

RESEARCH ARTICLE

A Novel Event-Triggered Control of DC Microgrids Against Probabilistic Actuator Fault

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ABSTRACT This article investigates a problem of event-triggered controller design for DC microgrid, in which multiple nonlinear Constant power loads (CPLs) and probabilistic actuator fault are considered. A novel pre-averaged event-triggered mechanism (PAETM) is put forward, under which the average value of each time interval is used to determine the triggering instead of using the sample data that represents the system characteristic partially. Benefit from this mechanism, triggering events are reduced and the network burden is mitigated while the system performance is ensured, which contributes to a higher efficiency for DC microgrid. Considering various disturbances in DC microgrid, a unified PAETM controller design for DC microgrid with probabilistic distribution actuator fault and disturbance is proposed. Finally, a simulation example is shown to illustrate the validity of the proposed control strategy.

INDEX TERMS DC microgrid, pre-averaged event-triggered mechanism (PAETM), constant power load, actuator fault.

I. INTRODUCTION

As renewable energy develops, DC microgrids as a novel form of power system containing generators, loads, and energy storage have aroused extensive attention in both academic and industrial field [1]. DC microgrids demonstrate multiple superiorities for having higher efficiency and reliability, simpler control design procedure, and a more natural interface for various energy storage systems (ESSs) and loads, because of that, microgrids draws multi studies such as [2]–[4]. Hence, the stability and stabilization of DC microgrids are significant to be addressed.

Constant power loads (CPLs), which are modeled by loads in DC microgrids have some undesired effects, like exhibiting negative impedance characteristics [5] that may increase the nonlinearity degree of the system or even destabilize the overall system [6]. Several methods have been proposed to alleviate the negative effects, which can be sketchily separated into two types: the passive damping way and the active damping way. The passive damping way is mostly achieved by adding

a series of capacitors [7], which is limited because of low efficiency and its physical constraints. On the other side, the active damping way mainly focuses on the modification of the control loop [8], [9]. In [10], the control loop is modified to increase the damping of passive elements. However, this kind of method may experience side effects such as transient oscillation or loads damage. For this reason, the method of using injecting current to stabilize the DC microgrids is proposed, which includes linear and nonlinear approaches in general. The linear approach like [11], is achieved by taking the nonlinearity of CPLs out of consideration. The nonlinear methods of backstepping [5], [12], sliding mode [13], and robust control [14] are adopted to obtain certain effects. Yet it should be noticed that DC microgrids are mostly distributed, and the constituents of DC microgrids may spatially separate far from each other, which means the control signal and system information will be needed to be transmitted through the network environment and certain communicating schemes needed to be considered [1], [15].

Introducing network as a communication medium of DC microgrids brings various advantages such as higher efficiency and reliability. While making DC microgrids much

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more intelligent, the involvement of the network also brings challenges and problems. Communication structure needs to be designed, and certain performances caused by network that may destabilize the system need to be further investigated. Firstly, there are generally three communication structures: centralized structure [16], distributed structure [17], [18], and decentralized structure [1]. A centralized structure for its efficiency and realizability is utilized in this paper, which is achieved by gathering the information of each unit in the center controller to generate control signal. Secondly, the problems induced by the network mainly are network-induced delay and packet drops [19]. Also, the limitation of bandwidth as an inherent property of network that inevitably influences system performance must be considered which is not fully covered in the aforementioned results.

To cope with the network limitation, an alternative of periodic communication can be realized by ETM [20]. The ETM is designed by replacing the determination of whether the control signal need to be sent to a predefined event-triggered condition. This means the control signal will only be sent when the triggered condition is violated, saving network resources efficiently. Plenty of results like [21]–[23] indicate that ETM can save communication resources while retain the system performance in an acceptable range. Event-triggering control as a widely investigated subject in recent years has expanded in various forms [24]–[29]. In [27], an event-triggered tracking controller was proposed, and battery energy storage system control involving event-triggering is mentioned in [28]. For DC microgrids, authors in [30] presented an adaptive triggered controller while model uncertainties are considered. An event-triggered communication-based dynamic consensus algorithm was proposed in [31] to achieve both proportional current sharing and DC voltage regulation. And [32] proposed a novel form of the event triggering control by designing triggering conditions under super twisting reaching law. Meanwhile, the event-triggered control itself has expanded many varieties in development, such as the self-triggered control (STC) [33], [34], which predicted the next event instant based on the historical information and system knowledge, and dynamical event-triggering like [27], [35], [36], which adds more flexibility items to the event-triggered control. However, the DC microgrid system can be affected easily by various physical reasons, which cause many extra triggering events when applying traditional ETM. Those extra triggering events increase the network burden and cause energy-wasting, which motivates the present work.

In this work, to stabilize the disturbed DC microgrid while reducing the unnecessary triggering events, a novel event-triggered controller is proposed. The main contributions are as follows:

- 1) A novel PAETM for nonlinear DC microgrid system is proposed by replacing the conventional sampled data in ETM with average data, which contains the system information in each certain time interval and better represents the trend of the system. The proposed PAETM

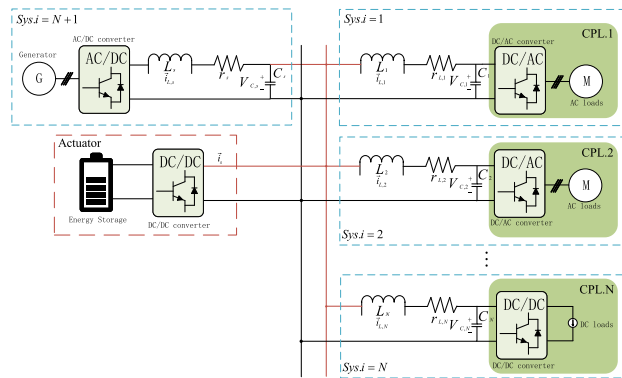


FIGURE 1. Circuit diagram.

effectively reduces the triggering events cause by disturbance, and mitigates the network burden and raises efficiency while ensuring system performance.

- 2) A new event-triggered control strategy is developed for nonlinear DC microgrid. Compared with the existing literatures, the probabilistic fault and external disturbance are considered in this research, which better reflect the actual interference experienced in DC microgrid. The use of this control strategy brings the lower consumption and higher efficiency of DC microgrid.

II. PROBLEM FORMULATION

A. SYSTEM DESCRIPTION

The structure of the DC microgrid with CPLs is depicted in Fig. 1. The basic physical variables of the DC microgrid is denoted the same as [37] for a convenience purpose. The microgrid is formed by $N + 1$ subsystems containing N CPLs and one ESS. By define the system state variable as $\tilde{x}_i(t) = [i_{L,i} \ v_{C,i}]^T$, $\tilde{x}_s = [i_{L,s} \ v_{C,s}]^T$. The state equation of i th CPL subsystem is considered as follows:

$$\dot{\tilde{x}}_i(t) = \mathcal{A}_i \tilde{x}_i(t) + f_i v_i(\tilde{x}_i(t)) + \mathcal{A}_{is} \tilde{x}_s(t), \quad (1)$$

where

$$\mathcal{A}_i = \begin{bmatrix} -\frac{r_{L,i}}{L_i} & -\frac{1}{L_i} \\ \frac{1}{C_i} & 0 \end{bmatrix}, f_i = \begin{bmatrix} 0 \\ \frac{1}{C_i} \end{bmatrix},$$

$$\mathcal{A}_{is} = \begin{bmatrix} 0 & \frac{1}{L_i} \\ 0 & 0 \end{bmatrix}, v_i(\tilde{x}_i(t)) = \frac{P_i}{v_{C,i}},$$

$$i = \{1, 2, \dots, N\}, s = N + 1.$$

Assuming that all the CPLs and powers are ideal and consider the current of ESS i_{es} as the control signal u . The state equation of DC source are as follows:

$$\dot{\tilde{x}}_s(t) = \mathcal{A}_s \tilde{x}_s(t) + bV_{dc} + b_u u(t) + \sum_{i=1}^N \kappa \tilde{x}_i(t), \quad (2)$$

where

$$\mathcal{A}_s = \begin{bmatrix} -\frac{r_s}{L_s} & -\frac{1}{L_s} \\ \frac{1}{C_s} & 0 \end{bmatrix}, b = \begin{bmatrix} \frac{1}{L_s} \\ 0 \end{bmatrix},$$

$$\kappa = \begin{bmatrix} 0 & 0 \\ -\frac{1}{C_s} & 0 \end{bmatrix}, b_u = \begin{bmatrix} 0 \\ -\frac{1}{C_s} \end{bmatrix}.$$

For the concise purpose the equilibrium point is shifted to origin by coordinate transformation. Augmenting the CPLs (1) and the ESS (2), and taking the external disturbance $\varrho(t) \in L_2[0, \infty)$ with appropriate dimension matrix \mathcal{W} into consideration, the state equation of the system is rewritten as:

$$\dot{x}(t) = \mathcal{A}x(t) + F\Upsilon(x(t)) + \mathcal{B}_u u(t) + \mathcal{W}\varrho(t), \quad (3)$$

where

$$x(t) = [x_1^T(t), x_2^T(t), \dots, x_N^T(t), x_s^T(t)]^T = \tilde{x}(t) - x_e,$$

$$\Upsilon(x(t)) = [v_1(x_1(t)), v_2(x_2(t)), \dots, v_N(x_N(t))]^T,$$

$$\mathcal{A} = \begin{bmatrix} \mathcal{A}_1 & 0 & \dots & 0 & \mathcal{A}_{1s} \\ 0 & \mathcal{A}_2 & \dots & 0 & \mathcal{A}_{2s} \\ \vdots & \vdots & \ddots & \vdots & \vdots \\ 0 & 0 & \dots & \mathcal{A}_N & \mathcal{A}_{Ns} \\ \kappa & \kappa & \dots & \kappa & \mathcal{A}_s \end{bmatrix},$$

$$F = \begin{bmatrix} f_1 & 0 & \dots & 0 \\ 0 & f_2 & \dots & 0 \\ \vdots & \vdots & \ddots & \vdots \\ 0 & 0 & \dots & f_N \\ 0 & 0 & \dots & 0 \end{bmatrix}, \mathcal{B}_u = \begin{bmatrix} 0 \\ \vdots \\ 0 \\ b_u \end{bmatrix},$$

and

$$v_i(x_i^T(t)) = \frac{P_i v_{C,i}}{v_{c0,i}(v_{C,i} + v_{c0,i})}, \quad (4)$$

in which x_e and $v_{c0,i}$ represent the equilibrium point of DC microgrid.

The nonlinear vector $\Upsilon(x(t))$ in the DC microgrid system (3) satisfies:

$$\Upsilon^T(x(t))\Upsilon(x(t)) = \sum_{i=1}^N v_i^T(x_i(t))v_i(x_i(t))$$

$$\leq \alpha^2 x^T(t)\mathcal{H}^T\mathcal{H}x(t), \quad (5)$$

where α is the robustness index, and the matrix \mathcal{H} is

$$\mathcal{H} = \begin{bmatrix} h & \dots & 0 & 0 \\ \vdots & \ddots & \vdots & \vdots \\ 0 & \dots & h_N & 0 \\ 0 & \dots & 0 & 0 \end{bmatrix}, h_j = \begin{bmatrix} 0 & 0 \\ 0 & 1 \end{bmatrix}, i \in 1, 2, \dots, N.$$

B. NOVEL EVENT-TRIGGERED SCHEME AND CONTROLLER DESIGN

The PAETM and the controller design will be developed in this part. An averaging mechanism is added to the system

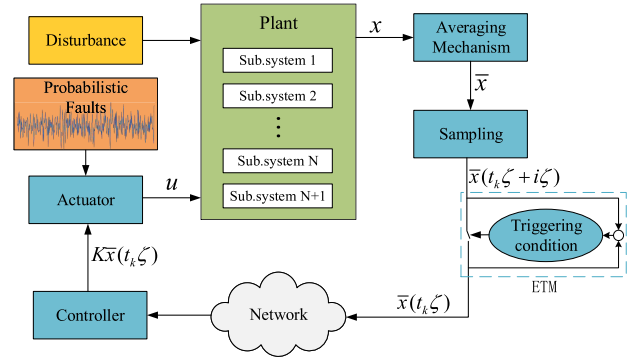


FIGURE 2. System structure.

before the sampling as Fig. 2 shows, which aims to achieve better performance. The averaging mechanism is designed as

$$\bar{x}(t) = \frac{1}{\mathcal{T}} \int_{t-\mathcal{T}}^t x(s)ds, \quad (6)$$

where \mathcal{T} denotes for the averaging period. The average mechanism (6) satisfies:

$$\frac{1}{\mathcal{T}} \int_{t-\mathcal{T}}^t x(s)ds \approx \frac{1}{6} [x(t) + 4x(t - \frac{\mathcal{T}}{2}) + x(t - \mathcal{T})]. \quad (7)$$

Remark 1: The average value of each time interval \mathcal{T} is sampled, and used to decide whether the system information is needed for stabilization. Under the traditional ETM, the fixed period sampling probably samples during the system jitter and generates sampling data that can not represent the system characteristic accurately. This data causes unnecessary triggering events. It may waste network resources and cause network jams. However, with this improvement, the unnecessary triggering caused by the aforementioned reason can be avoided, and the network resource can be efficiently used.

Remark 2: Notice that the average mechanism (6) is approximated by a time delay polynomials in (7), which makes the unified control design scheme achieved by the time-delay system approach possible.

Based on the averaging mechanism (6) and (7), the injecting current $u(t)$ as the control signal is considered as

$$u(t) = K\bar{x}(t), \quad (8)$$

where K represents the controller needed to be designed.

The injecting current of DC microgrid may experience fluctuation due to the load variation and interference from various reasons. Considering the probabilistic actuator faults, the controller (8) is rewritten as:

$$u(t) = \Lambda K\bar{x}(t) = \sum_{i=1}^m \lambda_i \mathcal{C}_i K\bar{x}(t), \quad (9)$$

where $\Lambda = \text{diag}\{\lambda_1, \dots, \lambda_m\}$; $\lambda_i (i = 1, \dots, m)$ stands for different independent stochastic variables which have

expectation $\bar{\lambda}_i(0 < \bar{\lambda} < \bar{\lambda}_{max})$ and variance β_i^2 ; $C_i = \text{diag}\{\underbrace{0, \dots, 0}_{i-1}, 1, \underbrace{0, \dots, 0}_{m-1}\}$.

Remark 3: DC microgrid experiences multiple influences from various sources, such as loads and powers. Therefore, probabilistic actuator fault and external disturbance are considered in this system model.

The release instants are denoted by $t_0\eta, t_1\eta, t_2\eta, \dots$, where $t_0\eta = 0$ is the initial instant, η denotes the sampling interval. By assuming the maximum delay time of the internet is ζ_M as a positive real number, the time-varying delay of network ζ_k has $\zeta_k \in [0, \zeta_M)$. By this, the signal sent at $\{t_0\eta, t_1\eta, t_2\eta, \dots\}$ will arrived at $\{t_0\eta + \zeta_0, t_1\eta + \zeta_1, t_2\eta + \zeta_2, \dots\}$, respectively. The definition of the network-induced delay $\zeta(t)$ and the event triggering error $\delta_k(t)$ is as follows:

$$\zeta(t) := t - t_k\eta - i\eta, \tag{10}$$

$$\delta_k(t) := \bar{x}(t_k\eta) - \bar{x}(t_k\eta + i\eta), \tag{11}$$

where $t \in \iota_i, i = 0, \dots, p_k, \zeta(t) \in [0, \eta + \zeta_M)$, and

$$\iota_i = \begin{cases} [t_k\eta + \zeta_k, t_k\eta + \eta + \zeta_M), & i = 0 \\ [t_k\eta + p_k\eta + \zeta_M, t_{k+1}\eta + \zeta_{k+1}), & i = p_k \\ [t_k\eta + i\eta + \zeta_M, t_k\eta + (i + 1)\eta + \zeta_M), & \textit{else} \end{cases}$$

Utilizing (7), the triggering condition is designed as

$$\delta_k^T(t)\Omega\delta_k(t) \leq \frac{\sigma}{36}m^T(t)\Omega m(t), \tag{12}$$

where

$$m(t) = x(t - \zeta(t)) + 4x(t - \zeta(t) - \frac{\mathcal{T}}{2}) + x(t - \zeta(t) - \mathcal{T}).$$

Then event triggered controller (9) can be expressed as follows by utilizing (10) and (11):

$$u(t) = \Lambda K(\delta(t) + \bar{x}(t - \zeta(t))). \tag{13}$$

Remark 4: The traditional ETM uses sample data to determine the triggering events and generates control signal. However, the fixed period sampling of this mechanism results in the system information loss between each two sampling instants. To solve this problem, an average value that contains the system information during sample intervals is used in our proposed PAETM, which can better represent the system characteristic. This information is used to decide whether triggering is necessary. This mechanism efficiently avoids the excess triggering events, which reduces the energy consumption and lengthens the operation life of the DC microgrid.

Remark 5: Obviously, the Zeno behavior can be successfully avoided under the proposed PAETM (12).

The dynamic of the DC microgrid (3) can be reconstructed as

$$\dot{x}(t) = \mathcal{A}x(t) + F\Upsilon(x(t)) + \mathcal{B}_u(\Lambda - \bar{\Lambda})K(\bar{x}(t - \zeta(t)) + \delta(t)) + \mathcal{B}_u\bar{\Lambda}K(\bar{x}(t - \zeta(t)) + \delta_k(t)) + \mathcal{W}\varrho(t), \tag{14}$$

where $\bar{\Lambda} = \text{diag}\{\bar{\lambda}_1, \dots, \bar{\lambda}_m\}$.

In this scheme, the feedback gain matrix K in (13) will be designed, which makes the system (14) globally asymptotically stable in mean square sense under the limited network environment.

III. MAIN RESULTS

In this section, based on the system discussed in (14) and the PAETM (12), under a given disturbance attenuation level γ , the state feedback control law will be designed to satisfy the condition $\|x(t)\|_2 \leq r \|\varrho(t)\|_2$ with $\varrho(t) \in L_2[0, \infty)$.

Theorem 1: For given scalars σ, α, γ and ρ , and gain matrix $K, \lambda_i(i = 1, \dots, m), \beta_i(i = 1, \dots, m)$. The DC microgrid system described as (14) is globally asymptotically stable in mean square sense if there exist matrices $P > 0, Q > 0, R > 0, \Omega > 0$ and S with appropriate dimensions that

$$\begin{bmatrix} \Xi_{M1} & * \\ \Xi_{M2} & \Xi_{M3} \end{bmatrix} < 0, \tag{15}$$

$$\begin{bmatrix} R & * \\ S & R \end{bmatrix} \geq 0, \tag{16}$$

where

$$\Xi_{M1} = \begin{bmatrix} \Xi_1 & * & * & * \\ \Xi_2 & -\Omega & * & * \\ \Xi_3 & 0 & -Q - R & * \\ \Xi_4 & \sqrt{\zeta_M}R\mathcal{B}_u\bar{\Lambda}K & 0 & -PR^{-1}P \end{bmatrix},$$

$$\Xi_{M2} = \begin{bmatrix} \Xi_5 & 0 & 0 & 0 \\ \Xi_6 & \theta & 0 & 0 \\ \Xi_7 & 0 & 0 & 0 \end{bmatrix},$$

$$\Xi_{M3} = \begin{bmatrix} -\alpha^{-2}I & * & * \\ 0 & \hat{R} & * \\ 0 & 0 & -I \end{bmatrix},$$

$$\Xi_1 = \begin{bmatrix} \xi_1 & * & * & * & * & * \\ F^T P & -I & * & * & * & * \\ \xi_2 & 0 & \frac{\sigma}{36}\Omega + \nu & * & * & * \\ \xi_3 & 0 & \frac{\sigma}{9}\Omega & \frac{4\sigma}{9}\Omega + \nu & * & * \\ \xi_4 & 0 & \frac{\sigma}{36}\Omega & \frac{\sigma}{9}\Omega & \frac{\sigma}{36}\Omega + \nu & * \\ \mathcal{W}^T P & 0 & 0 & 0 & 0 & -\gamma^2 I \end{bmatrix},$$

$$\Xi_2 = [K^T \bar{\Lambda}^T \mathcal{B}_u^T P \ 0 \ 0 \ 0 \ 0 \ 0],$$

$$\Xi_3 = [-\frac{1}{\zeta_M}S \ 0 \ \frac{1}{\zeta_M}(R + S) \ \frac{1}{\zeta_M}(R + S) \ \frac{1}{\zeta_M}(R + S) \ 0],$$

$$\Xi_4 = [\Xi_{41} \ \Xi_{42}],$$

$$\Xi_{41} = [\sqrt{\zeta_M}RA \ \sqrt{\zeta_M}RD \ \frac{1}{6}\sqrt{\zeta_M}R\mathcal{B}_u\bar{\Lambda}K],$$

$$\Xi_{42} = \{\frac{2}{3}\sqrt{\zeta_M}R\mathcal{B}_u\bar{\Lambda}K \ \frac{1}{6}\sqrt{\zeta_M}R\mathcal{B}_u\bar{\Lambda}K \ \sqrt{\zeta_M}R\mathcal{W}\},$$

$$\Xi_5 = [\mathcal{H} \ 0 \ 0 \ 0 \ 0 \ 0],$$

$$\Xi_6 = [0 \ 0 \ \theta \ \theta \ 0 \ 0],$$

$$\Xi_7 = [I \ 0 \ 0 \ 0 \ 0 \ 0],$$

$$\xi_1 = \mathcal{A}^T P + PA + Q - \frac{1}{\zeta_M}R,$$

$$\xi_2 = \frac{1}{6}K^T \bar{\Lambda}^T \mathcal{B}_u^T P + \frac{1}{\zeta_M}(R + S),$$

$$\xi_3 = \frac{2}{3}K^T \bar{\Lambda}^T \mathcal{B}_u^T P + \frac{1}{\zeta_M}(R + S),$$

$$\begin{aligned} \xi_4 &= \frac{1}{6}K^T \bar{\Lambda}^T \mathcal{B}_u^T P + \frac{1}{5M}(R + S), \\ v &= \frac{1}{5M}(-2R - S - S^T), \\ \theta &= [\beta_1 RBC_1 K, \beta_2 RBC_2 K, \dots, \beta_m RBC_m K]^T, \\ \hat{R} &= \text{diag}\{\underbrace{R, \dots, R}_m\}. \end{aligned}$$

Proof: Choose the following Lyapunov functional as

$$\begin{aligned} V(t) &= x^T(t)Px(t) + \int_{t-5M}^t x^T(s)Qx(s)ds \\ &\quad + \int_{t-5M}^t \int_s^t \dot{x}^T(v)R\dot{x}(v)dv ds. \end{aligned} \quad (17)$$

Definition (9) leads to $\bar{\Lambda} = \mathcal{E}\{\Lambda\}$. Then we can get

$$\mathcal{E}\{\Lambda - \bar{\Lambda}\} = 0, \quad (18)$$

where $\mathcal{E}\{\cdot\}$ stands for expectation. Take the expectation of the derivative of $V(t)$ yields:

$$\begin{aligned} \mathcal{E}\{\dot{V}(t)\} &= \mathcal{E}\{2\dot{x}^T(t)Px(t) + x^T(t)Qx(t) \\ &\quad - x^T(t-5M)Qx(t-5M) \\ &\quad + 5M\dot{x}^T(t)R\dot{x}(t) - \int_{t-5M}^t \dot{x}^T(s)R\dot{x}(s)ds\} \\ &= \mathcal{E}\{2[x^T(t)A^T Px(t) + Y^T(x(t))F^T Px(t) \\ &\quad + \frac{1}{6}x^T(t-\zeta(t)-\mathcal{T})K^T \bar{\Lambda}^T \mathcal{B}_u^T Px(t) \\ &\quad + \frac{2}{3}x^T(t-\zeta(t)-\frac{\mathcal{T}}{2})K^T \bar{\Lambda}^T B^T Px(t) \\ &\quad + \frac{1}{6}x^T(t-\zeta(t))K^T \bar{\Lambda}^T \mathcal{B}_u^T Px(t) \\ &\quad + \delta^T(t)K^T \bar{\Lambda}^T \mathcal{B}_u^T Px(t) + \varrho^T(t)W^T Px(t)] \\ &\quad + x^T(t)Qx(t) - x^T(t-5M)Qx(t-5M) \\ &\quad + 5M\dot{x}^T(t)R\dot{x}(t) - \int_{t-5M}^t \dot{x}^T(s)R\dot{x}(s)ds\}, \end{aligned} \quad (19)$$

where

$$\begin{aligned} \mathcal{E}\{\dot{x}^T(t)R\dot{x}(t)\} &= \mathcal{E}\{(Ax(t) + F\Upsilon(x(t)) + \frac{1}{6}\mathcal{B}_u \bar{\Lambda} K m(t) \\ &\quad + \mathcal{B}_u \bar{\Lambda} K \delta(t) + \mathcal{W}\varrho(t))R(Ax(t) \\ &\quad + F\Upsilon(x(t)) + \frac{1}{6}\mathcal{B}_u \bar{\Lambda} K m(t) \\ &\quad + \mathcal{B}_u \bar{\Lambda} K \delta(t) + \mathcal{W}\varrho(t)) \\ &\quad + \frac{1}{36}m^T(t)F m(t) + \frac{1}{36}m^T(t)F \delta(t) \\ &\quad + \frac{1}{36}\delta^T(t)F m(t) + \frac{1}{36}\delta^T(t)F \delta(t)\}, \end{aligned}$$

and

$$F = K^T(\Lambda - \bar{\Lambda})^T B^T R B(\Lambda - \bar{\Lambda})K.$$

Utilizing (9) and (18), follows

$$\mathcal{E}\{F\} = \sum_{i=1}^m \beta_i^2 K^T C_i^T B^T R B C_i K. \quad (20)$$

By Jensen's inequality, we have

$$\int_{t-5M}^t \dot{x}^T(s)R\dot{x}(s)ds \leq \frac{1}{5M}\epsilon^T(t)J\epsilon(t), \quad (21)$$

where

$$\begin{aligned} \epsilon(t) &= [x(t) \ x(t-\zeta(t)) \ x(t-5M)]^T, \\ J &= \begin{bmatrix} -R & * & * \\ R+S & -2R-S-S^T & * \\ -S & R+S & -R \end{bmatrix}, \end{aligned}$$

combine (19) (20) (21), and by Schur's complement, the result is established. ■

Theorem 2: For given scalars σ, α, γ and ρ , and $\lambda_i (i = 1, \dots, m)$, $\beta_i (i = 1, \dots, m)$. The system described by (14) with the feedback gain $K = YX^{-1}$ is globally asymptotically stable in mean square sense if there exist matrices $X > 0, \tilde{Q} > 0, \tilde{\Omega} > 0, \tilde{R} > 0, \tilde{\Sigma} > 0$ and \tilde{S}, Y with appropriate dimensions such that

$$\begin{bmatrix} \Psi_{M1} & * \\ \Psi_{M2} & \Psi_{M3} \end{bmatrix} < 0, \quad (22)$$

$$\begin{bmatrix} \tilde{R} & * \\ \tilde{S} & \tilde{R} \end{bmatrix} \geq 0, \quad (23)$$

where

$$\Psi_{M1} = \begin{bmatrix} \Psi_1 & * & * & * \\ \Psi_2 & -\tilde{\Omega} & * & * \\ \Psi_3 & 0 & -\tilde{Q} - \frac{1}{5M}\tilde{R} & * \\ \Psi_4 & \sqrt{5M}\mathcal{B}_u \bar{\Lambda} Y & 0 & \rho^2 \tilde{R} - 2\rho X \end{bmatrix},$$

$$\Psi_{M2} = \begin{bmatrix} \Psi_5 & 0 & 0 & 0 \\ \Psi_6 & \theta' & 0 & 0 \\ \Psi_7 & 0 & 0 & 0 \end{bmatrix},$$

$$\Psi_{M3} = \begin{bmatrix} -\alpha^{-2}I & * & * \\ 0 & \hat{R}' & * \\ 0 & 0 & -I \end{bmatrix},$$

$$\Psi_1 = \begin{bmatrix} \psi_1 & * & * & * & * & * \\ F^T & -I & * & * & * & * \\ \psi_2 & 0 & \frac{\sigma}{36}\tilde{\Omega} + v' & * & * & * \\ \psi_3 & 0 & \frac{\sigma}{9}\tilde{\Omega} & \frac{4\sigma}{9}\tilde{\Omega} + v' & * & * \\ \psi_4 & 0 & \frac{\sigma}{36}\tilde{\Omega} & \frac{\sigma}{9}\tilde{\Omega} & \frac{\sigma}{36}\tilde{\Omega} + v' & * \\ \mathcal{W}^T & 0 & 0 & 0 & 0 & -\gamma^2 I \end{bmatrix},$$

$$\Psi_2 = [Y^T \bar{\Lambda} \mathcal{B}_u^T \ 0 \ 0 \ 0 \ 0 \ 0],$$

$$\Psi_3 = [-\frac{1}{5M}\tilde{S} \ 0 \ \frac{1}{5M}(\tilde{R} + \tilde{S}) \ \frac{1}{5M}(\tilde{R} + \tilde{S}) \ \frac{1}{5M}(\tilde{R} + \tilde{S}) \ 0],$$

$$\Psi_4 = [\Psi_{41} \ \Psi_{42}],$$

$$\Psi_{41} = [\sqrt{5M}AX \ \sqrt{5M}D \ \frac{1}{6}\sqrt{5M}\mathcal{B}_u \bar{\Lambda} Y],$$

$$\Psi_{42} = [\frac{2}{3}\sqrt{5M}\mathcal{B}_u \bar{\Lambda} Y \ \frac{1}{6}\sqrt{5M}\mathcal{B}_u \bar{\Lambda} Y \ \sqrt{5M}\mathcal{W}],$$

$$\Psi_5 = [\mathcal{H} \ 0 \ 0 \ 0 \ 0 \ 0],$$

$$\Psi_6 = [0 \ 0 \ \theta' \ \theta' \ \theta' \ 0],$$

$$\Psi_7 = [I \ 0 \ 0 \ 0 \ 0 \ 0],$$

$$\psi_1 = XA^T + AX + \tilde{Q} - \frac{1}{5M}\tilde{R},$$

$$\psi_2 = \frac{1}{6}Y^T \bar{\Lambda}^T \mathcal{B}_u^T + \frac{1}{5M}(\tilde{R} + \tilde{S}),$$

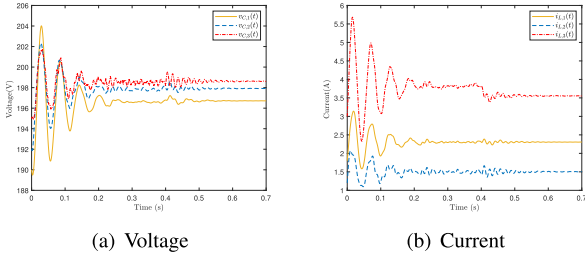


FIGURE 3. System responses with proposed ETM.

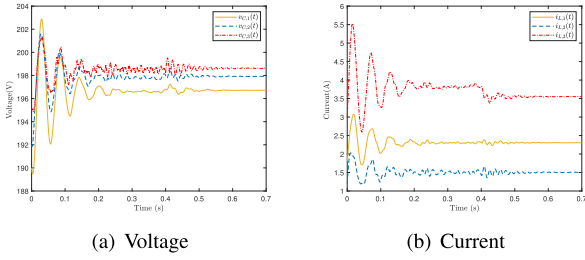


FIGURE 4. System responses with traditional ETM.

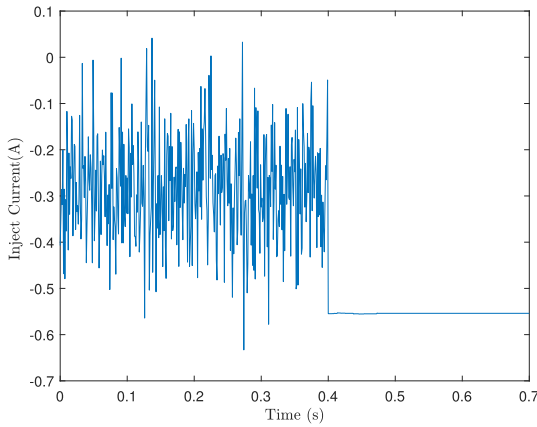


FIGURE 5. Inject current (A).

$$\psi_3 = \frac{2}{3} Y^T \bar{\Lambda}^T B_u^T + \frac{1}{\zeta_M} (\tilde{R} + \tilde{S}),$$

$$\psi_4 = \frac{1}{6} Y^T \bar{\Lambda}^T B_u^T + \frac{1}{\zeta_M} (\tilde{R} + \tilde{S}),$$

$$v' = -\frac{1}{\zeta_M} (2\tilde{R} + \tilde{S} + \tilde{S}^T),$$

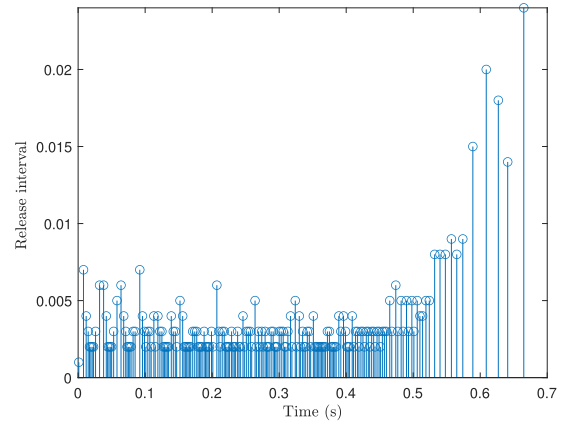
$$\theta' = [\beta_1 BC_1 Y, \beta_2 BC_2 Y, \dots, \beta_m BC_m Y]^T,$$

$$\hat{R}' = \text{diag}\{\underbrace{\tilde{R}, \dots, \tilde{R}}_m\}.$$

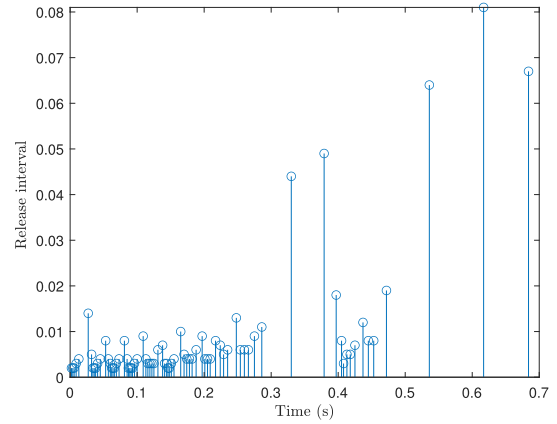
Proof: Based on the Theorem 1, post- and pre-multiplying the both sides of (15) with $\text{diag}\{X, I, X, X, X, X, I, X, R^{-1}, R^{-1}, I, I\}$ and its transpose, defining $X = P^{-1}$ and $\tilde{Q} = X^T Q X$, $\tilde{\Omega} = X^T \Omega X$, $\tilde{S} = X^T S X$, $\tilde{R} = X^T R X$, the (22) can be obtained. The proof is completed. ■

IV. SIMULATION

In this section, a simulation example is given as a verification of the presented control design method for the DC microgrid.



(a) Traditional ETM



(b) PAETM

FIGURE 6. Triggering event.

This example is a DC microgrid mentioned in [14], [37] and [38] which contains two CPLs and one ESS. The same system parameters of [14] are used in this section. The parameters needed are: $\sigma = 0.05$, $\zeta_M = 0.001$, $\rho = 0.1$, $\alpha = 0.09$. Selecting the disturbance attenuation level $r = 200$, while the external disturbance $q(t)$ and disturbance matrix \mathcal{W} chosen as follows:

$$q(t) = 30e^{-20t} \sin(100t), \quad (24)$$

$$\mathcal{W} = [1 \ 1 \ 1 \ 1 \ 1 \ 1]^T. \quad (25)$$

The actuator faults Λ is obeying a certain probabilistic distribution satisfied $\bar{\Lambda} = 0.5$ and $\beta = 0.2$, which indicate the actuator is experiencing backward gain while having fluctuations in small range. The averaging time is design as $\mathcal{T} = 0.03$, and the initial value of the system x_0 is chosen as:

$$x_0 = [1.80, 190.00, 1.20, 192.00, 3.00, 195.00]^T.$$

In order to gain better performance for this specific system, a restriction to enlarge controller K is considered as follows:

$$\|K\| \geq \mu, \quad (26)$$

where μ is a parameter need to be designed, we set $\mu = 0.046$ here.

From Theorem 2, it has $\|K\| = \|Y\| \|X\|^{-1}$. Then (26) can be rewrite as

$$\mu X^T X - Y^T Y \leq 0. \tag{27}$$

Define a new matrix $\mathcal{N} = Y^T Y$ and apply Schur's complement, there are

$$\begin{cases} \begin{bmatrix} -\mathcal{N} & X^T \\ X & -\frac{I}{\mu} \end{bmatrix} \leq 0, \\ \begin{bmatrix} -\mathcal{N} & Y^T \\ Y & -I \end{bmatrix} \leq 0. \end{cases} \tag{28}$$

By solving the Theorem 2 with the inequality (28), the matrix Ω and the feedback gain matrix K of the DC microgrid system are obtained as

$$\begin{aligned} \Omega &= 10^6 \times \begin{bmatrix} \Omega_{11} & \Omega_{12} \\ \Omega_{21} & \Omega_{22} \end{bmatrix}, \\ \Omega_{11} &= \begin{bmatrix} 4.9326 & -0.8863 & 0.0234 \\ -0.8863 & 3.9921 & -0.0008 \\ 0.0234 & -0.0008 & 4.9598 \end{bmatrix}, \\ \Omega_{12} &= \begin{bmatrix} -0.0035 & 0.0022 & -0.0238 \\ 0.0050 & -0.0073 & -0.0171 \\ -0.6546 & 0.0001 & -0.0434 \end{bmatrix}, \\ \Omega_{21} &= \begin{bmatrix} -0.0035 & 0.0050 & -0.6546 \\ 0.0022 & -0.0073 & 0.0001 \\ -0.0238 & -0.0171 & -0.0434 \end{bmatrix}, \\ \Omega_{22} &= \begin{bmatrix} 4.2574 & -0.0055 & -0.0163 \\ -0.0055 & 5.9847 & -0.0020 \\ -0.0163 & -0.0020 & 5.9819 \end{bmatrix}, \\ K &= [K_1 \ K_2], \\ K_1 &= [-0.0467 \ -0.0002 \ -0.0096], \\ K_2 &= [0.0001 \ 0.0016 \ -0.0096]. \end{aligned}$$

Figs. 3 – 6 present the simulation results in $[0, 0.7s]$, in which actuator fault occurs during $[0, 0.4s]$. Fig. 5 stands for the injecting-current which is the control input. The system performance with proposed PAETM is shown in Fig. 3, which indicate that even experiencing probabilistic actuator fault, the multiple nonlinear CPLs involved DC microgrid can still be stabilized. And the system performance with traditional ETM is shown in Fig. 4 by comparing it with Fig. 3, we can reach the conclusion that the system performance under proposed PAETM is still remain acceptable, while Fig. 6 further illustrates the effectiveness of the PAETM, subfigure (a) stands for the triggering event of the system with traditional mechanism, which has much more dense triggering events, especially when the actuator fault and disturbance occur, those extra triggering events cause much more energy consumption for ESS and rise the possibility of firmware damaging. Moreover, it occupies the network which may lead to system unstable. While subfigure (b) stands for the

TABLE 1. Releasing differences between two cases.

Cases	Normal	Improved
Total sampling	700	700
Total releasing	191	87
Releasing rate	27.29%	12.43%

system with the proposed average mechanism, it reduces non-essential triggering events while maintaining the system performance in certain degree. The data releasing rates between those two different cases are listed in the table 1.

It's obviously that, by using the proposed averaging mechanism, the data releasing rate drops 14.86% while the control performance remain acceptable.

The simulation result indicates that (i) The nonlinear CPLs involved DC Microgrid system are stable under the proposed control mechanism while the system experience external disturbance and uncertain actuator faults; (ii) By applying the proposed improvement, the triggering events are reduced while the system performance remains a certain level, which indicates the effectiveness of the proposed event-triggered mechanism on both saving network bandwidth and energy.

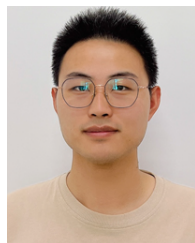
V. CONCLUSION

In this paper, a novel event-triggered control scheme design approach for DC microgrid system with actuator faults is proposed. This novel ETM can further reduce unnecessary triggering events. A practical actuator fault obeying certain distribution is taken into consideration. By utilizing Lyapunov stability theory and LMI method, the event-triggered controller has been designed. Furthermore, by introducing the averaging mechanism before the sampling, the average value of each sample interval has been obtained and used to evaluate the triggering condition. Benefit from this improvement, the quantity of triggering is reduced while the system performance is guaranteed. In the end, to verify the proposed control scheme for nonlinear DC microgrid system can stabilize the system and to illustrate the effectiveness of the proposed ETM, a simulation is given. For further study, the event-triggered fault diagnosis for DC microgrids with nonlinearities may worth deep investigation.

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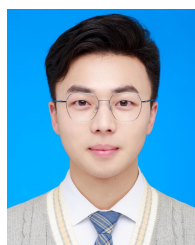
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