing46greenhouse gases emission [2].47

However, new security and privacy risks arise in the SG due 48 to the usage of ICT [3], [4]. For example, an eavesdropper can 49 gain access to sensitive information about a costumer's energy 50 consumption habit, which may lead to privacy violation or en-51 able malicious activities. Therefore, establishing secure links is 52 critical for ensuring the confidentiality, integrity, and availability 53 of sensitive data in SG communications. Using physical layer 54 security (PLS) techniques, which leverage the physical prop-55 erties of a communication channel to provide secure links [5], 56 [6], [7], offers certain advantages over traditional cryptographic 57 approaches in certain SG scenarios, such as reduced computa-58 tional burden, lower latency, and increased security features [8], 59 [9], [10]. Analyzing the PLS performance is crucial to ensure 60 robust and effective secure communication in wireless networks. 61 In this context, two essential metrics, namely, secrecy outage 62 probability (SOP) and average secrecy capacity (ASC), play 63 pivotal roles [11], [12]. SOP quantifies the likelihood that secure 64 communication is compromised due to unfavorable channel 65 conditions, providing insights into the system's vulnerability 66 against eavesdropping attacks. ASC measures the average rate 67 at which confidential information can be securely transmitted, 68 considering both achievable data rate and security against eaves-69 droppers [13], [14]. 70

A. Related Works

Several research efforts have focused on investigating the 72 PLS performance of SG communications in recent years. 73 Camponogara et al. [15] explored the benefits of hybrid power 74 line communication (PLC)/wireless channels for improving PLS 75 in low-bit-rate applications. They derived mathematical formu-76 lations for ASC and SOP, revealing the advantages of hybrid 77 PLC/wireless models in enhancing PLS when eavesdroppers 78 utilize a single data communication interface. Salem et al. [16] 79 delved into the PLS of cooperative relaying PLC systems with 80 artificial noise. They derived expressions for ASC, highlighting 81 the potential of cooperative relaying to significantly enhance 82 the security of PLC systems. Building on this, Salem et al. [17] 83 extended their study to consider PLS in correlated log-normal 84 cooperative PLC networks. Their work analyzed the impact of 85

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background and impulsive noise components, providing mathematical insights into ASC and SOP under various network
scenarios.

89 Odeyemi et al. [18] introduced a dynamic wide area network (WAN) for SGs featuring a friendly jammer to enhance network 90 secrecy. They derived closed-form expressions for connection 91 SOP and ASC, showcasing the network's enhanced security 92 performance. Atallah et al. [19] investigated PLS performance 93 in wireless sensor networks within SG environments. They con-94 95 sidered the impact of destination-assisted jamming on secrecy performance metrics and derived analytical expressions for SOP, 96 revealing the potential for significant improvement in security 97 using jamming techniques. El-Shafie et al. [20] studied the influ-98 ence of wireless network's PLS and reliability on demand-side 99 management in SGs. Their work explored the tradeoff between 100 101 security and reliability, proposing artificial-noise-aided schemes and encoding strategies to enhance security and reliability in 102 SG. Mohan et al. [21] examined PLS in low-frequency PLC 103 104 systems, focusing on ASC and SOP. They considered both the independent and correlated log-normal channel distributions, 105 106 incorporating the impact of impulsive noise and various network parameters. 107

In conventional SG communications, achieving robust PLS 108 performance has been challenging due to several factors such 109 110 as presence of interference, channel impairments, and unpredictable wireless conditions due to the dynamic and hetero-111 geneous nature of the SG environment. On the other hand, 112 the reconfigurable intelligent surface (RIS) [22], [23], [24] of-113 fers a promising avenue to enhance the PLS performance in 114 wireless communication systems. The RIS takes the advantage 115 116 of metamaterials to control the reflection and scattering of electromagnetic waves in a controlled manner to enhance the 117 118 overall communication performance [25]. The controlled manipulation of signal paths through the RIS enables the creation 119 of favorable transmission conditions for the intended receiver 120 while introducing signal degradation for potential eavesdrop-121 pers. This dynamic alteration of the wireless channel charac-122 teristics contributes to enhanced security levels [26], [27], [28], 123 124 [29], [30]. Furthermore, the RIS can be optimized to minimize 125 signal leakage to unintended directions, effectively confining the transmission to the intended recipient [31], [32], [33]. Through 126 these mechanisms, the RIS can play a pivotal role in bolstering 127 PLS, making unauthorized interception more challenging and, 128 thus, enhancing the overall security of wireless communication 129 systems. Quite recently, the RIS has been utilized to enhance 130 the communication performance in SG [34]. The authors in [35], 131 [36], [37], and [38] used the RIS in the SG WAN communication 132 system to enhance the signal-to-noise ratio (SNR) at the receiver. 133 To that end, they derived closed-form expressions for average bit 134 error rate and outage probability, showing that by improving the 135 quality and reliability of the wireless communication links in SG, 136 the RIS can help reducing the risk of communication failures, 137 improve the accuracy of data collection, and enhance the overall 138 performance of SG systems. Table I shows the distinctions 139 between prior research and our work, emphasizing the unique 140 aspects of our analysis in this article. 141

TABLE I COMPARISON OF RELATED WORKS IN SECRECY PERFORMANCE ANALYSIS OF SG COMMUNICATIONS

Works	I_1	I_2	I_3	I_4	I_5
[15], [17], [21]	\checkmark	\checkmark	×	×	P_2, P_3, P_4
[16]	×	\checkmark	×	×	P_3, P_4
[18]	\checkmark	\checkmark	\checkmark	×	P_2, P_3
[19], [20]	\checkmark	×	×	×	P_2, P_3, P_4
[35], [36]	×	×	\checkmark	\checkmark	P_1, P_2
[37], [38]	×	×	×	\checkmark	P_1, P_2
Ours	\checkmark	\checkmark	\checkmark	\checkmark	P_1, P_2, P_3, P_4, P_5

 I_1 : SOP analysis, I_2 : ASC analysis, I_3 : Asymptotic analysis, I_4 : RIS integration, I_5 : Considered system parameters, P_1 : Number of RIS elements, P_2 : NG's location, P_3 : Eve's location, P_4 : SM's transmission power, P_5 : Secrecy rate, \checkmark : Item is supported, and \times : Item is not supported.

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B. Motivations and Contributions

Within the framework of typical SG scenarios, attaining ef-143 fective secrecy performance presents a formidable challenge, 144 attributed to limited received signal strength, confined power 145 resources inherent to smart meters (SMs), the pervasive influ-146 ence of interference sources, the obstruction posed by physical 147 barriers, and an array of other intricate considerations. Although 148 the potential of RIS to enhance communication performance 149 in SG is intriguing [34], [35], [36], [37], [38], there has been 150 limited exploration on whether the RIS can also improve the 151 PLS performance of SG communication systems. Evaluating 152 secrecy performance metrics in PLS analysis allows us to assess 153 the system's ability to maintain secure communication, helping 154 to design resilient wireless networks that safeguard sensitive 155 information in SG. As a primary step in this regard, deriving 156 closed-form expressions of important secrecy metrics can pro-157 vide a quantitative analysis on the impact of various system 158 parameters on PLS performance in RIS-aided SG communica-159 tions. To that end, our analysis concentrates on evaluating the 160 SOP and ASC as vital PLS metrics to gain a comprehensive 161 understanding of the confidentiality and secrecy aspects of the 162 proposed system model. Specifically, our analysis pertains to the 163 communication between an SM and a neighborhood gateway 164 (NG) in the presence of a passive eavesdropper. To the best of 165 our knowledge, this is the first article that studies the PLS perfor-166 mance of the RIS-aided SG communication system. Therefore, 167 the main contributions of this article can be summarized as 168 follows. 169

- We analyze the secrecy performance of the RIS-aided SG communication by taking into account the impact of various system parameters, e.g., the number of reflecting elements in the RIS and the (limited) transmission power in the SM.
- 2) To that end, we first derive closed-form expressions of the probability density function (PDF) and the cumulative distribution function (CDF) of the received SNR at the NG and an eavesdropper in the considered system model 178 by assuming a perfect channel state information (CSI) 179 of the NG and an imperfect CSI of the eavesdropper at the RIS. Then, we introduce accurate compact analytical 181



System model of RIS-aided SG NAN communications. Fig. 1.

expressions of SOP and ASC by using the derived PDFs 182 and CDFs.

- 184 3) To examine the behavior of the RIS-aided SG communication system in conditions of high SNR and to 185 understand the core patterns and potential of SG com-186 munication systems in optimal settings, we conduct an 187 asymptotic analysis of the derived SOP and ASC using 188 the residue method, as described in [44]. 189
- 190 4) We validate the analytical results by leveraging the advantage of Monte Carlo simulation in different system 191 settings. Our results confirm the accuracy of the proposed 192 closed-form expressions and show that the RIS-aided SG 193 can achieve better secrecy performance than the conven-194 tional SG scenario without the RIS. 195

C. Organization and Notations 196

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The rest of this article is organized as follows. Section II 197 presents the system and channel model of RIS-aided SG com-198 munication. Section III demonstrates the SNR distribution at an 199 NG and an eavesdropper. The closed-form expressions of SOP 200 and ASC are obtained in Section IV. Section V presents the 201 asymptotic analysis of the secrecy metrics. The simulation re-202 sults are discussed in Section VI. Finally, Section VII concludes 203 this article. 204

205 *Notations:* $\Gamma(.)$ indicates the complete Gamma function [48, eq. (8.31)], $\Gamma(.,.)$ shows the upper Incomplete Gamma func-206 tion [48, eq. (8.35)], B(.,.) indicates the Beta function [48, 207 eq. (8.38)], $G_{p,q}^{m,n}(.)$ indicates the Meijer G-function [46, eq. (8.2.1.1)], $H_{p,q;p_1,q_1;...;p_r,q_r}^{m,n;m_1,n_1;...;m_r,n_r}(.)$ indicates the bivariate Fox 208 209 H-function [47], $i = \sqrt{-1}$, and \vec{X}^{T} indicates the transpose 210 of \vec{X} . 211

II. SYSTEM AND CHANNEL MODEL 212

213 Fig. 1 shows the proposed system model for an RIS-aided SG neighborhood area network (NAN) communications, where 214 an SM, usually as a resource-constrained device, is typically 215 installed at a customer's premise to measure and record the 216 customer's energy usage patterns and send it to a corresponding 217 218 NG by employing an RIS with M reflecting elements. The NG serves as a central hub for NAN communications, which 219

collects data from SMs and then transmits the data to a util-220 ity company for further analysis and control. We assume that 221 there is also a passive eavesdropper named Eve that tries to 222 analyze the transmitted packets in NAN over both a direct link 223 from the SM (SM-to-NG) and reflected links from the RIS 224 (SM-to-RIS-to-NG). Without loss of generality, we assume that 225 the SM knows the CSI of the NG, so the RIS is able to effectively 226 adjust the phase-shifting coefficients of its reflecting elements 227 for maximizing the received SNR at the NG [42]. We also assume 228 that SM, NG, and Eve are equipped with single antenna for 229 simplicity. Therefore, the received signal at NG and Eve can be 230 respectively expressed as 231

$$y_N = \sqrt{P_s} S(t) \left(h_{SN} + \vec{H}_{SR} \vec{\Theta} \vec{H}_{RN}^{\mathcal{T}} \right) + n_N \qquad (1)$$

$$y_E = \sqrt{P_s} S(t) \left(h_{SE} + \vec{H}_{SR} \vec{\Theta} \vec{H}_{RE}^{\mathcal{T}} \right) + n_E \tag{2}$$

where P_s represents the transmit power of the SM, S(t) is the 232 information signal of the SM with a unit power, and n_N and 233 n_E represent the additive white Gaussian noise (AWGN) at NG 234 and Eve with zero mean and variances σ_N^2 and σ_E^2 , respectively. 235 $\vec{\Theta}$ is the adjustable phase matrix induced by the reflection 236 of RIS, which is defined as $\vec{\Theta} = \text{diag}([e^{j\theta_1}, e^{j\theta_2}, \dots, e^{j\theta_M}]).$ 237 The terms h_{SN} and h_{SE} denote the channel coefficients 238 between SM and NG and between SM and Eve, respectively. 239 Besides, \vec{H}_{SR} contains the channel coefficients from the 240 SM to M reflecting elements of the RIS, H_{RN} includes 241 the channel coefficients from RIS's M elements to the NG, 242 and H_{RE} consists of the channel coefficients from each 243 element of RIS to Eve. The above channel vectors are given 244 as $\vec{H}_{SR} = d_{SR}^{-\chi} [h_{SR_1} e^{-j\alpha_1}, h_{SR_2} e^{-j\alpha_2}, \dots, h_{SR_M} e^{-j\alpha_M}],$ $\vec{H}_{RN} = d_{RN}^{-\chi} [h_{RN_1} e^{-j\beta_1}, h_{RN_2} e^{-j\beta_2}, \dots, h_{RN_M} e^{-j\beta_M}],$ and 245 246 $\vec{H}_{RE} = d_{RE}^{-\chi} [h_{RE_1} e^{-j\eta_1}, h_{RE_2} e^{-j\eta_2}, \dots, h_{RE_M} e^{-j\eta_M}]$ where 247 d_{SR} denotes the distance between the SM and the RIS, d_{RN} 248 is the distance between the RIS and NG, and d_{RE} defines the 249 distance between the RIS and Eve. The term χ indicates the 250 path-loss exponent. Furthermore, the terms h_{SR_m} , h_{RN_m} , and 251 h_{RE_m} , where $m \in \{1, 2, \dots, M\}$, are the amplitudes of the 252 corresponding channel coefficients, and $e^{-j\alpha_m}$, $e^{-j\beta_m}$, and 253 $e^{-j\eta_m}$ denote the phase of the respective links. We model all the 254 channel fading coefficients as independent Rayleigh distributed, 255 i.e., the channel power gains are exponentially distributed. 256

III. SNR DISTRIBUTION

In this section, an analysis is conducted on the SNR at both 258 NG and Eve. The closed-form expressions of PDF and CDF are 259 then obtained based on the received SNR. 260

A. Main Link

According to (1), the instantaneous SNR at the NG can be 262 given as 263

$$\gamma_N = \frac{\left|\sqrt{P_s}(h_{SN} + \vec{H}_{SR}\vec{\Theta}\vec{H}_{RN})\right|^2}{n_N} = \frac{P_s}{d_{SN}^{\chi}\sigma_N^2}|h_{SN}|^2$$

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$$+ \frac{P_s}{d_{SR}^{\chi} d_{RN}^{\chi} \sigma_N^2} \left| \sum_{m=1}^M h_{SR_m} h_{RN_m} e^{j(\theta_m - \alpha_m - \beta_m)} \right|^2$$
$$\stackrel{(a)}{=} \bar{\gamma}_{N_1} |h_{SN}|^2 + \bar{\gamma}_{N_2} \left| \sum_{m=1}^M h_{SR_m} h_{RN_m} \right|^2 \tag{3}$$

where (*a*) is derived by assuming the perfect knowledge of the CSI at the RIS that leads to the ideal phase adjusting for maximizing the SNR at the NG. Besides, $\bar{\gamma}_{N_1}$ and $\bar{\gamma}_{N_2}$ are the average SNR at the NG due to the direct link and the RIS-aided links, respectively. According to (3), we can express $\gamma_N = \gamma_{N_1} + \gamma_{N_2}$ Since γ_{N_1} follows Rayleigh distribution, the PDF of γ_{N_1} can be given as

$$f_{\gamma_{N_1}}(\gamma_{N_1}) = \frac{e^{-\frac{\gamma_{N_1}}{a_N}}}{\bar{\gamma}_{N_1}a_N} \tag{4}$$

where a_N represents the mean value of γ_{N_1} . According to [39], $f_{\gamma_{N_2}}(\gamma_{N_2})$ is obtained as

$$f_{\gamma_{N_2}}(\gamma_{N_2}) = \frac{\gamma_{N_2} \frac{c_N}{2} - 1}{2\bar{\gamma}_{N_2} \Gamma(c_N) d_N^{c_N}}$$
(5)

where $c_N = \frac{M\pi^2}{16-\pi^2}$ and $d_N = \frac{\sqrt{\bar{\gamma}_{N_2}}(16-\pi^2)}{4\pi}$. By having the PDF of both the terms of γ_N in (4) and (5), we can then use the moment-generating function (MGF) of γ_{N_1} and γ_{N_2} to obtain the PDF and the CDF of γ_k as

$$f_{\gamma_N}(\gamma_N) = \mathcal{L}^{-1}\left\{ M_{\gamma_{N_1}}(s) \ M_{\gamma_{N_2}}(s) \right\}$$
(6)

$$F_{\gamma_N}(\gamma_N) = \mathcal{L}^{-1} \left\{ \frac{1}{s} M_{\gamma_{N_1}}(s) M_{\gamma_{N_2}}(s) \right\}$$
(7)

277 where \mathcal{L}^{-1} shows the Laplace inverse and $M_{\gamma_{N_1}}(t) =$ 278 $M_{\gamma_{N_1}}(-s)$ and $M_{\gamma_{N_2}}(t) = M_{\gamma_{N_2}}(-s)$ show the MGF of γ_{N_1} 279 and γ_{N_2} , respectively.

Theorem 1: Assuming that all the channels follow Rayleigh distribution, the PDF and the CDF of γ_N are given by (8) and (9) shown at the bottom of this page, respectively, where

$$\mathscr{F}_N = \frac{(\frac{d_N a_N - 2}{2a_N})^{-\frac{c_N}{2}}}{2\bar{\gamma}_{N_1}\bar{\gamma}_{N_2}\Gamma(c_N)d_N^{c_N}a_N}$$

283 and $\mathcal{F}_N = \frac{1}{2\bar{\gamma}_{N_1}\bar{\gamma}_{N_2}\Gamma(c_N)d_N{}^{c_N}}$

$$f_{\gamma_N}(\gamma_N) = \mathscr{F}_N e^{-\frac{\gamma_k}{a_N}} \left(\Gamma\left(\frac{c_N}{2}\right) - \mathcal{G}_{1,2}^{2,0}\left(\frac{(d_N a_N - 2)\gamma_N}{2a_N} \middle| \frac{1}{0, \frac{c_N}{2}} \right) \right).$$
(8)

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285 *Proof:* The detailed proof for this theorem is presented in 286 Appendix A. \Box

B. Eavesdropping Link

Similarly, according to (2), the instantaneous SNR at Eve can 288 be obtained as 289

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$$\gamma_{E} = \frac{\left|\sqrt{P_{s}}(h_{SE} + \vec{H}_{SR}\vec{\Theta}\vec{H}_{RE})\right|^{2}}{n_{E}} = \frac{P_{s}}{d_{SE}^{\chi}\sigma_{E}^{2}}|h_{SE}|^{2} + \frac{P_{s}}{d_{SR}^{\chi}d_{RE}^{\chi}\sigma_{E}^{2}}\left|\sum_{m=1}^{M}h_{SR_{m}}h_{RE_{m}}e^{j(\theta_{m}-\alpha_{m}-\eta_{m})}\right|^{2} = \bar{\gamma}_{E_{1}}|h_{SE}|^{2} + \bar{\gamma}_{E_{2}}\left|\sum_{m=1}^{M}h_{SR_{m}}h_{RE_{m}}e^{j(\theta_{m}-\alpha_{m}-\eta_{m})}\right|^{2}$$
(10)

where $\bar{\gamma}_{E_1}$ and $\bar{\gamma}_{E_2}$ denote the average SNR at Eve regarding 290 the direct and RIS-aided links, respectively. When RIS element 291 phase shifts are optimally tailored according to the conditions 292 of the legitimate link, the resultant phase distributions for each 293 of the links to Eve $(\vec{H}_{SR}\vec{\Theta}\vec{H}_{RE}^{T})$ exhibit a uniform distribu-294 tion [40]. If phase-shift errors uniformly span the range $[-\pi]$, 295 π), implying a complete absence of knowledge about CSI of 296 Eve at the RIS and, consequently, a complete lack of knowl-297 edge about optimally adjusting the RIS phases according to 298 the Eve's CSI, the channel coefficient adheres to a circularly 299 symmetric complex normal distribution [41]. This resemblance 300 results in the equivalent channel displaying characteristics akin 301 to Rayleigh fading, as has been discussed in [42] and [43]. 302 Therefore, $f_{\gamma_E}(\gamma_E)$ can be represented as 303

$$f_{\gamma_E}(\gamma_E) = \frac{1}{a_E} e^{-\frac{\gamma_E}{a_E}} \tag{11}$$

where $a_E = M \bar{\gamma}_{E_2} + \bar{\gamma}_{E_1}$. Therefore, $F_{\gamma_E}(\gamma_E)$ is obtained as 304

$$F_{\gamma_E}(\gamma_E) = 1 - e^{-\frac{\tau_E}{a_E}}.$$
 (12)

IV. SECRECY PERFORMANCE ANALYSIS

In this section, we analyze the secrecy performance of RISaided SG communication by deriving closed-form expressions of SOP and ASC. First, we define the secrecy capacity (SC), the maximum rate at which information can be transmitted over the SG communication links between the SM and the NG while keeping the information confidential from the Eve, as 311

$$SC(\gamma_N, \gamma_E) = [C_N - C_E]^+$$
(13)

where $C_N = \log(1 + \gamma_N)$ and $C_E = \log(1 + \gamma_E)$ show the 312 wireless channel capacity between SM and NG, and SM and Eve, 313 respectively, and $[X]^+ = Max\{X, 0\}$. Note that $\log(.)$ stands for 314 logarithm in base 2. 315

$$F_{\gamma_N}(\gamma_N) = \mathcal{F}_N\left(\left(\frac{d_N}{2}\right)^{-\frac{c_N}{2}} \left(\Gamma\left(\frac{c_N}{2}\right) - \mathcal{G}_{1,2}^{2,0}\left(\frac{d_N\gamma_N}{2} \middle| \begin{matrix} 1\\ 0, \frac{c_N}{2} \end{matrix}\right)\right) - \left(\frac{d_Na_N - 2}{2a_N}\right)^{-\frac{c_N}{2}} e^{-\frac{\gamma_N}{a_N}} \left(\Gamma\left(\frac{c_N}{2}\right) - \mathcal{G}_{1,2}^{2,0}\left(\frac{(d_Na_N - 2)\gamma_N}{2a_N} \middle| \begin{matrix} 1\\ 0, \frac{c_N}{2} \end{matrix}\right)\right)\right).$$
(9)

316 A. Secrecy Outage Probability

Here, we present the analytical expression of SOP for RISaided SG NAN communication. As an information-theoretical metric to evaluate the PLS performance, SOP is defined as the probability that SC is less than a certain positive secrecy rate threshold, say R_S , as

$$P_{\text{SOP}} = \Pr(\text{SC} \le R_S). \tag{14}$$

By applying (13) in SOP definition, a mathematical expression for SOP can be derived as follows:

$$P_{\text{SOP}} = \Pr\left(\log\left(\frac{1+\gamma_N}{1+\gamma_E}\right) \le R_S\right) = \int_0^\infty F_{\gamma_N}(\gamma_t) f_{\gamma_E}(\gamma_E) d_{\gamma_E}$$
(15)

where $\gamma_t = (1 + \gamma_E)e^{R_S} - 1 = \gamma_E e^{R_S} + e^{R_S} - 1 = \gamma_E R_t + R'_t$ is the SNR threshold.

Theorem 2: The SOP for the RIS-aided SG communication
system under Rayleigh fading channels can be expressed by (16)
shown at the bottom of this page.

Proof: The detailed proof for this theorem is presented in Appendix B. \Box

331 B. Average Secrecy Capacity

1

The analytical expression of the ASC is presented in this section for RIS-aided SG NAN communications. ASC is the expected value of the SC over all the possible channel conditions and is a key metric in evaluating the PLS performance. According to (13), since SC for a complex AWGN wiretap channel is defined as the difference between the main and Eve channels when the Eve channel is noisier than the main channel, a mathematical expression for ASC can be derived as 339 follows: 340

$$ASC \stackrel{\Delta}{=} \int_0^\infty \int_0^\infty SC(\gamma_N, \gamma_E) f_{\gamma_N}(\gamma_N) f_{\gamma_E}(\gamma_E) d_{\gamma_E} d_{\gamma_E}.$$
(17)

Theorem 3: The ASC for the RIS-aided SG communication 341 system under Rayleigh fading channels can be expressed as 342

$$\bar{C}_s = \frac{1}{\ln 2} \left(\bar{C}_s^1 + \bar{C}_s^2 - \bar{C}_s^3 \right)$$
(18)

where \bar{C}_s^1 , \bar{C}_s^2 , and \bar{C}_s^3 are shown in (19)–(21), respectively 343

$$\bar{C}_s^3 = \mathcal{G}_{3,2}^{1,3} \left(a_E \Big| \begin{pmatrix} 0, 1, 1 \\ 1, 0 \end{pmatrix} \right).$$
(21)

Proof: The detailed proof is presented in Appendix C. 344 Remark 1: The SOP and the ASC of the considered RIS-aided 345 SG communication system can be accurately obtained according 346 to Theorems 2 and 3, respectively. It becomes evident that c_N 347 acts as a parameter of Fox H-function and as a variable of 348 complete Gamma function in (16), (19), and (20) shown at the 349 bottom of this page; thereby, both SOP and ASC are notably 350 affected by the number of RIS elements, M, since $c_N = \frac{M\pi^2}{16-\pi^2}$. 351 Consequently, as the number of RIS elements M increases, 352 we can expect improved performance in both SOP and ASC. 353 Furthermore, an analysis of a_E in SOP and ASC analytical 354 expressions reveals that increasing a_E results in a greater like-355 lihood of experiencing an outage and a decreased ASC. This 356 observation is attributed to the fact that $a_E = M \bar{\gamma}_{E_2} + \bar{\gamma}_{E_1}$ is a 357 function of average SNRs at Eve. Therefore, a larger a_E indicates 358 a more favorable channel condition for the eavesdropper. On the 359

$$P_{\text{SOP}} = \mathcal{F}_{N} \left(\frac{2}{d_{N}} \right)^{\frac{c_{N}}{2}} \left(\Gamma \left(\frac{c_{N}}{2} \right) + e^{\frac{R'_{t}}{a_{E}R_{t}}} \mathcal{H}_{1,0;1,2;1,1}^{0,1;2,0;0,1} \left(\frac{a_{E}d_{N}R_{t}}{R'_{t}} \middle| (0;1,1):(1,1);(1,1) - :(0,1),(\frac{c_{N}}{2},1);(0,1) \right) \right) - \mathcal{F}_{N} \left(\frac{2a_{N}}{d_{N}a_{N}-2} \right)^{\frac{c_{N}}{2}} \left(\frac{2\Gamma \left(\frac{c_{N}}{2} \right) e^{\frac{-a_{N}R'_{t}}{2}}}{2 + a_{E}a_{N}R_{t}} + \frac{2e^{\frac{R'_{t}}{a_{E}R_{t}}}}{2 + a_{E}a_{N}R_{t}} \mathcal{H}_{1,0;1,2;1,1}^{0,1;2,0;0,1} \left(\frac{a_{E}R_{t}(d_{N}a_{N}-2)}{a_{N}(2 + a_{E}a_{N}R_{t})} \right) - :(0,1),(\frac{c_{N}}{2},1);(0,1) \right) \right).$$

$$(16)$$

$$\begin{split} \bar{C}_{s}^{1} &= a_{N} \mathscr{F}_{N} \left(\Gamma \left(\frac{c_{N}}{2} \right) \mathcal{G}_{3,2}^{1,3} \left(a_{N} \Big|_{1,0}^{0,1,1} \right) - \mathcal{H}_{1,0;2,2;1,2}^{0,1;1,2;2,0} \left(\frac{a_{N}}{d_{N}a_{N}-2} \Big|_{-:(1,1),(0,1);(0,1);(0,1),(\frac{c_{N}}{2},1)} \right) \\ &- \frac{a_{E}}{a_{E} + a_{N}} \left(\Gamma \left(\frac{c_{N}}{2} \right) \mathcal{G}_{3,2}^{1,3} \left(\frac{a_{E}a_{N}}{a_{E} + a_{N}} \Big|_{1,0}^{0,1,1} \right) - \mathcal{H}_{1,0;2,2;1,2}^{0,1;1,2;2,0} \left(\frac{a_{E}a_{N}}{a_{E} + a_{N}} \Big|_{-:(1,1),(0,1);(0,1),(\frac{c_{N}}{2},1)} \right) \right) \right). \end{split}$$
(19)
$$\bar{C}_{s}^{2} &= \mathcal{F}_{N} \left(\left(\frac{2}{d_{N}} \right)^{\frac{c_{N}}{2}} \left(\Gamma \left(\frac{c_{N}}{2} \right) \mathcal{G}_{3,2}^{1,3} \left(a_{E} \Big|_{1,0}^{0,1,1} \right) - \mathcal{H}_{1,0;2,2;1,2}^{0,1;1,2;2,0} \left(\frac{a_{E}}{a_{E} + a_{N}} \Big|_{-:(1,1),(0,1);(0,1),(\frac{c_{N}}{2},1)} \right) \right) \right) \\ - \frac{2a_{N}}{a_{E} + 2a_{N}} \left(\frac{2a_{N}}{d_{N}a_{N} - 2} \right)^{\frac{c_{N}}{2}} \left(\Gamma \left(\frac{c_{N}}{2} \right) \mathcal{G}_{3,2}^{1,3} \left(\frac{a_{E}a_{N}}{a_{E} + a_{N}} \Big|_{1,0}^{0,1,1} \right) \right) \\ - \mathcal{H}_{1,0;2,2;1,2}^{0,1;1,2;2,0} \left(\frac{a_{E}a_{N}}{d_{N}a_{N} - 2} \right)^{\frac{c_{N}}{2}} \left(\Gamma \left(\frac{c_{N}}{2} \right) \mathcal{G}_{3,2}^{1,3} \left(\frac{a_{E}a_{N}}{a_{E} + a_{N}} \Big|_{1,0}^{0,1,1} \right) \right) \\ - \mathcal{H}_{1,0;2,2;1,2}^{0,1;1,2;2,0} \left(\frac{a_{E}a_{N}}{a_{E} + a_{N}} \right) \right|_{1,0}^{0,1,1} \left((0;1,1):(1,1),(1,1);(1,1) \right) \\ - \mathcal{H}_{1,0;2,2;1,2}^{0,1;1,2;2,0} \left(\frac{a_{E}a_{N}}{a_{E} + a_{N}} \right) \right|_{1,0}^{0,1,1} \left((0;1,1):(1,1),(0,1);(0,1),(\frac{c_{N}}{2},1) \right) \right) \right). \tag{20}$$

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other hand, the role of parameters related to the average SNRs 360 361 at the NG in SOP and ASC analytical expressions shows that the better channel condition at the NG can lead to performance 362 363 improvements in both SOP and ASC. It is important to note that the average SNRs at both Eve and NG are influenced by 364 various factors, including the SM's transmission power, the noise 365 power at NG and Eve, and the distance of NG and Eve from 366 the SM and the RIS. Consequently, adjusting these parameters 367 directly impacts the SOP and ASC performance. In addition, it 368 369 is worth noting that within the analytical expression for SOP, we can observe that the SOP performance is contingent on 370 the threshold SNR (denoted by R_t and R'_t) as a function of 371 secrecy rate R_S . Overall, as the numerical results show later, 372 our analysis demonstrates the intricate relationships between 373 various system parameters and the performance of SOP and ASC 374 in the RIS-aided SG communication system. Furthermore, our 375 study highlights the pivotal role of RIS in shaping the overall 376 system performance. 377

V. ASYMPTOTIC ANALYSIS

In this section, given the importance of the secrecy metric per-379 formance in the high-SNR regime, we evaluate the asymptotic 380 381 behavior of both SOP and ASC in RIS-aided SG communication by exploiting the residue approach [44]. 382

A. Asymptotic SOP 383

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384 Because the exact analytical expression of the SOP in the second and fourth terms of (16) is given in relation to the bi-385 variate Fox H-function, we are able to deduce derive the asymp-386 387 totic behavior of SOP as the SNR becomes significantly high 388 (specifically, when $\bar{\gamma}_N \to \infty$). This can be achieved through the utilization of the expansion of the bivariate Fox H-function. 389 To accomplish this, it is needed to assess the residues of the 390 corresponding integrands at the nearest poles to the contour. 391 These poles are identified as the minimum pole on the right 392 393 for cases with large arguments of the Fox H-function and the maximum pole on the left for cases with small arguments. In 394 light of this, the asymptotic SOP can be defined according to the 395 subsequent proposition. 396

Proposition 1: The asymptotic SOP (i.e., $\bar{\gamma}_N \to \infty$) for the 397 considered RIS-aided SG communication system is given by 398 (22). 399

Proof: The proof is elaborated in Appendix D. 400

B. Asymptotic ASC

Since the exact analytical expression of ASC in second and 402 fourth terms of (19) and (20) is in terms of the bivariate Fox 403 H-function, we can derive the asymptotic behavior of the ASC 404 at the high-SNR regime (i.e., $\bar{\gamma}_N \to \infty$) by using the expansion 405 of the bivariate Fox H-function. To do this, we need to evaluate 406 the residue of the corresponding integrands at the closest poles 407 to the contour, namely, the minimum pole on the right for large 408 Fox H-function arguments and the maximum pole on the left for 409 small ones. In addition, we use the same strategy for the used 410 Meijer G-functions in the first and third terms of (19) and (20). 411 Therefore, the asymptotic ASC can be determined according to 412 the following proposition. 413

Proposition 2: The asymptotic ASC for the considered RIS-414 aided SG communication system is given by (23).

Proof: The proof is elaborated in Appendix E.

Remark 2: By contrasting Theorems 2 and 3 with Proposi-417 tions 1 and 2, it becomes apparent that the analytical expressions 418 of SOP and ASC that are formulated in terms of the bivariate Fox 419 H-function can be streamlined into Meijer G-function when the 420 system is operating in a high-SNR regime, leveraging the residue 421 method. Similar to the explanation provided in Remark 1, we can 422 readily discern the manner in which various system parameters 423 influence the asymptotic behavior of SOP and ASC under high-424 SNR conditions. In addition, as shown in numerical findings, it 425 is noteworthy that the asymptotic results in (22) and (23) will 426 gradually approximate the exact SOP and ASC, respectively, 427 with high accuracy as $\bar{\gamma}_{\rm N} \to \infty$. 428

$$P_{\text{SOP}}^{\text{asy}} = \mathcal{F}_{N} \left(\left(\frac{2}{d_{N}} \right)^{\frac{c_{N}}{2}} \left(\Gamma\left(\frac{c_{N}}{2} \right) + \frac{R'_{t} e^{\frac{R'_{t}}{a_{E}R_{t}}}}{a_{E}R_{t}} \mathcal{G}_{1,2}^{2,0} \left(\frac{d_{N}R'_{t}}{2} \Big|_{\frac{c_{N}}{2}, -1} \right) \right) \right) - \left(\frac{2a_{N}}{d_{N}a_{N} - 2} \right)^{\frac{c_{N}}{2}} \left(\frac{2\Gamma\left(\frac{c_{N}}{2}\right) e^{-\frac{a_{N}R'_{t}}{2}}}{2 + a_{E}a_{N}R_{t}} + \frac{R'_{t} e^{\frac{R'_{t}}{a_{E}R_{t}}}}{a_{E}R_{t}} \mathcal{G}_{1,2}^{2,0} \left(\frac{R'_{t}(a_{N}d_{N} - 2)}{2a_{N}} \Big|_{\frac{c_{N}}{2}, -1} \right) \right) \right) \right).$$
(22)
$$\bar{C}_{s}^{\text{asy}} = \frac{\mathscr{F}_{N}a_{N}^{2}\Gamma\left(\frac{c_{N}}{2}\right)}{\ln 2} \left(1 - \left(\frac{a_{E}}{a_{E} + a_{N}} \right)^{2} \right) - \frac{1}{\ln 2}\mathcal{G}_{3,2}^{1,3} \left(a_{E} \Big|_{1,0}^{0,1,1} \right) + \frac{\mathcal{F}_{N}}{\ln 2} \left(\left(\frac{2}{d_{N}} \right)^{\frac{c_{N}}{2}} \left(\Gamma\left(\frac{c_{N}}{2}\right) a_{E} - \frac{2}{d_{N}a_{E}} \mathcal{G}_{3,2}^{1,3} \left(\frac{2}{d_{N}} \Big|_{1,-1}^{1,1,-\frac{c_{N}}{2}} \right) \right) \right) - \left(\frac{2a_{N}}{d_{N}a_{N} - 2} \right)^{\frac{c_{N}}{2}} \left(\Gamma\left(\frac{c_{N}}{2}\right) \left(\frac{2a_{N}a_{E}}{2a_{N} + a_{E}} \right)^{2} - \frac{2a_{N}}{a_{E}(d_{N}a_{N} - 2)} \mathcal{G}_{3,2}^{1,3} \left(\frac{2a_{N}}{d_{N}a_{N} - 2} \Big|_{1,-1}^{1,1,-\frac{c_{N}}{2}} \right) \right) \right).$$
(22)





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VI. ANALYTICAL AND SIMULATION RESULTS

In this section, we conduct a comprehensive validation of the
derived analytical expressions for both the SOP and the ASC
through rigorous Monte Carlo simulations. Moreover, we meticulously analyze the influence of various system parameters on
the secrecy performance of RIS-assisted SG communications.

435 A. Simulation Setup

We consider an RIS-aided SG NAN communication, featuring 436 an SM with limited transmission power, a passive eavesdropper, 437 an NG as a legitimate receiver, and an RIS with M reflecting ele-438 ments. As illustrated in Fig. 2, the SM maintains a fixed location 439 at coordinates (0,0,0), sending its collected private information 440 to the NG. The RIS (with an optimized phase shifting) is located 441 at coordinates (225,200,0) to enhance the connections at the 442 NG, thereby improving the system's secrecy performance. Eve 443 and NG are situated at (400,85,0) and (475,160,0), respectively, 444 positioning the NG farther from the RIS and the SM compared to 445 Eve's distance from these entities. This arrangement, designed 446 to encapsulate the worst case scenario and enable insightful 447 performance analysis, leads to the following fixed distances: 448 $d_{SR} = 300 \text{ m}, d_{SN} = 500 \text{ m}, d_{SE} = 400 \text{ m}, d_{RN} = 250 \text{ m},$ 449 and $d_{RE} = 200$ m. We consider $R_S = 1$ bps/Hz and model 450 all the relevant channels with independent complex Gaussian 451 random variables, representing Rayleigh fading with a path-loss 452 exponent $\chi = 3.5$. The noise power received at Eve and NG 453 is set as $\sigma_E^2 = -40$ dBm and $\sigma_N^2 = -60$ dBm, respectively. 454 Acknowledging the pragmatic limitation of transmission power 455 for SMs in real-world SG contexts, we set $P_S = 20$ dBm. 456 Notably, while commonly utilized mathematical software tools, 457 such as Mathematica, Maple, and MATLAB, lack inclusion 458 of the extended generalized bivariate Fox H-function, its im-459 plementation was successfully achieved through programming 460 functions, as exemplified in [45]. However, for implement-461 ing other mathematical functions, such as the Meijer G and 462 Gamma functions, we used the preexisting functions available in 463 464 MATLAB.



Fig. 3. SOP versus $\bar{\gamma}_{N_2}$ regarding various numbers of RIS elements.



Fig. 4. SOP versus $\bar{\gamma}_{N_2}$ regarding various $\bar{\gamma}_{E_2}$ and M = 10.

B. Results and Discussions

Fig. 3 demonstrates the behavior of SOP as a function of $\bar{\gamma}_{N_2}$ 466 for different values of RIS elements, M. The findings consis-467 tently reveal that as $\bar{\gamma}_{N_2}$ increases while keeping M constant, the 468 SOP decreases. Furthermore, as the number of RIS elements, M, 469 grows, there is a notable reduction in SOP. This improvement in 470 SOP can be attributed to the utilization of the RIS, which enables 471 the establishment of a high-quality communication channel. As 472 a result, there is an enhancement in the SNR at the receiver 473 node NG when the phase-shift matrix of the RIS is appropriately 474 configured. In Fig. 4, the behavior of SOP is depicted in terms of 475 $\bar{\gamma}_{N_2}$ for fixed M and selected values of $\bar{\gamma}_{E_2}$. As $\bar{\gamma}_{N_2}$ increases, we 476 observe a corresponding decrease in SOP, which is reasonable 477 given that the main channel conditions are improving. Moreover, 478 as $\bar{\gamma}_{E_2}$ increases, a higher value of SOP is obtained for a fixed 479 value of $\bar{\gamma}_{N_2}$ since the Eve's channel is experiencing better 480 conditions. Notably, even when the main channel is inferior to 481 the eavesdropper channel (i.e., $\bar{\gamma}_{N_2} < \bar{\gamma}_{E_2}$), SOP is greater than 482 0.5. This is due to the possibility of achieving a small positive 483 secrecy rate under such conditions. However, in practical SG 484 communication scenarios, the main objective is to achieve the 485 least possible value of SOP for secure communication, which 486 can be attained when $\bar{\gamma}_{N_2} \geq \bar{\gamma}_{E_2}$. Fig. 5 demonstrates the impact 487 of the secrecy rate, R_S , on the performance of SOP for various 488 M. The results indicate that as the secrecy rate increases, the 489 performance of SOP deteriorates to the point, where secure 490 communication is no longer feasible at high rates. Nevertheless, 491 the presence of an RIS with M elements results in a slower 492 attenuation of SOP compared to the scenario where no RIS is 493



Fig. 5. SOP versus S_R regarding various numbers of RIS elements.



Fig. 6. ASC versus $\bar{\gamma}_{N_2}$ regarding various numbers of RIS elements.



Fig. 7. ASC versus $\bar{\gamma}_{N_2}$ regarding various values of $\bar{\gamma}_{E_2}$ and M = 4.

employed. Fig. 6 depicts the performance of ASC as a function of 494 $\bar{\gamma}_{N_2}$ regarding different values M. The results suggest that ASC 495 exhibits a consistent increase as $\bar{\gamma}_{N_2}$ rises for a fixed value of M. 496 Moreover, as the value of M increases, there is a significant boost 497 in ASC. This can be attributed to the utilization of the RIS, which 498 facilitates the provision of a high-quality channel that improves 499 the received SNR at the NG when the phase matrix of the RIS 500 is appropriately adjusted. 501

Fig. 7 illustrates the performance of ASC as a function of $\bar{\gamma}_{N_2}$ 502 regarding various selected values of $\bar{\gamma}_{E_2}$, while keeping M fixed. 503 As $\bar{\gamma}_{N_2}$ increases, the ASC also increases, which is expected 504 because the main channel conditions improve. Moreover, as $\bar{\gamma}_{E_2}$ 505 increases, the ASC for a fixed $\bar{\gamma}_{N_2}$ decreases. However, it is evi-506 dent that even if $\bar{\gamma}_{N_2} \leq \bar{\gamma}_{E_2}$, the ASC can still be attained. Fig. 8 507 demonstrates the performance of ASC as a function of the SM's 508 transmission power, P_S , regarding different values of M. The 509



Fig. 8. ASC versus P_S regarding various numbers of RIS elements.

results indicate that ASC increases as P_S rises for a fixed value of 510 M. Moreover, when the value of M increases, a considerable en-511 hancement in ASC is observed due to gaining a superior channel 512 and higher SNR at the NG by using the RIS. In many practical SG 513 scenarios, increasing the SM's transmission power to improve 514 the communication performance is not a viable option due to 515 regulatory limits, energy consumption constraints, and interfer-516 ence concerns. However, as highlighted by the results, increasing 517 the number of RIS elements offers a notable enhancement in SG 518 communication performance, all while alleviating the burden on 519 SMs to operate at higher transmission power levels. This dual 520 benefit not only leads to improved ASC but also plays a crucial 521 role in extending the battery life of SMs, ensuring their sustained 522 operation at lower transmission power settings. As a result, the 523 utilization of RIS emerges as a practical and effective solution 524 for achieving improved secrecy performance while allowing 525 SMs to operate at lower transmission power levels. In summary, 526 both the analytical and simulation findings demonstrate that 527 the integration of RIS technology into the SG infrastructure 528 yields substantial improvements in PLS, significantly enhancing 529 security and confidentiality. Specifically, employing the RIS 530 with a larger value of M offers greater degrees of freedom 531 for efficient beamforming, significantly improving the secrecy 532 performance in SG communications. 533

VII. CONCLUSION

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In this article, we explored the transformative potential of 535 integrating RIS into SG communications to enhance the PLS 536 performance. Our study involved the deployment of an RIS 537 alongside key SG components, including SMs, NGs, and poten-538 tial eavesdroppers, creating a smart environment within the SG 539 infrastructure. Specifically, we evaluated the PLS performance 540 in terms of SOP and ASC. Our analytical approach began by 541 deriving closed-form expressions for the PDF and CDF of the 542 received SNR at both NG and Eve. Then, we derived accurate 543 analytical expressions for SOP and ASC. This allowed us to sys-544 tematically assess how various system parameters influence the 545 secrecy performance of RIS-aided SG communication system. 546 Furthermore, we conducted an asymptotic analysis under high-547 SNR conditions, recognizing the significance of understanding 548 system behavior in such regimes. To validate the analytical re-549 sults and reinforce the robustness of our findings, we performed 550

Monte Carlo simulations. The consistency between analytical
and simulated results further substantiates the effectiveness of
RIS in enhancing the secrecy performance of SG communica-

tions compared to SG scenarios without the RIS.

555 APPENDIX A 556 PROOF OF THEOREM 1

557 We use the definition of the MGF to obtain

 $M_{\gamma_{N_1}}(t)$

558 as

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$$M_{\gamma_{N_{1}}}(t) = \int_{0}^{\infty} e^{t\gamma_{N_{1}}} f_{\gamma_{N_{1}}}(\gamma_{N_{1}}) d\gamma_{N_{1}}$$
$$= \frac{1}{\bar{\gamma}_{N_{1}} a_{N}} \int_{0}^{\infty} e^{\gamma_{N_{1}} \left(t - \frac{1}{a_{N}}\right)} d\gamma_{N_{1}} = \frac{1}{\bar{\gamma}_{N_{1}} (1 - a_{N} t)}.$$
 (24)

559 Thus, we have $M_{\gamma_{N_1}}(s)$ as

$$M_{\gamma_{N_1}}(s) = \frac{1}{\bar{\gamma}_{N_1}(1 + a_N s)}.$$
(25)

560 Similar to (24), $M_{\gamma_{N_2}}(t)$ can be obtained as follows:

$$M_{\gamma_{N_{2}}}(t) = \frac{1}{2\bar{\gamma}_{N_{2}}\Gamma(c_{N}) d_{N}^{c_{N}}} \int_{0}^{\infty} e^{\gamma_{N_{2}}\left(t - \frac{1}{2d_{N}}\right)} \gamma_{N_{2}} \frac{c_{N}}{2} - 1} d\gamma_{N_{2}}$$
$$= \frac{\Gamma\left(\frac{c_{N}}{2}\right)}{2\bar{\gamma}_{N_{2}}\Gamma(c_{N}) d_{N}^{c_{N}}} \left(\frac{d_{N}}{2} - t\right)^{-\frac{c_{N}}{2}}.$$
 (26)

561 Then, we have $M_{\gamma_{N_2}}(s)$ as

$$M_{\gamma_{N_2}}(s) = \frac{\Gamma\left(\frac{c_N}{2}\right)}{2\bar{\gamma}_{N_2}\Gamma(c_N)d_N^{c_N}} \left(\frac{d_N}{2} + s\right)^{-\frac{c_N}{2}}.$$
 (27)

By using the Laplace inverse transform in Mathematica, (6) can 562 be obtained as 563

$$f_{\gamma_N}(\gamma_N) = \mathscr{F}_N e^{-\frac{\gamma_N}{a_N}} \left(\Gamma\left(\frac{c_N}{2}\right) - \Gamma\left(\frac{c_N}{2}, \left(\frac{d_N a_N - 2}{2a_N}\right) \gamma_N\right) \right).$$
(28)

Now, by writing the incomplete Gamma function based on the Meijer G-function using [47, eq. (8.4.16.2)], $f_{\gamma_N}(\gamma_N)$ is obtained as (8), and the proof is completed. According to (7) and taking the same steps of computing $f_{\gamma_N}(\gamma_N)$, $F_{\gamma_N}(\gamma_N)$ can be obtained as (29) shown at the bottom of this page. Now, by using [47, eq. (8.4.16.2)], $F_{\gamma_N}(\gamma_N)$ in (29) can be obtained as (9), and the proof is completed. 570

APPENDIX B571PROOF OF THEOREM 2572

According to the SOP definition in (15) and by having the 573 derived CDF for the received SNR at the NG in (9) and the PDF 574 of the received SNR at Eve in (11), we can rewrite (15) as (30)575 shown at the bottom of this page. In (30), we can simply obtain 576 $I_1 = a_E$. For computing I_2 , we use the integral-form definition 577 of the Meijer G-function. Thus, we have I_2 as (31) shown at the 578 bottom of this page. In order to compute I'_2 in (31), we use [48, 579 eq. (3.381.4)]; thus, we have I'_2 as 580

$$I_{2}' = a_{E}^{1+\zeta_{1}} R_{t}^{\zeta_{1}} e^{\frac{R_{t}'}{a_{E}R_{t}}} \mathcal{G}_{1,2}^{2,0} \left(\frac{R_{t}'}{a_{E}R_{t}} \middle| \begin{array}{c} 1\\ 0, 1+\zeta_{1} \end{array} \right).$$
(32)

Now, by putting (32) in (31) and using the integral-form definition of the Meijer G-function, we have I_2 as (33) shown at the bottom of the next page. Since (33) demonstrates the integral-form definition of the bivariate Fox H-function, we can show I_2 as the second term of P_{SOP} in (16). I_3 can also be simply 585

$$F_{\gamma_N}(\gamma_N) = \mathcal{F}_N\left(\left(\frac{d_N}{2}\right)^{-\frac{c_N}{2}} \left(\Gamma\left(\frac{c_N}{2}\right) - \Gamma\left(\frac{c_N}{2}, \frac{d_N\gamma_N}{2}\right)\right) - \left(\frac{d_Na_N - 2}{2a_N}\right)^{-\frac{c_N}{2}} e^{-\frac{\gamma_N}{a_N}} \left(\Gamma\left(\frac{c_N}{2}\right) - \Gamma\left(\frac{c_N}{2}, \left(\frac{d_Na_N - 2}{2a_N}\right)\gamma_N\right)\right)\right).$$

$$P_{\text{SOP}} = \frac{\mathcal{F}_N}{a_E} \left(\left(\frac{2}{d_N}\right)^{\frac{c_N}{2}} \Gamma\left(\frac{c_N}{2}\right) \underbrace{\int_0^\infty e^{\frac{-\gamma_E}{a_E}} d\gamma_E}_{I_1} - \left(\frac{2}{d_N}\right)^{\frac{c_N}{2}} \underbrace{\int_0^\infty e^{\frac{-\gamma_E}{a_E}} \mathcal{G}_{1,2}^{2,0}\left(\frac{d_N}{2}(R_t\gamma_E + R_t')\Big|_0, \frac{c_N}{2}\right) d\gamma_E}_{I_2} \right)$$

$$\left(-\frac{2a_N}{a_N}\right)^{\frac{c_N}{2}} \left(\Gamma\left(\frac{c_N}{2}\right) \int_0^\infty e^{\frac{-\gamma_E}{a_E}} e^{\frac{-(R_t\gamma_E + R_t')}{2}} dr_N - \left(\frac{2}{a_N}\right)^{\frac{c_N}{2}} \frac{e^{-\frac{(R_t\gamma_E + R_t')}{2}}}{I_2} dr_N \right) dr_N \right) dr_N$$

$$(29)$$

$$-\left(\frac{2a_N}{d_Na_N-2}\right)^{\frac{-\alpha}{2}} \left(\Gamma\left(\frac{c_N}{2}\right) \underbrace{\int_0^\infty e^{\frac{-\gamma_E}{a_E}} e^{\frac{-(R_t\gamma_E + R't)}{2a_N}} d\gamma_E}_{I_3} - \underbrace{\int_0^\infty e^{\frac{-\gamma_E}{a_E}} e^{\frac{-(R_t\gamma_E + R't)}{2a_N}} \mathcal{G}_{1,2}^{2,0} \left(\frac{(d_Na_N-2)(R_t\gamma_E + R'_t)}{2a_N}\Big|_{0,\frac{c_N}{2}}\right) d\gamma_E}_{I_4} \right).$$

$$(30)$$

$$I_{2} = \frac{1}{2\pi i} \underbrace{\int_{0}^{\infty} e^{-\frac{\gamma_{E}}{a_{E}}} \left(R_{t}\gamma_{E} + R_{t}'\right)^{\zeta_{1}} d\gamma_{E}}_{I_{2}'} \oint_{L_{1}} \frac{\Gamma(-\zeta_{1})\Gamma(\frac{c_{N}}{2} - \zeta_{1}) \left(\frac{d_{N}}{2}\right)^{\zeta_{1}}}{\Gamma(1 - \zeta_{1})} d\zeta_{1}.$$
(31)

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586 obtained as

$$I_3 = \frac{2a_E e^{-\frac{a_N R'_t}{2}}}{2 + a_E a_N R_t}.$$
 (34)

In order to solve I_4 , we take the exactly same steps as we took for computing I_2 ; thus, I_4 can be obtained as the fourth term of P_{SOP} in (16). Therefore, the SOP expression can be obtained as shown in (16), and the proof is completed.

591APPENDIX C592PROOF OF THEOREM 3

By inserting (13) into (17), ASC can be expressed as (35) 593 shown at the bottom of this page. For completing the proof, 594 we start with J_1 . For solving J_1 , we use the Meijer G-function 595 demonstration of the logarithm function, as shown in [46, eq. 596 (8.4.6.5)]. By inserting (8) and (12) into J_1 in (35), we can 597 rewrite J_1 as (36) shown at the bottom of this page. J_1^1 and J_1^2 598 can be computed using [46, eq. (2.24.3.1)] as shown in the first 599 and third terms of (19), respectively. For computing J_1^3 , we use 600 the integral-form definition of the Meijer G-function for both 601 the Meijer G-functions in the integral. Thus, we have J_1^3 as (37) 602 shown at the bottom of this page. In order to compute $J_1^{\prime 3}$, we 603

use [48, eq. (3.381.4)] as

$$J_1^{\prime 3} = a_N^{1+\zeta_1+\zeta_2} \Gamma(1+\zeta_1+\zeta_2).$$
(38)

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Now, by putting (38) in (37), we have J_1^3 as (39) shown at the bottom of the next page. Since (39) demonstrates the integralform definition of the bivariate Fox H-function, we can show J_1^3 as the second term of \bar{C}_s^1 in (19). In order to solve J_1^4 , we take the exactly same steps as we took for computing J_1^3 ; thus, J_1^4 can be obtained as the fourth term of \bar{C}_s^1 in (19). Therefore, J_1 in (35) can be derived as \bar{C}_s^1 shown in (19).

In order to solve J_2 , we insert (9) and (11) into J_2 in (35). 612 Therefore, we can rewrite J_2 as (40) shown at the bottom of the 613 next page. For solving J_2^1 , J_2^2 , J_2^3 , and J_2^4 in (40), since we have 614 the same integrals, we can take the exactly same steps that we 615 took for solving J_1^1 , J_1^3 , J_1^2 , and J_1^4 , respectively. Therefore, J_2 616 in (35) can be derived as \bar{C}_s^2 shown in (20). In order to solve J_3 , 617 we first insert (11) and the Meijer G-function demonstration of 618 the logarithm function into J_3 in (35). Then, we need to solve 619 the following integral: 620

$$J_{3} = \frac{1}{a_{E}} \int_{0}^{\infty} e^{\frac{-\gamma_{E}}{a_{E}}} \mathcal{G}_{2,2}^{1,2} \left(\gamma_{E} \Big| \begin{array}{c} 1, 1\\ 1, 0 \end{array}\right) d\gamma_{E}$$
(41)

which can be computed as \bar{C}_s^3 , as shown in (21) using [46, 621 eq. (2.24.3.1)]. Now, by inserting the obtained closed-form 622

$$I_{2} = \frac{a_{E}e^{\frac{R'_{t}}{a_{E}R_{t}}}}{2\pi i} \oint_{L_{1}} \frac{\Gamma(-\zeta_{1})\Gamma(\frac{c_{N}}{2}-\zeta_{1})\left(\frac{a_{E}d_{N}R_{t}}{2}\right)^{\zeta_{1}}}{\Gamma(1-\zeta_{1})} \mathcal{G}_{1,2}^{2,0}\left(\frac{R'_{t}}{a_{E}R_{t}}\Big|_{0,1+\zeta_{1}}^{1}\right) d\zeta_{1}$$
$$= -\frac{a_{E}e^{\frac{R'_{t}}{a_{E}R_{t}}}}{(2\pi i)^{2}} \oint_{L_{1}} \oint_{L_{2}} \frac{\Gamma(1+\zeta_{1}+\zeta_{2})\Gamma(-\zeta_{1})\Gamma(\frac{c_{N}}{2}-\zeta_{1})\left(\frac{a_{E}d_{N}R_{t}}{2}\right)^{\zeta_{1}}\Gamma(\zeta_{2})\left(\frac{a_{E}R_{t}}{R'_{t}}\right)^{\zeta_{2}}}{\Gamma(1-\zeta_{1})\Gamma(1+\zeta_{2})} d\zeta_{2}d\zeta_{1}.$$
(33)

$$\bar{C}_{s} = \underbrace{\int_{0}^{\infty} \log(1+\gamma_{N}) f_{\gamma_{N}}(\gamma_{N}) F_{\gamma_{E}}(\gamma_{N}) d\gamma_{N}}_{J_{1}} + \underbrace{\int_{0}^{\infty} \log(1+\gamma_{E}) f_{\gamma_{E}}(\gamma_{E}) F_{\gamma_{N}}(\gamma_{E}) d\gamma_{E}}_{J_{2}} - \underbrace{\int_{0}^{\infty} \log(1+\gamma_{E}) f_{\gamma_{E}}(\gamma_{E}) d\gamma_{E}}_{J_{3}}.$$
(35)

$$J_{1} = \frac{\mathcal{F}_{N}}{\ln 2} \left(\Gamma\left(\frac{c_{N}}{2}\right) \left(\underbrace{\int_{0}^{\infty} e^{\frac{-\gamma_{N}}{a_{N}}} \mathcal{G}_{2,2}^{1,2}\left(\gamma_{N} \Big| \frac{1,1}{1,0}\right) d\gamma_{N}}_{J_{1}^{1}} - \underbrace{\int_{0}^{\infty} e^{\frac{-\gamma_{N}}{a_{N}}} e^{\frac{-\gamma_{N}}{a_{E}}} \mathcal{G}_{2,2}^{1,2}\left(\gamma_{N} \Big| \frac{1,1}{1,0}\right) d\gamma_{N}}_{J_{1}^{2}} \right) \right)$$

$$-\underbrace{\int_{0}^{\infty} e^{\frac{-\gamma_{N}}{a_{N}}} \mathcal{G}_{2,2}^{1,2}\left(\gamma_{N}\Big|_{1,0}^{1,1}\right) \mathcal{G}_{1,2}^{2,0}\left(\frac{(d_{N}a_{N}-2)\gamma_{N}}{2a_{N}}\Big|_{0,\frac{c_{N}}{2}}^{1}\right) d\gamma_{N}}_{J_{1}^{3}} -\underbrace{\int_{0}^{\infty} e^{\frac{-\gamma_{N}}{a_{N}}} e^{\frac{-\gamma_{N}}{a_{E}}} \mathcal{G}_{2,2}^{1,2}\left(\gamma_{N}\Big|_{1,0}^{1,1}\right) \mathcal{G}_{1,2}^{2,0}\left(\frac{(d_{N}a_{N}-2)\gamma_{N}}{2a_{N}}\Big|_{0,\frac{c_{N}}{2}}^{1}\right) d\gamma_{N}}_{J_{1}^{4}} \\ \xrightarrow{(36)}$$

$$J_{1}^{3} = \frac{1}{(2\pi i)^{2}} \underbrace{\int_{0}^{\infty} \gamma_{N}^{\zeta_{1}+\zeta_{2}} e^{-\frac{\gamma_{N}}{a_{N}}} d\gamma_{N}}_{J_{1}^{\prime 3}} \oint_{L_{1}} \oint_{L_{2}} \frac{\Gamma^{2}(\zeta_{1})\Gamma(1-\zeta_{1})\Gamma(-\zeta_{2})\Gamma\left(\frac{c_{N}}{2}-\zeta_{2}\right) \left(\frac{a_{N}d_{N}-2}{2a_{N}}\right)^{\zeta_{2}}}{\Gamma(1+\zeta_{1})\Gamma(1-\zeta_{2})} d\zeta_{2} d\zeta_{1}.$$
(37)

expression of J_1 , J_2 , and J_3 into (35), the proof for ASC is completed.

625 APPENDIX D 626 PROOF OF PROPOSITION 1

In the case of $\bar{\gamma}_N \to \infty$, the integral-form demonstration of bivariate Fox H-function in (33) is assessed at the highest poles situated to the left of L_2 , which is when $\zeta_2 = -1 - \zeta_1$. As a result, we arrive at the integral presented in (42) pertaining to counter L_2

$$\mathcal{R}_{1} = \frac{1}{2\pi j} \oint_{L_{2}} \Gamma\left(1 + \zeta_{1} + \zeta_{2}\right) \underbrace{\frac{\Gamma\left(\zeta_{2}\right) \left(\frac{a_{E}R_{t}}{R_{t}'}\right)^{\zeta_{2}}}{\Gamma\left(1 + \zeta_{2}\right)}}_{\chi_{1}(\zeta_{2})} d\zeta_{2}.$$
 (42)

Since $\mathcal{R}_1 = \operatorname{Res}[\chi_1(\zeta_2), -1 - \zeta_1]$, we can rewrite (42) as

$$\mathcal{R}_{1} = \lim_{\zeta_{2} \to -1-\zeta_{1}} \left(1 + \zeta_{1} + \zeta_{2}\right) \chi_{1}(\zeta_{2})$$
$$= \frac{\Gamma\left(-1 - \zeta_{1}\right) \left(\frac{a_{E}R_{t}}{R_{t}'}\right)^{-1-\zeta_{1}}}{\Gamma\left(-\zeta_{1}\right)}.$$
(43)

Now, by inserting (43) into (33), the asymptotic I_2 can be obtained as follows:

$$I_{2}^{\text{asy}} = \frac{R_{t}'}{a_{E}R_{t}2\pi i} \oint_{L_{1}} \frac{\Gamma(\frac{c_{N}}{2} - \zeta_{1})\Gamma(-1 - \zeta_{1})\left(\frac{d_{N}R_{t}'}{2}\right)^{\zeta_{1}}}{\Gamma(1 - \zeta_{1})} d\zeta_{1}.$$
(44)

Now, based on the definition of the Meijer G-function, (44) can be shown as the second term of (22). Similarly, we can assess the bivariate Fox H-function in the fourth term of (16) the highest poles situated to the left of L_2 , which is when $\zeta_2 = -1 - \zeta_1$. By taking the exactly same steps, the asymptotic I_4 can be obtained in the form of a Meijer G-function, as shown in the fourth term of (22). As a result, the proof will be completed for asymptotic 641 SOP. 642

In the case of $\bar{\gamma}_N \to \infty$, the asymptotic ASC can be expressed 645 as 646

$$\bar{C}_{\rm s}^{\rm asy} = \bar{C}_s^{1,\rm asy} + \bar{C}_s^{2,\rm asy} - J_3.$$
 (45)

In order to compute $\bar{C}_s^{1,asy}$, we can see that the Meijer G-function 647 in the first term of (19) is evaluated at the highest poles on the left 648 of L_2 , i.e., $\zeta_1 = 1$, in its integral-form demonstration as follows: 649

$$\mathcal{R}_2 = \frac{1}{2\pi i} \oint_{L_1} \Gamma(1-\zeta_1) \underbrace{\Gamma^2(\zeta_1) a_N^{\zeta_1}}_{\chi_1(\zeta_1)} d\zeta_1.$$
(46)

Since $\mathcal{R}_2 = \text{Res}[\chi_1(\zeta_1), 1]$, we can rewrite (46) as

$$\mathcal{R}_2 = \lim_{\zeta_1 \to 1} \left(1 - \zeta_1 \right) \chi_1(\zeta_1) = a_N.$$
(47)

Following the same strategy, we can obtain the asymptotic 651 expression of the other Meijer G-function in \bar{C}_s^1 [third term of 652 (19)] as 653

$$\mathcal{R}_3 = \frac{a_E a_N}{a_E + a_N}.\tag{48}$$

Furthermore, the bivariate Fox H-function in C_s^1 [the second 654 term of (19)], as shown in (39), is evaluated at the highest poles on the left of L_2 , which is when $\zeta_2 = -1 - \zeta_1$. Thus, we have 656 the following integral for the counter L_2 : 657

$$\mathcal{R}_{4} = \frac{1}{2\pi j} \oint_{L_{2}} \Gamma \left(1 + \zeta_{1} + \zeta_{2}\right) \\ \times \underbrace{\frac{\Gamma \left(-\zeta_{2}\right) \Gamma \left(\frac{c_{N}}{2} - \zeta_{2}\right) \left(\frac{a_{N}d_{N} - 2}{2}\right)^{\zeta_{2}}}{\Gamma \left(1 - \zeta_{2}\right)}}_{\chi_{2}(\zeta_{2})} d\zeta_{2}.$$
(49)

$$J_{1}^{3} = \frac{a_{N}}{(2\pi i)^{2}} \oint_{L_{1}} \oint_{L_{2}} \frac{\Gamma(1+\zeta_{1}+\zeta_{2})\Gamma^{2}(\zeta_{1})\Gamma(1-\zeta_{1})a_{N}^{\zeta_{1}}\Gamma(-\zeta_{2})\Gamma\left(\frac{c_{N}}{2}-\zeta_{2}\right)\left(\frac{a_{N}d_{N}-2}{2}\right)^{\zeta_{2}}}{\Gamma(1+\zeta_{1})\Gamma(1-\zeta_{2})} d\zeta_{2}d\zeta_{1}.$$
(39)

$$J_{2} = \frac{\mathcal{F}_{N}}{a_{E} \ln 2} \left(\left(\frac{2}{d_{N}}\right)^{\frac{c_{N}}{2}} \left(\Gamma\left(\frac{c_{N}}{2}\right) \underbrace{\int_{0}^{\infty} e^{\frac{-\gamma_{E}}{a_{E}}} \mathcal{G}_{2,2}^{1,2}}_{J_{2}^{1}} \left(\gamma_{E} \Big| \frac{1,1}{1,0} \right) d\gamma_{E}}_{J_{2}^{1}} - \underbrace{\int_{0}^{\infty} e^{\frac{-\gamma_{E}}{a_{E}}} \mathcal{G}_{2,2}^{1,2}}_{J_{2}^{2}} \left(\gamma_{E} \Big| \frac{1,1}{1,0} \right) \mathcal{G}_{1,2}^{2,0} \left(\frac{d_{N}\gamma_{E}}{2} \Big| \frac{1}{0}, \frac{c_{N}}{2} \right) d\gamma_{E}}_{J_{2}^{2}} \right) - \left(\frac{2a_{N}}{a_{N}d_{N}-2}\right)^{\frac{c_{N}}{2}} \left(\Gamma\left(\frac{c_{N}}{2}\right) \underbrace{\int_{0}^{\infty} e^{\frac{-\gamma_{E}}{a_{E}}} e^{\frac{-\gamma_{E}}{2a_{N}}} \mathcal{G}_{2,2}^{1,2}}_{J_{2}^{2}} \left(\gamma_{E} \Big| \frac{1,1}{1,0} \right) d\gamma_{E}}_{J_{2}^{2}} - \underbrace{\int_{0}^{\infty} e^{\frac{-\gamma_{E}}{a_{E}}} e^{\frac{-\gamma_{E}}{2a_{N}}} \mathcal{G}_{2,2}^{1,2}} \left(\gamma_{E} \Big| \frac{1,1}{1,0} \right) \mathcal{G}_{1,2}^{2,0} \left(\frac{(d_{N}a_{N}-2)\gamma_{E}}{2a_{N}} \Big| \frac{1}{0}, \frac{c_{N}}{2} \right) d\gamma_{E}}_{J_{2}^{4}} \right) \right) \right).$$
(40)

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$$J_{1}^{3,\text{asy}} = \frac{1}{(a_{N}d_{N}-2)\pi i} \oint_{L_{1}} \frac{\Gamma\left(1-\zeta_{1}\right)\Gamma^{2}\left(\zeta_{1}\right)\Gamma\left(1+\frac{c_{N}}{2}+\zeta_{1}\right)\left(\frac{2a_{N}}{a_{N}d_{N}-2}\right)^{\zeta_{1}}}{\Gamma\left(2+\zeta_{1}\right)} d\zeta_{1} = \frac{2}{a_{N}d_{N}-2}\mathcal{G}_{3,2}^{1,3}\left(\frac{2a_{N}}{a_{N}d_{N}-2}\Big|^{0},1,-\frac{c_{N}}{2}\right).$$
(51)

$$\bar{C}_{s}^{2,\text{asy}} = \frac{\mathcal{F}_{N}}{\ln 2} \left(\left(\frac{2}{d_{N}}\right)^{\frac{c_{N}}{2}} \left(\Gamma\left(\frac{c_{N}}{2}\right) a_{E} - \frac{2}{d_{N}a_{E}} \mathcal{G}_{3,2}^{1,3} \left(\frac{2}{d_{N}} \left| \begin{array}{c} 1, 1, -\frac{c_{N}}{2} \\ 1, -1 \end{array} \right) \right) \right) \\ - \left(\frac{2a_{N}}{d_{N}a_{N} - 2} \right)^{\frac{c_{N}}{2}} \left(\Gamma\left(\frac{c_{N}}{2}\right) \left(\frac{2a_{N}a_{E}}{2a_{N} + a_{E}}\right)^{2} - \frac{2a_{N}}{a_{E}(d_{N}a_{N} - 2)} \mathcal{G}_{3,2}^{1,3} \left(\frac{2a_{N}}{d_{N}a_{N} - 2} \left| \begin{array}{c} 1, 1, -\frac{c_{N}}{2} \\ 1, -1 \end{array} \right) \right) \right).$$
(54)

Since $\mathcal{R}_4 = \operatorname{Res}[\chi_2(\zeta_2), -1 - \zeta_1]$, we can rewrite (49) as 658

$$\mathcal{R}_{4} = \lim_{\zeta_{2} \to -1-\zeta_{1}} \left(1 + \zeta_{1} + \zeta_{2}\right) \chi_{2}(\zeta_{2})$$
$$= \frac{\Gamma\left(1 + \zeta_{1}\right) \Gamma\left(1 + \frac{c_{N}}{2} + \zeta_{1}\right) \left(\frac{a_{N}d_{N} - 2}{2}\right)^{-1-\zeta_{1}}}{\Gamma\left(2 + \zeta_{1}\right)}.$$
 (50)

Now, by inserting (50) into (39), $J_1^{3,asy}$ can be determined as (51) 659 shown at the top of this page. Similarly, the other bivariate Fox 660 H-function in \overline{C}_s^1 [the fourth term of (19)] can also be evaluated at 661 the highest poles on the left of L_2 , which is when $\zeta_2 = -1 - \zeta_1$. Thus, by taking the exactly same steps, $J_1^{4,asy}$ can be obtained 662 663 664 as

$$J_{1}^{4,\text{asy}} = \frac{2(a_{E} + a_{N})}{a_{E}(a_{N}d_{N} - 2)} \mathcal{G}_{3,2}^{1,3} \left(\frac{2a_{N}}{a_{N}d_{N} - 2} \Big| \begin{matrix} 0, 1, -\frac{c_{N}}{2} \\ 1, -1 \end{matrix} \right).$$
(52)

Now, by inserting (47), (48), (51), and (52) into their corre-665 sponding Meijer G and bivariate Fox H-functions in (19), $\bar{C}_s^{1,asy}$ 666 is obtained as 667

$$\bar{C}_{s}^{\text{asy}} = \frac{\mathscr{F}_{N}a_{N}^{2}\Gamma\left(\frac{c_{N}}{2}\right)}{\ln 2} \left(1 - \left(\frac{a_{E}}{a_{E} + a_{N}}\right)^{2}\right).$$
 (53)

Similarly, and by taking the exactly same steps for \bar{C}_s^2 , $\bar{C}_s^{2,asy}$ 668 can be obtained as (54) shown at the top of this page. Finally, 669 by plugging (41), (53), and (54) into (45), (23) is obtained, and 670 the proof is completed for the asymptotic ASC. 671

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