Perfect Matching of Reactive Loads Through Complex Frequencies: From Circuital Analysis to Experiments

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*Abstract***— The experimental evidence of purely reactive loads impedance matching is here provided by exploiting the special scattering response under complex excitations. The study starts with a theoretical analysis of the reflection properties of an arbitrary reactive load and identifies the proper excitation able to transform the purely reactive load into a virtual resistive load during the time the signal is applied. To minimize reflections between the load and the transmission line, the excitation must have a complex frequency, leading to a propagating signal with a tailored temporal envelope. The aim of this work is to design and, for the first time, experimentally demonstrate this anomalous scattering behavior in microwave circuits, showing that the time-modulated signals can be exploited as a new degree of freedom for achieving impedance matching without introducing neither a matching network nor resistive elements that are typically used for ensuring power dissipation and, thus, zero reflection. The proposed matching strategy does not alter the reactive load that is still lossless, enabling an anomalous termination condition where the energy is not dissipated nor reflected but indefinitely accumulated in the reactive load. The stored energy leaks out the load as soon as the applied signal changes or stops.**

*Index Terms***— Complex frequency, impedance matching, time modulation, virtual perfect absorption, zero scattering.**

I. INTRODUCTION

IMPEDANCE matching is one of the fundamental concepts
in microwave circuit theory, allowing the maximum energy MPEDANCE matching is one of the fundamental concepts transfer to a load by canceling reflections at its terminals [1], [2]. Impedance matching is invoked when the impedances of the feeding transmission line Z_0 and the load Z_L do not satisfy the condition $Z_L = Z_0$, provided that the generator internal impedance equals the input impedance of the feeding transmission line connected to the load. Without impedance matching, reflections occur inevitably at the terminals where the impedance discontinuity takes place for ensuring the continuity of the physical quantities involved in the signal propagation, i.e., voltages and currents, along the transmission

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Fig. 1. Schematic representation of the impedance matching techniques: impedance transformation through (a) matching network, (b) temporal modulation of load, and (c) temporal modulation of the excitation signal.

 (b)

line. To avoid such undesired reflections, in the last century, several impedance matching techniques have been developed, which are based on the concept of impedance transformation, i.e., adding a properly designed microwave network composed by lumped and distributed elements between the line and the load [Fig. 1(a)]. A number of design techniques of matching networks [3]–[6] have been proposed in the state of the art to reach the theoretical limits imposed by the Bode–Fano adapting matching [16]–[18] to genetic algorithms techniques [19], [20]. Indeed, considering a frequency-dependent complex load $Z_L(\omega) = R(\omega) + jX(\omega)$ fed by a lossless transmission line with a purely resistive characteristic impedance $Z_0 = R_0$, the matching network is designed such that the load reactance vanishes and the load resistance transforms into R_0 at the desired frequency ω_0 . Therefore, conventional impedance matching techniques act on the network topology and the involved circuital elements, i.e., capacitance, inductance, and resistance [Fig. 1(a)].

Recently, a new degree of freedom has been introduced for achieving perfect matching: the temporal modulation of the constituting elements of the complex load [21]. Despite the earlier studies dated back to the 1960s, time-varying elements in electronic circuits [22], [23], as well as spacetime-varying material properties for engineering wave propagation [24]–[31], have only recently attracted the attention of researchers, due to the possibility to achieve magnet-less nonreciprocity and frequency conversion [32]–[34]. In [21], it has been numerically demonstrated that a purely reactive

 (a)

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load, i.e., an inductor or a capacitor, that is mismatched with an ideal feeding transmission line, can be transformed into a resistance *R* when a proper temporal modulation profile is applied to the inductance $L(t)$, or capacitance $C(t)$, of the load [Fig. 1(b)]. If the temporal modulation is present, the energy is accumulated within the reactive load without generating any reflection toward the source, leading to perfect matching. Such an approach requires extremely fast modulation of the reactive components and, therefore, the implementation complexity prevents its realization in realistic scenarios, despite some interesting attempts that have been provided [35].

In this work, we reply to the following intriguing question: can the temporal profile of the propagating signal enable a special impedance transformation, such that impedance matching of a purely reactive load terminating an ideal transmission line, as shown in Fig. 1(c), is achieved? A decade ago, the use of temporal profile of incoming signal has been exploited in [36]–[38] for enabling efficient coupling in single atoms and optical resonators. More recently, the same concept has been moved in optics, for enabling energy virtual absorption in lossless systems, making them appear as matched to free space if complex zeros of its scattering eigenmodes are excited [39]–[45], reporting also elastodynamic experimental proof in mechanical systems [46]. In particular, we have investigated in [45] the possibility to enable virtual absorption effects in metasurface-bounded cavities. The analysis of this problem led to the derivation of the complex zeros, and the corresponding limit values of the surface impedances of the metasurface. Even though the concepts of virtual absorption [39] and virtual critical coupling [44] have already been investigated in cavities and optical applications, here, we exploit it for achieving a similarly anomalous response also in microwave circuits composed of purely reactive lossless lumped elements, leading to virtual perfect matching, and opening the door to a new impedance matching strategy, as preliminarily shown in our recent conference work [47], [48].

This contribution aims at shedding light for the first time on this phenomenon from both the physical and the electrical point of view, through a detailed theoretical analysis and numerical and experimental results, deriving the fundamental limits of the impedance matching concept based on time-modulated excitation signals. We analyze all possible configurations of reactive loads reported in Fig. 2: single inductance [Fig. 2(a)] and capacitance [Fig. 2(b)] and series/parallel connection of those elements as reported in Fig. 2(c) and (d), respectively. The parallel connection of reactive loads has been already discussed in our recent work [45], where fundamental limits of virtual perfect absorption have been analyzed. Nevertheless, this study included preliminary analytic expressions, and it was related to free-space propagation, focusing on energy accumulation of the structure.

This article reveals that purely reactive loads can produce no reflection when connected to a lossless transmission line exhibiting a resistive characteristic impedance under special excitation conditions. The specific novelties introduced by this work in the state of the art can be summarized in the following four contributions.

Fig. 2. Schematics of a resistive transmission line with characteristic impedance *R*⁰ loaded with a single reactive element: (a) inductor *L* and (b) capacitor *C* and connection of *LC* elements in (c) series and (d) parallel.

Contribution 1: We develop and discuss in detail a general theoretical analysis of all element configurations available as reactive loads, deriving the operative regions for which the phenomenon takes place as a function of the natural frequency of the circuit and the circuit time constant.

Contribution 2: We provide a set of proper numerical simulations of all presented load cases, describing the physical insights and providing a comparison among them.

Contribution 3: We demonstrate that the analyzed phenomenon is not related to a delay along the line, setting a numerical simulation based on an electrically long microstrip line.

Contribution 4: We report the experimental results of perfect matching condition for the series and parallel configurations.

According to the aforementioned list, this article is organized as follows. In Section II, the theoretical analysis of the mismatching condition under complex excitation is reported and discussed (Contribution 1), considering all the different load configurations (single reactive loads in Section II-A and series and parallel connections in Section II-B). Section III is devoted to the theoretical results' discussion and to the constraints and limits evaluation on the load values for achieving the virtual perfect matching (Contribution 2). In Section IV, we report the numerical simulations for purely imaginary and complex excitations, and the demonstration that the phenomenon is not related to a delay along the line (Contributions 2 and 3). Finally, Section V presents the experimental results, demonstrating that the phenomenon can be observed in lumped microwave networks (Contribution 4). In Section VI, we draw the conclusions of this investigation.

II. REACTIVE LOAD UNDER TIME-MODULATED EXCITATION: CIRCUITAL ANALYSIS

Let us consider a circuit where a lossless transmission line with resistive characteristic impedance R_0 is loaded by

a generic reactive network. From the basic transmission line theory, we can write the reflection coefficient seen at the load as

$$
\Gamma(\omega) = \frac{Z_L(\omega) - R_0}{Z_L(\omega) + R_0}.\tag{1}
$$

Regardless of the complexity of the network, the load impedance can be always represented as $Z_L(\omega) = R_L(\omega) +$ $jX_L(\omega)$, where X_L is an effective frequency-dependent reactance, seen at the load terminals. Considering a purely reactive load network, thus having $Re[Z_L] = R_L = 0$ in (1), we can write the reflection coefficient amplitude as

$$
|\Gamma(\omega)| = \left| \frac{jX_L(\omega) - R_0}{jX_L(\omega) + R_0} \right|.
$$
 (2)

In general, this lossless transmission line is always mismatched to the load since X_L and R_0 will always have different values in the real frequency spectrum. Thus, the imaginary quantity $jX_L(\omega)$ should be converted into a real one and equated to the real characteristic impedance R_0 of the feeding transmission line. Exploiting the temporal modulation of the incoming signal, this can be done by introducing a complex value of the excitation frequency ω , i.e., $\omega = \omega_r + j\omega_i$ [41]. A complex frequency excitation is a harmonic signal of frequency ω_r , whose amplitude temporally varies following an exponential growing (or decaying) profile proportional to $e^{\omega_i t}$.

The reflection coefficient in (2) can be represented as a function of the frequency in the complex frequency plane, where it is possible to identify scattering singularities, i.e., zeros and poles, of the amplitude of the reflection coefficient function for specific combinations of real and imaginary frequencies. Hereafter, we state this analysis for a single reactance case and a combination of *LC* in series and parallel connection loads. Inductors and capacitors are linear components, in accordance with Ohm's law even when the applied voltage signals increase due to the exponential growth in amplitude dictated by the complex frequency. Nonlinearity in the circuit components may represent a further degree of freedom for these phenomena, not considered in this work.

A. Single Load Cases

Now, we consider a load consisting of a single inductor *L* or capacitor *C*, whose impedance is $Z_L = j\omega L$ or $Z_L = 1/j\omega C$, respectively [Fig. 2(a) and (b)]. Starting from (2), we can estimate the reflection coefficients at the load terminals for the two considered cases

$$
\Gamma^{L}(\omega) = \frac{j\omega\tau - 1}{j\omega\tau + 1} \tag{3}
$$

$$
\Gamma^{C}(\omega) = -\Gamma^{L}(\omega)
$$
 (4)

where superscripts "*L*" and "*C*" identify the cases reported in Fig. 2(a) and (b), respectively, and the quantity τ assumes the values $\tau = L/R_0 = \tau^L$ in (3) and $\tau = R_0 C = \tau^C$ in (4). In the circuit theory, the quantities τ^L and τ^C are the well-known circuit time constants for a transient step response for *RL* and *RC* circuits, and their value determines how fast the time response goes to zero.

Fig. 3. Reflection coefficient amplitude in the complex frequency plane for a single reactive load, inductive or capacitive. (a) Its 3-D representation in decibel showing diverging singularities on the imaginary frequency axis. (b) Singularities position and behavior according to time constants.

We now consider the complex frequency excitation of the two circuits in Fig. 2(a) and (b) by imposing $\omega = \omega_r + j\omega_i$ in (3) and (4). Fig. 3(a) reports the amplitude of the reflection coefficient in the complex frequency plane that exhibits two singularities: a pole (Fig. 3(a), red/yellow positive peak) is in the positive half-space of the imaginary frequency, whereas a zero (Fig. 3(a), blue negative peak) is in its negative halfspace. The reflection coefficient pole excitation leads to an anomalous condition for which the reflected energy is higher than the impinging one. In passive systems, this is a special scattering condition for which the scattered field decays slower than the excitation field, giving rise to a virtual gain effect [49]. On the other side, exciting the zero implies a zero-reflection condition: the load behaves as an indefinite accumulator for the illuminating signal, without dissipating its energy but rather storing it within itself. The zero-scattering condition is satisfied as long as the complex frequency is such to engage the scattering zero, thus leading to a zero-reflection coefficient. Modifying the signal excitation frequency, the reflection coefficient changes and assumes a nonzero value, and energy then leaks out from the reactive load.

Imposing (3) and (4) equal to zero, we derive the roots of the reflection coefficients $\Gamma^{L,C}$ with respect to frequency

$$
\omega_0^{L,C} = \omega_r + j\omega_i = 0 - j\tau^{-1}
$$
, with $\tau = \tau^{L,C}$. (5)

The reflection coefficient vanishes at purely imaginary frequencies $\omega_0^{L,C}$, as expected from Fig. 3(a). An excitation signal with an imaginary frequency is not oscillating, but

Fig. 4. 3-D representation of the reflection coefficient amplitude for series/parallel *LC* loads in the complex plane. (a)–(c) Zeros in the lower half-plane and poles in higher half-plane according to time constants. (d)–(f) Quality behavior of singularities, which are purely imaginary when $\tau \omega_{res} > 2$, coincident purely imaginary when $\tau \omega_{res} = 2$, and complex when $\tau \omega_{res} < 2$.

simply growing over time with a steepness given by the exponential factor $e^{-\omega_0^{L,C}}$. This is fully consistent with circuit theory where the charging and discharging behavior of an *RC* (*RL*) circuit is described by the same exponential curve with a factor $e^{-t/\tau}$ for voltage (current). It is clear, therefore, that the circuit time constant τ plays a fundamental role in the zero and pole positions in the complex frequency plane. In a reciprocal lossless system, zeros and poles are always complex conjugate; increasing the time constant τ , both zero and pole move inside the complex frequency spectrum, reducing the required steepness of the time-growing signal for being excited [Fig. 3(b)], always conserving complex conjugation.

B. Series and Parallel Load Cases

Let us now consider the load as a reactive network modeled as a series/parallel connection of an inductor and capacitor [Fig. 2(c) and (d)]. In these two scenarios, the load reactance can be found as

$$
jX_L^- = j\frac{\omega^2 - \omega_{res}^2}{\omega C \omega_{res}^2};\ jX_L^{//} = j\frac{\omega L \omega_{res}^2}{\omega_{res}^2 - \omega^2}
$$
(6)

where the superscripts "-" and "//" identify the series and parallel connection, respectively, and $\omega_{res} = 1/\sqrt{LC}$ is the natural resonant frequency of the *LC* circuit for both configurations. Substituting (6) into (2), we obtain

$$
\Gamma^{-}(\omega, \tau^{-}) = \frac{(\omega^2 - \omega_{res}^2) + j(\tau^{-} \omega_{res}^2) \omega}{(\omega^2 - \omega_{res}^2) - j(\tau^{-} \omega_{res}^2) \omega} \tag{7}
$$

$$
\Gamma''(\omega, \tau'') = -\Gamma^{-}(\omega, \tau^{-}) \tag{8}
$$

where τ^- = R_0C (τ ^{//} = L/R_0) are for series (parallel) configuration. By forcing (7) and (8) to vanish, we obtain the following perfect matched complex frequencies:

$$
\omega_0^{-1/7} = -\frac{j}{2}\omega_{res}\left(\tau\omega_{res} \pm \sqrt{\tau^2\omega_{res}^2 - 4}\right), \text{with } \tau = \tau^{-1/7}.
$$
\n(9)

The frequencies granting zero reflection are two due to " \pm " sign in (9) and seem to be purely imaginary, as in the case of a single reactive load; however, this is true only if the argument of the square root in (9) is positive, i.e., $\tau^2 \omega_{res}^2 - 4 \geq 0$. When this condition is not fulfilled, that is, $\tau^2 \omega_{res}^2 - 4 < 0$, (9) assumes a complex value, which allows achieving a complex frequency with nonzero real part, i.e., harmonic signals at frequency ω*^r* with temporal varying envelope, growing or decaying according to the sign of ω*ⁱ* .

Let us now plot and discuss the reflection coefficient complex frequency planes for the following cases, being the quantity $\tau \omega_{res}$ always positive: 1) $\tau \omega_{res} > 2$; 2) $\tau \omega_{res} = 2$; and 3) $\tau \omega_{res}$ < 2. In all three cases, the reflection coefficient always shows singularities, but their location significantly changes according to the current value of the product $\tau \omega_{res}$.

Case 1 consists of an *LC* circuit whose $\tau \omega_{res} > 2$. In this scenario, the system exhibits two separate frequencies for which zero reflection can be achieved [Fig. 4(a) and (d)]. The reflection coefficient has two zero-pole pairs symmetrically distributed along the imaginary frequency axis at $\pm \omega_{int}^{-3/7}$ and $\pm \omega_{ext}^{-1/7}$, where the subscripts *int* (*ext*) identify the zeros that are closer (farther) from the real frequency axis. Like

single load case, the system exhibits zero reflection only if the excitation signal is not oscillating. However, in this case, the loci of the zeros and poles of the reflection coefficient move differently with respect to the value of the circuit time constant τ . For higher values of the time constant, the external zero-pole pair at $\pm \omega_{ext}^{-1/7}$ moves farther, while the internal one at $\pm \omega_{\text{int}}^{-1}$ tends to the frequency plane origin. On the contrary, when τ decreases [Fig. 4(d)], both external and internal zero-pole pair move toward the imaginary counterpart of the natural frequency, $\pm j\omega_{res}$, which involves special responses from the system as discussed in the next cases.

In case 2, when $\tau \omega_{res} = 2$, the two zero-pole pairs of previous case degenerate to the imaginary counterpart of the natural resonant frequency $\pm j\omega_{res}$ [Fig. 4(b)]. The degeneration of the two zero-pole pair into two imaginary frequencies $\pm j\omega_{res}$ is confirmed in (9), where $\omega_0^{-,}/\sqrt{2} = -j\omega_{res}$ for $\tau \omega_{res} = 2$, and, consequently, $\omega_{pole}^{-/}/$ = $+j\omega_{res}$ [Fig. 4(d)]. Under this condition, then, the natural resonant frequency value ω*res* is not used to express the circuit oscillation as predicted in circuit theory; instead, it coincides with the exponential factor to provide perfect matching, and thus, $e^{-\omega_i t} = e^{t/(LC)^{1/2}}$.

The last case consists of an *LC* circuit whose $\tau \omega_{res} < 2$. In Fig. 4(c), the reflection coefficient exhibits two zeropole pairs for complex frequencies with a nonzero real part, demonstrating that it is possible to achieve zero reflection from a purely reactive load under monochromatic excitation at ω_r , provided that the amplitude of the wave follows the profile $e^{-\omega_i t}$. It is worth noticing that Fig. 4(c) reports two possible zeros symmetrically distributed with respect to the imaginary axis, but only the zero for positive real frequency can be excited. Hence, the left zero-pole pair can be neglected hereafter. The singularities behavior, in this case, is shown in Fig. 4(f): keeping the same ω_{res} and increasing τ , the zeropole pair tends to the two coincident values $\pm j\omega_{\text{res}}$, leading to case $\tau \omega_{\text{res}} = 2$.

III. DISCUSSION OF RESULTS AND PHYSICAL INSIGHTS

From this analysis, we can state that the imaginary resonant frequency $j\omega_{res}$ is a key parameter since it is the boundary frequency value between the two regions, and it is strongly related to the natural real resonant frequency of the *LC* circuit. From the analytical point of view, at $\omega_0 = -j\omega_{res}$, the reactive load terminating the transmission line exhibits the same real value of the transmission line characteristic impedance, i.e., $Z^{-, //}(ω_0) = jX^{-, //}(-jω_{res}) = R_0$. Imposing $\omega_0 = -j\omega_{res}$ into (6) and (7) and the reflection coefficient equal to zero, we derive the values shown by the load at any instant of time as long as the signal is applied, i.e., Z^- = $2(L/C)^{1/2} = R_0$ and $Z^{1/2} = 0.5(L/C)^{1/2} = R_0$ for the series and parallel case, respectively. From the physical point of view, all the energy provided to the load under exponentially growing signal is stored inside reactive components (with opposite sign), which are both gradually charged in time. The energy will be accumulated progressively and, at the same time, the voltage–current ratio at the load terminals always equals the transmission line resistance, thus forbidding reflections back to the source.

Fig. 5. In *LC* load configurations, (a) real and (b) imaginary parts of the scattering zeros frequency with respect to time constant and natural resonance frequency are shown in contour plots. The black line corresponds to $\tau \omega_{res} = 2$ and splits the scattering zeros plots in Region 1 where $\tau \omega_{res} > 2$ and Region 2 where $\tau \omega_{res} < 2$.

To provide further validation to our theoretical investigation, we can see that the proposed theoretical analysis resembles the damping behavior of *RLC* circuits, where the circuit behaves as overdamped, critically damped, or underdamped according to the roots (complex or real) of the circuit harmonic oscillator equation [50], [51]. In the circuit theory, damping is caused by the energy dissipation inside the resistance of an *RLC* network. We stress that, in our study, the resistance of the transmission line *R*⁰ does not dissipate energy leading to circuit damped response. Here, instead, we exploit complex excitation (having the role of resistance dissipation) to balance the corresponding circuit reflections that are zero in the transient response.

We now illustrate the behavior of the real and imaginary parts of zeros for both *LC* series and parallel connections, thus $\omega_0^{-1/7}$ as expressed in (9), with respect to the two parameters τ and ω_{res} . Fig. 5(a) and (b) shows that both real and imaginary parts of $\omega_0^{-7/7}$ plots are split into two regions, delimited by the hyperbolic curve $\tau \omega_{res} = 2$. As expected, the real part

TABLE I LOAD VALUES UNDER $e^{j\omega_0 t}$ EXCITATION ($\omega_0 = -j2 \times 10^8$ RAD/S)

Load type	Inductance [nH]	Capacitance [pF]
	250	---
\mathcal{C}		100
LC series	125	200
LC parallel	500	50

of $\omega_0^{-1/7}$ [Fig. 5(a)] is zero when $\tau \omega_{res} \geq 2$ (Region 1), meaning that zeros are purely imaginary, as predicted by (9). In Region 1, the imaginary part in Fig. 5(b) exhibits very highfrequency values, meaning that a sharper steepness is needed to engage the desired scattering zero. This region is not of interest for seeking virtual absorption with modulated signals. On the contrary, when $\tau \omega_{res}$ < 2 (Region 2), the real part is nonzero and, for a given τ , it is directly proportional to the *LC* resonant frequency ω_{res} . The imaginary part is, indeed, much smaller than the real part, meaning that the steepness is reduced, leading to an exponential slowly growing signal.

IV. SIMULATIONS RESULTS

The impedance matching achieved through the anomalous transient behavior of reactive loads under complex excitation has been numerically verified through CST Studio Suite [52]. We consider a lossless 50 Ω transmission line with different loads terminating it. In circuit schematics, the impedance transmission line coincides with the generator internal resistance. In the following, we will focus on the circuital schematic simulations of single and combined loads that show perfect matching under purely imaginary and complex frequency excitation cases in Sections IV-A and IV-B, respectively. Finally, in Section IV-C, full-wave simulations over a designed microstrip line are exposed.

A. Imaginary Excitation Cases

In the $\tau \omega_{res} > 2$ case, there are two purely imaginary scattering zeros that can be engaged to get perfect matching. We choose a series load composed of $L = 120$ nH and $C = 200$ pF, satisfying $\omega_{0,int} = -j1.67 \times 10^8$ rad/s and $\omega_{0,ext}^- = -j2.5 \times 10^8$ rad/s zeros, whose input signals are in Fig. 6(a), red and dark blue lines. The incident and reflected signals are recorded at the load terminals. As expected, the impinging signals are engaging the reflection coefficient zeros and no reflection takes place. Since the entire circuit is passive, energy cannot be dissipated since the load is purely reactive, allowing only energy storing in the reactive load. As soon as the signal stops, at kick-off time t_0 , the zero-reflection condition is not satisfied anymore, forcing the reactive load to release the stored energy (Fig. 6(a), orange and light blue lines). We can furthermore observe that both zeros satisfy the circuit, and the zeros present different growing envelopes according to the ω_0^- values.

To explore single reactance and critical ($\tau \omega_{res}$ = 2 for series/parallel connection) cases, we choose inductors and

Fig. 6. Transient response for (a) LC series case with $L = 120$ nH and $C = 200$ pF for $\tau \omega_{res} > 2$ case (two imaginary zeros), (b) four different loads satisfying $\tau \omega_{res} = 2$ whose parameters values are shown in Table I, and (c) *LC* parallel load with $L = 10$ nH and $C = 50$ pF for $\tau \omega_{res} < 2$ case.

capacitors values as described in Table I, all of them satisfying the same zero $\omega_0 = -j2 \times 10^8$ rad/s. The signal is not oscillating in time as predicted by (5)–(9), for $\tau \omega_{res} = 2$ (Fig. 6(b), gray line). The circuit's transient response verifies the perfect matching condition.

Reflected output signals are zero until kick-off instant *t*0, but after it, the accumulated energy is released. Each output shows a different behavior according to the circuit to which it is referred to and corresponds to *RC*, *RL*, and *RLC* series/parallel circuits where the charging and discharging behavior is described by the same exponential curve with a factor $e^{-t/\tau}$ for voltage and current, respectively.

B. Complex Excitation Cases

To verify the $\tau \omega_{res}$ < 2 case, we choose an *LC* parallel configuration where $L = 10$ nH and $C = 50$ pF.

Fig. 7. (a) Schematic of the microstrip line system with an *LC* shunt load with $L = 0.5$ nH and $C = 2$ pF excited at waveguide port by a time-modulated excitation $\omega_0 = 2\pi f_0 - 5 \times 10^9$. (b) Incident and released signals recorded at the port.

According to (9), the reflection coefficient zero is $\omega_0^{//}$ = $(1.4 \times 10^9 - j2 \times 10^8)$ rad/s, i.e., a monochromatic signal at frequency $f_r^{//} = 222$ MHz with a time-varying growing envelop following the profile $e^{2\times10^{8}t}$ (Fig. 6(c), blue signal). Perfect matching is achieved also for complex-valued frequencies, showing zero reflections up to the kick-off instant (Fig. 6(c), orange line).

C. Full-Wave Microstrip Verification

To further validate the observed phenomenon of perfect matching under complex excitation, we have considered a realistic microstrip line printed on a 0.5 mm-thick FR4 substrate $(\varepsilon_r = 4.3)$ and terminated on the parallel *LC* load. The microstrip line shown in Fig. 7(a) has been designed at $f_0 = 5$ GHz. The microstrip is made of copper with width $d = 0.9$ mm. The goal of this numerical analysis is to demonstrate that this phenomenon is not related to a propagation delay along the line, but to energy accumulation and release within the reactive load. The microstrip line has been chosen of a reasonable length $l \approx 66$ mm to let the reader appreciate the whole excitation on the line and the accumulation of energy. The loaded elements are a parallel *LC* where $L = 0.5$ nH and $C = 2$ pF. Referring to (9), a complex zero is required, working at the microstrip operative real frequency f_0 . The exponential envelope needed to excite the reflection coefficient complex zero corresponds to the imaginary frequency $\omega_i = -5 \times 10^9$ rad/radss.

In Fig. 7(b), we report the recorded signals at the port terminals over time. The blue curve represents the incident

Fig. 8. Experimental setup with Tektronix TBS1052EDU oscilloscope (left), breadboard with components (center), and AFG Tektronix 1062 (60 MHz) (right).

signal, and the orange curve represents the released signal. It is clear that the phenomenon is preserved since the envelope of the released signal is opposite with respect to the incident one, whereas in case of reflection, it would not, and the presence of the time delay between the two signals is due to their propagation along the line. Since the signals are detected at the waveguide port, the observed delay exactly corresponds to two times the line length over the phase velocity in the microstrip line, i.e.,

$$
\Delta t = 2l \frac{\sqrt{\varepsilon_{eff}}}{c} \tag{10}
$$

where ε_{eff} is the effective permittivity of the microstrip line and *c* is the light speed. The line delay naturally occurs during propagation over the microstrip, and it is independent of the perfect matching phenomenon. These numerical results clearly show that the signal is not only delayed because of the line length but also independently stored thanks to perfect matching due to the excitation of the reflection coefficient zeros in the complex frequency plane.

V. EXPERIMENTAL VERIFICATION

In the following, we set up an experiment for validating our analysis and demonstrate the perfect matching by using a reactive load consisting of an *LC* parallel and an *LC* series connection, as detailed in Sections V-A and V-B, respectively. In both configurations, we use the same components: a ceramic disk capacitor of $C_{eq} = 2$ nF and three axial lead inductors of $L = 1$ μ H that show, in shunt connection, an equivalent of L_{eq} = 333 nH. The use of multiple inductors or capacitors that correspond, in shunt or series connections, to an equivalent value does not affect the phenomenon that is preserved. A picture of the experimental setup is shown in Fig. 8, where the chosen components are mounted over a breadboard, connected to the arbitrary function generator (AFG) Tektronix 1062 that generates the time-modulated signals. On the other side, an oscilloscope Tektronix TBS1052EDU is connected to a probe to the board and detects the voltage signals.

Fig. 9. (a) Schematic of the system for *LC* shunt load. (b) Normalized simulated and (c) combined measured input signal (blue curve), output signal at port (CH1) reflected toward the AFG port (red curve) and output signal detected at the oscilloscope probe (CH2) (red curve).

A. Parallel LC Load

Following (8), the shunt connection of *Leq* and *Ceq* falls under condition $\tau^{1/\tau_{0}}_{res}$ < 2, so two complex zeros arise on the reflection coefficient complex plane, as shown in Fig. 4(c)–(f). The chosen complex frequency zero needed to get perfect matching has $f_r = 6.1$ MHz with a temporal modulation composed of an exponential rise given by the imaginary frequency $\omega_i = -5 \times 10^6$ rad/radss.

As shown in Fig. 9(a), the load is connected through a lumped-element Wilkinson power divider (WPD) designed at

 f_r to the AFG and the oscilloscope. The signal is generated by the AFG and is split into two signals: the former, CH1, is directly connected to the oscilloscope, and CH2 is connected to the WPD and combined into the line leading to the load. Here, the signal is accumulated and, later, is divided into the two ports that carry the signal back to the AFG and the oscilloscope. Both the output impedance of AFG and oscilloscope are set at $R_0 = 50 \Omega$, and also, the oscilloscope probe lead measures voltage over a 50 Ω load. In Fig. 9(b) and (c), the simulated response of the circuit detected at the probe port and the measured response detected at the AFG port are reported. As expected, the experiment clearly returns perfect matching phenomenon since the signal detected at the probe is zero up to kick-off instant t_0 , that is, reflections vanish. After t_0 instant, as soon as the temporal modulated excitation stops, the signal is released and is equally split by the power divider into CH1 and CH2 signals, being the perfect matching condition not satisfied anymore. A negligible difference between simulated and measured released signals can be observed by comparing the yellow curves in Fig. 9(b) and (c), due to the very small resistive behavior introduced by wires and connectors in the experiment that leads to a minor attenuation of the signals.

B. Series Load

In addition to the shunt *LC* load examination, a second analysis for an *LC* series connection has been carried. Here, the considered load is composed by a series connection of L_{ea} and C_{ea} elements. The series configuration of these two elements provides $\tau^- \omega_{\text{res}} > 2$ in (9). Consequently, perfect matching is obtained through two purely imaginary zeros that are $\omega_{int} = -j1.08 \times 10^7$ rad/s and $\omega_{ext} = -j1.41 \times 10^8$ rad/s, using the same notation of Section II. These zeros lay along the imaginary frequency axis, as shown in Fig. $4(a)$ – (d) . We have arbitrarily chosen ω_{int} zero to excite the circuit. Since now, the excitation ω_{int} required to get perfect matching is a static growing signal, the WPD element is not needed anymore, as shown in the experimental setup in Fig. 10(a). As for the shunt connection case, CH1 carries the port signal that comes from the BNC splitter and directly connects to the oscilloscope. CH2 carries the probe signal, detected by the probe on the breadboard. In this case, port and probe signals coincide in simulations since retards and small dissipation are not considered. However, since some delays and dissipations in measures naturally occur, we show both measured port and probe signals. In Fig. 10(b) and (c), we, respectively, show simulated normalized signals and the combined measured signals. As for series case presented in Fig. 6(b) (pink curve), perfect matching behaves similarly in both simulated and measured results. As for the measured signals in Fig. 10(c), signals at the probe exhibit an extremely small delay with respect to the ones at the port. However, it is enough to hide the negative peak at the probe that is indeed present in the simulated signals. The accuracy and sampling speed of measuring instruments have been optimally set for detecting any variation of the signal amplitude at the measuring points. Indeed, the extremely narrow negative peak curve, presented by the output signal at the port [orange dashed signal in

Fig. 10. (a) Schematic of the system for *LC* series load. (b) Normalized simulated input and output signals. (c) Normalized combined measured signals showed at port (CH1): input signal (blue dashed curve) and output signal (red dashed curve). Combined measured signals showed at probe (CH2): input signal (yellow curve), reflected toward the AFG port (red curve), and output signal detected at the oscilloscope probe (CH2) (purple curve).

Fig. $10(c)$], is correctly detected. The absence of the negative peak on the measured signal at the probe is, thus, due to the intrinsic charging and discharging time required by reactive circuital components, which in this case is longer than the duration of such a peak.

VI. CONCLUSION

To conclude, we have presented the first experimental validation and full theoretical derivation of perfect matching of purely reactive loads terminating a lossless transmission line by exploiting the concept of impedance transformation through time-varying complex signals. In particular, the work sheds light on the anomalous phenomenon of virtual perfect matching, bringing several novelties to the current state of the art of complex signals propagation in electromagnetic systems modeled through terminated transmission lines and, for the first time, proposing an experimental implementation. We have developed and discussed in detail a general theoretical analysis of all element configurations available as reactive loads, deriving the operative regions for which the phenomenon takes place as a function of the circuit natural frequency and time constant. The theoretical analysis has been verified through a set of proper numerical simulations of all presented load cases, describing all physical insights and providing a comparison among them. Moreover, we have clarified, by setting a numerical simulation based on an electrically long microstrip line, that the analyzed phenomenon is not related to the delay along the line. Finally, we have reported the first experimental results on virtual effects and, in particular, perfect matching condition for the series and parallel configurations. Although the required increasing envelope of the temporal profile is still a limit for making this concept exploitable in practical scenarios, the experimental verification provided in this article may provide a base for paving the way to a new impedance matching strategy in microwave circuits, which can be exploited together with the already proposed applications based on virtual effects such as wireless energy transfer and energy harvesting [53]–[55].

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