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# **Efficiency Map-Based PMSM Parameters Estimation Using Power-Oriented Modeling**

## DAVIDE TEBALDI

Department of Engineering "Enzo Ferrari," University of Modena and Reggio Emilia, 41125 Modena, Italy e-mail: davide.tebaldi@unimore.it

**ABSTRACT** This paper deals with two subjects. The first one is the presentation of a Matlab App created for PMSMs (Permanent Magnet Synchronous Motors) parameters estimation, both in the electrical and in the mechanical energetic domains. The second one is the presentation of a generalized PMSM Simulink superblock equipped with a user-friendly interface allowing to select options and to input the model parameters. The Matlab App and the PMSM superblock can be easily interfaced with each other. Finally, two simulation case studies are reported for the PMSM superblock.

**INDEX TERMS** Parameters estimation, PMSM, simulation, system efficiency, system modeling.

#### I. INTRODUCTION

PMSMs are employed in a very large variety of industrial fields, including robotics, aerospace, road and rail electric vehicles [1] and renewable energy applications such as solar water pumping [2]. Out of all the advantages PMSMs provide, good dynamic performances, high power density and high efficiency are surely among the most interesting ones [3]–[5]. The PMSM has to be chosen in order to satisfy the requirements of the given application, e.g. desired speed and torque range [5] etc. Once the most suitable PMSM has been identified, the modeling step has to be addressed, which is essential to effectively describe the machine behavior. Different modeling approaches can be found in the literature. As an example, the PMSMs modeling is addressed in a d-q discretetime reference frame in [6]. A modeling in the d-q frame is also employed in [7]-[10], whereas a fault diagnosis model based on a Siamese network is proposed in [11]. A fundamental advantage of model-based methods is the knowledge of the mathematical model of the system under consideration. This is not only important for an engineer to really understand the dynamics of the analyzed physical system, but it also allows to develop more effective control strategies which are based on the model knowledge. The PMSM models employed in all these works are very useful but lack of flexibility, i.e. they do not allow the user to select options, meaning whether to simulate in the three-phase static frame or the d-q frame or whether to account for the system mechanical dynamics or not, in order to perform lighter or heavier simulations. In [12] and [13], the Simulink blocks for interior and surface PMSM are presented. They allow a larger flexibility, but the inner structure of the model and the power flowing

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between the electrical and mechanical parts of the machine cannot be easily understood, since the power sections are not highlighted. The physical systems modeling can also be effectively addressed using suitable energy-based graphical formalisms such as Power-Oriented Graphs (POG) [14], Bond-Graph (BG) [15] and Energetic Macroscopic Representation (EMR) [15]. In this work, the POG modeling technique is used [14]. The latter is a graphical formalism which is very useful for describing systems dynamic models, as it allows to build block schemes which are directly implementable in Simulink and it also allows to effectively control the system power flows [16]. In this paper, a PMSM Simulink superblock is proposed [17]\PMSM\_Superblock, offering the following interesting functionalities: 1) straightforward compatibility with the PMSM parameters estimation Matlab App [17]\Estimation\_Matlab\_App proposed in this paper; 2) both speed and torque control are incorporated in the model; 3) the user can choose whether to compute the three-phase voltages and currents or not, leading to heavier or lighter simulations; 4) the user can choose if the rotor mechanical dynamics has to be included or not; 5) easy control and understanding of the power flows within the system.

The next important step to be addressed is PMSM parameters estimation, for which several approaches have been proposed in the literature. For example, a model reference adaptive system is proposed in [18], whereas a deterministic learning approach for identifying the system dynamics is addressed in [19]. A genetic algorithm for the search of the minimal point is studied in [20], whereas two offline and online estimation methods involving different system parameters are shown in [21] and [22]. Some other studies focus instead on the temperature estimation of PMSM, as shown in [23] where a Feedforward Neural Network is employed. In order to overcome the problem of parameters



estimation, efforts have been made to develop model-free control approaches for PMSMs, like the model-free predictive current control proposed in [24]. In this case, the concern is related to the current difference updating frequency in order to obtain a good performance. A compensated stator flux predictor is instead proposed in [25] in order to improve the prediction accuracy of the stator flux linkage vector. An exhaustive review of the current state of the art for PMSM offline and online estimation techniques is proposed in [5]. As far as online numerical methods are concerned, two examples are Recursive Least Square (RLS) and Extended Kalman Filter (EKF). Using RLS [26], a current injection-based method is proposed in [27], [28], whereas EKF is employed in [29].

In this paper, a Matlab App for PMSM parameters estimation [17]\Estimation\_Matlab\_App, both in the electrical and in the mechanical energetic domains, is proposed. This can be potentially suitable for self-commissioning applications, and can also be potentially extended to be used online. Furthermore, the Matlab App and the PMSM superblock can be easily interfaced with each other.

The remainder of this paper is organized as follows. Sec. II addresses the PMSM modeling and efficiency analysis. Sec. III presents the user interface and parameters definition of the Matlab App for PMSM parameters estimation, whereas Sec. IV describes its operation and working principles. Sec. V introduces the PMSM Simulink superblock together with two simulation examples, while the conclusions are finally reported in Sec. VI.

## **II. PMSM MODELING AND EFFICIENCY**

The state-space model of the PMSM in the d-q frame  $\Sigma_{\omega}$  can be written as follows:

$$\begin{bmatrix} p L_{se} & 0 & 0 & 0 \\ 0 & p L_{se} & 0 & 0 \\ \frac{0}{0} & 0 & p (L_{s} - M_{s0}) & 0 \\ 0 & 0 & 0 & 0 & J_{m} \end{bmatrix} \begin{bmatrix} {}^{\omega}I_{d} \\ {}^{\omega}\dot{I}_{g3} \\ \frac{\omega}{i_{g3}} \\ \dot{\omega}_{m} \end{bmatrix} = \begin{bmatrix} \mathbf{L} & \mathbf{X} \\ \mathbf{L} & \mathbf{L} \\ \mathbf{L} &$$

where L and A are the system energy and power matrices and x and u are the system state and input vectors. Terms  ${}^{\omega}K_d$ ,  ${}^{\omega}K_q$ ,  ${}^{\omega}K_s$ 3 are the three components of the PMSM torque vector  ${}^{\omega}K_{\tau}(\theta)$ , where  $\theta$  is the electric angle, whereas  ${}^{\omega}I_d$ ,  ${}^{\omega}I_q$ ,  ${}^{\omega}I_s$ 3 and  ${}^{\omega}V_d$ ,  ${}^{\omega}V_q$ ,  ${}^{\omega}V_s$ 3 are the three components of the PMSM current and voltage vectors  ${}^{\omega}I_s$  and  ${}^{\omega}V_s$ . The meaning

TABLE 1. Meaning of the parameters in systems (1), (2) and (3).

p	Number of polar expansions;
$R_s$	Stator phase resistance $(p=1)$ ;
$L_{se}$	$L_s + \frac{1}{2}M_{s0};$
$L_s$	Stator phase self inductance coefficient $(p = 1)$ ;
$M_{s0}$	Maximum value of mutual inductance between stator
	phases;
$b_m$	Rotor linear friction coefficient;
$\omega_m$	Motor angular velocity;
$^{\omega}K_q$	Motor torque constant;
$^{\omega}V_d$	Direct component of the motor input voltage vector;
$\omega V_q$	In-quadrature component of the motor input voltage
	vector;
$^{\omega}I_d$	Direct component of the motor output current vector;
$^{\omega}I_q$	In-quadrature component of the motor output current
	vector;
$ au_e$	External load torque applied to the motor;

of all the other parameters is reported in Table 1. The last component  ${}^{\omega}I_{s3}$  of the current vector  ${}^{\omega}I_{s}$  is proportional to the sum of currents  $I_{sh}$ , for  $h = \{1, 2, 3\}$ , circulating in the three stator phases. In order for the components of the torque vector  ${}^{\omega}K_{\tau}(\theta)$  to be constant, that is in order for the PMSM to be able to generate a constant torque if the current vector  ${}^{\omega}I_s$  is constant, the rotor flux has to be sinusoidal. In this way, only the in-quadrature component  ${}^{\omega}K_q$  of the torque vector  ${}^{\omega}K_{\tau}(\theta)$ is different from zero. Furthermore, under the hypothesis of star connected phases, a static constraint between the stator currents originates  $\sum_{h=1}^{3} I_{sh} = 0$ . This causes the third component  ${}^{\omega}I_{s3}$  of the current vector  ${}^{\omega}I_{s}$  to be equal to zero, which in turn implies that the electric part of the PMSM is described by a system having dynamic dimension equal to two. Therefore, under the hypothesis of sinusoidal rotor flux and star-connected stator phases, the state-space model of the PMSM in the d-q frame in (1) can be rewritten as:

$$\underbrace{\begin{bmatrix}
pL_{se} & 0 & 0 \\
0 & pL_{se} & 0 \\
\hline
0 & 0 & J_{m}
\end{bmatrix}}_{\mathbf{L}} \underbrace{\begin{bmatrix}
\omega \dot{I}_{d} \\
\omega \dot{I}_{q} \\
\dot{\omega}_{m}
\end{bmatrix}}_{\dot{\mathbf{x}}} = \underbrace{\begin{bmatrix}
pR_{s} & -p^{2}\omega_{m}L_{se} & 0 \\
p^{2}\omega_{m}L_{se} & pR_{s} & \omega K_{q} \\
\hline
0 & -\omega K_{q} & b_{m}
\end{bmatrix}}_{\mathbf{X}} \underbrace{\begin{bmatrix}\omega I_{d} \\
\omega I_{q} \\
\omega m
\end{bmatrix}}_{\mathbf{x}} + \underbrace{\begin{bmatrix}\omega V_{d} \\
\omega V_{q} \\
-\tau_{e}
\end{bmatrix}}_{\mathbf{u}} (2)$$

In steady-state conditions, the PMSM steady-state model (2) becomes [30]:

$$\mathbf{0} = \begin{bmatrix} pR_s & -p^2 \omega_m L_{se} & 0\\ p^2 \omega_m L_{se} & pR_s & \omega K_q \\ \hline 0 & -\omega K_q & b_m \end{bmatrix} \underbrace{\begin{bmatrix} \omega I_d \\ \omega I_q \\ \hline \omega_m \end{bmatrix}}_{\mathbf{x}_{ss}} - \underbrace{\begin{bmatrix} \omega V_d \\ -\tau_e \end{bmatrix}}_{\mathbf{x}_{ss}}, \quad (3)$$

where the parameters meaning is described in Table 1.



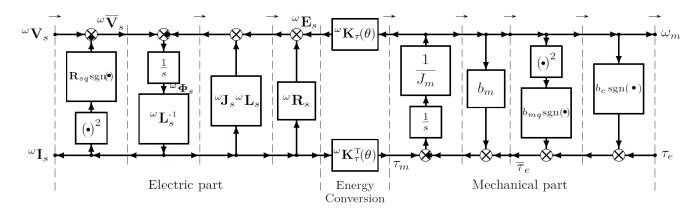


FIGURE 1. POG block scheme of the PMSM in the d-q frame with additional nonlinear friction terms.

Because the term highlighted in red in (3) is zero, it is convenient to enforce  ${}^{\omega}I_d=0$  since this is the condition maximizing the motor efficiency, as proven in [30]. Under this condition and doing some algebra, system (3) is reduced to:

$$\underbrace{\begin{bmatrix} {}^{\omega}I_{q} \\ \omega_{m} \end{bmatrix}}_{y} = \underbrace{\begin{bmatrix} b_{m} & {}^{\omega}K_{q} \\ pR_{s}b_{m} + {}^{\omega}K_{q}^{2} & pR_{s}b_{m} + {}^{\omega}K_{q}^{2} \\ {}^{\omega}K_{q} & pR_{s}b_{m} + {}^{\omega}K_{q}^{2} \end{bmatrix}}_{H_{0}} \underbrace{\begin{bmatrix} {}^{\omega}V_{q} \\ \tau_{e} \end{bmatrix}}_{u}. \tag{4}$$

If  ${}^{\omega}I_d = 0$  the PMSM behaves, in first approximation, as a linear system and its maximum efficiency  $E^*$  [30]- [31] is given by [30]-Eq. (30). At steady-state, the PMSM efficiency E when working as a motor, i.e. with a power flow oriented from section  $(y_1, u_1) = ({}^{\omega}I_q, {}^{\omega}V_q)$  to section  $(y_2, u_2) = (\omega_m, \tau_e)$ , is:

$$E = \frac{u_2 \, y_2}{u_1 \, y_1} = \frac{\tau_e \, \omega_m}{\omega \, V_a \, \omega \, I_a}. \tag{5}$$

In order for the considered model to reproduce an actual PMSM efficiency map, the linear approximation is not sufficient, and some nonlinear dissipative terms have to be added. A graphical representation of the PMSM dynamics including the needed nonlinear dissipative terms is given by the POG block scheme reported in Fig. 1. The power variables  ${}^{\omega}V_s$  and  $\tau_e$  in (4) must be replaced by  ${}^{\omega}\overline{V}_s$  and  $\overline{\tau}_e$ , defined as:

$${}^{\omega}\overline{V}_{s} = {}^{\omega}V_{s} - R_{sq}\operatorname{sgn}\left({}^{\omega}I_{s}\right){}^{\omega}I_{s}^{2},$$
  

$$\overline{\tau}_{e} = \tau_{e} + b_{c}\operatorname{sgn}(\omega_{m}) + b_{mq}\operatorname{sgn}(\omega_{m})\omega_{m}^{2}.$$
 (6)

Since  ${}^{\omega}I_d = 0$ , the first equation in (6) becomes:

$${}^{\omega}\overline{V}_{q} = {}^{\omega}V_{q} - R_{sq}\operatorname{sgn}\left({}^{\omega}I_{q}\right){}^{\omega}I_{q}^{2}. \tag{7}$$

The nonlinear friction terms in (6) and (7) are: the Coulomb friction  $b_c \operatorname{sgn}(\omega_m)$ , the air friction  $b_{mq} \operatorname{sgn}(\omega_m) \omega_m^2$  and the Joule dissipation  $R_{sq} \operatorname{sgn} \left( {}^{\omega}I_q \right) {}^{\omega}I_q^2$ . By rewriting (4) as a function of  $\tau_e$  and  $\omega_m$  and replacing  $\tau_e$  and  ${}^{\omega}V_q$  with  $\overline{\tau}_e$  and

 $\omega \overline{V}_q$  in (6) and (7), one obtains:

$$\begin{bmatrix} {}^{\omega}\overline{V}_{q} \\ {}^{\omega}I_{q} \end{bmatrix} = \begin{bmatrix} \frac{R_{s}p}{{}^{\omega}K_{q}} & \frac{{}^{\omega}K_{q}^{2} + pR_{s}b_{m}}{{}^{\omega}K_{q}} \\ \frac{1}{{}^{\omega}K_{a}} & \frac{b_{m}}{{}^{\omega}K_{a}} \end{bmatrix} \begin{bmatrix} \overline{\tau}_{e} \\ \omega_{m} \end{bmatrix}. \tag{8}$$

## **III. ESTIMATION ROUTINE APP: INTERFACE**

The main user interface of the PMSM parameters estimation Matlab App is shown in Fig. 2, where the reported parameters and results refer to a fictitious machine. The installation file for the proposed Matlab App, created with Matlab R2018b, is named PMSM\_parameters\_estimation.mlappinstall and can be found in the supplementary material in the dataset [17] \Estimation\_Matlab\_App. The operations the user needs to perform before the estimation begins are summarized in the flowchart of Fig. 3 and detailed in the next subsection.

## A. TO BE DEFINED BEFORE THE ESTIMATION BEGINS

Fig. 2 clearly shows the parameters to be estimated in the enlarged magenta window, which can be subdivided into two groups: known and unknown. If a dissipative parameter is known, its selection in the "Estimate?" window must be set to "No" and the corresponding input value will be interpreted as the exact one. If a dissipative parameter is unknown, its selection in the "Estimate?" window must be set to "Yes", the parameter will be estimated and the given value will be used as initial condition. The torque constant  ${}^{\omega}K_q$  is treated as a special case, as it allows one more choice for the user: • if the  ${}^{\omega}K_q$  knob is set to "Yes",  ${}^{\omega}K_q$  is unknown and will be estimated as in Sec. IV-A; • if "No" is selected,  ${}^{\omega}K_q$  is unknown and will be computed as in Sec. IV-B; • if "User Defined" is selected,  ${}^{\omega}K_q$  is known and the provided value will be interpreted as the exact final one. In the "Define the following parameters:" window, some information has to be user-defined. Among this, note that "Speed at Drop Torque: W\_jump" is the machine speed at which the motor

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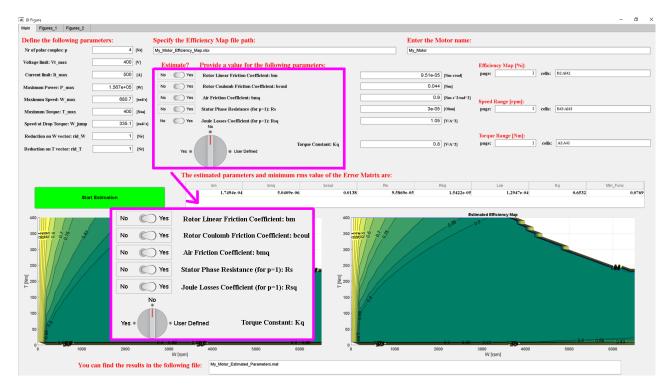


FIGURE 2. Home screen of the user interface created in app designer for the estimation routine.

torque drops following the constant maximum power curve  $(\omega_{m_i} \text{ in Fig. 4})$ , whereas "Reduction on W vector: rid\_W" and "Reduction on T vector: rid\_T" are two positive integer numbers,  $\in \{1 \ldots, m\}$  and  $\in \{1 \ldots, n\}$  respectively, used to reduce the number of elements in the speed and torque vectors  $\boldsymbol{\omega}_m \in \mathbb{R}^{(m \times 1)}$  and  $\boldsymbol{\tau}_e \in \mathbb{R}^{(n \times 1)}$  introduced in Sec. IV-A.

## **B. RESULTS OF THE ESTIMATION**

The Start Estimation button in Fig. 2 starts the estimation procedure and turns into Start Estimation until the estimation ends. The resulting estimated parameters are shown in the "The estimated parameters and minimum rms value of the Error Matrix are:" window, together with the final value "Min Func" of the objective function Q in (11). The left Matlab figure shows the actual efficiency map  $E_{map_{act}}(\omega_m, \tau_e)$  provided by the input Excel file. The right output Matlab figure shows the estimated efficiency map  $E_{map_{est}}(\omega_m, \tau_e)$  computed as described in Sec. IV-A and the maximum torque vs speed characteristic  $\tau_{e_{max}}(\omega_m)$  computed as described in Sec. IV-E. Other interesting output figures are provided by the Matlab App in the "Figures\_1" and "Figures\_2" screens, see PMSM\_parameters\_estimation.mlappinstall in [17]\Estimation\_Matlab\_App, such as the distribution of vectors  ${}^{\omega}V_s$  and  ${}^{\omega}I_s$  vs  $(\omega_m, \tau_e)$ , the  $E_{map_{error}}$  on plane  $(\omega_m, \tau_e)$  defined in (10), the resistive voltage due to  $R_s$  and to  $R_s$  and  $R_{sq}$  together, and the resistive torque due to  $b_m$  and to  $b_m$ ,  $b_{mq}$  and  $b_{coul}$  together.

## IV. ESTIMATION ROUTINE: THEORY

In this section, the theory and the implementation of the PMSM parameters estimation routine are analyzed and commented.

# A. ESTIMATION OF DISSIPATIVE TERMS AND ${}^{\omega}K_q$

Out of  $b_m$ ,  $R_s$ ,  $b_c$ ,  $b_{mq}$ ,  $R_{sq}$  and  ${}^{\omega}K_q$ , the user can select the unknown ones to be estimated, see Sec. III-A. The estimation makes use of the actual efficiency map  $E_{map_{act}}$  of the considered PMSM. The actual efficiency map  $E_{map_{act}}$  is, in general, a rectangular matrix  $E_{map_{act}} \in \mathbb{R}^{(n \times m)}$ , where n is the number of elements in the torque vector  $\boldsymbol{\tau}_e$  and m is the number of elements in the speed vector  $\boldsymbol{\omega}_m$ :  $\boldsymbol{\tau}_e \in \mathbb{R}^{(n \times 1)}$ ,  $\boldsymbol{\omega}_m \in \mathbb{R}^{(m \times 1)}$ . Using the user defined values of the parameters, representing the *initial value* for the unknown ones and the *exact final value* for the known ones, the routine loops over the set of operating points in the output plane  $(y_2, u_2) = (\omega_m, \tau_e) \in S$ , where the set S is defined as:

$$S = \{(\omega_{m_i}, \tau_{e_j}) \text{ s.t. } \omega_{m_i} \tau_{e_j} \leq P_{max} \},$$
  
for  $i \in \{1, 2, ... m\}$   $j \in \{1, 2, ... n\}$ , (9)

with  $P_{max}$  being the maximum motor power. For simplicity of notation, let  $S_h$  denote the generic couple  $(\omega_{m_i}, \tau_{e_j})$ , for i and j in (9). The routine exploits (6) and (8) to compute the couple  $(y_1, u_1) = ({}^{\omega}I_{qS_h}, {}^{\omega}V_{qS_h})$ , associated with the considered operating point on the output plane  $S_h \in S$ . By using (5), the estimated efficiency  $E_{map_{est_{S_h}}}$  of the PMSM in  $S_h \in S$  can be computed. By looping over all the output plane points  $S_h \in S$ , the estimation routine builds the estimated efficiency map



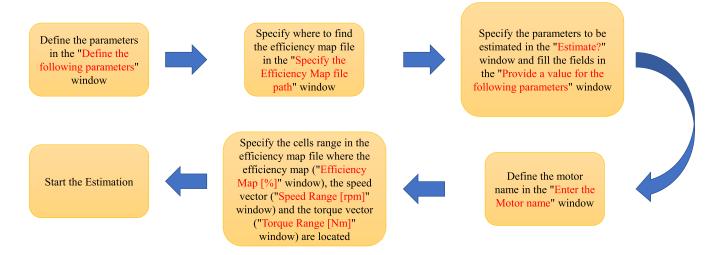
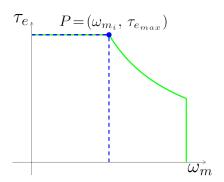


FIGURE 3. Operations to be performed before the estimation begins.



**FIGURE 4.** Point P =  $(\omega_{m_j}, \tau_{e_{max}})$  on the maximum torque vs speed characteristic  $\tau_{e_{max}}(\omega_m)$ .

 $E_{map_{est}}$ . The remaining empty elements  $E_{map_{est}}$ , for  $S_h \notin S$ , are set to zero. The efficiency error map is then computed:

$$E_{map_{error}} = |E_{map_{act}} - E_{map_{est}}|. (10)$$

The fminsearch Matlab function is then employed in order to perform a defined number of iterations allowing to identify the values of the parameters that the user has selected to estimate, in order to minimize the function:

$$Q = \sqrt{\left(\frac{1}{r}\right) \sum_{h=1}^{r} (E_{map_{error}S_h})^2}, \quad r = \dim(S).$$
 (11)

# B. COMPUTATION OF THE TORQUE CONSTANT ${}^\omega K_q$

In the " ${}^\omega K_q$  knob  $\to$  No" special case in Sec. III-A,  ${}^\omega K_q$  is computed as follows. Reference is made to the case of maximum torque generation  $\tau_{e_i} = \tau_{e_{max}}$ , i.e.  $|{}^\omega I_s| = |{}^\omega I_{s_{max}}|$ . Assuming  ${}^\omega I_d = 0$  and star-connected phases,  $|{}^\omega I_s| = |{}^\omega I_q|$  holds. From (3) and  $\tau_m = {}^\omega K_q {}^\omega I_q$  (see Fig. 1), and neglecting the dissipative terms affecting the mechanical part  $b_m$ ,  $b_c$  and  $b_{mq}$  (for the computation of  ${}^\omega K_q$  only) introduced in Fig. 1, (6) and (7), it follows  ${}^\omega K_q = \tau_{e_{max}}/|{}^\omega I_q| = \tau_{e_{max}}/|{}^\omega I_{s_{max}}|$ .

## C. COMPUTATION OF THE DYNAMIC TERM Lse

Let us assume  $\tau_{e_j} = \tau_{e_{max}}$ , for which  $|{}^{\omega}I_s| = |{}^{\omega}I_{s_{max}}|$  holds. Let operating point P on the output plane:

$$P = (y_2, u_2) = (\omega_{m_i}, \tau_{e_{max}})$$
 (12)

be the one giving the maximum motor torque and power:  $\tau_e = \tau_{e_{max}}$  and  $P_m = P_{max}$ . Point P is shown on the maximum torque vs speed characteristic  $\tau_{e_{max}}(\omega_m)$  of the motor reported in Fig. 4. Assuming  ${}^{\omega}I_d = 0$  and star-connected phases,  $|{}^{\omega}I_s| = |{}^{\omega}I_q|$  holds. From (3),  $\tau_m = {}^{\omega}K_q {}^{\omega}I_q$ , (6), (7), (8), and using point P in (12), it is:

$$|^{\omega}I_{q_{max}}| = |^{\omega}I_{s_{max}}|$$

$$= \frac{\tau_e + b_c \operatorname{sgn}(\omega_{m_j}) + b_{mq} \operatorname{sgn}(\omega_{m_j})\omega_{m_j}^2 + b_m \omega_{m_j}}{{}^{\omega}K_a}.$$

From (3), (6), (7) and (8), one can notice that:

$$^{\omega}V_{q_j} = pR_s^{\omega}I_{q_{max}} + ^{\omega}K_q\omega_{m_j} + R_{sq}\operatorname{sgn}(^{\omega}I_{q_{max}})^{\omega}I_{q_{max}}^2.$$

By assuming  $|{}^{\omega}V_s| = |{}^{\omega}V_{s_{max}}|$  in the considered operating point  $(\omega_{m_j}, \tau_{e_{max}}) \in S$ , and assuming star-connected stator phases, one obtains:  ${}^{\omega}V_{d_j} = \sqrt{|{}^{\omega}V_{s_{max}}|^2 - {}^{\omega}V_{d_j}^2}$ . From the first equation in (3), it follows:

$$L_{se} = \left| \frac{{}^{\omega}V_{dj}}{-p^2 \, \omega_m \, {}^{\omega}I_{q_i}} \right|. \tag{13}$$

From (13), parameter  $L_{se}$  is computed.

## D. DISTRIBUTION OF $|\omega V_s|$ AND $|\omega I_s|$ ON $(\omega_m, \tau_e)$

After the estimation, Eqs. (6), (7) and (8) are once again exploited to compute the couple  $({}^{\omega}I_{qS_h}, {}^{\omega}V_{qS_h})$  associated with all the operating points on the output plane  $S_h \in S$  in (9). Since  ${}^{\omega}I_d = 0$  is enforced,  $|{}^{\omega}I_s|(\omega_m, \tau_e) = |{}^{\omega}I_q|(\omega_m, \tau_e)$  holds. The latter is provided as output in the top-right figure of the "Figures\_1" results screen. As for the voltage vector  ${}^{\omega}V_s$ ,

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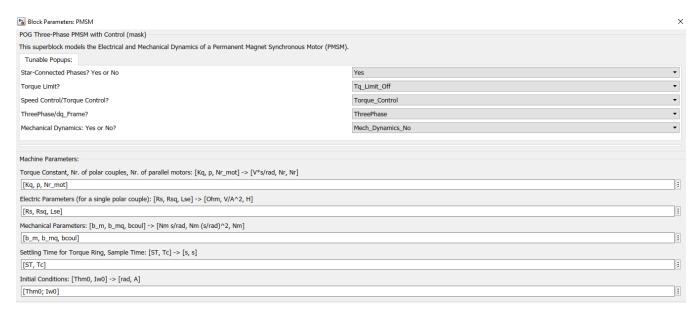


FIGURE 5. PMSM superblock user interface.

the remaining direct component  ${}^{\omega}V_d$  needs to be computed by using the first equation of (3). From  ${}^{\omega}V_d$  and  ${}^{\omega}V_q$ , the distribution  $|{}^{\omega}V_s|(\omega_m, \tau_e)$  can be computed. The latter is provided as output in the top-left figures of the "Figures\_1" and "Figures\_2" results screens.

# E. Derivation of characteristic $\tau_{e_{max}}(\omega_m)$

From  $\tau_m = {}^\omega K_q^\omega I_q$  and  ${}^\omega I_d = 0$ , it follows that the maximum motive torque is achieved when  $|{}^\omega I_q| = |{}^\omega I_{s_{max}}|$ . Additionally, from the third equation of (3) and from the second equation of (6) it is known that, at steady-state, the motive torque  $\tau_m = {}^\omega K_q{}^\omega I_q$  and the external torque  $\tau_e$  are related to each other through  $b_m$ ,  $b_c$  and  $b_{mq}$ . Since  ${}^\omega I_d = 0$ , let us define a new in-quadrature current component vector  $|{}^\omega I_{q_{vect}}|$  covering the whole range from 0 to  $|{}^\omega I_{s_{max}}|$  with steps of 1A, and let us call i the index looping over this vector covering the whole range of torque  $\tau_e$  from zero up to  $\tau_{e_{max}}$  thanks to the relation between the motive torque  $\tau_m$  and the external torque  $\tau_e$  highlighted above. The computation of the different torque versus speed characteristics  $\tau_e(\omega_m)$  up to  $\tau_{e_{max}}(\omega_m)$  for all current values within  $|{}^\omega I_{q_{vect}}|$  can then be performed.

### V. PMSM SUPERBLOCK

This section describes the mask interface of the PMSM superblock reported in Fig. 5, which is subdivided into two containers: "Machine Parameters" and "Tunable Popups". The PMSM superblock is provided in the Simulink block schemes EM\_Speed\_Control\_slx.slx and EM\_Torque\_Control\_slx.slx in [17]\PMSM\_Superblock created with Matlab R2018B. The "Machine Parameters" container minimal configuration is shown in Fig. 5, reporting the parameters that always have to be defined, whereas more parameters appear selecting the different options in the "Tunable Popups" container. The parameters meaning is described in the "Help" section

of the PMSM superblock interface. The parameters to be defined in the "Tunable Popups" container are: Star-Connected Phases? Yes or No  $\Rightarrow$  {Yes, No}, Torque Limit? ⇒ {Tq\_Limit\_On, Tq\_Limit\_Off}, Speed Control/Torque Control? ⇒ {Speed\_Control, Torque\_Control}, ThreePhase/ dq\_Frame? ⇒ {ThreePhase, dq\_Frame}, Mechanical Dynamics: Yes or No?  $\Rightarrow$  {Mech\_Dynamics\_Yes, Mech\_Dynamics\_No. The names of the popups reflect their meaning, and more details are also given in the "Help" section of the PMSM superblock interface, together with the new parameters to be defined in the "Machine Parameters" container when selecting the different "Tunable Popups" options. The tunable popup "Star-Connected Phases? Yes or No" must be set to "Yes" in order to interface the PMSM superblock with the parameters estimation routine. The external view of the PMSM superblock also changes depending on the options selected for the tunable popups. For the sake of brevity, only the external view of the PMSM superblock with one popups configuration is shown in this paper, see Fig. 6. The Reader is invited to try the other options in the Simulink block schemes EM\_Speed\_Control\_slx.slx and EM\_Torque\_Control\_slx.slx in [17]\PMSM\_ Superblock.

When compared with other simulation tools, such as the models made available by the Matlab/Simulink [12]- [13] for example, the proposed PMSM superblock offers some advantages. As far as the mechanical part of the motor is concerned, the proposed PMSM superblock accounts for one more friction effect, namely the air friction, exhibiting a square dependence on the motor speed. As far as the electrical part of the motor is concerned, the proposed PMSM superblock accounts for one more dissipative effect, namely the Joule losses, exhibiting a square dependence on the current vector components. These two dissipative effects are important when reproducing the efficiency map



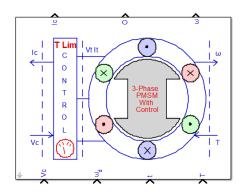


FIGURE 6. PMSM superblock external view with "Tq\_Limit\_On", "Speed\_Control", "ThreePhase" and "Mech\_Dynamics\_Yes" selected.

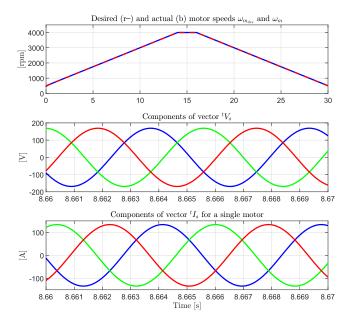


FIGURE 7. Simulation performed in EM\_Speed\_Control.m.

of an actual PMSM in the different operating points. Furthermore, an important advantage of the proposed PMSM superblock is the fact that it can be directly used in conjunction with the proposed PMSM parameters estimation Matlab App [17]\Estimation\_Matlab\_App. The user can first use the PMSM parameters estimation Matlab App to estimate the motor parameters from the efficiency map and then directly feed the estimated parameters to the PMSM superblock.

### A. SIMULATIONS

The supplementary material in the dataset [17]\PMSM\_Superblock reports two scripts EM\_Speed\_Control.m and EM\_Torque\_Control.m, simulating the Simulink models EM\_Speed\_Control\_slx.slx and EM\_Torque\_Control\_slx.slx, respectively. The two scripts contain two simulation examples applying a speed and a torque control to the PMSM, respectively. The PMSM parameters employed in this case are those of the fictitious machine

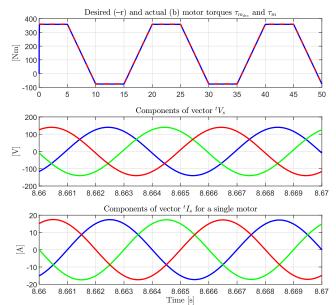


FIGURE 8. Simulation performed in EM\_Torque\_Control.m.

reported in My\_Motor\_Estimated\_Parameters. mat, estimated in [17]\Estimation Matlab App. Both in EM\_Speed\_Control.m and in EM\_Torque Control.m, the tunable popup options chosen in the two cases are set from line 10 to line 15 of the scripts, but can also be manually set from the PMSM superblock user interface itself. The remaining simulation parameters are set in the remaining part of the two scripts. Note that the tunable popup options set in EM\_Speed\_Control.m are such that the PMSM superblock external view in EM\_Speed\_Control\_slx.slx is exactly the one illustrated in Fig. 6. Some results for the two simulation case studies in EM\_Speed\_Control.m and EM\_Torque\_Control.m are reported in Fig. 7 and Fig. 8. The upper subplot of Fig. 7 shows the desired and actual motor speeds  $\omega_{m_{des}}$  and  $\omega_{m}$  in red dashed and blue lines, respectively. The middle subplot of Fig. 7 shows the three components of the voltage vector  ${}^{t}V_{s}$  in the original threephase frame. The lower subplot of Fig. 7 shows the three components of the current vector  ${}^{t}I_{s}$  in the original three-phase frame for a single motor, as three PMSMs are working in parallel in the considered simulation examples, see parameter Nr mot in EM Speed Control.m and EM\_Torque\_Control.m. The upper subplot of Fig. 8 shows the desired and actual motors torques  $\tau_{m_{des}}$  and  $\tau_{m}$ (the latter also accounting for the mechanical friction contributions) in red dashed and blue lines, respectively. The middle and lower subplots of Fig. 8 report the same information as those of Fig. 7 but for the torque control case. From the upper subplots of Fig. 7 and Fig. 8, it is possible to see the good superposition between the desired and actual characteristics, highlighting the effectiveness of the control.

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## **VI. CONCLUSION**

In this paper, a Matlab App created for PMSM parameters estimation has been presented. The App allows to estimate electrical and mechanical parameters and can be potentially implemented online. Next, a generalized PMSM Simulink superblock with a user-friendly interface has been introduced. The PMSM superblock is compatible with the parameters estimation Matlab App, allows both speed and torque control, and lets the user choose whether to compute the three-phase currents and voltages and if the rotor mechanical dynamics has to be included in the simulation or not. The results of two simulations performed on the PMSM superblock are finally reported, applying a speed and a torque control, respectively.

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**DAVIDE TEBALDI** was born in Pavullo nel Frignano, Italy, in 1992. He received the B.S. and M.S. degrees (*cum laude*) in electronic engineering and the Ph.D. degree in systems and control engineering from the University of Modena and Reggio Emilia, Italy, in 2015, 2018, and 2022, respectively. He is currently a Postdoctoral Researcher at the University of Modena and Reggio Emilia. His research interests include energetic modeling, control and simulation of mechatronic systems, with

main application in automotive, electrical machines, and power electronics fields.