

# Ultra-Wideband 3-D Microwave Absorbers With Composite Slotlines and Microstrip Lines: Synthetic Design and Implementation

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**ABSTRACT** This article proposes a class of ultra-wideband 3-D microwave absorbers with composite slotlines and microstrip lines from synthetic design to practical implementation. Firstly, the general equivalent transmission line (TL) model of the proposed 3-D absorber element is formed based on two sets of shunt short-ended stubs and an  $i$ -section nonuniform connecting line. Then, the synthetic procedure is theoretically investigated using the equivalent TL model, aiming to construct an ultra-wide absorption band with the Chebyshev equal-ripple response. According to the prescribed absorptive performance, such as maximum reflection coefficient ( $\Gamma$ ) and fractional bandwidth (FBW), the relevant parameters of the TL model can be directly calculated by the established synthesis approach. To validate the proposed concept, two prototypes, namely, absorber-I ( $i = 1$ ) and absorber-II ( $i = 2$ ), are designed, fabricated, and measured. Each prototype element applies a simple 3-D structure composed of slotlines, microstrip lines, and only one absorptive load, which are all etched on a single-layered substrate. Measured results agree well with synthetizations and simulations. For absorber-I, the measured bandwidth of 95.5% in a frequency range from 5.08 to 14.44GHz is successfully realized. Absorber-II obtains a measured FBW of 111.1% in a range from 4.48 to 15.68GHz. Average absorption ratios within the operating band are higher than 95.5% and 93.8% for absorber-I and absorber-II, respectively. Besides, the proposed 3-D absorbers are angularly stable within 60° oblique incidence. Therefore, such ultra-wideband 3-D microwave absorbers with simple structures possess the attractive potential for effectively absorbing electromagnetic waves.

**INDEX TERMS** 3-D microwave absorber, equivalent transmission line model, synthetic design, ultra-wideband absorber.

## I. INTRODUCTION

MICROWAVE absorbers have been widely used in varieties of applications for electromagnetic (EM) manipulations, such as antenna design, radar camouflage, electromagnetic compatibility (EMC), or measurement system [1]. With the rapid development of modern wireless systems, wider absorption bands are highly demanded in absorber designs for the complicated EM environment.

Conventional two-dimensional (2-D) absorbers, such as Dallenbache layer and Salisbury screen, were obtained based on a lossy dielectric or resistive screen [2], [3]. In order to realize a wider absorptive band, multilayer resistive screens

were employed in the Jaumann absorber [4]. For further improvement of the operating bandwidth, different materials were introduced into absorber designs [5], [6], [7], [8], [9], [10], [11], [12]. The ferrite backed with a conducting plate in [5] is applied to design a perfect absorber at the operating frequency. In [6], wideband absorbers with a single-layer substrate were explored utilizing periodic square resistive patches. To design a bandwidth-tunable absorber, graphene sheets were used in [7] to dynamically tune the surface impedance. In [8], the frequency-dispersive magnetic material was employed to obtain an ultrathin absorber with increased bandwidth. To design a wideband

polarization-insensitive multilayered absorber, the resistive ink was utilized in [9] for periodic resistive patterns. In [10], the ultra-wideband water-based microwave absorber was reported with angle and temperature stability. Using sustainable waste biomass, a simple and economical structural absorber was presented in [11] with enhanced absorption performance. In [12], an all-dielectric ultra-wideband absorber was realized using a resin shell and saline structure.

Another popular approach to designing wideband absorbers is loading lumped resistors in a circuit analog way [13], [14], [15], [16], [17]. In [13], a wideband single-layer absorber was designed by utilizing double-square-loop array loading with lumped resistors. Using slot arrays loaded with resistors, a switchable low-profile wideband absorber/absorber was presented in [14]. In [15], chip-resistors were embedded into metallic strips to realize a wideband absorber under multimode operation. For the design of an active absorber with ultrawide bandwidth and extremely low profile, non-foster devices and resistors were employed in [16]. In [17], an active tunable absorber was presented to obtain the ultrawide bandwidth.

Apart from the 2-D microwave absorbers mentioned above, the class of 3-D absorbers, which is based on the 2-D periodic structure of transmission lines, has been attracting considerable interest recently [18], [19], [20], [21], [22], [23], [24], [25], [26], [27], [28], [29], [30], [31], [32]. Based on a 2-D array of microstrip lines, the authors in [18] proposed the modeling and design of a wideband circuit analog absorber. In [19] and [20], the concept of 3-D frequency selective absorbers was presented with wide absorption bandwidths. Based on resistor-loaded strip lines, different 3-D absorptive structures were realized in [21], [22], [23], [24] for wideband performance. In [25] and [26], the honeycomb structure was employed to obtain wide bandwidths with reduced weight. To realize a 3-D frequency-selective absorber with wide absorption bandwidth, the multilayer structure and magnetic ferrite were utilized in [27]. Combining the ferrite and a slow wave structure, the absorber in [28] realized the wide absorption band and the ultrathin profile. In [29], the bistatic radar cross section reduction was obtained via introducing the spoof surface plasmon polariton (SSPP) structure into the absorber design. By controlling multiple resistive electric and magnetic resonances, a low-profile wideband microwave absorber was presented in [30]. In [31], the via-based hybrid metal-graphene metamaterial was employed to realize a wideband absorber with miniaturized periodicity. Using the cascaded multi-layered planar magnetic absorber, the absorptive transmission structure in [32] realized an extended absorption band.

In this article, we try to propose the synthetic design and implementation of a class of ultra-wideband 3-D microwave absorbers with composite slotlines and microstrip lines. Firstly, we construct the general equivalent transmission line (TL) model of the proposed 3-D absorber element based on two sets of shunt short-ended stubs and an  $i$ -section nonuniform connecting line. The equivalent model is

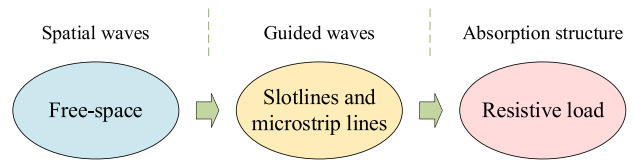


FIGURE 1. Working strategy of the proposed 3-D absorber.

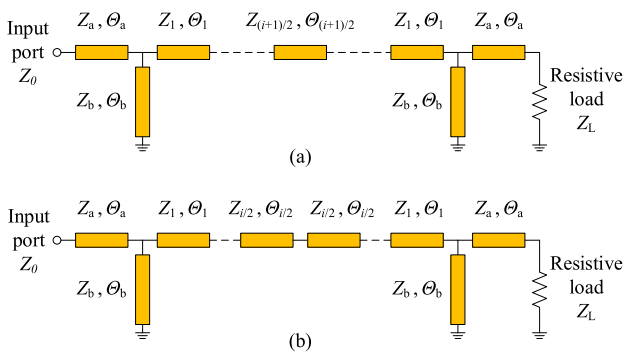
then utilized for the theoretical synthetic procedure, which aims to establish an ultrawide absorption band with the Chebyshev equal-ripple response. Using the above synthesis approach, the relevant parameters of the TL model can be directly calculated according to the specifications of absorptive performance, such as maximum reflection coefficient ( $\Gamma$ ) and fractional bandwidth (FBW). To prove our presented concept, two prototypes, namely, absorber-I ( $i = 1$ ) and absorber-II ( $i = 2$ ), are designed, fabricated, and measured. For each prototype element, a single-layered substrate is employed to obtain the very simple 3-D structure, which consists of slotlines, microstrip lines, and only one absorptive load. Measured results agree well with synthetizations and simulations. As for absorber-I, the measured (simulated) bandwidth of 95.5% in a frequency range from 5.08 to 14.44GHz (94.9% from 5.18 to 14.54GHz) is successfully realized. Absorber-II realizes a measured (simulated) bandwidth of 111.1% in a range from 4.48 to 15.68GHz (112.2% from 4.37 to 15.54GHz). Within the operating band, measured average absorption ratios (ARs) for absorber-I and absorber-II are higher than 95.5% and 93.8%, respectively. In addition, the proposed 3-D absorbers possess angular stability within  $60^\circ$  oblique incidence. Therefore, such ultra-wideband 3-D microwave absorbers with simple structures own their potential for EM waves absorption.

The remainder of this article is organized as follows. In Section II, the operation principle of the proposed 3-D absorber element is investigated, including the working strategy, the equivalent TL model, and the synthetic procedure. Section III details the implementation and measurement of two prototypes for validating the proposed concept. Finally, the conclusion is briefly presented in Section IV.

## II. OPERATION PRINCIPLE

Fig. 1 conceptually describes the working strategy of the proposed 3-D absorber. The incoming spatial waves from free-space impinge on the proposed 3-D absorber and then are effectively converted into the guided waves at the interface. After that, the guided waves propagate along the transmission lines, such as slotlines and microstrip lines. Finally, the guided waves are fully absorbed by a resistive load. Under this condition, the keys to obtain the proposed ultra-wideband absorber are establishing a symmetric equivalent model and realizing a 3-D structure.

Fig. 2 depicts the equivalent TL model of the proposed 3-D absorber element, which is mainly composed of two



**FIGURE 2.** Equivalent transmission line model of the proposed 3-D absorber element based on shunt short-ended stubs and an  $i$ -section nonuniform connecting line. (a)  $i$  is odd-integer (1, 3, 5, ...). (b)  $i$  is even-integer (0, 2, 4, ...).

sets of shunt short-ended stubs and an  $i$ -section nonuniform connecting line. It is shown in Fig. 2(a) and Fig. 2(b) for the odd- and even-integer  $i$ , respectively. The characteristic impedances and electrical lengths of each TL are  $Z_m$  and  $\Theta_m$  ( $m = a, b, 1, 2, 3, \dots$ ). In this work, all TLs are set with the same electrical length of  $\lambda/4$  at the center frequency in the desired operating band. Besides, the input spatial wave impedance  $Z_0$  is equal to the terminal absorptive load  $Z_L$ , which results in the equivalent TL model being horizontally symmetrical. It is worth noting that the output port is replaced by an absorptive resistor, thus the characteristic function of the equivalent model can be used to evaluate the absorptive performances.

For the universality, two examples ( $i = 1$  and  $i = 2$ ) are illustrated using the synthetic procedure similar to [33], [34]. As for to  $i = 1$ , the characteristic function of the equivalent TL model is derived as

$$F^I = j \left( k_1 \frac{\cos^4 \theta}{\sin \theta} + k_2 \frac{\cos^2 \theta}{\sin \theta} + k_3 \frac{1}{\sin \theta} \right) \quad (1)$$

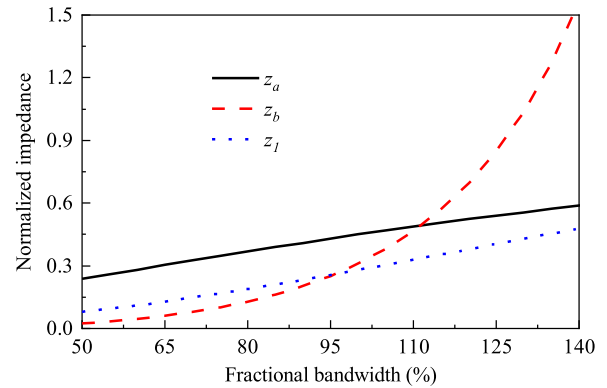
The coefficients of  $k_1$ ,  $k_2$ , and  $k_3$  are given by (A-1) in the Appendix. In this work, all the characteristic impedances are normalized with respect to  $Z_0$ , that is  $z_m = Z_m/Z_0$  ( $m = a, b, 1, 2, 3, \dots$ ).

When  $i = 2$ , the characteristic function can be calculated using the same synthesis approach as

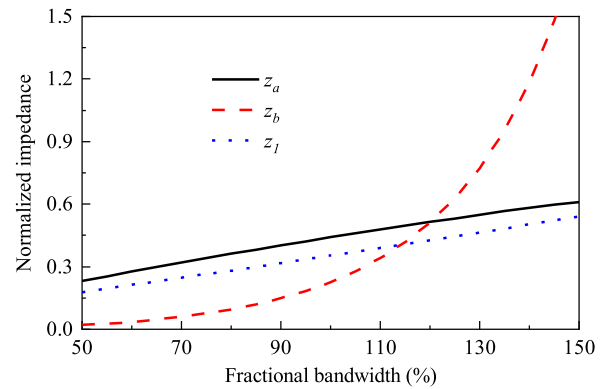
$$F^{II} = j \left( l_1 \frac{\cos^5 \theta}{\sin \theta} + l_2 \frac{\cos^3 \theta}{\sin \theta} + l_3 \frac{\cos \theta}{\sin \theta} \right) \quad (2)$$

The coefficients of  $l_1$ ,  $l_2$ , and  $l_3$  are given by (A-2) in the Appendix. By equalizing the coefficients  $k_1$ – $k_3$ ,  $l_1$ – $l_3$ , and the corresponding coefficients of the Chebyshev function, the normalized characteristic impedances can be explicitly determined by the specified absorptive performance.

To provide more design selection for ultra-wideband absorbers, Fig. 3 shows normalized characteristic impedances of  $z_a$ ,  $z_b$ , and  $z_1$  with respect to different fractional bandwidths under  $\Gamma = -10\text{dB}$  when  $i = 1$ . The normalized characteristic impedances under  $i = 2$  for  $\Gamma = -10\text{dB}$  are shown in Fig. 4. All impedances



**FIGURE 3.** Normalized characteristic impedances of  $z_a$ ,  $z_b$ , and  $z_1$  for different fractional bandwidths under  $\Gamma = -10\text{dB}$  when  $i = 1$ .



**FIGURE 4.** Normalized characteristic impedances of  $z_a$ ,  $z_b$ , and  $z_1$  for different fractional bandwidths under  $\Gamma = -10\text{dB}$  when  $i = 2$ .

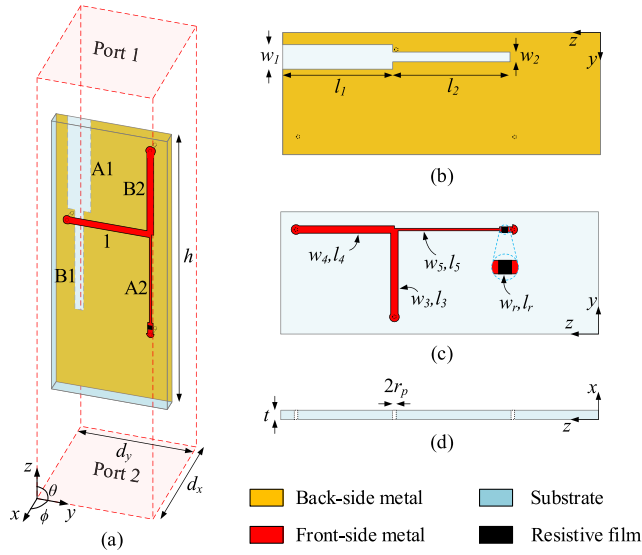
demonstrate similar increasing trends with the rise of the fractional bandwidth. From these theoretical results, it is clear that the proposed equivalent TL model can be employed to directly design ultra-wideband microwave absorbers using the above synthesis approach.

### III. IMPLEMENTATION AND VERIFICATION

To verify the proposed concept, two prototype examples of absorber-I and absorber-II are illustrated in this section from element design to array implementation.

#### A. ABSORBER-I

Fig. 5 shows the element configuration of the proposed 3-D absorber-I ( $i = 1$ ), where slotlines, microstrip lines, and one absorptive load are etched on a single-layered substrate. In this work, the resistive film from Omega (3770hm/square) is employed to form the absorptive load. The FR4 substrate with a relative permittivity of 4.4 and a dielectric loss tangent of 0.0166 is used for our design. To better clarify the relationship between the structural design and the equivalent model, each section of transmission lines is highlighted with corresponding marks. As seen in Fig. 5(b), two sections of the slotline are designed on the backside ground, resulting in the conversion from y-polarized spatial waves in free space to guided waves in the slotline. The first section of slotline

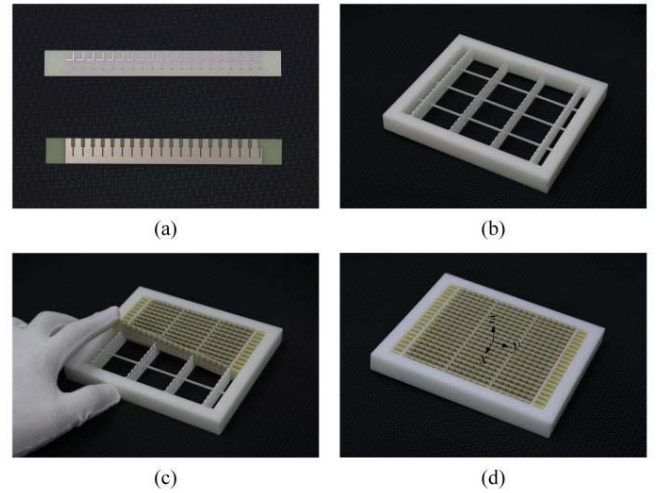


**FIGURE 5.** Element geometry of the proposed 3-D absorber-I. (a) Perspective view. (b) Back view. (c) Front view. (d) Side view.

$A1 (w_1, l_1)$  represents the first TL ( $Z_a, \Theta_a$ ) in the equivalent model. The short-circuited slotline  $B1 (w_2, l_2)$  denotes the first shunt short-ended stubs ( $Z_b, \Theta_b$ ). In Fig. 5(c), three sections of the microstrip line are etched on the front side and grounded through three shorting pins. Among them, the first section of microstrip line 1 ( $w_3, l_3$ ) not only acts as the connecting line ( $Z_1, \Theta_1$ ), but also transmits the guided wave from slotlines to microstrip lines. The microstrip line  $B2$  with a size of ( $w_4, l_4$ ) is the second shunt short-ended stub ( $Z_b, \Theta_b$ ). The third section of microstrip line  $A2 (w_5, l_5)$  represents the last TL ( $Z_a, \Theta_a$ ) in the equivalent model. In this geometry, only the  $y$ -polarized wave is supportable owing to the 3-D structure with one piece of the substrate. To overcome this polarization sensitivity, the proposed single-polarized design can be extended to a dual-polarized version by simply employing the cross-inserted structure.

Using the synthesis approach in Section II, the normalized characteristic impedances can be calculated as  $z_a = 0.45$ ,  $z_b = 0.31$ , and  $z_1 = 0.28$  with the prescribed absorptive performances of  $\Gamma = -10\text{dB}$ ,  $\text{FBW} = 100\%$ . For absorber-I, the input impedance is set as  $Z_0 = 377\Omega$ , which is related to the element distance along the  $x$  and  $y$  directions. The width and length of each slotline can be obtained by simulating an individual slotline in a periodic element for the desired characteristic impedance and electrical length. The sizes of microstrip lines are easily attained from the microstrip line calculator. To minimize unwanted discontinuities, the size of the resistive film is designed to be as small as possible under the limitation of manufacturing accuracy. The optimized geometrical parameters are determined based on the above results and then shown in Table 1.

Fig. 6 describes photographs of the proposed 3-D absorber-I with detailed fabrication stages. It can be observed in Fig. 6(a) that each set of 20 elements is printed on a long piece of substrate. In addition, the substrate is extended by



**FIGURE 6.** Photographs of the proposed 3-D absorber-I. (a) Substrate pieces. (b) 3-D printed fixing structure. (c) Fabrication procedure. (d) Final prototype.

**TABLE 1.** Geometrical parameters of the proposed 3-D absorber-I.

Parameter	$d_x$	$d_y$	$h$	$t$	$w_1$	$l_1$
Value (mm)	5	5	13	1.5	2	4.5
Parameter	$w_2$	$l_2$	$w_3$	$l_3$	$w_4$	$l_4$
Value (mm)	0.6	4.8	0.47	3.58	0.47	4.03
Parameter	$w_5$	$l_5$	$w_r$	$l_r$	$r_p$	
Value (mm)	0.1	4.3	0.22	0.22	0.1	

10mm at two edges without etching metal to provide the convenience of fixation. The total size of the substrate for absorber-I is  $120\text{mm} \times 13\text{mm}$ . As shown in Fig. 6(b), a 3-D printed fixing structure is designed with the photosensitive resin material to realize structural stability and accuracy. Fig. 6(c) shows the fabrication procedure, where each substrate is inserted into securing slots for the proper spacing of the element. After that, the fabricated prototype with  $20 \times 20$  elements is shown in Fig. 6(d).

To test the reflection coefficient and transmission coefficient of the prototype, the measurement system is set up as shown in Fig. 7. The transmitting antenna (Tx) and receiving antenna (Rx) are set at fixed places, where the distances between the prototype and two antennas are  $d^i$  and  $d^r$ , respectively. During the measurement, the distances of  $d^i$  and  $d^r$  are both selected as 1.5m to meet the far-field condition [35]. To further minimize the error in measurement, the calibration method in [36] is applied. By changing the positions of two antennas, this measurement system can work for different incident angles.

Fig. 8 illustrates the synthetizations, simulations, and measurements of the proposed 3-D absorber-I under normal incidence. The synthesized results are obtained based on the equivalent TL model using the synthesis approach in Section II. For the simulation, periodic boundary conditions and floquet ports are employed to obtain an infinite



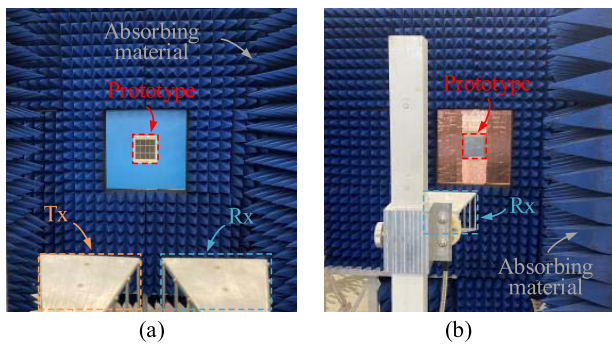


FIGURE 7. Photographs of testing set-up. (a) Reflection coefficient measurement. (b) Transmission coefficient measurement.

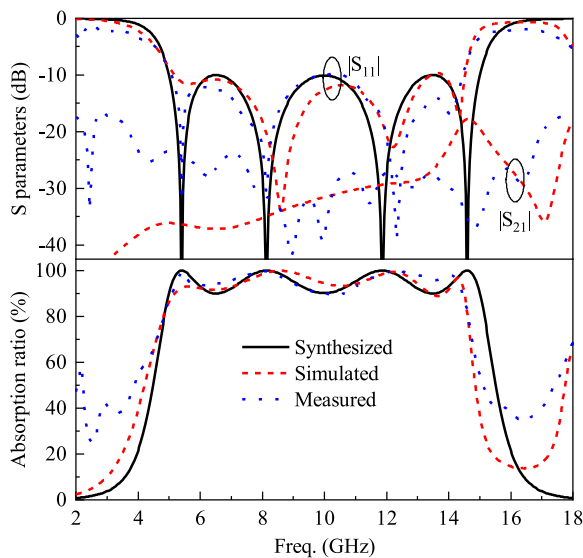


FIGURE 8. Synthesized, simulated and measured results of the proposed 3-D absorber-I under normal incidence.

array structure. Different from the ideal equivalent model, not all the spatial wave can be perfectly converted into guided waves. Here, the input spatial wave is provided by the upper floquet port (port 1) while the underside floquet port (port 2) is utilized to detect the undesired leaked spatial wave. The measured results are from the finite-sized prototype. As observed, synthesizations, simulations, and measurements are in good agreement within the operating band. The differences between measurements and simulations are mainly due to: 1) the larger loss of the actual substrate, and 2) unavoidable errors during the measurement, such as the introduction of the fixer, the accuracy of the manual testing system, and the deviation of calibration processing.

The simulated and measured FBWs are 94.9% (from 5.18 to 14.54GHz) and 95.5% (from 5.08 to 14.44GHz), respectively. Within the operating band, the  $S_{21}$  for simulation and measurement are less than  $-17.8\text{dB}$  and  $-23.5\text{dB}$ . The simulated and measured average in-band absorption ratios are higher than 95.0% and 95.5%. Here, the absorption ratio is

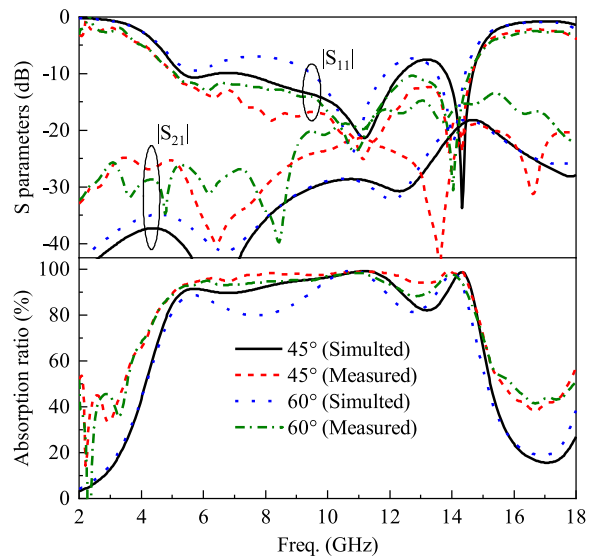


FIGURE 9. Simulated and measured results of the proposed 3-D absorber-I under oblique incidence at YOZ plane.

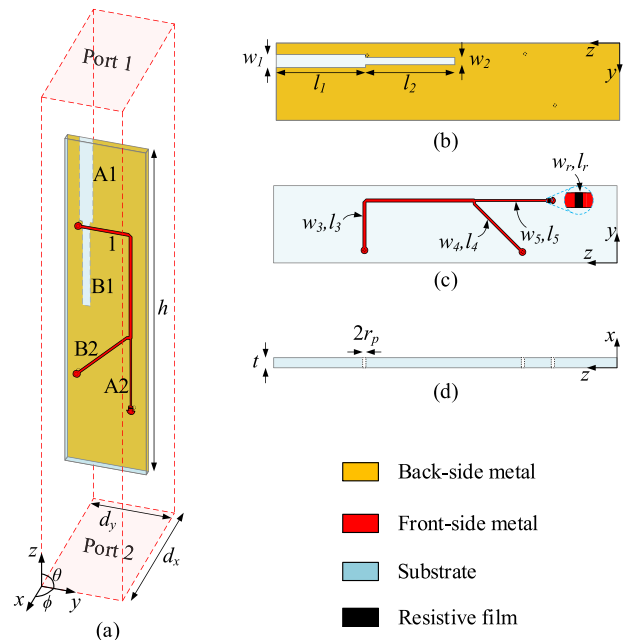


FIGURE 10. Element geometry of the proposed 3-D absorber-II. (a) Perspective view. (b) Back view. (c) Front view. (d) Side view.

calculated by

$$\text{Absorption ratio} = \sqrt{1 - |S_{11}|^2 - |S_{21}|^2} \quad (3)$$

The simulated and measured results of the proposed 3-D absorber-I under oblique incidence at YOZ plane are further comparatively investigated and described in Fig. 9. It can be seen that measured results agree well with simulations. Under the condition of  $45^\circ$  oblique incidence, the simulated and measured 80% absorption ratio bandwidths are 101.4% (from 4.84 to 14.8GHz) and 107.1% (from 4.48 to 14.8GHz).

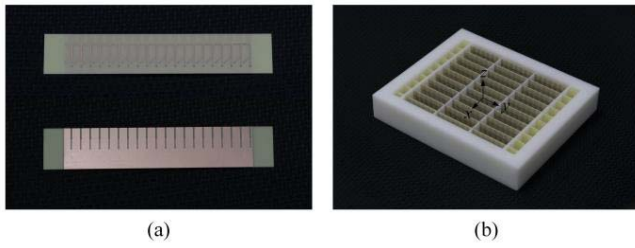


FIGURE 11. Photographs of the proposed 3-D absorber-II. (a) Substrate pieces. (b) Final prototype.

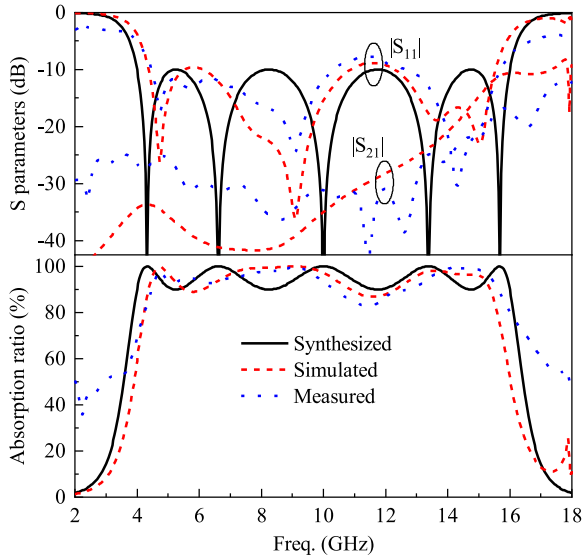


FIGURE 12. Synthesized, simulated and measured results of the proposed 3-D absorber-II under normal incidence.

TABLE 2. Geometrical parameters of the proposed 3-D absorber-II.

Parameter	$d_x$	$d_y$	$h$	$t$	$w_1$	$l_1$
Value (mm)	9	4.5	20	0.5	0.75	5.2
Parameter	$w_2$	$l_2$	$w_3$	$l_3$	$w_4$	$l_4$
Value (mm)	0.43	5.2	0.18	9.3	0.14	4.2
Parameter	$w_5$	$l_5$	$w_r$	$l_r$	$r_p$	
Value (mm)	0.12	4.2	0.22	0.11	0.1	

For 60° oblique incidence, the 80% absorption ratio bandwidths of 98.7% (from 4.96 to 14.6GHz) and 106.2% (from 4.52 to 14.76GHz) are still well obtained for simulations and measurements. These results clearly exhibit that using the structure of composite slotlines and microstrip lines, the proposed absorber-I indeed realizes an ultra-wideband absorptive performance under a large variety of incident angles.

**B. ABSORBER-II**

Fig. 10 shows the element configuration of the proposed 3-D absorber-II ( $i = 2$ ), which is similar to that of absorber-I. With the desired absorptive performances of  $\Gamma = -10$ dB,

TABLE 3. Comparisons of the proposed 3-D absorber-I ( $i = 1$ ).

	Synthesis	Simulation	Measurement
-10dB lower cutoff frequency	5GHz	5.18GHz	5.08GHz
Maximum in-band transmission coefficient	-	-17.8dB	-23.5dB
Average in-band absorption ratio	94.9%	95.0%	95.5%
-10dB upper cutoff frequency	15GHz	14.54GHz	14.44GHz

TABLE 4. Comparisons of the proposed 3-D absorber-II ( $i = 2$ ).

	Synthesis	Simulation	Measurement
-10dB lower cutoff frequency	4GHz	4.37GHz	4.48GHz
Maximum in-band transmission coefficient	-	-11.6dB	-16.9dB
Average in-band absorption ratio	94.9%	94.8%	93.8%
-10dB upper cutoff frequency	16GHz	15.54GHz	15.68GHz

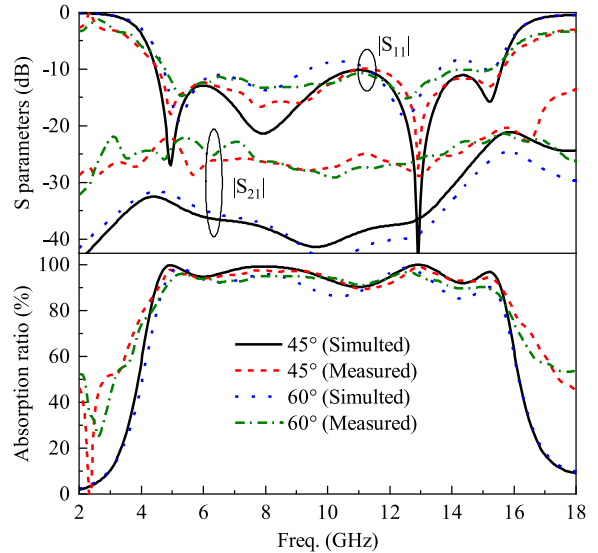


FIGURE 13. Simulated and measured results of the proposed 3-D absorber-II under oblique incidence at YOZ plane.

FBW = 120%, the normalized characteristic impedances are calculated as  $z_a = 0.52$ ,  $z_b = 0.51$ , and  $z_1 = 0.43$ . Here, the input impedance is set as  $Z_0 = 188\Omega$ . Table 2 tabulates the detailed geometrical parameters.

The detailed photographs of the proposed 3-D absorber-II are shown in Fig. 11. As can be seen in Fig. 11(a), each set of 20 elements is printed on a long piece of substrate. The total size of the substrate for absorber-II is 110mm×20mm. In Fig. 11(b), by inserting the substrate into securing slots, the fabricated prototype with 10 × 20 elements is completed.

Fig. 12 shows the synthetizations, simulations, and measurements of the proposed 3-D absorber-II under normal incidence. As seen, measurements agree well again with synthetizations and simulations. The simulated and measured

**TABLE 5.** Comparisons between the proposed design and other reported 3-D absorbers.

Ref.	Absorption bandwidth	Angular stability	Design method	No. of substrate	No. of resistive load	Thickness ( $\lambda_L$ )
[19]	63.8% (4.8GHz~9.3GHz)	40° (90%) (Only simulated)	Equivalent circuit model	3	1	0.31
[24]	156.6% (1.5GHz~12.31GHz)	45° (Only simulated)	Equivalent circuit model	6	4	0.1
[29]	85.8% (6.95GHz~17.4GHz)	65° (AR>80%)	Optimize the SSPP structure	4	18	0.18
[30]	59.3% (2.11GHz~3.89GHz)	60° (AR>80%) (Only simulated)	Multiple resistive resonances control	5	8	0.09
<b>Prop. Absorber-I</b>	<b>95.5%</b> <b>(5.08GHz~14.44GHz)</b>	<b>60° (AR&gt;80%)</b>	<b>Synthetic design based on Equivalent TL model</b>	<b>1</b>	<b>1</b>	<b>0.22</b>
<b>Prop. Absorber-II</b>	<b>111.1%</b> <b>(4.48GHz~15.68GHz)</b>	<b>60° (AR&gt;80%)</b>	<b>Synthetic design based on Equivalent TL model</b>	<b>1</b>	<b>1</b>	<b>0.29</b>

$\lambda_L$  is the wavelength at the lowest frequency in free space.

FBWs are 112.2% (from 4.37 to 15.54GHz) and 111.1% (from 4.48 to 15.68GHz), respectively. The simulated and measured  $S_{21}$  magnitudes within the operating band are less than  $-11.6$ dB and  $-16.9$ dB. The simulations and measurements of average in-band absorption ratios are higher than 94.8% and 93.8%.

Fig. 13 describes the simulated and measured results of the proposed 3-D absorber-II under oblique incidence at YOZ plane. Good agreement can be observed between measured and simulated results. For the 45° oblique incidence, the 80% absorption ratio bandwidths of 113.9% (from 4.32 to 15.76GHz) and 117.9% (from 4.12 to 15.96GHz) are realized for simulations and measurements. In the case of 60° oblique incidence, the simulated and measured 80% absorption ratio bandwidths are 110.3% (from 4.52 to 15.64GHz) and 112.9% (from 4.4 to 15.8GHz). These results indicate that the ultra-wideband absorptive performance can be successfully obtained by the proposed absorber-II under not only normal incidence, but also oblique incidence.

As a brief summary, two prototypes of absorber-I and absorber-II have been theoretically designed and practically implemented. Table 3 and Table 4 illustrate the comparisons for these two absorbers, showing that the input spatial wave can be effectively absorbed by using the proposed structures. The realized absorptive performances are very close to the expectation, which obviously proves the proposed design

concept. Table 5 shows the comparisons between our designs and other reported 3-D absorbers. It can be figured out that the proposed 3-D absorbers can be quickly designed using the presented equivalent TL model and synthesis approach, which leads to the ultra-wideband absorptive performance with a single-layered substrate and only one resistive load along a single absorber element. It should be noted that the proposed absorbers in this work are not placed above a metal plate. Considering the practical scenario where a metal object is presented behind the absorber, the proposed design can keep absorptive performances almost unchanged. This applicability can be attributed to the effectiveness of conversion from spatial waves to guided waves and absorption from the loaded resistor.

#### IV. CONCLUSION

In this article, the class of ultra-wideband 3-D microwave absorbers has been presented with synthetic design and practical implementation. Based on the equivalent transmission line model, the synthetic procedure of the proposed absorber element is theoretically investigated and executed, so as to explicitly establish the relationship between specific absorptive performance and network parameters. To validate the proposed concept, two prototypes with a simple 3-D structure composed of composite slotlines and microstrip lines are designed, fabricated, and tested. Measurements agree

$$\begin{cases} k_1 = \frac{-(z_a+1)(z_a-1)[(z_b+z_1)z_a+z_bz_1]}{2z_a^2z_b^2z_1} \\ k_2 = \frac{[-(-z_1^2-2z_bz_1-2z_b^2)z_a^4+2z_a^3z_bz_1(z_b+z_1)+z_a^2z_b^2(z_1^2-1)-2z_az_bz_1(z_b+z_1)-2z_b^2z_1^2]}{2z_a^2z_b^2z_1} \\ k_3 = \frac{-z_a^4z_b^2+z_b^2z_1^2}{2z_a^2z_b^2z_1} \end{cases} \quad (\text{A-1})$$

$$\begin{cases} l_1 = \frac{-(z_a+1)(z_a-1)[(z_b+z_1)z_a+z_bz_1]^2}{z_a^2z_b^2z_1} \\ l_2 = \frac{[(2z_b+z_1)z_a^3+z_a^2z_bz_1-z_az_b-2z_bz_1][(z_b+z_1)z_a+z_bz_1]}{z_a^2z_b^2z_1} \\ l_3 = \frac{z_b[(-z_b-z_1)z_a^4-z_a^3z_bz_1+z_az_bz_1+z_bz_1^2]}{z_a^2z_b^2z_1} \end{cases} \quad (\text{A-2})$$

well with synthesized and simulated results, showing the ultra-wideband absorptive performance under a large variety of incident angles. Therefore, it is our belief that such 3-D microwave absorbers possess the attractive potential for EM waves absorption.

## APPENDIX

The coefficients of  $k_1$ – $k_3$  and  $l_1$ – $l_3$  are given in (A-1) and (A-2), respectively, at the bottom of the previous page.

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