

# Design of Optimal IIR Band pass and Band stop Filters using TSA Technique and Their FPGA Implementation

V. Karthik, K. Susmitha, S. K. Saha, R. Kar

**Abstract**—A new optimizing technique, named Tree Seed Algorithm (TSA) is utilized for optimizing the coefficients of impulse infinite response (IIR) type bandpass filter (BPF) and bandstop filter (BSF) of order 8. The employed optimizing technique uses the error fitness (EF) function to enhance the performance capabilities of the filter in terms of stopband attenuation, passband ripples (PBR), stopband ripples (SBR) and transition width. The employed algorithm converges rapidly to the optimal solution in fair number of iterations. An analysis of optimally designed IIR filter is carried out by Verilog hardware description language on field programmable gate array (FPGA) platform.

**Keywords**—Tree Seed Algorithm; Convergence; IIR Filter; BPF; BSF.

## I. INTRODUCTION

Information is carried out by the signals. However, due to the presence of noise, signals are getting contaminated. Hence, at receiver-end to extract the information from the noise corrupted signal, a method called signal processing is employed. Signal processing may be digital, analog or both. It varies upon the nature and the point of application of the signal. Digital signal processing (DSP) is confined with addition, multiplication and recall of previous information; hence its application has increased in various fields. Digital filter utilizes less discrete components. So, its performance does not get effected by thermal drift.

Finite impulse response (FIR) and infinite impulse response (IIR) are two varieties of filter [1-2]. FIR filter is termed as non-recursive filter because the yield of this filter relies on the present and past values of input. Hence, less memory is required. While the IIR filter is termed as recursive filter, as the output of the filter relies on both previous and present inputs and previous outputs. So, a considerable memory is needed for storing of past outputs of the IIR filter.

As the design complexity and memory requirement are less, the FIR filter realisation is easier compared to IIR filter. In addition to these, stability and linear phase response over a wide frequency range are also the benefits of the FIR filter. On the other hand, IIR filter ensures to meet the specifications such as sharp transition width, lower PBR, SBR and higher stopband attenuation at lower order in comparison with FIR filter. Due to these, an adequately designed IIR filter can

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produce the frequency response (FR), which is close to ideal magnitude response and better in comparison with FIR filter response [3]. Various gradient based algorithms namely, steepest descent and quasi newton algorithms are employed for the design of optimal filters [4-5].

These algorithms provide the best solution only when a very simple search space is provided. But the search space is multimodal, multidimensional, discontinuous and highly complex. So, only global optimization techniques give the optimal solution. Several metaheuristic algorithms such as genetic algorithm [6], simulated annealing [7], variants of particle swarm optimization [8], artificial immune system [9], ant colony optimization [10] and bacteria foraging algorithm [11] are successfully applied for filter design problem. These optimized filters are applied in the fields of biomedicine for design of electrocardiogram [12].

### a. Contribution

In this paper, to obtain the optimal coefficients an algorithm called TSA [13] which is inspired by the relation between trees and seeds is utilized for optimizing the coefficients of filter.

### b. Organization of paper

The rest of the paper is structured as follows. Section 2 briefly illustrates the problem definition for the filter design. Section 3 discusses the TSA algorithm for optimizing the filter coefficients. Section 4 discusses the FPGA implementation of IIR filter, and section 5 presents the simulation results and discussions. Finally, section 6 concludes the work.

## II. PROBLEM DEFINITION OF FILTER

In this paper, IIR type BPF and BSF are designed by TSA technique. The difference equation of IIR filter [14] is presented in (1):

$$y(p) + \sum_{k=1}^n a_k y(p-k) = \sum_{k=0}^m b_k x(p-k) \quad (1)$$

where  $x(p)$  and  $y(p)$  are the input and output, respectively;  $n(\geq m)$  represents order of the filter;  $a_k$  represents the denominator coefficient, and  $b_k$  represents the numerator coefficient.

Transfer function (TF) of the IIR filter is stated by following equation:

$$H(z) = \frac{\sum_{k=0}^m b_k z^{-k}}{1 + \sum_{k=1}^n a_k z^{-k}} \quad (2)$$

The FR of the IIR filter is given (2) assuming  $z = e^{j\omega}$ :

$$H(e^{j\omega}) = \frac{\sum_{k=0}^m b_k e^{-kj\omega}}{1 + \sum_{k=1}^n a_k e^{-kj\omega}} \quad (3)$$

where  $\omega \in (0, \pi)$  in radians.

In this optimization problem, the fitness function,  $J(\omega)$  is defined in (4). The error fitness value of each search agent is calculated on the basis of magnitude response deviation from its practical response which includes the PBR ( $\delta_p$ ), SBR ( $\delta_s$ ), and transition width of the designed filter,  $|H_d(\omega)|$ .

$$J(\omega) = \sum_{\omega} \text{abs}[(|H_d(\omega)|) - \delta_s] + \sum_{\omega} \text{abs}[\text{abs}(|H_d(\omega)| - 1) - \delta_p] \quad (4)$$

EF function which is mentioned in (4) is the generalized EF function that is to be optimized by TSA optimization technique. The first part and second part of (4) give the error contribution in  $J(\omega)$  for stopband and passband regions, respectively.

### III. TREE SEED ALGORITHM

TSA is a natural phenomenon-based optimization technique that mimics the relation between the trees and the seeds [14]. Seeds that are spread over the surface become new trees which again spread seeds over the surface and this phenomenon continues. The surface area is considered as the search space of the optimization problem. For exploration the search starts randomly from multiple points on problem space by location of trees. The seed location which is produced by a tree plays a key role for solving optimization problem as this procedure contributes for the exploitation. This process can be done in two ways, first one gives the seed location by the tree location which produces this seed, and the better location in the tree population. Second one deals with the producing of a new seed from two different locations [15]. The equations for these phenomena are given by:

$$S_{i,j} = T_{i,j} + \alpha_{i,j} * (B_j - T_{r,j}) \quad (5)$$

$$S_{i,j} = T_{i,j} + \alpha_{i,j} * (T_{i,j} - T_{r,j}) \quad (6)$$

where,  $S_{i,j}$  represents the  $j^{th}$  vector of seed produced by  $i^{th}$  tree;  $T_{i,j}$  represents  $j^{th}$  vector of  $i^{th}$  tree;  $B_j$  represents the best tree location in the  $j^{th}$  vector;  $T_{r,j}$  represents the randomly selected  $r^{th}$  tree in  $j^{th}$  vector;  $\alpha$  is randomly generated scaling factor in range  $[-1,1]$  for  $i$  and  $r$  indices.

In TSA the exploration and exploitation rely on search tendency (ST), a controlling parameter in range  $[0,1]$ . The larger the value of ST, faster the convergence and provides the better exploitation. The smaller the value of ST, slower the convergence, and better the exploration. The initialization of location of trees is given by (7).

$$T_{i,j} = L_{j,\min} + r_{i,j} * (H_{j,\max} - L_{j,\min}) \quad (7)$$

where,  $L_{j,\min}$  and  $H_{j,\max}$  are lower and upper boundaries of search space;  $r_{i,j}$  is a randomly generated number in range  $[0,1]$ . The efficiency of exploitation also depends on the number of seeds. The range for number of seeds produced is 10% to 25% of number of trees. The termination criterion relies on the maximum number of iterations.

The flowchart of TSA for producing the optimal set of coefficients is given in Fig. 1.

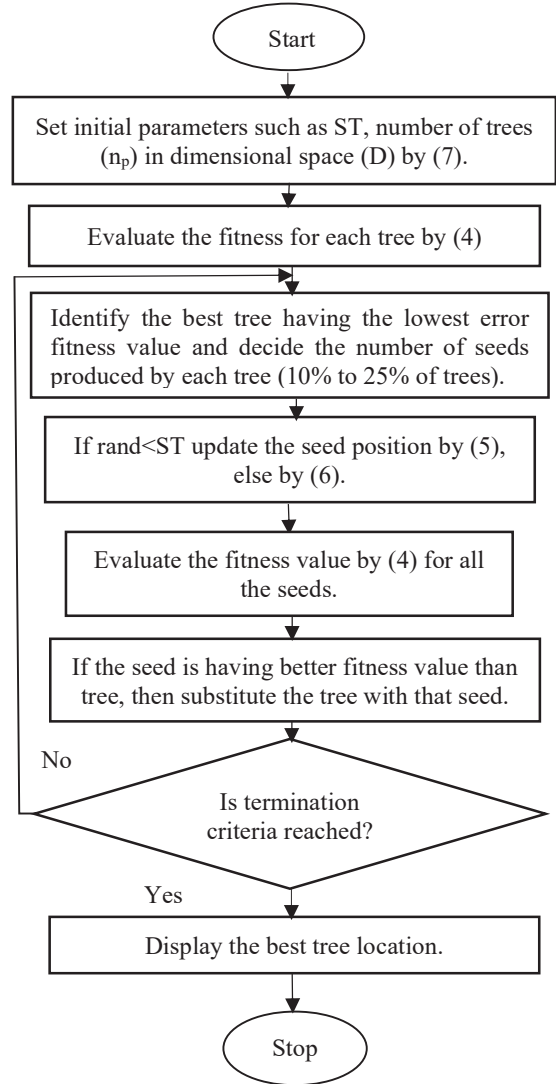


Fig. 1. Flowchart representing TSA for IIR filter design.

### IV. IIR FILTER IMPLEMENTATION

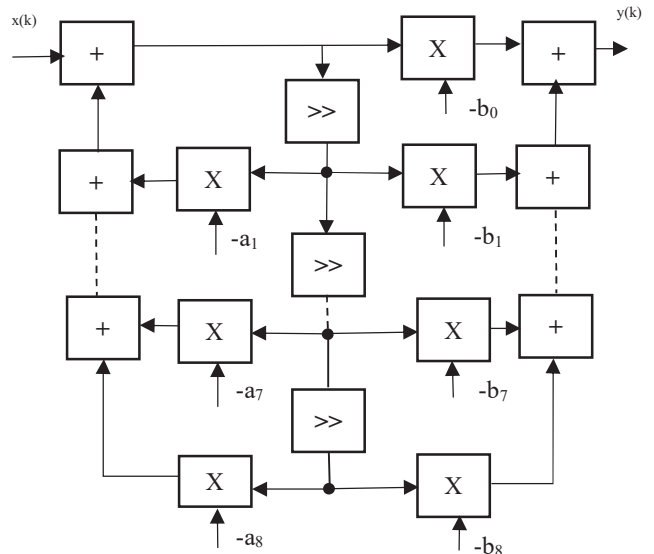


Fig. 2. Architecture of IIR filter.

The architecture of IIR filter implemented is shown in the Fig. 2. The filter is designed for order 8, with equal number of numerator and denominator coefficients.

## V. SIMULATION RESULTS

### a. Optimization of IIR BPF and BSF coefficients by TSA.

The TSA based optimally designed filter coefficients are obtained after 500 iterations. All the design parameters connected with algorithm and filter specifications are presented in Table I. This algorithm is executed on MATLAB 2017a version platform on Intel core i3 processor, 2.30GHz with 8GB RAM.

TABLE I. DESIGN PARAMETERS

Design parameters	Values
Number of trees (n)	25
Iteration cycle (iter <sub>max</sub> )	500
Search tendency (ST)	0.1
Dimensionality (D)	18
Upper limit of coefficients (d <sub>max</sub> )	+2
Lower limit of coefficients (d <sub>min</sub> )	-2
Stopband ripples (δ <sub>s</sub> )	0.001
Passband ripple (δ <sub>p</sub> )	0.01

In Table II and Table III, optimized coefficients approximated upto 5 decimal points of IIR BPF and BSF, respectively of order 8 are presented, with the optimal set of coefficients presented in Table II, for BPF is used to draw the magnitude response in dB and normalized magnitude response plots as shown in Figs. (3) – (4), respectively.

TABLE II. OPTIMALLY OBTAINED COEFFICIENTS BY TSA FOR BPF

Numerator coefficients (b <sub>k</sub> )	Denominator coefficients (a <sub>k</sub> )
b <sub>0</sub> = 0.00986	a <sub>0</sub> = 1.11071
b <sub>1</sub> = -0.07363	a <sub>1</sub> = 0.09074
b <sub>2</sub> = -0.07270	a <sub>2</sub> = 1.60576
b <sub>3</sub> = 0.11380	a <sub>3</sub> = -0.05861
b <sub>4</sub> = 0.15451	a <sub>4</sub> = 1.77204
b <sub>5</sub> = -0.10515	a <sub>5</sub> = 0.01578
b <sub>6</sub> = -0.15467	a <sub>6</sub> = 1.01974
b <sub>7</sub> = 0.02576	a <sub>7</sub> = 0.00229
b <sub>8</sub> = 0.08283	a <sub>8</sub> = 0.30200

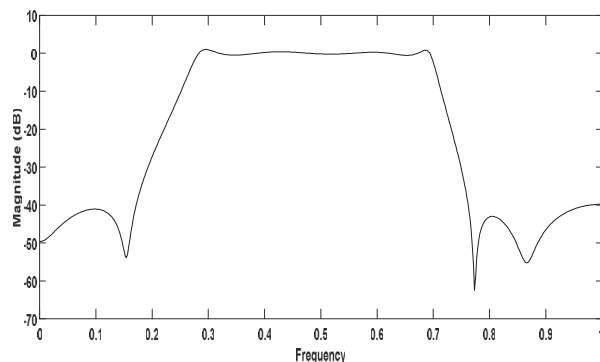


Fig. 3. Magnitude response (dB) plot of IIR BPF of order 8 designed by TSA.

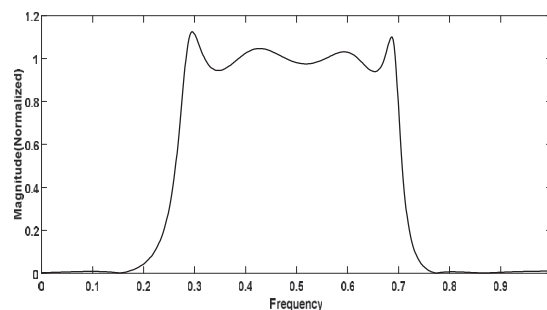


Fig. 4. Normalized magnitude response plot of IIR BPF of order 8 designed by TSA.

TABLE III. OPTIMALLY OBTAINED COEFFICIENTS BY TSA FOR BSF

Numerator coefficients (b <sub>k</sub> )	Denominator coefficients (a <sub>k</sub> )
b <sub>0</sub> = -0.23495	a <sub>0</sub> = -0.21851
b <sub>1</sub> = -0.00852	a <sub>1</sub> = -0.71535
b <sub>2</sub> = -0.87565	a <sub>2</sub> = 1.89002
b <sub>3</sub> = 0.11280	a <sub>3</sub> = 1.20077
b <sub>4</sub> = -1.3791	a <sub>4</sub> = 0.49315
b <sub>5</sub> = 0.19104	a <sub>5</sub> = -1.58091
b <sub>6</sub> = -1.15111	a <sub>6</sub> = 1.50957
b <sub>7</sub> = 0.09613	a <sub>7</sub> = 0.72490
b <sub>8</sub> = -0.45958	a <sub>8</sub> = 0.32883

Also, with the optimized coefficients presented in Table III, magnitude response plot in dB and normalized magnitude response plot are shown in Figs. (5) – (6) for BSF, respectively. From figures different performance metrics are calculated and presented in Table IV. Algorithm convergence plot for both the design problems are shown in Figs. (7) – (8) and the optimal solutions are obtained, those are ensured by these convergence plots.

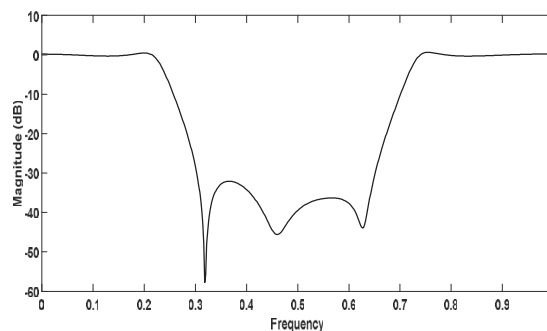


Fig. 5. Magnitude response (dB) plot of IIR BSF of order 8 designed by TSA.

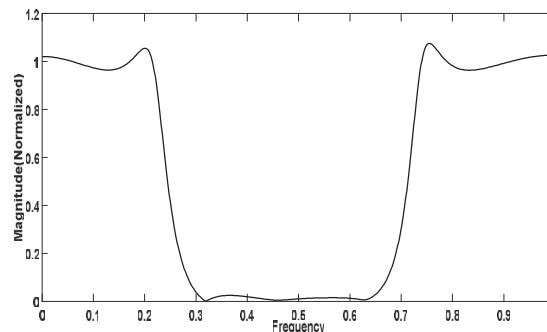


Fig. 6. Normalized magnitude response plot of IIR BSF of order 8 designed by TSA.

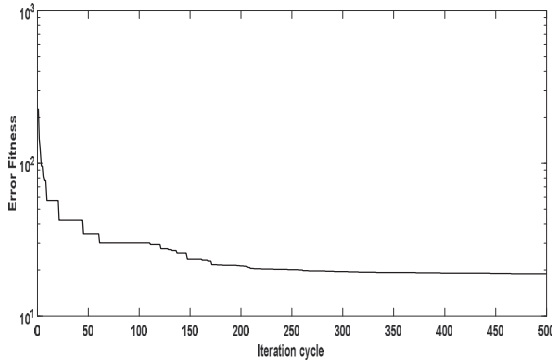


Fig. 7. Converging profile of TSA technique for 8<sup>th</sup> order IIR BPF design technique.

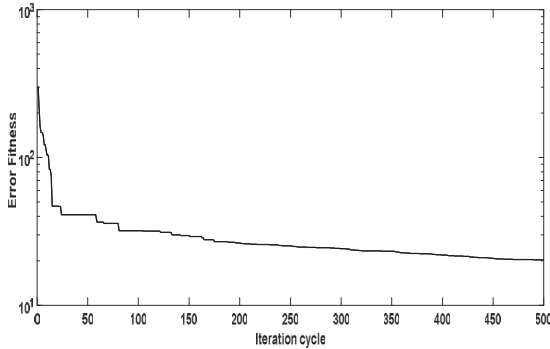


Fig. 8. Converging profile of TSA technique for 8<sup>th</sup> order IIR BSF design technique.

TABLE IV. ANALYSED DATA OF DESIGNED IIR BPF AND BSF.

Parameters	BPF	BSF
Maximum stop band attenuation (dB)	-42.99	-32.06
Maximum $\delta_p$	0.124	0.076
Maximum $\delta_s$	0.01025	0.02494
Average of $\delta_s$	0.00550215	0.0131145
Transition width	0.1289	0.1113

#### b. FPGA implementation of IIR BPF and BSF

IIR filter is realized in FPGA with the device name Vertex 7 with device name xc7vx330t-3ffg1157. The device utilization for the FPGA implementation of the IIR filter of order 8 are tabulated below.

TABLE V. DEVICE UTILIZATION FOR IIR BPF AND BSF.

Logic utilization	Used	Available	Utilization (%)
Look up tables (LUTs)	47	204000	0
Input output blocks (IOBs)	576	600	96
DSP48E1	106	1120	09

The optimal coefficients obtained are converted into the binary form, and the simulation response is done for the verilog HDL with the optimal coefficients. It has been observed that responses obtained from verilog HDL simulation study shown in Figs. (9) – (10) for BPF and BSF, respectively and the difference equation of the IIR filter are

same.

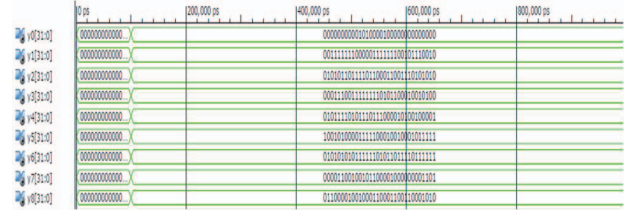


Fig. 9. Simulation response of the optimized coefficients for BPF IIR.

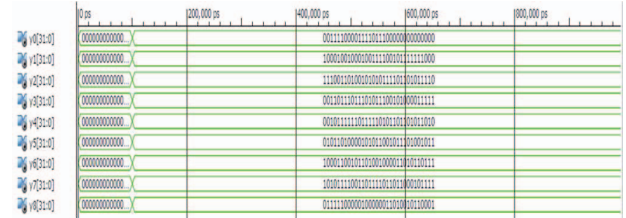


Fig. 10. Simulation response of the optimized coefficients for BSF IIR.

## VI. CONCLUSION

IIR BPF and BSF are designed by the optimization of coefficients using the TSA technique. This optimization technique attains the optimal solution in acceptable number of iterations and ensures the quality performance of the designed filter in terms of PBR, SBR, stop band attenuation and transition width. IIR filter is realized in the FPGA by Verilog HDL with the optimized coefficients.

## REFERENCES

- [1] Oppenheim, V. Alan, "Discrete-Time Signal Processing. Prentice-Hall," Englewood Cliffs, 1999.
- [2] Proakis, G. John, D. G. Manolakis, "Introduction to digital signal processing. Prentice-Hall," 1988.
- [3] S. A. Khan, "Digital design of signal processing systems a practical approach," John Wiley and Sons, 2011.
- [4] Antoniu, Andreas, "Digital Signal Processing: signals, systems and filters," McGraw Hill, 2006.
- [5] W. S. Lu, A. Antoniou, "Design of digital filters and filter banks by optimization: a state of the art review," European Signal Processing Conference," vol. 1, pp. 1-4, Finland, 2000.
- [6] N. Karaboga, B. Cetinkaya, "Design of minimum phase digital IIR filters by using Genetic algorithm," IEEE 6th Nordic Signal Processing Symposium, pp. 29-32, Finland, 2004.
- [7] S. Chen, R. Istepanian, B. L. Luk, "Digital IIR filter design using adaptive simulated annealing," Digital Signal Processing, vol. 11, no. 3, pp. 241-251, 2001.
- [8] S. K. Saha, S. Sarkar, R. Kar, D. Mandal, S. P. Ghoshal, "Digital stable IIR low pass filter optimization using particle swarm optimization with improved inertia weight," International Joint Conference on Computer Science and Software Engineering, pp. 147-152, Bangkok, 2012.
- [9] A. Kalinli, N. Karaboga, "Artificial immune algorithm for IIR filter design," Engineering Applications of Artificial Intelligence, vol. 18, no. 8, pp. 919-929, 2005.
- [10] N. Karaboga, A. Kalinli, D. Karaboga, "Designing digital IIR filter using ant colony optimization algorithm," Applications of Artificial Intelligence, vol. 17, no. 3, pp. 301-309, 2004.
- [11] S. K. Saha, R. Kar, D. Mandal, S. P. Ghosal, "Bacteria foraging optimization algorithm for optimal FIR filter design," International Journal Bio-Inspired Computation, vol. 5, no. 1, pp. 52-66, 2013.
- [12] C. Nayak, S. K. Saha, R. Kar, D. Mandal, "An efficient and robust digital fractional order differentiator based ECG pre-processor design for QRS detection," IEEE transactions on biomedical circuits and systems, vol. 13, no. 4, pp. 682-696, 2019.

- [13] M. S. Kiran, "TSA: Tree- seed algorithm for continuous optimization," *Expert Systems with Applications*, vol. 42, no. 19, pp. 6686-6698, 2015.
- [14] Z. M. Hussain, A. Z. Sadik, P. O'Shea, "Digital signal processing-an introduction with Matlab applications," Springer, 2011.
- [15] M. S. Kiran, "An implementation of tree-seed algorithm (TSA) for constrained optimization," *Intelligent and Evolutionary Systems*, pp. 189-197, Springer, 2016.
- [16] A. C. Cinar, M. S. Kiran, "Similarity and logic gate-based tree-seed algorithm for binary optimization," *Computers and Industrial Engineering*, vol. 115, pp. 631-646, 2018.
- [17] Z. Gao, X. Zeng, J. Wang, J. Liu, "FPGA implementation of adaptive IIR filters with particle swarm optimization algorithm," *IEEE International Conference on Communication Systems*, pp. 1364-1367, Singapore, 2008.
- [18] M. A. Eshtawie, M. Othman, "FPGA implementation of an optimized coefficients pulse shaping FIR filters," *IEEE International Conference on Semiconductor Electronics*, pp. 454-458, Kuala Lumpur, 2006.
- [19] Gang Li, M. Gevers, Y. Sun, "Performance analysis of a new structure for digital filter implementation," *IEEE Transactions on Circuits and Systems I: Fundamental Theory and Applications*, vol. 47, no. 4, pp. 474-482, 2000.
- [20] T. Dhaware, V. Nichante, G. Morankar, "Survey paper on pipelining in IIR and FIR filter," *International Journal of Research in Engineering, Social Sciences*, vol. 5, no. 1, pp. 12-17, 2015.
- [21] X. Yao, Y. Liu, G. Lin, "Evolutionary programming made faster," *IEEE Transactions on Evolutionary computation*, vol. 3, no. 2, pp. 82-102, 1999.