

RESEARCH ARTICLE

Integration of CNN in a Dynamic Model-Based Controller for Control of a 2DOF Helicopter With Tail Rotor Perturbations

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ABSTRACT This paper shows a proposal for a control scheme for the trajectory tracking problem in a Two Degree of Freedom Helicopter (2DOFH). For this purpose, a control scheme based on a feedback linearization combined with a Generalized Proportional Integral (GPI) controller is used. In order to implement linearization by feedback, it is required to know and have access to all the physical 2DOFH parameters, however, angular velocity and viscous friction are often not available. Commonly, state observers are used to know the angular velocity, however, estimating friction results out to be more complex. Therefore, we propose the use of a Convolutional Neural Network (CNN) to estimate viscous friction and angular velocity. The variables estimated by the CNN are entered into both the GPI and feedforward controllers. Thus, the system is brought to a linear representation that directly relates the GPI control to the dynamics of perturbations and non-model parameters. Finally, results of numerical simulations are shown that validate the robustness of our scheme in the presence of disturbances in the tail rotor, as well as the advantages of using a feedforward control based on a CNN.

INDEX TERMS Friction estimation, neural networks, non-linear system, tail rotor disturbance, two degrees of freedom helicopter.

I. INTRODUCTION

In recent years, rotary wing Unmanned Aerial Vehicles (UAV) have been used in areas where human actions are restricted [1]–[3]. One of the most popular rotary wing UAV is the helicopter, some of its main features are: Ability to rotate on its own axis, levitate, take off and land vertically, and move sideways or backwards while in air. [4]. Despite the number of applications in which a helicopter can be used [5], fully autonomous scale helicopters are not yet available. This is due to non-linearities, strong coupling, uncertainties and aerodynamic disturbances associated with this vehicle [6].

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Nowadays, there are different study areas focused on helicopters, being of special interest the improvement of its stability, autonomous navigation, takeoff and landing control, trajectory tracking, disturbance rejection, among others [7]–[10]. To achieve the above, it is necessary to know the behavior of the disturbances that frequently occur, which greatly impairs the Tail Rotor (TR), causing stability problems during flight and limiting maneuvering space [11], [12].

Hence, different experimental prototypes have been developed to study helicopter dynamics [13]–[15]. One of the most popular consists of a Two Degree of Freedom Helicopter (2DOFH), which recreates the dynamic behavior of the helicopter in its pitch (θ) and yaw (ψ) rotations [15], [16]. The orientations are controlled by two Motor-Propeller

Pairs (MPP) located at the ends of a rigid shaft, which can rotate on the horizontal and vertical axis [17].

Several studies have focused on the design of control algorithms for helicopters. For example, in [18] an observer based on sliding modes proposes to estimate angular velocities, obtaining results close to the real ones. Regarding the control of these systems, in [19] an output feedback algorithm H_∞ is used to study the problem of disturbance attenuation. In [20], a control scheme based on the active rejection of disturbances for a 2DOFH is proposed. The algorithm contemplates the use of GPI-type observers to estimate the speed and disturbances caused by non-modeled dynamics and external disturbances.

The design of algorithms and control schemes for UAV, such as those mentioned above, require solid mathematical model foundations to develop a controller based on the model. If you have a reliable mathematical model, it is possible to design a controller based on the model, which tends to linearize the system [21]. However, these controllers require a priori knowledge of the mathematical model parameters. Parametric identification allows an attractive option to obtain a numerical approximation of the unknown coefficients, when prior knowledge is absent [22].

UAVs are used in operations in operations where several types of disturbances exist, which are produced due to environmental conditions and their non-linear dynamics. Furthermore, parameters such as the friction of the actuators tend to change with respect to time; furthermore, not all variables can always be measured directly. This affects the performance of control algorithms based on the dynamic model [23].

Therefore, various works have been developed focused on the implementation of parametric identification techniques in UAVs. For example, [24] carries out the experimental identification of the rotational inertia and coefficient of friction of a quadrotor, which is achieved using Levenberg Marquardt optimization and quadratic optimization to minimize error criteria. Under another scheme, in [25] an extended Kalman filter is used to identify the linear and angular velocities of a quadrotor. Finally, in [26] the inertial parameters of a helicopter are identified using recursive least squares, highlighting that the method is capable of updating the estimated parameters while the vehicle is in flight.

As mentioned, there are different techniques used for parameter estimation. It should be emphasized that the implementation of model-based control schemes requires knowledge of the variables in real time, therefore, online estimation techniques shall be used [27]. Under this premise, machine learning techniques are a reliable alternative option to perform parametric identification online, with artificial neural networks being the most used.

One of the most widely used neural networks consists of the Multi-Layer Perceptron (MLP) architecture [28], however, the accuracy of its results is affected by problems in the learning algorithm such as local minimums or lack of information. Some works on parametric identification for aeronautical systems using MLP topology are: [29] and [30], showing the feasibility of incorporating this type

of schemes into aircraft control algorithms. Therefore, the MLP has been modified, resulting in a Convolutional Neural Network (CNN) algorithm, which is a deep learning technique [31]. Although CNNs are mostly used for image processing, it has been reported that CNNs can also be used for the identification of non-linear systems [32].

Therefore, in this paper we propose the use of a CNN to estimate the coefficient of viscous friction, $\dot{\theta}$ and $\dot{\psi}$, which are introduced to a feedforward control, linearizing the system around all its equilibrium points. The feedforward controller is combined with a GPI to provide robustness in the presence of disturbances in the TR.

This work is organized as follows: section 2 describes system mathematical model of the system considering disturbances in the TR. Section 3 shows the proposed control scheme for trajectory tracking. In section 4 we describe the CNN design for the estimation of $\dot{\theta}$, $\dot{\psi}$ and viscous friction. Moreover, section 5 shows the comparison of two feedforward control schemes, highlighting the differences when using information from CNN. Finally, the last section contains the conclusions of this work.

II. MATHEMATICAL MODEL

Figure 1a shows the 2DOFH prototype used in this work, which has dimensions of 74 cm long and 35 cm high. In addition, it has a mechanical coupling to generate disturbances (see Fig. 1b and c).

Fig. 2 shows the free body diagram of the 2DOFH, as well as the parameters and variables of interest in the system. F_{TR} and F_{MR} are the thrust forces generated by TR and the Main Rotor (MR), respectively. F_g corresponds to the force of gravity and L_{cm} is the length from the center of mass to the pitch axis. r_y and r_p are the distance from TR and MR to θ , respectively. Finally, ψ is the angle around the Z axis and ϕ is the angle of incidence of the TR (ϕ directly affects the thrust force of the TR).

The displacement in the X, Y and Z axes depends on the variation of the 2DOFH angles and is expressed by

$$\begin{aligned} X &= L_{cm}c\psi c\theta, \\ Y &= L_{cm}s\psi c\theta, \\ Z &= L_{cm}s\theta, \end{aligned} \quad (1)$$

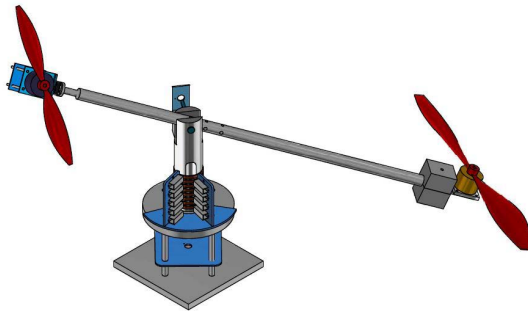
where $s = \sin(\cdot)$ and $c = \cos(\cdot)$. Subsequently, the dynamic model is obtained from the Euler-Lagrange (EL) form [33]

$$\frac{d}{dt} \frac{\partial L}{\partial \dot{q}} - \frac{\partial L}{\partial q} = \tau - B\dot{q}; \quad (2)$$

with $L = T - U$, T and U denote the kinetic and potential energies respectively, $\tau = [\tau_\theta \ \tau_\psi]^T$ are the generalized force associated with the generalized coordinates $q = [\theta \ \psi]^T$ and $B = [B_\theta \ B_\psi]^T$ is the viscous friction.

Next, the kinetic and potential energy are defined as:

$$\begin{aligned} T &= T_{rp} + T_{ry} + T_t, \\ U &= m_h L_{cm} g s\theta, \end{aligned} \quad (3)$$



(a) 2DOFH prototype.



(b) Coupling for disturbance in the TR.



(c) Photograph of perturbation coupling in the TR.

FIGURE 1. 2DOFH prototype design.

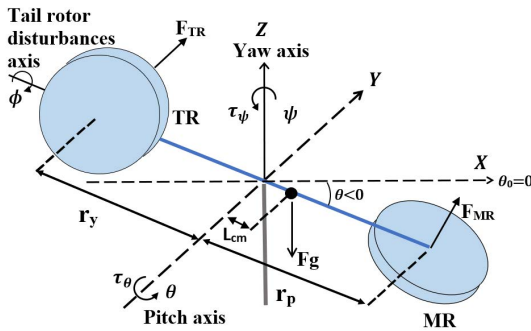


FIGURE 2. 2DOFH diagram.

where m_h is the mass of the helicopter, g is the force of gravity. T_t is the translational kinetic energy, T_{rp} and T_{ry} are the rotational kinetic energy in ψ and θ , defined as [34]:

$$\begin{aligned} T_{rp} &= \frac{1}{2} J_{eq_p} \dot{\theta}^2, \\ T_{ry} &= \frac{1}{2} J_{eq_y} \dot{\psi}^2, \\ T_t &= \frac{1}{2} m_h (V_x^2 + V_y^2 + V_z^2), \end{aligned} \quad (4)$$

with J_{eq_p} and J_{eq_y} equal to the moments of inertia when rotating over θ and ψ , respectively. The velocity on each axis is obtained with the rotation angles and equation (1). Therefore, total kinetic energy is defined as:

$$T = \frac{1}{2} J_{eq_p} \dot{\theta}^2 + \frac{1}{2} J_{eq_y} \dot{\psi}^2 + \frac{1}{2} m_h L_{cm}^2 (\dot{\theta}^2 + (\dot{\psi} c\theta)^2). \quad (5)$$

Thus, equation (2) results in:

$$\begin{aligned} & \begin{bmatrix} \ddot{\theta} (J_{eq_p} + m_h L_{cm}^2) + m_h L_{cm}^2 s\theta c\theta \dot{\psi}^2 + m_h g L_{cm} c\theta \\ \ddot{\psi} (J_{eq_y} + m_h (c\theta L_{cm})^2) - 2m_h L_{cm}^2 \dot{\theta} s\theta c\theta \dot{\psi} \end{bmatrix} \\ &= \begin{bmatrix} k_{pp} & k_{yy} s\phi + k_{py} c\phi \\ k_{yp} & k_{yy} c\phi + k_{py} s\phi \end{bmatrix} \begin{bmatrix} U_\theta \\ U_\psi \end{bmatrix} - \begin{bmatrix} B_\theta \dot{\theta} \\ B_\psi \dot{\psi} \end{bmatrix}, \end{aligned} \quad (6)$$

where τ_θ and τ_ψ are the torque applied to each axis of rotation, U_θ and U_ψ are the control actions applied to the MR and TR, respectively. k_{pp} and k_{yy} are the thrust force constants in relation to the control action [Nm/%pwm] derived from the direct incidence of the rotor thrust of the rotor MR and TR on the axis θ and ψ , respectively. k_{py} and k_{yp} are the thrust force constants in relation to the control action [Nm/%pwm] derived from the torque generated by the rotation of the rotor propellers TR and MR in the axis θ and ψ [15], [35].

A. PARAMETRIC IDENTIFICATION USING CNN

The implementation of control algorithms based on the mathematical model requires knowledge of all parameters. If any parameter is unknown, the mathematical model must be adjusted to experimental data by a parameter identification algorithm. In this context, there are on-line and off-line methods based on the least squares method [36], [37].

Currently, Artificial Neural Networks (ANN) are used to model and identify parameters in dynamic systems, due to their ability to approximate nonlinear functions and predict variables [38]–[42]. Therefore, deep learning methods together with Neural Networks (NN) have been used for the identification of unknown parameters, unmodeled dynamics and external perturbations for control systems [43]–[46]. Under this approach, most identification applications use adaptive or recursive NN, another common deep neural network is the CNN [38], [47].

In particular, since the estimation of friction coefficient is a complicated task, in this work we propose the use of a CNN to estimate viscous friction and velocity at each degree of freedom of the helicopter. CNN training is performed offline (calculation of synapotic weights). After training, the CNN is implemented in line with the control scheme. In other words, viscous friction and speed are estimated online, these variables are introduced into the control scheme.

The estimation of the friction and velocity term is carried out using CNNs, for which, a different CNN is used for each of them, i.e. $\hat{\beta}_\theta = B_\theta \hat{\theta}$ and $\hat{\beta}_\psi = B_\psi \hat{\psi}$, with $\hat{\beta}_\theta$ and $\hat{\beta}_\psi$ are the output of the respectively CNN. Thus, we can estimate the velocities $\hat{\theta}$ and $\hat{\psi}$ in the form:

$$\begin{aligned} \hat{\theta} &= \hat{\beta}_\theta / \bar{B}_\theta, \\ \hat{\psi} &= \hat{\beta}_\psi / \bar{B}_\psi, \end{aligned} \quad (7)$$

where, \bar{B}_θ and \bar{B}_ψ are estimated constants of the viscous friction of B_θ and B_ψ .

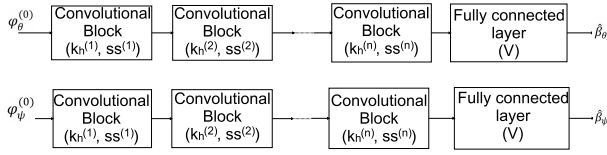


FIGURE 3. CNN for parametric estimation of $B_\theta \hat{\theta}$ and $B_\psi \hat{\psi}$.

Thus, (6) is rewritten as a function of the variables estimated by the CNN, resulting in:

$$\begin{aligned} & \begin{bmatrix} \ddot{\theta}(J_{eq_p} + m_h L_{cm}^2) + m_h L_{cm}^2 s \theta c \hat{\psi}^2 + m_h g L_{cm} c \theta \\ \ddot{\psi}(J_{eq_y} + m_h (c \theta L_{cm})^2) - 2 m_h L_{cm}^2 \hat{\theta} s \theta c \hat{\psi} \end{bmatrix} \\ &= \begin{bmatrix} k_{pp} & k_{yy} s \phi + k_{py} c \phi \\ k_{yp} & k_{yy} c \phi + k_{py} s \phi \end{bmatrix} \begin{bmatrix} U_\theta \\ U_\psi \end{bmatrix} - \begin{bmatrix} \hat{\beta}_\theta \\ \hat{\beta}_\psi \end{bmatrix}, \quad (8) \end{aligned}$$

To estimate the friction terms, we use the Nonlinear Auto Regressive Exogenous (NARX) model:

$$\hat{\beta} = \text{CNN} \left[\varphi^{(0)} \right], \quad (9)$$

where $\text{CNN}[\cdot]$ is the proposed structure of the CNN and $\varphi^{(0)}$ is the input, It is defined for each CNN as:

$$\begin{aligned} \varphi_\theta^{(0)}(\xi) &= [\tau_p(\xi) \cdots \tau_p(\xi - r_\theta) \theta(\xi) \cdots \theta(\xi - r_{\theta_2})]^T, \\ \varphi_\psi^{(0)}(\xi) &= [\tau_y(\xi) \cdots \tau_y(\xi - r_{\psi_1}) \psi(\xi) \cdots \psi(\xi - r_{\psi_2})]^T, \end{aligned} \quad (10)$$

ξ indicates the current instant of time, r_θ and r_ψ are the regression order for each data.

Fig. 3 shows the structure of the CNN, this being our proposal for the estimation of $\hat{\beta}_\theta$ and $\hat{\beta}_\psi$. Our proposal consists of two convolutional blocks ($n = 4$) followed by a fully connected layer.

Each convolutional block consists of two different layers, a convolutional layer and a subsample layer, with their respectively hyper-parameters. The first is the fundamental part of this algorithm [48], in it the convolution operation is carried out between the input of the convolutional block $\varphi^{(\ell-1)}$ and the filters of this layer $\kappa^{(\ell)}$ which their size are 3, thus generating the feature maps $\chi^{(\ell)}$ as follows:

$$\chi_h^{(\ell)} = \kappa_h^{(\ell)} \odot \varphi_h^{(\ell-1)}, \quad (11)$$

where the superscript (ℓ) indicates the current layer in which the operations are performed, \odot represents the convolution operation and h represents how many filters there are present in the layer.

Once these maps have been generated, we proceed to use the ReLU activation function [48]:

$$\vartheta_h^{(\ell)} = \max(\chi_h^{(\ell)}, 0). \quad (12)$$

The $\max(\cdot, \cdot)$ operation picks up the largest element of its arguments and passes them to the next layer, this operation is applied to each element in the feature maps. The subsample layer, in which the max-pool operation is performed [49], follows this activation function, here the large value in a group

of consecutive elements of the input vectors are chosen this is a simplification applied only to vectors instead of matrices, thus obtaining the output of the convolutional block as:

$$\varphi_h^{(\ell)} = \text{max-pool}(\vartheta_h^{(\ell-1)}, ss^{(\ell)}), \quad (13)$$

ss indicates the amount of elements to be considered in the max-pool operation, this value can vary in each convolutional block. These steps are repeated for the amount of convolutional blocks that are occupied within the structure.

After the convolutional block is complete, the output of CNN is generate by:

$$\hat{\beta} = V \varrho, \quad (14)$$

where V are the synaptic weights in the output layer and ϱ is the concatenated vector of the output of the last convolutional block defined as:

$$\varrho = [\varphi_1^n \ \varphi_1^n \ \cdots \ \varphi_1^n]. \quad (15)$$

To train the CNN, the back propagation algorithm is employed and modified in order to adapt it to the convolutional blocks.

The weights V in the final layer of CNN are fully-connected as in a MLP. The cost function to be minimized is the square error defined as:

$$J(r) = \frac{1}{2} e^2(r) = \left[\hat{\beta}(r) - \beta(r) \right]^2, \quad (16)$$

where r is each the training iteration. The update law for the output weights is:

$$V_i(r+1) = V_i(r) - \eta \frac{\partial J}{\partial V_i}, \quad (17)$$

with V_i been each element in matrix V . For the sub-sample layer, the update law here its defined as:

$$\frac{\partial J}{\partial \vartheta^{(\ell-1)}} = \text{up} \left(\frac{\partial J}{\partial \varphi^{(\ell)}}, ss^{(\ell)} \right), \quad (18)$$

where $\text{up}(\cdot, \cdot)$ is the opposite function to the *maxpool*. This operation passes the gradient to the position of the elements that in the feedforward had the largest contribution in this layer, i.e. the elements chosen by the operation *maxpool* so the gradient is propagated through the CNN.

Then, the reverse operation to ReLU function is used, where its derivative $f'(x)$ needs to be defined first as:

$$f'(x) = \begin{cases} 1 & \text{if } x > 0 \\ 0 & \text{otherwise.} \end{cases}$$

For the convolutional layers, there are two operations, one is to update the filters, the other one is to propagate the gradient to the previous layer. The update law for the filters is given by;

$$\frac{\partial J}{\partial \kappa_{h,a}^{(\ell)}} = \sum_{i=0}^{N-f_i} \frac{\partial J}{\partial \vartheta_i^{(\ell)}} \frac{\partial \vartheta_i^{(\ell)}}{\partial \chi_i^{(\ell)}} \frac{\partial \chi_i^{(\ell)}}{\partial \kappa_i^{(\ell)}}, \quad (19)$$

Algorithm 1 Estimation of $\hat{\beta}_\theta$ and $\hat{\beta}_\psi$

- 1: Acquire the training (DTR) and testing (DTE) data-sets from the system in open loop, with $DTR \neq DTE$
 - 2: Choose the hyper-parameters: number of layers ℓ , training epochs r , filters κ and learning rate η
 - 3: Initialization the weights V in $[0, 1]$ and the filters κ in $[-1, 1]$
 - 4: Training stage:
 - 5: **for** r times **do**
 - 6: Forward CNN
 - 7: Backward CNN
 - 8: **end for**
 - 9: Testing stage:
 - 10: Forward CNN
 - 11: Calculate the MSE
- return** Return the hyper-parameters and weights matrix used to Control simulation

where

$$\frac{\partial \vartheta_i^{(\ell)}}{\partial \chi_i^{(\ell)}} = f'(\chi_{h,i}^{(\ell)}) \tag{20}$$

So, (19) can be written as:

$$\frac{\partial J}{\partial \kappa_{h,a}^{(\ell)}} = \sum_{i=0}^{N-f_i} \left(\delta_{h,i}^{(\ell)} \right) \varphi_{h,i+a}^{(\ell-1)} \tag{21}$$

with

$$\delta_{h,i}^{(\ell)} = \frac{\partial J}{\partial \varphi_{h,i}^{(\ell)}} f'(\chi_{h,i}^{(\ell)}) \tag{22}$$

To obtain the gradient of the previous layers, we have:

$$\frac{\partial J}{\partial \varphi_i^{(\ell-1)}} = \sum_{a=0}^{f_i-1} \frac{\partial J}{\partial \chi_{i-a}^{(\ell)}} \kappa_a^{(\ell)} \tag{23}$$

which in terms of a convolutional operation this previous equation is:

$$\frac{\partial J}{\partial \varphi_h^{(\ell-1)}} = \delta_h^{(\ell)} \odot \text{rot}180(\kappa_h^{(\ell)}), \tag{24}$$

where $\text{rot}180(\cdot)$ is equivalent to performing a convolution of $\delta_h^{(\ell)}$ with the filter $K_h^{(\ell)}$ starting with the last element in the vector and finishing with the first one $^\circ$, \odot is the convolutional operation.

The **Algorithm 1** explains the methodology to estimate the frictions terms $(\hat{\beta}_\theta, \hat{\beta}_\psi)$. Even with ANN architectures like the one proposed in this work, the accuracy of the CNN estimation depends on the hyper-parameters, however, there is no deterministic way to choose them. Therefore, they are chosen randomly and based on trial and error, the best possible ones are selected within a given set of tests.

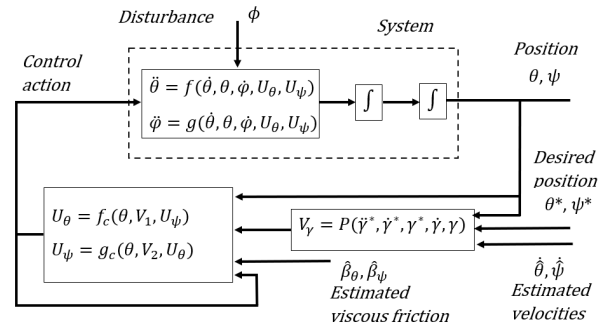


FIGURE 4. Proposed control scheme, feedforward GPI control with variables estimated by the CNN.

III. CONTROL SCHEME

The control objective is to track the trajectory in θ and ψ despite the presence of disturbances in the TR. For this, a control strategy is proposed that combines a feedback linearization with a GPI controller (see Fig. 4), this is made up of 2 control actions U_θ and U_ψ in charge of compensating the dynamics of the system (6) (with $\phi = 0$) and likewise has auxiliary control actions V_θ and V_ψ dedicated to compensating endogenous and exogenous disturbances. Thus, the system approximates a form $\ddot{\gamma} = V_i + \xi$, where ξ are the endogenous and exogenous disturbances and $\ddot{\gamma}$ the acceleration of the coordinate [3], [15].

A. STRATEGY CONTROL

From the above, based on (6) (with $\phi = 0$), the following feedforward controllers are proposed for the θ and ψ angles:

$$\begin{aligned} U_\theta &= \left[V_\theta (J_{eq-p} + m_h L_{cm}^2) - k_{py} U_\psi + \hat{\beta}_\theta \hat{\theta} \right. \\ &\quad \left. + m_h L_{cm}^2 s \theta c \theta \hat{\psi}^2 + m_h g L_{cm} c \theta \right] \frac{1}{k_{pp}}; \\ U_\psi &= \left[V_\psi (J_{eq-y} + m_h (c \theta L_{cm})^2) + \hat{\beta}_\psi \hat{\psi} \right. \\ &\quad \left. - 2 m_h L_{cm}^2 \hat{\theta} s \theta c \theta \hat{\psi} - k_{yp} U_\theta \right] \frac{1}{k_{yy}}, \end{aligned} \tag{25}$$

where V_θ and V_ψ are auxiliary controls, defined as [3], [15]:

$$\begin{aligned} V_\gamma &= \ddot{\gamma}^* - K_{3\gamma} \dot{e}_\gamma(t) - K_{2\gamma} e_\gamma - K_{1\gamma} \int_{\tau_1=0}^t e_\gamma(\tau_1) d\tau_1 \\ &\quad - K_{0\gamma} \int_{\tau_1=0}^t \int_{\tau_2=0}^{\tau_1} e_\gamma(\tau_2) d\tau_2 d\tau_1, \end{aligned} \tag{26}$$

with $\gamma = \theta, \psi$; $e_\gamma(t) = \gamma(t) - \gamma^*(t)$; $\dot{e}_\gamma(t) = \dot{\gamma}(t) - \dot{\gamma}^*$; γ^* , $\dot{\gamma}^*$ and $\ddot{\gamma}^*$ are the desired position, velocity, and accelerations, respectively. $K_{\sigma\gamma}$ are the gains of the controllers, with $\sigma = 0, 1, 2, \dots, 4$. $\hat{\gamma}$ corresponds to the estimates of the variables $\hat{\theta}$ and $\hat{\psi}$, respectively, which are obtained using the CNN described in Section 3.

From the above, substituting (25) into (8) and solving the equation:

$$0 = -\ddot{\theta} + V_\theta + \frac{-k_{py} + k_{yy} s \phi + k_{py} c \phi}{J_{eq-p} + m_h L_{cm}^2} U_\psi; \tag{27}$$

TABLE 1. Poles and gains.

γ	Poles	$k_{3,\gamma}$	$k_{2,\gamma}$	$k_{1,\gamma}$	$k_{0,\gamma}$
θ	$s_0 = 0.78; s_1 = 0.56;$ $s_{2,3} = -5.32 \pm 2.052j$	12	47.39	48.69	14.44
ψ	$s_0 = -0.5; s_1 = -0.78;$ $s_{1,2} = -3.2 \pm 0.204$	7.69	18.93	15.79	4.06

$$0 = -\ddot{\psi} + \left(c\phi + \frac{k_{py}}{k_{yy}} s\phi \right) V_\psi + \left(1 - c\phi - \frac{k_{py}}{k_{yy}} s\phi \right) \frac{k_{yp}U_\theta - B_\psi \dot{\psi} + 2m_h L_{cm}^2 \dot{\theta} s\theta c\theta \dot{\psi}}{J_{eq,y} + m_h c^2 \theta L_{cm}^2}, \quad (28)$$

then, substituting (26) for (27) and (28):

$$0 = \ddot{e}_\theta - K_{3\theta} \dot{e}_\theta(t) - K_{2\theta} e_\theta - K_{1\theta} \int_{\tau_1=0}^t e_\theta(\tau_1) d\tau_1 - K_{0\theta} \int_{\tau_1=0}^t \int_{\tau_2=0}^{\tau_1} e_\theta(\tau_2) d\tau_2 d\tau_1 + \frac{-k_{py} + k_{yy} s\phi + k_{py} c\phi}{J_{eq,p} + m_h L_{cm}^2} U_\psi; \quad (29)$$

$$0 = \left(c\phi + \frac{k_{py}}{k_{yy}} s\phi \right) \left[\ddot{\psi}^* - \frac{\ddot{\psi}}{c\phi + \frac{k_{py}}{k_{yy}} s\phi} - K_{3\psi} \dot{e}_\psi(t) - K_{2\psi} e_\psi - K_{1\psi} \int_{\tau_1=0}^t e_\psi(\tau_1) d\tau_1 - K_{0\psi} \int_{\tau_1=0}^t \int_{\tau_2=0}^{\tau_1} e_\psi(\tau_2) d\tau_2 d\tau_1 \right] + \left(1 - c\phi - \frac{k_{py}}{k_{yy}} s\phi \right) \frac{k_{yp}U_\theta - B_\psi \dot{\psi} + 2m_h L_{cm}^2 \dot{\theta} s\theta c\theta \dot{\psi}}{J_{eq,y} + m_h c^2 \theta L_{cm}^2}. \quad (30)$$

From the above, performing the Routh-Hurwitz analysis, the controller is capable of compensating for step-type disturbances, for tracking step and ramp trajectories in yaw and parabola type for the pitch axis. So, for when ϕ is zero and by differentiating equations A and B twice, obtain

$$0 = e_\theta^{(4)} + K_{3\theta} e_\theta^{(3)} + K_{2\theta} \ddot{e}_\theta + K_{1\theta} \dot{e}_\theta + K_{0\theta} e_\theta; \quad (31)$$

$$0 = e_\psi^{(4)} + K_{3\psi} e_\psi^{(3)} + K_{2\psi} \ddot{e}_\psi + K_{1\psi} \dot{e}_\psi + K_{0\psi} e_\psi. \quad (32)$$

B. TUNING

For GPI controller tuning, the resulting dynamics are expressed in terms of the tracking error, obtaining the following characteristic polynomial [15], [50]:

$$S^4 + K_{3\gamma} S^3 + K_{2\gamma} S^2 + K_{1\gamma} S + K_{0\gamma} = 0, \quad (33)$$

the coefficients $k_{\sigma\gamma}$ are selected so that the characteristic polynomial has its roots on the left side of the complex plane (Hurwitz) [50], [51]. The gains of the GPI controller for θ and ψ are shown in the Table 1:

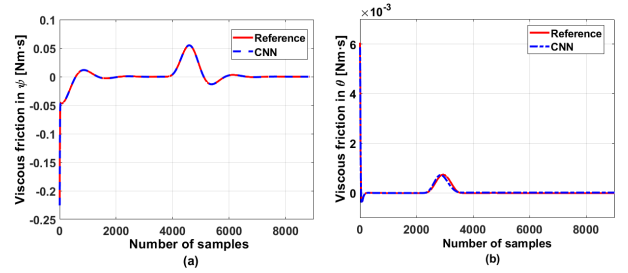
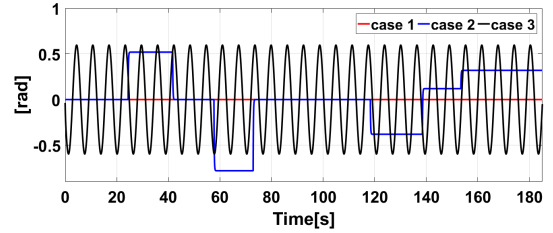

FIGURE 5. Estimation of the terms (a) $\hat{\beta}_\psi$ and (b) $\hat{\beta}_\theta$.

FIGURE 6. Disturbances.

TABLE 2. MSE obtained with CNN, DN and MLP.

Model	MSE for θ	MSE for ψ
CNN	4.07×10^{-4}	0.0011
DNN	3.48×10^{-3}	0.075
MLP	2.75×10^{-2}	0.14

TABLE 3. Bezier polynomial parameters.

γ	γ_i^*	γ_f^*	t_i	t_f
θ	$-0.7rad$	$0.2rad$	45s	75s
ψ	$-0.3rad$	$0.3rad$	75s	105s

IV. NUMERICAL SIMULATIONS

In this section the results of this work are described. First, the behaviour of the CNN for estimating the friction and velocity present in each coordinate are shown. Subsequently, we proceed to incorporate the CNN into the control scheme, showing the numerical results.

A. CNN RESULTS

Simulations for the estimation of friction terms are shown next. Two data set were used, consisting of 9250 samples of position, torque and friction. One data-set was used for training, whereas the other was used for testing. These data-set were obtained from the system in open loop and this process was made off-line. The matrix weights of the final iteration are used in control stage. For each CNN, the structure has two convolutional blocks, which implies that are 2 convolutional layers and 2 subsample layers, i.e. $n = 4$. The initialization of hyper-parameters is made within the range of $[-1, 1]$.

With respect to $\hat{\beta}_\theta$, the CNN as the regression order $r_{\theta_1} = r_{\theta_2} = 4$, there are $h = 10$ filters in each convolutional layer, the subsample length are $s^{(2)} = s^{(4)} = 2$. Estimation

TABLE 4. 2DOFH parameters.

Parameters	Variable	Magnitude	Units
Distance between the RP and the axis of rotation	rp	0.432	m
Distance between the RC and the axis of rotation	ry	0.233	m
Distance from the center of mass on the axis of rotation	L_{cm}	0.164	m
Helicopter body mass in motion at <i>pitch</i>	m_h	1.03	kg
Moment of inertia of the rotating body in <i>pitch</i>	$J_{eq,p}$	0.09359	kgm^2
Moment of inertia of the rotating body in <i>yaw</i>	$J_{eq,y}$	0.0947	kgm^2
RP force constant over <i>pitch</i>	k_{pp}	0.7901	$Nm/\%pwm$
RP force constant over <i>yaw</i>	k_{yy}	0.1426	$Nm/\%pwm$
RC force constant over <i>yaw</i>	k_{yy}	-0.5078	$Nm/\%pwm$
RC force constant over <i>pitch</i>	k_{py}	0.0329	$Nm/\%pwm$

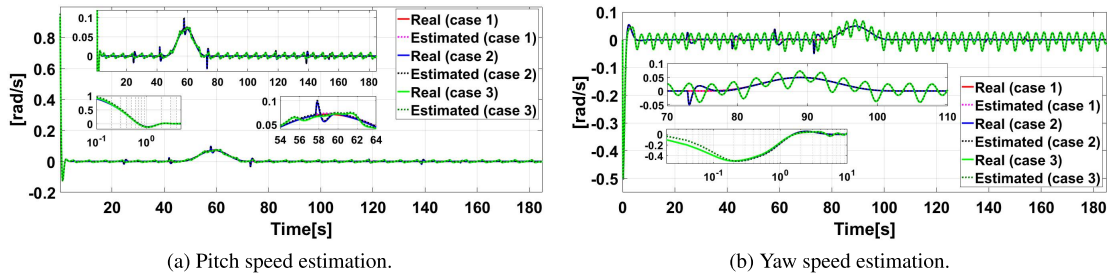


FIGURE 7. Speed estimation by CNN.

results are presented in Fig. 5a, the Mean Square Error (MSE) obtained is 4.07×10^{-4} .

For $\hat{\beta}_\psi$, the regression order are $r_{\theta_1} = 18$ and $r_{\theta_2} = 10$, 18 filters were used in each convolutional layer and subsample length are the same as before, $s^{(2)} = s^{(4)} = 2$. Simulation results are shown in Fig. 5b, obtaining an MSE of 0.0011.

The results obtained were compared with a MultiLayer Perceptron (MLP) and a modern Deep-Neural Network (DNN) structure [52]. It should be noted that CNN presented a lower MSE compared to MLP and DNN (see Table 2).

The DNN used for comparison contains 5 hidden layers and 80 entries for *theta*, 150 entries for *psi* and approximately 200 training epochs were needed to obtain acceptable results. The synaptic weight matrices were randomly initialized. Similar conditions were used for MLP, highlighting the better performance of the proposed CNN.

Remark 1: The coefficients obtained in Table 2 shall be interpreted alongside with the simulation conditions and their subsequent applicability in a physical environment for experimental tests, this means that the application of the DN and MLP architectures will hardly be used since their precision. It will be subject to specific conditions in the selection of a robust digital control system that guarantees the correct estimation of the parameters necessary for the control of the helicopter. Therefore, the CNN proposed by having more relaxed characteristics such as the number of inputs, will facilitate its application in a control system.

B. TRAJECTORY TRACKING

Several numerical simulations were made for the validation of the control scheme described in (25). The control objective

is to follow Bezier polynomial (γ^*) trajectories in both θ and ψ . Table 3 shows the parameters used for the reference trajectories, (γ_i^*) and (γ_f^*) correspond to the initial and final position, respectively; while (t_i) and (t_f) indicates the start and end time of the trajectories.

The simulations were carried out considering the following initial conditions: $\theta(0) = 0.92 \text{ rad}$ (equivalent to the initial state of the system is at rest), $\psi(0) = 0 \text{ rad}$, $\dot{\theta} = \dot{\psi} = 0 \text{ rad/s}$. Table 4 shows the physical parameters of 2DOFH.

The experiments carried out were based on 3 scenarios: The first considers the RC without disturbances present; whereas the second considers step-type disturbances that occur randomly in the RC; finally, the presence of constant oscillations in ϕ is contemplated (see Fig. 6).

V. COMPARISON AND DISCUSSION

In this section, we evaluate our proposed control scheme against the one reported in [15]. Both schemes use feedforward GPI controllers; however, [15] proposes the use of an integral reconstructor to approximate $\dot{\gamma}$, which is used only within the GPI controller; therefore, an exact linearization of the system is not achieved. In contrast, the current proposal contemplates the use of a CNN to estimate the speed and friction present in each degree of freedom, achieving a better compensation of the 2DOFH dynamics.

Thus, both control schemes were subjected to the disturbances described in Section IV-B. Subsequently, the Incremental Error (IE), Incremental Absolute Error (IAE), and Mean Square Error (MSE) metrics obtained in each experiment were compared.

Fig. 7 shows behavior of the velocities in θ and ψ for cases 1, 2 and 3, which are compared with the estimation

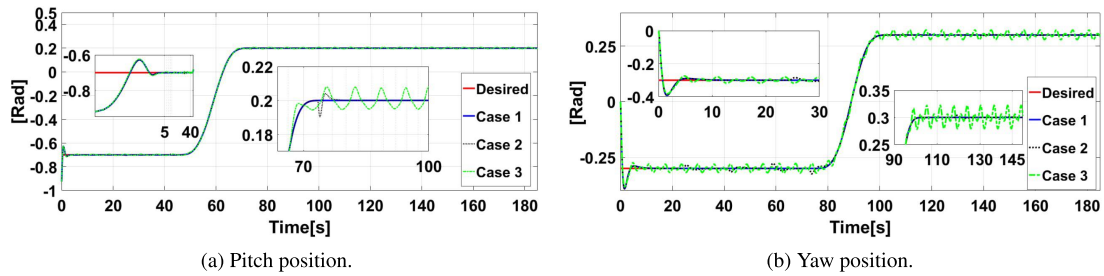


FIGURE 8. Results when using the variables estimated by the CNN.

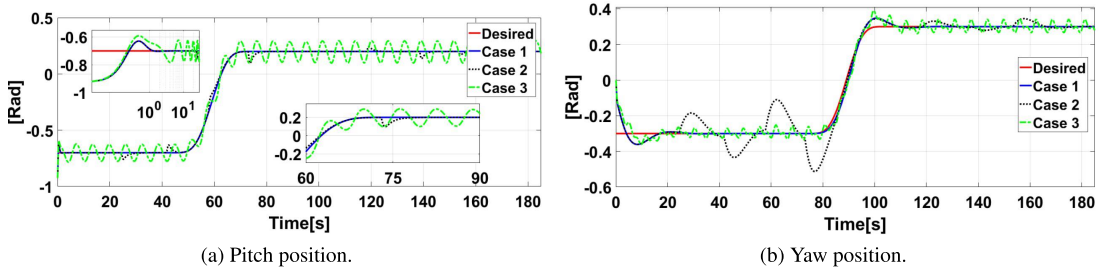


FIGURE 9. Results when using an integrative reconstructor.

TABLE 5. Incremental error (IE).

Case	Feedforward with CNN		Feedforward with integral reconstructor	
	Pitch	Yaw	Pitch	Yaw
1	-0.1135	0.2999	-0.1125	0.15
2	-0.1137	0.2999	-4.6972	17.2636
3	-0.1264	0.0821	3.9036	21.8791

TABLE 6. Incremental absolute error (IAE).

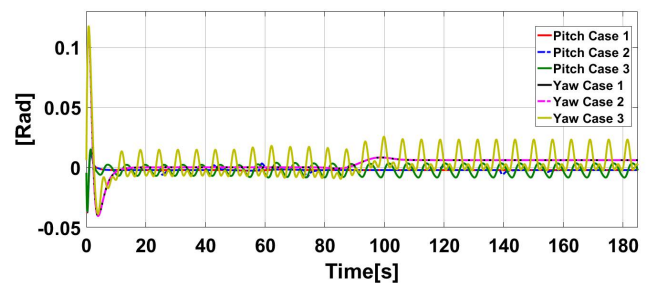
Case	Feedforward with CNN		Feedforward with integral reconstructor	
	Pitch	Yaw	Pitch	Yaw
1	0.1032	0.3263	0.0754	1.8060
2	0.1569	0.5891	1.0461	7.4910
3	0.7405	1.9566	10.7584	4.0783

TABLE 7. Mean of the squared error (MSE).

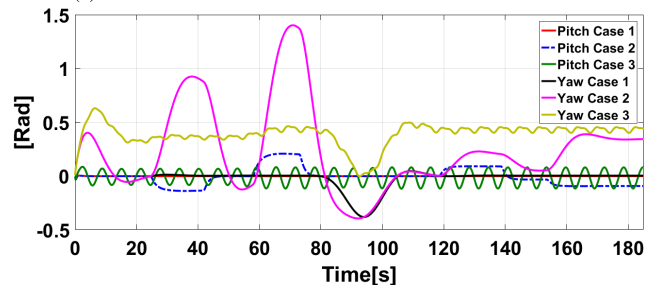
Case	Feedforward with CNN		Feedforward with integral reconstructor	
	Pitch	Yaw	Pitch	Yaw
1	44.89×10^{-6}	0.187×10^{-3}	0.0478×10^{-3}	0.5977×10^{-3}
2	45.94×10^{-6}	0.2×10^{-3}	0.2653×10^{-3}	4.27×10^{-3}
3	62.59×10^{-6}	0.31×10^{-3}	4.212×10^{-3}	1.075×10^{-3}

given by CNN. The CNN takes approximately 0.5s to converge to the real value of the velocity (even in case 3). However, it is observed that the network has a lower performance in the presence of aggressive disturbances. Despite the above, the estimation is quite good and favors the performance of the control scheme.

Figs. 8 and 9 show the results obtained for the trajectory tracking in θ and ψ , respectively. The results correspond to the cases defined in Section IV-B. Fig. 8 shows the system behaviour before a feedforward GPI controller in



(a) IE of the feedforward controller combined with the CNN.



(b) IE of the feedforward controller combined with an integrative reconstructor.

FIGURE 10. IE for θ and ψ .

combination with the estimation of speed and friction by means of a CNN; for its part, Fig. 9 shows the behavior of the helicopter when using the scheme described in [15]. It is observed that the proposed controller better approximates the desired trajectories. We must highlight the considerable improvement in the angle θ ; however, it seems that the angle ψ (case 3) has a similar behavior in both schemes, which is due to the direct incidence of RC disturbances in ψ , although the oscillations are of smaller amplitude when CNN is used.

The results of the IE, IAE and MSE metrics are shown in Tables 5, 6 and 7, respectively. The indices were applied in both control schemes to quantitatively evaluate their performance. It should be noted that for case 1, the IE and the IAE are lower when using an integral reconstructor; however, in the presence of disturbances, the feedforward scheme in conjunction with CNN performs better.

Fig. 10 shows the behavior of IE, which presents oscillations closer to zero with the scheme feedforward with CNN compared to the feedforward with an integral reconstructor.

VI. CONCLUSION

The simulation results showed that the feedforward controller in combination with the CNN provides higher performance compared to the scheme reported in (25). It should be noted that both schemes retain the active disturbance rejection properties of a GPI controller; however, the use of CNN reduces the need for integral reconstructors and allows the system to be approximated to a more linear representation.

The proposed CNN showed a good estimation of the parameters even when the system was subjected to disturbances in the TR. Despite the deviation that usually occurs in the estimation when subjecting the system to disturbances, the friction and speed obtained allowed a good compensation of the 2DOFH dynamics. Hence, the robustness of the proposed scheme against disturbances in the TR is demonstrated. Also, we must emphasize that CNN does not update its weights in real time, which reduces the computational requirements for its future implementation. Finally, it is important to mention that the use of CNN to estimate velocities and frictions consumes a higher computational cost compared to the integral reconstructor.

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