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# A Geometrical Optimization Rule of the Synaptic **Pass-Transistor for a Low Power Analog Accelerator**

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**ABSTRACT** We present a simulation framework on a geometrical optimization rule of the synaptic passtransistor (SPT) for a low power analog accelerator (AA). Here, the SPT is a synaptic transistor (Syn-Tr) in series with a load resistor to be scaled with respect to a geometrical ratio between a channel length and width of the Syn-Tr. When only the load resistance is increased for the reduction of the power consumption of the SPT, a synaptic characteristics (e.g. a synaptic dynamic ratio,  $DR_w$ ) is hard to be maintained. To overcome this, the channel geometrical ratio and scaling factor of the load resistance are required to be increased equally, thus a geometrical optimization rule. Here, the load resistance is equivalent to a geometric mean where two extreme cases of the synaptic full facilitation and full depression are considered. To verify the proposed rule, we perform a semiconductor device simulation for a static and pulsed characteristics of the SPT. When the SPT is scaled based on the geometrical optimization rule, from the simulation results, it is found that the static-power consumption is decreased while maintaining the DR<sub>w</sub>. As a trade-off relation, however, the noise power-spectral-density is found to be increased due to a higher thermal noise associated with a higher total resistance of the scaled SPT. Here, the increased noise power-spectral-density of a single SPT may affect the performance of the AA based on the SPT-array, so we also show a crossbar simulation, checking the classification accuracy against a standard dataset (e.g. MNIST).

**INDEX TERMS** Synaptic pass-transistor, geometrical optimization rule, analog accelerator, synaptic weight, synaptic dynamic ratio, full depression, full facilitation, maximum static-power consumption.

### I. INTRODUCTION

A neuromorphic system, which mimics behaviors of a biological nervous system, has been considered as a promising candidate due to a more efficient computing capability compared to the conventional computer system based on the von Neumann architecture [1]-[5]. For example, the data can be efficiently processed with an artificial neural network (ANN) which mimics the connection of the biological neurons. Here, a multi-layer perceptron (MLP) structure can be employed for a simple ANN (see Fig. 1(a)) [6], [7]. Besides a higher data processing efficiency of the neuromorphic system, a low-power characteristics of a synaptic device, which is a fundamental building block, is essential for

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a high-level intelligence of the system [8]–[11]. Here, a level of the intelligence is proportional to the number of synaptic devices, resulting in the increase of a total power consumption proportionally. In this respect, the power consumption of a single synaptic device has to be minimized. In the case of the human brain having a high-level intelligence, it is known that its total power consumption is only 10 W in spite of a huge number of synapses (i.e.  $10^{15}$ ) in the brain [12], [13]. This is mainly because the power consumption per synapse is very small level of 0.01 pW. Note that a single central processing unit (CPU) for the conventional computer system shows a high-power consumption of 100 W approximately, which is 10 times higher compared to the total power consumption of the brain [14], [15].

As a typical two-terminal synaptic device, a memristor with a low-power consumption has been reported,



**FIGURE 1.** (a) Schematic of an artificial neural network (ANN) as a simple multi-layer perceptron (MLP) structure with three layers (e.g. the input layer, hidden layer, and output layer). Here, the  $I_n$  is  $n^{th}$  neuron of an input layer,  $H_m$  is  $m^{th}$  neuron of a hidden layer,  $O_k$  is  $k^{th}$  neuron of an output layer,  $w_{nm}$  is a synaptic weight between In and  $H_m$ , and  $w_{mk}$  is a synaptic weight between  $I_m$  and  $O_k$ . (b) Schematic of the synaptic pass-transistor (SPT) with a charge trapping layer (CTL) and (c) the three-dimensional view of the synaptic transistor (Syn-Tr). Here, the equivalent resistance ( $R_{tr}$ ) of the Syn-Tr can be varied when electrons are trapped or de-trapped depending on the polarity of the programming-voltage ( $V_G^{Prog}$ ) and number of programming-pulses applied to the gate.

indicating its power consumption in the range of nano-watts [11], [16]–[19]. However, that is about six orders of magnitude larger compared to a biological synapse (e.g. 0.01 pW per synapse). It may be because a high voltage to generate memristive phenomena, such as an electro-chemical metallization and valency change, is still required [20], [21]. Therefore, it is expected that a higher-level intelligence of the neuromorphic system based on memristors with these memory phenomena is difficult to be achieved due to a limitation for reducing the power consumption of each device. As another type, three-terminal synaptic devices based on a metal-oxide-semiconductor field-effect transistor (MOSFET) have been investigated for a low power operation [22]–[24]. For a memory function of this synaptic device, programming-pulses are required to be applied to a gate terminal for a memory function, such as a read/write operation, in these synaptic devices. However, a high programming-voltage for both short-term memory phenomena (e.g. an impact ionization) and long-term memory (e.g. a trapping and de-trapping of charges through a tunneling) phenomena of the MOSFET-based synaptic device is needed giving rise to a high burst current. This is expected to lead to an increase of the static-power consumption, thus a limitation of a high-level intelligence in the neuromorphic system.

As a method to limit the burst current, synaptic devices can be connected with a load resistor, which leads to a low-power operation. For example, a synaptic pass-transistor (SPT), where a n-channel synaptic transistor (Syn-Tr) is connected in series with the load resistor, was introduced, as depicted in Fig. 1(b) [25]. Here, a load resistance ( $R_L$ ) of the SPT limits the maximum current level as  $V_I / R_L$  where the  $V_I$  is a fixed input voltage. In addition, the power dissipation of the SPT can be reduced by the increase of  $R_L$ . However, the increase of  $R_L$  may cause side-effects, such as a degradation of a synaptic characteristics. Therefore, a selection of an appropriate  $R_L$  is important.

In this paper, a simulation framework on a geometrical optimization rule (GOR) of the SPT for a low power analog accelerator (AA). Here, the SPT is a Syn-Tr in series with the load resistor, is presented scaling  $R_L$  with respect to a geometrical ratio  $(L_{ch}/W_{ch})$  between a channel length  $(L_{ch})$ and width  $(W_{ch})$  of the Syn-Tr for a low-power operation. To reduce the power consumption of the SPT, when only the  $R_L$  is increased, the synaptic characteristics, such as a synaptic dynamic ratio (DR<sub>w</sub>) between the fully-facilitated and fully-depressed weights, are difficult to be maintained. To maintain this DR<sub>w</sub>, the  $L_{ch}/W_{ch}$  and scaling factor of  $R_L$ are needed to be increased with the same rate, so a GOR is suggested. Here, the  $R_L$  is equivalent to a geometric mean where two extreme synaptic states of the full facilitation and full depression of the Syn-Tr are considered. To check the GOR, a semiconductor device simulation for the static and pulsed characteristics of the SPT is performed. When both the  $L_{ch}/W_{ch}$  and scaling factor of  $R_L$  are equally scaled up with applying the GOR, it is found that the static-power consumption is reduced while maintaining the DR<sub>w</sub> wider compared to the case without applying the GOR. As a tradeoff relation, however, it is found that the noise power-spectraldensity (PSD) of the SPT is increased due to the increase of the thermal noise which is related to the increase of  $R_L$  and equivalent resistance  $(R_{tr})$  of the Syn-Tr. Here, when the SPTs are arrayed as an AA, it is expected that the increased noise PSD of a single SPT can lead to the decrease of the classification accuracy of the AA based on the SPT-array. From the crossbar simulation for the Modified National Institute of Standards and Technology database (MNIST), it is also found that the classification accuracy is decreased due to the



**FIGURE 2.** (a) Conceptual plot of the current-voltage characteristics to express the synaptic process through the threshold voltage shifts changed by programming-pulses. Here, the SS is a subthreshold slope. (b) Notional plot of the current-voltage characteristics when only  $\alpha_L$  is increased without applying the geometrical optimization rule (GOR). Note that the  $v_1$  and  $v_2$  are an amount of the shifted  $V_T$ .

higher noise PSD, as increasing  $R_{tr}$  and  $R_L$ . Therefore, it is shown that the classification accuracy can be decreased due to the increased total resistance of each arrayed SPT although we can expect the reduction of the power consumption in the AA, suggesting a trade-off relation between the power consumption and classification accuracy.

#### **II. SPT AND RELATED THEORIES**

### A. BASIC STRUCTURE AND OPERATING PRINCIPLE

As shown in Fig. 1(b), the SPT consists of the Syn-Tr and  $R_L$ . Here, the  $R_L$  is added for a voltage output  $(V_Q)$ , employing the pass-transistor concept. For the Syn-Tr, a memory function is implemented with a charge trapping layer (CTL) in the insulator system based on a semiconductor-oxide-nitride-oxidesemiconductor (SONOS), as seen in Fig. 1(c). With this CTL, charges (e.g. electrons) are trapped or de-trapped depending on the polarity of the programming-voltage  $(V_G^{prog})$  and number of programming-pulses applied to the gate. Thus, a threshold voltage  $(V_T)$  is varied according to the number of electrons trapped in the CTL, which results in a change of the drain current  $(I_D)$  at a fixed read voltage  $(V_G^{read})$ . Since the  $R_{tr}$  can be expressed as  $V_I/I_D$ , the change of  $I_D$  leads to a variation of  $R_{tr}$ . Assuming that the SPT operates only in the subthreshold region, the  $R_{tr}$  can be represented as follows [25],

$$R_{tr} = \frac{L_{ch}}{W_{ch}} \frac{V_I}{K_{sub} exp\left\{q(V_G^{read} - V_T)/(n_t kT)\right\}},$$
(1)

where  $K_{sub}$  is a constant related to the diffusion coefficient in the subthreshold regime,  $n_t$  is an ideality factor about the interface state, kT is a thermal energy, q is an elementary charge, and  $V_T = V_{T0} + \Delta V_T$ . Here,  $\Delta V_T$  is the amount of the threshold voltage shift from the initial value  $(V_{T0})$ . Also,  $\Delta V_T$  can be represented as  $-Q_e^{trap}/C_i$ , where  $Q_e^{trap}$  is the magnitude of a negative charge density per area, corresponding to the number of electrons trapped in the CTL, and  $C_i$  is a gate-insulator capacitance per area. Note that the operation in the subthreshold regime can be a key aspect for an ultralowpower synaptic device due to a low operating current and high sensitivity of the current for a small variation of  $\Delta V_T$  [26]. By defining  $L_{ch}/W_{ch} \equiv \alpha_{tr}$  and  $R_{tr}/\alpha_{tr} \equiv R_{tr0}$ , Eq. (1) can be rewritten as,

$$R_{tr} = \alpha_{tr} R_{tr0}.$$
 (2)

Here, the  $R_{tr0}$  at  $V_G = V_G^{read}$  is the rest channel resistance normalized with  $\alpha_{tr}$ , which is a function of  $V_T$  depending on the polarity and number of programming-pulses. Since the SPT can be considered as  $R_{tr}$  in series with  $R_L$ , the  $V_O$  is determined as,

$$V_O = \frac{R_L}{R_L + R_{tr}} V_I. \tag{3}$$

With the definition of  $w \equiv V_O/V_I$ , the *w* can be expressed as shown below,

$$w = \frac{R_L}{R_L + R_{tr}}.$$
 (4)

Thus, the *w* is varied depending on the change of  $R_{tr}$  which is a function of  $\Delta V_T$ .

## B. DETAILED PROCEDURE OF THE SYNAPTIC OPERATION

As the Syn-Tr is based on the n-channel MOSFET, the initial state of the SPT is a full facilitation (FF) with  $V_T = V_{T0}(\Delta V_T = 0)$  (see Fig. 2(a)). The channel resistance at the FF (i.e.  $R_{tr}^{ff}$ ) can be expressed as  $V_I/I_D^{ff}$ , where the  $I_D^{ff}$  is the drain current for the FF at  $V_G = V_G^{read}$ . From this FF condition, multiple positive programming-pulses are applied to get a positive  $\Delta V_T$  of  $v_1 > 0$ , which leads to the decrease of  $I_D$  at  $V_G = V_G^{read}$ . As shown in Fig. 2(a), when the  $I_D$  has become  $n_1$  times lower compared to the FF condition, it is defined as the reference drain current ( $I_D^{ref}$ ). This state is to be called a reference state of the SPT with  $V_T = V_{T0} + v_1$  at which the reference channel resistance (i.e.  $R_{tr}^{ref}$ ) is denoted as  $V_I/I_D^{ref}$ . Since  $I_D^{ref} = I_D^{ff}/n_1$ , the  $R_{tr}^{ref}$  can be expressed as,

$$R_{tr}^{ref} = n_1 R_{tr}^{ff}.$$
 (5)

Here, the  $R_{tr}^{ref}$  is to be  $R_L$  for the SPT operation, so the  $R_L$  is given from Eq. (5),

$$R_L = n_1 R_{tr}^{ff}.$$
 (6)

Since the *w* at the FF  $(w^{ff})$  is found by replacing the  $R_{tr}$  with  $R_{tr}^{ff}$  in Eq. (4), the  $w^{ff}$  can be represented with Eq. (6), as follows,

$$w^{ff} = \frac{R_L}{R_L + R_{tr}^{ff}} = \frac{n_1}{n_1 + 1} \approx 1,$$
(7)

where  $w^{\text{ff}}$  is almost unity (i.e. the FF) with the condition of  $n_1 \gg 1$ . Note that the  $w^{\text{ff}}$  can be generalized as a maximum  $w(w_{max})$  for any  $n_1$ , as follows,

$$w_{max} = \frac{n_1}{n_1 + 1}.$$
 (8)

By applying multiple positive programming-pulses, the  $V_T$  can be further increased by  $v_2 > 0$  from the reference condition. So, the  $I_D$  is further decreased by  $n_2$  times, as described in Fig. 2(a). For this case, a full depression (FD) with  $V_T = V_{T0} + v_1 + v_2(\Delta V_T = v_1 + v_2)$  is assumed to be made. The channel resistance at the FD (i.e.  $R_{tr}^{fd}$ ) is represented as  $V_I/I_D^{fd}$ . Here, the  $I_D^{fd}$  is the drain current for the FD at  $V_G = V_G^{read}$ . Since  $I_D^{fd} = I_D^{ref}/n_2$ , the  $R_{tr}^{fd}$  is expressed as  $n_2 R_{tr}^{ref}$ . Along with Eq. (5), it can also be rewritten as,

$$R_{tr}^{fd} = n_1 n_2 R_{tr}^{ff}.$$
(9)

In Eq. (4), the  $R_{tr}$  is  $R_{tr}^{fd}$  at the FD. Along with Eqs. (6) and (9), the *w* at the FD ( $w^{fd}$ ) is derived as,

$$w^{fd} = \frac{R_L}{R_L + R_{tr}^{fd}} = \frac{1}{1 + n_2} \approx 0,$$
 (10)

where the  $w^{fd}$  approaches zero (i.e. the FD) with the condition of  $n_2 \gg 1$ . Similar to Eq. (8), the  $w^{fd}$  can also be generalized as a minimum  $w(w_{min})$  for any  $n_2$ , as follows,

$$w_{min} = \frac{1}{1+n_2}.$$
 (11)

In addition, with the  $w_{max}$  and  $w_{min}$  of the SPT, the DR<sub>w</sub> is defined as,

$$DR_{w} \equiv \frac{w_{max}}{w_{min}} = \frac{n_{1}(1+n_{2})}{n_{1}+1}.$$
 (12)

Here, the DR<sub>w</sub> becomes  $n_2$  with the condition of both  $n_1$  and  $n_2 \gg 1$  while achieving both  $w_{max} = w^{ff}$  and  $w_{min} = w^{fd}$  of the SPT.

# C. LOAD RESISTANCE AND TWO EXTREME SYNAPTIC STATES

Since the  $I_D^{fd}$  is limited to the off-current floor  $(I_{off})$ , the  $n_1$  and  $n_2$  are also limited, thus limited  $\Delta V_T$ . In this respect, the optimum condition of  $n_1$  and  $n_2$  should be found with the limited number of programming-pulses. Assuming that the transistor is always operated in the subthreshold regime and subthreshold slope (SS) is constant, it is found that  $n_1n_2$  is a constant for the constant  $\Delta V_T$  as  $v_1 + v_2$ . So,  $n_1 = n_2$  is optimum to be both the  $n_1$  and  $n_2 \gg 1$ , satisfying  $v_1 = v_2$ . Otherwise, either  $n_1$  or  $n_2$  is decreased, which results in the lack of the condition of  $n_1 \gg 1$  or  $n_2 \gg 1$ . Especially, for the case of  $n_1 > n_2$ , because the FD is difficult to be made (see Eq. (11)), the DR<sub>w</sub> could be reduced, as can be seen in Eq. (12). Now, in order to maintain this optimum after a scaling of the SPT, a scaling condition to keep  $n_1 = n_2$  is discussed. Based on Eq. (2), the  $R_T^{ff}$  can be defined as,

$$R_{tr}^{ff} \equiv \alpha_{tr} R_{tr0}^{ff}.$$
 (13)

Here, the  $R_{tr0}^{ff}$  is the rest channel resistance at the FF, which is  $R_{tr0}$  at  $V_T = V_{T0}$ . With this, Eqs. (6) and (9) can also be rewritten as, respectively,

$$R_L = n_1 \alpha_{tr} R_{tr0}^{\text{ff}}, \qquad (14)$$

$$R_{tr}^{fd} = n_1 n_2 \alpha_{tr} R_{tr0}^{ff}.$$
 (15)

Also, the  $R_L$  is individually defined as,

$$R_L \equiv \alpha_L R_{L0},\tag{16}$$

where the  $\alpha_L$  is a scaling factor of  $R_L$  and  $R_{L0}$  is the rest load resistance. With Eqs. (14) and (16), we set  $R_{L0} = n_1 R_{tr0}^{ff}$  and  $\alpha_{tr} = \alpha_L$  to maintain  $n_1 = n_2$ . Under these conditions, the  $R_L$  is determined as a geometric mean associated with  $R_{tr}$  for two extreme synaptic states from Eqs. (13) to (16),

$$R_L = \sqrt{R_{tr}^{ff} R_{tr}^{fd}}.$$
 (17)

So, when the  $\alpha_L$  and  $\alpha_{tr}$  are changed to the same value, the  $R_L$  and  $R_{tr}$  are determined obtaining a wide DR<sub>w</sub> from Eq. (12). And Eq. (17) is also satisfied. Accordingly, both the  $\alpha_L$  and  $\alpha_{tr}$  should be equally increased to maintain an optimum state in terms of the synaptic characteristics, thus the GOR.

# D. GEOMETRICAL OPTIMIZATION RULE AND POWER CONSUMPTION

As mentioned earlier, since the SPT consists of the Syn-Tr and the load resistor, the increase of  $R_L$  can reduce the power



**FIGURE 3.** Current-voltage characteristics of the Syn-Tr at the full depression (FD) and the full facilitation (FF) for (a)  $\alpha_{tr} = 1$ , (b)  $\alpha_{tr} = 10$ , (c)  $\alpha_{tr} = 10^2$ , (d)  $\alpha_{tr} = 10^3$ , and (e)  $\alpha_{tr} = 10^4$  ( $\alpha_{tr} = \alpha_L = \alpha$ ). The load resistance can be determined at each reference current level where  $n_1 = n_2 \gg 1$ , which satisfies the GOR. Here, the off-current floor ( $I_{off}$ ) is assumed to be  $10^{-13}$  A.

consumption of the SPT. There are two kinds of the power consumption of the SPT: a static-power consumption ( $P_{static}$ ) and a dynamic-power consumption ( $P_{dyn}$ ). Here, the  $P_{dyn}$  is negligible because it can be sufficiently smaller than  $P_{static}$ by extending the rising and falling time of the programmingpulse. So, it is important to reduce  $P_{static}$ , which is dominant in the power consumption of the SPT. Here, since  $P_{static} = V_I^2/(R_{tr} + R_L)$ , the maximum of  $P_{static}$  ( $P_{static}^{max}$ ) in the SPT is expressed for  $R_{tr} \ll R_L$ , as follows [27],

$$P_{static}^{max} \approx \frac{V_I^2}{R_L}.$$
 (18)

Thus, the increase of  $\alpha_L$  makes  $R_L$  bigger, which results in the decrease of  $P_{static}^{max}$  as seen in Eq. (18). Here, according to the proposed GOR, the  $\alpha_{tr}$  should be increased together to keep the condition of  $\alpha_{tr} = \alpha_L$  for  $n_1 = n_2$ . This can also keep an optimally large DR<sub>w</sub>. However, when only the  $R_L$  is increased, the  $\alpha_L$  is greater than  $\alpha_{tr}$ , thus  $n_1 > n_2$  (see Fig. 2(b)). For this case, the FD is difficult to be made because the  $w_{min}$  is hard to approach zero, which can be explained with the decreased  $n_2$  (see Eq. (11)). So, based on Eq. (12), the lack of the synaptic depression happens while the  $DR_w$ is smaller. To examine this and a low-power consumption of the SPT scaled with the GOR, it is suggested to firstly find a proper  $R_L$  with the static characteristics of the Syn-Tr. After finding a proper  $R_L$  based on the GOR, the power consumption and DR<sub>w</sub> of the scaled SPT can be analyzed with the pulsed characteristics for the synaptic depression and facilitation.

#### **III. RESULTS AND DISCUSSION**

#### A. METHODOLOGY

Based on the theoretical analysis on the GOR in the previous section, a low-power consumption and wide DR<sub>w</sub> of the SPT are expected to be achieved, as applying the GOR. To check this, a static and pulsed characteristics of the SPT (i.e. a combination of the Syn-Tr and R<sub>L</sub>) are shown in the following Sections III-B and C. For this, the semiconductor device simulation is performed with the SILVACO<sup>TM</sup> ATLAS<sup>TM</sup>. Here, based on the GOR, the  $\alpha_{tr}$  and  $\alpha_L$  are set to be the same value, which is defined as a single scaling factor  $\alpha (\equiv \alpha_{tr} = \alpha_L)$  for a convenience. As increasing  $\alpha$ , the  $R_{tr}$  is scaled up with the same rate as the  $R_L$ . Besides  $\alpha_{tr}$  and  $\alpha_L$ , other device properties are given in Ref. 26. As increasing the  $\alpha$ , it is also expected that the noise characteristics (e.g. a noise PSD) of the SPT is varied. To verify this, the noise characteristics is monitored.

With the extracted data for both the synaptic weight-update and noise characteristics in the device level, when a SPT-array composed of these SPTs is used as the AA, it is expected that the performances (e.g. classification accuracy (CA)) of the AA are affected due to the variation of the noise PSD. To check this, the  $\Delta w$ -w plot and classification accuracy are described in the following Section III-D. For this, the AA simulation is performed using a resistive memory simulator, called the CrossSim<sup>TM</sup> of which the detailed description is shown in the Supplementary Material (see Section S1) [28]–[30]. Also, the descriptions with respect to the validation of the proposed models (i.e. the SPT and AA) are shown in the Supplementary Material (see Section S2).

#### **B. STATIC CHARACTERISTICS OF THE SYN-TR**

As seen with the graphical analysis in Fig. 2(a), to find the value of  $R_L$  which satisfies the condition of  $n_1 = n_2$ , the static characteristics of the Syn-Tr needs to be analyzed. In addition, to check whether this condition of  $n_1 = n_2$  can be maintained with applying the GOR, the current-voltage characteristics is required to be monitored as scaling the Syn-Tr. Hence, we show the transfer characteristics of each Syn-Tr scaled up with  $\alpha_{tr}$ . Fig. 3 shows the I-V curves at the FF and FD of the Syn-Tr, respectively, for five different values of  $\alpha_{tr}$ . Here, when the  $R_L$  as the geometric mean of  $R_{tr}^{ff}$  and  $R_{tr}^{fd}$ is determined with Eq. (17), the  $\alpha_{tr}$  and  $\alpha_L$  are to be the same value, thus the GOR. As depicted in Fig. 3(a), for  $\alpha_{tr} = 1$  as a reference case, it is found that  $I_D^{ff} \approx 10^{-5}$  A and  $I_D^{fd} \approx 10^{-9}$  A at  $V_G^{read} = 0.2$  V. With them, the level of  $I_D^{ref}$  is chosen as  $10^{-7}$  A where  $n_1 = n_2 \approx 10^2$ . With this, the equivalent  $R_L$  is calculated as  $10^6 \Omega$  for  $V_I = 0.1$  V. This is because  $R_L \equiv V_I / I_D^{ref}$ , which is also corresponding to the geometric mean for  $R_{tr}^{ff} = 10^4 \Omega$  and  $R_{tr}^{fd} = 10^8 \Omega$ , using Eq. (17). When the value of this load resistor is set to the  $R_{L0}$ , the  $\alpha_L$  becomes unity, thus  $\alpha_L = \alpha_{tr} = 1$ . Based on this reference case, as seen in Figs. 3(b)-(e), when the  $\alpha_{tr}$  is gradually scaled up by a factor of 10, it is found that the level of  $I_D^{ff}$  and  $I_D^{fd}$  is equally decreased tenfold. Meanwhile, the  $I_D^{ref}$  is selected as a level decreased tenfold, so the  $R_L$  is increased with the rate of  $\alpha_{tr}$ , which is found to satisfy  $\alpha_L = \alpha_{tr}$  with Eq. (16). It is because the  $n_1$  and  $n_2$  are maintained as the same value of  $10^2$ , approximately. This is also consistent with the geometric mean of  $R_{tr}^{ff}$  and  $R_{tr}^{fd}$  for each case. These results indicate that the  $\alpha_{tr}$  and  $\alpha_{L}$  are required to be increased equally to maintain the synaptic characteristics, such as a DR<sub>w</sub> with the optimum condition of  $n_1$  and  $n_2$ .

#### C. PULSED CHARACTERISTICS OF THE SYN-TR

From the analysis on the static characteristics of the Syn-Tr, it is expected that the DR<sub>w</sub> of the SPT is maintained, which satisfies  $n_1 = n_2 \approx 10^2$  with the GOR. In addition, the increase of both  $R_{tr}$  and  $R_L$  based on the GOR can result in the decrease of  $I_D$ . So, it is expected that the  $P_{static}$  of the SPT is reduced with the decrease of  $I_D$ . To verify these DR<sub>w</sub> and  $P_{static}$ , the pulsed characteristics for  $V_O$  and  $I_D$  of the SPT needs to be monitored for the synaptic depression and facilitation processes, respectively, depending on the polarity and number of the programming-pulses.

For the synaptic depression, the positive programmingpulses are applied with  $V_G^{prog} = 8$  V,  $V_G^{read} = 0.2$  V, and pulse-width = 1  $\mu$ s (see Fig. 4(a)). After 20 cycles of the positive programming-pulses, it starts to apply the negative programming-pulses for the synaptic facilitation, where  $V_G^{prog} = -4$  V,  $V_G^{read} = 0.2$  V, and pulse-width = 2  $\mu$ s



**FIGURE 4.** (a) Waveform of the positive programming-pulses (with  $V_{G}^{prog} = 8 V$  and  $V_{G}^{read} = 0.2 V$ ) and negative programming-pulses (with  $V_{G}^{prog} = -4 V$  and  $V_{G}^{read} = 0.2 V$ ) for the synaptic depression and facilitation, respectively. (b) Voltage output which appears on the load resistor and (c) drain current of the SPT over 40 cycles of programming-pulses for five different values of  $\alpha$ . (d) The maximum static power consumption as a function of  $\alpha$  which is calculated with the maximum output voltage ( $V_{O}^{max}$ ) and maximum drain current ( $I_{D}^{max}$ ) indicated in (b) and (c), respectively.

(see Fig. 4(a)). Note that common specifications of the programming-pulses are as follows, the duty cycle, rising time, and falling time are 50 %,  $10^{-7}$ s, and  $10^{-7}$ s, respectively. Fig. 4(b) shows the  $V_O$  sampled at  $V_G = V_G^{read}$  for each  $\alpha$ , where the positive and negative programming-pulses are repeated 20 times for the synaptic depression and facilitation processes, respectively.

As shown in Fig. 4(b), for  $\alpha = 1$  (reference case), it is found that the  $V_O$  is gradually decreased with applying the positive programming-pulses for the synaptic depression, approaching  $V_O \approx 0$ . It is because the  $R_{tr}$  is gradually increased, which can be explained with Eqs. (1) and (3). And the  $V_O$  finally arrives at around zero, corresponding to the FD as a synaptic state, because the  $R_{tr}$  is approximately 100 times larger compared to  $R_L$ , suggesting  $n_2 \approx 10^2$  (see Eq. (3)). Afterward, for the synaptic facilitation, it is also found that the  $V_{O}$  is gradually increased with a series of negative programming-pulses. This is because the  $R_{tr}$  is gradually decreased, which can also be explained with Eqs. (1) and (3). After 20 cycles of negative programming-pulses for the synaptic facilitation, the  $V_O$  approaches the maximum value  $(V_Q^{max})$  of  $V_Q$  (i.e.  $V_Q^{max} \approx V_I = 0.1$  V), which corresponds to the synaptic state of the FF. This is due to a relative dominance between  $R_{tr}$  and  $R_L$  (i.e.  $R_{tr} \ll R_L$ ), satisfying  $n_1 \approx 10^2$  (see Eq. (3)). As this reference case, although the  $\alpha$  is increased up to  $10^4$ , it is shown that the trends of  $V_O$  remain the same in all cases of  $\alpha$ . This is because both the  $R_{tr}$  and  $R_L$  are equally scaled up with  $\alpha$ . It is consistent with Eq. (3) where the  $\alpha$  is canceled out.

Since it is expected that these increased  $R_{tr}$  and  $R_L$  can lead to the decrease of  $I_D$ , the  $I_D$  as another factor of  $P_{static}$  needs to be monitored. Fig. 4(c) describes the  $I_D$  also sampled at  $V_G = V_G^{read}$  for the synaptic depression and facilitation processes, respectively, for five different values of  $\alpha$ . As seen in Fig. 4(c), for the reference case (i.e.  $\alpha = 1$ ), it is found that the  $I_D$  decays with a series of the positive programming-pulses for the synaptic depression. This is also because the  $R_{tr}$  is gradually increased with the positively shifted  $V_T$  (i.e.  $\Delta V_T >$ 0), which is explained with Eq. (1) and  $I_D = V_I/(R_{tr} + R_L)$  for  $V_I = 0.1$  V. After the positive programming-pulses continued for 20 cycles, the  $I_D$  reaches the current level of  $10^{-9}$  A, which is two orders of magnitude smaller compared to its maximum level  $(I_D^{max})$ . This is because the  $R_{tr}$  is 100 times larger compared to  $R_L$  (i.e.  $n_2 \approx 10^2$ ). Afterward, for the synaptic facilitation, the I<sub>D</sub> is gradually increased with applying the negative programming-pulses, recovering to  $I_D^{max}$ . It is because of the  $R_{tr}$  decreased gradually with a negative shift (i.e.  $\Delta V_T < 0$ ) of  $V_T$ , which is also explained with Eq. (1) and  $I_D = V_I / \alpha (R_{tr} + R_L)$  for  $V_I = 0.1$  V. And the  $I_D$  finally arrives at  $I_D^{max}$  due to  $R_{tr} \ll R_L$ , satisfying  $n_1 \approx 10^2$ . When the  $\alpha$  is increased by a factor of 10, it appears that the  $I_D$  is scaled down tenfold while maintaining the same trend as the reference case. It is because the  $R_{tr}$  and  $R_L$  are equally scaled up with  $\alpha$ , satisfying  $I_D = V_I / (R_{tr} + R_L)$  for  $V_I = 0.1$  V (see Eqs. (2) and (16)). Accordingly, as seen in Figs. 4(b) and (c), since the  $V_O$  is equally maintained for all cases of  $\alpha$ , it implies that the *P*<sub>static</sub> can be reduced with the decrease of  $I_D$ . Here, as a maximum value of  $P_{static}$ , the  $P_{static}^{max}$  can be calculated as a product of  $V_O^{max}$  and  $I_D^{max}$  at the FF for each  $\alpha$ , as shown in Fig. 4(d). For the reference case (i.e.  $\alpha = 1$ ), as can be seen, it is found that the  $P_{static}^{max}$  is about 10 nW, which is consistent with the calculation for  $R_L$  =  $10^6\Omega$  and  $V_I = 0.1$  V (see Eq. (18)). When the  $\alpha$  is increased



**FIGURE 5.** Synaptic weight versus the number of programming-pulses for two cases of  $\alpha_{tr} = \alpha_L$  (with the GOR) and  $\alpha_{tr} = 1 \ll \alpha_L$  (without applying the GOR) under four different conditions of (a)  $\alpha_L = 10$ , (b)  $\alpha_L = 10^2$ , (c)  $\alpha_L = 10^3$ , and (d)  $\alpha_L = 10^4$ . We apply the same number of pulses for the synaptic depression and facilitation, respectively, considering the symmetrical aspect of the weight-update.

by a factor of 10, as expected, the  $P_{static}^{max}$  is reduced due to  $I_D^{max}$  decreased with  $\alpha$ , as shown in Fig. 4(c). This can also be explained with Eq. (18). The increase of  $\alpha$  leads to the increased  $R_L$  (see Eq. (16)), thus a reduction of  $P_{static}^{max}$  for a fixed  $V_I$ . Note that the  $P_{dyn}$  is expected to be observed for the synaptic depression and facilitation processes, respectively,



**FIGURE 6.** PSD of the voltage noise extracted for the SPT scaled with five different values of  $\alpha$ .



**FIGURE 7.** Conceptual diagram of the  $n \times m$  SPT-array (i.e. SPT-based AA) constructed for the crossbar simulation. For every column of the SPT-array, SPTs are connected with a single load resistor. Here, the synaptic weight of each SPT ( $w_{nm}$ ) is varied with the nth input voltage ( $V_{In}$ ),  $n^{th}$  gate voltage ( $V_{Gn}$ ), and  $m^{th}$  load resistance ( $R_{Lm}$ ). The voltage output for the  $m^{th}$  column, which appears on each load resistor, is the signal for the hidden layer ( $V_{Hm}$ ) to be transferred toward the output layer of the ANN.

due to the existence of the displacement current associated with the voltage difference changed for a rising time and falling time of the programming-pulse.

According to the trend of  $V_O$  observed in Fig. 4(b), the *w*, which is defined as  $V_O/V_I$ , is found to be fully depressed (i.e.  $w_{min} \approx w^{fd}$ ) and fully facilitated (i.e.  $w_{max} \approx w^{ff}$ ) regardless of the increased  $\alpha$  to reduce the power consumption of the SPT. In other words, the DR<sub>w</sub> is expected to be wider than the DR<sub>w</sub> for the case without applying the GOR. To clarify this, the weight dynamics needs to be monitored for the comparison between SPTs scaled with the GOR and without applying the GOR. Fig. 5 depicts the synaptic weight dynamics for two cases of  $\alpha_{tr} = \alpha_L$  (i.e. with the GOR) and  $\alpha_{tr} = 1 \ll \alpha_L$ (i.e. without applying the GOR), which is plotted for each  $\alpha_L$ . Here, for the scaling based on the GOR, the *w* is calculated with its definition (i.e.  $w \equiv V_O / V_I$ ) and the given input voltage (i.e.  $V_I = 0.1$  V), as seen in Fig. 4(b). Similarly, for the case without applying the GOR, the *w* is also extracted from the  $V_O$  over 40 cycles of programming-pulses.

As depicted in Fig. 5, the trends of w remain identical in all the GOR-based cases, corresponding to the trends of  $V_O$ , as seen in Fig. 4(b). This appears due to the  $R_{tr}$  and  $R_L$  scaled up with the same rate of  $\alpha$ , which can also be explained with Eq. (4) where all scaling factors are canceled out. Further, it is found that the DR<sub>w</sub> is maintained as 112, which is calculated with Eq. (12). This is because the optimum condition of  $n_1 = n_2 \approx 10^2$  is always satisfied with the GOR, as shown in Fig. 3. On the other hand, for the cases of  $\alpha_{tr} = 1 \ll \alpha_L$ , it is also found that the DR<sub>w</sub> is reduced with the increase of  $\alpha_L$ . As mentioned earlier, since the product of  $n_1$  and  $n_2$ is constant, the  $n_1$  increases and  $n_2$  decreases when only  $\alpha_L$ is increased for a fixed  $\alpha_{tr}$  (i.e.  $\alpha_{tr} = 1$ ). Then, the  $w_{min}$  is very difficult to be zero due to the decreased  $n_2$ , which is explained with Eq. (11). In this respect, the DR<sub>w</sub> is reduced (see Eq. (12)), approaching  $1+n_2$  with the increase of  $n_1$  and decrease of  $n_2$ . Note that, for the case of  $\alpha_{tr} = 1 \ll \alpha_L$ , the  $w_{max}$  is easy to be almost unity because of  $n_1$  which is larger compared to  $n_2$ . And this can also be explained with Eq. (8).

Consequently, it is verified that the DR<sub>w</sub> can be maintained as a relatively large value of 112 while achieving a low-power consumption of the SPT when both the  $R_{tr}$  and  $R_L$  are scaled up with applying the GOR.

### D. CLASSIFICATION ACCURACY OF THE SPT-ARRAY AS THE ANALOG ACCELERATOR

When the  $\alpha$  is increased, the  $P_{static}$  is reduced due to the increase of  $R_{tr}$  and  $R_L$  while maintaining a wide  $DR_w$  of 112 for  $w_{min} \approx w^{fd}$  and  $w_{max} \approx w^{ff}$ . However, it is expected that the increased  $R_{tr}$  and  $R_L$  can lead to a higher PSD of the voltage noise (e.g. a thermal noise and flicker noise) for the SPT scaled with the GOR. Indeed, as shown in Fig. 6, when the  $\alpha$  increases, it is found that the PSD of the voltage noise is gradually increased with the rate of  $\alpha$ . This is because the thermal noise, which is a dominant noise source in the SPT, is proportional to the  $R_{tr}$  and  $R_L$  [31].

When a SPT-array composed of these SPTs (see Fig. 7) is used as the AA based on the MLP structure seen in Fig. 1(a), it is expected that the increased noise PSD of each SPT can result in the degradation of performances, such as a classification accuracy (CA), in the AA. To verify this, it is required to firstly monitor the weight-update of the SPT-array based on the noise characteristics shown in Fig. 6. Fig. 8 shows the weight-update of the SPT-array with color maps of the cumulative distribution function (CDF) for five different values of  $\alpha$ . The CDF distribution illustrated in Figs. 8(a) and (b) represents the probabilistic change of w with respect to a given synaptic state for each synaptic process (e.g. a synaptic depression and facilitation). Here,  $\Delta w$  is defined as a difference between  $w_n$  and  $w_{n-1}$ where the  $w_n$  is w after applying the  $n^{th}$  programming-pulse and  $w_{n-1}$  is w before applying the  $n^{th}$  programmingpulse. These are extracted based on the weight dynamics



FIGURE 8. Δw vs w plots for (a) the synaptic depression and (b) synaptic facilitation for each α shown with the cumulative distribution function (CDF) of the probabilistic change in w. Here, 20 cycles of the programming-pulses are applied to arrayed SPTs for the synaptic depression and facilitation, respectively.



**FIGURE 9.** Classification accuracies of the SPT-array based AA versus training epochs for each  $\alpha$ . In the inset, the comparison table of average classification accuracies for different values of  $\alpha$  is shown. Here, the classification task is tested for the MNIST.

and noise PSD shown in Figs. 5 and 6, respectively, with a resistive memory simulator, called the CrossSim<sup>TM</sup>. As seen in Fig. 8(a) and (b), the variability of  $\Delta w$  becomes greater with the increase of  $\alpha$  for the synaptic depression and facilitation, respectively. It is because of the increased noise PSD of each scaled SPT, as depicted in Fig. 6. This implies that the weight-update can be less predictable for the SPT-array scaled with the increased  $\alpha$  compared to the reference case. These results also suggest that the training for the classification task may be more disturbed with the increased noise PSD of scaled SPTs, leading to a decrease of CA in the AA.

To clearly check the relation between the CA of the SPT-array and noise PSD of a single SPT, the CA with respect to the weight-update shown in Fig. 8 also needs to be monitored with a standard dataset, the MNIST [32], [33]. Fig. 9 describes the CA for the MNIST classification task which is tested for the SPT-array composed of SPTs scaled with five different cases of  $\alpha$ . When the  $\alpha$  is gradually scaled up by powers of 10, as can be seen, an average value of the CA extracted for 40 epochs is slightly reduced from

91.32 % to 91.04 %, as increasing  $\alpha$ . This is because the noise PSD increased with  $\alpha$  can reduce the signal to noise ratio (SNR) which is inversely proportional to the noise PSD [31]. In addition, since it is known that the CA is proportional to the SNR, the decreased SNR can lead to a reduction of the CA [34]–[36].

Consequently, these results indicate that the power consumption of a single SPT is reduced while maintaining a relatively wide  $DR_w$  due to the increased  $R_{tr}$  and  $R_L$ . However, since the noise characteristics of the SPT is degraded by the increase of total resistance, the CA of the AA, where SPTs are arrayed, is decreased, thus a trade-off relation between the power consumption and CA in the AA. In addition, in terms of a scaling of the semiconductor device, the SPT is scaled down with the GOR where both  $W_{ch}$  and  $R_L$  are considered for maintaining  $DR_w$  and satisfying a low power operation. This is expected that the level of integration would be high, thus a high-level intelligence.

#### **IV. CONCLUSION**

In this article, the simulation framework on the GOR has been presented for a low-power SPT which is the Syn-Tr in series with the load resistor scaled with respect to the geometrical ratio between the channel length and width of the Syn-Tr. It has been shown that the synaptic characteristics, such as the DR<sub>w</sub> between the fully-facilitated and fully-depressed weights, can be varied due to the simply-increased load resistance of the SPT for a low-power consumption. To optimize this, the GOR has been suggested, allowing the DR<sub>w</sub> to remain constant by equally increasing the channel geometrical ratio and scaling factor of the load resistance. Here, it has been found that the load resistance can be determined as a geometric mean with respect to extreme states of the synaptic full facilitation and full depression. To substantiate the GOR, the results of the semiconductor device simulation have been analyzed for the static and pulsed characteristics of the scaled SPT. From the SPT scaled with the GOR, it has been found that the low-power operation of the SPT

can be achieved due to a reduced operating current at the read voltage while maintaining the maximum DR<sub>w</sub> of 112. As a trade-off relation, however, it has been also found that a higher noise PSD appears due to the increase of the thermal noise which is proportional to the total resistance of the scaled SPT. Additionally, to check the influence of this scaled SPT on the performance of the AA based on the SPT-array, the weight-update and classification task against the MNIST have been simulated. From the crossbar simulation, it has been found that the classification accuracy of this AA is decreased due to the increase of the noise PSD in the scaled SPTs. Here, the power consumption over the SPT-array as the AA can be reduced due to the decreased static-power consumption of a single SPT, thus a trade-off relation between the power consumption and classification accuracy in the AA based on the SPT-array. Consequently, when SPTs are scaled down for a high-level integration associated with the level of intelligence which is proportional to the number of synaptic devices, it can be believed that the GOR would be essential for the semiconductor device scaling, maintaining DR<sub>w</sub> and achieving a low power consumption.

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(Danyoung Cha and Yeonsu Kang contributed equally to this work.) Soobin Lee developed the theory. All the authors wrote the manuscript together.

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