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# Magnetic Field Prediction of Module-Combined Stator Permanent Magnet Synchronous Motor Based on a Nonlinear Hybrid Analytical Model

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**ABSTRACT** Module-combined stator permanent-magnet machines have several independent stator modules and each module can be controlled independently. To predict the magnetic field distribution of module-combined stator permanent-magnet machines accurately under asymmetric conditions, this paper proposes a novel nonlinear subdomain and magnetic equivalent circuit hybrid analytical model. The main novelty of the proposed nonlinear hybrid analytical model is representing nonlinear effect by equivalent current sheets on the edges of slots. Equivalent current densities are calculated from magnetic equivalent circuit and used as boundary conditions in the improved subdomain model. The values of the equivalent current sheets are obtained in an iterative algorithm. The nonlinear hybrid analytical model considering saturation effect can accurately calculate magnetic field distribution and electromagnetic performance even under overload conditions. The finite element analysis is performed to validate the accuracy of the proposed hybrid analytical model. A prototype with three stator modules is manufactured and the experimental results verified these predictions.

**INDEX TERMS** Magnetic field prediction, saturation effect, hybrid analytical model, module-combined stator, permanent magnet motor.

#### I. INTRODUCTION

Permanent magnet synchronous machines (PMSM) are widely used in many applications due to high efficiency and torque density. In some applications, higher reliability and fault tolerance of machines are required, such as railway traction drive, wind power generation, compressor application and electric aircraft [1]–[4]. Traditional permanent magnet machines do not have the ability of fault tolerance.

This article proposes a novel module-combined stator permanent magnet machine, which is consisted of several sector-shaped stator modules [5], [6]. The windings in each stator module have two kinds of span, which realize the independence of each module. Each stator module has its own independent inverter. Compared with conventional permanent magnet machines, module-combined stator permanent-magnet machines have better fault tolerance ability and are suitable for the applications that require higher reliability. When one stator module or its inverter fails to

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operate, the other modules can be in operation normally. In order to ensure the output torque unchanged, current in the wingdings of healthy modules should be increased. Then healthy modules operate under overload conditions, which will cause stator core seriously saturated. It is very important to predict magnetic field distribution accurately for analyzing the electromagnetic performances of module-combined stator permanent-magnet machines under asymmetric conditions.

There are four methods, FEA, analytical, magnetic equivalent circuit, hybrid method, to predict magnetic field distribution. FEA can predict magnetic field distribution accurately by considering saturation effect and the complex geometric models of machines [7], [8]. It is very time-consuming and the accuracy is depended on the quality of mesh. It cannot obtain results effectively with parameter variables, so it is not suitable for initial design of machines. Analytical method is an effective method to analyze the electromagnetic performances of machines. The conformal mapping method represents permanent magnet by equivalent current densities, and slotting effect is introduced by relative permeance function of air-gap [9], [10]. The subdomain model divides the whole machine into several solving regions. By applying interface and boundary conditions, the subdomain model solves the governing functions of each region and obtains all harmonic coefficient [11]–[13]. However, the disadvantage of the subdomain model is that it assumes that the core permeability is infinite and neglect the saturation effect. In [14], the relative permeability of core was taken into account in the analytical model, but permanent magnet is not considered. Magnetic equivalent circuit method can calculate the performance considering saturation effect. The whole motor is equivalent to a magnetic network which is composed of nonlinear reluctances with regular shape [15]–[17]. The accuracy of magnetic equivalent circuit method is poor compared with other analytical methods.

Some hybrid analytical models which combine conventional analytical methods and magnetic equivalent circuit method were presented. The hybrid models have the advantage of two methods. There are hybrid analytical models are based on the conformal mapping method [18]–[20]. However, these hybrid models cannot calculate slot leakage accurately. A hybrid model in [21] combines subdomain model and magnetic circuit model, however, the magnetic field in stator slots is predicted by the magnetic equivalent circuit method of the hybrid model, which cannot meet the precision. Subdomain and magnetic circuit hybrid model was proposed in [22] for open-circuit prediction, the magnetic field distribution is calculated based on the improved subdomain method of the proposed hybrid model. On-load magnetic field of permanent magnet machine was analyzed based on the hybrid model in [23]. However, the electromagnetic performances of permanent magnet machines under asymmetric conditions were not analyzed.

In this paper, the structure and power supply mode of the module-combined stator permanent-magnet machines is introduced. A nonlinear subdomain and magnet equivalent circuit hybrid analytical model is proposed for magnetic field distribution and electromagnetic performance prediction in module-combined stator permanent-magnet machines. The magnetic potential drop of nonlinear stator core can be represented by equivalent current densities on the edges of slots. Therefore, the nonlinear analytical model can be transformed to linear analytical model with equivalent current densities on the boundary of the slots. Equivalent current densities are obtained by magnetic equivalent circuit and used as boundary conditions in the improved subdomain model, and the flux sources flowing to the magnetic equivalent circuit are obtained by the improved subdomain model. The values of the equivalent current sheets are obtained in an iterative algorithm. According to the nonlinear magnetization curve of the core material, the relative permeability distribution of stator core at any time can be obtained. The nonlinear hybrid analytical model can accurately calculate air gap flux density, back EMF and electromagnetic torque. The electromagnetic characteristics of module-combined stator permanent magnet motor under asymmetric conditions are mainly analyzed.

The finite element analysis is performed and a prototype is manufactured, the results of the proposed nonlinear hybrid analytical model show a good agreement with finite element results and experimental results.

### **II. MODULE-COMBINED STATOR**

### A. STATOR MODULE STRUCTURE

The stator of traditional permanent magnet machine is manufactured as a whole, which cannot be achieved modularization. The stator of module-combined stator permanent magnet machine is made into several sector modules and all modules are assembled. The stator structure of module-combined stator permanent magnet machine is shown in Fig. 1.



FIGURE 1. Structure of stator.

### **B. WINDING CONNECTION**

The large and small span hybrid windings were introduced in each stator module. The independence of each stator module is achieved by the combination of the two unequal span windings. Compared with the traditional winding, the change is only the end wingding connection, the section in stator slot of winding is not changed. The diagram of wingding connection is shown in Fig. 2.



FIGURE 2. Winding connection of module stator.

The windings in each module are not connected to the wingdings in other modules. Each stator module is controlled independently by its own inverter. When one stator module or inverter fails, the other modules can continue to operate. The novel module-combined stator permanent magnet machines have good ability of fault tolerance.

### **III. HYBRID ANALYTICAL MODEL**

### A. EQUIVALENCE OF ANALYTICAL MODELS

The principle that the saturation effect of stator core is considered in the analytical model is that the magnetic potential generated by the equivalent current on the boundary of the linear core is equal to the magnetic potential drop on the nonlinear stator core. Then, the nonlinear analytical model is equivalent to linear analytical by applying equivalent current densities on the slot edges. The saturation level of rotor yoke is usually not high. Therefore, equivalent current densities are only used on the boundaries of stator slot. The nonlinear analytical model and the equivalent linear analytical model are shown in Fig. 3.



FIGURE 3. Equivalence of the two analytical models: (a) Nonlinear model; (b) Linear model with equivalent current sheets.

In Fig. 3,  $\alpha_i$  is the center angle of the *i*th slot,  $b_{sa}$  is the angle of slot width,  $R_{sb}$ ,  $R_s$ ,  $R_m$  and  $R_r$  are the radius of slot bottom, slot opening, permanent magnet, rotor yoke, respectively,  $J_{i1}$ ,  $J_{i2}$ ,  $J_{i3}$  are the equivalent current densities on the *i*th stator slot edges,  $\mu_0$  and  $\mu_r$  are the permeability of vacuum and stator core, respectively.

The nonoverlapping wingding layout is shown in Fig. 4.  $J_{ami1}$  and  $J_{ami2}$  are the current densities of the windings on both sides of the *i*th slot, *d* is the width of one winding side.



FIGURE 4. Winding layout.

### **B. IMPROVED SUBDOMAIN MODEL**

The improved subdomain model is transformed to a linear model with equivalent current sheets on slot edges. Compared with traditional subdomain model, the boundaries conditions on slot edges in the improved subdomain model are not zero, they are replaced by equivalent current densities. The permeability of the core in the improved subdomain model is infinite, which is the same as the assumption of the traditional subdomain model. The basic assumptions of traditional subdomain model are applicable to improved subdomain model. The boundaries conditions on slot edges are modified to equivalent current densities, the analytical expressions have to be deduced.

### 1) MAGNETIC FIELD DISTRIBUTION IN SLOTS

The boundaries conditions on the *i*th slot edges are

$$H_{3ri}\Big|_{\alpha=\alpha_i+b_{sa}/2} = J_{i1} \tag{1}$$

$$H_{3ri}\Big|_{\alpha=\alpha_i-b_{sa}/2} = -J_{i2} \tag{2}$$

$$H_{3\alpha i}\big|_{r=R_{sh}} = -J_{i3} \tag{3}$$

The vector potential in stator slot region satisfies Laplace equation. The general solution for nonoverlapping winding in slot is

$$A_{z3i}(r,\alpha) = A_{z3i0} + \sum_{n} A_{z3in} \cos \left[ E_n \left( \alpha + b_{sa}/2 - \alpha_i \right) \right]$$
(4)

where

$$A_{z3in} = \left(B_{3n}G_3 - \frac{E_n W_n R_{sb}}{1 - E_n^2} - \frac{2\mu_0 J_{amn} R_{sb}^2}{E_n \left(E_n^2 - 4\right)}\right) \left(\frac{r}{R_{sb}}\right)^{E_n} + B_{3n} \left(\frac{r}{R_s}\right)^{-E_n} + \frac{rE_n^2 W_n}{1 - E_n^2} + \frac{\mu_0 J_{amn} r^2}{E_n^2 - 4}$$
(5)

$$A_{z3i0} = \mu_0 J_{am0} \left( 2R_{sb}^2 \ln r - r^2 \right) / 4 + C_i \ln r - \mu_0 \left( J_{i1} + J_{i2} \right) r / b_{sa} + Q_{3i}$$
(6)  
$$W_n = 2\mu_0 \{ - \left( J_{i1} + J_{i2} \right) \left( -1 \right)^n$$

(11)

$$+J_{i2}[(-1)^n - 1]\}/\left(E_n^2 b_{sa}\right)$$
(7)

$$C_{i} = R_{sb} \left[ \mu_{0} J_{i3} + \mu_{0} \left( J_{i1} + J_{i2} \right) / b_{sa} \right]$$
(8)

$$J_{iam0} = (J_{iam1} + J_{iam2})/2$$
(9)

$$J_{iamn} = 2 (J_{iam1} - J_{iam2}) \sin(npi/2) / (npi)$$
(10)

$$E_n = npi/b_{sa}$$

$$G_3 = (R_s/R_{sb})^{E_n} \tag{12}$$

where  $Q_{3i}$  and  $B_{3n}$  are the undetermined constants

Then, the radial and circumferential flux densities in slot region can be obtained by

$$B_{3ir}(r,\alpha) = \sum_{n} B_{3irn} \sin \left[ E_n \left( \alpha + b_{sa}/2 - \alpha_i \right) \right]$$
(13)

$$B_{3i\alpha}(r,\alpha) = B_{3i\alpha0} + \sum_{n} B_{3i\alpha n} \cos\left[E_n\left(\alpha + b_{sa}/2 - \alpha_i\right)\right]$$
(14)

where

$$B_{3irn} = -E_n \left\{ \frac{E_n^2 W_n}{1 - E_n^2} + \frac{\mu_0 J_{amn} r}{E_n^2 - 4} + \frac{B_{3n}}{R_s} \left(\frac{r}{R_s}\right)^{-E_n - 1} + \left[\frac{B_{3n} G_3}{R_{sb}} + \frac{E_n W_n}{1 - E_n^2} - \frac{2\mu_0 J_{amn} R_{sb}}{E_n \left(E_n^2 - 4\right)}\right] \times \left(\frac{r}{R_{sb}}\right)^{E_n - 1} \right\}$$
(15)

$$B_{3i\alpha n} = -\left[ \left( \frac{B_{3n}E_nG_3}{R_{sb}} - \frac{E_n^2W_n}{1 - E_n^2} - \frac{2\mu_0 J_{amn}R_{sb}}{(E_n^2 - 4)} \right) \times \left( \frac{r}{R_{sb}} \right)^{E_n - 1} - \frac{B_{3n}E_n}{R_s} \left( \frac{r}{R_s} \right)^{-E_n - 1} \frac{E_n^2W_n}{1 - E_n^2} + \frac{2\mu_0 J_{amn}r}{E_n^2 - 4} \right]$$
(16)

$$B_{3i\alpha0} = -\frac{\mu_0 J_{am0} \left(R_{sb}^2/r - r\right)}{2} - \frac{C_i}{r} + \frac{\mu_0 \left(J_{i1} + J_{i2}\right)}{b_{sa}} \quad (17)$$

## 2) MAGNETIC FIELD DISTRIBUTION IN MAGNET AND AIR-GAP

The solving process for magnetic field distributions in permanent magnetic and air-gap region are the same as traditional subdomain model. The detailed derivation process for the two regions is omitted in this article. The detailed derivation process and all coefficients can be found in [12].

The general solution in permanent magnetic and air-gap are

$$A_{z1} = \sum_{k} (C_{1k}A_1 + C_{2k}M_{\alpha ck} - C_{3k}M_{rsk})\cos(k\alpha) + \sum_{k} (C_{1k}C_1 + C_{2k}M_{\alpha sk} - C_{3k}M_{rck})\sin(k\alpha) \quad (18)$$

$$A_{z2} = \sum_{k} \left[ A_2(r/R_s)^k + B_2(r/R_m)^{-k} \right] \cos(k\alpha) + \sum_{k} \left[ C_2(r/R_s)^k + D_2(r/R_m)^{-k} \right] \sin(k\alpha)$$
(19)

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The radial flux densities in permanent magnetic and air-gap are

$$B_{1r} = -\sum_{k} (k/r) \cdot (C_{1k}A_1 + C_{2k}M_{\alpha ck} - C_{3k}M_{rsk})\sin(k\alpha) + \sum_{k} (k/r) \cdot (C_{1k}C_1 + C_{2k}M_{\alpha sk} - C_{3k}M_{rck})\cos(k\alpha)$$
(20)

$$B_{2r} = -\sum_{k} (k/r) \cdot \left[ A_2(r/R_s)^k + B_2(r/R_m)^{-k} \right] \sin(k\alpha) + \sum_{k} (k/r) \cdot \left[ C_2(r/R_s)^k + D_2(r/R_m)^{-k} \right] \cos(k\alpha)$$
(21)

The circumferential flux densities in permanent magnetic and air-gap are

$$B_{1\alpha} = -\sum_{k} (1/r) \cdot (C_{4k}A_1 + C_{5k}M_{\alpha ck} - C_{6k}M_{rsk}) \cos(k\alpha) - \sum_{k} (1/r) \cdot (C_{4k}C_1 + C_{5k}M_{\alpha sk} - C_{6k}M_{rck}) \sin(k\alpha)$$
(22)

$$B_{2\alpha} = -\sum_{k} (k/r) \cdot \left[ A_2 (r/R_s)^k - B_2 (r/R_m)^{-k} \right] \cos(k\alpha) + -\sum_{k} (k/r) \cdot \left[ C_2 (r/R_s)^k - D_2 (r/R_m)^{-k} \right] \sin(k\alpha)$$
(23)

where  $A_1$ ,  $C_1$ ,  $A_2$ ,  $B_2$ ,  $C_2$  and  $D_2$  are undetermined coefficients.  $C_{1 k}$ ,  $C_{2 k}$ ,  $C_{3 k}$ ,  $C_{4 k}$ ,  $C_{5 k}$ ,  $C_{6 k}$ ,  $M_{\alpha sk}$ ,  $M_{\alpha ck}$ ,  $M_{rsk}$  and  $M_{rck}$  are known coefficients.

### 3) INTERFACE CONDITIONS

The interface and boundary conditions of all solving regions are

$$A_{z1}(R_m,\alpha) = A_{z2}(R_m,\alpha)$$
(24)

$$A_{z2}(R_s,\alpha) = A_{z3i}(R_s,\alpha) \tag{25}$$

$$H_{1\alpha}(R_m,\alpha) = H_{2\alpha}(R_m,\alpha)$$
(26)

$$H_{2\alpha}(R_s,\alpha) = H_{3\alpha i}(R_s,\alpha) \tag{27}$$

$$H_{1\alpha}\left(R_r,\alpha\right) = 0 \tag{28}$$

All undetermined coefficients can be obtained by applying these interface and boundary conditions.

### C. MEC CONSIDERING SATURATION EFFECT

After the general solutions considering equivalent current sheets of all regions are obtained, it is necessary to accurately calculate current densities. The equivalent magnetic circuit of stator is shown in Fig. 5. The number of equivalent permeances in each stator tooth and yoke can be selected respectively according to the degree of nonlinearity effect.

The flux flowing into the nodes of equivalent magnetic circuit in Fig. 5 can be calculated from radial and circumferential flux densities in stator slot and air-gap by the improved



FIGURE 5. Magnetic equivalent circuit in stator slot.

subdomain analytical model

$$\phi_{sti} = R_s l_{ef} \int_{\alpha_i - \tau_t/2}^{\alpha_i - b_{sa}/2} B_{2r}(\alpha, R_s, t) d\alpha$$
(29)

$$\phi_{syi} = R_{sb} l_{ef} \int_{\alpha_i - b_{sa}/2}^{\alpha_i + b_{sa}/2} B_{3r}(\alpha, R_s, t) d\alpha \qquad (30)$$

$$\phi_{ss2i} = l_{ef} \int_{(R_{sb}+R_s)/2}^{R_{sb}} B_{3\alpha} (\alpha_i + b_{sa}/2, r, t) dr$$
(31)

$$\phi_{ss(2i-1)} = -l_{ef} \int_{(R_{sb}+R_s)/2}^{R_{sb}} B_{3\alpha} (\alpha_i - b_{sa}/2, r, t) dr$$
(32)

$$\phi_{ss(2i+2N_s)} = l_{ef} \int_{R_s}^{(R_{sb}+R_s)/2} B_{3\alpha} (\alpha_i + b_{sa}/2, r, t) dr$$
(33)

$$\phi_{ss(2i+2N_s-1)} = -l_{ef} \int_{R_s}^{(R_{sb}+R_s)/2} B_{3\alpha} (\alpha_i - b_{sa}/2, r, t) dr$$
(34)

After all the flux sources flowing into the nodes are calculated, flux in branch of the equivalent magnetic circuit can be obtained by Kirchhoff's Current Law. The permeability of each tooth and yoke section is determined by flux passing through them. Then, the permeability of each section in stator is determined according to the B-H curve of iron core material. The B-H curve of iron core material is shown in Fig. 6.



FIGURE 6. B-H characteristic of DW465-50.

Finally, the permeance of each tooth and yoke section can be calculated by the permeability and geometrical parameters. The magnetic potential matrix of nodes in equivalent magnetic circuit is

$$\mathbf{V} = \left(\mathbf{A}\boldsymbol{\Lambda}\mathbf{A}^{\mathrm{T}}\right)^{-1}\boldsymbol{\Phi}$$
(35)

where **A** is the incidence matrix, **A** is the permeance matrix, and  $\Phi$  is the node flux matrix. The values of equivalent current densities on the *i*th stator slot edges can be calculated from nodes magnetic potential

$$J_{i1} = \left( V_{3N_s + i + 1} - V_{2i+1} \right) / (R_{sb} - R_s)$$
(36)

$$J_{i2} = (V_{2i-1} - V_{3N_s+i}) / (R_{sb} - R_s)$$
(37)

$$J_{i3} = (V_{2i+1} - V_{2i-1}) / (R_{sb} \cdot b_{sa})$$
(38)

where  $R_{sb} - R_s$  and  $R_{sb} \cdot b_{sa}$  are the lengths of each tooth and yoke, respectively.

### D. COMBINATION OF MEC AND SUBDOMAIN

In the proposed hybrid analytical model, the equivalent current densities used as boundaries conditions in the improved subdomain model are calculated from equivalent magnetic circuit, and the flux sources flowing to the equivalent magnetic circuit are obtained by the improved subdomain model. Therefore, an iterative algorithm is required to find convergent solutions. The calculation flowchart of the proposed hybrid model is shown in Fig. 7. Then, magnetic field distributions and electromagnetic performances of module-combined stator permanent magnet machines can be calculated.



FIGURE 7. Calculation process of the hybrid model.

### **IV. FEA AND EXPERIMENT VALIDATION**

In order to verify the effectiveness of the proposed hybrid analytical model, FEA is performed and a prototype with three stator modules is manufactured. The main parameters of the prototype in shown in table 1.

TABLE 1.	Main	parameters	of the	prototype.
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Parameter	Value
Number of slots	72
Number of poles	30
Number of modules	3
Slot bottom radius $R_{sb}$ (mm)	229
Stator inner radius $R_s$ (mm)	195
Magnet outer radius $R_m$ (mm)	194.2
Rotor outer radius $R_r$ (mm)	188.2
axial length $L_{ef}$ (mm)	225
Number of turns	41
Pole-arc coefficient	0.88
Magnet remanence (T)	1.18
Slot width $b_{sa}$ (degree)	2.77
Wingding width $d$ (degree)	1.3

Fig. 8 shows the stator of prototype machine with three modules. Fig. 9 shows the flux density distributions of stator module with different current predicted by FEA, I, II and III are operated with 1, 1.5 and 3 times rated current, respectively.



FIGURE 8. Stator of the prototype.

### A. PERFORMANCES UNDER NORMAL CONDITIONS

Fig. 10 shows the radial and tangential flux densities in the middle of air-gap calculated by the conventional subdomain model, hybrid model and FEA method. The RMS value errors of radial and tangential flux densities of conventional subdomain model and finite element method are 4.3% and 4%, respectively. The RMS value errors of radial and tangential flux densities of the proposed hybrid analytical model and finite element analysis are 1.2% and 1.6%, respectively. The calculation results of the proposed hybrid analytical model have good consistency with FEA method. The conventional subdomain model cannot consider the nonlinearity effect, therefore, the results predicted by conventional subdomain overestimates.



FIGURE 9. Flux density distribution of stator under load condition.



FIGURE 10. Air-gap flux densities: (a) Radial; (b) Tangential.

Fig. 11 shows the back EMF predicted by three calculation methods mentioned above and the measured results. The results predicted by the hybrid analytical model are almost identical with FEA method. But the conventional subdomain model overestimates without taking saturation effect into consideration. The back EMF curves of measurement results and predictions by the proposed hybrid model and FEA match greet well, which verifies the high accuracy of the proposed hybrid analytical model with considering nonlinearity effect. The RMS values of the prediction by hybrid model and measured results are 218V and 215.7V, respectively. The error between the prediction of proposed hybrid analytical model

and the experiment results is 1.1% due to the manufacturing errors and without considering the end effect.



FIGURE 11. Phase no-load back EMF: (a) Calculated; (b) Measured.

Fig. 12 shows the electromagnetic torque predicted by the conventional subdomain model, hybrid model, FE model and the measurement. The hybrid model predictions are in good agreement with FEA results, while results predicted by the conventional subdomain are higher without taking saturation effect into account.



FIGURE 12. Electromagnetic torque.

### **B. TORQUE UNDER ASYMMETRIC CONDITIONS**

When one stator module or the inverter fails during operation, the other modules can continue to operate without being affected. The module-combined stator permanent magnet machines have good ability of fault tolerance. In this section, the torque characteristics of the module-combined stator permanent magnet machine under asymmetric conditions are analyzed.

The electromagnetic torques with one and two modules in rated operation calculated by conventional subdomain model, the proposed hybrid model and FEA method are shown in Fig. 13. The average torque predicted by each method change linearly when different number stator modules are in rated operation. However, it cannot maintain the rated output torque.



FIGURE 13. Torque with different modules in rated operations.

In order to maintain rated output torque unchanged, the current in the windings of modules in operation should be increased. When one and two modules are in operation, current need to be increased to 3 and 1.5 times, respectively. Fig. 14 shows torque with different modules in overload operations. Due to the neglection of saturation, the results calculated by conventional subdomain model are the same under different conditions. The results predicted by hybrid model and FEA model show a good agreement even under overload conditions. The difference between the conventional model and the proposed hybrid model is more significant when the saturation level is higher, which proves that the proposed hybrid model can accurately calculate the performances considering the nonlinearity effect. Due to the heavy saturation effect under overload conditions, the output torques of two modules with 1.5 times rated current in operation and one



FIGURE 14. Torque with different modules in overload operations.

module with 3 times rated current in operation decrease to 98.9% and 94.2% of the rated torque, respectively.

Fig. 15 shows the experiment platform. The torques varied with current under different stator modules in operations are measured. As shown in Fig. 16, the predicted results by the proposed hybrid analytical model and the measured results have good agreement. The accuracy of the proposed hybrid analytical method even under heavy saturation conditions is verified.



FIGURE 15. Experiment platform.



FIGURE 16. Torque varied with current.

### **V. CONCLUSION**

This paper proposes a new nonlinear subdomain and magnetic equivalent circuit hybrid analytical model for magnetic field prediction in module-combined stator permanent-magnet machines. Saturation effect is considered by introducing equivalent current densities on the slot edges. The proposed hybrid model combines the advantages of the two analytical models. The nonlinear hybrid analytical model improved the accuracy compared to conventional linear model by considering saturation effect. It can reduce computational time significantly compared with finite element method. The results predicted by the proposed model, including air-gap flux densities, back-EMF and electromagnetic torque, match well with finite element results even under heavy saturation conditions. The experimental results of the prototype machine prove these predictions.

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