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Numerical Simulations of Vaccination and Wolbachia on Dengue Transmission Dynamics in the Nonlinear Model

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ABSTRACT In this study, it is indicated that the world can get rid of the dengue virus by using vaccines and Wolbachia. In many findings, it is observed that Wolbachia therapy is efficacious in those regions that display the minimal to moderate the transmission level. On the contrary, vaccination is highly successful when used in serologically persons and places with large transmission levels. The resilience of stochastic methodology based on the numerical computing schemes will be used to exploit the artificial neural networks (ANNs) modelling legacy, as well as the metaheuristic intelligence using the hybrid of global and local search schemes thru genetic algorithms (GAs) and active-set method (ASA). The combination of both strategies is used to manage the numerical therapies of the mathematical form of the dengue model. The optimal control results through GA-ASA can be retrieved by offering an error-based fitness function generated for dengue model represented via nonlinear systems of equations. The acquired findings are compared to the Adams numerical results to ensure that the suggested stochastic system is accurate. For determining convergence, the training contours are based on various contact rate values. Furthermore, the statistical achievements of the suggested stochastic scheme to solve the novel developed dengue model, which demonstrate the stability and dependability of the dynamical system scheme.

INDEX TERMS Dengue model, vaccination, Wolbachia treatment, genetic algorithm, active set algorithm.

I. INTRODUCTION

Dengue fever, sometimes known as "tropical flu", is a viral spreading infection by Aedes mosquitoes. There are four dominant prevalent isoforms (DEN-1, DEN-2, DEN-3, and DEN-4) of this virus globally [1]. The existence of the Aedes species in various Cameroonian locations is reported in [2], whereas others show that this mosquito only attacks daytime [3]. Females' mosquito, mostly Aedes aegypti to a smaller degree carry dengue virus. Each serotype can cause yellow fever, Chikungunya, dengue shock syndrome, and Ebola infections. Dengue fever affects about three billion

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people around the world, making it a major global public health issue. In high-endemicity urban and suburban regions, this virus is responsible for extremely high mobility and mortality [4]. Dengue fever has increased by 30 times globally during 1960 and 2010, owing to rising population growth, global climate change, rapid urbanization, ineffective mosquito control, extensive air transport, and a lack of access to health facilities. Dengue endemic areas have a population of 2.5 billion people, with around 400 million illnesses each year and a fatality rate of 5–20 percent in some places. Dengue fever is a disease that affects over 100 countries worldwide [5]. Different types of dengue vaccines are under observations comprising Inactivated vaccine, live-attenuated vaccine, DNA vaccine, and viral vectored vaccine, etc. [6]. They work principally by boosting immunogenicity to the E protein and non-structural protein 1 (NS1) of the dengue virus (DENV) [7]. Researching the immunogenicity to DENV can aid in the development of an efficient dengue vaccination strategy [8]. However, the prevalence of four immunologically different dengue virus serotypes, all potentially of generating cross-reactive and disease-enhancing antibody responses against with the three remaining sterotypes, has made the production of a dengue vaccine a difficult process [9]. Scientifically, theoretical calculation of mosquito density reduction is vital, and mosquito density decreases by half on the borders in the region of operations. Ross [10] proposed the concept of mosquito density reduction through the construction of mathematical models several decades earlier.

In recent years, the application of mathematical models to the study of infectious disease epidemic spread has benefited the field of public health in general. For dengue virus propagation, mathematical epidemiological investigations of interaction models involving host-vector and human populations have been developed [11]–[14]. Many dengue mathematical models have been constructed to evaluate the efficiency of Vaccine and Wolbachia intervention in lowering dengue transmission. They discovered that Vaccine and Wolbachia could lower the frequency of dengue cases by up to 80%, especially in areas where propagation is low to moderate [15]-[17]. To observe the heterogeneity and dispersing effects of dengue, mathematical models based on the life cycle and diffusion of mosquitos, as well as geographic heterogeneity of mosquitos, have been constructed. Furthermore, diffusion approaches are used when space is treated as a continual component [18]-[20].

Even though various mathematical models have been developed to examine dengue groove in the presence of vaccination and Wolbachia, rare have considered the combination of the two techniques. It is critical to analyze the results of both approaches independently and collectively. The objective of this research is to explore a mathematical model of vaccination and Wolbachia used for dengue transmission and dispersal and its analysis in the form of simulation solutions to assist in understanding dynamic behavior using a stochastic technique. Exploring the prospect of fixing linear/nonlinear systems using the high predictive capabilities of feedforward artificial neural networks (ANNs) optimized with the combined capabilities of local/global search methods is a significant potential of meta-heuristic computing paradigm based on stochastic approach [21]–[23]. Soft computing techniques reported in different diseases such as Convolution neural networks for analysis of plant diseases [24], [25], for COVID-19 disease [26]-[29], artificial neural networks for tuberculosis [30], for forecasting disease [31], for skin diseases [32], chest disease [33], for diagnosis of kidney stone diseases [34], respiratory disease [35], for HIV infection [36], to analyze influenza disease model [37] and for stomach model [38]. In the field of fluid mechanic, ANNs successfully tightened the claws as these techniques have been proved best for nonlinear complicated flow system [39]–[43]. Forecasting and finance require soft computing for rapid marketing [44], [45].

It is investigated that the vaccination and Wolbachia have been used to prevent the dengue spread. Wolbachia possesses properties that differ from the insecticide-based technique, which could have an impact on disease transmission dynamics. We shall demonstrate the effectiveness of these tactics separately or jointly after simulating the model. The goal of the research is to find the numerical solutions via artificial neural network understanding of the strategy's effectiveness, hence a single serotype dengue model will suffice.

Key procedure is as under

- The effectiveness is validated using statistical evaluations of the dengue nonlinear system based on differential equations on numerous ANN-GA-ASA trials in terms of mean absolute deviation, semi-interquartile range and 'Theil's inequality coefficient.'
- Aside from the accurate results for the Dengue nonlinear differential model with initial conditions, additional valuable features include ease of understanding, faster operation, stability, broad applicability, and robustness.

The paper is arranged into 4 sections. Section 2 comprises the formulation of dengue model and its parameters along values. Section 3 shows the ANN-GA-ASA methodology for solving the dengue, as well as the mathematical form of the statistical operators. Section 4 contains the summary of the findings.

II. FORMULATION OF MATHEMATICAL MODEL

A predictable mathematical model is constructed for the dengue treatment that covers Wolbachia and vaccinated presented by Nedii *et al.* [17]. In this model the attacking agent (mosquito) and effected agent human are distributed into two separate compartments. Attacking agent population are distributed into Aquatic A, Susceptible S, Exposed E and Infectious I, whereas human population are distributed into Susceptible S_H , Vaccinated V_H , Exposed E_H , Infectious I_H and Recovered R_H .

The purpose of this paper is to get a broad understanding of the potential efficacy of vaccines and Wolbachia. The basic assumptions used to build the model are as follows:

- Mosquitoes have no recovery class because they are contagious for the remainder of their lives.
- It is sufficient to utilize a single serotype dengue model.

When susceptible individuals are attacked by contaminated non-Wolbachia and Wolbachia-carrying mosquitoes at a rate of λ_n and λ_W , respectively, they become infected. The human species are injected at a rate of V_H . Vaccinated people, on the other hand, are exposed to dengue when the vaccine loses its efficiency at a rates $(1 - \varepsilon)$ and they are struck by diseased non-Wolbachia and Wolbachia-carrying mosquitoes at rates λ_n and λ_W , respectively. We consider diminishing immunity, which occurs at a rate of φ_h , as well as randomized bulk vaccination. The mathematical constrain for disease model

Symbols	Description	Values (day ⁻¹)
β	Birth rate	1/(66.38×365)
$\mu_{_{H}}$	Natural death rate	1/(66.38×365)
p	Vaccinated rate	0.20
Е	Vaccine efficacy	0.538
arphi	Waning immunity	0.10
ω	Maternal transmission	0.90
$b_{_N}$	Non-wolbachia biting rate	0.63
$b_{\scriptscriptstyle W}$	Wolbachia biting rate	0.95 of $b_{_N}$
$\mu_{\scriptscriptstyle N}$	Adult mosquito death rate	0.070
$\mu_{\scriptscriptstyle AW}$	Aquatic death rate	0.070
$\mu_{\scriptscriptstyle W}$	Wolbachia death rate	1.1 of $\mu_{\scriptscriptstyle N}$
$ au_{\scriptscriptstyle W}$	Maturation rate of Wolbachia	0.10
$ au_{_N}$	Maturation rate on non- Wolbachia	1.25
$ au_{\scriptscriptstyle W}$	Maturation rate on Wolbachia	0.10
${\gamma}_{\scriptscriptstyle H}$	Exposed to infectious human progression rate	0.182
${\gamma}_{\scriptscriptstyle N}$	Exposed to infectious non- Wolbachia progression rate	0.10
$T_{_N}$	Transmission Probability	0.2614
${\gamma}_{\scriptscriptstyle W}$	Exposed to infectious progression rate	0.10
$ ho_{\scriptscriptstyle N}$	Non-Wolbachia reproduction rate	1.25
$ ho_{\scriptscriptstyle W}$	Wolbachia reproduction rate	0.95 of $ ho_{\scriptscriptstyle N}$
α	Recovery rate	0.25
T_{HW}	Infectious W to human transfer probability	0.50 of T_N
λ_n	Non-Wolbachia carrying mosquitoes rate	0.1647
$\lambda_{_{W}}$	Wolbachia carrying mosquitoes rate	0.95
$I_{_N}$	Non-Wolbachia infectious rate	0.3
$I_{\scriptscriptstyle W}$	Wolbachia infectious rate	0.2

TABLE 1. Brief description with symbols and their numerical values per day as unite [17].

is given as:

$$\begin{split} S'_{H}(t) &= \beta N_{H} - (\lambda_{n} + p + \lambda_{w} + \mu_{H})S_{H}(t) + \varphi V_{H}(t), \\ V'_{H}(t) &= pS_{H} - (1 - \varepsilon)V_{H}(t)\left(\lambda_{n} + \lambda_{w}\right) - V_{H}(t)\left(\varphi + \mu_{h}\right), \\ E'_{H}(t) &= (\lambda_{n} + \lambda_{w})S_{H}(t) + (1 - \varepsilon)V_{H}(t)\left(\lambda_{n} + \lambda_{w}\right) \\ &- E_{H}(t)\left(\gamma_{H} + \mu_{H}\right), \\ I'_{H}(t) &= \gamma_{H}E_{H}(t) - \alpha I_{H}(t) - \mu_{H}S_{H}(t), \\ R'_{H}(t) &= \alpha I_{H}(t) - \mu_{H}R_{H}(t), \end{split}$$

$$\begin{aligned} A'_{N}(t) &= \frac{1}{2(F_{N} + F_{W})} \rho_{N} F_{N}^{2} \left(1 - \frac{(A_{N}(t) + A_{W}(t))}{K} \right) \\ &- A_{N}(t) (\tau_{N} + \mu_{NA}) , \\ S'_{N}(t) &= \frac{A_{N}(t)\tau_{N}}{2} + (1 - \omega) \frac{A_{N}(t)\tau_{N}}{2} - \frac{T_{N} b_{N} I_{H}(t) S_{N}(t)}{N_{H}} \\ &- \mu_{N} S_{N}(t) , \\ E'_{N}(t) &= \frac{T_{N} b_{N} I_{H}(t) S_{N}(t)}{N_{H}} - \gamma_{N} E_{N}(t) - \mu_{N} E_{N}(t) , \\ I'_{N}(t) &= \gamma_{N} E_{N}(t) - \mu_{N} I_{N}(t) , \\ A'_{W}(t) &= \frac{\rho_{W} F_{W}}{2K} \left(K - (A_{N}(t) + A_{W}(t)) \right) \\ &- A_{W}(t) \left(\mu_{WA} - \tau_{W} \right) , \\ S'_{W}(t) &= \frac{\omega A_{W}(t) \tau_{W}}{2} - \frac{S_{W}(t)}{N_{H}} \left(\mu_{W} + b_{W} T_{N} I_{H}(t) \right) , \\ E'_{W}(t) &= \frac{b_{W} T_{N} I_{H}(t) S_{W}(t)}{N_{H}} - \gamma_{W} E_{W}(t) - \mu_{W} E_{W}(t) , \\ I'_{W}(t) &= \gamma_{W} E_{W}(t) - \mu_{W} I_{W}(t) , \end{aligned}$$

where

$$\lambda_n = rac{T_N b_N I_N}{N_H}, \quad \lambda_W = rac{b_W T_{HW} I_W}{N_H}.$$

We calculate the basic reproduction number, which is the average number of new viruses created by one infected adult in a completely vulnerable group, using the notion of the next generation matrix. In the absence of modifications, the basic reproduction number is,

$$R_{A} = \sqrt{\frac{T_{N}^{2} b_{N}^{2} \gamma_{N} \gamma_{H} S_{N}}{\mu_{N} N_{H} (\alpha + \mu_{H}) (\gamma_{H} + \mu_{H}) (\gamma_{N} + \mu_{N})}}$$

III. METHODOLOGY

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For addressing the nonlinear mathematical dengue model, the developed structure of ANNs utilizing GA-ASA optimum is provided in two steps, as follows:

- The fitness function design is described for the ANNs parameters.
- The hybrid combination of GA-ASA provides vital settings for optimizing fitness function.

A. STRUCTURE OF ANNS

This section contains the mathematical formulas for solving each class of the nonlinear Causative Agent Prevention Virus (dengue model). The functions of the nonlinear dengue model are respectively represented as S_H , V_H , E_H , I_H , R_H , A_N , S_N , E_N , I_N , A_W , S_W , E_W , and I_W given as (2), shown at the bottom of the next page.

W signifies the unidentified weights in the above system, given as:

$$W = [W_{S_{H}}, W_{V_{H}}, W_{E_{H}}, W_{I_{H}}, W_{R_{H}}, W_{S_{N}}, W_{E_{N}}, W_{A_{N}}, W_{I_{N}}, W_{A_{W}}, W_{S_{W}}, W_{E_{W}}, W_{I_{W}}], \text{ for}$$

$$W_{S_{H}} = [k_{S_{H}}, \omega_{S_{H}}, c_{S_{H}}], \quad W_{V_{H}} = [k_{V_{H}}, \omega_{V_{H}}, c_{V_{H}}], W_{E_{H}} = [k_{E_{H}}, \omega_{E_{H}}, c_{E_{H}}], \quad W_{I_{H}} = [k_{I_{H}}, \omega_{I_{H}}, c_{I_{H}}], W_{R_{H}} = [k_{R_{H}}, \omega_{R_{H}}, c_{R_{H}}], \quad W_{A_{N}} = [k_{A_{N}}, \omega_{A_{N}}, c_{A_{N}}],$$

and

$$\begin{split} \boldsymbol{W}_{I_W} &= [\boldsymbol{k}_{I_W}, \boldsymbol{\omega}_{I_W}, \boldsymbol{c}_{I_W}].\\ \boldsymbol{k}_{SH} &= [k_{SH,1}, k_{SH,2}, \dots, k_{SH,m}],\\ \boldsymbol{k}_{VH} &= [k_{VH,1}, k_{VH,2}, \dots, k_{VH,m}],\\ \boldsymbol{k}_{EH} &= [k_{EH,1}, k_{EH,2}, \dots, k_{EH,m}],\\ \boldsymbol{k}_{IH} &= [k_{IH,1}, k_{IH,2}, \dots, k_{IH,m}],\\ \boldsymbol{k}_{RH} &= [k_{RH,1}, k_{RH,2}, \dots, k_{RH,m}],\\ \boldsymbol{k}_{RH} &= [k_{RH,1}, k_{RH,2}, \dots, k_{RH,m}],\\ \boldsymbol{k}_{SN} &= [k_{SN,1}, k_{SN,2}, \dots, k_{SN,m}],\\ \boldsymbol{k}_{EN} &= [k_{EN,1}, k_{EN,2}, \dots, k_{EN,m}],\\ \boldsymbol{k}_{EN} &= [k_{EN,1}, k_{EN,2}, \dots, k_{EN,m}],\\ \boldsymbol{k}_{EN} &= [k_{EN,1}, k_{EN,2}, \dots, k_{EN,m}],\\ \boldsymbol{k}_{EW} &= [k_{LN,1}, k_{LN,2}, \dots, k_{LN,m}],\\ \boldsymbol{k}_{AW} &= [k_{SW,1}, k_{SW,2}, \dots, k_{SW,m}],\\ \boldsymbol{k}_{EW} &= [k_{SW,1}, k_{SW,2}, \dots, k_{SW,m}],\\ \boldsymbol{k}_{EW} &= [k_{EW,1}, k_{EW,2}, \dots, k_{EW,m}],\\ \boldsymbol{k}_{EW} &= [k_{EW,1}, k_{EW,2}, \dots, k_{EW,m}],\\ \boldsymbol{k}_{EW} &= [k_{EW,1}, k_{EW,2}, \dots, k_{EW,m}],\\ \boldsymbol{k}_{IW} &= [k_{IW,1}, k_{IW,2}, \dots, k_{IW,m}],\\ \boldsymbol{k}_{SH} &= [w_{SH,1}, w_{SH,2}, \dots, w_{SH,m}], \end{split}$$

$$\begin{bmatrix} S_{H}(t), \quad V_{H}(t), \quad E_{H}(t), \quad I_{H}(t) \\ I_{N}(t), \quad A_{N}(t), \quad S_{N}(t), \quad E_{N}(t), \\ I_{W}(t) \end{bmatrix} = \begin{bmatrix} \sum_{i=1}^{m} k_{S_{H},i}g(w_{S_{H},i}t + c_{S_{H},i}), \quad \sum_{i=1}^{m} k_{I_{H},i}g(w_{I_{H},i}t + c_{I_{H},i}), \\ \sum_{i=1}^{m} k_{I_{H},i}g(w_{I_{H},k}t + c_{I_{H},i}), \quad \sum_{i=1}^{m} k_{I_{H},i}g(w_{I_{H},i}t + c_{I_{H},i}), \\ I_{N}(t), \quad A_{W}(t), \quad S_{W}(t), \quad E_{W}(t), \\ I_{W}(t) \end{bmatrix} = \begin{bmatrix} \sum_{i=1}^{m} k_{S_{H},i}g(w_{S_{H},k}t + c_{S_{H},i}), \quad \sum_{i=1}^{m} k_{I_{H},i}g(w_{E_{N},i}t + c_{E_{N},i}), \\ \sum_{i=1}^{m} k_{S_{N},i}g(w_{S_{N},i}t + c_{S_{N},i}), \quad \sum_{i=1}^{m} k_{E_{N},i}g(w_{E_{N},i}t + c_{E_{N},i}), \\ \sum_{i=1}^{m} k_{S_{N},i}g(w_{S_{N},i}t + c_{S_{N},i}), \quad \sum_{i=1}^{m} k_{E_{N},i}g(w_{E_{N},i}t + c_{E_{N},i}), \\ \sum_{i=1}^{m} k_{S_{W},i}g(w_{I_{W},k}t + c_{S_{H},i}), \quad \sum_{i=1}^{m} k_{E_{W},i}g(w_{E_{W},i}t + c_{E_{W},i}), \\ \sum_{i=1}^{m} k_{S_{W},i}g(w_{I_{W},k}t + c_{S_{H},i}), \quad \sum_{i=1}^{m} k_{E_{W},i}g'(w_{H_{H},i}t + c_{H_{H},i}), \\ \sum_{i=1}^{m} k_{E_{H},i}g'(w_{E_{H},i}t + c_{E_{H},i}), \quad \sum_{i=1}^{m} k_{E_{W},i}g'(w_{H_{H},i}t + c_{H_{H},i}), \\ \sum_{i=1}^{m} k_{E_{H},i}g'(w_{E_{H},i}t + c_{E_{H},i}), \quad \sum_{i=1}^{m} k_{E_{H},i}g'(w_{E_{N},i}t + c_{E_{N},i}), \\ \sum_{i=1}^{m} k_{E_{N},i}g'(w_{E_{N},i}t + c_{E_{H},i}), \quad \sum_{i=1}^{m} k_{E_{N},i}g'(w_{E_{N},i}t + c_{E_{N},i}), \\ \sum_{i=1}^{m} k_{E_{N},i}g'(w_{E_{N},i}t + c_{E_{N},i}), \quad \sum_{i=1}^{m} k_{E_{N},i}g'(w_{E_{N},i}t + c_{E_{N},i}), \\ \sum_{i=1}^{m} k_{E_{N},i}g'(w_{E_{N},i}t + c_{E_{N},i}), \quad \sum_{i=1}^{m} k_{E_{N},i}g'(w_{E_{N},i}t + c_{E_{N},i}), \\ \sum_{i=1}^{m} k_{E_{N},i}g'(w_{E_{N},i}t + c_{E_{N},i}), \quad \sum_{i=1}^{m} k_{E_{N},i}g'(w_{E_{N},i}t + c_{E_{N},i}), \\ \sum_{i=1}^{m} k_{E_{N},i}g'(w_{E_{N},i}t + c_{E_{N},i}), \quad \sum_{i=1}^{m} k_{E_{N},i}g'(w_{E_{N},i}t + c_{E_{N},i}), \\ \sum_{i=1}^{m} k_{E_{N},i}g'(w_{E_{N},i}t + c_{E_{N},i}), \quad \sum_{i=1}^{m} k_{E_{N},i}g'(w_{E_{N},i}t + c_{E_{N},i}), \\ \sum_{i=1}^{m} k_{E_{N},i}g'(w_{E_{N},i}t + c_{E_{N},i}), \quad \sum_{i=1}^{m} k_{E_{N},i}g'(w_{E_{N},i}t + c_{E_{N},i}), \\ \sum_{i=1}^{m} k_{E_{N},i}g'(w_{E_{N},i}t + c_{E_{N},i}), \quad \sum$$

 $c_{I_N} = [c_{I_N,1}, c_{I_N,2}, \dots, c_{I_N,m}],$ $c_{A_W} = [c_{A_W,1}, c_{A_W,2}, \dots, c_{A_W,m}],$ $c_{S_W} = [c_{S_W,1}, c_{S_W,2}, \dots, c_{S_W,m}],$ $c_{E_W} = [c_{E_W,1}, c_{E_W,2}, \dots, c_{E_W,m}],$ $c_{I_W} = [c_{I_W,1}, c_{I_W,2}, \dots, c_{I_W,m}].$

In the above system, the activation function log-sigmoid $g(\tau) = 1/(1 + E^{\wedge}(-\tau))$ is applied given as (3), shown at the bottom of the page.

The GA-ASA techniques are used to optimize an errorbased 'fitness function,' which is given as:

$$e = \sum_{n=1}^{14} e_n,$$

$$e_1 = \frac{1}{N} \sum_{i=1}^{N} \left[(\hat{S}'_H)_i - \beta N_H + (\lambda_n + p + \lambda_w + \mu_H) (\hat{S}_H)_i \right]$$
(4)

$$-\varphi(\hat{V}_H)_i\Big]^2,\tag{5}$$

$$e_{2} = \frac{1}{N} \times \sum_{i=1}^{N} \left[(\hat{V}'_{H})_{i} - p(\hat{S}_{H})_{i} + (1 - \varepsilon)(\hat{V}_{H})_{i} (\lambda_{n} + \lambda_{w}) + (\hat{V}_{H})_{i} (\varphi + \mu_{h}) \right]^{2}, \qquad (6)$$

$$e_{3} = \frac{1}{N} \times \sum_{i=1}^{N} \left[(\hat{E}'_{H})_{i} - (\lambda_{n} + \lambda_{w}) (\hat{S}_{H})_{i} - (1 - \varepsilon) (\hat{V}_{H}(t))_{i} \times (\lambda_{n} + \lambda_{w}) + (\hat{E}_{H})_{i} (\gamma_{H} + \mu_{H}) \right]^{2}, \quad (7)$$

$$e_{4} = \frac{1}{1} \sum_{i=1}^{N} \sum_{j=1}^{N} \left[(\hat{I}'_{H})_{i} - \gamma_{H} (\hat{E}_{H})_{i} + \alpha (\hat{I}_{H})_{i} + \mu_{H} (\hat{S}_{H})_{i} \right]^{2}, \quad (7)$$

$$e_{4} = \frac{1}{N} \sum_{i=1}^{N} \left[(\hat{I}'_{H})_{i} - \gamma_{H} (\hat{E}_{H})_{i} + \alpha (\hat{I}_{H})_{i} + \mu_{H} (\hat{S}_{H})_{i} \right]^{2},$$
(8)

$$e_{5} = \frac{1}{N} \sum_{i=1}^{N} \left[(\hat{R}'_{H})_{i} - \alpha (\hat{I}_{H})_{i} + \mu_{H} (\hat{R}_{H})_{i} \right]^{2}, \qquad (9)$$

$$e_{6} = \frac{1}{N}$$

$$N \times \sum_{i=1}^{N} \left[(\hat{A}'_{N})_{i} - \frac{1}{2(F_{N} + F_{W})} \rho_{N} F_{N}^{2} + \left(1 - \frac{\left((\hat{A}_{N})_{i} + (\hat{A}_{W})_{i} \right)}{K} \right) + (\hat{A}_{N})_{i} (\tau_{N} + \mu_{NA}) \right]^{2},$$

$$(10)$$

$$\begin{aligned} e_{7} &= \frac{1}{N} \\ &\times \sum_{i=1}^{N} \left[(\hat{S}'_{N})_{i} - \frac{(\hat{A}_{N})_{i}\tau_{N}}{2} - (1-\omega) \frac{(\hat{A}_{N})_{i}\tau_{N}}{2} \\ &+ \frac{T_{N}b_{N}(\hat{I}_{H})_{i}(\hat{S}_{N})_{i}}{N_{H}} + \mu_{N}(\hat{S}_{N})_{i} \right]^{2}, \end{aligned}$$
(11)

$$e_{8} = \frac{1}{N} \sum_{i=1}^{N} \left[(\hat{E}'_{N})_{i} - \frac{T_{N} b_{N} (\hat{I}_{H})_{i} (\hat{S}_{N})_{i}}{N_{H}} + \gamma_{N} (\hat{E}_{N})_{i} + \mu_{N} (\hat{E}_{N})_{i} \right]^{2}, \qquad (12)$$

$$e_9 = \frac{1}{N} \sum_{i=1}^{N} \left[(\hat{I'}_N)_i - \gamma_N (\hat{E}_N)_i - \mu_N (\hat{I}_N)_i \right]^2, \quad (13)$$

$$e_{10} = \frac{1}{N} \sum_{i=1}^{N} \left[(\hat{A'}_W)_i - \frac{\rho_W F_W}{2K} \left(K - \left((\hat{A}_N)_i + (\hat{A}_W)_i \right) \right) - (\hat{A}_W)_i \left(\mu_{WA} - \tau_W \right) \right]^2,$$
(14)

$$e_{11} = \frac{1}{N} \sum_{i=1}^{N} \left[(\hat{S}'_W)_i - \frac{\omega(\hat{A}_W)_i \tau_W}{2} - \frac{(\hat{S}_W)_i}{N_H} \times \left(\mu_W + b_W T_N(\hat{I}_H)_i \right) \right]^2,$$
(15)

$$e_{12} = \frac{1}{N} \sum_{i=1}^{N} \left[(\hat{E}'_W) - \frac{b_W T_N (\hat{I}_H)_i (\hat{S}_W)_i}{N_H} - \gamma_W (\hat{E}_W)_i - \mu_W (\hat{E}_W)_i \right]^2,$$
(16)

$$e_{13} = \frac{1}{N} \sum_{i=1}^{N} \left[(\hat{I'}_W)_i - \gamma_W (\hat{E}_W)_i + \mu_W (\hat{I}_W)_i \right]^2, \quad (17)$$

$$\begin{aligned} e_{14} &= \frac{1}{13} \\ & \left[\begin{array}{c} ((\hat{S}'_{H})_{i} - I_{1})^{2} + ((\hat{V}'_{H})_{i} - I_{2})^{2} + ((\hat{E}'_{H})_{i} - I_{3})^{2} \\ + ((\hat{I}'_{H})_{i} - I_{4})^{2} + ((\hat{R}'_{H})_{i} - I_{5})^{2} + ((\hat{A}'_{N})_{i} - I_{6})^{2} \\ + ((\hat{S}'_{N})_{i} - I_{7})^{2} + ((\hat{E}'_{N})_{i} - I_{8})^{2} + ((\hat{I}'_{N})_{i} - I_{9})^{2} \\ + ((\hat{A}'_{W})_{i} - I_{10})^{2} + ((\hat{S}'_{W})_{i} - I_{11})^{2} + ((\hat{E}'_{W})_{i} - I_{12})^{2} \\ + ((\hat{I}'_{W})_{i} - I_{13})^{2} \end{array} \right]. \end{aligned}$$

$$(18)$$

where

$$(\hat{S}_H)_i = S_H(t_i), \quad (\hat{V}_H)_i = V_H(t_i), (\hat{E}_H)_i = E_H(t_i), \quad (\hat{I}_H)_i = I_H(t_i), (\hat{R}_H)_i = R_H(t_i), \quad (\hat{A}_N)_i = A_N(t_i), (\hat{S}_N)_i = S_N(t_i), \quad (\hat{E}_N)_i = E_N(t_i), (\hat{I}_N)_i = I_N(t_i), \quad (\hat{A}_W)_i = A_W(t_i), (\hat{S}_W)_i = S_W(t_i), \quad (\hat{E}_W)_i = E_W(t_i), (\hat{I}_W)_i = I_W(t_i).$$

The quantites $e_1, e_2, e_3...$ and e_{13} indicate the fitness functions associated to differential system (1), whereas the corresponding initial conditions is represented in e_{14} .

B. OPTIMIZATION PERFORMANCES: GA-ASA

Optimal performance of nonlinear mathematical model of dengue virus with treatment procedure is simulated thru the artificial technique GA-ASA. The genetic algorithm (GA) is a paradigm of abiogenesis introduce by John Holland et al. [46]. He was widely credited as being the first one to bring the concept of crossover, mutation and selections in artificial system which are the necessary parts of genetic algorithm arise as problem-solving agent. Since that day, a variety of genetic algorithm versions have now been devised and utilized in a variety of optimization problems, ranging from discrete systems like salesperson travelling problem to continuous systems arise in designation of airfoils in aerospace, from coloring of graph to pattern recognition, and from monetary markets to multi-objective engineering optimization [47]. Many other applications of GA are in biomedical field such as cancer datasets with multi-dimensional [48], categorization of anomalous computed tomography brain tumor images [49], transcriptomic cancer classifier [50], prediction of liver diseases model [51], in transportation field applicable in vehicle routing model and monorail dynamics model [52], [53], in geophysical side for prediction of air blast [54], cloud model [55], and for groundwater flow model [56], and wind power systems [57], etc.

Using the hybridize with the local search technique, quick convergence is achieved by combining global search with any local search approach. As an initial input, the best GA values are assigned. To standardize the variables, the local search active set algorithm is used. In optimization theory, the active set is highly crucial since it decides which constraints will have an impact on the result of optimization. The active set, for instance, specifies the hyperplanes that cross at the solution point while solving a linear programming issue. Here are few contributions that us ASA such that water supply model to manage the flow [58], optimal control issue based on PDE [59], node-based shape optimization [60], and for electrodynamic problems [61].

The constructed ANNs-GA-ASA for the dengue model is illustrated in Figure 2.

TABLE 2. Optimization procedure thru ANN-GA-ASA for dengue mathematical model.

GA
Inputs: The selection of the chromosomes is
$$W = [K, W, C]$$

Population: A chromosomes vector is provided as:
 $W = [W_{S_{H}}, W_{V_{H}}, W_{E_{H}}, W_{L_{H}}, W_{R_{H}}, W_{A_{H}}, W_{S_{H}}, W_{E_{H}}, W_{A_{H}}, W_{S_{H}}, W_{E_{H}}, W_{L_{H}}, M_{L_{H}}, 0_{I_{H}}, c_{I_{H}}], for
 $W_{S_{H}} = [k_{S_{H}}, a_{S_{H}}, c_{S_{H}}], W_{V_{H}} = [k_{V_{H}}, a_{V_{H}}, c_{V_{H}}], W_{E_{H}} = [k_{E_{H}}, a_{E_{H}}, c_{L_{H}}], W_{I_{H}} = [k_{I_{H}}, a_{I_{H}}, c_{I_{H}}], W_{S_{H}} = [k_{S_{H}}, a_{S_{H}}, c_{S_{H}}], W_{E_{H}} = [k_{E_{H}}, a_{E_{H}}, c_{E_{H}}] = and$
 $W_{I_{H}} = [k_{I_{H}}, a_{I_{H}}, c_{I_{H}}], W_{A_{H}} = [k_{A_{H}}, a_{A_{H}}, c_{A_{H}}], W_{S_{H}} = [k_{S_{H}}, a_{S_{H}}, c_{S_{H}}], W_{E_{H}} = [k_{E_{H}}, a_{E_{H}}, c_{E_{H}}] = and$
 $W_{I_{H}} = [k_{I_{H}}, a_{I_{H}}, c_{I_{H}}].$
Outputs: Global weight vectors are W_{B-GA}
Initialization: For chromosomes selection, use W_{B-GA}
Fit Valuation: Adjust the fitness (e) in population using Eqs 4-18
• Stopping standards: [Tol-Con=Tol-Fun=10⁻²¹], [Stall-Limit=150], [Generations = 110], [e = 10⁻²²] & [Pop-Size=240].$
Move to storage
Storage: W_{B-GA} , iterations, time, e and count of function.
End of GA
ASA
Inputs: W_{B-GA} .
Output: $W_{G-A,ASA}$ assignments, iterations, and other perks.
Stopping merits: $[e - 10^{-21}], [Tol-Con = 10^{-21}], [Iterations = 930], [Tol-X = Tol-Fun= 10-18] and [Max-Fun-Evals= 247000].$
Fit Valuation: Calculate e and W for Eqs 4-18.
Amendments: Regulate 'finincon' for ASA
Accumulate: Transform e, $W_{G-A,ASA}$, time, function counts and iterations for ASA.
ASA End

C. PERFORMANCE MEASURES

In this section, the statistical operator characteristics relying on "Theil's inequality coefficient (TIC)", "Variance account for (VAF)", "Mean absolute deviation (MAD)", and "Semi interquartile range (S.I.R)" are theoretically described in order to solve dengue mathematical model. (19)–(21), as shown at the bottom of pages 10 and 11, respectively. $\begin{cases} \text{S.I Range} = 0.5 \times (q_3 - q_1), \\ q_1 = 1^{st} \text{ quartile & } q_3 = 3^{rd} \text{ quartile,} \end{cases}$ (22)

r shows the grid point, while \hat{S}_H , \hat{V}_H , \hat{E}_H , \hat{I}_H , \hat{R}_H , \hat{A}_N , \hat{S}_N , \hat{E}_N , \hat{I}_N , \hat{A}_W , \hat{S}_W and \hat{I}_W are the approximate outcomes.



FIGURE 1. Structures of the existing approach to solve the mathematical dengue model.



xiii) Weight of $\left(I_{\scriptscriptstyle W}
ight)$ with 5 neurons

FIGURE 2. Trained weight of dengue model with best fitness.

IV. SIMULATIONS AND RESULTS

This section contains thorough reviews of the acquired findings for the dengue treatment in the presence of Wolbachia and non-Wolbachia (1). Equation (1) comprises the 3 cases of dengue reduction. (i) Vaccination (ii) Wolbachia treatment and (iii) Vaccination and Wolbachia combine. The Genetic Algorithm and active set algorithm is adopted for 0-1 inputs along 0.1 step size of the dengue mathematical model in equation (1). The findings of the Adams comparison show that the dengue modeling approach is valid. Moreover, statistical findings are provided to ensure that the planned procedure is precise and accurate.

$$\begin{split} S'_{H}(t) &= 0.0005852 - (1.3298)S_{H}(t) + 0.1V_{H}(t), \\ I_{1} &= 0.1, \\ V'_{H}(t) &= 0.2S_{H}(t) - 0.4144V_{H}(t) - 0.1151V_{H}(t), \end{split}$$

$$\left[\begin{array}{c} \mathsf{VAF}_{Sy}, \mathsf{VAF}_{Uy}, \mathsf{VAF}_{Uy}, \mathsf{VAF}_{Ey}, \mathsf{VAF}_{Ey}, \mathsf{VAF}_{Ey} \\ \mathsf{VAF}_{Sy}, \mathsf{VAF}_{W}, \mathsf{VAF}_{W}, \mathsf{VAF}_{Sy}, \mathsf{VAF}_{Ey}, \mathsf{VAF}_{Ey} \\ \mathsf{VAF}_{W}, \mathsf{VAF}_{W}, \mathsf{VAF}_{W}, \mathsf{VAF}_{W}, \mathsf{VAF}_{W}, \mathsf{VAF}_{Ey} \\ \mathsf{VAF}_{W}, \mathsf{VAF}_{W}, \mathsf{VAF}_{W}, \mathsf{VAF}_{W}, \mathsf{VAF}_{W}, \mathsf{VAF}_{W} \\ \mathsf{VAF}_{W}, \mathsf{VAF}_{W}, \mathsf{VAF}_{W}, \mathsf{VAF}_{W}, \mathsf{VAF}_{W}, \mathsf{VAF}_{W} \\ \mathsf{VAF}_{W}, \mathsf{VAF}_{W}, \mathsf{VAF}_{W} \\ \mathsf{VAF}_{W}, \mathsf{VAF}_{W}, \mathsf{VAF}_{W} \\ \mathsf{VAF}_{W}, \mathsf{VAF}_{W} \\ \mathsf{VAF}_{W}, \mathsf{VAF}_{W}, \mathsf{VAF}_{W} \\ \mathsf{VAF}_{W}, \mathsf{VAF}_{W} \\ \mathsf{VAF}_{W}, \mathsf{VAF}_{W} \\ \mathsf{VAF}_{W}, \mathsf{VAF}_{W}, \mathsf{VAF}_{W} \\ \mathsf{VA$$

٠N

LN

$$\begin{split} I_2 &= 0.1, \\ E'_H(t) &= 1.1147S_H(t) + 0.4144V_H(t) - 0.18204E_H(t), \\ I_3 &= 0.1, \\ I'_H(t) &= 0.182E_H(t) - 0.25I_H(t) - 0.0151S_H(t), \\ I_4 &= 0.1, \\ R'_H(t) &= 0.25I_H(t) - 0.0151R_H(t), \\ I_5 &= 0.1, \\ A'_N(t) &= 0.0833 \left(1 - \frac{(A_N(t) + A_W(t))}{2}\right) \\ &- 1.3214A_N(t), \\ I_6 &= 0.1, \\ S'_N(t) &= 1.15A_N(t) - 4.7052I_H(t)S_N(t) - 0.07S_N(t), \\ I_7 &= 0.1, \\ E'_N(t) &= 4.70521I_H(t)S_N(t) - 0.1E_N(t) - 0.07E_N(t), \\ I_8 &= 0.1, \\ I'_N(t) &= 0.1E_N(t) - 0.07I_N(t), \end{split}$$

$$I_{9} = 0.1,$$

$$A'_{W}(t) = 0.00687 (2 - (A_{N}(t) + A_{W}(t))) + 0.03A_{W}(t),$$

$$I_{10} = 0.1,$$

$$S'_{W}(t) = 0.045A_{W}(t) - S_{W}(t)$$

$$\times (2.0263 + 4.46886I_{H}(t)),$$

$$I_{11} = 0.1,$$

$$E'_{W}(t) = 4.4686I_{H}(t)S_{W}(t) - 0.182E_{W}(t)$$

$$-0.071E_{W}(t),$$

$$I_{12} = 0.1,$$

$$I'_{W}(t) = 0.182E_{W}(t) - 0.077I_{W}(t),$$

$$I_{13} = 0.1.$$
(23)

Using the above system, the fitness function may be written as (24), shown at the bottom of the next page.

The dengue mathematical system is solved utilizing the hybrid GA-ASA for 100 iterations with 120 parameters by optimizing the above fitness function. The proposed solutions of the dengue mathematical system are represented by the best weight vectors, which are as follows:

$$\hat{S}_{H}(t) = \frac{0.7473}{1 + e^{-(-0.8078t - 0.5602)}} - \frac{-1.8513}{1 + e^{-(-.8105t - 1.5264)}} \\ - \frac{2.4967}{1 + e^{-(-1.33565t - 2.6888)}}, \quad (25)$$

$$\hat{V}_{H}(t) = \frac{0.2023}{1 + e^{-(-0.1105t - 0.8327)}} - \frac{0.0652}{1 + e^{-(0.1713t + 1.7523)}} \\ - \frac{-0.1710}{1 + e^{-(0.9462t + 0.2607)}}, \quad (26)$$

$$\begin{bmatrix} \operatorname{TIC}_{\mathcal{S}_{H}}, \operatorname{TIC}_{V_{H}}, \\ \operatorname{TIC}_{\mathcal{S}_{N}}, \operatorname{TIC}_{\mathcal{E}_{N}}, \\ \operatorname{TIC}_{\mathcal{S}_{N}, \operatorname{TIC}_{\mathcal{E}_{N}}, \\ \operatorname{TIC}_{\mathcal{S}_{N}}, \operatorname{TIC}_{\mathcal{E}_{N}}, \\ \operatorname{TIC}_{\mathcal{S}_{N}}, \operatorname{TIC}_{\mathcal{E}_{N}}, \\ \operatorname{TIC}_{\mathcal{S}_{N}, \operatorname{TIC}_{\mathcal{S}_{N}, \\ \operatorname{TIC}_{\mathcal{S}_{N}, \operatorname{TIC}_{\mathcal{S}_{N}}, \\ \operatorname{TIC}_{\mathcal{S}_{N}, \operatorname{TIC}_{\mathcal{S}_{N}}, \\ \operatorname{TIC}_{\mathcal{S}_{N}, \operatorname{TIC}_{\mathcal{S}_{N}, \\ \operatorname{$$

t	$(S_{\scriptscriptstyle H})$						
	Min	Max	Med	Mean	S.I Range	ST.D	
0	9.0119E-07	3.0444E-05	7.8165E-06	1.0058E-05	5.5727E-06	8.9102E-06	
0.05	3.7423E-07	2.5754E-05	4.2771E-06	7.1361E-06	3.5672E-06	7.8253E-06	
0.1	5.9058E-07	2.6260E-05	3.7032E-06	7.5301E-06	3.5474E-06	7.5801E-06	
0.15	1.9850E-07	3.1778E-05	9.5762E-06	1.0995E-05	4.6081E-06	8.0832E-06	
0.2	1.3148E-06	3.7704E-05	1.5796E-05	1.5166E-05	5.0600E-06	8.7289E-06	
0.25	2.0960E-06	4.2165E-05	1.8732E-05	1.8457E-05	5.9925E-06	9.5456E-06	
0.3	1.6505E-06	4.4103E-05	1.8670E-05	2.0329E-05	6.9399E-06	1.0692E-05	
0.35	5.4068E-07	4.3109E-05	1.9400E-05	2.0624E-05	8.8440E-06	1.2200E-05	
0.4	4.6515E-07	4.3539E-05	1.9377E-05	2.0443E-05	8.8407E-06	1.2021E-05	
0.45	1.1320E-06	4.2514E-05	2.0047E-05	1.9293E-05	7.6501E-06	1.1305E-05	
0.5	1.4241E-06	3.8804E-05	1.7343E-05	1.6799E-05	8.0163E-06	1.0780E-05	
0.55	6.0147E-07	3.2855E-05	1.3060E-05	1.3536E-05	6.6635E-06	9.7397E-06	
0.6	9.0710E-09	2.8290E-05	8.0802E-06	1.0025E-05	4.3658E-06	8.0140E-06	
0.65	1.2809E-07	2.0351E-05	6.1322E-06	6.9766E-06	4.1943E-06	5.9087E-06	
0.7	7.0510E-07	1.3073E-05	5.7889E-06	5.9150E-06	3.1439E-06	3.8942E-06	
0.75	8.9725E-08	1.4835E-05	4.4094E-06	6.3250E-06	3.4339E-06	4.9033E-06	
0.8	1.2538E-06	1.7678E-05	7.7740E-06	8.4981E-06	4.9879E-06	5.6778E-06	
0.85	3.1750E-07	2.8242E-05	9.9109E-06	9.7936E-06	4.2978E-06	6.6571E-06	
0.9	8.9169E-07	3.3816E-05	8.4099E-06	9.3942E-06	3.7136E-06	7.1088E-06	
0.95	2.2563E-07	3.2089E-05	5.0364E-06	6.8002E-06	2.3532E-06	6.6200E-06	
1	1.3103E-07	2.0733E-05	1.6795E-06	3.1559E-06	1.5291E-06	4.4429E-06	

TABLE 3. Statistical form for the dengue model based (S_H) class.

$$e = \frac{1}{N} \times \sum_{i=1}^{N} \left\{ \begin{bmatrix} (\hat{s}'_{H} - 0.000413N_{H} + (\frac{0.165\hat{l}_{N}}{N_{H}} - 0.200413 - \frac{0.078\hat{l}_{H}}{N_{H}})\hat{s}_{H}(i) - 0.1 \hat{v}_{H} \end{bmatrix}^{2} \\ + \left[\hat{v}'_{H} - 0.2\hat{s}_{H} + 0.462 \left(\frac{0.165\hat{l}_{N} + 0.078\hat{l}_{H}}{N_{H}} \right) \hat{v}_{H} - 0.1000413 \hat{v}_{H} \right]^{2} + \\ \left[\hat{E}'_{H} - \left(\frac{0.165\hat{l}_{N} + 0.078\hat{l}_{H}}{N_{H}} \right) \hat{s}_{H} - 0.462 \left(\frac{0.165\hat{l}_{N} + 0.078\hat{l}_{H}}{N_{H}} \right) \hat{v}_{H} - 0.18204\hat{E}_{H} \right]^{2} \\ + \left[\hat{t}'_{H} - 0.182\hat{E}_{H} + 0.25\hat{l}_{H} - 0.000413\hat{s}_{H} \right]^{2} + \left[\hat{R}'_{H} - 0.25\hat{l}_{H} + 0.000413\hat{R}_{H} \right]^{2} \\ + \left[\hat{k}'_{N} - \frac{1.25\hat{k}}{2(E_{N} + F_{W})} F_{N}^{2} \left(1 - \frac{(\hat{A}_{N} + \hat{A}_{W})}{K} \right) + 1.3214\hat{A}_{N} \right]^{2} \\ + \left[\hat{s}'_{N} - \frac{1.25\hat{k}_{N}}{N_{H}} - 0.525\frac{\hat{A}_{N}}{N} + \frac{0.164682\hat{l}_{H}\hat{S}_{N}}{N_{H}} + 0.07\hat{s}_{N} \right]^{2} \\ + \left[\hat{k}'_{N} - \frac{0.164682\hat{l}_{H}\hat{S}_{N}}{N_{H}} + 0.1\hat{E}_{N} + 0.07\hat{E}_{N} \right]^{2} + \left[\hat{t}'_{N} - 0.1\hat{E}_{N} + 0.07\hat{l}_{Nr} \right]^{2} \\ + \left[\hat{k}'_{W} - \frac{0.1564\hat{l}_{H}\hat{S}_{W}}{N_{H}} + 0.182\hat{E}_{W} + 0.071\hat{E}_{W} \right]^{2} + \left[\hat{t}'_{W} - 0.182\hat{E}_{W} + 0.077\hat{l}_{Wr} \right]^{2} \\ + \left[\hat{s}'_{W} - 0.045\hat{A}_{W} - \frac{\hat{s}_{W}}{N_{H}} \left(0.077 + 0.1564\hat{l}_{H} \right) \right]^{2} \\ + \left[\hat{t}'_{W} - 0.182\hat{E}_{W} + 0.012\hat{E}_{W} + 0.012\hat{E}_{W} + 0.071\hat{k}_{W} \right]^{2} + \left[\hat{t}'_{W} - 0.182\hat{E}_{W} + 0.077\hat{l}_{Wr} \right]^{2} \\ + \left[\hat{s}'_{W} - 0.045\hat{A}_{W} - \frac{\hat{s}_{W}}{N_{H}} \left(0.077 + 0.1564\hat{l}_{H} \right) \right]^{2} \\ + \left[\hat{t}'_{W} - 0.182\hat{E}_{W} + 0.012\hat{E}_{W} + 0.012\hat{E}_{W} + 0.071\hat{k}_{W} \right]^{2} \\ + \left[\hat{t}'_{W} - 0.182\hat{E}_{W} + 0.012\hat{E}_{W} + 0.012\hat{E}_{W} + 0.012\hat{E}_{W} + 0.071\hat{k}_{W} \right]^{2} \\ + \left[\hat{s}'_{W} - 0.012\hat{E}_{W} + \left(\hat{s}'_{N} \hat{s}_{N} - 0.1 \right)^{2} + \left(\hat{s}'_{N} \hat{s}_{N} - 0.1 \right)^{2} + \left(\hat{s}'_{H} \hat{s}_{N} - 0.1 \right)^{2} \\ + \left(\hat{s}'_{W} - 0.1 \right)^{2} + \left(\hat{s}'_{W} - 0.1 \right)^{2} + \left(\hat{s}'_{W} \hat{s}_{W} - 0.1 \right)^{2} \\ + \left(\hat{s}'_{W} - 0.1 \right)^{2} + \left(\hat{s}'_{W} \hat{s}_{W} - 0.1 \right)^{2} \\ + \left(\hat{s}'_{W} \hat{s}_{W} - 0.1 \right)^{2} + \left(\hat{s}'_{W} \hat{s}_{W} - 0.1 \right)^{2} \\ + \left(\hat{s}'_{W} - 0.1 \right)^{2} \\ + \left(\hat{s}'_{W}$$



FIGURE 3. The comparison of best, reference and mean solutions for the dengue system.



FIGURE 3. (Continued.) The comparison of best, reference and mean solutions for the dengue system.



FIGURE 3. (Continued.) The comparison of best, reference and mean solutions for the dengue system.



FIGURE 3. (Continued.) The comparison of best, reference and mean solutions for the dengue system.

t	$\left(V_{H} ight)$			$(E_{_H})$		
ı	Min	Mean	SIR	Min	Mean	SIR
0	3.6422E-07	6.5115E-06	2.7337E-06	7.5419E-09	3.6699E-06	2.0173E-06
0.05	5.2119E-07	6.5544E-06	4.9721E-06	4.0348E-07	5.4235E-06	3.0752E-06
0.1	4.1417E-08	5.3032E-06	3.4655E-06	9.3905E-08	5.8395E-06	2.7715E-06
0.15	2.5081E-08	3.1696E-06	1.6652E-06	1.1956E-06	8.4596E-06	3.7464E-06
0.2	1.2513E-07	3.7049E-06	1.6638E-06	5.4210E-07	1.3313E-05	6.9568E-06
0.25	1.8019E-06	6.6436E-06	2.6579E-06	4.4302E-08	1.8309E-05	1.0745E-05
0.3	2.2371E-06	1.0330E-05	3.5366E-06	8.8951E-07	2.2846E-05	1.2980E-05
0.35	1.5874E-06	1.3436E-05	4.5109E-06	1.3166E-06	2.5320E-05	1.3583E-05
0.4	4.1607E-07	1.5636E-05	4.6203E-06	2.8165E-06	2.6679E-05	1.2005E-05
0.45	4.5545E-07	1.7393E-05	4.5637E-06	4.3227E-06	2.6236E-05	1.1362E-05
0.5	6.0411E-07	1.8274E-05	4.0531E-06	5.4209E-07	2.4372E-05	1.1389E-05
0.55	2.7215E-06	1.8480E-05	3.4664E-06	2.8862E-06	2.1930E-05	1.2365E-05
0.6	3.3306E-06	1.7784E-05	6.4698E-06	1.9315E-06	1.8005E-05	9.2645E-06
0.65	6.9005E-07	1.6294E-05	7.0020E-06	1.9474E-06	1.3781E-05	5.7768E-06
0.7	6.3459E-07	1.5131E-05	6.9748E-06	1.0868E-06	9.5022E-06	3.6048E-06
0.75	3.4524E-08	1.4662E-05	7.8556E-06	6.5266E-07	9.1659E-06	3.2564E-06
0.8	2.5847E-07	1.4968E-05	9.5660E-06	2.3698E-07	1.1440E-05	7.3359E-06
0.85	7.9934E-07	1.5434E-05	1.0342E-05	3.6194E-07	1.3411E-05	7.8354E-06
0.9	4.2685E-08	1.4725E-05	9.8697E-06	5.9012E-08	1.3918E-05	7.3681E-06
0.95	2.5231E-07	1.2342E-05	8.7474E-06	3.8457E-08	1.2114E-05	6.1957E-06
1	1.4343E-07	7.7854E-06	6.4931E-06	1.5980E-06	8.4306E-06	3.6624E-06

TABLE 4. Statistical form for the dengue model based (V_H) and (E_H) classes.

$$\hat{E}_{H}(t) = \frac{-1.1560}{1 + e^{-(0.1434t + 0.3753)}} - \frac{0.5852}{1 + e^{-(2.0046t + 2.4891)}} - \frac{0.3524}{1 + e^{-(0.009178)}},$$
(27)
$$\hat{I}_{H}(t) = \frac{0.0009178}{1 + e^{-(0.2297t - 0.1076)}} - \frac{0.0975}{1 + e^{-(1.1845t - 0.5986)}} - \frac{0.2455}{1 + e^{-(-0.6195t - 1.0212)}},$$
(28)

$$\hat{R}_{H}(t) = \frac{0.3716}{1 + e^{-(0.2188t + 1.7740)}} - \frac{0.1099}{1 + e^{-(-0.5871t + 0.5293)}} \\ - \frac{-0.3944}{1 + e^{-(-0.2998 + 0.9808)}},$$
(29)
$$\hat{A}_{N}(t) = \frac{-1.0474}{1 + e^{-(-0.1646t - 0.2226)}} - \frac{0.7539}{1 + e^{-(0.0439t + 0.8545)}} \\ - \frac{0.0524}{1 + e^{-(1.4054t + 0.8575)}},$$
(30)



FIGURE 4. Relative observation of absolute errors for 5 number of neurons.



FIGURE 4. (Continued.) Relative observation of absolute errors for 5 number of neurons.

$$\hat{S}_{N}(t) = \frac{-0.9953}{1 + e^{-(0.0833t - 1.0666)}} - \frac{0.4806}{1 + e^{-(0.1958t + 0.7104)}} \qquad \hat{I}_{N}(t) = \frac{-0.5449}{1 + e^{-(0.5943t + 0.8333)}} - \frac{0.5565}{1 + e^{-(0.4906t + 0.1319)}} \\ - \frac{0.1787}{1 + e^{-(0.6518t - 1.4993)}}, \qquad (31) \qquad - \frac{0.5985}{1 + e^{-(0.0263t - 08180)}}, \qquad (33) \\ \hat{E}_{N}(t) = \frac{1.0246}{1 + e^{-(0.5340t + 2.0261)}} - \frac{-0.6639}{1 + e^{-(-0.6442t - 1.9707)}} \qquad \hat{A}_{W}(t) = \frac{-0.0265}{1 + e^{-(0.592t + 0.6220)}} - \frac{-0.0525}{1 + e^{-(-0.9524t - 1.3714)}} \\ - \frac{-1.3326}{1 + e^{-(-0.1368 + 0.1736)}}, \qquad (32) \qquad - \frac{0.2641}{1 + e^{-(0.1429t - 0.0633)}}, \qquad (34)$$



a) Convergence measurements for $\left(S_{_H}
ight)$, $\left(V_{_H}
ight)$, $\left(E_{_H}
ight)$, and $\left(I_{_H}
ight)$ on TIC in the y-axis, and independent dengue model trials in the x-axis.



b) Convergence measurements for $(R_{\!_H})$, $(A_{\!_N})$, $(S_{\!_N})$, and $(E_{\!_N})$ on TIC in the y-axis, and independent dengue model trials in the x-axis.



c) Convergence measures for $(I_{_N})$, $(A_{_W})$, $(S_{_W})$, $(E_{_W})$ and $(I_{_W})$ on TIC in the y-axis, and independent dengue model trials in the x-axis.

FIGURE 5. Convergence schemes for the TIC values to solve the dengue nonlinear model.



a) Convergence measurements for $\left(S_{_H}
ight)$, $\left(V_{_H}
ight)$, $\left(E_{_H}
ight)$, and $\left(I_{_H}
ight)$ on MAD in the y-axis, and independent dengue model trials in the x-axis.



b) Convergence measures for $(R_{_H})$, $(A_{_N})$, $(S_{_N})$, and $(E_{_N})$ on MAD in the y-axis, and independent dengue model trials in the x-axis.



c) Convergence measures for $(I_{_N})$, $(A_{_W})$, $(S_{_W})$, $(E_{_W})$ and $(I_{_W})$ on MAD in the y-axis, and independent dengue model trials in the x-axis.

FIGURE 6. Convergence schemes for the MAD values to solve the dengue nonlinear model.



a) Convergence measures for $(S_{_H})$, $(V_{_H})$, $(E_{_H})$, and $(I_{_H})$ on EVAF in the y-axis, and independent dengue model trials in the x-axis.



b) Convergence measures for (R_H) , (A_N) , (S_N) , and (E_N) on EVAF in the y-axis, and independent dengue model trials in the x-axis.



c) Convergence measures for (I_N) , (A_W) , (S_W) , (E_W) and (I_W) on EVAF in the y-axis, and independent dengue model trials in the x-axis.



t		$\left(I_{_{H}} ight)$		$\left(R_{_{H}} \right)$		
-	Min	Mean	SIR	Min	Mean	SIR
0	6.8759E-08	7.1580E-06	6.6030E-07	1.9753E-08	1.1876E-06	6.6030E-07
0.05	2.3127E-07	8.0927E-06	2.7552E-06	5.8774E-07	5.0776E-06	2.7552E-06
0.1	2.7678E-07	9.1988E-06	4.6141E-06	4.4038E-09	7.5132E-06	4.6141E-06
0.15	8.5945E-07	8.7245E-06	5.5475E-06	6.0788E-08	8.4415E-06	5.5475E-06
0.2	2.3589E-07	1.0316E-05	5.0755E-06	5.3117E-07	8.5977E-06	5.0755E-06
0.25	1.9916E-06	1.4301E-05	4.1884E-06	6.8261E-08	8.0375E-06	4.1884E-06
0.3	2.3096E-06	1.8415E-05	3.1132E-06	2.3372E-06	7.4379E-06	3.1132E-06
0.35	2.0664E-06	2.2480E-05	3.4069E-06	6.8024E-07	6.4427E-06	3.4069E-06
0.4	1.1085E-06	2.6726E-05	3.1850E-06	2.5349E-07	6.1583E-06	3.1850E-06
0.45	1.3300E-06	2.9531E-05	2.9512E-06	2.0032E-07	7.4419E-06	2.9512E-06
0.5	3.3303E-06	3.0699E-05	3.8385E-06	3.8055E-07	9.5303E-06	3.8385E-06
0.55	3.2109E-06	3.0116E-05	5.0687E-06	2.6708E-07	1.2142E-05	5.0687E-06
0.6	1.2149E-06	2.8046E-05	6.2759E-06	1.1715E-06	1.4489E-05	6.2759E-06
0.65	2.3925E-07	2.5034E-05	6.9703E-06	1.9542E-06	1.6355E-05	6.9703E-06
0.7	1.0334E-06	2.1624E-05	7.8247E-06	1.1441E-06	1.7626E-05	7.8247E-06
0.75	1.8793E-06	1.9380E-05	8.3431E-06	3.1358E-07	1.8308E-05	8.3431E-06
0.8	1.0064E-06	1.7776E-05	8.2485E-06	4.4313E-07	1.8420E-05	8.2485E-06
0.85	1.9363E-07	1.6869E-05	8.3080E-06	1.0235E-06	1.7732E-05	8.3080E-06
0.9	4.5808E-07	1.6550E-05	7.7312E-06	1.3135E-06	1.6144E-05	7.7312E-06
0.95	1.0644E-06	1.4301E-05	6.4529E-06	9.5472E-07	1.3594E-05	6.4529E-06
1	1.4327E-06	1.1225E-05	4.7152E-06	5.4109E-07	1.0031E-05	4.7152E-06

TABLE 5. Statistical form for the dengue model based (I_H) and (R_H) classes.

TABLE 6. Statistical form for the dengue model based (A_N) and (S_N) classes.

t		$(A_{_N})$			(S_N)		
	Min	Mean	SIR	Min	Mean	SIR	
0	3.9986E-08	1.3070E-06	6.3971E-07	1.1826E-07	3.1741E-06	1.3048E-06	
0.05	7.4790E-04	7.6505E-04	3.0964E-06	6.0299E-07	4.7772E-06	2.4540E-06	
0.1	1.5031E-03	1.5264E-03	5.8109E-06	2.7733E-06	8.8789E-06	3.3144E-06	
0.15	2.2581E-03	2.2842E-03	7.5700E-06	6.0040E-06	1.3280E-05	3.3605E-06	
0.2	3.0119E-03	3.0381E-03	7.9224E-06	2.6973E-08	1.8125E-05	3.5124E-06	
0.25	3.7638E-03	3.7879E-03	8.0957E-06	7.1703E-06	2.4493E-05	3.2025E-06	
0.3	4.5129E-03	4.5334E-03	5.6376E-06	9.5425E-07	3.2112E-05	3.3380E-06	
0.35	5.2586E-03	5.2744E-03	3.8691E-06	1.1961E-05	4.2074E-05	2.7576E-06	
0.4	5.9958E-03	6.0107E-03	2.4351E-06	2.5950E-05	5.3826E-05	2.6889E-06	
0.45	6.7277E-03	6.7422E-03	5.2662E-06	4.2913E-05	6.7482E-05	3.7117E-06	
0.5	7.4517E-03	7.4688E-03	8.4429E-06	6.2751E-05	8.3120E-05	4.8389E-06	
0.55	8.1712E-03	8.1903E-03	1.0613E-05	7.6837E-05	1.0078E-04	6.5836E-06	
0.6	8.8845E-03	8.9067E-03	1.2218E-05	9.1791E-05	1.2047E-04	6.8966E-06	
0.65	9.5916E-03	9.6180E-03	1.4398E-05	1.0945E-04	1.4216E-04	6.6988E-06	
0.7	1.0294E-02	1.0324E-02	1.5872E-05	1.3003E-04	1.6580E-04	7.6023E-06	
0.75	1.0993E-02	1.1025E-02	1.8000E-05	1.5374E-04	1.9131E-04	8.3460E-06	
0.8	1.1688E-02	1.1720E-02	1.8524E-05	1.8073E-04	2.1859E-04	9.0482E-06	
0.85	1.2380E-02	1.2411E-02	1.8087E-05	2.1044E-04	2.4752E-04	9.4689E-06	
0.9	1.3068E-02	1.3096E-02	1.5800E-05	2.4367E-04	2.7797E-04	9.0129E-06	
0.95	1.3753E-02	1.3776E-02	1.2377E-05	2.8101E-04	3.0979E-04	7.5381E-06	
1	1.4435E-02	1.4451E-02	7.3635E-06	3.2264E-04	3.4282E-04	4.6908E-06	

TABLE 7. Statistical form for the dengue model based (E_N) and (I_N) classes.

t		(E_N)			(I_N)		
	Min	Mean	SIR	Min	Mean	SIR	
0	6.7817E-08	3.1481E-06	1.5148E-06	3.7997E-08	2.4965E-06	5.6616E-07	
0.05	6.1056E-07	4.1646E-06	7.9355E-07	8.2454E-08	5.4743E-06	1.9614E-06	
0.1	3.8718E-07	4.6992E-06	1.6388E-06	3.1200E-07	7.1752E-06	2.0987E-06	
0.15	1.7872E-07	5.4966E-06	2.3462E-06	5.0197E-08	7.4165E-06	3.5179E-06	
0.2	2.4110E-07	7.6291E-06	2.2365E-06	6.0621E-07	7.6521E-06	4.4114E-06	
0.25	9.9928E-07	9.9748E-06	1.8943E-06	3.7268E-07	8.1770E-06	3.3622E-06	
0.3	1.1497E-06	1.2751E-05	3.1555E-06	3.0067E-07	8.5030E-06	4.6976E-06	
0.35	4.0627E-06	1.7631E-05	3.7362E-06	4.0227E-07	9.1942E-06	5.6627E-06	
0.4	6.9358E-06	2.2972E-05	4.9581E-06	3.0425E-07	9.7818E-06	6.2956E-06	
0.45	1.1060E-05	2.8798E-05	7.3598E-06	6.3480E-08	9.7856E-06	6.2793E-06	
0.5	1.6060E-05	3.5195E-05	7.8271E-06	6.0136E-08	1.0983E-05	6.6834E-06	
0.55	1.7465E-05	4.2308E-05	7.8929E-06	1.4528E-07	1.1729E-05	7.0932E-06	
0.6	1.9852E-05	5.0334E-05	8.3368E-06	1.1485E-07	1.2077E-05	6.2800E-06	
0.65	2.3729E-05	5.9512E-05	8.0676E-06	1.6628E-09	1.2087E-05	5.3430E-06	
0.7	2.9676E-05	7.0121E-05	6.8826E-06	2.0423E-07	1.1765E-05	4.9978E-06	
0.75	3.8339E-05	8.2467E-05	6.8887E-06	4.9059E-09	1.1213E-05	5.1541E-06	
0.8	5.0427E-05	9.6883E-05	7.5204E-06	5.4467E-07	1.1199E-05	5.4431E-06	
0.85	6.6698E-05	1.1372E-04	8.8536E-06	7.0160E-07	1.1123E-05	5.2847E-06	
0.9	8.7962E-05	1.3335E-04	9.3697E-06	9.4606E-08	1.0878E-05	4.9130E-06	
0.95	1.1506E-04	1.5613E-04	9.5236E-06	2.0659E-07	9.5843E-06	4.1418E-06	
1	1.4792E-04	1.8247E-04	8.9417E-06	2.0205E-07	6.7054E-06	3.6067E-06	

TABLE 8. Statistical form for the dengue model based $({\it A_W})$ and $({\it S_W})$ classes.

t		(A_W)			(S_w)			
	Min	Mean	SIR	Min	Mean	SIR		
0	3.0060E-07	4.1044E-06	2.2249E-06	5.9308E-07	7.1652E-06	3.3208E-06		
0.05	3.5595E-07	5.1307E-06	1.4137E-06	2.6052E-08	5.3058E-06	1.8424E-06		
0.1	5.0885E-07	6.6664E-06	2.3319E-06	1.6815E-07	4.7316E-06	2.0576E-06		
0.15	6.5754E-07	7.5955E-06	3.7213E-06	3.1043E-07	9.1789E-06	2.8217E-06		
0.2	7.3599E-07	7.9459E-06	4.4309E-06	3.0524E-06	1.5063E-05	4.3481E-06		
0.25	6.7229E-07	8.1159E-06	3.6385E-06	8.9662E-07	2.0378E-05	7.7740E-06		
0.3	5.0286E-07	8.1837E-06	2.4326E-06	2.4110E-07	2.4707E-05	1.0886E-05		
0.35	3.0965E-07	8.1917E-06	2.7320E-06	4.2679E-07	2.6959E-05	1.3480E-05		
0.4	6.6627E-08	8.3747E-06	4.5958E-06	1.2684E-07	2.6819E-05	1.4697E-05		
0.45	8.8853E-08	9.1617E-06	6.0794E-06	1.0298E-06	2.4613E-05	1.3919E-05		
0.5	2.6991E-07	1.0275E-05	6.9935E-06	2.6653E-07	2.0617E-05	1.3052E-05		
0.55	4.2605E-07	1.1387E-05	7.4624E-06	6.3562E-08	1.5929E-05	1.0371E-05		
0.6	3.4533E-08	1.2233E-05	6.5800E-06	8.5327E-07	1.1219E-05	5.0649E-06		
0.65	6.2955E-07	1.2915E-05	6.9225E-06	2.2427E-07	7.9768E-06	3.9237E-06		
0.7	3.9156E-07	1.3353E-05	6.7272E-06	9.1504E-07	9.0692E-06	4.6328E-06		
0.75	2.4959E-08	1.3524E-05	6.1437E-06	1.5198E-06	1.3221E-05	5.5814E-06		
0.8	4.2372E-07	1.3201E-05	6.5823E-06	9.1690E-08	1.6045E-05	7.2992E-06		
0.85	5.4248E-07	1.2428E-05	7.0547E-06	7.9736E-07	1.7158E-05	7.2016E-06		
0.9	4.0630E-07	1.1204E-05	6.8802E-06	1.2240E-06	1.5861E-05	6.0380E-06		
0.95	2.2764E-07	9.3822E-06	5.7449E-06	3.5560E-07	1.1748E-05	5.0309E-06		
1	8.0483E-09	7.2522E-06	3.9326E-06	5.7371E-08	4.5970E-06	2.9665E-06		

TABLE 9. Statistical form for the dengue model based (E_W) and (I_W) classes.

+		(E_W)		(I_w)			
l	Min	Mean	SIR	Min	Mean	SIR	
0	2.22036068933673e-	4.55740269105220e-	2.81025462517057e-	4.30973995935169e-	2.19396852703530e-	1.53890110822161e-	
	07	06	06	08	06	06	
0.05	6.18705254668006e-	3.12758782485684e-	2.77803390168890e-	1.99001820716527e-	2.69690746059620e-	1.33045010846863e-	
	08	06	06	08	06	06	
0.1	8.62512108679159e-	3.36078502992804e-	2.88895797916772e-	9.22018819904391e-	3.97175380598483e-	2.40724890424385e-	
	08	06	06	08	06	06	
0.15	4.94028725706031e-	4.68194134068054e-	1.96802824653855e-	2.82509819302113e-	6.09409680109654e-	3.64424396391214e-	
	08	06	06	07	06	06	
0.2	1.41536377312734e-	6.44911819071420e-	3.18038397158216e-	7.66144813965641e-	9.97033965875194e-	4.72938900709236e-	
	07	06	06	07	06	06	
0.25	7.08367172003177e-	8.31549556966418e-	4.70418892403735e-	2.44135442427351e-	1.32180646199416e-	5.60675552728485e-	
	08	06	06	06	05	06	
0.3	7.41952215166375e-	1.01646475519190e-	4.76086058360387e-	3.57195298777979e-	1.53452836494122e-	9.04327235668953e-	
	07	05	06	06	05	06	
0.35	6.60289123335933e-	1.13893451675791e-	4.62957037290768e-	1.71520291196436e-	1.63704146105406e-	1.06750598916558e-	
	07	05	06	06	05	05	
0.4	5.53418413123952e-	1.19475458050432e-	4.03248311831375e-	8.74847849247074e-	1.66388879970190e-	1.08797981379603e-	
	07	05	06	07	05	05	
0.45	3.97599815835092e-	1.23241039415030e-	3.31504358980911e-	7.72196147719173e-	1.59575817948662e-	1.09022539181748e-	
	07	05	06	08	05	05	
0.5	1.84286355391083e-	1.25304332618679e-	3.68402659661760e-	1.76063608580551e-	1.45136350228371e-	8.96045462660776e-	
	07	05	06	06	05	06	
0.55	1.14414647846284e-	1.21839900377979e-	5.53138083305392e-	1.94728208258860e-	1.23825380772453e-	8.47303178585189e-	
	07	05	06	06	05	06	
0.6	2.03233698481409e-	1.13043309435130e-	5.22910495942032e-	4.85065860859890e-	1.01596599801676e-	6.80307602976896e-	
	08	05	06	07	05	06	
0.65	7.15506884199635e-	1.02562708311420e-	5.06517497191397e-	4.59354057978645e-	9.07019588327826e-	6.06885376842718e-	
	07	05	06	07	06	06	
0.7	1.37998670678846e-	8.93627649299622e-	4.80546180759746e-	2.54231998467191e-	7.99206278630574e-	3.35308269086218e-	
	06	06	06	07	06	06	
0.75	9.45604892346741e-	7.41064554232417e-	4.62076132870005e-	5.93791905090235e-	6.95638891492698e-	4.57931108864378e-	
	07	06	06	08	06	06	
0.8	4.13881895908186e-	6.20251523308080e-	3.80613068615490e-	2.27567551726315e-	8.40673494992110e-	4.53299347690471e-	
	07	06	06	07	06	06	
0.85	3.44634046252346e-	6.75760671177451e-	4.68890659976844e-	2.91919035437516e-	9.19251446562276e-	4.24978184380802e-	
	07	06	06	07	06	06	
0.9	9.28101204986098e-	6.75723953484364e-	4.86213214240944e-	2.53674047268060e-	8.53200385312058e-	4.12755832495358e-	
	08	06	06	07	06	06	
0.95	3.01514209224973e-	5.97137549516631e-	3.49017660701036e-	1.78503050271561e-	6.27280924491852e-	3.34325665435516e-	
	08	06	06	07	06	06	
1	4.40170110499460e-	4.05983374677857e-	2.94002991492980e-	3.47950698947885e-	2.55137703230775e-	2.00388436789878e-	
	08	06	06	08	06	06	

$$\hat{S}_{W}(t) = \frac{-0.0038}{1 + e^{-(1.6262t - 2.6939)}} - \frac{3.7533}{1 + e^{-(-1.5112t - 3.7917)}} \\ - \frac{0.0323}{1 + e^{-(-1.0341t + 0.1005)}}, \quad (35)$$

$$\hat{E}_{W}(t) = \frac{-0.5196}{1 + e^{-(1.3278t + 1.8181)}} - \frac{0.6266}{1 + e^{-(0.2059t + 0.2056)}} \\ - \frac{0.4311}{1 + e^{-(-.4109t - 0.1291)}}, \quad (36)$$

$$\hat{I}_{W}(t) = \frac{0.0020}{1 + e^{-(-12.7782t - 3.4483)}} - \frac{1.1030}{1 + e^{-(-0.8979t - 2.7955)}} \\ - \frac{0.5522}{1 + e^{-(-1.3383t - 2.6500)}}, \quad (37)$$

Optimization of equation (1) is made through hybrid computing technique GA-ASA by setting 100 runs along 5 neurons. The balance weight of dengue model by GA-ASA are performed and then trained weight along 5 neurons of dengue model is set in Figure 2(i-xiii) for all classes such as S_H , V_H , E_H , I_H , R_H , A_N , S_N , E_N , I_N , A_W , S_W , E_W , and I_W given in equation (1). Figure 3 (i-xiii) constructed the best output of individual class as a result whereas the second half Figure 3 (xiv-xvii) show the comparison result of best weight between GA-ASA with Adam numerical method to solve the dengue model. The visible differences are not seen in all graphs yield close agreement of both strategies. Figure 4 dispatched the Absolute error of proposed model and Adam method where Figure (4a-4m) indicates the AE for S_H in range 10^{-7} to 10^{-5} , for V_H ranging 10^{-6} to 10^{-4} , for E_H in range 10^{-7} to 10^{-5} , I_H in interval 10^{-5} to 10^{-075} , for R_H



a) Histogram convergence plots for $\, \left(S_{_H}
ight)$, $\left(V_{_H}
ight)$, $\, \left(E_{_H}
ight)$, and $\left(I_{_H}
ight)$ on y-axis.



b) Histogram convergence plots for $\,\left(\,R_{_H}\,
ight)$, $\,\left(\,A_{_N}\,
ight)$, $\,\left(\,S_{_N}\,
ight)$, and $\,\left(\,E_{_N}\,
ight)$ on y-axis.



c) Histogram convergence plots for $(I_{_N})$, $(A_{_W})$, $(S_{_W})$, $(E_{_W})$ and $(I_{_W})$ on y-axis.

FIGURE 8. Comparison histogram plots of EVAF, MAD, and TIC for dengue nonlinear model.

TABLE 10.	Global TIC,	MAD and	E-VAF gages	for dengue	e model.
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Class	'G-MAD'		'G-]	ГІС'	'G-EVAF'	
Class	Min	SIR	Min	SIR	Min	SIR
(S_{H})	1.1636E-05	3.7116E-06	5.6555E-10	1.8412E-10	1.2386E-07	8.4516E-08
$\left(V_{H}\right)$	9.3185E-06	3.4545E-06	4.4188E-10	1.7559E-10	2.5326E-07	2.8162E-07
$\left(E_{H}\right)$	1.3504E-05	8.0419E-06	6.3888E-10	4.0287E-10	2.8825E-07	4.2281E-07
(I_H)	1.2905E-05	5.7073E-06	6.5340E-10	2.3561E-10	7.5572E-05	4.9109E-05
(R_H)	1.2243E-05	4.3911E-06	5.6940E-10	2.0673E-10	1.3411E-06	8.2096E-07
(A_N)	7.3785E-03	4.8948E-06	3.4929E-07	3.4528E-10	1.0251E-01	4.1984E-04
(S_N)	1.1845E-04	3.2523E-06	6.5360E-09	1.6845E-10	1.1884E-03	7.8390E-05
(E_N)	5.1762E-05	4.1151E-06	2.9793E-09	1.7539E-10	1.8364E-06	2.2532E-07
(I_N)	7.3991E-06	3.7211E-06	3.7317E-10	1.6379E-10	2.8975E-06	2.6266E-06
(A_w)	6.9579E-06	4.0029E-06	3.4331E-10	2.0404E-10	6.8653E-07	6.8112E-07
(S_w)	1.3897E-05	5.3805E-06	6.6657E-10	2.7031E-10	1.6343E-07	1.5222E-07
(E_w)	5.5785E-06	3.6408E-06	2.5119E-10	1.7026E-10	3.1541E-08	5.0920E-08
(I_w)	8.1631E-06	4.5888E-06	3.9105E-10	2.4293E-10	7.6442E-08	1.1903E-07

in range 10⁻⁶ to 10⁻³, for A_N in range 10⁻⁶ to 10⁻³, for S_N in interval 10⁻⁶ to 10⁻², E_N ranging 10⁻⁸ to 10⁻⁴, for I_N in range 10⁻⁷ to 10⁻⁵, A_W in interval 10⁻⁸ to 10⁻⁴, S_W in 10⁻⁷ - 10⁻⁵, E_W in the range 10⁻⁷ to 10⁻⁵, and I_W in interval 10⁻⁷ to 10⁻⁵ proven the resemblance of GA-ASA with numerical Adam method.

Figure 5 (a-c) -7 (a-c) signifies the concert operators built on E-VAF, TIC and MAD to decipher the dengue mathematical model. It is noted that the finest results of S_H , V_H , E_H , and I_H classes with E-VAF, MAD and TIC lie about 10^{-10} to 10^{-2} , 10^{-6} to 10^{-04} and 10^{-10} - 10^{-8} , respectively. The good result of R_H , A_N , S_N , and E_N lie around $10^{-8} - 10^{-6}$, $10^{-6} 10^{-2}$ and $10^{-6} - 10^{-4}$, for these operators, respectively. While, another appropriate results of I_N , A_W , S_W , E_W , and I_W lie around 10^{-9} to 10^{-4} , 10^{-06} to 10^{-4} and 10^{-11} to 10^{-9} , respectively. Since these findings, one might conclude that the proposed strategy is accurate. Figures 8 (a-c) show visualization tools with histograms employing statistical operations to validate the convergence measures for solving the dengue model. Throughout average resemblance of S_H , V_H , E_H , and I_H classes in histogram representation is in the range of 10^{-10} to 10^{-0} , for R_H , A_N , S_N , and E_N in interval 10^{-10} to 10^{-0} , and for I_N , A_W , S_W , E_W , and I_W classes in interval 10^{-11} to 10^{-5} in the case of EVAF, MAD, and TIC declared the convergence region of dengue model via GA-ASA.

Tables 3–8 show statistical analyses for all categories of the dengue mathematics system employing the tools Minimum (Min), Average (Mean), Maximum (Max), Median, SD, SI-Range for highly precise and consistency examination (ST-D).

The better outcomes of the suggested ANN-GA-ASA for handling the dengue mathematical model are the Minimal values whereas the Max values are worth of the suggested ANN-GA-ASA for tackling the dengue model. Based on these proofs of attained results, it is proved that ANN-GA-ASA is reliable and exact.

Convergence tabulation presentation for 100 iterations of ANN-GA-ASA of [G-FIT], [G-MAD], and [G-TIC] tools for each category of dengue model is shown in Table 10. The average values [G-FIT], [G-MAD], and [G-TIC] lie in

ranging $10^{-3}-10^{-6}$, $10^{-7}-10^{-10}$, and $10^{-1}-10^{-7}$ whereas SI values in interval $10^{-5} - 10^{-10}$ shows the significance for each category of dengue model. The close optimum outputs were observed by the global evaluations indicate to the ANN-GA-ASA's precision, reliability, and consistency.

V. CONCLUSION

This study is related to design a new coding scheme for tackling the nonlinear dengue mathematical model concern with treatment process. The treatment process is studied for three different situations such as vaccination, Wolbachia therapy, and combine both therapies. Artificial neural networks are used in conjunction with the features of the Genetic algorithm's global and Active-set algorithm as local search methodologies. The dengue nonlinear model is properly tested by manipulating the GA-ASA with neural networks layer structure for 5 number of neurons. The suggested model is tested through overlapping results with Adams numerical technique in the appropriate precision level while simulate the dengue model. Statistical tools in the form of "Mean", "Median", "Semi inter quartile range", "coefficient of Theil's inequality", "Mean absolute deviation", and "Variance account for" reveal the exactness and worth of adopted algorithm. "Mean", and "Semi inter quartile range" operators are used for global significance of nonlinear mathematical dengue model. The MAD and TIC operators are used to calculate the satisfactory values of the performance indices.

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