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Ferromagnetic Silicene Superlattice Based Thermoelectric Flexible Renewable Energy Generator Device

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ABSTRACT The object of the current research manuscript is to analyze the valley-spin thermoelectric properties and Nernst coefficient at two different temperatures for ferromagnetic silicene superlattice. Photon-assisted tunneling probability is used to identify the resolved thermoelectric parameters including (valley, spin, and charge) electronic thermal conductance, Seebeck coefficient, figure of merit, and also electrical conductance and Nernst coefficient. The results show oscillatory behavior to all investigated parameters. The improved data of Seebeck coefficient (valley, spin, and charge) could be because of quantum confinement effect of the present investigated nanodevice. The figure of merit (valley, spin, and charge) attains quite high values with good high thermoelectric efficiency. The enhancement of Nernst coefficient (valley, spin, and charge) might consider Nernst effect is suitable for thermoelectric heat energy conversion system of the present flexible ferromagnetic silicene superlattice. The ferromagnetic silicene superlattice nanodevices are good candidates for flexible renewable energy generation as demonstrated by this analysis.

INDEX TERMS Electron thermal conductance, Seebeck coefficient, electrical conductance, figure of merit, thermoelectric efficiency, Nernst coefficient.

I. INTRODUCTION

The dramatic increase of power demand in electrical power grids is noticed in the recent decades. Added to that, the environmental concerns and economic constrains initiate many research efforts in different aspects. Many efforts are investigated for involving the different types of renewable energy resources into electrical grid for enhancing the overall system performance as for solving the optimal power flow [1], modeling of solar cells and modules [2] for improving the efficiency of radial distribution systems with wind power existence [3], [4], for economic and environmental concerns [5], for considering the economic concerns in emergency events [6], and for solving reactive power problem with renewable energy resources [7]. The need of flexible renewable energy generation acts an important issue to assure acceptable performance of renewable energy resources. So, the motivation of this work lies in this trend.

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On the other hand, around half of the world's generated energy is wasted as heat [8]–[11]. The electricity generation from the temperature gradient using thermoelectric, solid-state devices could be a good waste heat energy recovery [8]–[11]. Heat produced by unconcentrated or concentrated sunlight can also be converted to electrical power using thermoelectric devices. The importance here comes from the fact that the radiation in infrared range has photon energy lower than the photo-sensitizers band gap so it is squandered as heat [8]–[11]. Without moving parts, the Peltier effect and Seebeck effect can directly convert heat to electricity so that, thermoelectric materials can handle a lot of energy problems. The efficiency of thermoelectric conversion can be measured by the dimensionless figure of merit [12]–[16]. In spintronics and conventional electronics to process and carry information the two intrinsic electron characteristics, spin and charge are utilized [17]–[19]. Recently, there is another degree of freedom in some materials, the valley degree of freedom, which can be utilized to process and carry information, and this research field is called valleytronics [20]–[23]. Many literatures in this field emphasis the ability of superlattice

structures to successfully control the transport properties of graphene [24], [25], silicene [26], [27] and semiconductors [28], [29].

The phenomena of thermoelectric and spin transport involving spin Seebeck tunneling [30], anomalous Nernst effects [31], [32], spin [32], thermal spin transfer torque [33], and spin dependent thermopower [34] are related in the spin caloritronics field. In monolayer transition metal dichalcogenides (TMDCs), theoretically, various valley/spin-dependent thermoelectric effects already have been anticipated, involving valley Nernst effect (VNE) [35]–[37] and spin Nernst effect, which is the thermoelectric analogy of the spin Hall effect [38], [39].

Therefore, a new field has been aroused called valley caloritronics in [40]–[42] as the experimental demonstration of these effects with help of spin-valley degree of freedom, which is more reliable than spin regarded to external magnetic fields because of enormous intrinsic spin–orbit coupling (SOC).

Non-volatility, ultra-low heat dissipation and faster speed make spintronic devices a perfect candidate for electronics' future. In addition, because of their remarkable spin-dependent properties, such as spin diffusion length, Rashba SOC, ultra-long spin relaxation time, quantum spin Hall effect and spin-valley locking, 2D materials such as black phosphorus (BP), graphene, silicene [43] and TMDCs have provided an excellent forum for spintronic study.

Additionally, new opportunities for the practical application of spintronics have been brought by 2D materials, and improvements are expected in low-power computing, communication and storage. For nanoelectronic applications, silicene, a cousin of graphene, is presently of interest to studies in the area of 2D materials [40], [41], [44]. Compared to graphene and other 2D materials, the benefits of silicene are that it is compatible with existing silicon-based electronics and can easily be integrated into them [42].

It is well known that the effect of both Nernst coefficient and valley degree of freedom on spin thermoelectric energy efficiency has not been considered upto this moment in ferromagnetic silicene superlattice. So, this work aims to explore thermoelectric energy conversion and valley-spin Nernst effect of ferromagnetic silicene superlattice. The important features can be summarized as:

- The valley-spin thermoelectric properties and Nernst coefficient at two different temperatures for ferromagnetic silicene superlattice are investigated.
- The oscillatory behavior of all parameters is discussed.
- The figure of merits (valley, spin, and charge) attains quite high values at good high thermoelectric efficiency.
- The enhancement of Nernst coefficient (valley, spin, and charge) considering the Nernst effect is suitable for thermoelectric heat energy conversion system of the presented flexible ferromagnetic silicene superlattice.

- The ferromagnetic silicene superlattice nanodevices can be considered as good candidates for flexible renewable energy generation.

II. THE PROPOSED DEVICE

2N ferromagnetic strips interweave (2N-1) normal strips of equally length single-layer silicene [27], [45] are forming the proposed model. This device's source and drain are formed of metal as seen in Fig. 1.

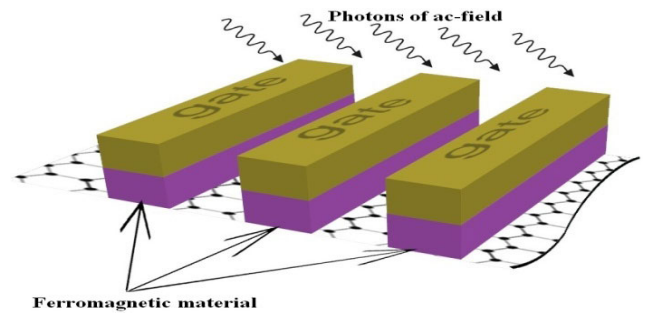


FIGURE 1. A schematic diagram of the proposed model.

The transport of valley-spin polarization under induced ac field is implemented. Photon-assisted conduction channels also can be introduced with help of ac-oscillating fields which can be modulated with the gated voltage to set it into the window of conduction of the device [23], [27], [45]–[47]. The transport is distinguishable for spin alignment because of Zeeman splitting which is imposed in presence of magnetic field, there are valley possibilities also in addition to conduction channels of the photo-assisted transport, so this resulted in photon-assisted spin and valley resolved conduction. The tunneling probability, $\Gamma_{ac\text{-field}}(E)$, is calculated as [27], [45]:

$$\Gamma_{ac\text{-field}}(E) = \sum_{n=1}^{\infty} J_n^2\left(\frac{eV_{ac}}{n\hbar\omega}\right) \cdot |t_{\eta\sigma}|^2 \quad (1)$$

where $J_n\left(\frac{eV_{ac}}{n\hbar\omega}\right)$ is first kind Bessel function of order n^{th} , V_{ac} is the induced ac-field peak and ω is its angular frequency and $t_{\eta\sigma}$ represents transmission coefficient, with $\eta(\eta') = +1(-1)$ conforms to $K(K')$ valley, $\sigma = +1(-1)$ is for up spin and down spin configuration [27], [45].

The categories of conductance, G , in silicene are [48]–[50]: Valley resolved conductance, $G_{K(K')}$, is:

$$G_{K(K')} = \frac{G_{K(K')\uparrow\uparrow} + G_{K(K')\uparrow\downarrow}}{2} \quad (2)$$

The spin alignments are distinguished by $\uparrow\uparrow$ for parallel and $\uparrow\downarrow$ for antiparallel. Spin resolved conductance, $G_{\uparrow(\uparrow\downarrow)}$ is:

$$G_{\uparrow(\uparrow\downarrow)} = \frac{G_{K\uparrow(\uparrow\downarrow)} + G_{K'\uparrow(\uparrow\downarrow)}}{2} \quad (3)$$

The Dirac fermion conductance for the three cases charge, valley and spin respectively are:

$$G_C = \frac{1}{2}(G_{\uparrow\uparrow} + G_{\uparrow\downarrow}) \quad (4)$$

$$G_V = G_K - G_{K'} \tag{5}$$

$$G_S = G_{\uparrow\uparrow} - G_{\uparrow\downarrow} \tag{6}$$

Using the function, $L_m(\mu)$, electronic thermal conductance,

K_e , and Seebeck coefficient, S , are calculated [51], [52]:

$$L_m = \frac{2}{h} \int_{E_F}^{E_F+\hbar\omega} \int_{-\pi/2}^{\pi/2} \Gamma_{withphoton}(E) \cdot (E - \mu)^m \cdot \left(-\frac{\partial f_{FD}(E)}{\partial E} \right) \cdot \cos \theta d\theta dE \tag{7}$$

$$K_e = \frac{1}{T} \left(L_2 - \frac{L_1^2}{L_0} \right) \tag{8}$$

$$S = \frac{1}{eT} \cdot \frac{L_1}{L_0} \tag{9}$$

where ($m = 0, 1, 2$), \hbar , μ , T , and e are reduced Planck's constant, electrochemical potential, absolute temperature and electronic charge [8], [10], [51], [52] and $\left(-\frac{\partial f_{FD}}{\partial E} \right)$ represents first derivative of Fermi-Dirac distribution function.

The thermoelectric figure of merit, ZT , of present nanodevice will be given as [8], [10], [51], [52]:

$$ZT = \frac{S^2 G T}{K_e + K_L} \tag{10}$$

where K_L is the lattice (phonon) thermal conductance.

Of single-layer silicene, the intrinsic lattice thermal conductivity is 9.4W/mK much smaller than that of bulk silicon or graphene at room temperature [53]–[55]. It is well known that interfaces impact on thermal conductivity in superlattices can have different sources, including specular scattering because of acoustic mismatch [56], phonon localization and bandgap formation [57]. This is supposed to lead to a greater decrease in thermal conductivity than that in electrical conductivity because of lower mobility. For the optimization of electronic transport, superlattices can be engineered by controlling quantum confinements, band offsets and tunneling processes among different material layers [58], [59]. Therefore, it is of present and imminent interest to design suitable superlattices with the purpose of optimizing thermoelectric performance. Hence the calculations will be performed at low temperatures as will be shown in the results below. Then thermoelectric figure of merit, ZT , of this device will be calculated as [27], [45]:

$$ZT = \frac{S^2 G T}{K_e} \tag{11}$$

In silicene the Seebeck coefficient, S , classified into two cases:

Valley resolved Seebeck coefficient, $S_{K(K')}$, is:

$$S_{K(K')} = S_{K(K')\uparrow\uparrow} + S_{K(K')\uparrow\downarrow} \tag{12}$$

Spin resolved Seebeck coefficient, $S_{\uparrow(\uparrow\downarrow)}$, is:

$$S_{\uparrow(\uparrow\downarrow)} = S_{K\uparrow(\uparrow\downarrow)} + S_{K'\uparrow(\uparrow\downarrow)} \tag{13}$$

The charge Seebeck coefficient is computed as [60]:

$$S_c = \frac{1}{2}(S_{\uparrow\uparrow} + S_{\uparrow\downarrow}) \tag{14}$$

The spin Seebeck coefficient is computed as [60]:

$$S_S = (S_{\uparrow\uparrow} - S_{\uparrow\downarrow}) \tag{15}$$

Also, the valley Seebeck coefficient, S_V , in analogy with S_S can be defined as:

$$S_V = S_K - S_{K'} \tag{16}$$

The charge electronic thermal conductance also, is computed as [60]:

$$K_{ec} = \frac{1}{2}(K_{e\uparrow\uparrow} + K_{e\uparrow\downarrow}) \tag{17}$$

The valley and spin electronic thermal conductance are computed as [60]:

$$K_{eV} = K_{eK} - K_{eK'} \tag{18}$$

$$K_{eS} = (K_{e\uparrow\uparrow} - K_{e\uparrow\downarrow}) \tag{19}$$

For electricity generation, the thermoelectric device ideal efficiency, η , is [8]–[11]:

$$\eta = \eta_c \frac{\sqrt{1 + ZT} - 1}{\sqrt{1 + ZT} - \left(\frac{T_c}{T_h}\right)} \tag{20}$$

where T_h and T_c are the temperatures of hot side (heat source) and cold side (heat sink), respectively, of the proposed device and η_c represents Carnot efficiency and $\eta_c = 1 - T_c/T_h$. The figure of merit relates the efficiency of device through Eq.(20) which is a materials property, so a lot of thermoelectric field's work is provided to materials development for enhancement of thermal electrical conversion efficiency. The charge, spin, valley efficiency, η_c , η_s , and η_V will be computed as shown below.

The Nernst coefficient, N_T , is expressed as [10], [51], [61]:

$$N_T = \frac{1}{8\pi k_B T^2} \int_{E_F}^{E_F+\hbar\omega} \int_{-\pi/2}^{\pi/2} \Gamma_{withphoton}(E) \cdot (E - \mu) \cdot \left(-\frac{\partial f_{FD}(E)}{\partial E} \right) \cdot \left(1 + \frac{\partial f_{FD}(E)}{\partial E} \right) \cdot \cos \theta d\theta dE \tag{21}$$

$$\left(-\frac{\partial f_{FD}}{\partial E} \right) = (4k_B T)^{-1} \cosh^{-2} \left(\frac{E - E'_F + n\hbar\omega}{2k_B T} \right) \tag{22}$$

where k_B is Boltzmann constant and $\left(-\frac{\partial f_{FD}}{\partial E} \right)$ represents first derivative of Fermi-Dirac distribution function. The charge, spin, valley Nernst coefficients will be given as respectively:

$$N_{cT} = \frac{1}{2}(N_{T\uparrow\uparrow} + N_{T\uparrow\downarrow}) \tag{23}$$

$$N_{ST} = (N_{T\uparrow\uparrow} - N_{T\uparrow\downarrow}) \tag{24}$$

$$N_{VT} = (N_{KT} - N_{K'T}) \tag{25}$$

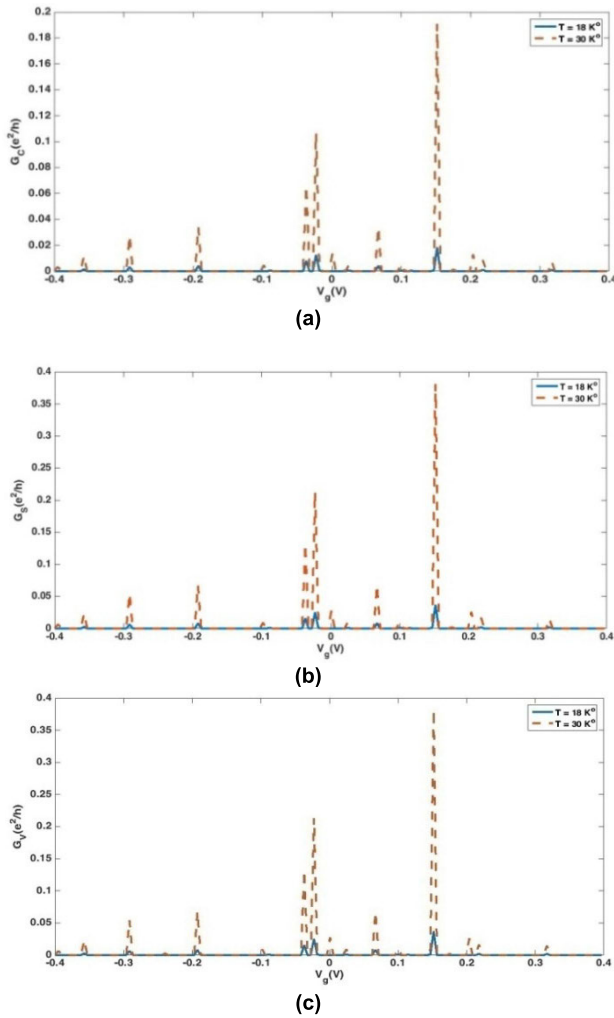


FIGURE 2. The variation of electric resolved conductance versus, V_g , at both temperatures for (a) charge, (b) spin, and (c) valley.

III. RESULTS AND DISCUSSIONS

Thermal power parameters of the explored silicene-based nanostructure model are computed numerically by taking $N = 1$ which means that the nanostructure is a lead of normal silicene before a (ferromagnetic /normal / ferromagnetic strips of silicene) then a lead of normal silicene. The parameters' values are as follow [35], [36], [39], [45], [50]:

ac-field peak	$V_{ac} = 0.25 \text{ V}$
Fermi velocity	$v_F \approx 5.5 \times 10^5 \text{ m/s}$
Lande g-factor	$g = 2$
intrinsic spin-orbit coupling	$\lambda_{SO} = 3.9 \text{ meV}$
on-site potential difference between A and B sublattices	$\Delta_z = 2 \text{ meV}$
y-direction junction width	$d = 30 \text{ nm}$
width	$W = 20 \text{ nm}$
barrier height	$V_b = 50 \text{ meV}$

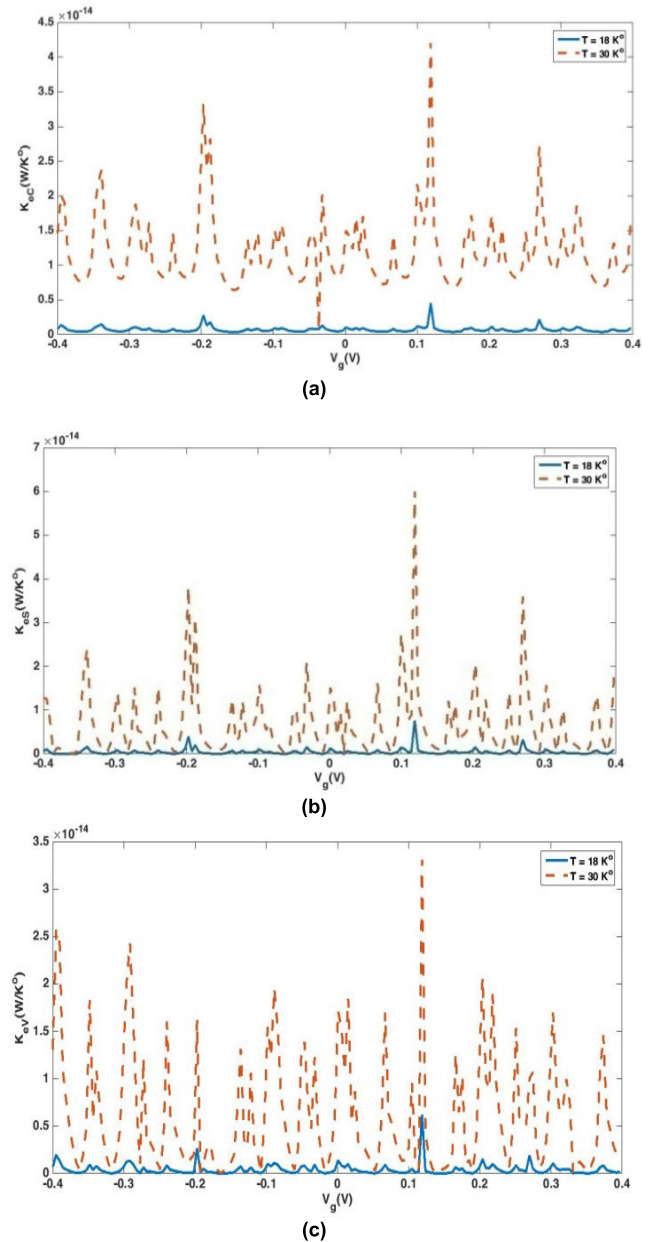


FIGURE 3. The electronic thermal conductance variation versus, V_g , at both temperatures for (a) charge, (b) spin, and (c) valley.

The external applied magnetic field of 0.1T is taken as an optimum value in the tested model [46], [51]. The quasiparticle Dirac fermions carrier density, n' , is used by (Eq.26) to compute the modulated Fermi energy, E'_F [45], [54], [60].

$$E'_F = \sqrt{\pi} \hbar v_F \sqrt{n'} \quad (26)$$

Since the parameter n' is tuned by proximity effect of single layer ferromagnetic silicene [45], [54], [61] then, the parameter, n' , is determined by the theory of density function to get the optimum magnitude of E'_F . The usual electric field resulted from gate voltage, V_g , could modulate the previously mentioned parameters which generates possibilities for tunable energy gap applications.

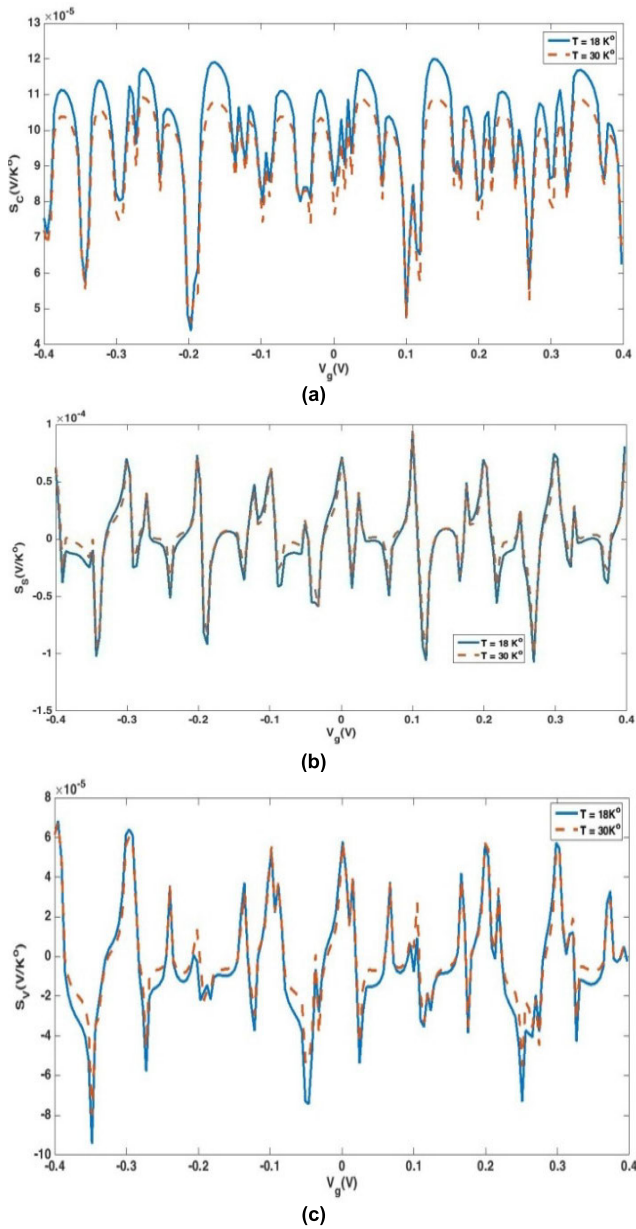


FIGURE 4. The Seebeck coefficient variation versus, V_g , at both temperatures for (a) charge, (b) spin, and (c) valley.

The IR range is supposed to be the best range to enrich the thermoelectric parameters of explored nanostructure, so the induced ac-field frequency choose to be 1.25THz [27], [45]. All figures plotted against gate voltage at different two temperatures, $T_c = 18K$ and $T_h = 30K$.

Fig.2 declares the electric conductance in terms of (e^2/h) for case of charge (a), spin (b) and valley (c) versus, V_g , at the both temperatures. It exhibits a selective behavior at specific values of, V_g , with maxima at 0.1519V and equals $0.01854(e^2/h)$ at 18K and equals $0.1907(e^2/h)$ at 30K for charge electric conductance, while for spin electric conductance and valley electric conductance they show the same behavior with maxima at 0.1519V and equals $0.03708(e^2/h)$

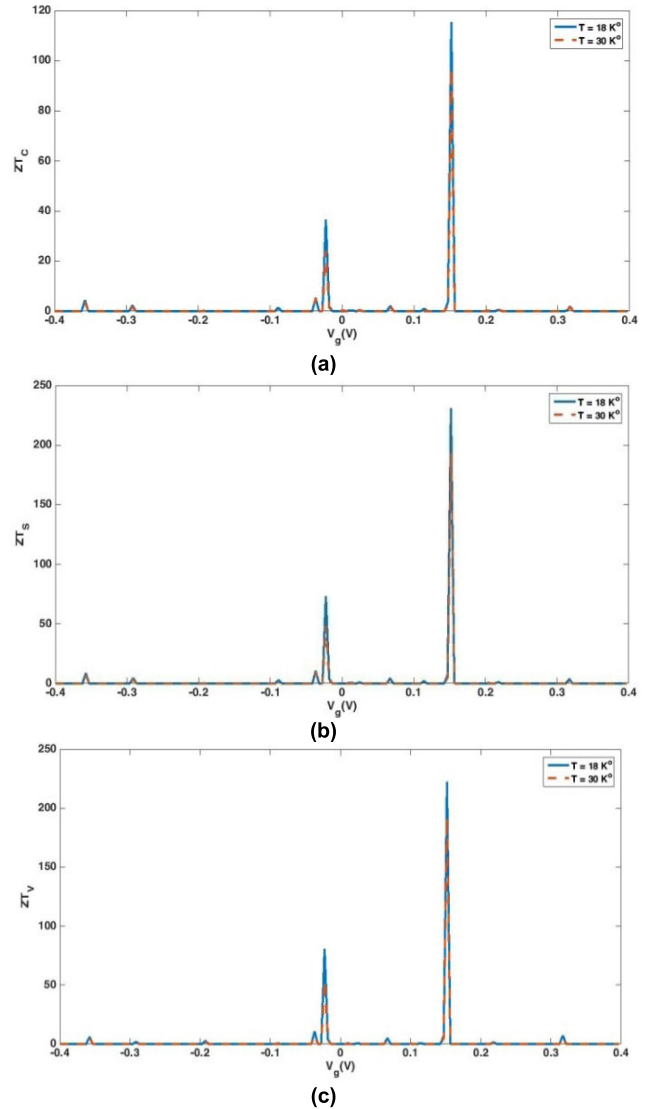


FIGURE 5. The figure of merit variation versus, V_g , at both temperatures for (a) charge, (b) spin, and (c) valley.

at 18K and equals $0.3813(e^2/h)$ at 30K. Also, the widths of such oscillations and its peak height might be controlled by magnetic proximity effect and electric field of EuO ferromagnetic insulator [22], [23], [42], [45], [62].

Fig.3 declares the variation of electronic thermal conductance in terms of (W/K) for case of charge (a), spin (b) and valley (c) versus, V_g , at both temperatures. It is obvious that as the temperature rises, electronic thermal conductance increases. and shows multi peaks with maxima $4.204 \cdot 10^{-14} W/K$ at 30K and $4.512 \cdot 10^{-15} W/K$ at 18K for charge electronic thermal conductance, $6.007 \cdot 10^{-14} W/K$ at 30K and $7.674 \cdot 10^{-15} W/K$ at 18K for spin electronic thermal conductance and $3.312 \cdot 10^{-14} W/K$ at 30K and $6.235 \cdot 10^{-15} W/K$ at 18K for valley electronic thermal conductance. All maxima take place at 0.1189 V.

Fig.4 declares the variation of Seebeck coefficient in terms of (V/K) for case of charge (a), spin (b) and valley

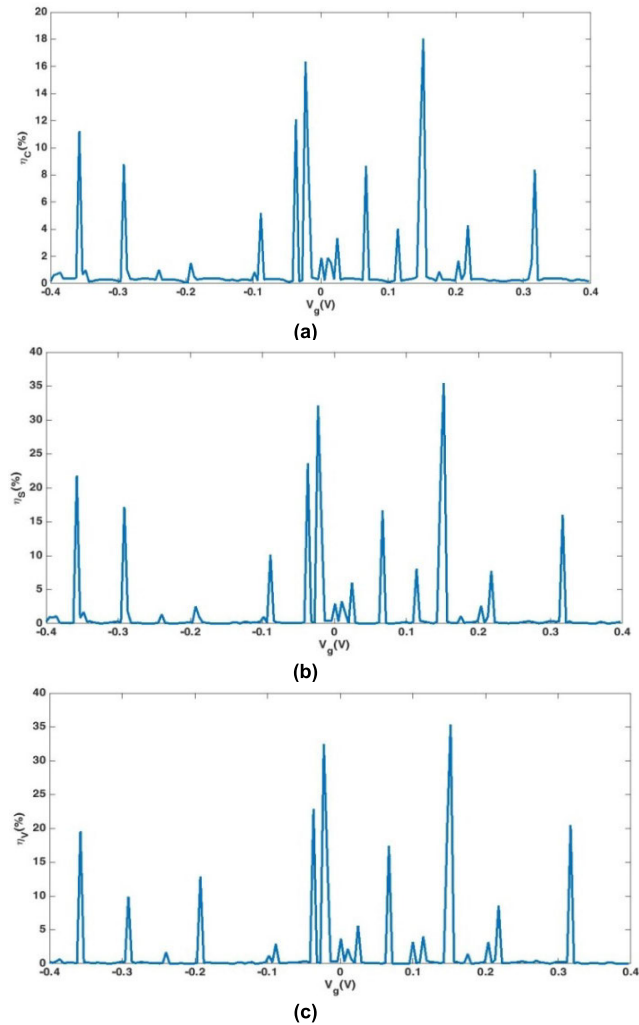


FIGURE 6. The conversion efficiency variation versus, V_g , at both temperatures for (a) charge, (b) spin, and (c) valley.

(c) versus, V_g , at the both temperatures. It demonstrates a periodic like manner and temperature insensitive in this range. The charge Seebeck coefficient varies from 4.384×10^{-5} to 1.19×10^{-4} V/K, the spin Seebeck coefficient varies from -1.074×10^{-4} to 9.403×10^{-5} V/K and the valley Seebeck coefficient varies from -9.437×10^{-5} to 6.744×10^{-5} V/K. Also, it is shown from this figure that Seebeck coefficient magnitudes (charge, spin, valley) are quite high. This is because of quantum confinement effects of this nanostructure [26], [42], [45], [58], [59], [63]–[65].

Fig.5 declares the variation of figure of merit for case of charge (a), spin (b) and valley (c) versus, V_g , at the both temperatures. It demonstrates a sharp selective behavior at specific gate voltage magnitudes with two noticeable maxima at 0.1519V with $ZT_C = 115.4$ at 18K, $ZT_C = 96.56$ at 30K and at -0.0226V with $ZT_C = 36.75$ at 18K, $ZT_C = 24.15$ at 30K for charge figure of merit, while for spin figure of merit and valley figure of merit they show the same behavior with maxima at 0.1519V with $ZT_S = ZT_V = 230.8$ at 18K,

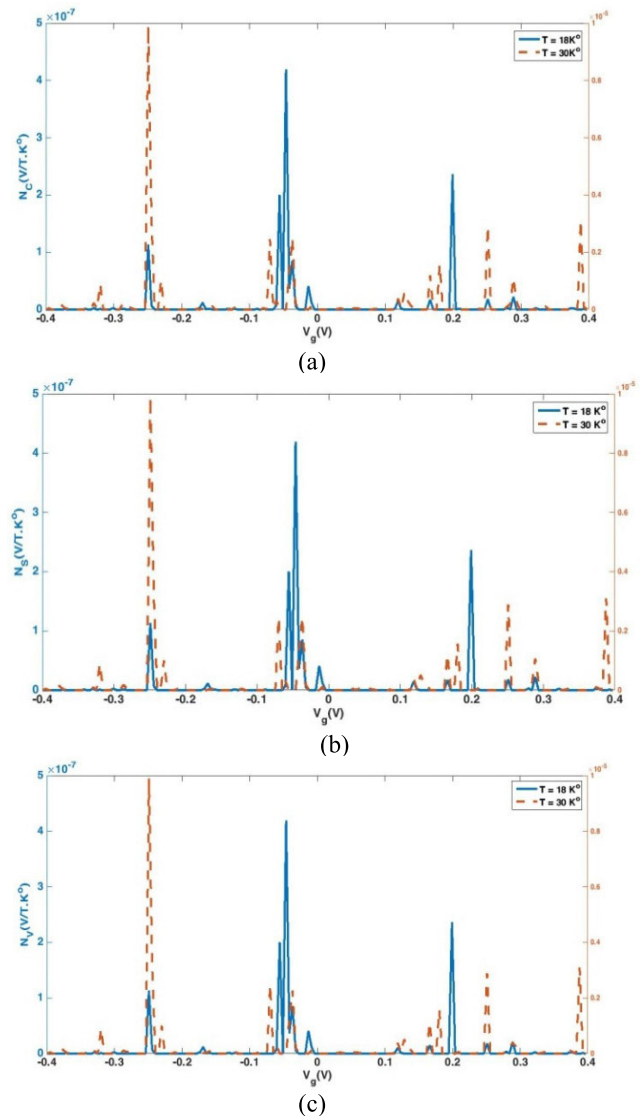


FIGURE 7. Nernst coefficient variation versus, V_g , at both temperatures for (a) charge, (b) spin, and (c) valley.

$ZT_S = ZT_V = 193$ at 30K and at -0.0226V with $ZT_S = ZT_V = 73.46$ at 18K, $ZT_S = ZT_V = 48.3$ at 30K.

Fig.6 declares the conversion efficiency for case of charge (a), spin (b) and valley (c) versus, V_g . It shows a selective behavior with periodic like nature and has maximum at 0.1519V equals 18.07% for charge case. While for spin and valley cases they show the same behavior with maximum at 0.1519V and equals 35.44%. Also, Figs. (5,6) demonstrate that figure of merits magnitudes (charge, spin, valley) are larger than one at some values of gate voltage. This figure of merits improvement is because of enhancement of corresponding Seebeck coefficients (Fig.4) [50], [66]. So in the present results show that ferromagnetic silicene superlattice whose minibands are formed with specific bandwidth segregated by forbidden bands [45], [59] because of which an optimal density of states pattern to provide thermoelectric

figure of merit enrichment results and the corresponding quite high values for thermoelectric efficiencies (Fig.6).

-Fig.7 declares the Nernst coefficient in terms of (V/T.K) for case of charge (a), spin (b) and valley (c) versus, V_g , at the both temperatures. It demonstrates a selective behavior at specific magnitudes of gate voltage with maxima at $-0.04623V$ and equals $2.098 \times 10^{-7} V/T.K$ at 18K and at $-0.2491V$ equals $4.949 \times 10^{-6} V/T.K$ at 30K for charge Nernst coefficient, while for spin Nernst coefficient and valley Nernst coefficient they show the same behavior with maximum at $-0.04623V$ and equals $4.196 \times 10^{-7} V/T.K$ at 18K and at $-0.2491V$ equals $9.898 \times 10^{-6} V/T.K$ at 30K. It is shown from Fig.(7) that Nernst coefficients magnitude (charge, spin, valley) are quite high at certain values of the gate voltage. This enhancement of present Nernst coefficients might be due the effects of the applied electric current and ferromagnetic exchange magnetic field of the ferromagnetic silicene [67], [68]. Also, the modulation of Fermi energy and strong spin orbit coupling of silicene might play an important role for enhancement of Nernst coefficients (charge, spin, and valley).

IV. CONCLUSION

The ferromagnetic silicene superlattice valley-spin thermoelectric transport properties are investigated at different temperatures. Since Nernst coefficient represents the natural manifestation of electric current normal to temperature gradient and magnetic field, then spin-valley Nernst coefficients of the present nanodevice are also investigated. Results demonstrate that the computed thermoelectric parameters and Nernst coefficient are enriched to very acceptable values with high thermoelectric efficiency. According to this work, for high-efficiency energy harvesting nanodevices and flexible thermoelectric power generation, ferromagnetic silicene superlattice is very promising.

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