

Received May 17, 2021, accepted June 30, 2021, date of publication July 12, 2021, date of current version July 30, 2021.

Digital Object Identifier 10.1109/ACCESS.2021.3096419

Synthesis of Planar and Conformal Single-Layered Double-Sided Parallel-Cross Dipole FSS Based on Closed-Form Expression

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ABSTRACT A simple synthesis method for ultra-thin double-sided cross-dipole-based Frequency Selective Surfaces (FSS) is presented in this paper. The presented technique is used to design a flexible band-stop FSS for Electromagnetic Interference (EMI) shielding applications operating at 10 GHz. An Equivalent Circuit (EC) model in combination with closed-form expression is used to synthesize and validate the response of the proposed element. In addition, a parametric study of the proposed FSS aiming to optimize the bandwidth has been presented. The proposed FSS holds similar responses for TE and TM mode of polarization at normal incidence. Further, the conformal behavior of the proposed FSS in comparison with planar FSS is presented and evaluated. The proposed FSS is validated with the full-wave EM solver for simulation and a prototype is fabricated. The size of the proposed unit cell is $0.4\lambda_0 \times 0.4\lambda_0$, where λ_0 is the free space wavelength at the desired resonant frequency. In addition, the fractional bandwidth for TE and TM modes is 10.42% at normal incidence. The measured results of a proposed FSS are presented and validated in comparison with the simulations with good agreement.

INDEX TERMS Frequency selective surfaces, equivalent circuit model, bandwidth, conformal elements.

I. INTRODUCTION

Recently, a new concept of periodic structures is used to meet the rapid development of communication technology in terms of high data rates and system capacity. The idea revolves around the deployment of periodic structures into the building walls to make the propagation environment more favorable [1]–[4]. Among these periodic structures, FSS is a prominent structure used to isolate interference with adjacent wireless systems and enhance wireless security. Moreover, several numerical techniques have been proposed to analyze FSS. These techniques include full-wave analysis [5], iterative approach [6], and an equivalent circuit model [7]–[10]. As the electromagnetic performance of the FSS can be expressed by the inductive and capacitive behavior, the equivalent circuit model is the most widely used technique due to its simplicity. The analysis of FSS is essentially a method based on geometric parameters like the period of the unit

cell (p), metal length (l), metal width, and the gap between the adjacent strips (g). In these techniques, the knowledge of the physical parameters is vital for accurate design.

On the other hand, to find these parameters for given filtering properties, a few synthesis methods are presented in the literature, especially for double-sided parallel-cross-dipoles-based FSS. In this regard, this paper proposes a straightforward technique for synthesizing a flexible double-sided parallel cross-dipoles-based FSS for a particular frequency band and provides the required size for the double-sided parallel cross-dipoles topology. Besides, producing a specific bandwidth is another degree of freedom relevant to the proposed synthesis technique and is different from the techniques reported in the open literature. The double-sided parallel cross-dipoles-based FSS in the article is a deformation of the Jerusalem cross-slot [11]. However, the proposed closed-form equations in this paper deal with FSS synthesis. The proposed synthesis method in this paper allowing the prediction of the physical parameters of the unit cell for Double-Sided Parallel-Cross Dipole FSS operating at 10 GHz and for an

The associate editor coordinating the review of this manuscript and approving it for publication was Flavia Grassi¹.

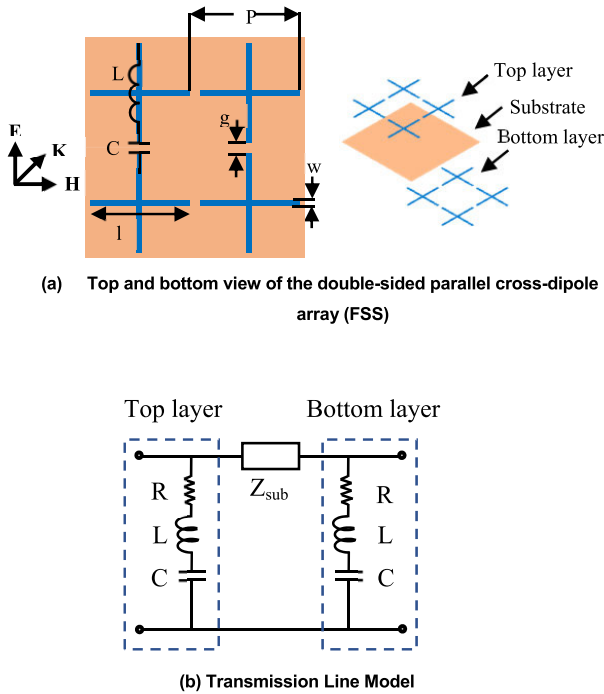


FIGURE 1. Double-sided parallel cross dipoles FSS structure and its equivalent circuit model.

arbitrary value of quality factor $Q = 7.5$. The proposed FSS has the same frequency response for TE and TM polarizations with a fractional bandwidth of 10.42% at normal incidence. In addition, the structure presents a high level of shielding performance for both polarizations.

The Section II of the manuscript explains the theory of operation of double-sided parallel cross dipoles-based FSS. In Section III, the result obtained by the analytical solution is compared with the numerical simulation. Section IV explores the bandwidth control technique of double-sided parallel cross-dipoles. In Section V, the band-stop principle of double-sided parallel cross-dipoles FSS design at 10 GHz has been explored. Finally, the work is concluded in Section VI.

II. THEORETICAL APPROACH

According to Marcuvitz [12], the electromagnetic behavior of the metal strip lines is represented by the polarization of the wave. The parallel strips to the electric field are equivalent to an inductive element, and the perpendicular strips to the electric field correspond to a capacitive element, as presented in Fig. 1(a). The proposed double-sided parallel cross-dipoles-based FSS can be described by the equivalent circuit model shown in Fig. 1(b).

The equivalent circuit model of the proposed FSS is shown in Fig. 1(b), represents a band-stop filter. With this circuit, a double-sided parallel cross dipoles FSS can be synthesized to control the reflection level of the signal and the bandwidth enhancement. Therefore, by specifying the operating frequency ($f_0 = 1/2\pi\sqrt{LC}$) [13] and the approximate quality factor of the overall circuit $(Q_1 + Q_2)/2$, where

($Q_1 = Q_2 = \sqrt{L/R\sqrt{C}}$) [14], all the circuit parameters can be determined. The first step in the proposed synthesis procedure is to obtain the parameters of the equivalent circuit model presented in Fig. 1(b). The series RLC resonator is implemented with the periodic arrangement of the metal strips, where ‘L’ is an equivalent inductance of the vertical dipoles, ‘C’ is the capacitance between the vertical ends of the two double-sided parallel crossed dipoles and the equivalent resistance ‘R’ corresponds to the ohmic losses of the metallic strips. The lumped element values of the equivalent circuit are commonly calculated using (1), (6), and (8), where ‘P’, ‘l’, ‘w’, and ‘g’ are the dimensions of the unit cell of a double-sided parallel crossed-dipole respectively. The ‘ θ ’ is the incidence angle with the normal incidence.

The equivalent inductance ‘L’ is given by Marcuvitz [12] as

$$\omega L = Z_0 \frac{l}{P} \cos \theta F(P, w, \lambda_0, \theta) \tag{1}$$

where ‘ ω ’ is an angular frequency, Z_0 and λ_0 are free-space wave impedance, and wavelength respectively, and (2) and (3), as shown at the bottom of the next page, where,

$$A_{\pm} = \frac{1}{\sqrt{\left[1 \pm \frac{2P \sin \theta}{\lambda_0}\right]^2 - \left(\frac{P \cos \theta}{\lambda_0}\right)^2}} - 1 \tag{4}$$

$$\beta = \sin\left(\frac{\pi s}{2P}\right), \quad \text{with } s = w \text{ or } g \tag{5}$$

The equivalent capacitance ‘C’ is given by Langley and Drinkwater [15] as

$$\omega C = 4Y_0 \frac{(2 \times w + g)}{P} \cos \theta F(P, g, \lambda_0, \theta) \epsilon_{eff} \tag{6}$$

where ‘ ω ’ is the angular frequency, Y_0 and λ_0 are free-space wave admittance and wavelength, respectively.

The factor ϵ_{eff} in (6) represents an effective permittivity [14] and is calculated by

$$\epsilon_{eff} = \epsilon_{rh} + (\epsilon_{rh} - 1) \left[\frac{-1}{\exp^N(x)} \right] \tag{7}$$

with $x = (10^*h/P)$; where ‘h’ is the thickness of the substrate, ‘P’ is the size of the unit-cell, $\epsilon_{rh} = \epsilon_r$ (if dielectric presents on both sides of the FSS) and $\epsilon_{rh} = (\epsilon_r + 1)/2$ (if dielectric presents only on one side), and N is an exponential factor that varies from 1.3 to 1.8 for different cell shapes in terms of the unit-cell filling factor. For double-sided parallel cross-dipole-based FSS, the optimal value of ‘N’ is 1.3.

The equivalent resistance ‘R’ can be calculated from [16] as

$$R \approx R_s \frac{S}{A} \tag{8}$$

where ‘ R_s ’ is the surface resistance, $S = P^2$ is the area of one-unit-cell, and ‘A’ is the surface area of the lossy element within a single unit cell. Using Equations (1) to (8), the equivalent circuit parameters in Fig. 1(b) can be readily determined.

Finally, the quality factor Q of the proposed FSS can be derived by substituting (1), (2) and (8) in the quality factor expression ($Q = \sqrt{L/R\sqrt{C}}$) as

$$Q = \frac{Z_0 A}{2R_s S} \sqrt{\frac{l \times F(P, w, \lambda_0, \theta)}{(2 \times w + g) \times F(P, g, \lambda_0, \theta) \epsilon_{eff}}}$$
 (9)

From these formulas, it can be concluded that the Q factor is a function of the different geometric parameters of the unit cell. However, the values of the strip length and periodicity cannot be chosen freely. The dipole length is approximately equal to $\lambda/2$ at the resonance frequency, while the periodicity of the structure must be much smaller than the wavelength. Subsequently, the quality factor can be controlled freely by the strip width.

In summary, the synthesis procedure of the proposed FSS can be simplified as follows:

- A. First, with the given values of the center frequency (f_0) and quality factor (Q), the parameters of the equivalent circuit elements can be obtained.
- B. The dipole length ' l ' is approximately equal to $\lambda/2$ at the resonance frequency.
- C. Based on this calculated dipole length ' l ' and with a starting value of the metal width ' w ', estimate the value of the FSS's periodicity using the relation of equivalent resistance i.e., Eq. (8).
- D. By enforcing the angle of incidence at normal incidence and for a given substrate, determine the value of the metal width ' w ' using Eq. (6).

The above method allows the equivalent circuit shown in Fig. 1(b) to synthesize the desired filtering response. It demonstrates the relationship between the equivalent circuit elements and the physical dimensions of the proposed FSS.

III. NUMERICAL RESULTS

The synthesis steps described in Section II are followed to design a stop-band FSS having a resonant frequency at 10 GHz for an arbitrary value of quality factor $Q = 7.5$. Hence, the values of EC parameters are calculated as $R = 0.05 \Omega$, $C = 0.031 \text{ pF}$, and $L = 8 \text{ nH}$. After acquiring the equivalent circuit parameters and choosing the dielectric substrate ($\epsilon_r = 2.94$, $h = 0.13 \text{ mm}$, $\tan \delta = 0.02$), the initial values of the unit-cell dimensions are obtained. Hence, the dipole length ' l ' = 11.1 mm, the element size (or the period of the unit cell) ' P ' = 11.6 mm, and the dipole strip width ' w ' = 0.2 mm. It should mention that these physical parameters are obtained for the normal incidence. Based on these values, the proposed FSS is designed, and verified with

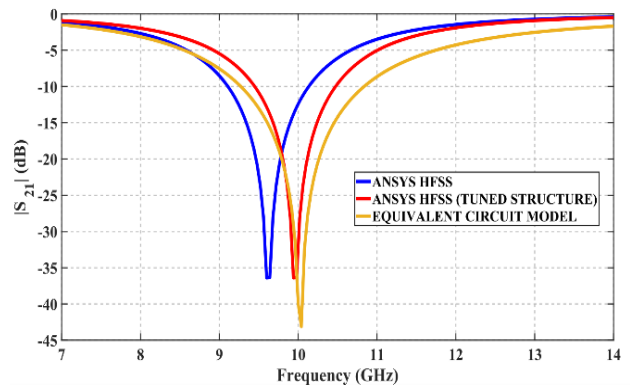


FIGURE 2. Transmission coefficient obtained by different methods for normal incidence.

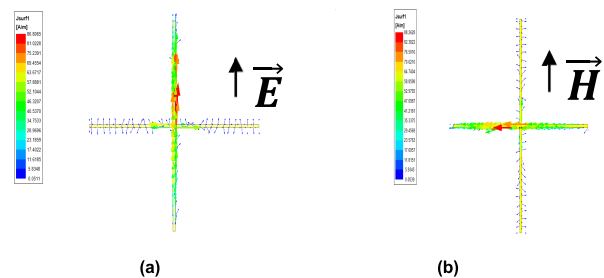


FIGURE 3. Surface current distribution of the proposed FSS at 10 GHz. (a) TE, and (b) TM mode of polarization.

the full-wave simulation. The obtained geometrical parameters of the unit-cell are tuned by using Ansys HFSS [17] to reach the desired frequency response. The transmission coefficient predicted by the equivalent circuit model is compared with the simulated results obtained by the initial geometry parameters and the tuned parameters are shown in Fig. 2. It is observed that the optimized HFSS simulated results are in close agreement with the obtained theoretical results. The surface current distribution of the proposed FSS for TE and TM modes is depicted in Fig. 3. From this figure, it is evident that the proposed model has the same frequency response for both modes.

IV. BANDWIDTH ENHANCEMENT

To obtain a wide stopband, the quality factor (Q) has to be decreased. Based on the filter theory [13], Q can be reduced by reducing the equivalent inductance and increasing the equivalent capacitance at the same time. From Eq. (1) described in section II, it is evident that using a large value of inductive element implies a gradual shift of the resonance

$$F(P, s, \lambda_0, \theta) = \frac{P}{\lambda_0} \left[\ln \left\{ \frac{\csc \pi s}{2P} \right\} \right] + G(P, s, \lambda_0, \theta)$$
 (2)

$$G(P, s, \lambda_0, \theta) = \frac{(1 - \beta)^2 [(1 - \beta^2/4)(A_+ + A_-) + 4\beta^2 A_+ A_-]}{2 \times (1 - \beta^2/4) + \beta^2 (1 + \beta^2/4 - \beta^2/4)(A_+ + A_-) + 2\beta^6 A_+ A_-}$$
 (3)

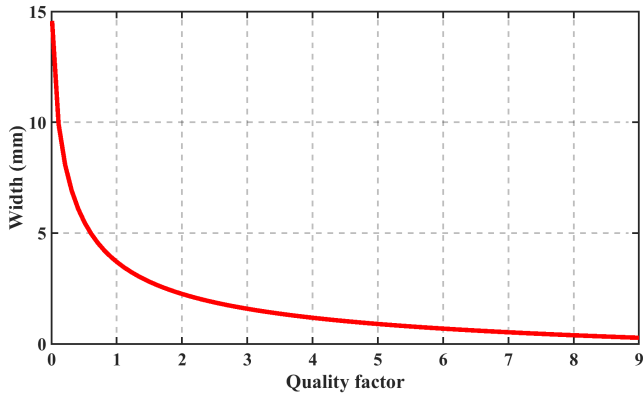


FIGURE 4. Plot for strip-width (w) as a function of the quality factor.

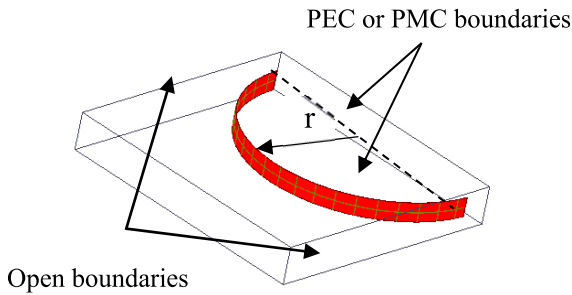
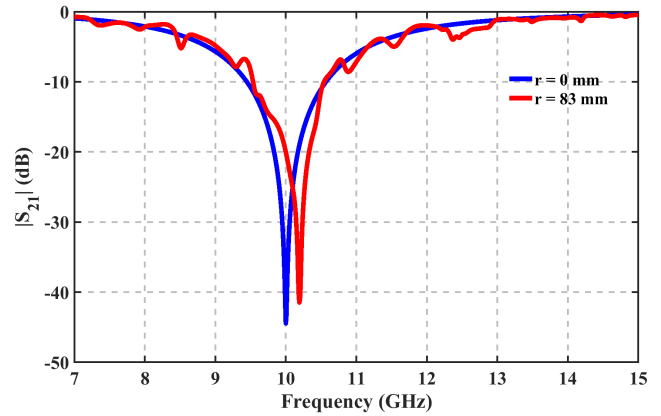


FIGURE 5. Simulation setup of the conformal FSS.

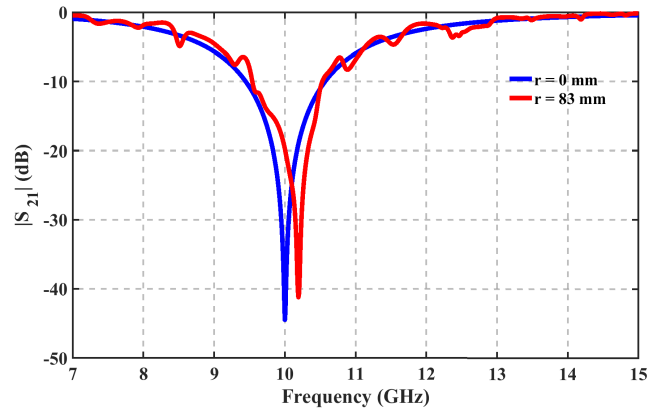
frequency and generates poor stability under oblique incidence. Therefore, it is necessary to keep the inductance constant and, at the same time, increase the capacitance of the FSS to obtain a larger bandwidth. From Eq. (6) described in section II, it is necessary to choose a wider element to increase the capacitance of the FSS. For this reason, the metal width of the unit-cell is predicted as a function of the quality factor Q . Based on Eq. (9), the value of the metal width can be estimated for various values of Q . By using this synthesis method, the dipole width of the unit-cell is estimated for given frequency response and dielectric substrate at normal incidence. The data used for this case is as follows: the resonant frequency is 10 GHz, and the FSS is designed on a 0.13 mm thick RT/Duroid 6002 substrate with a relative dielectric constant of 2.94. The illustrated Fig.4 represents the strip width ' w ' of the unit-cell under the quality factor variation. It can be observed that, for a wider bandwidth performance, should use a wider metal strip.

V. CONFORMAL BEHAVIOUR

In real-time applications, such as aerospace fuselage, parabolic reflectors, radome antennas, and many others, the conformal FSS has a significance, which is flesh mounted to the surface. Hence, the conformal behavior of the proposed FSS is analyzed using the bending option in Ansys HFSS. Based on a semi-infinite model described in [18], the conformal FSS is evaluated, and the same is simulated, as shown in Fig. 5. A finite array of FSS with 1×25 is



(a)



(b)

FIGURE 6. Simulated transmission coefficient for conformal and planar FSS at normal incidence (a) TE, and (TM) modes respectively.

simulated using wave ports. The top and bottom walls of the waveguide are assigned as PEC or PMC boundaries, whereas the side walls are assigned as open boundaries. This technique helps to evaluate the conformal structure at normal incidence. Fig. 6 shows the simulated transmission coefficient for planar and conformal FSS. It should also mention that the frequency response of the planar geometry is obtained by using periodic boundary conditions.

Fig. 6 presents the comparison of the simulated transmission coefficient of the conformal FSS and the planar FSS at the normal angle of incidence for both polarizations. It is observed that the resonant frequency for the FSS shifts from 10 GHz when the structures are bent. Fig. 6(a) shows that for the TE mode of polarization at the normal incidence, when the FSS is bent with a radius (r) of 83 mm, the simulated resonance frequency is shifted from 10 GHz to 10.19 GHz. On the other hand, for the TM mode of polarization, as shown in Fig. 6(b), the resonance frequency is shifted from 10 GHz to 10.2 GHz. This slight variation in the resonance frequency for both the polarization is attributed to the variation of the impedance properties and the interelement coupling of the FSS when it is bent [19].

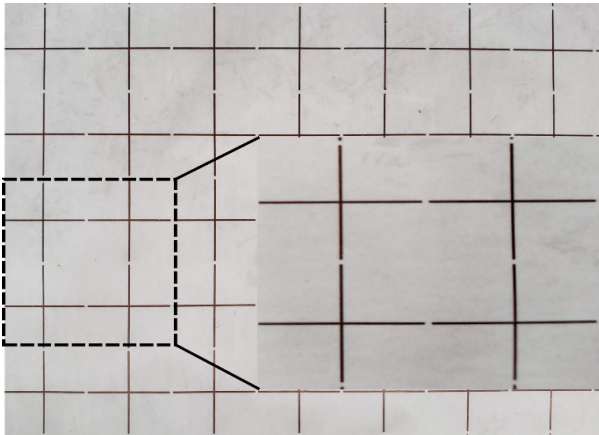
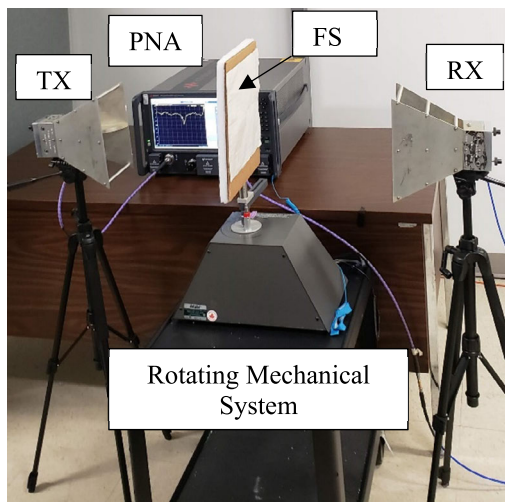
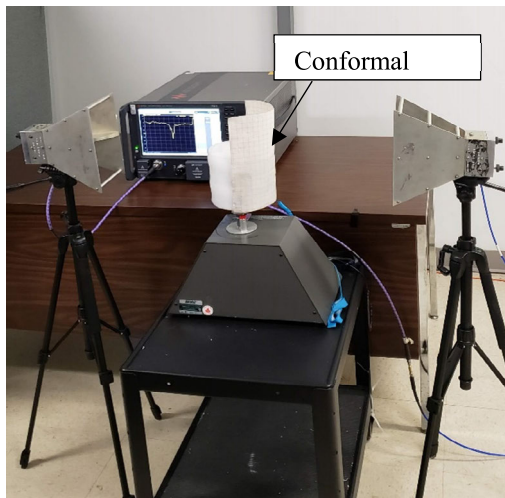


FIGURE 7. Photograph of the fabricated FSS prototype.



(a)



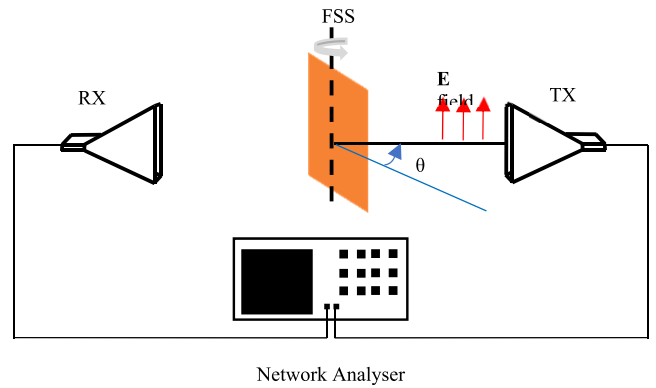
(b)

FIGURE 8. Experimental setup for measuring transmission coefficient for (a) Planar and (b) Conformal FSS.

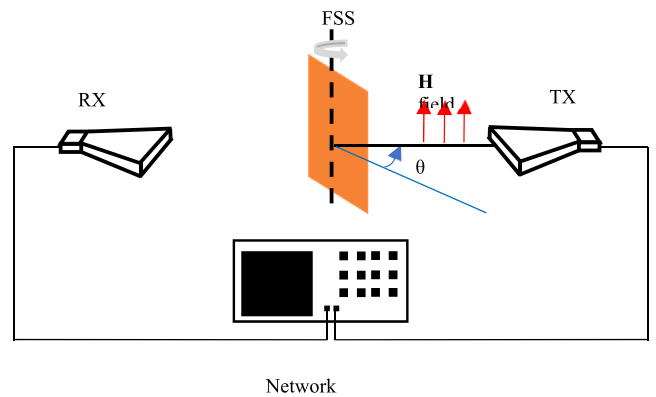
VI. EXPERIMENTAL RESULTS

A. PLANAR FSS

To experimentally validate the synthesis method described in section II, a prototype of the double-sided parallel



(a)

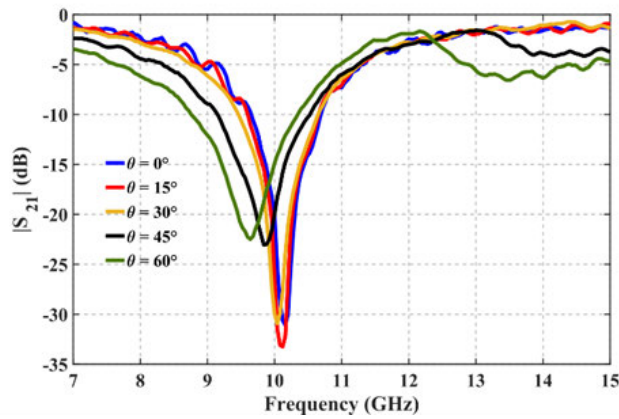


(b)

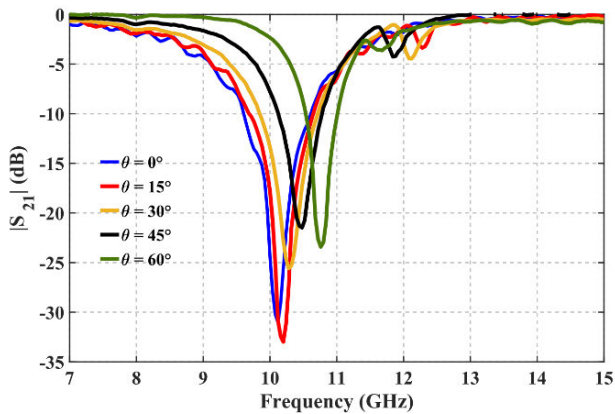
FIGURE 9. Measurement method for (a) TE, and (b) TM mode of polarization.

cross-dipoles FSS, as shown in Fig. 7, is fabricated and measured. The dimensions of the FSS prototype are $304 \text{ mm} \times 304 \text{ mm}$, containing 25×25 elements for a metal width of 0.2 mm , a dipole length of 11.91 mm , and a periodicity of 12.16 mm , respectively. The measurement is performed in an enclosed room, where two wideband horns (1 GHz to 18 GHz) are used in the experimental setup. As shown in Fig. 8, the FSS prototype is placed between horn antennas, and the measurements are taken using an Agilent (PNA-X N5242A) network analyzer. As a reference, the transmission coefficient without FSS structure is measured. After that, the subsequent measurements of the transmission coefficients, for various angles of incidence and polarization, are obtained using a rotating mechanical system. The TE and TM modes were measured by using the method described in Fig. 9.

The measured transmission coefficient for both TE and TM mode of polarizations for various angles of incidence are plotted in Fig. 10. The measured FSS response for the TE polarization with different angles of incidence is plotted in Fig. 10(a). For the TE mode of polarization, it is observed that, as the angle of incidence increases, the bandwidth



(a)



(b)

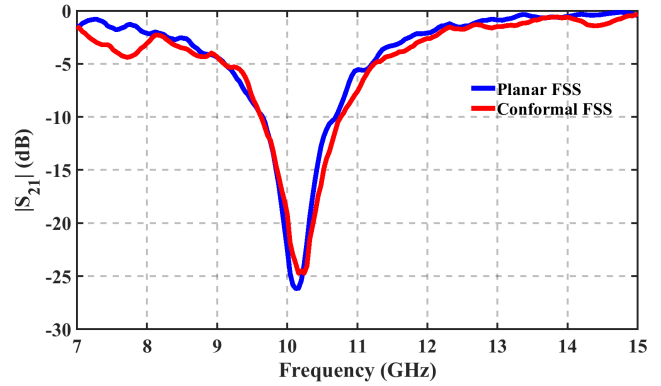
FIGURE 10. Measured transmittance for (a) TE, and (b) TM mode of polarization.

increases. Different behavior is observed for TM mode of polarization as shown in Fig. 10(b), when the angle of incidence increases from 0° to 60°, the bandwidth decreases. The resonant frequency shift is observed for both polarizations when the incident wave angle varies from 0° to 60°. This occurs due to the impedance on the angle of incidence as given by the relation ($Z_{TE} = Z_0 / \cos \theta$, $Z_{TM} = Z_0 * \cos \theta$).

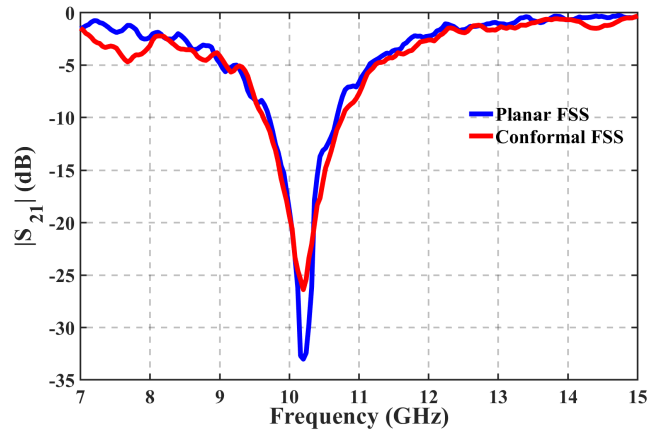
B. CONFORMAL FSS

The transmission coefficient of the conformal FSS is obtained with a setup shown in Fig. 8(b) at normal incidence for both TE and TM modes. The planar FSS is bent on an arc of radius ‘r’ of 83 mm. The structure is attached to semi-circular cylinder foam that has similar dielectric properties with the free space ($\epsilon_r = 1$). Fig. 11 shows the comparison of the measured transmission coefficient for both configurations. The conformal FSS exhibits a stable frequency response compared to the planar FSS at normal incidence for both polarizations.

To understand the shielding performance of the proposed FSS, shielding effectiveness (SE) is obtained using the equa-



(a)



(b)

FIGURE 11. Measured transmission coefficient for conformal and planar FSS at normal incidence (a) TE, and (TM) modes respectively.

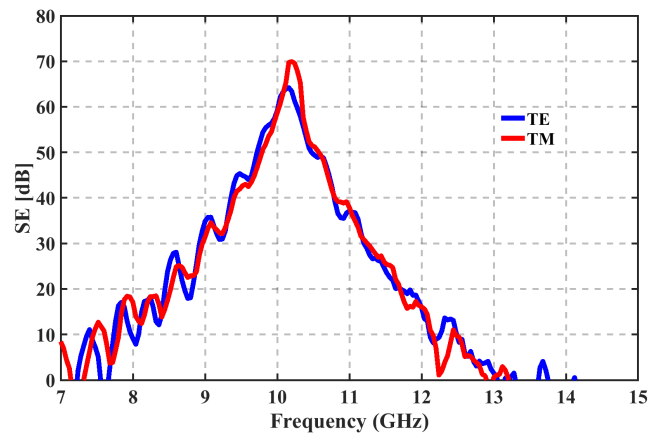


FIGURE 12. Measured shielding effectiveness of the proposed FSS for both polarizations at normal incidence.

tion (10):

$$SE (dB) = -20 \times \log \left| \frac{E_t}{E_i} \right| \tag{10}$$

Fig. 12 presents the shielding performance (SE) of the proposed FSS for both polarizations at normal incidence. It is evident that the proposed FSS provides a high SE level around

TABLE 1. Comparison with related works.

Ref	Element used	Center frequency (GHz)	Method	Flexibility	Number of layers
[11]	Complementary JC element	10	Analysis method	Yes	Single
[21]	Square loop	13.5	Synthesis method	No	Double
[22]	Crossed dipoles	8	Synthesis method	No	Single
[23]	Patch	10	Analysis	No	Single
<i>Proposed work</i>	Double-sided Crossed dipoles	10	Synthesis	Yes	Single

10 GHz for both TE and TM modes. Hence, the proposed FSS is suitable for EMI shielding applications.

Further, the comparison of the proposed work with the related works is shown in Table 1. It is evident from Table 1 that the proposed design method solves the synthesis problem, which is rarely described in the literature especially for double-sided crossed dipoles. The proposed synthesis method is based on the equivalent circuit model provides a simple way for designing conformal FSS, which can be applied in electromagnetic interference shielding applications. In addition, this method provides a formula for the Q factor as a function of the geometric parameters of the unit cell, which can be used to improve the bandwidth.

VII. CONCLUSION

In this paper, a simple method for synthesizing band-stop FSS and control of bandwidth is presented. The band-stop FSS consists of double-sided parallel cross-dipoles. The proposed conformal FSS is analyzed based on the equivalent circuit model at the desired frequency response, which allows acquiring the optimized physical parameters. The proposed work is verified by designing an ultra-thin FSS prototype having a band-stop response with a quality factor of 7.5 at 10 GHz. Full-wave simulations and experimental verifications have demonstrated the performance of the proposed FSS. The fabricated FSS is tested under different incident wave angles for both TE and TM modes of polarization.

ACKNOWLEDGMENT

The authors thank the valuable support and encouragement of the National Sciences and Engineering Research Council of Canada (NSERC) in executing the project.

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