

Predictive Field-Oriented Control for Electric Drives

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Abstract: Model predictive field-oriented control (PFOC) is a novel control strategy belonging to the class of finite control set model predictive control (FCS-MPC) for electric drive systems. It is a direct control scheme which minimizes the cost function through the convergence of errors between the given and predictive stator currents. In this paper, PFOC is thoroughly presented and analyzed through its dynamics and steady state operations under wide range of speed and varying torque conditions. In light of PFOC's model based characteristics, its robustness and influence under model parameters' mismatch is also investigated. Experiments are conducted to show these performance and sensitivities.

Keywords: Model predictive control, electric drives, induction machine.

1 Introduction

The most widely applied electric drive strategy nowadays for AC motors is field-oriented control (FOC)^[1]. As a linear control method, FOC requires system linearization, however, it is hard to integrate nonlinear controller with linear controllers such as PID controller. Meanwhile, with the cascaded control structure, FOC restricts the control rates of different control loops, i.e. inner current controllers' control speed must be much faster than that of the outer speed controller. This requirement on control loops also leads to limited control bandwidth, thus slower system response. Moreover, since it generates continuous voltage reference, pulse width modulation (PWM) hardware is required for voltage source inverter (VSI)'s switching state transformation. Being able to solve the above mentioned problems of FOC, model predictive control (MPC), as a kind of emerging nonlinear and direct control strategy for power electronics and electric drives^[2-4], has become a research hot spot in the area.

MPC is very suitable for the control of power electronics converters because it has a discrete nature with finite number of switching states^[5-6]. Similarly, a digital controller, with a sample-based manner of control, also has a discrete nature. Thus, MPC is naturally adaptable to the digital controller and requires no linearization^[7]. When controlling electric drives, MPC was first presented as predictive torque control (PTC)^[8-9]. PTC minimizes the error of electromagnetic torque and magnitude of the stator flux through the cost function^[10]. Predictive field-oriented control (PFOC) was first proposed and applied on a VSI with RL load^[11]. Because it can achieve direct nature of current control and even simpler algorithm than PTC without sacrificing performance at either steady state or transient state, it has attracted the attention of

researchers and has been widely applied on various power electronics converters with both traditional and novel topologies^[3,12]. However, PFOC was seldom researched for electric drives^[13]. When controlling electric drives, compared to PTC, PFOC requires no weighting factor for the controlled current components in the cost function, while PTC has to pre-calculate this factor in light of the different physical attributes of controlled torque and flux quantities^[14]. Thus, PFOC is theoretically much simpler than PTC for electric drives, though the research on this is in the starting phase. To unearth the PFOC's application potential in depth, this paper focuses on the analysis and experimental assessments of PFOC for electric drives. In order to discover the characters of PFOC thoroughly, experiments on a PFOC controlled induction machine with varying speed references and load torques as well as parameters' deviations are conducted^[15-16], and their corresponding performance is shown and analyzed.

2 Models of voltages source inverter and induction machine

2.1 Mathematic model of inverter

A two-level three-phase VSI serves as the power converter in this work. Its topology and all feasible voltage vectors are displayed in Fig.1. Switching state \mathbf{S} is in the form of a vector sum:

$$\mathbf{S} = \frac{2}{3} (S_a + aS_b + a^2S_c) \quad (1)$$

in which $\mathbf{a} = e^{j2\pi/3}$. $S_i, \bar{S}_i = 1, 0$ shows the on, off states of the upper, lower switches of lag i , with $i = a, b, c$. The output voltage vector \mathbf{v} is of the same amplitude of DC link voltage and calculated from switching state \mathbf{S} as:

$$\mathbf{v} = V_{dc} \mathbf{S} \quad (2)$$

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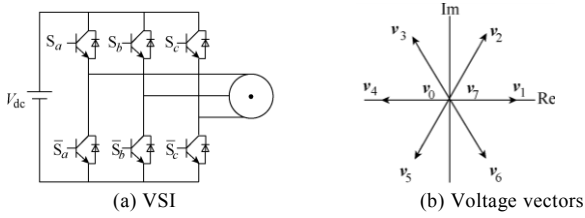


Fig.1 Two-level three-phase VSI

2.2 Mathematic model of induction machine

A squirrel-cage IM serves as the test motor within this work. It is described by five classic electrical and mechanical equations in stationary reference frame as follows:

$$\mathbf{v}_s = \mathbf{i}_s \cdot R_s + \frac{d}{dt} \boldsymbol{\psi}_s \quad (3)$$

$$0 = \mathbf{i}_r \cdot R_r + \frac{d}{dt} \boldsymbol{\psi}_r - j \cdot \omega \cdot \boldsymbol{\psi}_r \quad (4)$$

$$\boldsymbol{\psi}_s = L_s \cdot \mathbf{i}_s + L_m \cdot \mathbf{i}_r \quad (5)$$

$$\boldsymbol{\psi}_r = L_r \cdot \mathbf{i}_r + L_m \cdot \mathbf{i}_s \quad (6)$$

$$T_e = \frac{3}{2} \cdot p \cdot \text{Im} \{ \boldsymbol{\psi}_s^* \cdot \mathbf{i}_s \} \quad (7)$$

In the previous set of equations, \mathbf{v}_s is stator voltage vector. $\boldsymbol{\psi}_s$ and $\boldsymbol{\psi}_r$ represent the stator/rotor flux. \mathbf{i}_s and \mathbf{i}_r denote the stator/rotor currents. R_s and R_r are the stator/rotor resistances.

L_s , L_r and L_m are stator, rotor and mutual inductances. Electrical speed and pole pair number are ω and p . Electromagnetic torque is T_e .

3 Predictive field-oriented control

Fig.2 shows the block diagram of electric drive system with predictive field-oriented control. It is named “field-oriented control” because it requires rotor flux orientation, which is similar as the conventional field-oriented control (FOC).

3.1 Stator current prediction

Stator currents are firstly predicted with all feasible voltage vectors, and these predictions are evaluated through a cost function. The voltage vector minimizing the cost function is selected as the optimal gate signal of the IGBTs in the next sampling cycle. For long prediction steps, only the first voltage vector (corresponding to the next time step) of this optimal set is applied to the inverter referring to the receding horizon principle.

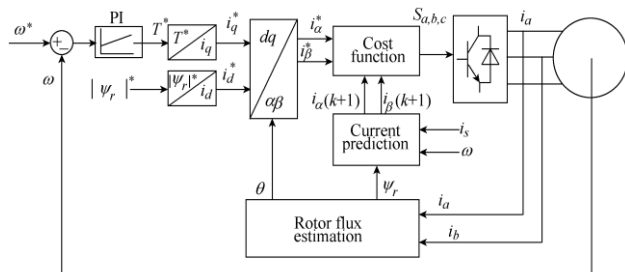


Fig.2 PFOC electric drive system

From the IM model described in section II, stator current can be further described as below:

$$\mathbf{i}_s = -\frac{1}{R_\sigma} \left\{ \left[L_\sigma \cdot \frac{d\mathbf{i}_s}{dt} - k_r \cdot \left(\frac{1}{\tau_r} - j \cdot \omega \right) \cdot \boldsymbol{\psi}_r \right] - \mathbf{v}_s \right\} \quad (8)$$

where $k_r = L_m / L_r$, $L_\sigma = \sigma \cdot L_s$ and $R_\sigma = R_s + k_r^2 \cdot R_r$.

First order forward Euler discretization is adopted to predict the next step's value with T_s as the system sampling period:

$$\frac{dx}{dt} \approx \frac{x(k+1) - x(k)}{T_s} \quad (9)$$

With (8) and (9), the prediction of next step's stator current is:

$$\hat{\mathbf{i}}_s(k+1) = \frac{\tau_\sigma}{\tau_\sigma + T_s} \cdot \mathbf{i}_s(k) + \frac{T_s}{L_\sigma(\tau_\sigma + T_s)} \cdot \mathbf{v}_s(k) + \frac{k_r T_s}{\tau_r L_\sigma(\tau_\sigma + T_s)} \cdot \left(1 - j \cdot \frac{1}{L_\sigma} \cdot \omega(k) \right) \cdot \boldsymbol{\psi}_r(k) \quad (10)$$

where $L_\sigma = \sigma \cdot L_s$ and $\tau_\sigma = L_\sigma / R_\sigma$.

The generation of the current references is necessary for PFOC controller. The torque reference is obtained through speed PI controller, while the rotor flux reference considered as a constant. The values of the field-producing and torque-producing current components in rotor flux reference frame are calculated as:

$$i_d^* = \frac{|\boldsymbol{\psi}_r^*|}{L_m} \quad (11)$$

$$i_q^* = \frac{2}{3} \frac{L_r}{L_m} \frac{T^*}{|\boldsymbol{\psi}_r^*|} \quad (12)$$

The corresponding stator current vector composed with the above components is transferred into the stationary $\alpha\beta$ frame before given to the cost function.

3.2 Cost function

PFOC, as a class of FCS-MPC, contains the merit of high flexibility in cost function design and strong nonlinear control ability. Terms of control objects and system constraints can be extensively added into the cost function. The cost function in this work is expressed by the following integrated equation:

$$g_j = \sum_{h=2}^N \{ |i_\alpha^* - i_\alpha(k+h)_j| + |i_\beta^* - i_\beta(k+h)_j| + \lambda \cdot |F_s(k+1) - F_s(k)| + \text{Im}(k+h)_j \} \quad (13)$$

Because two-level VSI containing 7 different switching states is applied in this system, $j=0..6$. With these 7 voltage vectors as presented in Fig.1, the cost function calculates 7 times. Thus, there are 7 possible values of g_j . The voltage vectors minimizing g_j is selected as the reference and its corresponding switching state is given to the VSI as next period's action. N is the predictive horizon. In this work, time

delay compensation is considered, thus two-steps prediction of PFOC is applied with $N=h=2$. The first two terms are the current control components of PFOC. Since they are both currents, no weighting factors are needed to be tuned between these two terms as in PTC. The third term of the cost function is the switching frequency control term that shows the switching number of the current state with the applied voltage vector. $F_s(k)$ represents the switching state for three lags of VSI. For example, if only the upper leg of the a phase is switched on, $F_s(k)=100$. λ is the weighting factor that can be tuned according to the importance of switching frequency control.

The fourth term is current limitation term:

$$I_m(k+h) = \begin{cases} 0 & \text{if } |i(k+h)| \leq |i_{\max}| \\ \gamma \gg 0 & \text{if } |i(k+h)| > |i_{\max}| \end{cases} \quad (14)$$

where $|i(k+h)| = \sqrt{|i_\alpha^2 - i_\alpha(k+h)| + |i_\beta^2 - i_\beta(k+h)|}$.

If the current is smaller than the maximum current $|i_{\max}|$, the fourth term of the cost function is effective in control only when the voltage vector leads a current beyond the current limit. For the over current situation, this part increases the cost function value and thus the corresponding voltage vector is abandoned. Therewith the current limitation of the system is realized.

Based on the previous explanation, the execution of PFOC can be shown in Algorithm 1. Firstly, the rotor speed and stator currents are measured. Then the rotor flux vector is estimated. Its angle, together with the torque and flux producing currents components i_d^* and i_q^* , is used for stator current calculation in stationary frame. After that, current predictions with respect to all available voltage vectors will be made. These predictions are substituted into the cost function, and the prediction which minimizes the cost function is treated as the optimal and its corresponding voltage vector used as the applied vector for the electric drives in the next control cycle.

Algorithm 1 Execution process of PFOC strategy

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Initialize the system;
Measurement of  $\omega$  and  $i_s$ ;
Estimation of  $\psi_r$ ;
Calculation of  $i_\alpha^*$  and  $i_\beta^*$ ;
for  $j=0:6$  do
Prediction of  $\hat{i}_{sj}(k+1) = f(v_{sj})$ ;
 $g_j = \sum_{h=2}^N \{ |i_\alpha^* - i_\alpha(k+h)_j| + |i_\beta^* - i_\beta(k+h)_j| + \lambda \cdot |F_s(k+1) - F_s(k)| + \text{Im}(k+h)_j \}$ 
Keep the minimum value of  $g_j$  and the corresponding  $v_{sj}$ ;
end for
0: Apply  $v_{sj}$  to electric machine through VSI at next control cycle.

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4 Experimental results

4.1 Motor parameters

Experiments are conducted on an IM machine with parameters in Table 1. Test bench is shown in Fig.3. The sampling frequency is set to be 16kHz.

Table 1 Induction machine parameters

Parameters	Value
DC link voltage V_{dc}/V	582
R_s/Ω	2.68
R_r/Ω	2.13
L_m/mH	275.1
L_s/mH	283.4
L_r/mH	283.4
p	1.0
$\omega_{nom}/(r/min)$	2772.0
$T_{nom}/(N \cdot m)$	7.2
$J/(kg \cdot m^2)$	0.005

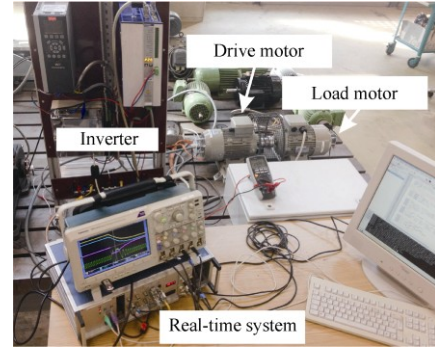


Fig.3 Test bench

4.2 Experimental results

4.2.1 Dynamic and steady states performance

In the first test, the motor operates in the full speed range. A speed reversal maneuver of rated speed from 2772r/min to $-2772r/min$ is conducted. Fig.4 demonstrates the full speed range performance of the motor control system. The torque is set to its maximum value in the speed transition process in order to decelerate at its highest rate. Both the stator current and flux maintain their smoothness.

In the second test, a sudden torque with rated value of $7.5N \cdot m$ is loaded on the motor shaft. It is seen in Fig.5 that the system can fully drag this load instantly within 50ms, while the speed is hardly reduced by this sudden load. In order to balance this torque, more power should be transferred. Thus, the magnitude of both the stator currents and stator magnetic flux are increased.

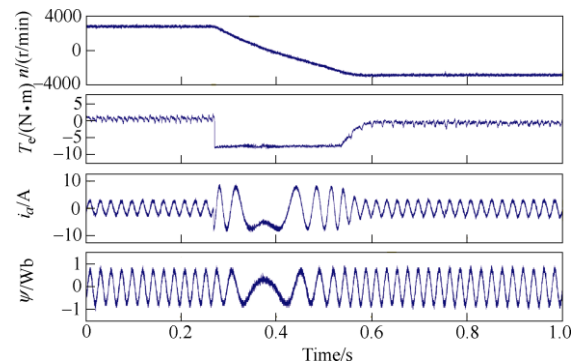


Fig.4 Behaviour under speed reversal

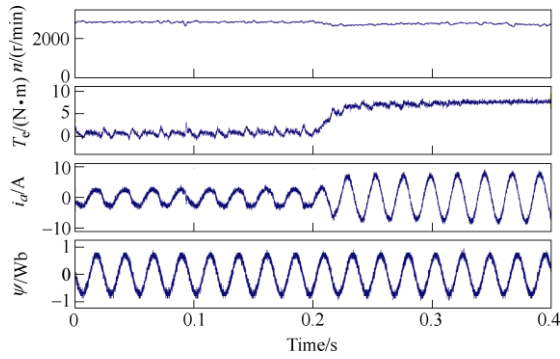


Fig.5 Behaviour under torque variation

The third test is to show the proposed PFOC electrical drive system's steady state performance. The motor is rotating at rated speed without load. From Fig.6, it is seen that in steady state, the control system has very satisfactory performance without obvious speed or torque oscillation and there is only small ripples in stators current and flux. Fig.7 observes the three phase stator currents at steady state with rated speed and torque. It proves that at the rated condition, the controlled AC motor with PCC method operates smoothly with a set of balance three phase currents. And the stator flux magnitude is kept at a constant.

4.2.2 Robustness analysis

As PFOC is model-based control, the machine model mismatches will deteriorate the control precision and dynamic performance. PFOC with longer prediction horizon control will even enlarge the cumulative error when the machine model parameters mismatches appear. Therefore, it is necessary to reveal the sensitivity and robustness of the system under parameter variation.

Firstly, the robustness against L_m variation is investigated. Since the stator flux of IM is calculated based on ratio of the measured current and L_m , the deviation of L_m causes large estimation error in flux estimation and the system may become unstable. However, compared to PTC, where both the stator and rotor fluxes estimation require L_m , in PFOC, it is only needed for stator flux estimation. Thus, PFOC should be less sensitive against L_m variation in theory. However, Fig.8 and Fig.9 show that PFOC becomes unstable with a 4% increase in L_m . Thus, it is very sensitive for L_m at both high and low speed conditions.

Electric machines, after continuous operations under loaded conditions and with the temperature

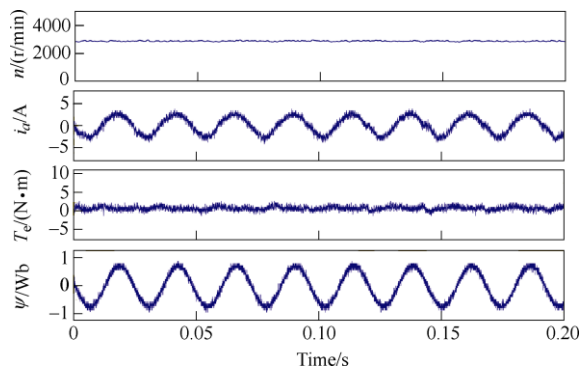


Fig.6 Steady state behaviour at rated speed without load

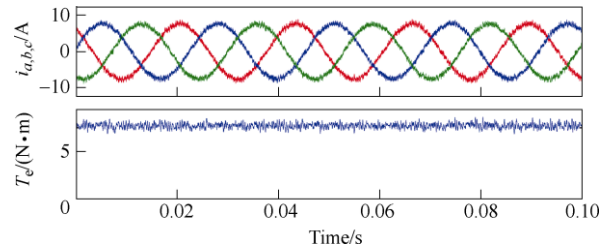


Fig.7 Steady state behaviour at rated speed with rated load

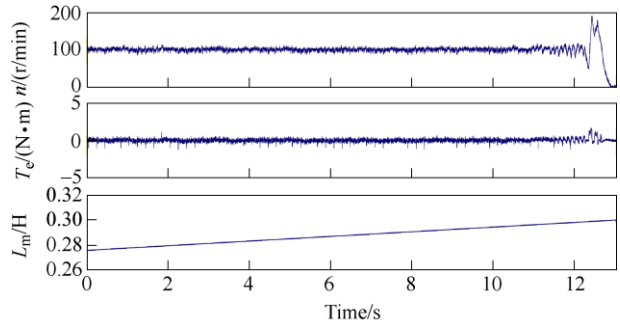


Fig.8 Sensitivity of L_m at 100r/min

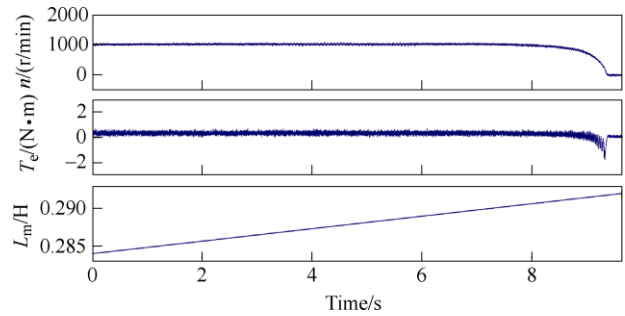


Fig.9 Sensitivity of L_m at 1000r/min

variation, will have change in resistance values. Thus, the system's robustness under resistance deviation should be studied as well.

Fig.10 shows that the system becomes unstable when the value of R_r is increased when the motor is rotating at 100 rpm, which is as expected. But when compared to the situation of L_m , system, it is much less sensitive against R_r variation. It enters the critical unstable state only when R_r is increased with 14%. As shown in Fig.11 and different from L_m , even when R_r is increased to 380% and the motor is of a speed of 1000 r/min, it is still stable without torque fluctuation.

The trend of robustness against R_s variation is similar to that of the R_r , which is shown in Fig.12 and Fig.13. The critical unstable value for R_s under 100r/min condition is with an increase of 19%.

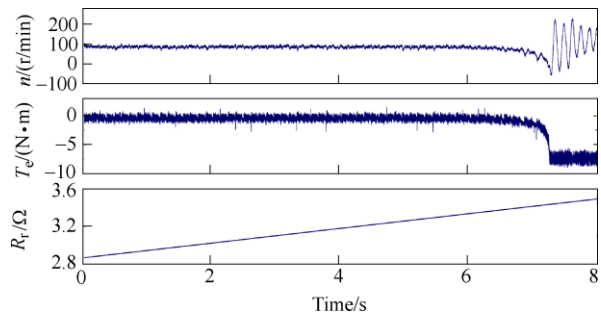
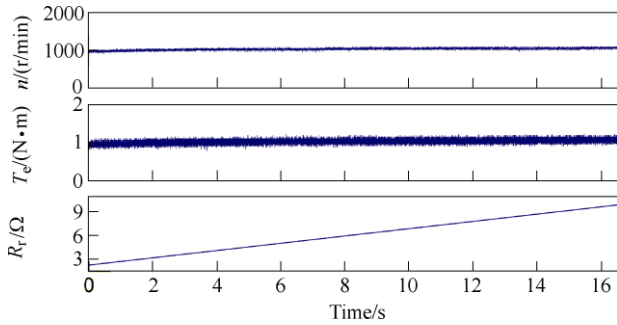
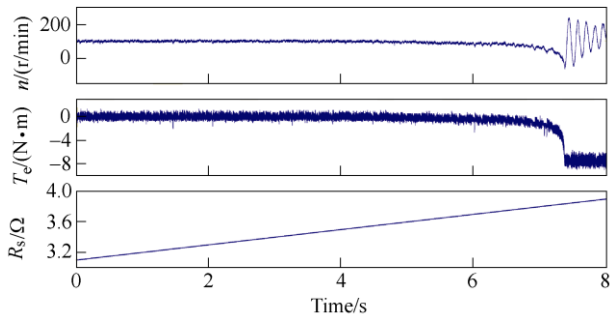
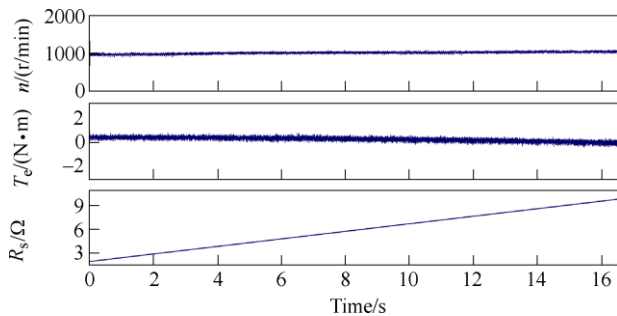


Fig.10 Sensitivity of R_r at 100r/min

Fig.11 Sensitivity of R_r at 1000r/minFig.12 Sensitivity of R_s at 100r/minFig.13 Sensitivity of R_s at 1000r/min

From the above results, it is found that system's robustness is closely related to the speed. For both inductance and resistances, the motor is less sensitive to their parameters' deviations when operating at middle and higher speed.

5 Conclusions

In this paper, a finite-control-set model predictive field oriented controller is proposed and applied in an induction machine control system. The experimental results show its high performance. PFOC reduces the system cost, shortens its response time and improves the general dynamics. Moreover, there is hardly any work for the cost function. These advantages are confirmed in a wide speed range at both no load and loaded conditions. PFOC controlled system's steady speed control performance, low torque ripples, ideal sinusoidal current waveform and fast response, which are essential for the low voltage drive systems. This also implies that the predicted currents can track the references very precisely. Investigations on system's robustness reveal that PFOC is sensitive to inductance deviation, and therefore a parameter observer is

suggested for further improvement for implementation. At higher speed region, PFOC behaves more robustly, which verifies again a mutual character of model based controllers or estimators.

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