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# Lightweight Three-Factor-Based Privacy-Preserving Authentication Scheme for IoT-Enabled Smart Homes

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**ABSTRACT** Smart homes are an emerging paradigm of Internet of Things (IoT) in which users can remotely control various home devices via the internet anytime and anywhere. However, smart home environments are vulnerable to security attacks because an attacker can inject, insert, intercept, delete, and modify transmitted messages over an insecure channel. Thus, secure and lightweight authentication protocols are essential to ensure useful services in smart home environments. In 2021, Kaur and Kumar presented a two-factor based user authentication protocol for smart homes using elliptic curve cryptosystems (ECC). Unfortunately, we demonstrate that their scheme cannot resist security attacks such as impersonation and session key disclosure attacks, and also ensure secure user authentication. Moreover, their scheme is not suitable in smart home environments because it utilizes public-key cryptosystems such as ECC. Hence, we design a secure and lightweight three-factor based privacy-preserving authentication scheme for IoT-enabled smart home environments to overcome the security problems of Kaur and Kumar's protocol. We prove the security of the proposed scheme by using informal and formal security analyses such as the ROR model and AVISPA simulation. In addition, we compare the performance and security features between the proposed scheme and related schemes. The proposed scheme better provides security and efficiency compared with the previous schemes and is more suitable than previous schemes for IoT-enabled smart home environments.

**INDEX TERMS** Smart homes, privacy-preserving, authentication, security protocol.

## I. INTRODUCTION

With the advances in 5G communication and portable device technologies, smart homes are emerging as an exciting new paradigm of Internet of Things (IoT) and also it has attracted a lot of attention from both scientific and academic communities. Smart homes [1]–[3] are networking environments in which smart devices such as smart curtains, smart washing machines, smart light bulbs, smart TV, and smart door locks/control mechanisms can communicate with other devices, and also are remotely controlled.

In smart home environments, users are able to enjoy new smart functionalities and services such as a high level of comfort, and improved quality of life using a portable device. For example, if a user opens the door and enters the home, the smart home system starts working and turns on the

lights and boiler in the house. Moreover, the smart home can ensure convenient and efficient services to chronic diseases, disabled, and elderly people by identifying their health and behavioral patterns through smart devices. However, despite the multiple advantages of the smart home, it may cause serious privacy issues [4] since the collected data in smart devices are transmitted over an insecure channel. If collected data in smart devices is compromised, a malicious attacker can obtain the sensitive information of legitimate users, including daily habits and routines in the home, and also can utilize the information for criminal purposes. Moreover, the smart devices deployed in smart home environments are not suitable to apply public key cryptosystems (PKC) because it is resource-limited in terms of computation and communication overheads [5], [6]. Thus, secure and lightweight authentication and key agreement (AKA) schemes are essential to provide security and privacy for legitimate users [7]–[9].

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In 2019, Shuai *et al.* [10] proposed a two-factor based anonymous authentication protocol for smart homes using elliptic curve cryptography (ECC). However, Kaur and Kumar [11] pointed out that Shuai *et al.*'s scheme [10] is vulnerable to replay, insider, session key disclosure, offline password guessing, and gateway bypass attacks. In 2021, Kaur and Kumar [11] presented cryptanalysis and improvement of a two-factor based authentication scheme for smart homes using ECC to enhance the security flaws of Shuai *et al.*'s scheme [11]. However, we prove that Kaur and Kumar's scheme [11] is still vulnerable to impersonation, session key disclosure attacks, and also cannot provide mutual authentication. Moreover, their scheme is not suitable for resource-limited devices because it utilizes ECC that generates high computation and communication overheads. Therefore, we design a secure and lightweight three-factor based privacy-preserving authentication scheme for IoT-enabled smart homes to resolve the security problems Kaur and Kumar's scheme [11]. The proposed AKA scheme additionally utilizes the fuzzy extractor mechanism to improve the security level of the two-factor AKA scheme. Even if two of the three factors are compromised, our AKA scheme is secure. Moreover, our scheme is suitable for resource-limited smart devices in smart home environments because it uses hash and XOR functions that generate low computation overheads.

### A. CONTRIBUTIONS

The main contributions of the proposed AKA scheme are summarized as follows:

- We design a secure and lightweight three-factor based privacy-preserving user authentication scheme in IoT-enabled smart home environments to provide secure home services for legitimate users.
- The proposed AKA scheme resists various security attacks such as impersonation attack, and session key disclosure attack, and also provides the security functionalities such as mutual authentication, anonymity, and privacy.
- We perform formal (simulation) security of the proposed protocol using the Automated Verification of Internet Security Protocols and Applications (AVISPA) [12], [13], which evaluates security against various security attacks. Furthermore, we perform formal (mathematical) security analysis using the Real-or-Random (ROR) model [14] to evaluate the session key security of the proposed AKA scheme.
- We perform a comparative analysis of the proposed protocol and related schemes in terms of security features, computation costs, communication costs, and storage costs.

### B. MOTIVATIONS

The major goal of this paper is to resolve the security weaknesses and inefficient efficiency present in Kaur and Kumar's

scheme [11]. Their scheme does not provide the essential security functionalities such as session key disclosure attack, impersonation attack, and mutual authentication in IoT-enabled smart home environments. In addition, Kaur and Kumar's scheme [11] is not suitable for resource-constrained smart devices because it uses ECC, which generates high computation and communication overheads. These facts motivated us to propose a new secure and lightweight authentication protocol, which can provide the necessary security functionalities and effective efficiency and resolve security flaws that exist in IoT-enabled smart home environments. Thus, the proposed AKA scheme utilizes the fuzzy extractor mechanism to improve the security level of the two-factor AKA scheme and also ensures efficient performance because it utilizes only hash function and XOR operation that generate low computation and communication overheads.

### C. ORGANIZATIONS

The structure of this paper is organized as follows. Section II presents the overview of related works for smart homes and Section III introduces the overview of the preliminaries. In Section IV, we review a detailed overview of Kaur and Kumar's scheme. In Section V and Section VI, we analyze the security flaws of Kaur and Kumar's scheme and proposes a secure and lightweight three-factor based privacy-preserving authentication scheme for IoT-enabled smart homes. Section VII presents the security analyzes of the proposed AKA scheme by using informal and formal security analysis. In Section VIII, we demonstrate the performance comparative analysis of the proposed AKA scheme with the previous schemes. Finally, we conclude this paper in Section IX.

### II. RELATED WORKS

In the last few years, numerous AKA mechanisms have been presented to provide the security and privacy of users in various environments [1], [15]–[18]. In 2008, Jeong *et al.* [19] presented an AKA protocol to provide security in smart home environments using one-time password (OTP) and smart card. Jeong *et al.* [19] were claimed that their protocol ensures security from various security attacks. However, their protocol is vulnerable to potential security attacks such as smart card theft and insider attacks. In addition, their protocol is not provided mutual authentication between gateway and smart device and also is not achieved the untraceability and anonymity as the identity of the legitimate user is transmitted in plaintext over an open channel. Thus, their schemes [19] using smart card and OTP could not resist the various security attacks such as offline password guessing and smart card stolen attacks. In 2011, Vaidya *et al.* [20] presented a secure one-time password based AKA scheme using smart card in smart home environments. However, Kim *et al.* [21] proved that Vaidya *et al.*'s scheme [20] cannot resist offline password guessing attacks and does not ensure forward secrecy with smart card stolen attacks. Kim *et al.* [21] subsequently presented an enhanced AKA scheme to improve the security

weaknesses of the Vaidya *et al.*'s scheme [20]. However, Kim *et al.*'s scheme [21] also fails to ensure user anonymity and untraceability of the smart device and legitimate user. These two-factor based AKA schemes for smart home cannot prevent various security attacks such as offline password guessing and smart card stolen attacks.

In the past few years, many researchers have been proposed symmetric/asymmetric-based AKA schemes for smart homes [22]–[24] to overcome the above-mentioned security flaws. In 2011, Vaidya *et al.* [25] proposed an ECC-based secure and lightweight AKA scheme for smart home networks. However, their scheme [25] suffered from insider, impersonation, and offline password guessing attacks. In 2015, Santoso *et al.* [26] presented a secure AKA scheme using ECC in smart home environments. However, Santoso *et al.*'s scheme [26] is insecure against stolen verifier and insider attacks. In 2019, Shuai *et al.* [10] presented a two-factor based lightweight AKA mechanism for smart home with provable security using ECC. However, Kaur and Kumar [11] proved that Shuai *et al.*'s scheme [10] is insecure against insider, replay, session key disclosure, gateway bypass, and offline password guessing attacks. In 2020, Wazid *et al.* [27] presented the symmetric key cryptography and hash function based efficient AKA scheme for smart homes. However, Lyu *et al.* [28] claimed that Wazid *et al.*'s scheme [27] cannot resist compromised server and desynchronization attacks. These symmetric/asymmetric-based AKA schemes for smart homes are still cannot various security attacks, and also not suitable for the resource-limited smart devices in smart home environments since it requires high computational costs.

In 2021, Kaur and Kumar [11] proposed an enhanced two-factor based AKA scheme in smart home environments to overcome the security problems of Shuai *et al.*'s scheme [10]. They were claimed that their protocol can resist potential security attacks and also guarantees user anonymity, privacy, and mutual authentication. However, we proved that Kaur and Kumar's scheme also is vulnerable to impersonation and session key disclosure attacks, and does not achieve mutual authentication. Moreover, their scheme is not suitable for resource-constrained devices because it utilizes public-key cryptosystems such as ECC. Thus, we design a secure and lightweight three-factor based privacy-preserving AKA scheme for IoT-enabled smart homes to resolve the security flaws Kaur and Kumar's scheme [11].

### III. PRELIMINARIES

We introduce the overview of the preliminaries to enhance the readability of this article.

#### A. THREAT MODEL

This section presents the widely-known Dolev-Yao (DY) model [29] to demonstrate the security of the proposed AKA scheme. In the DY model, the capabilities of a malicious adversary are as follows.

- In this model, a malicious adversary (*MA*) can insert, delete, eavesdrop, replay, modify transmitted messages over an insecure channel.
- If a smart card of the legitimate user is stolen, its secret credentials can be extracted by *MA* using power-analysis attacks [30]–[32].
- The smart devices can be tampered, and physically captured by *MA* in the registration phase. Thus, *MA* can extract the secret credentials stored in its memory [33]–[35].
- *MA* can attempt offline identity and offline password guessing attacks. Thus, *MA* can guess the real identity and password of the legitimate user simultaneously.
- After getting the secret credentials of the smart device and smart card, *MA* may try potential security attacks such as offline guessing, session key disclosure, impersonation, and privileged insider attacks [36], [37].

#### B. FUZZY EXTRACTOR

This section introduces the basic concepts of the fuzzy extractors [38]. The fuzzy extractors are a cryptographic method using user biometric to perform a secure authentication and it consists of the two operations as the generator  $Gen(\cdot)$  and reproduction  $Rep(\cdot)$  which are denoted as follows:

1.  $Gen(\cdot)$ : Given a user's biometric input  $BIO$ ,  $Gen(\cdot)$  selects a biometric secret key  $\gamma_i \in \{0, 1\}^l$  and a public reproduction parameter  $\beta_i \in \{0, 1\}^*$ , which is a probabilistic function.
2.  $Rep(\cdot)$ : Given a noisy biometric input  $BIO$ ,  $Rep(\cdot)$  reproduces  $\gamma_i$  using value  $\beta_i$ , which is public reproduction related with  $BIO$ .

#### C. SYSTEM MODEL

This section introduces the system model for IoT-enabled smart homes in Figure 1. The proposed system model consists of four entities: the registration authority, user, gateway, and smart device. The detailed descriptions of each entity are as follows:

- Registration authority (RA): The registration authority is a trusted authority and is responsible for the registration of participants.
- Gateway: The gateway manages the collected data in smart devices to provide useful home services for legitimate users. In addition, the gateway is a powerful entity and serves as a bridge between the smart device and legitimate user.
- User: The authorized user by the registration authority can access useful home services through the gateway using a portable device at anytime and anywhere.
- Smart Devices: The smart devices (e.g. sensors and things) deployed in smart homes are resource-limited, collect a large amount of real-time data and transmit the collected data to the legitimate user.

### IV. REVIEW OF KAUR AND KUMAR'S SCHEME

We review Kaur and Kumar's scheme [11] for smart homes. Their scheme consists of three phases: 1) initialization,

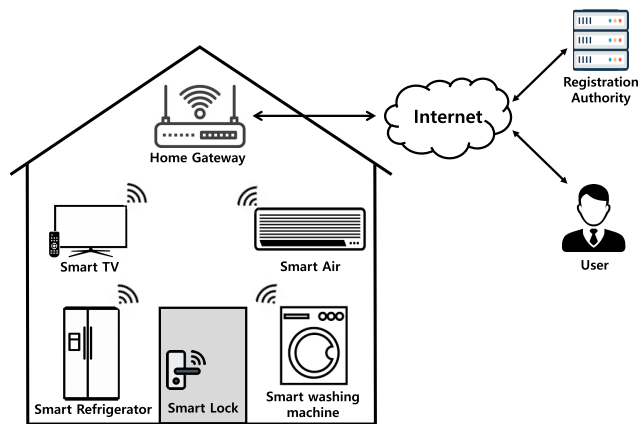


FIGURE 1. System model for IoT-enabled smart homes.

2) registration and 3) mutual authentication. The symbols used in this paper are as shown in Table 1.

TABLE 1. Symbols.

Symbol	Description
$U_i$	User
$SD_j$	Smart device
$GW$	Gateway
$RA$	Registration authority
$ID_i, PW_i$	$U_i$ 's identity and password
$SID_j, GID_i$	Identity of $SD_j$ and $GW_i$
$T_i$	Timestamp
$v$	Fuzzy verifier
$SK$	Session key
$K_G$	$GW$ 's master key
$X_{GU}$	Common secret key between $U_i$ and $GW$
$X_{GS}$	Common secret key between $SD_j$ and $GW$
$h(\cdot)$	Hash function
$\oplus$	XOR operation
$\parallel$	Concatenation operations

## A. INITIALIZATION PHASE

The registration authority  $RA$  performs the initialization tasks as follows:

- **IP-1:**  $RA$  selects an elliptic curve  $E$  on the basic field  $F_p$  and forms an additive group  $AG$  of the order  $p$  generated by  $G$ .
- **IP-2:** After that,  $RA$  generates a private key  $z$  and public key  $PK = z \cdot G$  and also selects a master key  $K_G$  for  $GW$ .
- **IP-3:**  $RA$  stores  $z$  and  $K_G$  in the memory of  $GW$ , and then loads system public parameters  $\{E(F_p), AG, G, PK, h(\cdot)\}$  in  $GW$  and  $SD_j$ , which are publicly known to all  $U_i$ .
- **IP-4:** Finally,  $RA$  selects the identities of  $SD_j$  and also stores it in the memory of  $SD_j$ .

## B. REGISTRATION PHASE

This phase includes the user and smart device registration phases. The detailed descriptions are as below:

### 1) USER REGISTRATION PHASE

$U_i$  performs the following steps with  $RA$  to register in the system.

- **URP-1:**  $U_i$  chooses a  $ID_i$  and a  $PW_i$  and generates a random number  $r$ . After that,  $U_i$  calculates  $RID_i = h(ID_i || r)$ ,  $RPW_i = h(PW_i || r)$ , and transmits it to  $RA$  via a secure channel.
- **URP-2:**  $RA$  verifies whether  $RID_i$  chosen by  $U_i$  is already assigned or not. If it is already assigned  $U_i$  is asked to select a new identity. Otherwise,  $RA$  computes  $X_{GU} = h(RID_i || K_G)$  and  $B_1 = X_{GU} \oplus RPW_i$ . Then,  $RA$  keeps track of number of attempts taken in  $T$  while logging in which initially have the zero value in it.  $RA$  stores the credential  $\{B_1, T\}$  in smart card ( $SC$ ) and transmits it to  $U_i$ .
- **URP-3:**  $U_i$  computes  $B_2 = r \oplus h(ID_i || PW_i)$  and  $B_3 = h(RID_i || RPW_i) \bmod v$  which  $v$  is fuzzy verifier whose value is  $2^4 \leq v \leq 2^8$ . Finally,  $U_i$  stores  $\{B_2, B_3\}$  in memory of smart card.

### 2) SMART DEVICE REGISTRATION PHASE

$SD_j$  performs the following steps with  $RA$  to register in the system.

- **SDRP-1:**  $SD_j$  selects a  $SID_j$  and transmits it to  $RA$  via a secure channel.
- **SDRP-2:**  $RA$  verifies whether  $SID_j$  already assigned to other  $SD_j$  or not. If  $SD_j$  is already assigned registration request is terminated. Otherwise,  $RA$  computes  $X_{GS} = h(SID_j || K_G)$  and transmits it to  $SD_j$ .
- **SDRP-3:** Finally,  $SD_j$  stores  $X_{GS}$  in memory of  $SD_j$ .

## C. MUTUAL AUTHENTICATION PHASE

In this phase,  $U_i$  and  $SD_j$  must establish a common session key with the help of  $GW$  to access secure home services. We describe the detailed mutual authentication phase of Kaur and Kumar's scheme [11] as follows:

- **MAP-1:**  $U_i$  first enters  $ID_i$  and  $PW_i$  and calculates  $r^* = h(ID_i || PW_i) \oplus B_2$ ,  $RPW_i^* = h(PW_i || r^*)$ ,  $RID_i^* = h(ID_i || r^*)$ ,  $B_3^* = h(RID_i^* || RPW_i^*) \bmod v$  and verifies if  $B_3^* \stackrel{?}{=} B_3$ . If the condition is correct,  $U_i$  generates a random numbers  $x_1$  and  $c$ , and selects the identity  $SID_j$  of  $SD_j$  with whom  $U_i$  wants to connect.  $U_i$  calculates  $X_{GU} = RPW_i \oplus B_1$ ,  $B_4 = c \cdot G$ ,  $B_5 = c \cdot PK$ ,  $PID_i = RID_i \oplus B_5$ ,  $N_1 = (x_1 || SID_j) \oplus X_{GU} \oplus T_1$ , and  $W_1 = h(RID_i || x_1 || X_{GU} || N_1)$ . Then,  $U_i$  transmits  $\{PID_i, B_4, N_1, W_1, T_1\}$  to  $GW$  over a public channel.
- **MAP-2:** On getting the messages from  $U_i$ ,  $GW$  computes  $B_5^* = z \cdot B_4$ ,  $RID_i^* = PID_i \oplus B_5^*$ ,  $X_{GU} = h(RID_i^* || K_G)$ ,  $(x_1^* || SID_j) = N_1 \oplus X_{GU} \oplus T_1$ , and  $W_1^* = h(RID_i^* || x_1^* || X_{GU} || N_1)$  and checks if  $W_1^* \stackrel{?}{=} W_1$ . If it is valid,  $GW$  generates a random number  $x_2$  and calculates  $X_{GS} = h(SID_j || K_G)$ ,  $N_2 = X_{GS} \oplus T_2 \oplus (RID_i || GID_i || x_1 || x_2)$ , and  $W_2 = h(RID_i || GID_i || X_{GS} || x_1 || x_2)$ . After that,  $GW$  sends  $\{N_2, W_2, T_2\}$  to  $SD_j$ .
- **MAP-3:**  $SD_j$  computes  $(RID_i || GID_i || x_1 || x_2) = N_2 \oplus X_{GS} \oplus T_2$  and  $W_2^* = h(RID_i || GID_i || X_{GS} || x_1 || x_2)$ , and then checks if  $W_2^* \stackrel{?}{=} W_2$ . If the condition is valid,  $SD_j$

generates a random number  $x_3$  and computes a session key  $SK = h(RID_i||GID_i||SID_j||x_1||x_2||x_3)$ ,  $N_3 = x_3 \oplus X_{GS} \oplus T_3$ , and  $W_3 = h(x_3||X_{GS}||SK)$ . After that,  $SD_j$  transmits  $\{N_3, W_3, T_3\}$  to  $GW$  over a public channel.

- **MAP-4:** On getting the messages from  $SD_j$ ,  $GW$  computes  $x_3 = N_3 \oplus X_{GS} \oplus T_3$ ,  $SK = h(RID_i||GID_i||SID_j||x_1||x_2||x_3)$ , and  $W_3^* = h(x_3||X_{GS}||SK)$ , and verifies if  $W_3^* \stackrel{?}{=} W_3$ . If it is valid,  $GW$  computes  $N_4 = (GID_i||x_2||x_3) \oplus X_{GU} \oplus T_4$  and  $W_4 = h(X_{GU}||SK||x_2||x_3)$ , and then sends  $\{N_4, W_4, T_4\}$  to  $U_i$ .
- **MAP-5:**  $U_i$  computes  $(GID_i||x_2||x_3) = N_4 \oplus X_{GU} \oplus T_4$ ,  $SK = h(r_U||r_{GW}||r_{SD}||RID_i||GID_i||SID_j)$ , and  $W_4^* = h(X_{GU}||SK||x_2||x_3)$  and checks if  $W_4^* \stackrel{?}{=} W_4$ . If it is valid, the mutual authentication between  $U_i$  and  $SD_j$  is successful, and also a common session key is established between them.

## V. CRYPTANALYSIS OF KAUR AND KUMAR'S SCHEME

In this section, we perform the cryptanalysis of Kaur and Kumar's scheme [11]. Kaur and Kumar [11] claimed that their scheme can prevent various security attacks, and also provide mutual authentication. Unfortunately, we prove that their scheme cannot resist potential security attacks such as impersonation and session key disclosure attacks, and also does not ensure mutual authentication.

### A. IMPERSONATION ATTACK

Referring to Section III-A, if  $MA$  captures  $SD_j$ ,  $MA$  can extract the secret parameters  $\{SID_j, X_{GS}\}$  stored in its memory. In addition,  $MA$  can insert, delete, eavesdrop, replay, and modify the exchanged messages over an insecure channel. The detailed descriptions of this attack are as below.

- **Step 1:**  $MA$  computes  $(RID_i||GID_i||x_1||x_2) = N_2 \oplus X_{GS} \oplus T_2$ . Then,  $MA$  generates a new random number  $x_{MA}$ ,  $SK_{MA} = h(RID_i||GID_i||SID_j||x_1||x_2||x_{MA})$ ,  $N_{MA3} = x_{MA} \oplus X_{GS} \oplus T_3$ , and  $W_{MA3} = h(x_{MA}||X_{GS}||SK_{MA})$ . After that,  $MA$  transmits  $\{N_{MA3}, W_{MA3}, T_3\}$  to  $GW$  over a public channel.
- **Step 2:** After obtaining the messages,  $GW$  computes  $x_{MA} = N_{MA3} \oplus X_{GS} \oplus T_3$ ,  $SK = h(RID_i||GID_i||SID_j||x_1||x_2||x_{MA})$ ,  $W_{MA3}^* = h(x_{MA}||X_{GS}||SK_{MA})$ , and checks if  $W_{MA3}^* \stackrel{?}{=} W_{MA3}$ . If the condition is valid,  $GW$  generates a timestamp  $T_4$  and computes  $N_{MA4} = (GID_i||x_2||x_{MA3}) \oplus X_{GU} \oplus T_4$ , and  $W_{MA4} = h(X_{GU}||SK_{MA}||x_2||x_{MA3})$ . Then,  $GW$  sends  $\{N_{MA4}, W_{MA4}, T_4\}$  to  $U_i$ .
- **Step 3:**  $U_i$  computes  $(GID_i||x_2||x_{MA3}) = N_{MA4} \oplus X_{GU} \oplus T_4$ ,  $SK_{MA} = h(RID_i||GID_i||SID_j||x_1||x_2||x_{MA3})$ , and  $W_{MA4}^* = h(X_{GU}||SK_{MA}||x_2||x_{MA3})$ , and verifies if  $W_{MA4}^* \stackrel{?}{=} W_{MA4}$ . If it is correct,  $MA$  impersonate as  $SD_j$  successfully and also shares the common session key  $SK_{MA}$  with  $U_i$  successfully.

### B. SESSION KEY DISCLOSURE ATTACK

In this attack,  $MA$  can calculate a session key  $SK = h(RID_i||GID_i||SID_j||x_1||x_2||x_3)$  between  $U_i$  and  $SD_j$ .

According to Section III-A,  $MA$  can extract the secret parameters  $\{SID_j, X_{GS}\}$  stored in  $SD_j$ . Then,  $MA$  computes  $(RID_i||GID_i||x_1||x_2) = N_2 \oplus X_{GS} \oplus T_2$  and  $x_3 = N_3 \oplus X_{GS} \oplus T_3$ .  $MA$  can calculate a session key  $SK = h(RID_i||GID_i||SID_j||x_1||x_2||x_3)$  successfully. Therefore, Kaur and Kumar's scheme is insecure to session key disclosure attacks.

### C. MUTUAL AUTHENTICATION

Kaur and Kumar claimed that their scheme provides mutual authentication among  $U_i$ ,  $GW$ , and  $SD_j$ . However, according to Section V-A and V-B,  $MA$  can calculate the authentication request message  $W_2 = h(RID_i||GID_i||X_{GS}||x_1||x_2)$  and response message  $W_3 = h(x_3||X_{GS}||SK)$  successfully. Thus, Kaur and Kumar's scheme does not provide a secure mutual authentication.

## VI. PROPOSED SCHEME

We design a secure and lightweight three-factor based privacy-preserving AKA scheme for IoT-enabled smart homes to enhance the security weaknesses of Kaur and Kumar's scheme [11]. The proposed AKA scheme consists of four phases: 1) initialization, 2) registration, 3) mutual authentication, and 4) password and biometric update. The detailed descriptions are as follows:

### A. INITIALIZATION PHASE

In the proposed scheme, the pre-configured during manufacturing production or reconfigured during maintenance, a master key is assumed to be pre-shared in the tamper-resistant memory of the security module such as the trusted platform module (TPM). Before  $GW$  and  $SD_j$  are deployed in smart home environments,  $RA$  first generates a master key  $K_G$  and then stores it in the tamper-resistant memory of  $GW$ .  $SD_j$  chooses a  $SID_j$  and sends it to  $RA$  via a secure channel. Then,  $RA$  checks whether  $SID_j$ . If it is correct,  $RA$  stores it in the tamper-resistant memory of  $GW$  and then generates a master key  $K_{SD}$  of  $SD_j$  and stores it in the tamper-resistant memory of  $SD_j$ .

### B. REGISTRATION PHASE

This phase includes the user and smart device registration phases. The detailed descriptions are as below:

#### 1) USER REGISTRATION PHASE

$U_i$  must register with  $RA$  to access the useful home services.

- **URP-1:**  $U_i$  generates a random number  $a_i$  and enters a unique  $ID_i$  and  $PW_i$ , and imprints biometric  $BIO$ . Then,  $U_i$  computes  $Gen(BIO) = \langle \gamma_i, \beta_i \rangle$ , and  $RID_i = h(ID_i||\gamma_i)$ , and  $RPW_i = h(PW_i||\gamma_i)$  and transmits  $\{RID_i, RPW_i, a_i\}$  to  $RA$  over a secure channel.
- **URP-2:**  $RA$  computes  $X_{GU} = h(RID_i||K_G||a_i)$  and  $A_1 = X_{GU} \oplus h(a_i||RPW_i)$ . Then,  $RA$  sends  $\{X_{GU}\}$  to the  $GW$  via a secure channel. Then,  $GW$  computes  $L_i = h(GID_i||K_G) \oplus X_{GU}$  and stores  $\{L_i\}$  in secure database. Finally,  $RA$  stores  $\{A_1\}$  in the smart card and issues the smart card to  $U_i$  via a secure channel.

- **URP-3:**  $U_i$  computes  $K_i = h(ID_i || PW_i || \gamma_i)$ ,  $A_2 = E_{K_i}(A_1)$ ,  $A_3 = a_i \oplus h(RID_i || RPW_i)$ , and  $A_4 = h(RID_i || RPW_i || a_i)$ . After that,  $U_i$  eliminates  $\{A_1\}$  in the smart card and then stores  $\{A_2, A_3, A_4\}$  in the smart card. As a result, the smart card contains the secret parameters  $\{A_2, A_3, A_4\}$ .

## 2) SMART DEVICE REGISTRATION PHASE

$SD_j$  performs the following steps with  $RA$  to provide the useful home services.

- **SDRP-1:**  $SD_j$  generates a random number  $b_j$  and computes  $PID_j = h(SID_j || b_j)$ . Then,  $SD_j$  transmits  $\{b_j, PID_j\}$  to  $RA$  over a secure channel.
- **SDRP-2:**  $RA$  computes  $X_{GS} = h(PID_j || K_G || b_j)$ . After that,  $RA$  stores  $\{PID_j, b_j\}$  in secure database of  $GW$  and transmits  $\{X_{GS}\}$  to  $SD_j$  via a secure channel.
- **SDRP-3:**  $SD_j$  computes  $B_1 = h(SID_{SD} || K_{SD}) \oplus b_j$  and  $B_2 = h(K_{SD} || b_j) \oplus X_{GS}$ . Finally,  $SD_j$  stores  $\{B_1, B_2\}$  in the memory.

## C. MUTUAL AUTHENTICATION PHASE

The registered  $U_i$  and  $SD_j$  must establish a common session key with the help of  $GW$  to utilize secure home services. Figure 2 shows the mutual authentication phase of the proposed AKA scheme and also the detailed processes are as follows:

- **MAP-1:**  $U_i$  inputs  $ID_i$ ,  $PW_i$  and imprints  $BIO$ . Then,  $U_i$  computes  $\gamma_i = Rep(BIO, \beta_i)$ ,  $RID_i = h(ID_i || \gamma_i)$ ,  $RPW_i = h(PW_i || \gamma_i)$ ,  $K_i = h(ID_i || PW_i || \gamma_i)$ , and retrieves  $\{A_2\}$  in mobile devices. After that,  $U_i$  computes  $A_1 = D_{K_i}(A_2)$ ,  $a_i = A_3 \oplus h(RID_i || RPW_i)$ ,  $X_{GU} = A_1 \oplus h(a_i || RPW_i)$  and  $A_4^* = h(RID_i || RPW_i || a_i)$ , and checks whether  $A_4^* \stackrel{?}{=} A_4$ . If the condition is valid,  $U_i$  generates a random nonce  $r_U$ , and a timestamp  $T_1$ . Then,  $U_i$  selects a identity  $SID_j$  of the  $SD_j$  and computes  $M_1 = (SID_j || r_U) \oplus X_{GU}$ ,  $M_2 = RID_i \oplus h(X_{GU} || r_U)$ , and  $M_{UG} = h(RID_i || X_{GU} || r_U)$ . After that,  $U_i$  transmits  $\{M_1, M_2, M_{UG}\}$  to  $GW$  over a public channel.
- **MAP-2:** After getting the messages from  $U_i$ ,  $GW$  retrieves  $\{L_i\}$  in secure database and computes  $X_{GU} = h(GID_i || K_G) \oplus L_i$ ,  $(SID_j || r_U) = M_1 \oplus X_{GU} \oplus T_1$ ,  $RID_i = M_2 \oplus h(X_{GU} || r_U || T_1)$ , and  $M_{UG}^* = h(RID_i || X_{GU} || r_U || T_1)$ . Then,  $GW_i$  verifies if  $M_{UG}^* \stackrel{?}{=} M_{UG}$ . After that,  $GW$  generates a  $r_{GW}$  and a  $T_2$ . Then,  $GW$  computes  $X_{GS} = h(SID_j || K_G)$ ,  $M_3 = (RID_i || GID_i || r_U || r_{GW}) \oplus h(SID_j || X_{GS} || T_2)$  and  $M_{GS} = h(RID_i || GID_i || X_{GS} || r_U || r_{GW} || T_2)$ . Then,  $GW$  transmits  $\{M_3, M_{GS}, T_2\}$  to  $SD_j$ .
- **MAP-3:** On getting the messages from  $GW$ ,  $SD_j$  retrieves  $\{B_1, B_2\}$  in the memory and computes  $b_j = B_1 \oplus h(PID_j || K_{SD})$ ,  $X_{GS} = B_2 \oplus h(K_{SD} || b_j)$ ,  $(RID_i || GID_i || r_U || r_{GW}) = M_3 \oplus h(SID_j || X_{GS} || T_2)$  and  $M_{GS}^* = h(RID_i || GID_i || X_{GS} || r_U || r_{GW} || T_2)$ , and checks if  $M_{GS}^* \stackrel{?}{=} M_{GS}$ . If it is valid,  $SD_j$  generates a  $r_{SD}$  and  $T_3$ . After that,  $SD_j$  generates a

random nonce  $r_{SD}$  and a timestamp  $T_3$ . Then,  $SD_j$  computes  $M_4 = r_{SD} \oplus h(X_{GS} || RID_i || GID_i || T_3)$ ,  $SK = h(r_U || r_{GW} || r_{SD} || RID_i || GID_i || SID_j)$ , and  $M_{SG} = h(SID_j || r_{SD} || X_{GS} || SK || T_3)$ . Finally,  $SD_j$  transmits  $\{M_4, M_{SG}, T_3\}$  to  $GW$  via a public channel.

- **MAP-4:** After getting the messages from  $SD_j$ ,  $GW$  computes  $r_{SD} = M_4 \oplus h(X_{GS} || RID_i || GID_i || T_3)$ ,  $SK = h(r_U || r_{GW} || r_{SD} || RID_i || GID_i || SID_j)$ ,  $M_{SG}^* = h(SID_j || r_{SD} || X_{GS} || SK || T_3)$ , and checks if  $M_{SG}^* \stackrel{?}{=} M_{SG}$ . If the condition is correct,  $GW$  generates a timestamp  $T_4$  and computes  $M_5 = (GID_i || r_{GW} || r_{SD}) \oplus h(RID_i || X_{GU} || r_U || T_4)$  and  $M_{GU} = h(RID_i || GID_i || r_U || r_{GW} || SK || T_4)$ . Finally,  $GW$  transmits  $\{M_5, M_{GU}, T_4\}$  to  $U_i$ .
- **MAP-5:** On getting the messages from  $GW$ ,  $U_i$  computes  $(GID_i || r_{GW} || r_{SD}) = M_5 \oplus h(RID_i || X_{GU} || r_U || T_4)$ ,  $SK = h(r_U || r_{GW} || r_{SD} || RID_i || GID_i || SID_j)$ , and  $M_{GU}^* = h(RID_i || GID_i || r_U || r_{GW} || SK || T_4)$ , and checks if  $M_{GU}^* \stackrel{?}{=} M_{GU}$ . If it is valid, the mutual authentication between  $U_i$  and  $SD_j$  is successful, and also a common session key is established between them.

## D. PASSWORD AND BIOMETRIC UPDATE PHASE

If an authorized user wants a new password and biometric, and biometric,  $U_i$  can easily update their own old password and old biometric. The detailed descriptions are as follows:

- **PBUP-1:**  $U_i$  first inputs a identity  $ID_i$ , a old password  $PW_i^{old}$ , and imprints a old biometric  $BIO^{old}$ .
- **PBUP-2:** After that,  $SC$  computes  $\gamma_i = Rep(BIO^{old}, \beta_i)$ ,  $RID_i = h(ID_i || \gamma_i)$ ,  $RPW_i^* = h(PW_i^{old} || \gamma_i)$ ,  $K_i = h(ID_i || PW_i^{old} || \gamma_i)$ , and retrieves  $\{A_2\}$  in mobile device. After that,  $SC$  computes  $A_1 = D_{K_i}(A_2)$ ,  $a_i = A_3 \oplus h(RID_i || RPW_i^*)$ ,  $X_{GU} = A_1 \oplus h(a_i || RPW_i^*)$ , and  $A_4^* = h(RID_i || RPW_i^* || a_i)$ , and checks whether  $A_4^* \stackrel{?}{=} A_4$ . If it is not valid,  $SC$  canceled the current session, otherwise  $SC$  requests a new password  $PW_i^{new}$  and a new biometric  $BIO^{new}$  to  $U_i$ .
- **PBUP-3:** Then,  $U_i$  inputs a new password  $PW_i^{new}$  and a new biometric  $BIO^{new}$  in  $SC$ .
- **PBUP-4:** After that,  $SC$  computes  $\gamma_i^{new} = Rep(BIO^{new}, \beta_i^{new})$ ,  $RPW_i^{new} = h(PW_i^{new} || \gamma_i^{new})$ ,  $K_i^{new} = h(ID_i || PW_i^{new} || \gamma_i^{new})$ ,  $A_2^{new} = E_{K_i^{new}}(A_1)$ ,  $A_3^{new} = a_i \oplus h(RID_i^{new} || RPW_i^{new})$ , and  $A_4^{new} = h(RID_i^{new} || RPW_i^{new} || a_i)$ . Finally,  $SC$  replaces  $\{A_2^{new}, A_3^{new}, A_4^{new}\}$  with  $\{A_2, A_3, A_4\}$  in the memory.

## VII. SECURITY ANALYSIS

We assess the security of the proposed AKA scheme by utilizing informal security and formal security analyzes, including ROR model and AVISPA.

### A. INFORMAL SECURITY ANALYSIS

The security of the our scheme is proved by performing the informal security analysis. We demonstrate that our scheme

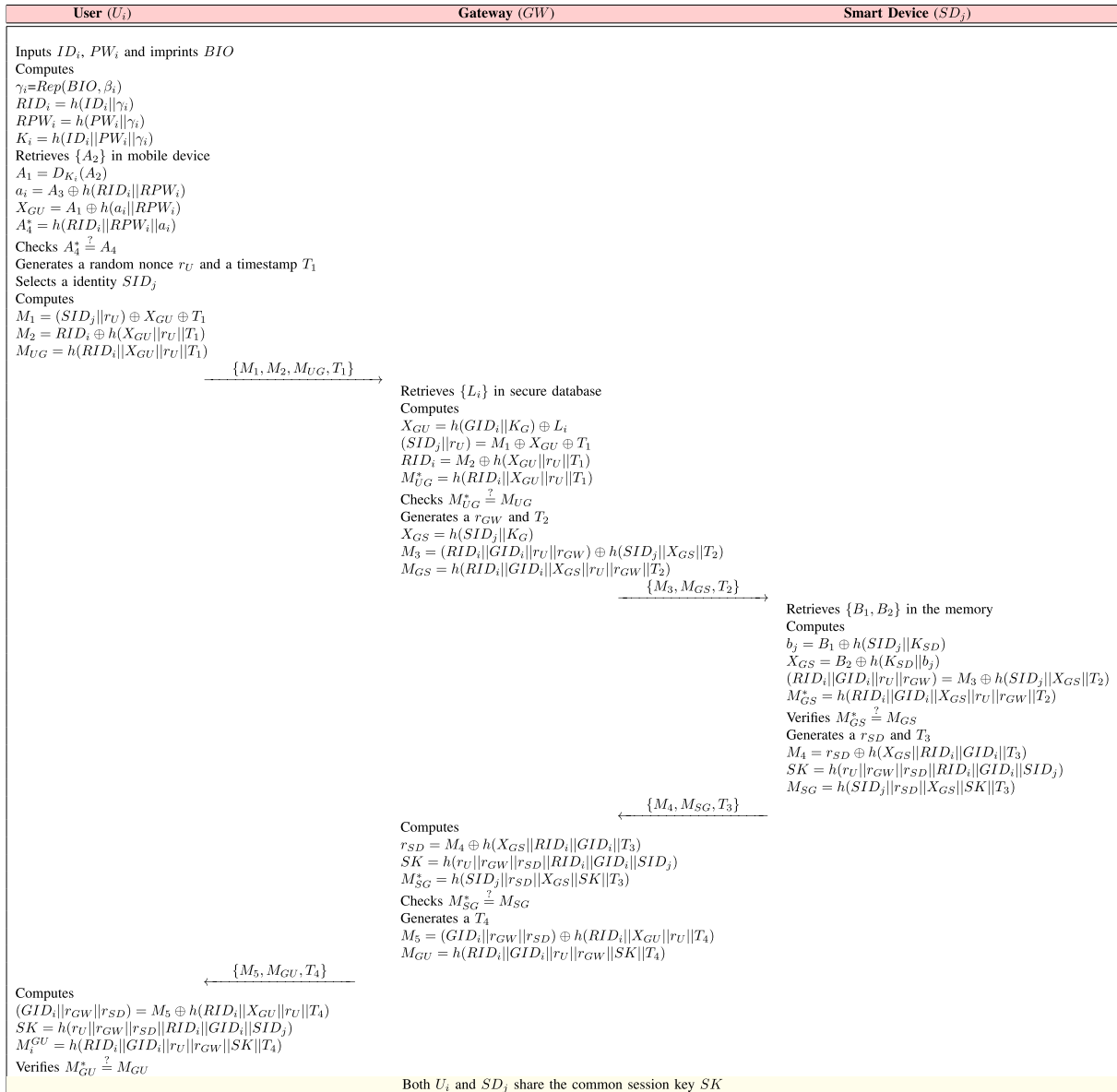


FIGURE 2. Authentication and key agreement phase of our scheme.

can withstand various security attacks, and also ensure user anonymity and mutual authentication.

### 1) IMPERSONATION ATTACK

When  $MA$  wants to masquerade a legal  $U_i$ ,  $MA$  must calculate the authentication request messages  $\{M_1, M_2, M_{UG}, T_1\}$  and response messages  $\{M_5, M_{GU}, T_4\}$ . However, it is difficult to generate the authentication request and response messages because  $MA$  does not know a secret key  $X_{GU}$ , a random nonce  $r_U$ , and a pseudo-identity  $RID_i$ . Therefore, our protocol prevents impersonation attacks since  $MA$  cannot generate the authentication request message and response of the legal user successfully.

### 2) SESSION KEY DISCLOSURE ATTACK

Referring to Section III-A, we assume that  $MA$  can steal the smart card and extract all secret credentials  $\{A_2, A_3, A_4\}$

in the memory. In the proposed AKA scheme,  $MA$  should obtain the random nonces  $\{r_U, r_{GW}, r_{SD}\}$  to generate session key  $SK = h(r_U || r_{GW} || r_{SD} || RID_i || GID_i || SID_j)$  successfully. However,  $MA$  cannot calculate a  $SK$  because  $X_{GU}$  and  $X_{GS}$  are masked with  $GW$ 's master key  $K_G$  and random numbers  $\{a_i, b_j\}$  by using hash function. Moreover, the random nonces  $\{r_U, r_{GW}, r_{SD}\}$  cannot be obtained since  $MA$  does not know the secret keys  $\{X_{GU}, X_{GS}\}$ , Hence, the proposed AKA scheme is resilient against session key disclosure attacks.

### 3) SMART DEVICE CAPTURE ATTACK

Assuming that the smart device is physically captured by  $MA$ ,  $MA$  can extract all secret parameters  $\{B_1, B_2\}$  in the memory, where  $B_1 = h(SID_j || K_{SD}) \oplus b_j$  and  $B_2 = h(K_{SD} || b_j) \oplus X_{GS}$ . However,  $MA$  cannot calculate  $X_{GS}$  without knowing the  $SD$ 's master key  $K_{SD}$ , identity  $SID_j$ , and random number  $b_j$ . And

also,  $MA$  cannot calculate a session key  $SK$  since  $MA$  does not know a  $SD_j$ 's secret key  $X_{GS}$ , a  $GW$ 's master key  $K_G$ , and a  $SD_j$ 's real identity  $SID_j$ . Thus, the proposed AKA scheme is secure against smart device capture attacks.

#### 4) REPLAY ATTACK

Suppose that  $MA$  intercepts all exchanged messages  $\{M_1, M_2, M_{UG}, T_1\}$ ,  $\{M_3, M_{GS}, T_2\}$ ,  $\{M_4, M_{SG}, T_3\}$ , and  $\{M_5, M_{GU}, T_4\}$  in authentication phase. If  $MA$  resends all exchanged messages in the previous session, our scheme checks the validation of the current timestamp. Moreover, all messages are protected with the random nonces  $\{r_U, r_{GW}, r_{SD}\}$  and secret keys  $\{X_{GU}, X_{GS}\}$ . Hence, the proposed AKA scheme is resilient against replay attacks.

#### 5) MAN-IN-THE-MIDDLE (MITM) ATTACK

Assuming that  $MA$  eavesdrops all transmitted messages  $\{M_1, M_2, M_{UG}, T_1\}$ ,  $\{M_3, M_{GS}, T_2\}$ ,  $\{M_4, M_{SG}, T_3\}$ , and  $\{M_5, M_{GU}, T_4\}$ , then MITM attacks may be possible. However,  $MA$  cannot generate the authentication request and response messages since all messages are masked with the secret keys  $\{X_{GU}, X_{GS}\}$ , random nonces  $\{r_U, r_{GW}, r_{SD}\}$ , and identities  $\{RID_i, SID_j, GID_i\}$  using hash function. Therefore, the proposed AKA scheme is secure against MITM attacks.

#### 6) OFFLINE PASSWORD GUESSING ATTACK

Suppose that smart card is stolen or lost,  $MA$  can extract the sensitive information  $\{A_2, A_3, A_4\}$  stored in the memory, where  $A_2 = E_{K_i}(A_1)$ ,  $A_3 = a_i \oplus h(RID_i || RPW_i)$ , and  $A_4 = h(RID_i || RPW_i || a_i)$ . Consequently,  $MA$  is computationally infeasible to derive the real password of the legitimate user from  $\{A_2, A_3, A_4\}$  without the knowledge of  $\gamma_i$  and  $RPW_i$ .

#### 7) PERFECT FORWARD SECRECY

The security for perfect forward secrecy means that the past session key  $SK$  will not be disclosed even if the long-term secret key of communication entities is revealed. However, if  $GW$ 's master key  $K_G$  and  $SD_j$ 's secret key  $K_{SD}$  are compromised,  $MA$  cannot compute the session key  $SK = h(r_U || r_{GW} || r_{SD} || RID_i || GID_i || SID_j)$  without knowledge of  $SID_j$ ,  $b_j$ ,  $X_{GU}$ , and  $X_{GS}$ . Thus, our protocol is resilient to perfect forward secrecy.

#### 8) ANONYMITY AND UNTRACEABILITY

Assuming that  $MA$  intercepts all transmitted messages during AKA phase.  $MA$  is impossible to compute the  $U_i$ 's identity  $ID_i$ , pseudo-identity  $RID_i$ , the  $SD_j$ 's identity  $SID_j$  and pseudo-identity  $PID_j$  without knowing secret credentials  $\{X_{GU}, X_{GS}\}$ . Hence, the proposed scheme provides anonymity for  $U_i$  and  $SD_j$ . Moreover, the timestamps and random nonces are different in any session, that is the transmitted messages in each session are unique and dynamic, so  $MA$  cannot trace  $U_i$  and  $SD_j$  from different sessions. Therefore, the proposed AKA scheme achieves untraceability for  $U_i$  and  $SD_j$ .

TABLE 2. Queries and descriptions.

Queries	Descriptions
$Execute(\mathcal{P}_U^{t_1}, \mathcal{P}_{GW}^{t_2}, \mathcal{P}_{SD}^{t_3})$	Based on <i>Execute</i> query, $MA$ performs the active/passive attacks by eavesdropping all messages between each participants via a public channel.
$CorruptSC(\mathcal{P}_U^{t_1})$	This query is modeled as the smart card stolen attacks, where $MA$ is able to extract the secret parameters stored in $SC$ .
$Send(\mathcal{P}^t, Msg)$	Based on <i>Send</i> query, $MA$ is able to send the message $Msg$ to the $\mathcal{P}^t$ , and also receive the response message accordingly.
$Test(\mathcal{P}^t)$	In this query, an unbiased coin $c$ is tossed prior to starting of the games. If $MA$ obtains the condition $c = 1$ using <i>Test</i> () query, it denotes a $SK$ between $P_U^{t_1}$ and $P_{SD}^{t_2}$ is fresh. If $MA$ gets the condition $c = 0$ , it denotes a $SK$ is not fresh, otherwise $MA$ gets a null value ( $\perp$ ).
$Reveal(\mathcal{P}^t)$	Based on <i>Reveal</i> query, $MA$ reveals a $SK$ established between $P_U^{t_1}$ and $P_{SD}^{t_2}$ .

#### 9) MUTUAL AUTHENTICATION

In our scheme, all parties perform mutual authentication successfully. After obtaining the message  $\{M_1, M_2, M_{UG}, T_1\}$ ,  $GW$  checks  $M_{UG}^* \stackrel{?}{=} M_{UG}$ . If it is valid,  $GW$  authenticates  $U_i$ . Upon getting the message  $\{M_3, M_{GS}, T_2\}$  from  $GW$ , the  $SD_j$  verifies  $M_{GS}^* \stackrel{?}{=} M_{GS}$ . If the condition is equal,  $SD_j$  authenticates  $GW$ . After getting the message  $\{M_4, M_{SG}, T_3\}$ ,  $GW$  checks  $M_{SG}^* \stackrel{?}{=} M_{SG}$ . If it is correct,  $GW$  authenticates  $SD_j$ . Upon obtaining the message  $\{M_5, M_{GU}, T_4\}$  from  $GW$ , the  $U_i$  verifies  $M_{GU}^* \stackrel{?}{=} M_{GU}$ . If the condition is valid,  $U_i$  authenticates  $GW$ . Consequently, all parties in our scheme are mutually authenticated since  $MA$  cannot generate the transmitted authentication messages  $\{M_{UG}, M_{GS}, M_{SG}, M_{GU}\}$  successfully.

### B. FORMAL SECURITY ANALYSIS

The security of the proposed AKA scheme is proved by using formal security analysis such as ROR model and AVISPA simulation.

#### 1) ROR MODEL

This section evaluates a  $SK$  security of the proposed AKA protocol from  $MA$  by performing ROR model [14]. We first briefly introduce the ROR model prior to demonstrate  $SK$  security for our protocol.

In our scheme, there are three participants: the user  $P_U^{t_1}$ , gateway  $P_{GW}^{t_2}$ , and smart device  $P_{SD}^{t_3}$ , where  $P_U^{t_1}$ ,  $P_{GW}^{t_2}$ , and  $P_{SD}^{t_3}$  are instances  $t_1^{th}$  of  $U_i$ ,  $t_2^{th}$  of  $GW_j$ , and  $t_3^{th}$  of  $SD_j$ , respectively. In Table 2, we introduce overviews of each query such as *Execute*(), *CorruptSC*(), *Send*(), *Reveal*(), and *Test*() to perform ROR model. In addition, we use an one-way hash function *Hash* as the random oracle and also utilize Zipf's law [39] to prove  $SK$  security.

**Theorem.**  $Adv_{MA}^{AKA}$  denotes the advantages of  $MA$  in violating  $SK$  security for our protocol. Then, we have the following inequality.

$$Adv_{MA}^{AKA} \leq \frac{q_h^2}{|Hash|} + 2\{C \cdot q_{send}^s, \frac{q_s}{2^b}\}$$



$Hash$ ,  $q_h$ , and  $q_{send}$  are the number of  $Hash$  queries, the range space of the hash function  $h(\cdot)$ , and  $Send()$  query respectively. Furthermore,  $C$ ,  $s$ , and  $l_b$  are the Zipf's parameters [39].

**Proof.** We describe a sequence of four games denoted by  $GM_i$  ( $i = 0, 1, 2, 3$ ) played by  $MA$ . We indicate that  $Adv_{MA,GM_i}^{AKA}$  is the probability of  $MA$  winning the  $GM_i$ . All games are described as follows:

**Game  $GM_0$ :** This game represents the real security attacks executed by  $MA$  against the proposed AKA scheme.  $MA$  must guess a bit  $c$  correctly to win the game. We obtain the following result:

$$Adv_{MA}^{AKA} = |2 \cdot Adv_{MA,GM_0}^{AKA} - 1| \quad (1)$$

- **Game  $GM_1$ :** This game is modeled that  $MA$  simulates eavesdropping attacks in which exchanged messages are intercepted during AKA process performing  $Execute()$ . After getting exchanged messages,  $MA$  performs  $Reveal()$  and  $Test()$  queries to check whether it is a  $SK$  or a random number.  $MA$  needs secret credentials such as  $K_G$ ,  $X_{GU}$ , and  $X_{GS}$  to derive  $SK = h(r_U || r_{GW} || r_{SD} || RID_i || GID_i || SID_j)$ . Hence,  $MA$  does not at all help in increasing the winning probability of this game by intercepting on the exchanged messages. Based on this game, the following is obtained:

$$Adv_{MA,GM_1}^{AKA} = Adv_{MA,GM_0}^{AKA} \quad (2)$$

- **Game  $GM_2$ :** This  $GM_2$  is considered as the active/passive attacks, where simulations of  $Send()$  and  $Hash()$  queries are included. In  $GM_2$ , the  $MA$  is able to intercept all transmitted messages  $\{M_1, M_2, M_{UG}, T_1\}$ ,  $\{M_3, M_{GS}, T_2\}$ ,  $\{M_4, M_{SG}, T_3\}$ , and  $\{M_5, M_{GU}, T_4\}$  during AKA process. However, all exchanged messages are safeguarded utilizing the hash function  $h(\cdot)$ . Furthermore, the random nonces  $r_U$ ,  $r_{GW}$ , and  $r_{SD}$  are not revealed from the exchanged messages since the random nonces are also protected by hash function  $h(\cdot)$ . By applying the birthday paradox, we obtain the following result:

$$|Adv_{MA,GM_2}^{AKA} - Adv_{MA,GM_1}^{AKA}| \leq \frac{q_h^2}{2|Hash|} \quad (3)$$

- **Game  $GM_3$ :** This game is modeled by using  $CorruptSC()$ . In  $GM_3$ , the  $MA$  is able to extract the secret credentials  $\{A_2, A_3, A_4\}$  in the  $SC$  memory using power-analysis attacks. Generally, the legitimate user uses the low-entropy password. Using stored secret credentials  $\{A_2, A_3, A_4\}$  of the  $SC$ ,  $MA$  may attempt to extract the password  $PW_i$  by performing offline password guessing attack. However, in our scheme,  $MA$  cannot obtain the  $PW_i$  of the legitimate user correctly via  $Send()$  query without the biometric information  $\gamma_i$  and secret credential  $RPW_i$ . Moreover, the probability of guessing the  $l_b$  bits of the biometric secret key  $b_i$  is approximately  $\frac{1}{2^{l_b}}$ . Hence,  $GM_2$  and  $GM_3$  are indistinguishable if the offline

password/biometric guessing attacks are not present. Based on this game, the following is obtained:

$$|Adv_{MA,GM_3}^{AKA} - Adv_{MA,GM_2}^{AKA}| \leq \{C \cdot q_{send}^s, \frac{q_s}{2^{l_b}}\} \quad (4)$$

After  $GM_{0-3}$  are played successfully,  $MA$  tries to guess the correct bit  $c$  to win the game by using  $Test()$ . Therefore, we obtain the following result:

$$Adv_{MA,GM_3}^{AKA} = \frac{1}{2} \quad (5)$$

By applying Eq. (1), (2) and (5), we get the following result:

$$\begin{aligned} \frac{1}{2} Adv_{MA}^{AKA} &= |Adv_{MA,GM_0}^{AKA} - \frac{1}{2}| \\ &= |Adv_{MA,GM_1}^{AKA} - \frac{1}{2}| \\ &= |Adv_{MA,GM_1}^{AKA} - Adv_{MA,GM_3}^{AKA}| \end{aligned} \quad (6)$$

By applying Eq. (4), (5) and (6), we obtain the following result using the triangular inequality:

$$\begin{aligned} \frac{1}{2} Adv_{MA}^{AKP} &= |Adv_{MA,GM_1}^{AKP} - Adv_{MA,GM_3}^{AKP}| \\ &\leq |Adv_{MA,GM_1}^{AKP} - Adv_{MA,GM_2}^{AKP}| \\ &\quad + |Adv_{MA,GM_2}^{AKP} - Adv_{MA,GM_3}^{AKP}| \\ &\leq \frac{q_h^2}{2|Hash|} + \{C \cdot q_{send}^s, \frac{q_s}{2^{l_b}}\}. \end{aligned} \quad (7)$$

Multiplying both sides of Eq. (7) by the factor of two, the following result is obtained:

$$Adv_{MA}^{AKA} \leq \frac{q_h^2}{|Hash|} + 2\{C \cdot q_{send}^s, \frac{q_s}{2^{l_b}}\}$$

## 2) AVISPA SIMULATION

In the past few years, numerous studies using AVISPA simulation have been proposed [40]–[42]. AVISPA simulation is a role-based security validation tool that demonstrates whether the authentication protocol is secure against potential security attacks based on DY model [29]. This simulation mechanism is implemented using High-Level Protocol Specification Language (HLPSL) [43] to generate input format (IF) of the back-ends, including Constraint Logic-based Attack Searcher (CL-AtSE), SAT-based Model Checker (SATMC), Tree Automata based on Automatic Approximations for Analysis of Security Protocol (TA4SP), and On-the-Fly Model Checker (OFMC). IF is provided as the input to one of the four back-ends, which produces the output format (OF). In addition, OF indicates the security of the proposed AKA scheme.

To analyze the security of the AKA scheme, we express based on a rule-oriented HLPSL. The detailed HLPSL specifications for AVISPA can be found in [12], [13]. The specification roles for the user  $U_i$ , the gateway  $GW$ , and the smart device  $SD$ , and the mandatory roles for the environments, sessions, and security goals are implemented in HLPSL. Because XOR operations are not supported for

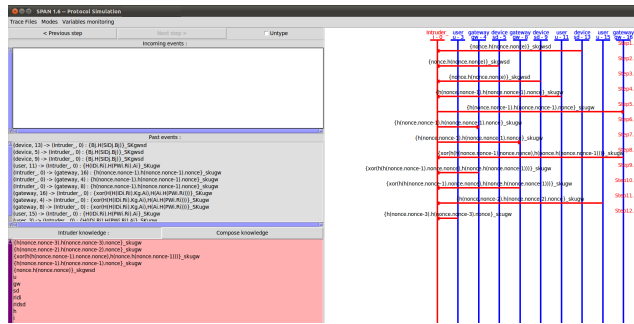


FIGURE 3. AVISPA results using SPAN.

<p><b>SUMMARY</b> SAFE</p> <p><b>DETAILS</b> BOUNDED_NUMBER_OF_SESSIONS PROTOCOL</p> <p>/home/span/span/testsuite/results/AVISPA_sjyu.if</p> <p><b>GOAL</b> As_Specified</p> <p><b>BACKEND</b> OFMC</p> <p><b>COMMENTS</b> STATISTICS parseTime: 0.00s searchTime: 1.30s visitedNodes: 1040 nodes depth: 9 plies</p>	<p><b>SUMMARY</b> SAFE</p> <p><b>DETAILS</b> BOUNDED_NUMBER_OF_SESSIONS TYPED_MODEL PROTOCOL</p> <p>/home/span/span/testsuite/results/AVISPA_sjyu.if</p> <p><b>GOAL</b> As_Specified</p> <p><b>BACKEND</b> CL-AtSe</p> <p><b>STATISTICS</b> Analysed : 63 states Reachable : 63 states Translation: 0.03 seconds Computation : 0.01 seconds</p>
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FIGURE 4. AVISPA results using OFMC and CL-AtSe.

TA4SP and SATMC back-ends, AVISPA simulation results for two back-ends are not included. We simulate the proposed AKA scheme using the Security Protocol ANimator (SPAN) as shown in Figure 3. In addition, we demonstrate that our scheme resists replay and MITM attacks using OFMC and CL-AtSe back-ends as shown in Figure 4.

### VIII. PERFORMANCE ANALYSIS

This section analyzes the comparative analysis of our scheme with the related schemes [10], [11], [27] in terms of the computation, communication, and storage costs, and security features.

#### A. COMPUTATION COSTS

We evaluate the computation costs of the proposed AKA with related schemes [10], [11], [27] in terms of  $MU_i$ ,  $GW$ , and  $SD_j$  during AKA process. According to [11], [44], the execution times of each operation are acquired based on a desktop

TABLE 3. A comparative summary: computation costs.

Schemes	User	Gateway (GW)	Smart device (SD)	Total costs	Execution times
Shuai <i>et al.</i> [10]	$6T_h + 2T_{ecc}$	$7T_h + T_{ecc}$	$3T_h$	$16T_h + 3T_{ecc}$	1.366 ms
Wazid <i>et al.</i> [27]	$11T_h + T_{ed} + T_{fe}$	$11T_h + 2T_{ed}$	$7T_h + T_{ed}$	$29T_h + 4T_{ed} + T_{fe}$	0.6644 ms
Kaur and Kumar [11]	$6T_h + 2T_{ecc}$	$7T_h + T_{ecc}$	$3T_h$	$16T_h + 3T_{ecc}$	1.366 ms
Our scheme	$11T_h + T_{fe} + T_{ed}$	$11T_h$	$7T_h$	$29T_h + T_{fe} + T_{ed}$	0.5999 ms

TABLE 4. A comparative summary: communication costs.

Nodes	Shuai <i>et al.</i> [10]	Wazid <i>et al.</i> [27]	Kaur and Kumar [11]	Our scheme
User to GW	768 bits	480 bits	800 bits	512 bits
GW to SD	320 bits	448 bits	352 bits	352 bits
SD to GW	320 bits	512 bits	352 bits	352 bits
GW to user	320 bits	828 bits	352 bits	352 bits
<b>Total costs</b>	1728 bits	2268 bits	1856 bits	1568 bits

with a Windows 8 Intel(R) Core TM I7-4710HQ 2.50 GHZ, 8 GB Memory. Moreover, the software development environment was implemented using Visual C++ 2010, MIRACL C/C++ Library. We denote the execution times of the following parameters based on [44].  $T_{ed}$ ,  $T_{ecc}$ , and  $T_h$  denote the execution times for symmetric encryption/decryption ( $\approx 0.0215$  ms), ECC point multiplication ( $\approx 0.4276$  ms), and hash function ( $\approx 0.0052$  ms), respectively. Moreover, It is also assumed that the execution time for fuzzy extractor  $T_{fe}$  is equal to  $T_{ecc}$  presented in [11]. In Table 3, we show the comparison results of the computation overhead and execution times between the proposed AKA scheme and those of related schemes. Consequently, our protocol has the lowest computation overhead of those compared with the previous schemes [10], [11], [27].

#### B. COMMUNICATION COSTS

We analyze the communication costs of the proposed AKA with previous schemes [10], [11], [27] during AKA process. We assume the communication costs of the following parameters based on Shuai *et al.*'s scheme [10]. The length of timestamp, random nonce, secret key, hash function, message authentication code, identity, pseudo-identity, symmetric encryption/decryption, and ECC point multiplication are as 32 bits, 160 bits, 160 bits, 160 bits, 160 bits, 128 bits, 128 bits, 256 bits, and 320 bits, respectively. In Table 4, we show the comparison results of the communication cost between the proposed scheme and previous schemes. Consequently, the proposed AKA scheme provides a superior communication cost compared with the related schemes [10], [11], [27].

#### C. STORAGE COSTS

We compare the storage costs for the basis of bytes stored in smart card of the proposed AKA and related schemes [10], [11], [27]. We assume the storage costs of the following parameters. We assume that the bits for the length of the secret parameters presented in Section VIII-B are equal to the storage costs. Table 5 presents the comparison results of the storage cost between the proposed scheme and previous schemes. Although the storage cost of the proposed AKA is somewhat higher than Kaur and Kumar [11], it ensures

**TABLE 5. A comparative summary: storage costs.**

Schemes	Storage costs
Shuai et al. [10]	512 bits
Wazid et al. [27]	640 bits
Kaur and Kumar [11]	384 bits
Our scheme	480 bits

**TABLE 6. A comparative summary: security features.**

Feature	Shuai et al. [10]	Wazid et al. [27]	Kaur and Kumar [11]	Our scheme
$SFT_1$	×	×	○	○
$SFT_2$	×	○	○	○
$SFT_3$	×	○	○	○
$SFT_4$	○	○	×	○
$SFT_5$	×	○	○	○
$SFT_6$	×	○	×	○
$SFT_7$	×	○	○	○
$SFT_8$	○	○	×	○
$SFT_9$	×	○	○	○
$SFT_{10}$	○	○	○	○
$SFT_{11}$	○	○	○	○

○: Resistance of security features; ×: Non-resistance of security features;  $SFT_1$ : Replay attack;  $SFT_2$ : Offline password guessing attack;  $SFT_3$ : Gateway bypass attack;  $SFT_4$ : User impersonation attack;  $SFT_5$ : User device stolen attack;  $SFT_6$ : Session key disclosure attack;  $SFT_7$ : Insider attack;  $SFT_8$ : Mutual authentication;  $SFT_9$ : User anonymity;  $SFT_{10}$ : User untraceability;  $SFT_{11}$ : Perfect forward secrecy.

superior security, computation cost, and communication cost than other related schemes [10], [27].

#### D. SECURITY FEATURES

This section evaluates the security features of the proposed AKA scheme compared to previous schemes [10], [11], [27]. Table 6 shows that previous schemes suffer from various security attacks, including offline password guessing, replay, and impersonation attacks, and so on, and also does not provide mutual authentication and user anonymity. In contrast, the proposed AKA scheme resists various security attacks, and also provides forward secrecy, mutual authentication, and user anonymity. Hence, the proposed AKA scheme offers more security and functionality features compared with previous schemes [10], [11], [27].

#### IX. CONCLUSION

We proved that Kaur and Kumar et al.'s scheme is insecure to various security attacks such as impersonation and session key disclosure attacks, and also does not ensure mutual authentication. We design a lightweight three-factor based privacy-preserving authentication scheme for IoT-enabled smart homes to overcome the security flaws of Kaur and Kumar et al.'s scheme. We demonstrated that the proposed AKA scheme resists various security threats, and also allows user anonymity, untraceability, and mutual authentication. We then proved using well-known accepted AVISPA simulation and ROR model that the proposed AKA scheme is secure against various security attacks. Moreover, we compared the computation, communication, and storage costs of the proposed AKA scheme with other related schemes. Thus, the proposed AKA scheme improved security and privacy, and also ensured the low computation, communication, and storage costs compared with the other related schemes using only fuzzy extractor, hash, and XOR functions, which generate low computation and communication costs. Our scheme

is suitable for IoT-enabled smart home environments because it is more secure and lightweight than existing schemes.

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