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RESEARCH ARTICLE

Downlink Analysis for the D2D Underlaid Multigroup Multicast Cell-Free Massive MIMO With Low-Resolution ADCs/DACs

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ABSTRACT To fully utilize the scarce spectrum resources, the downlink device-to-device (D2D) underlaid multigroup multicast cell-free massive multi-input multi-output (MIMO) systems is proposed, where the geographically distributed access points (APs) serving both multi-antenna cell-free users (CFUEs) and D2D users (DUEs) pair over the same time/frequency resource blocks. Specially, the low-resolution analog-todigital converters/digital-to-analog converters (ADCs/DACs) are adopted at the AP to effectively reduce hardware damage and energy costs. The imperfect channel state information (CSI) is obtained firstly by the standard minimum mean square error (MMSE), then the lower bounds of the closed-form achievable downlink rates for both CFUEs and DUEs are derived. Aside from that, the sum energy efficiency (EE) is also explored using the established power consumption model. Finally, numerical simulations are assessed to verify the analytical results and provide insights into the effects of the key system parameters. It demonstrates that increasing the number of APs can improve the sum SE, however, the sum EE decreases with the number of the APs sharply. Furthermore, increasing the density of DUEs can significantly improve the system capacity. The findings highlight the significance of the collaborative deployment of D2D and multigroup multicast cell-free massive MIMO technology, which can serve as a valuable reference and guide for the actual deployment of future communication systems.

INDEX TERMS Cell-free massive MIMO, D2D, energy efficiency, low-resolution ADCs/DACs, multigroup multicast, spectral efficiency.

I. INTRODUCTION

As a novel incarnation of centralized massive multi-input multi-output (MIMO) and distributed network MIMO, the advent of cell-free massive MIMO was yet pioneered in the groundbreaking contributions [1], [2]. In such systems, an enormous number of geographically distributed access

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points (APs) are deployed cooperatively communicating relative small users over the same time/frequency resource blocks and all APs have liaised with a central processing unit (CPU) via fronthaul links. It has been demonstrated that a fivefold gain in 95%-likely per-user throughput can be obtained when compared to the small cell scheme. Since it can potentially contribute multitudinous merits in terms of tremendous macroscopic diversity, coverage probability, ultrahigh spectral efficiency (SE), and energy efficiency (EE), it has

been consequently considered as one of the main building blocks toward the forthcoming beyond fifth-generation/sixthgeneration (B5G/6G) projected to evolve [3], [4], [5], which has also been seriously triggered the growing research interest from the community of academic, industrial, and standardization bodies [4], [5], [6], [7].

Promoted by the above myriad benefits, the majority of recent research efforts have been focused on a roll [8], [9], [10], [11], [12], [13], [14]. The early works that relied on existing related contributions were mostly carried out within the specific context of the following techniques. For instance, a novel non-orthogonal multiple-access (NOMA) aided cell-free massive MIMO system was investigated in [8], [9], and [10] to meet the conflicting demands of high SE/EE/reliability and massive connectivity with low latency. Furthermore, as it can provide an outstanding capability of agilely moving in three-dimensional space, in [11] and [12] an unmanned aerial vehicle (UAV) enabled cell-free massive MIMO systems were considered for a wide-range of applications, which is able to remarkably relieve spatial limitations. Unlike traditional secrecy through cryptographic encryption, the authors in [13] and [14] use the trajectory design to tackle the physical layer security from an information-theoretic standpoint. To achieve the energy-efficient load balancing, in [15], the minimized total power consumption optimization was considered by jointly transmitting powers and hardware dissipation [16]. However, the works mentioned above only consider the general unicast transmissions.

Currently, the Global Internet Phenomena Report, released in January 2022, indicates that accounting for 53.72 percent of the entire Internet is primarily dominated by multicast applications, such as video conferencing, software updates, and streaming media, in the daily routines and shows a trend of explosive growth [17]. However, the increasing demand places a significant strain due to the scarcity and insufficient the available radio spectrum resource, which has become a major factor limiting the system performance and making it difficult to provide the users with the expected quality of experience (QoE) provisioning as well. These enormous drivers have inspired generous research efforts toward efficient spectrum utilization.

A. BACKGROUND AND MOTIVATION

As an effective way of allowing multiple multicast contents to deliver to various groups simultaneously, multicast multigroup transmission has triggered rapid advances in full swing since it can efficaciously relieve the pressure of ultrahigh volumes of network traffic in conventional systems and it is a consensus that will play a pivotal role in the forthcoming system. In reality, multigroup multicast named as evolved multimedia broadcast/multicasting service (eMBMS) has been incorporated into the third-Generation Partnership Project (3GPP) Release-17 [18]. For this, the literature [19] analyzed the performance of multicast multigroup cell-free massive MIMO systems by using the distributed conjugate beamforming (CB) precoder with the

short-term power constraint. It demonstrates that the larger group number or higher Eve's spoofing pilot power leads to significant degradation of secrecy performance. On this basis, the work [20] further investigated the physical layer security performance in the presence of pilot spoofing attack, and [21] explored the effects of multiantenna users and low-resolution analog-to-digital converters/digital-to-analog converters (ADCs/DACs) on multigroup multicast downlink cell-free massive MIMO systems. It reveals that substituting 5-bit DACs for full-resolution can achieve the same performance, and when DAC quantization is equal to 2-bit, the maximum sum EE can be achieved. By taking the effects of channel estimation, pilot contamination, and different precoding schemes into account, a joint unicast and multigroup multicast cell-free massive MIMO was studied in [22], proving the proposed architecture can effectively achieve the higher SE.

In parallel, as a compelling candidate enabler that allows direct transmission between devices located in close proximity, device-to-device (D2D) is continuously evolving and engulfing a wide diversity of intensive applications, which has been considered as one of the pivotal technologies to making more efficient use of spectrum resources and was originally conceived for long term evolution-advanced (LTE-A) under the 3GPP Release-12 [23], [24], [25]. With all the benefits listed above, D2D proposes a new epitome to take full advantage of the proximity of users for efficient utilization of available resources, features of D2D could be explored to shed light on the potential of offloading wireless traffic, reducing transmission latency, corroborating proximity-based services, extending the battery life of users, and upgrading SE/EE. Inspired by the preceding consideration, various research communities around have been intensively exploring the potential techniques of the D2D underlaid paradigm to enable its seamless integration with the B5G/6G. In academia, D2D communication was first proposed in [26] to enable multihop relays in cellular networks. Later, the research in [27] looked into the potential of D2D communication for improving the SE of cellular networks. For the traditional massive MIMO systems, the works [28], [29], and [30] examined the interaction between the traditional massive MIMO systems and underlay D2D communication.

The work [31] first studied the coexistence of D2D and cell-free massive MIMO uplink systems with low-resolution ADC. It shows that activating D2D links has a positive impact on SE. Besides, by assuming imperfect CSI is available in [32], we considered a D2D underlaid downlink cell-free massive MIMO system. To maximize the average sum rate, a path-following algorithm was proposed.

B. CONTRIBUTIONS AND OUTCOMES

To the best of the authors' knowledge, the amalgamation of these two disjoint networking techniques, known as multigroup multicast cell-free massive MIMO and D2D communication, has not received further attention by the research

academic, particularly for the regimes of multiantenna both at APs and users.

Promoted by the preceding consideration, in this paper, the novelty and specific contribution are summarized as follows.

- 1) Assuming that the imperfect CSI is available, the estimated channel properties of both two links are derived by using the general minimum mean square error (MMSE) technique, which is paimarily used for multiplexing in the sequence.
- 2) With the CB precoder and maximal ratio transmission (MRT), the closed-form achievable rate for both cell-free users (CFUEs) and D2D users (DUEs) are calculated, respectively. After performing the capacity bounding technique and several analyses, some significant insights are attained with the derived results.
- 3) Based on the established power consumption model and the derived sum rates, a system-level sum EE is then derived. Finally, numerical simulations are provided to enable us to give insights into the effects of the key system parameters. It shows that increasing the number of APs can improve the sum SE, however, the sum EE decreases as the number of the APs increases.

C. ORGANIZATION AND NOTATIONS

Organization: The remainder of this paper is briefly organized as follows. The considered D2D underlaid multigroup multicast cell-free massive MIMO model is described in Section II and the analysis methodology of achievable rate is conducted in Section III. Then the sum-EE is performed based on the established system-level power cost model in Section IV. Moreover, the main derived results and derivations are presented in Section V which is further supported by numerical simulations. Finally, we draw out our concluding remarks in Section VI and prove our various claims in the Appendices.

Notation: For notational simplicity, we mention the common notations used in this article. Boldface uppercase **X** and lowercase **x** are denoted matrices and vectors. The superscripts $(.)^T$, $(.)^*$, $(.)^{-1}$, and $(.)^H$ represent the transpose, conjugate, inverse, and conjugate transpose, respectively. The symbol E{.} stands for the statistical expectation operator. Likewise, the shorthand notation $\mathbf{n} \sim \mathcal{CN}(0, \sigma^2)$ denotes that the random vector **n** follows a zero-mean circularly symmetric complex Gaussian distribution with covariance matrix σ^2 .

II. SYSTEM MODEL AND PRELIMINARIES

In this paper, the D2D underlaid multigroup multicast cell-free massive MIMO model is outlined as shown in Fig. 1, where *M* geographically distributed APs over a large area to serve $J \times K$ multi-antenna CFUEs and *L* DUEs pair in the same time/frequency resource blocks,^{[1](#page-2-0)} $M \geq J$. Besides,

FIGURE 1. D2D underlaid multigroup multicast cell-free massive MIMO model.

each AP, CFUE, and DUE has N_A , N , and N_D antennas, respectively. As presumed in [1], all APs are coordinated and connected to a CPU via an ideal backhaul link with error-free and infinite capacity.

A. CHANNEL MODEL

For sake of analysis, the wireless channel is assumed to experience quasi-static Rayleigh block fading [1], [4], [13], [21], [32]. That is, the fading coefficients remain constant during each transmission slot and change independently from one to another.

Assuming that the uncorrelated Rayleigh channel is used, we denote $\mathbf{G}_{mjk}^{\text{a}} \in {}^{N_A \times N}$ as the channel response from the *m*th AP to the *k*th CFUE in the *j*th group, which can be modelled as [33]

$$
\mathbf{G}_{mjk}^{\text{a}} = \beta_{mjk}^{1/2} \mathbf{H}_{mjk},\tag{1}
$$

where β_{mik} , $\forall m, \forall j, \forall k$ accounts for the large-scale fading (LSF) factor associated with path loss and shadow fading, and **H***mjk* captures the small-scale fading (SSF) matrix whose entries are independent and identically distributed (i.i.d.) random variables, according to (0, 1).

Subsequently, for the *l*th D2D pairs, the channel matrix between the DUE transmitter $DUE_{l'}^{Tx}$ and the receiver DUE_{l}^{Rx} , $G_{ll'}^{d} \in \mathbb{C}^{N_{D} \times N_{D}}$ can be given as follows

$$
\mathbf{G}_{ll'}^{\mathrm{d}} = \beta_{ll'}^{1/2} \mathbf{H}_{ll'},\tag{2}
$$

where $\beta_{ll'}$ stands for the LSF and the elements of random matrix, $\mathbf{H}_{ll'}$ of Rayleigh distribution denotes i.i.d. random variables $[\mathbf{H}_{ll'}]_{mn}$ ∼ CN (0, 1), [31], [32].

B. MMSE CHANNEL ESTIMATION

During the uplink training phase, the time division duplexing (TDD) mode is adopted. By exploiting the channel reciprocity, the downlink channel is typically obtained via estimating the uplink channel, which can be exploited to facilitate adaptive transmission for improving the system performance, without incurring a feedback overhead penalty. During the τ_c -length coherence interval, the τ_p -length orthogonal pilot sequences $\mathbf{E} \in \mathbb{C}^{\tau_p \times \tau_p}$ are allowed with $\mathbf{E}^H \mathbf{E} = \mathbf{I}_{\tau_p}$,

¹ In attention, all *JK* CFUEs are equally scattered into *J* groups and each CFUE only listens to a single group.

 $\tau_p \geq K + L N_D$. Here, the pilot sequence set used by CFUEs and DUEs are respectively given as $\Phi \in \Xi$ and $\Omega \subset \Xi$. Then the assigned pilots of CFUE_k and $DUE_{l'}^{Tx}$ are expressed $\Phi_j \in \mathbb{C}^{\tau_p \times N}$ and $\Omega_l \in \mathbb{C}^{\tau_p \times N_D}$.

1) FOR THE AP TO CFUE CHANNEL

To effectively reduce the limited pilot resource overhead, it is assumed that the same pilot sequence is assigned within each group of users as [19], [20], and [21]. Then, the received pilot signal at the *m*th AP is given as

$$
\mathbf{Y}_{p,m}^{\text{a}} = \sqrt{\tau_p \rho_p^{\text{c}}} \sum_{j=1}^{J} \sum_{k=1}^{K} \mathbf{G}_{mjk}^{\text{a}} \boldsymbol{\Phi}_j^H
$$

$$
+ \sqrt{\tau_p \rho_p^{\text{d}}} \sum_{l'=1}^{L} \mathbf{G}_{ml'}^{\text{a}} \boldsymbol{\Omega}_{l'}^H + \mathbf{W}_{p,m}^{\text{a}}, \tag{3}
$$

where ρ_p^c and ρ_p^d model the corresponding normalized signalto-noise ratio (SNR) of CFUE_k and DUE_I^{Tx}, respectively. Besides, $G_{ml'} \in \mathbb{C}^{N_A \times N_D}$ and $W_{p,m}^a \in \mathbb{C}^{N_A \times \tau_p}$ characterize the transmission channel from m th AP to l' th DUE $_{l'}^{Rx}$, and the additive white Gaussian noise (AWGN) at the *m*th AP.

Likewise, the received pilot signals at the DUE_l^{Rx} are as follows

$$
\mathbf{Y}_{p,l}^{d} = \sqrt{\tau_p \rho_p^c} \sum_{j=1}^{J} \sum_{k=1}^{K} \mathbf{G}_{lk}^{d} \boldsymbol{\Phi}_{j}^{H}
$$

$$
+ \sqrt{\tau_p \rho_p^d} \sum_{l'=1}^{L} \mathbf{G}_{ll'}^{d} \boldsymbol{\Omega}_{l'}^{H} + \mathbf{W}_{p,l}^{d}, \qquad (4)
$$

where the entries of AWGN $W_{p,l}^d$ are i.i.d. random variables as well, and $\mathbf{G}_{lk}^d \in \mathbb{C}^{N_D \times N}$ denotes the transmit channel for DUEs communication link.

Following the execution of the dispreading operation, in the following, the processed signal can be represented as [34]

$$
\mathbf{Y}_{p,mj}^{\text{a}} \triangleq \mathbf{Y}_{p,m}^{\text{a}} \boldsymbol{\Phi}_j
$$
\n
$$
= \sqrt{\tau_p \rho_p^{\text{c}}} \sum_{j'=1}^{J} \sum_{k'=1}^{K} \mathbf{G}_{mj'k'}^{\text{a}} \boldsymbol{\Phi}_j^H \boldsymbol{\Phi}_j
$$
\n
$$
+ \sqrt{\tau_p \rho_p^{\text{d}}} \sum_{l'=1}^{L} \mathbf{G}_{ml'}^{\text{a}} \boldsymbol{\Omega}_{l'}^H \boldsymbol{\Phi}_j + \mathbf{W}_{p,m}^{\text{a}} \boldsymbol{\Phi}_j
$$
\n
$$
= \sqrt{\tau_p \rho_p^{\text{c}}} \sum_{j'=1}^{J} \sum_{k'=1}^{K} \mathbf{G}_{mj'k'}^{\text{a}} \boldsymbol{\Phi}_j^H \boldsymbol{\Phi}_j + \widetilde{\mathbf{W}}_{p,mj}, \qquad (5)
$$

where $\widetilde{\mathbf{W}}_{p,mj} \triangleq \mathbf{W}_{p,m}^a \boldsymbol{\Phi}_j$ is composed of $N_A \times N$ i.i.d. components. Besides, assuming $\Omega_l^H \Phi_j = 0$ for eliminating the pilot coupling [31], [32].

Considering the huge hardware costs and energy consumption at AP, in this paper, the low-resolution ADCs are deployed as [6], [21], and [32]. For simplicity, the general additive quantization noise model (AQNM) is performed.

$$
\widetilde{\mathbf{Y}}_{\text{p},mj}^{\text{a}} = \lambda_m \mathbf{Y}_{\text{p},mj}^{\text{a}} + \widetilde{\mathbf{W}}_{\text{p},m} \n= \lambda_m \sqrt{\tau_p \rho_p^{\text{c}}} \sum_{j=1}^{J} \sum_{k=1}^{K} \mathbf{G}_{mjk}^{\text{a}} \boldsymbol{\Phi}_j^H \boldsymbol{\Phi}_j \n+ \lambda_m \widetilde{\mathbf{W}}_{\text{p},mj} + \widetilde{\mathbf{W}}_{\text{p},m},
$$
\n(6)

where λ_m , $\forall m$ represents the linear gain associated with the quantization bits b_m^{ADC} , and the covariance of the additive Gaussian quantization noise matrix $\widetilde{W}_{p,m}$ can be written as

$$
R_{\widetilde{\mathbf{W}}_{p,m}} \stackrel{\Delta}{=} \lambda_m (1 - \lambda_m) \operatorname{diag} \left(\left\{ \mathbf{Y}_{p,mj}^{\mathbf{a}} \left(\mathbf{Y}_{p,mj}^{\mathbf{a}} \right)^H \right\} \right)
$$

= $N_A \lambda_m (1 - \lambda_m)$

$$
\times \left(\tau_p \rho_p^{\mathbf{c}} \sum_{j'=1}^J \sum_{k'=1}^K \beta_{mj'k'} \left\| \boldsymbol{\Phi}_{j'}^H \boldsymbol{\Phi}_j \right\|^2 + \mathbf{I}_{\tau_p} \right). (7)
$$

Theorem 1: Following the MMSE, the estimated channel response $\widehat{\mathbf{G}}_{mjk}^{a}$ can be expressed as [35]

$$
\widehat{\mathbf{G}}_{mjk}^{\mathrm{a}} = \frac{\sqrt{\tau_{\mathrm{p}} \rho_{\mathrm{p}}^{\mathrm{c}} \beta_{mjk}}}{\tau_{\mathrm{p}} \rho_{\mathrm{p}}^{\mathrm{c}} \sum_{j'=1}^{J} \sum_{k'=1}^{K} \beta_{mjk'} \left\| \boldsymbol{\Phi}_{j'}^{H} \boldsymbol{\Phi}_{j} \right\|^{2} + \mathbf{I}_{N}} \widetilde{\mathbf{Y}}_{\mathrm{p},mj}^{\mathrm{a}}, \qquad (8)
$$

where $\mathbf{G}_{mjk} = \widehat{\mathbf{G}}_{mjk} + \mathbf{E}_{mjk}$, in which \mathbf{E}_{mjk} denotes the channel estimation error.

For notational compactness, the covariance of the entries of term $\widehat{\mathbf{G}}_{mjk}^a$ can be accordingly given by, mathematically

$$
\gamma_{mjk} \stackrel{\Delta}{=} \mathbb{E}\left\{\left|\left[\widehat{\mathbf{G}}_{mjk}^{a}\right]_{m,n}\right|^{2}\right\} = \frac{\lambda_{m}\tau_{p}\rho_{p}^{c}\beta_{mjk}^{2}}{\tau_{p}\rho_{p}^{c}\sum\limits_{k'=1}^{K}\beta_{mjk'}+1}.
$$
 (9)

With reference to [19] and [21], as such, in principle the estimated matrix \widehat{G}_{mjk}^a can be re-expressed as

$$
\widehat{\mathbf{G}}_{mjk}^{\mathrm{a}} \stackrel{\Delta}{=} \gamma_{mjk}^{1/2} \mathbf{Z}_{mj}^{\mathrm{a}},\tag{10}
$$

where $\mathbb{Z}_{mj}^{\text{a}}$ stands for the beamforming matrix which can be expressed as $\left[\mathbf{Z}_{mj}^{\text{a}}\right]_N \sim \mathcal{CN}\left(0,\mathbf{I}_{N_{\text{A}}}\right)$. *Proof 1:* See Appendix A.

2) FOR THE DUE TO DUE CHANNEL

Without loss of generality, for D2D links, DUE_l^{Rx} performs despreading operation to estimate $G_{ll'}$, which can be rewritten as

$$
\widetilde{\mathbf{Y}}_{\mathrm{p},ll}^{\mathrm{d}} \triangleq \mathbf{Y}_{\mathrm{p},l}^{\mathrm{d}} \mathbf{\Omega}_{l} = \sqrt{\tau_{\mathrm{p}} \rho_{\mathrm{p}}^{\mathrm{d}}} \sum_{l'=1}^{L} \mathbf{G}_{ll'}^{\mathrm{d}} \mathbf{\Omega}_{l'l} + \mathbf{W}_{\mathrm{p},l}^{\mathrm{d}} \mathbf{\Omega}_{l}, \quad (11)
$$

where $\Omega_{l'l}$ is defined as $\Omega_{l'l} \triangleq \Omega_{l'}^H \Omega_l$.

Guided by the above consideration as Theorem 1, consequently, the estimated D2D channel matrix $\widehat{G}_{ll'}^{d}$ can be expressed as

$$
\widehat{\mathbf{G}}_{ll'}^{\mathrm{d}} = \widetilde{\mathbf{Y}}_{\mathrm{p},ll'}^{\mathrm{d}} \mathbf{C}_{ll'},\tag{12}
$$

where C_{ll} is specified as

$$
\mathbf{C}_{ll'} = \frac{\sqrt{\tau_p \rho_p^d} \beta_{ll}^d}{\tau_p \rho_p^d \sum_{l'=1}^L \beta_{ll'}^d \mathbf{\Omega}_{l'l}^H \mathbf{\Omega}_{l'l} + \mathbf{I}_{N_D}}.
$$
 (13)

C. DOWNLINK DATA TRANSMISSION

In this phase, we consider implementing the linear CB precoder at AP to separate the signals sent by multiple users thanks to its implementation simplicity. Then the emitted signal at the *m*th AP is given as [1], [2],

$$
\mathbf{x}_{m}^{\text{a}} = \sqrt{\rho^{\text{a}}} \sum_{j=1}^{J} \sum_{k=1}^{K} \eta_{mjk}^{1/2} \mathbf{Z}_{mj}^{\text{a}} \mathbf{q}_{j},
$$
(16)

where ρ^a stands for the maximum transmitted power of AP, η_{mjk} denotes the power distribution coefficient, and q_j represents the desired independent multicast Gaussian signal for the *j*th multicast group, which following $\mathbb{E}\left\{\mathbf{q}_j\mathbf{q}_j^H\right\} = \mathbf{I}_N$.

To elaborate on the signal processing at the AP and considering the fact that the low-resolution DACs are deployed, by virtue of [\(16\)](#page-4-0), the quantized signal after processing is given as

$$
\widetilde{\mathbf{x}}_m^{\mathbf{a}} = \alpha_m \mathbf{x}_m^{\mathbf{a}} + \widetilde{\mathbf{n}}_m
$$
\n
$$
= \sqrt{\rho^{\mathbf{a}}} \alpha_m \sum_{j=1}^J \sum_{k=1}^K \eta_{mjk}^{1/2} \mathbf{Z}_{mj}^{\mathbf{a}} \mathbf{q}_j + \widetilde{\mathbf{n}}_m, \qquad (17)
$$

where α_m refers to the linear gain decided by the quantification bits b_m^{DAC} and $\tilde{\mathbf{n}}_m$ describes the additive Gaussian quantization noise. Furthermore, α_m and $\tilde{\mathbf{n}}_m$ are independent of each other and $\tilde{\mathbf{n}}_m$ follows Gaussian-distribution with zero means [31] and [32].

Referring to the derivation process as [7] and [36], the covariance matrix of $\tilde{\mathbf{n}}_m$ can be denoted by

$$
R_{\tilde{\mathbf{n}}_m} \stackrel{\Delta}{=} \alpha_m (1 - \alpha_m) \operatorname{diag} \left(\mathbb{E} \left\{ \mathbf{x}_m^a (\mathbf{x}_m^a)^H \right\} \right)
$$

= $N \rho^a \alpha_m (1 - \alpha_m) \sum_{j=1}^J \left(\sum_{k=1}^K \eta_{mjk}^{1/2} \right)^2 \mathbf{I}_{N_A}.$ (18)

To meet the power constraint of each AP, i.e., $\mathbb{E}\left\{\left\|\widetilde{\mathbf{x}}_{m}^{\mathrm{a}}\right\| \right\}$ $\left\{ \frac{2}{5}\right\} \leq \rho^a$, the power constraint can be written as

$$
\mathbb{E}\left\{\|\widetilde{\mathbf{x}}_{m}^{\mathrm{a}}\|^{2}\right\} = N_{\mathrm{A}}N\rho^{\mathrm{a}}\alpha_{m}^{2} \sum_{j=1}^{J} \left(\sum_{k=1}^{K} \eta_{mjk}^{1/2}\right)^{2} + N_{\mathrm{A}}N\rho^{\mathrm{a}}\alpha_{m} (1 - \alpha_{m}) \sum_{j=1}^{J} \left(\sum_{k=1}^{K} \eta_{mjk}^{1/2}\right)^{2} = N_{\mathrm{A}}N\rho^{\mathrm{a}}\alpha_{m} \sum_{j=1}^{J} \left(\sum_{k=1}^{K} \eta_{mjk}^{1/2}\right)^{2}.
$$
 (19)

Using these notations and further simplifying, we can obtain

$$
\sum_{j=1}^{J} \left(\sum_{k=1}^{K} \eta_{mjk}^{1/2} \right)^2 \le \frac{1}{\alpha_m N_A N}.
$$
 (20)

For the D2D links, similarly, it is assumed that the MRT precoder is used in DUE_l^{Tx} , the emitted signal \mathbf{x}_l^d is also given by [16], [28]

$$
\mathbf{x}_l^{\mathrm{d}} = \sqrt{\rho^{\mathrm{d}} u_l} \widehat{\mathbf{G}}_{ll}^{\mathrm{d}} \mathbf{s}_l,\tag{21}
$$

where ρ^d is the maximum SNR of the *l*th DUE transmitter, u_l denotes the power allocation coefficient, and s_l represents the desired Gaussian signal for the *l*th DUE receiver, which following $\mathbb{E}\left\{\mathbf{s}_l\mathbf{s}_l^H\right\} = \mathbf{I}_{N_\text{D}}$. To satisfy the power constraint of each DUE, $\mathbb{E}\left\{\|\mathbf{x}_l^{\text{d}}\|$ $\left\{ \frac{1}{2} \right\} \leq \rho^d$, it can be rewritten as

$$
\mathbb{E}\left\{\left\|\mathbf{x}_{l}^{\mathrm{d}}\right\|^{2}\right\} = \rho^{\mathrm{d}}u_{l}\mathbb{E}\left\{\tau_{p}\rho_{p}^{\mathrm{d}}\left(\beta_{ll}^{\mathrm{d}}\right)^{2}\mathbf{\Omega}_{l'l}\mathbf{C}_{ll}\mathbf{C}_{ll}^{H}\mathbf{\Omega}_{l'l}^{H}\right\} \n= \rho^{\mathrm{d}}N_{\mathrm{D}}u_{l}\mathrm{tr}\left(\mathbf{\Gamma}_{ll}\right),
$$
\n(22)

where Γ_{ll} can be expressed as

$$
\mathbf{\Gamma}_{ll} \stackrel{\Delta}{=} \sqrt{\tau_p \rho_p^d} \beta_{ll}^d \mathbf{C}_{ll'}.
$$
 (23)

Therefore, we have

$$
\text{tr}\left(\mathbf{\Gamma}_{ll}\right) \le \frac{1}{\mu_l N_{\text{D}}}.\tag{24}
$$

Mathematically, the received signal for the *k*th CFUE in the *j*th group can be given by [29]

$$
\mathbf{r}_{jk}^{\mathrm{c}} = \sum_{m=1}^{M} \left(\mathbf{G}_{mjk}^{\mathrm{a}}\right)^{H} \widetilde{\mathbf{x}}_{m}^{\mathrm{a}} + \sum_{l=1}^{L} \left(\mathbf{G}_{lk}^{\mathrm{d}}\right)^{H} \mathbf{x}_{l}^{\mathrm{d}} + \mathbf{n}_{jk}, \quad (25)
$$

$$
R_{jk}^{\rm c} = N \log_2 \left(1 + \frac{\left(N_{\rm A} \sqrt{\rho_{\rm d}^{\rm a}} \sum_{m=1}^{M} \sum_{k'=1}^{K} \eta_{mj'k'}^{1/2} \gamma_{mjk}^{1/2} \right)^2}{\sum_{m=1}^{M} \sum_{k'=1}^{K} \sum_{m'=1}^{K} \gamma_{mj'k'}^{2/2} \gamma_{mjk}^{1/2}} \right), \tag{14}
$$

$$
\rho_{\rm d}^{\rm a} NN_{\rm A} \sum_{m=1}^{M} \sum_{k'=1}^{K} \sum_{k''=1}^{K} \alpha_m^2 \beta_{mjk} \eta_{mjk'}^{1/2} \eta_{mjk''}^{1/2} + \Theta_{mj} + N_{\rm D}^2 \sum_{l=1}^{L} \mu_l \beta_{lk}^{\rm d} \text{tr}(\mathbf{\Gamma}_{ll}) + 1
$$

$$
\Theta_{mj} = \rho_{\rm d}^{\rm a} NN_{\rm A} \sum_{m=1}^{M} \sum_{j=1}^{J} \alpha_m (1 - \alpha_m) \beta_{mjk} \left(\sum_{k'=1}^{K} \eta_{mjk'}^{1/2} \right)^2 - \left(N_{\rm A} \sqrt{\rho_{\rm d}^{\rm a}} \sum_{m=1}^{M} \sum_{k'=1}^{K} \alpha_m \eta_{mjk'}^{1/2} \gamma_{mjk}^{1/2} \right)^2.
$$
 (15)

where \mathbf{n}_{jk} indicates the AWGN satisfying $\mathbf{n}_{jk} \sim \mathcal{CN}(\mathbf{0}, \mathbf{I}_N)$.

Guided by the preceding consideration, the received signal at *l* th receiver DUE_l^{Rx} is formulated as

$$
\mathbf{r}_{l}^{\mathrm{d}} = \sum_{m=1}^{M} \left(\mathbf{G}_{ml}^{\mathrm{a}}\right)^{H} \widetilde{\mathbf{x}}_{m}^{\mathrm{a}} + \sum_{l'=1}^{L} \left(\mathbf{G}_{l'l}^{\mathrm{d}}\right)^{H} \mathbf{x}_{l'}^{\mathrm{d}} + \mathbf{n}_{l},\qquad(26)
$$

where \mathbf{n}_l is additive noise, $\mathbf{n}_l \sim \mathcal{CN}(\mathbf{0}, \mathbf{I}_{N_D})$.

III. ANALYSIS METHODOLOGY OF ACHIEVABLE RATE

Based on the preceding evolution, in this section, the expected rate analysis of both CFUEs and DUEs is performed as follows, which primarily through the use of a general bounding technique [19], [37].

A. ACHIEVABLE DOWNLINK RATE OF CFUEs

Based on the derived results as (17) and (25) , it can be rewritten as

$$
\mathbf{r}_{jk}^{\mathrm{c}} = \underbrace{\sqrt{\rho^{\mathrm{a}}}\sum_{m=1}^{M}\sum_{j=1}^{J}\sum_{k=1}^{K} \alpha_{m} \eta_{mjk}^{1/2} (\mathbf{G}_{mjk}^{\mathrm{a}})^{H} \mathbf{Z}_{mj}^{\mathrm{a}} \mathbf{q}_{j}}_{\mathbf{H}_{jk}} + \underbrace{\sqrt{\rho^{\mathrm{d}}}\sum_{l=1}^{L} \sqrt{u_{l}} (\mathbf{G}_{lk}^{\mathrm{d}})^{H} \mathbf{\widehat{G}}_{ll}^{\mathrm{d}} \mathbf{s}_{l}}_{\mathbf{H}_{m+1}} + \sum_{m=1}^{M} (\mathbf{G}_{mjk}^{\mathrm{a}})^{H} \mathbf{\widetilde{n}}_{m} + \mathbf{n}_{jk}.
$$
 (29)

Capitalizing on the received signal \mathbf{r}^c_{jk} and side information $\bar{\mathbf{H}}_{jk}$ [19], [21], [26], [32], [38], the achievable downlink rate of *k*th CFUE in the *j*th group can be obtained as

$$
R_{jk}^{\rm c} = \log_2 \left| \mathbf{I}_N + \bar{\mathbf{H}}_{jk}^H \left(\bar{\boldsymbol{\Psi}}_{jk}^{\rm c} \right)^{-1} \bar{\mathbf{H}}_{jk} \right|, \tag{30}
$$

where $\bar{\mathbf{H}}_{jk}$ and $\bar{\mathbf{\Psi}}_{jk}^{\mathrm{c}}$ can be respectively denoted by

$$
\bar{\mathbf{H}}_{jk} \stackrel{\Delta}{=} \mathbb{E}\left\{\mathbf{H}_{jk}\right\} = \mathbb{E}\left\{\sqrt{\rho_{\rm d}^{\rm a}}\sum_{m=1}^{M}\sum_{k'=1}^{K} \alpha_m \eta_{mjk'}^{1/2} \mathbf{G}_{mjk}^{\rm a} \mathbf{Z}_{mj}^{\rm a}\right\},\tag{31}
$$

and

i

$$
\bar{\Psi}_{jk}^{\rm c} \triangleq \mathbb{E}\left\{\rho_{\rm d}^{\rm a}\sum_{m=1}^{M}\sum_{n=1}^{N}\sum_{j'=1}^{J}\sum_{k'=1}^{K}\sum_{k''=1}^{K}\alpha_{m}\alpha_{n}\eta_{m'j'k'}^{1/2}\eta_{njk''}^{1/2}\right\}
$$

$$
\times \left(\mathbf{G}_{mjk}^{\mathbf{a}}\right)^{H} \mathbf{Z}_{mj'}^{\mathbf{a}} \left(\mathbf{Z}_{nj'}^{\mathbf{a}}\right)^{H} \mathbf{G}_{njk}^{\mathbf{a}} + \mathbf{I}_{N} \n+ \rho^{d} \sum_{l=1}^{L} \mu_{l} \left(\mathbf{G}_{lk}^{\mathbf{d}}\right)^{H} \widehat{\mathbf{G}}_{ll}^{\mathbf{d}} \left(\widehat{\mathbf{G}}_{ll}^{\mathbf{d}}\right)^{H} \mathbf{G}_{lk}^{\mathbf{d}} \n+ \sum_{m=1}^{M} \left(\mathbf{G}_{mjk}^{\mathbf{a}}\right)^{H} \widetilde{\mathbf{n}}_{m} \widetilde{\mathbf{n}}_{m}^{H} \mathbf{G}_{mjk}^{\mathbf{a}} - \bar{\mathbf{H}}_{jk} \bar{\mathbf{H}}_{jk}^{H} \right\}.
$$
\n(32)

Theorem 2: Using the central-limit theorem and capacity bounding technique from [1] and [10], in the following, we give the lower bound on the achievable rate for the *k*th CFUE in the *j*th group by skipping tedious derivation which can be given as [\(14\)](#page-4-3), shown at the bottom of the previous page.

Proof 2: See Appendix B.

B. ACHIEVABLE DOWNLINK RATE OF DUEs

With the preceding in mind, the received signal \mathbf{r}_l^d in [\(26\)](#page-5-0) can be rewritten as [38]

$$
\mathbf{r}_{l}^{\mathrm{d}} = \underbrace{\sqrt{\rho^{\mathrm{d}} \sum_{l'=1}^{L} \sqrt{\mu_{l'}} \left(\mathbf{G}_{l'l}^{\mathrm{d}}\right)^{H} \mathbf{\widehat{G}}_{l'l'}^{\mathrm{d}} \mathbf{q}_{l'}}}_{\mathbf{S}_{l'l'} + \underbrace{\sqrt{\rho^{\mathrm{a}} \sum_{m=1}^{M} \sum_{j=1}^{J} \sum_{k=1}^{K} \alpha_{m} \eta_{mjk}^{1/2} (\mathbf{G}_{ml}^{\mathrm{a}})^{H} \mathbf{Z}_{mj}^{\mathrm{a}} \mathbf{q}_{j}}}_{\mathbf{m} = 1} + \sum_{m=1}^{M} \left(\mathbf{G}_{ml}^{\mathrm{a}}\right)^{H} \mathbf{\widetilde{n}}_{m} + \mathbf{n}_{l}. \tag{34}
$$

As a result, the achievable downlink rate of *l*th DUE receiver is given by

$$
R_l^{\rm d} = \log_2 \left| \mathbf{I}_{N_{\rm D}} + \bar{\mathbf{S}}_l^H \left(\bar{\boldsymbol{\Psi}}_l^{\rm d} \right)^{-1} \bar{\mathbf{S}}_l l \right|, \tag{35}
$$

where $\bar{\mathbf{S}}_{ll}$ and $\bar{\mathbf{\Psi}}_{l}^{\text{d}}$ $\frac{d}{dt}$ can be respectively expressed as follows

$$
\bar{\mathbf{S}}_{ll} \stackrel{\Delta}{=} N_{\mathbf{D}} \sqrt{\rho^{\mathbf{d}} \mu_l} \mathbf{\Gamma}_{ll},\tag{36}
$$

and

$$
\mathbf{\bar{\Psi}}_{l}^{\text{d}} = \rho^{\text{d}} N_{\text{D}}^{2} \sum_{l^{\prime}\neq l}^{L} \mu_{l^{\prime}} \left(\beta_{l^{\prime}l}^{\text{d}} \middle/ \beta_{l^{\prime}l^{\prime}}^{\text{d}}\right)^{2} \text{tr}\left(\|\mathbf{\Omega}_{ll^{\prime}} \mathbf{\Gamma}_{l^{\prime}l^{\prime}}\|^{2}\right) \mathbf{I}_{N_{\text{D}}}
$$

$$
R_{l}^{\text{d}} = N_{\text{D}} \log_{2} \left(1 + \frac{\rho^{\text{d}} N_{\text{D}}^{2} \mu_{l} \text{tr} \left(\left\| \mathbf{\Gamma}_{ll} \right\|^{2} \right)}{\rho^{\text{d}} N_{\text{D}}^{2} \sum_{l' \neq l}^{L} \mu_{l'} \left(\beta_{l'l}^{\text{d}} / \beta_{l'l'}^{\text{d}} \right)^{2} \text{tr} \left(\left\| \mathbf{\Omega}_{ll'} \mathbf{\Gamma}_{l'l'} \right\|^{2} \right) + \Delta_{l} + \rho^{\text{a}} N_{\text{A}} \sum_{m=1}^{M} \sum_{j=1}^{K} \sum_{k=1}^{K} \alpha_{m} \eta_{mjk} \beta_{ml}^{a} + 1} \right), \tag{27}
$$
\n
$$
\Delta_{l} = \rho^{\text{d}} N_{\text{D}} \sum_{l'=1}^{L} \mu_{l'} \beta_{l'l}^{\text{d}} \left(\tau_{\text{p}} \rho_{\text{p}}^{\text{d}} \beta_{l'l'}^{\text{d}} \text{tr} \left(\left\| \mathbf{\Omega}_{ll'} \mathbf{C}_{l'l'} \right\|^{2} \right) + \left(\sum_{l'' \neq l}^{L} \beta_{l'l''}^{\text{d}} + 1 \right) \text{tr} \left(\left\| \mathbf{\Omega}_{l'} \mathbf{C}_{l'l'} \right\|^{2} \right) \right). \tag{28}
$$

$$
+ \rho^d N_D \sum_{l'=1}^{L} \mu_{l'} \beta_{l'l}^d \left(\tau_p \rho_p^d \beta_{l'l}^d \text{tr} \left(\|\mathbf{\Omega}_{ll'} \mathbf{C}_{l'l'}\|^2 \right) \right) + \left(\sum_{l'' \neq l}^{L} \beta_{l'l''}^d + 1 \right) \text{tr} \left(\|\mathbf{\Omega}_{l'} \mathbf{C}_{l'l'}\|^2 \right) \right) \mathbf{I}_{N_D} + \rho^a N_A \sum_{m=1}^{M} \sum_{j=1}^{J} \sum_{k=1}^{K} \alpha_m \eta_{mjk} \beta_{ml}^a \mathbf{I}_{N_D} + \mathbf{I}_{N_D}. \tag{37}
$$

Theorem 3: Using the random matrix theory, the lower bound on the achievable rate for the *l*th DUE receiver can be given as [\(27\)](#page-5-1), shown at the bottom of the previous page.

Proof 3: Following a similar derivation as in the case of Theorem 2, Theorem 3 can be derived.

C. ASYMPTOTIC RATE ANALYSIS OF DUEs

Next, we then provide some insights into the achievable downlink rate of DUEs when *M* is very large, in this subsection. Based on the received signal for the *k*th CFUE in the *j*th group can be given by [\(29\)](#page-5-2), we have

$$
\mathbf{r}_{jk}^{\mathrm{c}} = \underbrace{\sqrt{\rho^{\mathrm{a}} \sum_{m=1}^{M} \sum_{j=1}^{J} \sum_{k=1}^{K} \alpha_{m} \eta_{mjk}^{1/2} (\mathbf{G}_{mjk}^{\mathrm{a}})^{H} \mathbf{Z}_{mj}^{\mathrm{a}} \mathbf{q}_{j}}^{\mathrm{D}S_{k}}}_{\text{DS}_{k}} + \underbrace{\sqrt{\rho^{\mathrm{d}} \sum_{l=1}^{L} \sqrt{u_{l}} (\mathbf{G}_{lk}^{\mathrm{d}})^{H} \mathbf{\widehat{G}}_{ll}^{\mathrm{d}} \mathbf{s}_{l}}^{\mathrm{D}U_{k}}}_{\mathrm{D}U_{k}} + \sum_{m=1}^{M} (\mathbf{G}_{mjk}^{\mathrm{a}})^{H} \mathbf{\widetilde{n}}_{m} + \mathbf{n}_{jk}, \qquad (38)
$$

where DS_k and DUI_k denote the desired signal and interference signal, respectively. By using the term $\mathbf{G}^{\text{a}}_{mjk} = \widehat{\mathbf{G}}^{\text{a}}_{mjk} + \widehat{\mathbf{G}}^{\text{a}}_{mjk}$ \mathbf{E}_{mjk}^a , we have

$$
\left(\mathbf{G}_{mjk}^{\mathrm{a}}\right)^{H}\mathbf{Z}_{mj}^{\mathrm{a}}=\gamma_{mjk}^{1/2}\left(\mathbf{Z}_{mj}^{\mathrm{a}}\right)^{H}\mathbf{Z}_{mj}^{\mathrm{a}}=\gamma_{mjk}^{1/2}N\mathbf{I}_{N_{\mathrm{A}}},\qquad(39)
$$

and

$$
\left(\mathbf{G}_{lk}^{\mathrm{d}}\right)^{H}\widehat{\mathbf{G}}_{ll}^{\mathrm{d}} = \frac{\tau_{\mathrm{p}}\rho_{\mathrm{p}}^{\mathrm{d}}\beta_{lk}^{1/2}\beta_{ll}^{1/2}\sum\limits_{l'=1}^{L}\beta_{ll'}^{\mathrm{d}}\mathbf{\Omega}_{l'l}}{\tau_{\mathrm{p}}\rho_{\mathrm{p}}^{\mathrm{d}}\sum\limits_{l'=1}^{L}\beta_{ll'}^{\mathrm{d}}\mathbf{\Omega}_{l'l'}^{\mathrm{H}}\mathbf{\Omega}_{ll} + \mathbf{I}_{N_{\mathrm{D}}}}.
$$
(40)

By using Tchebyshev's theorem as shown in [39], we have

$$
\frac{1}{M} {\rm DS}_k - \frac{1}{M} \sqrt{\rho^a} \sum_{m=1}^M \sum_{j=1}^J \sum_{k=1}^K \alpha_m \eta_{mjk}^{1/2} N \gamma_{mjk}^{1/2} \mathbf{I}_{N_A} \mathbf{q}_j
$$

and

 $\xrightarrow{a.s.} M \rightarrow \infty$

$$
\frac{1}{M}DUI_k - \frac{1}{M} \frac{\tau_p \rho_p^d \beta_{lk}^{1/2} \beta_{ll}^{1/2} \sum\limits_{l'=1}^L \beta_{ll'}^d \Omega_{l'l}}{\tau_p \rho_p^d \sum\limits_{l'=1}^L \beta_{ll'}^d \Omega_{l'l'}^H \Omega_{ll} + I_{N_D}} \xrightarrow[M \to \infty]{} 0.
$$
\n(42)

0, (41)

Combining [\(41\)](#page-6-0) and [\(42\)](#page-6-1), therefore, the asymptotic analysis for the *k*th CFUE in the *j*th group can be given as follows [\(33\)](#page-6-2), shown at the bottom of the page.

IV. ACHIEVABLE DOWNLINK SUM EE

In light of [21] and [32], the achievable downlink sum EE can be defined as follows

$$
\eta_{\rm EE} \stackrel{\Delta}{=} \frac{B \times R_{\rm sum}}{P_{\rm sum}},\tag{43}
$$

where the sum rate of the system under consideration can be given as

$$
R_{\text{sum}} = \sum_{j=1}^{J} \sum_{k=1}^{K} R_{jk}^{c} + \sum_{l=1}^{L} R_{l}^{d}, \qquad (44)
$$

where $L = D^2 \lambda_d$ denotes the average number of $DUE_{l'}^{Rx}$. Furthermore, R_{jk}^c and R_l^d are respectively given by [\(14\)](#page-4-3) and [\(27\)](#page-5-1). In addition, the λ_d denotes the DUEs' density obeying independent homogeneous Poisson point process (PPP). Furthermore, D^2 represents $D \times D$ coverage area where *M* APs, $J \times K$ CFUEs, and *L* DUE pairs are distributed as uniformly scattered.

The sum power consumption of the considered downlink D2D underlaid multigroup multicast cell-free massive MIMO systems with multi-antenna users can be modeled by

$$
P_{\text{sum}} = \sum_{m=1}^{M} P_m + \sum_{l=1}^{L} P_l + \sum_{m=1}^{M} (B \cdot R_{\text{sum}} \cdot P_{\text{bt},m} + P_{0,m}),
$$
\n(45)

where *B* represents the system bandwidth, P_m , P_l , P_{bt_m} , and $P_{0,m}$ are the power costs at *m*th AP and *l*th $DUE_l^{\{Rx\}}$, the traffic-fronthaul power associated with the *m*th AP, and the fixed power consumption per fronthual link, respectively. To be more specific, the term P_m can be written as

$$
P_m = N_A \cdot P_{\text{tc},m} + \frac{1}{\delta_m} \rho_{\text{d}}^a N_0 \left(\alpha_m N N_A \sum_{j=1}^J \left(\sum_{k=1}^K \eta_{mjk}^{1/2} \right)^2 \right), \tag{46}
$$

$$
\frac{1}{M}\mathbf{r}_{jk}^{\mathrm{c}} - \frac{1}{M} \left(\sqrt{\rho^{a}} \sum_{m=1}^{M} \sum_{j=1}^{J} \sum_{k=1}^{K} \alpha_{m} \eta_{mjk}^{1/2} N \gamma_{mjk}^{1/2} \mathbf{I}_{N_{\mathrm{A}}} \mathbf{q}_{j} + \frac{\tau_{\mathrm{p}} \rho_{\mathrm{p}}^{d} \beta_{lk}^{1/2} \beta_{ll}^{1/2} \sum_{l'=1}^{L} \beta_{ll'}^{d} \mathbf{\Omega}_{l'l}}{\tau_{\mathrm{p}} \rho_{\mathrm{p}}^{d} \sum_{l'=1}^{L} \beta_{ll'}^{d} \mathbf{\Omega}_{l'l}^{H} \mathbf{\Omega}_{ll} + \mathbf{I}_{N_{\mathrm{D}}} } \right) \xrightarrow{a.s.} \mathbf{0.}
$$
\n(33)

where $0 \leq \delta_m \leq 1$ stand for the power amplifier efficiency, and the noise power. Besides, the power consumption at *m*th AP, $P_{tc,m}$, can be described as

$$
P_{\text{tc},m} = N_{\text{A}} \left(c_{\text{ADC},m} P_{\text{AGC},m} + P_{\text{ADC},m} \right) + N_{\text{A}} \cdot P_{\text{res},m}
$$

$$
+ N_{\text{A}} \left(c_{\text{ADC},m} P_{\text{AGC},m} + P_{\text{DAC},m} \right), \quad (47)
$$

where $P_{\text{AGC},m}$ and $P_{\text{res},m}$ represent the power consumption of the automatic generation control (AGC) and the residual components at the *m*th AP. Additionally, the $P_{ADC,m}$ and *P*_{DAC,*m*} can be denoted by

$$
P_{\text{ADC},m} = \frac{3V_{\text{dd}}^2 L_{\text{min}} \left(2B + f_{\text{cor}}\right)}{10^{-0.1525 b_m^{\text{ADC}} + 4.838}},\tag{48}
$$

and

$$
P_{\text{DAC}, m} = \frac{1}{2} V_{\text{dd}} I_0 \left(2^{b_m^{\text{DAC}}} - 1 \right) + b_m^{\text{DAC}} C_p \left(2B + f_{\text{cor}} \right) V_{\text{dd}}^2,\tag{49}
$$

where V_{dd} , C_p , f_{cor} , and I_0 remark the power supply of converter, the parasitic capacitance of each switch in converter, the corner frequency of the $1/f$, and the unit current source related to the least significant bit (LSB) is limited by the noise floor and device mismatch, respectively.

Moreover, the $c_{ADC,m}$ and $c_{DAC,m}$ indicate the sign associated with the low-resolution ADC/DAC precision $b_m^{\text{ADC}}/b_m^{\text{DAC}}$, which can be specified as

$$
c_{\text{ADC/DAC},m} = \begin{cases} 0, & b_m^{\text{ADC}}/b_m^{\text{DAC}} = 1\\ 1, & b_m^{\text{ADC}}/b_m^{\text{DAC}} > 1. \end{cases}
$$
(50)

Plugging the equations [\(46\)](#page-6-3)-[\(50\)](#page-7-0) into [\(45\)](#page-6-4), and combining [\(43\)](#page-6-5)-[\(44\)](#page-6-6), the sum EE can be obtained after several simple algebraic calculations.

V. SIMULATION RESULTS

In this section, the performance analysis of the derived results is evaluated to verify our analytical result and evaluate the performance of D2D underlaid multigroup multicast cell-free massive MIMO for multi-antenna at both the APs and users, as well as other key parameters.

A. PARAMETERS SETUPS

In this paper, we primarily focus on the scenario with $JK =$ 10 CFUEs, $N_D = 2$ antennas of DUEs. All APs and CFUEs are uniformly and randomly scattered in the square area of 1 [km²]. For the sake of analysis, we assume $\lambda_m = \alpha_m =$ 5, ∀*m*. This area is also wrapped around to avoid the boundary effects as well. We only consider the effect of low-resolution DACs due to the fact that the uplink estimation is very similar to the downlink transmission. Besides, the DUEs are represented as an independent homogeneous PPP with the density λ_d and the three-slope path loss model is adopted. Unless specifically mentioned, the other parameters setups are given as in [7], [21], and [32].

FIGURE 2. Achievable downlink sum rate versus the number of APs for different K, with $L = 10$, $N_D = 2$.

FIGURE 3. Achievable downlink sum rate versus the number of antennas of each CFUEs, with $N_A = 5, N = 2$.

B. PERFORMANCE EVALUATION

First, the achievable downlink sum rate versus the number of APs for different *K* are exhibited in Fig. [2,](#page-7-1) with $L =$ $10, N_D = 2$. Note that, all Simulated Results are based on (30) , (35) and obtained by averaging over $10⁴$ independent channel realizations, while the Analytical Results are generated according to [\(14\)](#page-4-3), [\(27\)](#page-5-1). As can be readily observed, due to the interference and estimation error, the relative performance gaps of the achievable sum rate are marginal, confirming the accuracy of our analytical finding.

Next, we depict the achievable downlink sum rate versus the number of antennas of each CFUE in Fig. [3,](#page-7-2) where $N_A =$ $5, N = 2$. From the results we can know that the achievable sum rate for the multicast multigroup configuration $J =$ 2, $K = 5$ precedes the one of the unicast $J = 1, K = 10$. The results show that the achievable sum rate behaves differently in scenarios with a low and high number of antennas of CFUEs. To be more specific, when the antennas of each CFUE are lower than the optimal value, the achievable sum rate increases with it consensually grows and vice versa. This fully demonstrates the significant benefits of the multigroup

FIGURE 4. Achievable sum rate of CFUEs versus the number of APs, with $L = 10, N_D = 2.$

FIGURE 5. Achievable downlink sum rate versus the DAC quantization bits, with $N_A = 20$, $N_D = 2$.

multicast strategy in D2D underlaid cell-free massive MIMO systems.

In Fig. [4,](#page-8-0) the achievable sum rate of CFUEs versus the number of APs is given, where $L = 10, N_D = 2$. It shows that the sum rate of CFUEs increases with the number of APs. The reason for this is that having a large numbers of APs allows for more favorable channels and excellent channel hardening performance. Despite this, the greater the number of the AP antennas, the greater the multiplexing gain and spatial freedom for the system.

Fig. [5](#page-8-1) describes the achievable downlink sum rate against the DAC quantization bits, with $N_A = 20$, $N_D = 2$. As the obtained results despited in Fig. 2, the achievable sum rate for the multicast multigroup precedes the one of the unicast both for the antennas of APs of $N = 2$ and $N = 1$. Besides, we also can obtain that with the DAC quantization bits increases, the achievable sum rate can be improved with the fact that the corresponding quantization noise decrease when $b_m^{\text{DAC}} \leq 5$; while as further increases, the sum rate for different configurations all grows slowly and eventually converges to each capacity limit.

FIGURE 6. Achievable downlink CFUEs rate versus the number of CFUEs, with $L = 10, N = 2$.

FIGURE 7. Achievable downlink sum rate versus the DUE densities, with $N_A = 20, JK = 10.$

In Fig. [6,](#page-8-2) the achievable downlink rate of CFUEs versus the number of CFUEs is presented, with $L = 10, N = 2$. For the current simulation setup, we can see that the rate of CFUEs decreases as the number of the CFUEs increases. The reason for this is that large amounts of DUEs and CUEs will cause serious interference such as pilot contamination, CFUEs-DUEs, DUEs-DUEs, and CFUEs-DUEs, thus deteriorating the performance of the considered system.

In Fig. [7,](#page-8-3) the achievable downlink sum rate against the DUE densities is plotted, with $N_A = 20$, $JK = 10$. With the derived results we can deduce from the sum rate increases nearly linearly with the density of DUEs. It fully illustrates the enormous benefits of D2D communication underlaid to improve the sum SE of the system. To be more specific, using multiple antennas at DUEs can also sharply boost the system performance.

In Fig. [8,](#page-9-0) the achievable downlink sum rate versus the number of antennas at each AP, with $N = 2$, $N_D = 2$, is provided. We see that increasing the number of antennas of each AP can effectively improve the achievable the sum rate. The reason is that the more APs deployed, the more favorable

FIGURE 8. Achievable downlink sum rate versus the number of antennas at each AP, with $N = 2$, $N_D = 2$.

FIGURE 9. Achievable downlink sum EE versus the number of APs, with $L = 10, N_D = 2.$

of the transmission channel and thus the more obvious the channel hardening. To be specific, the diversity gain and multiplexing gain can be obtained by the light of nature. Furthermore, as despited in Figs. [6](#page-8-2) and [7,](#page-8-3) the achievable sum rate can be improved by increasing the density of DUEs.

Up till now, the achievable sum rate for the considered D2D underlaid multigroup multicast cell-free massive MIMO with multi-antenna users has been explored. Next, the performance of sum EE is then exhibited. In Fig. 9, the effects of the achievable sum EE against the number of the APs are shown first, with $L = 10$, $N_D = 2$. The simulation results show that the sum EE decreases with the number of the APs sharply due to the fact that sum rate gains by employing much APs are less than the sum energy consumption by the introduced APs.

In Fig. [10,](#page-9-1) the network performance in terms of the sum EE against the DAC quantization bits is given, with $M =$ 20 , $N_A = 10$. We can observe that the indeed the low DAC bits scenario does benefits in terms of the consumption by the DAC dominates the performance and rapidly leads to a gradual decrease in sum EE. As the figure implies, there exists an optimal number of DAC quantization bits, $b_m^{\text{DAC}} = 2$, for the maximum sum EE.

FIGURE 10. Achievable downlink sum EE versus the DAC quantization bits, with $M = 20$, $N_A = 10$.

FIGURE 11. The tradeoff between the sum EE and sum SE versus the DAC quantization bits, with $M = 20$, $N_A = 10$.

FIGURE 12. Joint impact of the number of APs and DAC quantization bits on sum rate, with $N = 2$, $N_D = 2$.

In Fig. 11, the tradeoff between the sum EE and sum SE versus the DAC quantization bits is expressed, with $M =$ 20, $N_A = 10$. It should be noticed that the resultant curves are plotted by letting the value of bits vary from 1 to 11 with steps

FIGURE 13. Joint impact of the number of APs and DAC quantization bits on sum EE, with $L = 10, N_D = 2$.

of 1. We can see that the rightmost point indicates the largest sum rate value while the highest point means the largest sum EE value. As a supplement, Figs. 12 and 13 give the joint impact of the number of APs and DAC quantization bits on both the achievable sum rate and sum EE.

VI. CONCLUSION

In this paper, the downlink D2D underlaid multigroup multicast cell-free massive MIMO systems with multi-antenna users have been considered, where the DUEs are distributed according to PPP. Assuming that the imperfect CSI can be acquired, the achievable rates of both CFUEs and DUEs are calculated. Following that, the sum EE is conducted using the constructed energy consumption model. The obtained results allow us to quantitatively investigate the effects of the number/antenna of APs/CFUEs/DUEs, the density of DUEs, and the quantization bits. To be more specific, increasing the number of APs can improve the sum SE, however, the sum EE decreases with the number of the APs sharply. The obtained results demonstrate the significance of the collaborative deployment of D2D and multigroup multicast cell-free massive MIMO technology, providing important references and guidance for future practical deployments of B5G/6G.

APPENDICES

A. PROOF OF THEOREM 1

For the sake of analysis, we first calculate the following values:

$$
\mathbb{E}\left\{\widetilde{\mathbf{W}}_{p,m}^{H}\widetilde{\mathbf{W}}_{p,m}\right\} \n= \lambda_{m} (1 - \lambda_{m}) \operatorname{diag}\left(\mathbb{E}\left\{\mathbf{Y}_{p,mj}^{a}\left(\mathbf{Y}_{p,mj}^{a}\right)^{H}\right\}\right) \n= N_{A}\lambda_{m} (1 - \lambda_{m}) \left(\tau_{p}\rho_{p}^{c}\sum_{j'=1}^{J}\sum_{k'=1}^{K}\beta_{mj'k'}\left\|\boldsymbol{\Phi}_{j'}^{H}\boldsymbol{\Phi}_{j}\right\|^{2} + \mathbf{I}_{\tau_{p}}\right).
$$
\n(51)

By using [\(6\)](#page-3-0), we have

$$
\mathbb{E}\left\{\left(\mathbf{G}_{mjk}^{a}\right)^{H}\widetilde{\mathbf{Y}}_{p,mj}^{a}\right\}\n= \mathbb{E}\left\{\lambda_{m}\sqrt{\tau_{p}\rho_{p}^{c}}\sum_{j=1}^{J}\sum_{k=1}^{K}\left(\mathbf{G}_{mjk}^{a}\right)^{H}\mathbf{G}_{mjk}^{a}\right\}\n+ \mathbb{E}\left\{\lambda_{m}\left(\mathbf{G}_{mjk}^{a}\right)^{H}\widetilde{\mathbf{W}}_{p,mj}\right\} + \mathbb{E}\left\{\left(\mathbf{G}_{mjk}^{a}\right)^{H}\widetilde{\mathbf{W}}_{p,m}\right\}\n= N_{A}\lambda_{m}\sqrt{\tau_{p}\rho_{p}^{c}}\beta_{mjk}.
$$
\n(52)

Therefore, the $\mathbb{E}\left\{\left\|\widetilde{\mathbf{Y}}_{\text{p}}^{\text{a}}\right\|$ p,*mj* $\left\{\begin{array}{c} 2 \\ \text{can be derived as} \end{array}\right\}$

$$
\mathbb{E}\left\{\left\|\widetilde{\mathbf{Y}}_{\mathrm{p},mj}^{a}\right\|^{2}\right\}= N_{\mathrm{A}}\lambda_{m}^{2}\tau_{\mathrm{p}}\rho_{\mathrm{p}}^{c}\sum_{j'=1}^{J}\sum_{k'=1}^{K}\beta_{mjk'}\left\|\boldsymbol{\Phi}_{j'}^{H}\boldsymbol{\Phi}_{j}\right\|^{2} + N_{\mathrm{A}}\lambda_{m}^{2}\mathbf{I}_{N}+ N_{\mathrm{A}}\lambda_{m}\left(1-\lambda_{m}\right)\left(\tau_{\mathrm{p}}\rho_{\mathrm{p}}^{c}\sum_{j'=1}^{J}\sum_{k'=1}^{K}\beta_{mjk'}\left\|\boldsymbol{\Phi}_{j'}^{H}\boldsymbol{\Phi}_{j}\right\|^{2} + \mathbf{I}_{N}\right)= N_{\mathrm{A}}\lambda_{m}\tau_{\mathrm{p}}\rho_{\mathrm{p}}^{c}\left(\sum_{j'=1}^{J}\sum_{k'=1}^{K}\beta_{mjk'}\left\|\boldsymbol{\Phi}_{j'}^{H}\boldsymbol{\Phi}_{j}\right\|^{2} + \mathbf{I}_{N}\right). (53)
$$

To that end, the estimated channel $\widehat{\mathbf{G}}^{a}_{mjk}$ can be derived as

$$
\widehat{\mathbf{G}}_{mjk}^{a} = \frac{\mathbb{E}\left\{\mathbf{G}_{mjk}^{a}\left(\widetilde{\mathbf{Y}}_{p,mj}^{a}\right)^{H}\right\}}{\mathbb{E}\left\{\left\|\widetilde{\mathbf{Y}}_{p,mj}^{a}\right\|^{2}\right\}}\widetilde{\mathbf{Y}}_{p,mj}^{a}
$$
\n
$$
= \frac{\sqrt{\tau_{p}\rho_{p}^{c}}\beta_{mjk}}{\tau_{p}\rho_{p}^{c}\sum_{j'=1}^{I}\sum_{k'=1}^{K}\beta_{mjk'}\left\|\mathbf{\Phi}_{j'}^{H}\mathbf{\Phi}_{j}\right\|^{2}+\mathbf{I}_{N}}\widetilde{\mathbf{Y}}_{p,mj}^{a}.
$$
\n(54)

Combining [\(6\)](#page-3-0) and [\(54\)](#page-10-0), we have

$$
\left(\widehat{\mathbf{G}}_{mjk}^{a}\right)^{H}\widehat{\mathbf{G}}_{mjk}^{a}=N_{\mathrm{A}}\frac{\lambda_{m}\sqrt{\tau_{\mathrm{p}}\rho_{\mathrm{p}}^{c}}\beta_{mjk}}{\tau_{\mathrm{p}}\rho_{\mathrm{p}}^{c}\sum_{j'=1}^{J}\sum_{k'=1}^{K}\beta_{mjk'}\left\Vert \mathbf{\Phi}_{j'}^{H}\mathbf{\Phi}_{j}\right\Vert ^{2}+\mathbf{I}_{N}}.
$$
\n(55)

Based on the previous consideration, we can complete the proof of Theorem 1 by skipping the tedious derivation.

B. PROOF OF THEOREM 2

From [\(31\)](#page-5-5) we can know that

$$
\bar{\mathbf{H}}_{jk} = \mathbb{E}\left\{\sqrt{\rho_{\rm d}^{\rm a}}\sum_{m=1}^{M}\sum_{k'=1}^{K} \alpha_{m} \eta_{mjk'}^{1/2} \mathbf{G}_{mjk}^{\rm a} \mathbf{Z}_{mj}^{\rm a}\right\} \n= \mathbb{E}\left\{\sqrt{\rho_{\rm d}^{\rm a}}\sum_{m=1}^{M}\sum_{k'=1}^{K} \alpha_{m} \eta_{mjk'}^{1/2} \left(\widehat{\mathbf{G}}_{mjk}^{\rm a} + \mathbf{E}_{mjk}^{\rm a}\right) \mathbf{Z}_{mj}^{\rm a}\right\},
$$
\n(56)

where $\mathbf{G}_{mjk}^{\text{a}} = \widehat{\mathbf{G}}_{mjk}^{\text{a}} + \mathbf{E}_{mjk}^{\text{a}}$.

With the above consideration, $\bar{\mathbf{H}}_{jk}^H \bar{\mathbf{H}}_{jk}$ can be, mathematically, given as

$$
\bar{\mathbf{H}}_{jk}^{H} \bar{\mathbf{H}}_{jk} = \mathbb{E} \left\{ \sqrt{\rho_{\rm d}^{\rm a}} \sum_{m=1}^{M} \sum_{k'=1}^{K} \alpha_{m} \eta_{mjk'}^{1/2} \left(\left(\widehat{\mathbf{G}}_{mjk}^{\rm a} + \mathbf{E}_{mjk}^{\rm a} \right) \mathbf{Z}_{mj}^{\rm a} \right)^{H} \right\} \times \mathbb{E} \left\{ \sqrt{\rho_{\rm d}^{\rm a}} \sum_{m=1}^{M} \sum_{k'=1}^{K} \alpha_{m} \eta_{mjk'}^{1/2} \left(\widehat{\mathbf{G}}_{mjk}^{\rm a} + \mathbf{E}_{mjk}^{\rm a} \right) \mathbf{Z}_{mj}^{\rm a} \right\} \n= \left(N_{\rm A} \sqrt{\rho_{\rm d}^{\rm a}} \sum_{m=1}^{M} \sum_{k'=1}^{K} \alpha_{m} \eta_{mjk'}^{1/2} \gamma_{mjk}^{1/2} \right)^{2} \mathbf{I}_{N}.
$$
\n(57)

By virtue of the [\(29\)](#page-5-2) and [\(31\)](#page-5-5), we have the following calculations

$$
\Psi_{jk}^{\text{c}} = \mathbb{E}\left\{\mathbf{r}_{jk}^{\text{c}}\left(\mathbf{r}_{jk}^{\text{c}}\right)^{H}|\bar{\mathbf{H}}_{jk}\right\}
$$
\n
$$
= \mathbb{E}\left\{\rho_{\text{d}}^{\text{a}}\sum_{m=1}^{M}\sum_{n=1}^{N}\sum_{j'=1}^{J}\sum_{k'=1}^{K}\sum_{k''=1}^{K}\alpha_{m}\alpha_{n}\eta_{mj'k'}^{1/2}\eta_{njk''}^{1/2}\left(\mathbf{G}_{mjk}^{\text{a}}\right)^{H} \times \mathbf{Z}_{mj'}^{\text{a}}\left(\mathbf{Z}_{nj'}^{\text{a}}\right)^{H}\mathbf{G}_{njk}^{\text{a}} + \sum_{m=1}^{M}\left(\mathbf{G}_{mjk}^{\text{a}}\right)^{H}\tilde{\mathbf{n}}_{m}\tilde{\mathbf{n}}_{m}^{H}\mathbf{G}_{mjk}^{\text{a}} + \sum_{l=1}^{L}\rho^{\text{d}}\mu_{l}\left(\mathbf{G}_{lk}^{\text{d}}\right)^{H}\tilde{\mathbf{G}}_{ll}^{\text{d}}\left(\tilde{\mathbf{G}}_{ll}^{\text{d}}\right)^{H}\mathbf{G}_{lk}^{\text{d}} + \mathbf{I}_{N}\right\}.
$$
\n(58)

With the fact that $\bar{\mathbf{\Psi}}_{jk}^{\mathrm{c}} = \mathbf{\Psi}_{jk}^{\mathrm{c}} - \bar{\mathbf{H}}_{jk}^H \bar{\mathbf{H}}_{jk}$, we can complete the proof of the Theorem 2 after several algebraic calculations by combining the equations of [\(56\)](#page-10-1)-[\(58\)](#page-11-0).

C. PROOF OF THEOREM 3

With the equation [\(36\)](#page-5-6), we have

$$
\bar{\mathbf{S}}_{ll}^H \bar{\mathbf{S}}_{ll} = \rho^d N_D^2 \sum_{l'=l}^L \mu_{l'} \left(\mathbf{\Omega}_{ll'} \mathbf{\Gamma}_{l'l} \mathbf{\Gamma}_{l'l}^H \mathbf{\Omega}_{ll'}^H \right). \tag{59}
$$

By using [\(34\)](#page-5-7) and [\(36\)](#page-5-6), then

$$
\Psi_{l}^{\mathrm{d}} = \mathbb{E}\left\{\mathbf{r}_{l}^{\mathrm{d}}\left(\mathbf{r}_{l}^{\mathrm{d}}\right)^{H}|\bar{\mathbf{S}}_{ll}\right\}\n= \mathbb{E}\left\{\mathbf{S}_{l'l'}\mathbf{S}_{l'l'}^{H}\right\} + \mathbb{E}\left\{\mathbf{n}_{l}\mathbf{n}_{l}^{H}\right\}\n+ \mathbb{E}\left\{\sum_{m=1}^{M}\left(\mathbf{G}_{ml}^{\mathrm{a}}\right)^{H}\tilde{\mathbf{n}}_{m}\tilde{\mathbf{n}}_{m}^{H}\mathbf{G}_{ml}^{\mathrm{a}}\right\}\n+ \mathbb{E}\left\{\sum_{m=1}^{M}\sum_{j=1}^{J}\sum_{k=1}^{K}\alpha_{m}^{2}\left(\mathbf{G}_{ml}^{\mathrm{a}}\right)^{H}\mathbf{Z}_{mj}^{\mathrm{a}}\left(\mathbf{Z}_{mj}^{\mathrm{a}}\right)^{H}\mathbf{G}_{ml}^{\mathrm{a}}\right\}.
$$
\n(60)

The term $\mathbb{E} \left\{ \mathbf{S}_{l'l'} \mathbf{S}_{l'l'}^{H} \right\}$ in $\boldsymbol{\Psi}_{l}^{\text{d}}$ can be first calculated as

$$
\mathbb{E}\left\{{\bf S}_{l'l'}{\bf S}_{l'l'}^H\right\}=\mathbb{E}\left\{{\rho^{\rm d}}{\sum_{l'=1}^L\mu_{l'}}{\left({\bf G}_{l'l}^{\rm d}\right)}^H{\bf \widehat{G}}_{l'l'}^{{\rm d}}{\left({\bf \widehat{G}}_{l'l'}^{{\rm d}}\right)}^H{\bf G}_{l'l}^{{\rm d}}\right\}
$$

 $= \rho^d$ $\sqrt{ }$ $\tau_p \rho_p^d \sum$ *L* $l'=1$ $\mathbf{D}_{11} + \tau_{\rm p} \rho_{\rm p}^{\rm d} \sum$ *L* $l'' \neq l$ $D_{12} + D_{13}$ \setminus $\vert \cdot \vert$ (61)

where D_{11} , D_{12} , and D_{13} can be derived as, respectively

$$
\mathbf{D}_{11} = \mathbb{E}\left\{ \left(\mathbf{G}_{l'l}^{\mathrm{d}}\right)^{H} \mathbf{G}_{l'l}^{\mathrm{d}} \underbrace{\mathbf{\Omega}_{ll'} \mathbf{C}_{l'l'} \mathbf{C}_{l'l'}^{H} \mathbf{\Omega}_{ll'}^{H}}_{\mathbf{B}_{l'l}} \left(\mathbf{G}_{l'l}^{\mathrm{d}}\right)^{H} \mathbf{G}_{l'l}^{\mathrm{d}} \right\}
$$
\n
$$
\stackrel{(a)}{=} N_{\mathrm{D}} \left(\beta_{l'l}^{\mathrm{d}}\right)^{2} \mathbf{J}_{ll'}
$$
\n
$$
= N_{\mathrm{D}} \left(\beta_{l'l}^{\mathrm{d}}\right)^{2} \text{tr} \left(\mathbf{\Omega}_{ll'} \mathbf{C}_{l'l'} \mathbf{C}_{l'l'}^{H} \mathbf{\Omega}_{ll'}^{H}\right) \mathbf{I}_{N_{\mathrm{D}}} + N_{\mathrm{D}}^{2} \left(\beta_{l'l}^{\mathrm{d}} / \sqrt{\tau_{\mathrm{p}} \rho_{\mathrm{p}}^{\mathrm{d}} \beta_{l'l'}^{d}}\right)^{2} \left(\mathbf{\Omega}_{ll'} \mathbf{C}_{l'l'} \mathbf{C}_{l'l'}^{H} \mathbf{\Omega}_{ll'}^{H}\right), \tag{62}
$$

and

$$
\mathbf{D}_{12} = \mathbb{E}\left\{\left(\mathbf{G}_{l'l}^{\mathrm{d}}\right)^{H}\mathbf{G}_{l'l'}^{\mathrm{d}}\mathbf{\Omega}_{l'}\mathbf{C}_{l'l'}\mathbf{C}_{l'l'}^{H}\mathbf{\Omega}_{l'}^{H}\left(\mathbf{G}_{l'l'}^{\mathrm{d}}\right)^{H}\mathbf{G}_{l'l}^{\mathrm{d}}\right\}= N_{\mathrm{D}}\beta_{l'l}^{\mathrm{d}}\beta_{l'l''}^{\mathrm{d}}\mathrm{tr}\left(\mathbf{\Omega}_{l'}\mathbf{C}_{l'l'}\mathbf{C}_{l'l'}^{H}\mathbf{\Omega}_{l'}^{H}\right)\mathbf{I}_{N_{\mathrm{D}}},\tag{63}
$$

and

$$
\mathbf{D}_{13} = \mathbb{E}\left\{ \left(\mathbf{G}_{l'l}^{\mathrm{d}}\right)^{H} \mathbf{W}_{\mathrm{p},l}^{\mathrm{d}} \mathbf{\Omega}_{l'} \mathbf{C}_{l'l'} \mathbf{C}_{l'l'}^{H} \mathbf{\Omega}_{l'}^{H} \mathbf{W}_{\mathrm{p},l}^{\mathrm{d}} \mathbf{G}_{l'l}^{\mathrm{d}} \right\} = N_{\mathrm{D}} \beta_{l'l}^{\mathrm{d}} \mathrm{tr} \left(\mathbf{\Omega}_{l'} \mathbf{C}_{l'l'} \mathbf{C}_{l'l'}^{H} \mathbf{\Omega}_{l'}^{H} \right) \mathbf{I}_{N_{\mathrm{D}}},
$$
(64)

where (*a*) is given by $J_{ll'}$ as

$$
\mathbf{J}_{ll'} = \text{tr} \left(\mathbf{B}_{l'l} \right) \mathbf{I}_{N_{\rm D}} + N_{\rm D} \text{diag} \left(\mathbf{B}_{l'l} \right), \tag{65}
$$

and the element of $J_{ll'}$ is given as follows

$$
j_{ll} = \sum_{l}^{L} b_{ll} + N_{\rm D} b_{ll}.
$$
 (66)

The substitution of (62) , (63) , and (64) into (61) , then the $\mathbb{E} \left\{ \mathbf{S}_{l'l'} \mathbf{S}_{l'l'}^H \right\}$ can be given further as

$$
\mathbb{E}\left\{\mathbf{S}_{l'l'}\mathbf{S}_{l'l'}^{H}\right\} \n= \rho^{d}N_{D}\sum_{l'=1}^{L}\mu_{l'}\left(\tau_{p}\rho_{p}^{d}\left(\beta_{l'l}^{d}\right)^{2}\mathrm{tr}\left(\mathbf{\Omega}_{ll'}\mathbf{C}_{l'l'}\mathbf{C}_{l'l'}^{H}\mathbf{\Omega}_{ll'}^{H}\right)\mathbf{I}_{N_{D}} \n+ N_{D}\left(\beta_{l'l}^{d}\right/\beta_{l'l'}^{d}\right)^{2}\left(\mathbf{\Omega}_{ll'}\mathbf{\Gamma}_{l'l'}\mathbf{\Gamma}_{l'l'}^{H}\mathbf{\Omega}_{ll'}^{H}\right) \n+ \rho^{d}N_{D}\sum_{l'=1}^{L}\sum_{l''\neq l}\mu_{l'}\beta_{l'l}^{d}\beta_{l'l'}^{d}\mathrm{tr}\left(\mathbf{\Omega}_{l'}\mathbf{C}_{l'l'}\mathbf{C}_{l'l'}^{H}\mathbf{\Omega}_{l'}^{H}\right)\mathbf{I}_{N_{D}} \n+ \rho^{d}N_{D}\sum_{l'=1}^{L}\mu_{l'}\beta_{l'l}^{d}\mathrm{tr}\left(\mathbf{\Omega}_{l'}\mathbf{C}_{l'l'}\mathbf{C}_{l'l'}^{H}\mathbf{\Omega}_{l'}^{H}\right)\mathbf{I}_{N_{D}}.
$$
\n(67)

To be more specific, we can calculate the following

$$
\mathbf{\bar{\Psi}}_{l}^{\text{d}} = \mathbf{\Psi}_{l}^{\text{d}} - \bar{\mathbf{S}}_{ll}\bar{\mathbf{S}}_{ll}^{H}
$$

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$$
= \rho^{d} N_{D}^{2} \sum_{l' \neq l}^{L} \mu_{l'} \left(\beta_{l'l}^{d} / \beta_{l'l'}^{d} \right)^{2} tr \left(\|\mathbf{\Omega}_{ll'} \mathbf{\Gamma}_{l'l'}\|^{2} \right) \mathbf{I}_{N_{D}} + \rho^{d} N_{D} \sum_{l'=1}^{L} \mu_{l'} \beta_{l'l}^{d} \left(\tau_{P} \rho_{P}^{d} \beta_{l'l}^{d} tr \left(\|\mathbf{\Omega}_{ll'} \mathbf{C}_{l'l'}\|^{2} \right) \right) + \left(\sum_{l'' \neq l}^{L} \beta_{l'l''}^{d} + 1 \right) tr \left(\|\mathbf{\Omega}_{l'} \mathbf{C}_{l'l'}\|^{2} \right) \right) \mathbf{I}_{N_{D}} + \rho^{a} N N_{A} \sum_{m=1}^{M} \sum_{j=1}^{J} \alpha_{m} \left(1 - \alpha_{m} \right) \beta_{ml}^{a} \left(\sum_{k=1}^{K} \eta_{mjk}^{1/2} \right)^{2} + \rho^{a} N N_{A} \sum_{m=1}^{M} \sum_{j=1}^{J} \sum_{k=1}^{K} \alpha_{m}^{2} \eta_{mjk} \beta_{ml}^{a} \mathbf{I}_{N_{D}} + \mathbf{I}_{N_{D}}. \quad (68)
$$

Combining the [\(61\)](#page-11-4) and [\(67\)](#page-11-5), the proof of Theorem 3 can be completed after several algebraic derivations.

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