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Drone Mobile Networks: Performance Analysis Under 3D Tractable Mobility Models

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ABSTRACT Reliable wireless communication networks are a significant but challenging mission for post-disaster areas and hotspots in the era of information. However, with the maturity of unmanned aerial vehicle (UAV) technology, drone mobile networks have attracted considerable attention as a prominent solution for facilitating critical communications. This paper provides a system-level analysis for drone mobile networks on a finite three-dimensional (3D) space. Our aim is to explore the fundamental performance limits of drone mobile networks taking into account practical considerations. Most existing works on mobile drone networks use simplified mobility models (e.g., fixed height), but the movement of the drones in practice is significantly more complicated, which leads to difficulties in analyzing the performance of the drone mobile networks. Hence, to tackle this problem, we propose a stochastic geometry-based framework with a number of different mobility models including a random Brownian motion approach. The proposed framework allows to circumvent the extremely complex reality model and obtain upper and lower performance bounds for drone networks in practice. Also, we explicitly consider certain constraints, such as the small-scale fading characteristics relying on line-of-sight (LOS) and non line-of-sight (NLOS) propagation, and multi-antenna operations. The validity of the mathematical findings is verified via Monte-Carlo (MC) simulations for various network settings. In addition, the results reveal some design guidelines and important trends for the practical deployment of drone networks.

INDEX TERMS Drone mobile networks, mobility models, performance boundary, stochastic geometry theory, system-level analysis.

I. INTRODUCTION

The exponential growth of wireless data driven by mobile devices (e.g., tablets) has promoted the need for non-terrestrial networks [1]. However, it's a challenging task for operators to provide data services in special use-cases and

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circumstances such as large-gatherings (e.g., competitions) and man-made or natural disasters (e.g., earthquake). The latter in particular, is unpredictable by nature and has critical effects in terms of both ecological and economic costs. Securing communications capability is a vital component for disaster relief and response [2]. However, the conventional cellular communication systems are difficult to provide stable and reliable network connectivity. In the past few years,

drone technology has matured and widely used in smart city construction, such as security monitoring, real-time video streaming [3]. The drone can be quickly deployed by carrying a wireless communication module to form a drone air base station, thereby alleviating network congestion in hotspots [4], [5]. Drone opens up the possibility for rapid restoration of damaged cellular system. Drone assisted network is considered as a potential scheme for improving conventional terrestrial cellular networks, so it has received considerable attention in both industry and academia recently. Field experiments show that the air base station can effectively improve the user experience in the area with poor coverage and achieve the change of throughput from valley-to-peak [6]. The results shown that the UAV-based solution can provide stable network access capabilities compared to conventional systems in the scenario of large-scale gatherings and terrestrial communication infrastructure being destroyed. Therefore, current fifth generation (5G) and future integrated sixth generation (6G) wireless network also consider the application of UAVs in the system [7]. While there is no doubt about the advantages of UAVs, it still has some challenges for large-scale applications.

The stochastic theory is an approach widely used in the analysis of wireless networks because it can well capture the connection distance and randomness between nodes in many scenarios. The work in [8] used stochastic theory to study device-to-device (D2D) communications in post-disaster area. In [9], the authors borrowed tools from stochastic theory to modeling the channel in high-speed railway scenarios. The authors studied the coverage probability of low-earth-orbit satellites using stochastic geometry tools in [10]. The authors used stochastic geometry approach to describe the cache-enabled heterogeneous networks (HetNets) in [11]. Zhang *et al.* [12] analyzed the performance of cellular networks with cooperative relays using tools provided by stochastic geometry. The optimization of non-orthogonal multiple access (NOMA) in massive machine-type communications via stochastic theory has been studied in [13]. The authors evaluated the performance of full-duplex cooperative NOMA networks using stochastic geometry tools in [14]. The system coverage probability of UAV networks with the blockage effect using stochastic tools has been studied in [15]. In [16], the authors combined NOMA and full-duplex to solve the scarce of spectrum in UAV network using stochastic approach. The 3D-UAV enabled networks based on stochastic geometry as well as air-to-ground (A2G) channel modeling are studied in [17], and various effects such as the impact of shadowing in [18], [19] or the adoption of point process for modeling the UAVs distribution in [20], [21] are investigated. In [22], the authors analyzed the A2G channel model based on stochastic tools, where the 3D arbitrary trajectory changed.

Several studies on the performance of drone cellular networks based on stochastic geometry have also been reported in the literature. The downlink coverage probability was obtained ignoring LOS and NLOS propagation in [23].

In [24], the authors investigated the impact of Nakagami- m and LOS propagation in drone networks ignoring NLOS propagation. In [25], the authors studied the single drone MIMO networks where NLOS propagation was considered. In [26], the authors studied the coverage probability of static drone networks at a certain height considering LOS and NLOS propagation. In [27], the single drone network was investigated with considering a single slope path loss model where the drone could move to certain points. The single drone moving cyclically along the cell edge was studied based on stochastic geometry in [28]. The performance of multiple drone networks with hovering flight drone and cruising drone was studied in [29]. In [30], the authors compared the performance of sub-6 GHz and millimeter wave (mmWave) under drone hovering case. In [31], the authors investigated coverage probability of energy-harvesting-powered drones in 3D space with randomly deployed drones between maximum and minimum height. The 3D space drone cellular network is simplified to 2D plane by distributing UAVs at fixed height in [32].

A. CONTRIBUTIONS

In contrast to the drone networks considering either LOS or NLOS propagation in [23]–[25] and simplified drone mobility model (e.g., hovering, cruising, fixed height, static) in [27]–[32], we consider LOS and NLOS propagation with random mobility model in drone cellular networks. Although some random mobility models in HetNets have been provided in [33]–[36], the random mobility model of drone cellular networks has not been extensively studied. The main obstacle is the complex analysis of random mobility model, especially the Markov mobility model (i.e., the realistic mobility model [37]). Motivated by the above works, we present an analytical framework for the finite 3D drone mobile networks based on stochastic geometry. In this framework, we use the 3D Brownian motion and deterministic motion model to obtain performance boundaries of realistic drone mobile networks. Also, by considering LOS and NLOS propagation, a closed-form expression for spectral efficiency (SE) and outage probability of different mobility models including a random (Brownian) model are consequently provided. The main contributions of this paper can be summarized as follows:

- We provide a system-level analysis of the drone mobile networks, and the closed-form expressions of signal-to-interference-plus-noise ratio (SINR), SE and outage probability are derived. Also, we explicitly account for small-scale and large-scale fading characteristics relying on LOS and NLOS propagation and multi-slope path-loss.
- Instead of applying the complex Markov mobility model, we use the 3D Brownian motion and deterministic motion model to obtain performance boundaries of realistic drone mobile networks. The proposed framework allows for the study of drone mobile networks

under a number of mobility models including a random Brownian) motion model.

- Theoretical results are validated through MC simulations. The results show that the key features of drone mobile networks, in terms of high number of antennas and lower transmit power.

B. PAPER ORGANIZATION

The remainder of this paper is organized as follows. In Section II, the system description is given and a number of mobility models are presented. The spectrum efficiency and outage probability analysis of drone mobile network are provided in Section III. Numerical results are presented in Section IV, and finally, conclusions are provided in Section V.

Notation: \mathbf{x} denotes a vector; $\Pr[\cdot]$ denotes the probability; $\mathbb{E}_x[\cdot]$ indicates the expectation; $\mathcal{F}_x[\cdot]$ indicates the cumulative distribution function (CDF); $\mathcal{P}_x[\cdot]$ denotes the probability density function (PDF); $\mathcal{M}_x[\cdot]$ illustrates the m.g.f.; $|x|$ denotes the modulus; $\|\mathbf{x}\|$ indicates the Euclidean norm; $\mathcal{L}_x[\cdot]$ denotes the Laplace transform (LT) function; $\mathbf{I}_()$ is the identity matrix; $\delta(\cdot)$ indicates the Delta function; $\mathcal{H}(\cdot)$ indicates the Heaviside step function; $\mathcal{G}(\kappa, \theta)$ denotes the Gamma distribution with shape parameter κ and scale parameter θ ; $\mathcal{N}(\mu, \sigma^2)$ denotes the Gaussian distribution with mean μ and variance σ^2 ; $\Gamma(\cdot)$ and $\Gamma(\cdot, \cdot)$ are respectively the Gamma and incomplete (upper) Gamma functions.

II. SYSTEM DESCRIPTION

A. NETWORK TOPOLOGY

We consider a large-scale drone mobile network as shown in Fig. 1, where K base stations (BSs) (i.e., UAVs) are deployed on the finite 3D ball of radius R following a homogeneous poisson point process (PPP) Φ with spatial density λ . The PPP-based abstraction model is confirmed to be a reliable approach for drone mobile networks. Let K_{LOS} and K_{NLOS} representing the number of drones under LOS and NLOS propagation (i.e., $K = K_{\text{LOS}} + K_{\text{NLOS}}$), respectively. Based on Slivnyak’s theorem [38], and the stationary property of PPP, the analysis is carried for the typical user o supposed to be located at the origin.

B. PROPAGATION MODEL

In this network, the drones are mounted with M antennas, and be assumed to serve a user at each resource block. The typical user equip with single antenna. We assume each transmitter drone has perfect knowledge of typical user channel. $\mathbf{h}_b^T \sim \mathcal{CN}(\mathbf{0}, \mathbf{I}_M)$ indicates the small-scale fading channel between user o and its serving drone b . Here, we utilize the Nakagami- m distributed to capture the small-scale fading for LOS propagation, and use the Rayleigh distributed (i.e., $\exp(1)$) for NLOS propagation. Noted that the exponential distribution is a special case of Gamma distribution with $m = 1$, so the Nakagami- m parameter for NLOS propagation is $m_N = 1$. In addition, η indicates the additive white

Gaussian noise (AWGN) at the typical user, where the mean and variance σ^2 are zero.

Considering the drones apply conjugate-beamforming (CB) in downlink (DL) direction of communications, the intended small-scale fading channel power gains g_b (from the serving drone b) experiencing LOS and NLOS propagation follow the distribution $\mathcal{G}(m_L M, \frac{1}{m_L})$ and $\mathcal{G}(M, \frac{1}{m_N})$, where m_L and m_N respectively denote the Nakagami- m parameter for LOS and NLOS. The interfering small-scale fading channel power gains g_i (from the transmitting drone i) experiencing LOS and NLOS propagation follow the distribution $\mathcal{G}(m_L, \frac{1}{m_L})$ and $\mathcal{G}(1, 1)$, respectively [39], [40]. Then, the two-slope path-loss function can be constructed as

$$L(r) = \begin{cases} \max(\beta_0, \beta_1 r^{-\alpha_L}), & \text{LOS propagation} \\ \max(\beta_0, \beta_1 r^{-\alpha_N}), & \text{NLOS propagation} \end{cases} \quad (1)$$

where α_L and α_N represent path-loss exponents for LOS and NLOS links respectively with $\alpha_N > \alpha_L > 2$. β_0 illustrates the minimum coupling loss, β_1 indicates a constant parameter, r denotes the distance. Here, $\beta_1 = \frac{1}{\epsilon} \left(\frac{c}{4\pi f_c} \right)^2$, where f_c denotes the carrier frequency, and c represents the speed of light. For LOS ($L_{\text{LOS}}(r)$) and NLOS ($L_{\text{NLOS}}(r)$) links, $\epsilon = \epsilon_{\text{LOS}} = 1$ dB and $\epsilon = \epsilon_{\text{NLOS}} = 20$ dB, respectively [41].

A commonly used distance-dependent ITU-R Umi LOS and NLOS model (referred to as 3GPP LOS and NLOS model) is given as (2). By using (2), the LOS probability can be obtained as follows

$$\Pr[\text{LOS}, r] = \min\left(\frac{18}{r}, 1\right) \left(1 - e^{-\frac{r}{36}}\right) + e^{-\frac{r}{36}}. \quad (2)$$

The function of LOS probability can be expressed as the following simplified model, which approximates widely utilized 3GPP channel model [42]–[44].

$$\Pr[\text{LOS}, r_{()} = r] = \begin{cases} 1, & r \in [0, D) \\ 0, & r \in [D, R] \end{cases} \quad (3)$$

where D indicates the critical distance, $\Pr[\text{NLOS}, r] = 1 - \Pr[\text{LOS}, r]$. According to the independence of homogeneous PPP Φ , the drones are divided into two parts (i.e., LOS drones and NLOS drones). The average number of LOS and NLOS drones are $\bar{K}_{\text{LOS}} = \frac{4}{3}\pi D^3 \lambda$ and $\bar{K}_{\text{NLOS}} = \frac{4}{3}\pi (R^3 - D^3) \lambda$, respectively [45].

C. CELLULAR ASSOCIATION

The cellular association strategy is the path-loss based strategy. Mathematically, this strategy is given as

$$L(r_b) = \arg \max(L(r_l)), \quad \forall l \in \Phi, \quad (4)$$

where $L(r_b)$ represents the path-loss of serving drone b , and $L(r_l)$ indicates the path-loss of the l -th drone.

In next subsection, we will discuss three drone mobility models. Actually, the realistic drone mobility trajectory should follow the Markov mobility model, but Markov mobility model does not offer tractability for mathematical analysis. Hence, in this paper, we propose drone mobility model

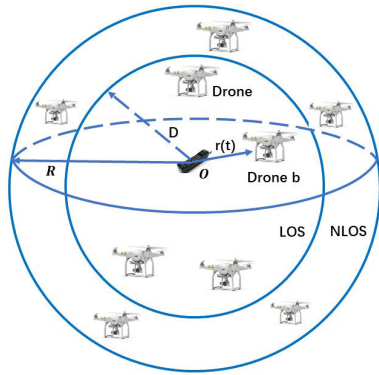


FIGURE 1. Depicting the finite 3D drone mobile network topology and propagation model with the path-loss based cellular association strategy.

(i.e., DM, 3D BM) to obtain upper and lower performance bounds for practical drone networks.

First, we discuss the CDF and PDF of $r_{b,LOS}$ with uniformly-deployed under LOS case, where $r_{b,LOS}$ denotes the distance between user o and its serving LOS drone.

Assuming K_{LOS} LOS drones (i.e., $K_{LOS} > 0$) deployed on the finite 3D ball of radius D following uniformly distribution, the CDF and PDF of $r_{b,LOS}$ are formulated as [46, Eqn. (6)]

$$\mathcal{F}_{r_{b,LOS}}(r) = 1 - \left(1 - \frac{r^3}{D^3}\right)^{K_{LOS}}, \quad 0 \leq r \leq D \quad (5)$$

and

$$\mathcal{P}_{r_{b,LOS}}(r) = \frac{3 r^2 K_{LOS}}{D^3} \left(1 - \frac{r^3}{D^3}\right)^{K_{LOS}-1}, \quad 0 \leq r \leq D. \quad (6)$$

Next, we aim to obtain the CDF and PDF of $r_{b,NLOS}$ with uniformly-deployed under NLOS case, where $r_{b,NLOS}$ denotes the distance between user o and its serving NLOS drone.

Assuming K_{NLOS} NLOS drones (i.e., $K_{LOS} = 0$) deployed on the finite 3D ball double-bounded by radii R and D ($D < R$) following uniformly distribution, the CDF and PDF of $r_{b,NLOS}$ are formulated as [47, Eqn. (3)]

$$\mathcal{F}_{r_{b,NLOS}}(r) = 1 - \left(1 - \frac{r^3 - D^3}{R^3 - D^3}\right)^{K_{NLOS}}, \quad D \leq r \leq R \quad (7)$$

and

$$\begin{aligned} \mathcal{P}_{r_{b,NLOS}}(r) &= \frac{3 r^2 K_{NLOS}}{R^3 - D^3} \left(1 - \frac{r^3 - D^3}{R^3 - D^3}\right)^{K_{NLOS}-1}, \quad D \leq r \leq R. \end{aligned} \quad (8)$$

In this part, we obtain the CDF and PDF of $r_{b,LOS}$ and $r_{b,NLOS}$ with uniformly-deployed under LOS and NLOS case. Next part, we will consider the mobility model of the drones.

D. DRONE MOBILITY

We consider two case in 3D Brownian motion and deterministic motion mode. (i) At any given time, the distance between the mobile LOS drone and origin is smaller than D (i.e., $r_{LOS,j}(t) = \max(0, \min(D, \hat{r}(t)))$, $j \in \{BM, DM\}$). (ii) At any given time, the distance between the mobile NLOS drone and origin is smaller than R and larger than D (i.e., $r_{NLOS,j}(t) = \max(D, \min(R, \hat{r}(t)))$, $j \in \{BM, DM\}$). In this network, the interfering drones are randomly generated in every time according to Poisson distributed in a 3D finite space. Also, because the cell association takes place in a slower time frame, once the user has been assigned a serving drone, it will be some time before the user changes the serving drone.

1) 3D BROWNIAN MOTION

In this subsection, we will analyze the mobility model 3D Brownian motion (BM) and deterministic motion (DM). In the mobility model, only the serving drone move, other interfering drones still fixed. The serving drone will move following the 3D BM model, the movement of the drone can be obtained according to the following stochastic differential equation (SDE) [48]

$$dl(t) = v db(t) \quad (9)$$

where $l(t) = \{l_x(t), l_y(t), l_z(t)\}$ denotes a vector for the Cartesian coordinates at time t , $b(t) = \{b_x(t), b_y(t), b_z(t)\}$ indicates the Wiener process (i.e., standard BM) vector at time t , and v (i.e., representing average velocity) indicates a positive constant. Then, according to the characteristics of the Wiener process, we can obtain $b_x(t), b_y(t), b_z(t) \sim \mathcal{N}(0, t)$. $\hat{r}(t) = \sqrt{l_x^2(t) + l_y^2(t) + l_z^2(t)}$ is the corresponding Euclidean distance to the origin at time t . First, we will derive the CDF and PDF of $r_{LOS}(t)$, where $r_{LOS}(t)$ denotes the distance to the origin under LOS propagation at time t . Recall the mobility model for LOS drone under consideration, $r_{LOS,j}(t) = \max(0, \min(D, \hat{r}(t)))$. The CDF of $r_{LOS,j}(t)$ (a function of three variables) can be expressed as [49]

$$\mathcal{F}_{r_{LOS,j}(t)}(w) = \mathcal{F}_0(w) \mathcal{F}_{\min(D, \hat{r}(t))}(w), \quad (10)$$

where $\mathcal{F}_0(w)$ indicates the CDF of constant 0, and $\mathcal{F}_{\min(D, \hat{r}(t))}(w)$ represents the CDF of function $\min(D, \hat{r}(t))$. Based on the 3D BM, $\hat{r}(t) = \sqrt{l_x^2(t) + l_y^2(t) + l_z^2(t)}$. By solving the Fokker-Plank equation (FPE) based on satisfying the SDE in (9) and considering $b_x(t), b_y(t), b_z(t) \sim \mathcal{N}(0, t)$, we can obtain $l_x(t), l_y(t), l_z(t) \sim \mathcal{N}(0, 2vt)$. Hence, we can readily apply the Central Limit Theorem (CLT) to obtain $\hat{r}^2(t) \sim \mathcal{G}(\frac{3}{2}, 4vt)$. Then, $\hat{r}(t) \sim \text{Nakagami}(\frac{3}{2}, 6vt)$. According to the characteristic of Nakagami- m distribution, the CDF and PDF can be directly given by

$$\mathcal{F}_{\hat{r}(t)}(w) = 1 - \frac{2}{\sqrt{\pi}} \Gamma\left(\frac{3}{2}, \frac{w^2}{4vt}\right) \quad (11)$$

and

$$\mathcal{P}_{\hat{r}(t)}(w) = \frac{w^2}{2\sqrt{\pi} (vt)^{\frac{3}{2}}} \exp\left(-\frac{w^2}{4vt}\right). \quad (12)$$

The CDF and PDF of x (a constant parameter), $\mathcal{F}_x(w)$ and $\mathcal{P}_x(w)$, are respectively given by

$$\mathcal{F}_x(w) = \mathcal{H}(w - x) \quad (13)$$

and

$$\mathcal{P}_x(w) = \delta(w - x). \quad (14)$$

Hence, we can arrive at the CDF and PDF expressions of $r_{\text{LOS,BM}}(t)$ in (15) and (16), as shown at the bottom of the next page.

Considering the 3D BM mobility, the CDF and PDF of $r_{\text{LOS,BM}}(t)$ (i.e., mobile LOS drone distance) are formulated as (15) and (16), respectively.

$$\begin{aligned} &\mathcal{F}_{r_{\text{LOS,BM}}(t)}(w) \\ &= \left(1 + \frac{2}{\sqrt{\pi}} \Gamma\left(\frac{3}{2}, \frac{w^2}{4vt}\right) (\mathcal{H}(w - D) - 1)\right) \mathcal{H}(w) \end{aligned} \quad (15)$$

Next, we will derive the CDF and PDF of $r_{\text{NLOS,BM}}(t)$ based on the 3D BM mobility model, where $r_{\text{NLOS,BM}}(t)$ indicates the distance to the origin under NLOS propagation at time t . Recall the mobility model for NLOS drone, $r_{\text{NLOS,BM}}(t) = \max(D, \min(R, \hat{r}(t)))$. We can express the corresponding CDF as [49]

$$\mathcal{F}_{r_{\text{NLOS,BM}}(t)}(w) = \mathcal{F}_D(w) \mathcal{F}_{\min(R, \hat{r}(t))}(w), \quad (17)$$

where $\mathcal{F}_D(w)$ indicates the CDF of constant D , $\mathcal{F}_{\min(R, \hat{r}(t))}(w)$ represents the CDF of function $\min(R, \hat{r}(t))$.

In formula (11) and formula (13), we derived the probability distribution of $\mathcal{F}_{\hat{r}(t)}(w)$, $\mathcal{F}_R(w)$ and $\mathcal{F}_D(w)$. Hence, with some basic numerical steps, we can arrive at the CDF and PDF expressions of $r_{\text{NLOS,BM}}(t)$ in (18) and (19), as shown at the bottom of the next page.

Considering the 3D BM mobility, the CDF and PDF of $r_{\text{NLOS,BM}}(t)$ (i.e., mobile NLOS drone distance) are formulated as (18) and (19), respectively.

$$\begin{aligned} &\mathcal{F}_{r_{\text{NLOS,BM}}(t)}(w) \\ &= \left(1 + \frac{2}{\sqrt{\pi}} \Gamma\left(\frac{3}{2}, \frac{w^2}{4vt}\right) (\mathcal{H}(w - R) - 1)\right) \mathcal{H}(w - D) \end{aligned} \quad (18)$$

Also, we can obtain the CDF and PDF for LOS and NLOS based on homogeneous PPP with density λ . The distribution of BM movement distance is equivalent to the distribution of the nearest drone distance following homogeneous PPP with density λ [48], and we can obtain the CDF of homogeneous PPP in (5), where $K_{\text{LOS}} = \frac{4}{3}\pi D^3 \lambda$, so (5) is identical to (15) [48]. Then, by solving this equation, we can obtain the density for LOS as shown at the bottom of the next page (20). Also, a similar approach can be used to obtain the density for NLOS given in (21), as shown at the bottom of the next page.

2) DETERMINISTIC MOTION

In this part, the characteristic of the deterministic motion (i.e., moving towards a target at a constant speed) is studied. Once the transmission link has been established, the serving drone cannot move toward other targets. The corresponding Euclidean distance to the origin (i.e., $t > 0$) can be given by

$$\hat{r}(t) = r_0 - vt \quad (22)$$

where v indicates a constant (e.g., representing velocity) and r_0 denotes the distance at time $t = 0$. It should be noted that a positive value v means same direction and vice versa. Then, we will derive the CDF and PDF of $r_{\text{LOS,DM}}(t)$, where $r_{\text{LOS,DM}}(t)$ indicates the distance to the origin under LOS propagation at time t . Recall the deterministic mobility model for LOS drone, $r_{\text{LOS,DM}}(t) = \max(0, \min(D, \hat{r}(t)))$, where $\hat{r}(t) = r_0 - vt$. Consider $Y = aX - b$, where Y and X are random variables, and a and b are constants. Hence, based on this linear transformation, the PDF of Y is constructed as [30]

$$\mathcal{P}_Y(y) = \frac{1}{|a|} \mathcal{P}_X\left(\frac{y - b}{a}\right). \quad (23)$$

Then, the CDF and PDF of $\hat{r}_{\text{LOS}}(t)$ can be respectively formulated as

$$\mathcal{F}_{\hat{r}_{\text{LOS}}(t)}(w) = 1 - \left(1 - \frac{(vt + w)^3}{D^3}\right)^{K_{\text{LOS}}} \quad (24)$$

and

$$\mathcal{P}_{\hat{r}_{\text{LOS}}(t)}(w) = \frac{3(vt + w)^2 K_{\text{LOS}}}{D^3} \left(1 - \frac{(vt + w)^3}{D^3}\right)^{K_{\text{LOS}} - 1} \quad (25)$$

The CDF and PDF of $\hat{r}_{\text{NLOS}}(t)$ can be respectively formulated as

$$\mathcal{F}_{\hat{r}_{\text{NLOS}}(t)}(w) = 1 - \left(1 - \frac{(vt + w)^3 - D^3}{R^3 - D^3}\right)^{K_{\text{NLOS}}} \quad (26)$$

and

$$\begin{aligned} &\mathcal{P}_{\hat{r}_{\text{NLOS}}(t)}(w) \\ &= \frac{3(vt + w)^2 K_{\text{NLOS}}}{R^3 - D^3} \left(1 - \frac{(vt + w)^3 - D^3}{R^3 - D^3}\right)^{K_{\text{NLOS}} - 1}. \end{aligned} \quad (27)$$

Using the above, together with the aid of similar expression in (10) and (17), we can arrive at the results in (28) and (30).

Considering the deterministic motion mobility, the CDF and PDF of $r_{\text{LOS,DM}}(t)$ are formulated in (28) and (29), as shown at the bottom of the next page.

$$\begin{aligned} &\mathcal{F}_{r_{\text{LOS,DM}}(t)}(w) \\ &= \mathcal{H}(w) \left(1 + (\mathcal{H}(w - D) - 1) \left(1 - \frac{(vt + w)^3}{D^3}\right)^{K_{\text{LOS}}}\right) \end{aligned} \quad (28)$$

Considering the deterministic motion mobility, the CDF and PDF of $r_{\text{NLOS,DM}}(t)$ are formulated in (30) and (31), as shown at the bottom of the next page.

$$\mathcal{F}_{r_{\text{NLOS,DM}}(t)}(w) = \mathcal{H}(w - D) \left(1 + (\mathcal{H}(w - R) - 1) \times \left(\frac{R^3 - (vt + w)^3}{R^3 - D^3} \right)^{K_{\text{NLOS}}} \right) \quad (30)$$

E. SINR FORMULATION

Using the formula above, the received SINR can be formulated as

$$\text{SINR} = \frac{X}{I_{\text{agg}} + \sigma^2} \quad (32)$$

where

$$X = pg_b L(r_b) \quad (33)$$

and

$$I_{\text{agg}} = \sum_{i \in \Phi \setminus \{b\}} pg_i L(r_i) \quad (34)$$

with σ^2 and p used to indicate the noise variance and transmit power, respectively.

III. PERFORMANCE ANALYSIS

In this section, we will analysis the performances of spectral efficiency and outage probability.

First, the spectral efficiency (in nat/s/Hz) of the typical user is expressed as (35), as shown at the bottom of the next page [50], where $\text{Pr}[\text{LOS}, r = r_b]$ and $\text{Pr}[\text{NLOS}, r = r_b]$ denote the distance-dependent LOS and NLOS probabilities given in (3). $\mathcal{P}_{r_b}(r)$ and $\mathcal{F}_{\text{SINR}|r_b=r}[\gamma]$ indicate the PDF of the transmitter-receiver distance (expressed in (6) and (8)), and the CDF of the SINR conditioned on $r_b = r$.

By using MGF methodology, the spectral efficiency of the typical user conditioned on transmitter-receiver distance r_b is obtained.

$$\begin{aligned} & \mathbb{E} [\log(1 + \text{SINR})] \\ &= \int_0^R \int_0^{+\infty} \left[(1 - \mathcal{M}_{X|r_b}(z)) \times \mathcal{M}_{I_{\text{agg}}|r_b}(z) \right] \\ & \quad \times \frac{\exp(-z\sigma^2)}{z} \mathcal{P}_{r_b}(r) dz dr \end{aligned} \quad (36)$$

where $\mathcal{M}_{X|r_b}(z)$ can be easily derived and $\mathcal{M}_{I_{\text{agg}}|r_b}(z)$ can be obtained by the LT of aggregate interference. The $\mathcal{M}_{X|r_b}(z)$ conditioned on LOS and NLOS are respectively given by

$$\mathcal{M}_{X|r_b}(z) = \left(1 + \frac{zpL(r_b)}{m_L} \right)^{-Mm_L} \quad (37)$$

$$\begin{aligned} \mathcal{P}_{r_{\text{LOS,BM}}(t)}(w) &= \left(1 + \frac{2}{\sqrt{\pi}} \Gamma \left(\frac{3}{2}, \frac{w^2}{4vt} \right) (\mathcal{H}(w - D) - 1) \right) \delta(w) \\ & \quad + \left(\frac{2}{\sqrt{\pi}} \Gamma \left(\frac{3}{2}, \frac{w^2}{4vt} \right) \delta(w - D) - \frac{w^2}{2\sqrt{\pi}(vt)^{\frac{3}{2}}} \exp \left(-\frac{w^2}{4vt} \right) (\mathcal{H}(w - D) - 1) \right) \mathcal{H}(w). \end{aligned} \quad (16)$$

$$\begin{aligned} \mathcal{P}_{r_{\text{NLOS,BM}}(t)}(w) &= \left(1 + \frac{2}{\sqrt{\pi}} \Gamma \left(\frac{3}{2}, \frac{w^2}{4vt} \right) (\mathcal{H}(w - R) - 1) \right) \delta(w - D) \\ & \quad + \left(\frac{2}{\sqrt{\pi}} \Gamma \left(\frac{3}{2}, \frac{w^2}{4vt} \right) \delta(w - R) - \frac{1}{2\sqrt{\pi}w} \left(\frac{w^2}{vt} \right)^{\frac{3}{2}} \exp \left(-\frac{w^2}{4vt} \right) (\mathcal{H}(w - R) - 1) \right) \mathcal{H}(w - D). \end{aligned} \quad (19)$$

$$\lambda = \frac{3 \log \left(1 - \frac{\mathcal{H}(w)}{\sqrt{\pi}} \left(2\mathcal{H}(w - D) \Gamma \left(\frac{3}{2}, \frac{w^2}{4vt} \right) - 2\Gamma \left(\frac{3}{2}, \frac{w^2}{4vt} \right) + \sqrt{\pi} \right) \right)}{4\pi D^3 \log \left(1 - \frac{w^3}{D^3} \right)} \quad (20)$$

$$\lambda = \frac{3 \log \left(1 - \frac{\mathcal{H}(w-D)}{\sqrt{\pi}} \left(2\mathcal{H}(w - R) \Gamma \left(\frac{3}{2}, \frac{w^2}{4vt} \right) - 2\Gamma \left(\frac{3}{2}, \frac{w^2}{4vt} \right) + \sqrt{\pi} \right) \right)}{4\pi (R^3 - D^3) \log \left(1 - \frac{w^3 - D^3}{R^3 - D^3} \right)}. \quad (21)$$

$$\begin{aligned} \mathcal{P}_{r_{\text{LOS,DM}}(t)}(w) &= \delta(w) + (\mathcal{H}(w) \delta(w - D) + (\mathcal{H}(w - D) - 1)\delta(w)) \left(1 - \frac{(vt + w)^3}{D^3} \right)^{K_{\text{LOS}}} \\ & \quad - \mathcal{H}(w) (\mathcal{H}(w - D) - 1) \frac{3 K_{\text{LOS}}(vt + w)^2}{D^3} \left(1 - \frac{(vt + w)^3}{D^3} \right)^{K_{\text{LOS}}-1}. \end{aligned} \quad (29)$$

and

$$\mathcal{M}_{X|r_b}(z) = \left(1 + \frac{zpL(r_b)}{m_N}\right)^{-M}. \quad (38)$$

After deriving the expression of spectral efficiency, we will deduct the expression of outage probability.

The CDF of the SINR (outage probability) conditioned on $r_o = r$ is given by (39), as shown at the bottom of the next page, with (i) written using the identity $x^n f(x) \equiv (-1)^n \frac{d^n}{ds^n} \mathcal{L}_f(x)[s]$ (a property of LT function). Hence, the CDF of the SINR (outage probability) of the typical user can be expressed by (40), as shown at the bottom of the next page, where $\Pr[\text{LOS}, r = r_b]$ and $\Pr[\text{NLOS}, r = r_b]$ denote the distance-dependent LOS and NLOS probabilities given in (3).

Next, we will obtain the LT of the aggregate interference under LOS and NLOS propagation by invoking the probability generating functional (PGFL).

The LT of the aggregate interference under LOS and NLOS propagation are respectively given by

$$\begin{aligned} \mathcal{L}_{I_{\text{LOS}}}[s] &= \mathbb{E}[\exp(-sI_{\text{LOS}})] \\ &= \mathbb{E}\left[\exp\left(-s \sum_{i \in \Phi_{\text{LOS}} \setminus \{b\}} pg_i L_{\text{LOS}}(r_i)\right)\right] \\ &= \mathbb{E}_{\Phi_{\text{LOS}}}\left[\prod_{i=1}^{K_{\text{LOS}}} \frac{1}{\left(1 + \frac{sp}{m_L} L_{\text{LOS}}(r_i)\right)^{m_L}}\right] \\ &= \mathbb{E}_{r_i}\left[\left(\frac{1}{\left(1 + \frac{sp}{m_L} L_{\text{LOS}}(r_i)\right)^{m_L}}\right)^{K_{\text{LOS}}}\right] \end{aligned} \quad (41)$$

and

$$\mathcal{L}_{I_{\text{NLOS}}}[s] = \mathbb{E}[\exp(-sI_{\text{NLOS}})]$$

$$\begin{aligned} &= \mathbb{E}\left[\exp\left(-s \sum_{i \in \Phi_{\text{NLOS}} \setminus \{b\}} pg_i L_{\text{NLOS}}(r_i)\right)\right] \\ &= \mathbb{E}_{\Phi_{\text{NLOS}}}\left[\prod_{i=1}^{K_{\text{NLOS}}} \mathbb{E}_{g_i}[\exp(-spg_i L_{\text{NLOS}}(r_i))]\right] \\ &= \mathbb{E}_{\Phi_{\text{NLOS}}}\left[\prod_{i=1}^{K_{\text{NLOS}}} \frac{1}{1 + spL_{\text{NLOS}}(r_i)}\right] \\ &= \mathbb{E}_{r_i}\left[\left(\frac{1}{1 + spL_{\text{NLOS}}(r_i)}\right)^{K_{\text{NLOS}}}\right] \end{aligned} \quad (42)$$

Hence, the LT of the aggregate interference under LOS and NLOS propagation are respectively given by

$$\begin{aligned} \mathcal{L}_{I_{\text{LOS}}}[s] &= \int_r^R \Pr[\text{LOS}, r_i = y] \left(\frac{1}{\left(1 + \frac{sp}{m_L} L_{\text{LOS}}(y)\right)^{m_L}}\right)^{K_{\text{LOS}}} \\ &\quad \times \frac{3y^2}{R^3 - r^3} dy \end{aligned} \quad (43)$$

and

$$\begin{aligned} \mathcal{L}_{I_{\text{NLOS}}}[s] &= \int_r^R \Pr[\text{NLOS}, r_i = y] \left(\frac{1}{1 + spL_{\text{NLOS}}(y)}\right)^{K_{\text{NLOS}}} \\ &\quad \times \frac{3y^2}{R^3 - r^3} dy. \end{aligned} \quad (44)$$

IV. NUMERICAL RESULTS

In this section, we analyze the performances of drone mobile networks under the path-loss based strategies. We provide some examples to verify the proposed analytical framework, and compare the Monte-Carlo simulations with theoretical results.

$$\begin{aligned} \mathcal{P}_{r_{\text{NLOS,DM}}(t)(w)} &= \delta(w - D) \left(1 + (\mathcal{H}(w - R) - 1) \left(\frac{R^3 - (vt + w)^3}{R^3 - D^3}\right)^{K_{\text{NLOS}}}\right) + \mathcal{H}(w - D) \\ &\quad \times \left(\delta(w - R) \left(\frac{R^3 - (vt + w)^3}{R^3 - D^3}\right)^{K_{\text{NLOS}}} - \frac{3K_{\text{NLOS}}(\mathcal{H}(w - R) - 1)(vt + w)^2}{R^3 - D^3} \left(\frac{R^3 - (tv + w)^3}{R^3 - D^3}\right)^{K_{\text{NLOS}} - 1}\right). \end{aligned} \quad (31)$$

$$\begin{aligned} &\mathbb{E}[\log(1 + \text{SINR})] \\ &= \int_0^{+\infty} \Pr[\log(1 + \text{SINR}) > \gamma] d\gamma \\ &= \mathbb{E}_{r_b} \left[\int_0^{+\infty} \Pr[\text{LOS}, r_b = r] \Pr[\log(1 + \text{SINR}) > \gamma | r_b = r] + \Pr[\text{NLOS}, r_b = r] \Pr[\log(1 + \text{SINR}) > \gamma | r_b = r] d\gamma \right] \\ &= \int_0^R \int_0^{+\infty} \Pr[\text{LOS}, r_b = r] \frac{1 - \mathcal{F}_{\text{SINR}|r_b=r}[\gamma]}{1 + \gamma} \mathcal{P}_{r_b}(r) + \Pr[\text{NLOS}, r_b = r] \frac{1 - \mathcal{F}_{\text{SINR}|r_b=r}[\gamma]}{1 + \gamma} \mathcal{P}_{r_b}(r) d\gamma dr \end{aligned} \quad (35)$$

TABLE 1. Simulations parameters.

Parameter	Symbol	Value
Path-loss parameter in LOS link	α_L	3
Path-loss parameter in NLOS link	α_N	4
UAV Transmit power	p	20 W
Bandwidth	BW	20 MHz
Sphere radius	R	100 m
Critical distance	D	18 m
Carrier frequency	f_c	30 GHz

A. MONTE-CARLO SIMULATIONS

The method utilized for evaluating the spectral efficiency and outage probability in single-user multi-antenna drone mobile networks with CB using Monte-Carlo simulations are presented below.

- 1) Set the number of PPP deployment density λ , Nakagami- m fading parameter m_L and m_N , serving drone velocity v , transmit power p , number of antennas M , path-loss exponent α_L , α_N , and noise variance σ^2 .
- 2) Define the 3D finite region radius R around the typical user o located at the origin and the critical distance D .
- 3) Generate the statistical number of LOS drone and NLOS drone using Poisson distribution with average $\bar{K}_{LOS} = \frac{4}{3}\pi D^3 \lambda$ and $\bar{K}_{NLOS} = \frac{4}{3}\pi (R^3 - D^3) \lambda$. Then, uniformly-deployed in the region of volume $\frac{4}{3}\pi D^3$ and $\frac{4}{3}\pi (R^3 - D^3)$, respectively.
- 4) Generate independent fading channel power gains from all deployed drones to the typical user.
- 5) Associate the typical receiver to the nearest transmitter drone based on path-loss strategy. Then, the serving drone will move according to three mobility models,

and the intended signal power X during the movement process can be obtained.

- 6) Calculate the aggregate network interference on the typical user I_{agg} using the sum of received signal powers from all remaining interfering links.
- 7) Obtain the instantaneous SINR and spectral efficiency (nat/s/Hz) of the typical receiver using $SINR = \frac{X}{I_{agg} + \sigma^2}$ and $\log(1 + SINR)$, respectively.
- 8) By repeating the step 3-7 with a large number of times and calculating the averages, we can compute the spectral efficiency and outage probability.

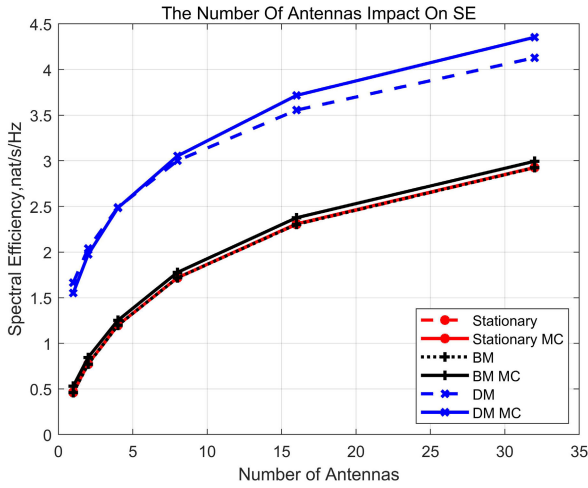
Next, we will explain the theoretical results and Monte-Carlo simulations based on a standard workstations at present time. The execution time for Monte-Carlo simulations which were repeated 20k times over a radius of 100 m required can range from four hours to more than ten hours depending on the network settings. The deployment density, path-loss exponents, mobility model increase the complexity of the Monte-Carlo trials. However, with the presented theoretical framework, similar results can be obtained in few minutes. In this paper, all the parameters are set according to Table 1 unless otherwise stated in the subsequent results analysis. Furthermore, all the parameters in this section are merely chosen to illustrate the performance in an example, and it can be modified to any other values depending on the needs of different scenarios.

B. IMPACT OF NUMBER OF ANTENNAS

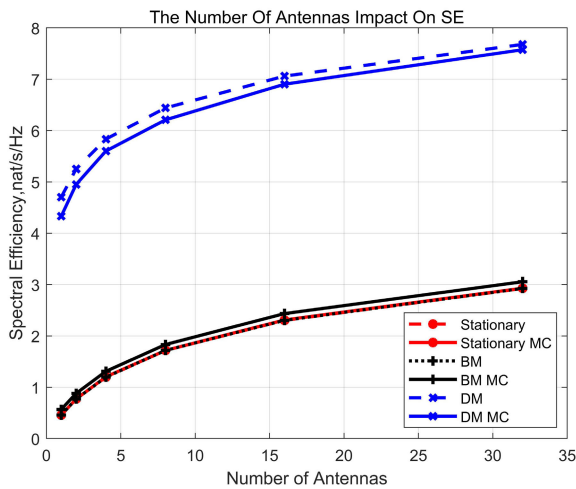
We investigate the effect of the number of antennas on the SE in Fig. 2. Here, we consider three mobility models, consisting (i) stationary model (red curves), (ii) deterministic mobility

$$\begin{aligned}
 \mathcal{F}_{SINR|r_b=r}[\gamma] &= \Pr[LOS, r_b = r] \Pr[SINR \leq \gamma | LOS, r_b = r] \\
 &\quad + \Pr[NLOS, r_b = r] \Pr[SINR \leq \gamma | NLOS, r_b = r] \\
 &= 1 - \Pr[LOS, r_b = r] \Pr[SINR > \gamma | LOS, r_b = r] \\
 &\quad - \Pr[NLOS, r_b = r] \Pr[SINR > \gamma | NLOS, r_b = r] \\
 &= 1 - \Pr[LOS, r_b = r] \Pr\left[g_b > \frac{\gamma}{pL_{LOS}(r)} (I_{LOS} + I_{NLOS} + \sigma^2) \mid LOS, r_o = r \right] \\
 &\quad - \Pr[NLOS, r_b = r] \Pr\left[g_b > \frac{\gamma}{pL_{NLOS}(r)} (I_{NLOS} + \sigma^2) \mid NLOS, r_o = r \right] \\
 &\stackrel{(i)}{=} 1 - \Pr[LOS, r_b = r] \sum_{n=0}^{m_L M - 1} \left\{ \frac{(-s)^n}{n!} \frac{d^n}{ds^n} \exp(-s\sigma^2) \mathcal{L}_{I_{LOS}}[s] \mathcal{L}_{I_{NLOS}}[s] \right\}_{s=\frac{m_L \gamma}{pL_{LOS}(r)}} \\
 &\quad - \Pr[NLOS, r_b = r] \sum_{n=0}^{M-1} \left\{ \frac{(-s)^n}{n!} \frac{d^n}{ds^n} \exp(-s\sigma^2) \mathcal{L}_{I_{NLOS}}[s] \right\}_{s=\frac{\gamma}{pL_{NLOS}(r)}} \tag{39}
 \end{aligned}$$

$$\begin{aligned}
 \mathcal{F}_{SINR}[\gamma] &= 1 - \int_0^R \left(\Pr[LOS, r_b = r] \sum_{n=0}^{m_L M - 1} \left\{ \frac{(-s)^n}{n!} \frac{d^n}{ds^n} \exp(-s\sigma^2) \mathcal{L}_{I_{LOS}}[s] \mathcal{L}_{I_{NLOS}}[s] \right\}_{s=\frac{m_L \gamma}{pL_{LOS}(r)}} \right. \\
 &\quad \left. + \Pr[NLOS, r_b = r] \sum_{n=0}^{M-1} \left\{ \frac{(-s)^n}{n!} \frac{d^n}{ds^n} \exp(-s\sigma^2) \mathcal{L}_{I_{NLOS}}[s] \right\}_{s=\frac{\gamma}{pL_{NLOS}(r)}} \right) \mathcal{P}_{r_b}(r) dr \tag{40}
 \end{aligned}$$



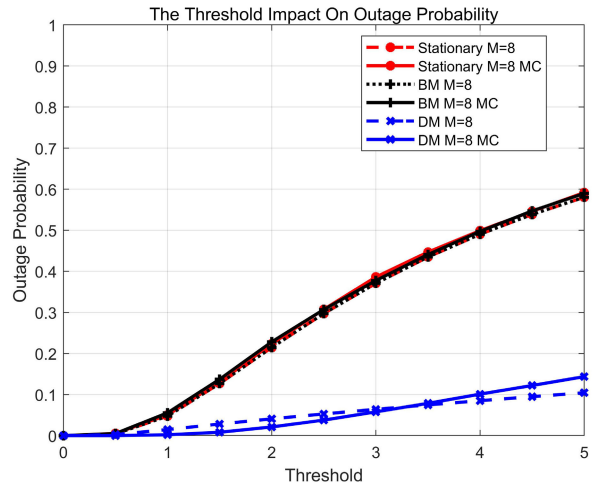
(a)



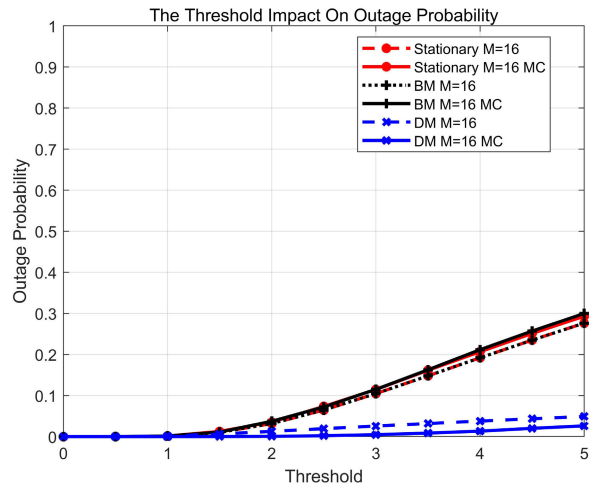
(b)

FIGURE 2. Spectral efficiency against different number of antennas. System parameters are: $m_L = 3$, $m_N = 1$, $R = 100$ m, $D = 18$ m, $\lambda = 10^{-5} / m^3$, $v = 3$ m/s, $p = 20$ W, $\epsilon = \epsilon_{LOS} = 1$ dB, $\epsilon = \epsilon_{NLOS} = 20$ dB. (a) Time $t = 1$ s. (b) Time $t = 3$ s.

model (blue curves), and (iii) 3D Brownian mobility model (black curves). In order to compare the network performances at different time, we obtain the SE values at time $t = 1$ s and $t = 3$ s with different mobility models, respectively. The reason is because the serving drone is just starting to move according mobility models at time $t = 1$ s, and the drone mobile networks will have a better network performance at time $t = 3$ s. As it can be seen in Fig. 2(a) and Fig. 2(b), the SE performance in all mobility models always increases in the number of antennas. Furthermore, our findings show that drone mobile networks applied CB can obtain a better performance with more transmit antennas. Next, the effect of connecting threshold on outage probability with 8 and 16 antennas are investigated in Fig. 3(a) and Fig. 3(b), respectively. We can observe that the outage probability will



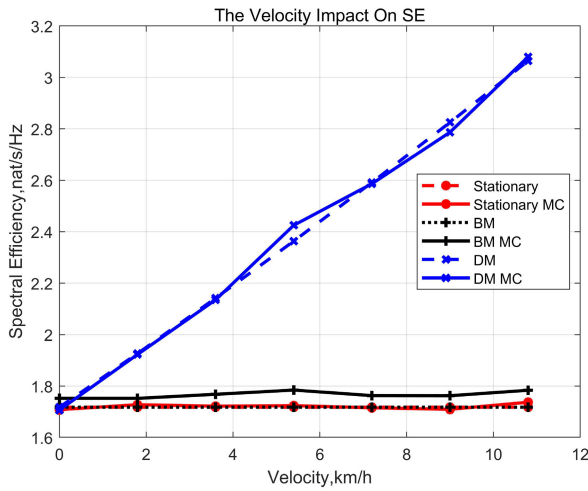
(a)



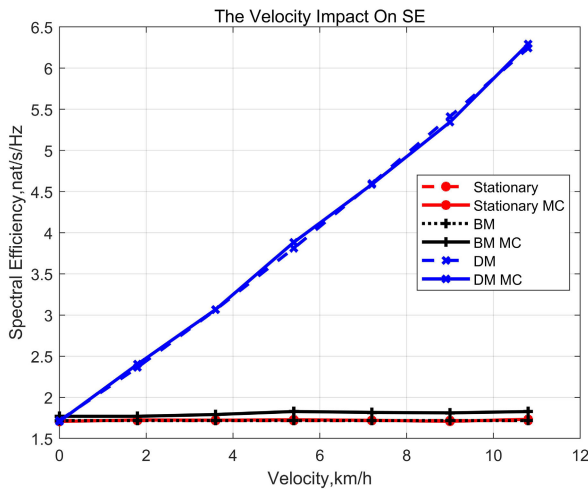
(b)

FIGURE 3. Outage probability against threshold with different number of antennas. System parameters are: $m_L = 3$, $m_N = 1$, $R = 100$ m, $D = 18$ m, $\lambda = 10^{-5} / m^3$, $v = 3$ m/s, $p = 20$ W, $t = 3$ s, $\epsilon = \epsilon_{LOS} = 1$ dB, $\epsilon = \epsilon_{NLOS} = 20$ dB. (a) Number of antennas $M = 8$. (b) Number of antennas $M = 16$.

increase and become stable with the increasing of threshold in all mobility models. The reason is because the serving drone will change to LOS condition under deterministic mobility model at time $t = 3$ s, but the serving drone still under NLOS condition in other mobility models. It is important to note that communication under LOS condition can enhance the network performance. In addition, it can be observed that the outage probability performance under $M = 16$ is better than $M = 8$, that phenomenon fits the conclusion in Fig. 2. In Fig. 2 and Fig. 3, we can observe that the multi-antenna communications will increase the drone mobile performances. The reason is because the multi-antenna communications will improve the channel power gain, and hence, the useful signal power will be stronger, whilst the interference level remains the same. This trend highlights the important role of multi-antenna in



(a)



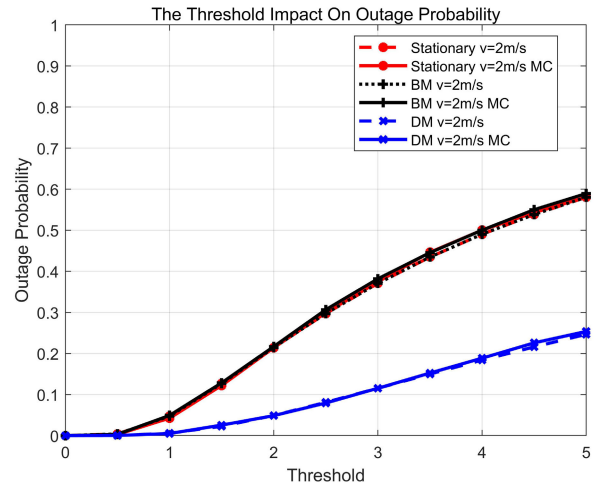
(b)

FIGURE 4. The serving drone velocity impact on Spectral efficiency. System parameters are: $M = 8, m_L = 3, m_N = 1, R = 100 \text{ m}, D = 18 \text{ m}, \lambda = 10^{-5} / \text{m}^3, p = 20 \text{ W}, \epsilon = \epsilon_{\text{LOS}} = 1 \text{ dB}, \epsilon = \epsilon_{\text{NLOS}} = 20 \text{ dB}$. (a) Time $t = 1 \text{ s}$. (b) Time $t = 3 \text{ s}$.

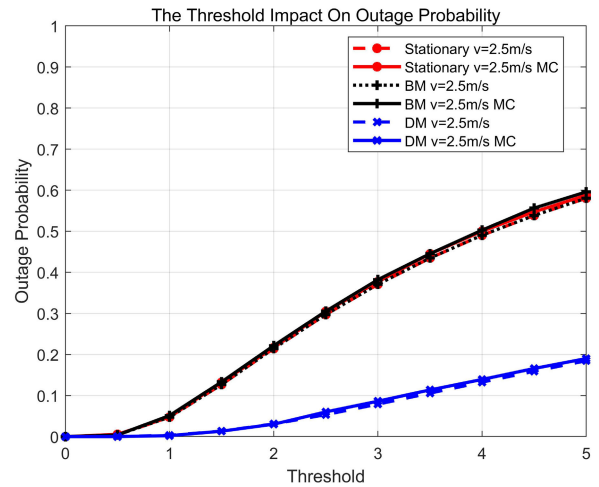
the drone mobile networks. In addition, it should be noted that 3D BM is the disordered mobility model, and deterministic motion is the ideal mobility model, in practical. So we can say that the performance of 3D BM is the lower bound of the reality drone networks and the performance of deterministic model is the upper bound. This conclusion will help to simplify the drone mobile networks in practical (i.e., Markov-motion model).

C. IMPACT OF DRONE VELOCITY

The effect of the serving drone velocity on SE under three mobility models at time $t = 1$ and time $t = 3$ are demonstrated in Fig. 4(a) and Fig. 4(b). As we can find that the SE under deterministic mobility model increase in the serving drone velocity, but the velocity has little impact on SE under stationary and 3D BM model. Depending on the characteris-



(a)



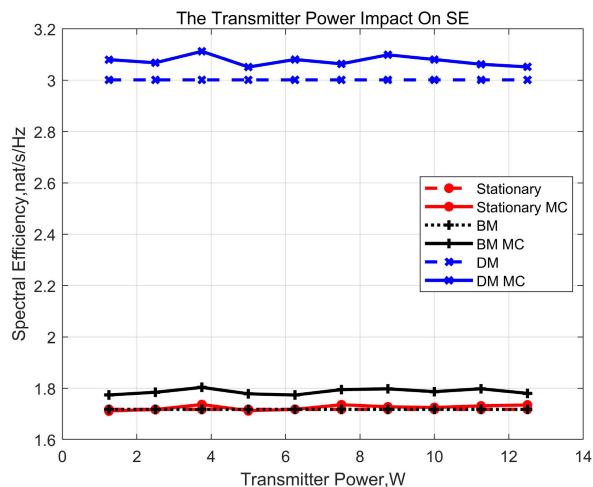
(b)

FIGURE 5. The threshold impact on Outage probability with different serving drone velocities. System parameters are: $M = 8, m_L = 3, m_N = 1, R = 100 \text{ m}, D = 18 \text{ m}, \lambda = 10^{-5} / \text{m}^3, p = 20 \text{ W}, t = 3 \text{ s}, \epsilon = \epsilon_{\text{LOS}} = 1 \text{ dB}, \epsilon = \epsilon_{\text{NLOS}} = 20 \text{ dB}$. (a) serving drone velocity $v = 2 \text{ m/s}$. (b) serving drone velocity $v = 2.5 \text{ m/s}$.

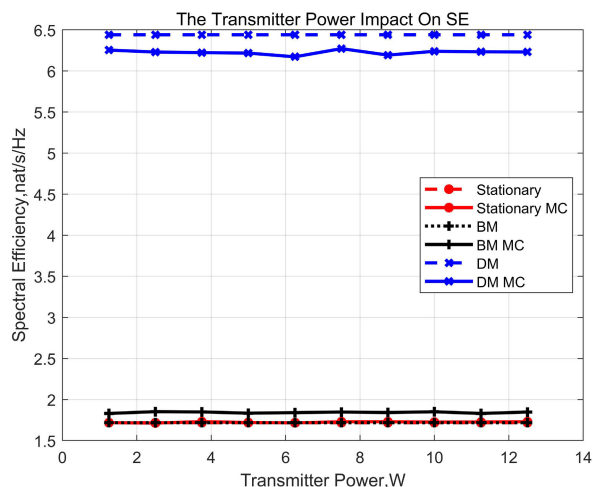
tics of different mobility models, the distance between typical user and serving drone will decrease with the increasing of serving drone velocity. On the other hand, it is important to note that the distance has little change under stationary and 3D BM model. We depict the impact of connecting threshold on outage probability with $v = 7.2 \text{ km/h}$ and $v = 9 \text{ km/h}$ in Fig. 5(a) and Fig. 5(b). As expected, the velocity of drones will increase the drone mobile performances. Although the serving drone velocity will enhance the performance of drone mobile networks in practical, but it should be noted that strike a balance between secure and performance. However, this beyond the scope of this article.

D. IMPACT OF TRANSMITTER POWER

Finally, we proceed by studying the effect of transmitter power on SE under three mobility models in Fig. 6.



(a)



(b)

FIGURE 6. The transmitter power impact on Spectral efficiency. System parameters are: $M = 8$, $m_L = 3$, $m_N = 1$, $R = 100$ m, $D = 18$ m, $\lambda = 10^{-5}$ / m^3 , $v = 3$ m/s, $\epsilon = \epsilon_{LOS} = 1$ dB, $\epsilon = \epsilon_{NLOS} = 20$ dB. (a) Time $t = 1$ s. (b) Time $t = 3$ s.

As expected, we can observe that the transmitter power has little impact on SE. The reason is because the intended signal power improve with the increasing of transmitter power, but the aggregate interference power also increase. Furthermore, it should be noted that the noise variance is small comparing with intended signal and aggregate interference, so the spectral efficiency and outage probability will remain stable at different transmit power. Hence, we can effectively allocate the limited energy of battery to other requirements to boost the overall performance of drone mobile networks in practical.

V. CONCLUSION

In this paper, a system-level analysis of the drone mobile networks is presented. Aiming to provide meaningful insights into the performance drone mobile networks in practice, we provided a framework for the study of mobile drone

networks considering a number of mobility models, including a 3D Brownian motion model. Then, the expressions of SINR, spectral efficiency and coverage probability are obtained by using mathematical tools provided by stochastic geometry. Furthermore, a novel bounded formulations are given towards computing a lower-bound and upper-bound for the spectral efficiency and outage probability of the considered drone mobile networks. The Monte-Carlo simulation results validate the theoretical derivation and confirm the feasibility of a number of proposed mobility models. As for future work, one direction is to combine NOMA and full-duplex to improve the performances of drone mobile networks. Another direction is to evaluate and optimize the energy efficiency for drone mobile networks with considerations of simultaneous wireless information and power transfer (SWIPT). In addition, the performance of drone mobile networks considering shadowing and terrestrial base stations is worth being developed to satisfy the demands of wireless networks.

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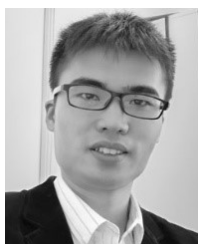


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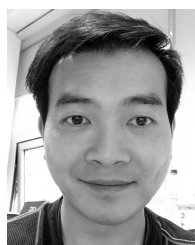


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