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# Deadlock Control and Fault Detection and Treatment in Reconfigurable Manufacturing Systems Using Colored Resource-Oriented Petri Nets Based on Neural Network

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**ABSTRACT** A reconfigurable manufacturing system (RMS) means that it can be reconfigured and become more complex during its operation. In RMSs, deadlocks may occur because of sharing of reliable or unreliable resources. Various deadlock control techniques are proposed for RMSs with reliable and unreliable resources. However, when the system is large-sized, the complexity of these techniques will increase. To overcome this problem, this paper develops a four-step deadlock control policy for the detection and treatment of faults in an RMS. In the first step, a colored resource-oriented timed Petri net (CROTPN) is designed for rapid and effective reconfiguration of the RMS without considering resource failures. In the second step, “sufficient and necessary conditions” for the liveness of a CROTPN are introduced to guarantee that the model is live. The third step considers the problems of failures of all resources in the CROTPN model and guarantees that the model is reliable by designing a common recovery subnet and adding it to the obtained CROTPN model at the second step. The fourth step designs a new hybrid method that combines the CROTPN with neural networks for fault detection and treatment. A simulation is performed using the GPenSIM tool to evaluate the proposed policy under the RMS configuration changes and the results are compared with the existing approaches in the literature. It is shown that the proposed approach can handle any complex RMS configurations, solve the deadlock problem in an RMS, and detect and treat failures. Furthermore, is simpler in its structure.

**INDEX TERMS** Simulation, modeling, deadlock avoidance, colored Petri net, reconfigurable manufacturing system, neural network.

## I. INTRODUCTION

The recent innovation in manufacturing is a reconfigurable manufacturing system (RMS). An RMS can be described as a series of discrete events, which characterizes a system. An RMS can modify its system structure, such as adding new machines, products, handling devices, and the rework of the process. To achieve these modifications, it requires a control program with a variety of features including quickness, validity, cost-effectiveness, and flexibility [1], [2]. In RMSs, when

resources are shared, some operations may not be conducted because of deadlocks. Thus, deadlock control is necessary for RMSs. Moreover, in real world, the occurrence of resource faults may lead to new deadlocks. In general, faults are described as disturbances, failures, or mistakes that cause unbearable or unwanted resource behavior and thus cannot be ignored in the RMS. It is important to perform an early diagnosis and treatment of faults on machines and equipment to maintain efficiency and avoid performance degradations. It is necessary to design a deadlock prevention method in the RMS under unreliable resources, which can detect and treat faults.

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Petri nets (PNs) are an excellent mathematical modeling tool widely used for deadlock control in automated manufacturing systems (AMSs) [1], [3]. PNs can be used to model the dynamic behaviors, e.g., concurrency, synchronization, causal dependence, sequencing, and conflict in automated manufacturing systems. Many policies have been developed in the literature based on Petri nets, focusing on three strategies: prevention of deadlocks, avoidance of deadlocks, and detection and recovery of deadlocks [4], [5]. Most of these policies assume that the resources in automated manufacturing systems are reliable [6]–[13], and others assume that they are unreliable [14]–[25]. Two analysis techniques in PNs are used to design deadlock control policies: reachability graph analysis [26]–[28] and structural analysis [3], [6]. In addition, three criteria are needed to design and evaluate the supervisor of AMS, which include structural complexity that leads to design a supervisor with a number of monitors [3], [7], [29], computational complexity that means a supervisor can be implemented on small and large sized systems [3], [30], and behavioral permissiveness that leads to improve the time performance (utilization, throughput, and throughput time) of the system [4], [25], [31].

Several studies have been proposed on deadlock control, faults diagnosis and treatment for unreliable resources in AMSs over the past several years. Two policies for one-unit resource allocation systems with unreliable resources are developed in [16]. Liu *et al.* propose deadlock control approaches for AMSs under unreliable resources using divide-and-conquer [18], a reachability graph partition approach [23], a  $\max'$ -controlled siphon control method, and an elementary siphons approach [32]. Li *et al.* [33] propose a two-step deadlock control approach and a legal marking using an elementary siphon approach [34] for AMSs under unreliable resources. In [35], [36], a deadlock control policy based on a strict minimal siphon and colored Petri nets is proposed for AMSs with unreliable resources.

The study in [37] develops a multi-layered feedforward neural network method for defect diagnosis in industrial operations. The work in [38] uses a multi-layer perceptron neural network method to propose a continuous-time approach for a motor system for fault diagnosis and isolation. A distributed Petri net approach is used in [39] to develop a supervisor for fault detection in manufacturing systems operations. Bayesian networks and Petri diagnostic networks are integrated in [40] for defect diagnosis and treatment of malfunctions in automated machines. Miyagi and Riascos [41] integrate standard Petri nets and hierarchical networks; the integrated model is used to model and analyze fault-tolerant systems. Artificial neural networks are used in [42] for fault detection in technical systems, and a fuzzy neural network approach is proposed [43] for fault diagnosis in waste water treatment systems using online sensors. A deadlock control strategy based on neural networks and colored Petri nets is proposed in [44] for AMS for fault diagnosis and treatment under unreliable resources.

It is well-known that various deadlock control approaches have been developed with unreliable resources. However, the disadvantage of these approaches is that when a system is changed completely or a system is large, its size and complexity will also become large. Therefore, this paper aims to develop a four-step deadlock control policy for the RMS for fault diagnosis and treatment under unreliable resources. First, a CROTPN is designed for rapid and effective reconfiguration of the RMS without considering resource failures. Wu and Zhou have made significant contributions in deadlock avoidance using CROPN for AMSs, automated guided vehicles (AGV) systems, and robots [45]–[62]. Sufficient and necessary conditions are introduced at the second step for the liveness of the CROTPN to guarantee that the model is deadlock-free. The third step models the failures of all resources in the CROTPN model, where a single recovery subnet is developed and inserted into the CROTPN model at the second step to guarantee that the model is reliable. The fourth step integrates neural networks with the CROTPN for fault detection and treatment. The contributions of this paper are stated as follows.

1. A new approach is developed to solve the deadlock problem, detect and treat failures; compared with current studies, it can handle any dynamic changes in an RMS.
2. Sufficient and necessary conditions are introduced for the liveness of the CROTPN, which are more succinct than those in [1].
3. A single recovery subnet is developed to handle all resource failures in a CROTPN.
4. A simulation code is designed using the GPenSIM tool for modeling, validation, and performance comparison of the proposed CROTPN; the experimental results are compared with those of the current methods.

The rest of this study is structured as follows. The synthesis of the CROTPN is shown in Section II. Section III presents a deadlock avoidance policy for the CROTPN. The unreliable CROTPN is presented in Section IV. The integration of neural networks and the CROTPN for fault detection and treatment is presented in Section V. The application of the developed approaches is illustrated in Section VI. The conclusions, benefits, drawbacks, and future work of this study are described in Section VII.

## II. DESIGN OF CROTPN

Most of Petri net models [5]–[13], [28], [31], [36], [63]–[70] do not undergo dynamic configurations, such as the addition of new machines, removal of old machines, addition of new products, processing rework, machine breakdowns, or change processing routes induced by the competitive global market. Therefore, a CROTPN is proposed to deal with dynamic configurations in an RMS. This section presents the formal definitions and properties of CROTPN.

A CROTPN is a directed bipartite graph with an initial state called the initial marking. It consists of two sorts of

nodes: places, and transitions. Places are graphically drawn by circles and transitions by bars or boxes. There are directed arcs from a place to a transition or from a transition to a place, which labeled with their weights (positive integers). Each place can hold black dots (tokens), or a nonnegative integer representing their number. A marking assigns tokens to each place to represent a state of the modeled system.

*Definition 1:* An eight-tuple  $N = (P, T, C, I, O, D, K, M_o)$  is said to be a CROTPN if

1.  $P = \{p_o\} \cup \{p_r\} \cup P_R$ , where  $p_o$ ,  $p_r$ , and  $P_R$  are respectively an idle place (a load/unload station), a common material handling resource (transportation resources), and a finite set of resource places with  $P_R = \cup_{i \in m} \{p_i\}$ , where  $m > 0$ ;
2.  $T = \cup_{j \in n} \{t_j\}$  is a finite set of transitions with  $n > 0$ ,  $P \cup T \neq \emptyset$  and  $P \cap T = \emptyset$ ;
3. The sets  $C(p_i)$  and  $C(t_j)$  respectively correspond to the colors of place  $p_i$  and transition  $t_j$ , where
  - a)  $p_i \in P, u_i = |C(p_i)|, C(p_i) = \{a_{i1}, a_{i2}, \dots, a_{iu}\}$
  - b)  $t_j \in T, v_j = |C(t_j)|, C(t_j) = \{b_{j1}, b_{j2}, \dots, b_{jv}\}$
4.  $I(p_i, t_j)(a_{ih}, b_{jk}): C(p_i) \times C(t_j) \rightarrow \mathbf{IN}$  denotes the input function of  $N$  and  $O(p_i, t_j)(a_{ih}, b_{jk}): C(p_i) \times C(t_j) \rightarrow \mathbf{IN}$  denotes the output function of  $N$ , where  $\mathbf{IN} = \{0, 1, 2, \dots\}$ ;
5.  $D$  is a firing delay function that adds to each transition  $t$  the firing delay  $D(t)$  with  $D: T \rightarrow \mathbf{TS}$ , where  $\mathbf{TS} > 0$ ;
6.  $K: P \rightarrow \mathbf{IN}$  denotes the capacity function that allocates the maximal number of tokens to each place  $K(p_i)$ ;
7.  $M_o$  is the initial marking function that allocates the number of tokens to each place with color  $a_{ih}$  with  $M_o: P \rightarrow \mathbf{IN}$ , i.e.,  $M_o = (M_o(p_1, a_{1h}), M_o(p_2, a_{2h}), \dots, M_o(p_m, a_{mh}))^T, a_{ih} \in C(p_i)$ .

*Definition 2:* Let  $N$  be a CROTPN with  $N = (P, T, C, I, O, D, K, M_o)$ . Let  $F = I \cup O$ . Let  $p_i$  and  $t_j$  be respectively a place and a transition node in  $N$ . Then  $\cdot p_i = \{t_j \in T | (t_j, p_i) \in F\}$  and  $p_i \cdot = \{t_j \in T | (p_i, t_j) \in F\}$  are a preset and postset of node  $p_i$ , respectively.  $\cdot t_j = \{p_i \in P | (p_i, t_j) \in F\}$  and  $t_j \cdot = \{p_i \in P | (t_j, p_i) \in F\}$  are the preset and postset of node  $t_j$ , respectively.

Definitions 3 and 4 introduce various CROTPN subclasses that fulfill particular structural conditions.

*Definition 3:* Let  $N$  be a CROTPN with  $N = (P, T, C, I, O, D, K, M_o)$ .  $N$  is said to be an ordinary net if  $I(p_i, t_j)(a_{ih}, b_{jk}) = 1, p_i \in P, t_j \in T, \forall (p_i, t_j) \in F$ . It is called a weighted net if  $\exists p_i \in P, \exists t_j \in T, \forall (p_i, t_j) \in F$  such that  $I(p_i, t_j)(a_{ih}, b_{jk}) > 1$ .

*Definition 4:* Let  $N$  be a CROTPN with  $N = (P, T, C, I, O, D, K, M_o)$ .  $N$  is said to be self-loop free if  $p_i \in P, t_j \in T, \forall (p_i, t_j) \in F, I(p_i, t_j)(a_{ih}, b_{jk}) > 0$  implies that  $O(p_i, t_j)(a_{ih}, b_{jk}) = 0$ .  $N$  contains a self-loop if  $\exists p_i \in P, \exists t_j \in T, \forall (p_i, t_j) \in F, I(p_i, t_j)(a_{ih}, b_{jk}) > 0$  implies that  $O(p_i, t_j)(a_{ih}, b_{jk}) > 0$ .

The enabling and firing rules of transitions can be introduced based on the definitions of the input and output functions, colors, and markings.

*Definition 5:* Let  $N$  be a CROTPN with  $N = (P, T, C, I, O, D, K, M_o)$ . At marking  $M$ , a transition  $t_j$  is said to be enabled with respect to color  $b_{jk} \in C(t_j)$  if

$$\forall p_i \in P, \quad \forall p_i \in \cdot t_j, a_{ih} \in C(p_i), M(p_i, a_{ih}) \geq I(p_i, t_j)(a_{ih}, b_{jk}) \quad (1)$$

and

$$\forall p_i \in P, \quad \forall p_i \in t_j \cdot, a_{ih} \in C(p_i), K(p_i) \geq M(p_i, a_{ih}) + O(p_i, t_j)(a_{ih}, b_{jk}) - I(p_i, t_j)(a_{ih}, b_{jk}) \quad (2)$$

Definition 5 indicates that  $t_j$  is enabled if conditions (1) and (2) are satisfied; then  $t_j$  is called process-enabled and resource-enabled.

At marking  $M$ , if a transition  $t_j$  is enabled, it can fire with respect to color  $b_{jk}$  and the marking changes from  $M$  to  $M'$  based on the following definition.

*Definition 6:* Let  $N$  be a CROTPN with  $N = (P, T, C, I, O, D, K, M_o)$ . At marking  $M$ , an enabled transition  $t_j$  with respect to color  $b_{jk} \in C(t_j)$  is represented by  $M[t]M'$ ;  $M'$  occurs from the firing of  $t_j$  and can be modified from  $M$  to  $M'$  in time interval  $(\alpha_j, \alpha_j + D(t_j))$  as follows:

$$\forall p_i \in P, \quad a_{ih} \in C(p_i), M'(p_i, a_{ih}) = M(p_i, a_{ih}) + O(p_i, t_j)(a_{ih}, b_{jk}) - I(p_i, t_j)(a_{ih}, b_{jk}) \quad (3)$$

where transition  $t_j$  starts firing at time  $\alpha_j$  and the time delay for firing  $t_j$  is  $D(t_j)$ .

The incidence matrix describes the dynamic behaviour of nets, which determines all possible interconnections between places and transitions in a net. The incidence matrix for CROTPN is defined as follows.

*Definition 7:* Let  $N$  be a CROTPN with  $N = (P, T, C, I, O, D, K, M_o)$ . Let  $[N]$  be the incidence matrix of  $N$ , where  $[N]$  is a  $\sum_{i=1}^m u_i \times \sum_{j=1}^n v_j$  matrix with  $[N_{ij}] = O(p_i, t_j)(a_{ih}, b_{jk}) - I(p_i, t_j)(a_{ih}, b_{jk})$ .

*Definition 8:* Let  $N$  be a CROTPN with  $N = (P, T, C, I, O, D, K, M_o)$ . Let  $A$  be a finite set of colors with cardinality  $|A| = l, A \neq \emptyset$ . Let  $Y$  be a set of places function with respect to  $A$ , represented on  $p_i$  as  $Y(p_i): A \times C(p_i) \rightarrow \mathbf{IZ}$ , where  $\mathbf{IZ} = \{\dots, -2, -1, 0, 1, 2, \dots\}$ .

*Definition 9:* Let  $N$  be a CROTPN with  $N = (P, T, C, I, O, D, K, M_o)$ . Let  $\Psi$  be a weighted matrix with  $\Psi = [\Psi_1, \Psi_2, \dots, \Psi_m]^T$  that indicates a set of places, where  $\Psi_i$  is a matrix with  $l \times u_i$  integer dimensions.  $\Psi$  is said to be a place invariant of  $N$  if

$$[N]^T \Psi = \mathbf{0} \quad (4)$$

*Definition 10:* Let  $N$  be a CROTPN with  $N = (P, T, C, I, O, D, K, M_o)$ . Let  $M(C) = (M(p_1, a_{11}), M(p_1, a_{12}), \dots, M(p_1, a_{1u_1}), M(p_2, a_{21}), \dots, M(p_2, a_{2u_2}), \dots, M(p_m, a_{m1}), \dots, M(p_m, a_{mm}))^T$ . If  $\Psi$  is a place invariant of a CROTPN, then we have

$$\forall M \in R(N, M_o), \quad M(C)^T Y = M_o(C)^T Y \quad (5)$$

where  $R(N, M)$  denotes the set of reachable markings from  $M$  in  $N$ .

The behavioral properties in a CROTPN are essential in the analysis and control of a system. Some of the most important behavioral properties are introduced in the following definitions, which are conservativeness, boundedness, safeness, and reversibility.

**Definition 11:** Let  $N$  be a CROTPN with  $N = (P, T, C, I, O, D, K, M_o)$ . Let  $x$  be a positive integer vector with  $x = [x_1, x_2, \dots, x_m]$ .  $N$  is said to be conservative if

$$\forall M \in R(N, M_o), \quad M^T x = M_o^T x \quad (6)$$

**Definition 12:** Let  $N$  be a CROTPN with  $N = (P, T, C, I, O, D, K, M_o)$ .  $N$  is called a bounded net if  $\forall p_i \in P, a_{ih} \in C(p_i), \forall M \in R(N, M_o), M(p_i, a_{ij}) \leq q, q \in \{1, 2, 3, \dots\}$ .  $N$  is called a safe net if  $\forall p_i \in P, a_{ih} \in C(p_i), \forall M \in R(N, M_o), M(p_i, a_{ij}) \leq 1$ .  $N$  is called  $q$ -safe if it is  $q$ -bounded.

**Definition 13:** Let  $N$  be a CROTPN with  $N = (P, T, C, I, O, D, K, M_o)$ . If  $M_o$  is reachable from a marking  $M' \in R(N, M_o)$ , then a marking  $M_o$  is said to be reversible.

Finally, the processing routes of parts in a CROTPN can be described as the following definition.

**Definition 14:** Let  $N$  be a CROTPN with  $N = (P, T, C, I, O, D, K, M_o, PR)$ , where  $PR = \{PR_1, PR_2, PR_3, \dots, PR_\pi\}$  indicates all feasible processing routes for all part types  $\pi$ ,  $\pi = \{1, 2, 3, \dots\}$ .  $PR_i$  is  $R_o \rightarrow R_{i1} \rightarrow R_{i2} \rightarrow \dots \rightarrow R_{i\epsilon_i} \rightarrow R_o$ ,  $\epsilon_i = \{1, 2, 3, \dots\}$ .  $R_o$  indicates an infinite load/unload area of  $N$ , and  $R_i (i \neq 0)$  indicates a machine (resource). The processing sequence starts at  $R_o$  and finishes at  $R_o$ . In the existence of more than one processing sequence for each part such that  $R_i \rightarrow R_j (i \neq j)$ , there exists a sequence from  $R_i$  to  $R_j$ . If the part shifts from  $R_i$  to  $R_j$ , a part handling device (called a transportation resource) such as an AGV or a robot, is needed to move the part.

Based on Definitions 1–14, the developed CROTPN for modeling processing routes of the system is constructed in Algorithm 1.

### III. DEADLOCK AVOIDANCE POLICY FOR CROTPN

A CROTPN includes many circuits owing to its high connectedness. A production process circuit (PPC) is a special circuit in a CROTPN and plays a vital role in the liveness of the CROTPN. Because of the routing complexity of an RMS, a CROTPN may contain multiple PPCs, but only some of them can be found in a CROTPN.

**Definition 15:** Let  $N$  be a CROTPN with  $N = (P, T, C, I, O, D, K, M_o, PR)$ . Let PPCs be circuits (which do not include place  $p_o$ ) in a CROTPN, expressed as  $PPCs = \{e_1, e_2, \dots, e_k\}$ ,  $k = \{1, 2, 3, \dots\}$ . A PPC  $e_k$  is called an elementary circuit if it moves from a node  $z$ , through several nodes, back to the starting node  $z$ , and no node is repeated.

If a PPC  $e_k$  does not fulfill the condition given in Definition 15, then the PPC  $e_k$  is said to be a nonelementary.

The number of PPC  $e_k$  places must be equal to that of transitions on  $e_k$  in a CROTPN, and the transition input place for  $e_k$  must be on  $e_k$ .

#### Algorithm 1 Construction of a CROTPN

**Input:** A Part type  $i \in \pi$ , and its processing route  $PR_i$ .

**Output:** A net CROTPN.

**Initialization:**  $P = \{p_o, p_r\}$ ,  $T = \emptyset$ ,  $F = \emptyset$ ,  $M_o = \emptyset$ ,  $C = \emptyset$ ,  $\mu = \{R_{io}\}$ ,  $i = 0$ , and  $j = 0$ .

1. **for**  $(I, |\pi|, i++)$ , choose  $PR_i \in PR$ , **do**
2.     **for**  $(I, |\epsilon_i|, j++)$ , **do**
3.         For  $R_{i(j-1)}$ , add a place  $p_x$ ;
4.         For  $R_{ij}$ , add a place  $p_y$ ;
5.         Add a transition  $t_{xyi}$ ;
6.         Add arcs and weights  $(p_x, t_{xyi})$  and  $(t_{xyi}, p_y)$ ;
7.          $P := P \cup \{p_x, p_y\}$  and  $T := T \cup \{t_{xyi}\}$ ;
8.          $F := F \cup ((P \times T) \cup (T \times P))$ ;
9.          $\mu := \mu \cup \{R_{ij}\}$ ;
10.        **if**  $t_{xyi}$  needs  $p_r$  to transfer part type  $i$ , **then**
11.            Add arcs and weights  $(p_r, t_{xyi})$  and  $(t_{xyi}, p_r)$ ;
12.             $F := F \cup ((P \times T) \cup (T \times P))$ ;
13.            **end if**
14.     **end for**
15.         For  $R_{i0i}$ , add a place  $p_x$ ;
16.         Add a transition  $t_{x0i}$ ;
17.         Add arcs and weights  $(p_x, t_{x0i})$  and  $(t_{x0i}, p_o)$ ;
18.          $T := T \cup \{t_{x0i}\}$ ;
19.          $F := F \cup ((P \times T) \cup (T \times P))$ ;
20.         **if**  $t_{x0i}$  needs  $p_r$  to transfer part type  $i$ , **then**
21.            Add arcs  $(p_r, t_{x0i})$  and  $(t_{x0i}, p_r)$ ;
22.             $F := F \cup ((P \times T) \cup (T \times P))$ ;
23.            **end if**
24.     **end for**
25.     /\* Construct the  $M_o^*$ !
26.          $M_o(p_o) = \{c_{p1}, c_{p2}, \dots, c_{pm}\}$ ;
27.          $M_o(p_r) = \{c_{t1}, c_{t2}, \dots, c_{tk}\}$ ;
28.          $M_o(p) = 0, \forall p \in PR$ ;
29.          $M_o := M_o \cup M_o(p_o) \cup M_o(p_r) \cup M_o(p)$ ;
30.          $C := C(p_o) \cup C(p_r)$ .
31.     Output a net CROTPN.
32. **End**

**Definition 16:** Let  $N$  be a CROTPN with  $N = (P, T, C, I, O, D, K, M_o, PR)$ . Let  $P(e_k)$  and  $T(e_k)$  be respectively the sets of places and transitions in  $e_k$  such that  $|P(e_k)| = |T(e_k)|$ ,  $p_i \in \cdot t_j$ , and  $\cdot t_j \in P(e_k)$ . Let  $M(p_i, e_k)$  be the number of tokens in place  $p_i$  that enables  $t_j$  in  $e_k$ . If  $t_j$  is fired and the tokens leave  $e_k$ , then the tokens in  $e_k$  are called the leaving tokens of  $e_k$ . If  $t_j$  is fired and the tokens do not leave  $e_k$ , then the tokens in  $e_k$  are called the cycling tokens of  $e_k$ , expressed as

$$p_i \in P(e_i), \quad M(e_i) = \sum M(p_i, e). \quad (7)$$

The interaction of PPCs in CROTPN complicates the liveness problem of the net. The following definitions discuss interactive PPC subnets.

**Definition 17:** Let  $N$  be a CROTPN with  $N = (P, T, C, I, O, D, K, M_o, PR)$ . A circuit  $e_k^n$  is said to be interactive,

consisting of  $n$  PPCs, if it is strongly connected and its places and transitions are shared with at least another PPC. Let  $P(e_k^n)$  and  $T(e_k^n)$  be respectively the sets of places and transitions in  $e_k^n$  such that  $T_i = \{t \in p_i \cdot \cap T(e_k^n)\}$  and  $p_i \in P(e_k^n)$ . Let  $M(p_i, e_k^n)$  be the number of tokens in place  $p_i$  that enables  $t_j$  in  $e_k^n$ . If  $t_j \in T_i$  is fired and the tokens leave  $e_k^n$ , then the tokens in  $e_k^n$  are called the leaving tokens of  $e_k^n$ . If  $t_j \in T_i$  is fired and the tokens do not leave  $e_k^n$ , then the tokens in  $e_k^n$  are called the cycling tokens of  $e_k^n$ , expressed as

$$p_i \in P(e_k^n), \quad M(e_k^n) = \Sigma M(p_i, e_k^n) \quad (8)$$

*Definition 18:* Let  $N$  be a CROTPN with  $N = (P, T, C, I, O, D, K, M_o, PR)$ . At marking  $M$ , a PPC  $e_k$  has no free space in the places (called full) if

$$p_i \in P(e_k), \quad \Sigma M(p_i) = \Sigma K(p_i) = K(e_k) \quad (9)$$

*Theorem 1:* Let  $N$  be a CROTPN with  $N = (P, T, C, I, O, D, K, M_o, PR)$ . The necessary condition for  $N$  to be deadlocked (not live) is that there exists at least one PPC  $e$  such that

$$M_o(p_o) \geq K(e_k). \quad (10)$$

*Proof:* Proved in [50].

Before addressing deadlock-free conditions and control policy in a CROTPN, we introduce some necessary definitions and notation.

*Definition 19:* Let  $N$  be a CROTPN with  $N = (P, T, C, I, O, D, K, M_o, PR)$ . A transition  $t_j$  is called a controlled transition if the  $t_j$  enabling conditions (1) and (2) in Definition 5 are satisfied. If at least one transition is controlled in the  $N$ , then it is called a controlled transition. A PPC  $e_k$  in the  $N$  is enabled when it is process- and resource-enabled. A PPC  $e_k$  is called a live transition if for each  $t_j \in T(e_k)$ ,  $t_j$  is live.

Consequently, the CROTPN's control policy is limited. It decides whether any controlled transition may fire by monitoring the net state, even if both process and resource are satisfied. If a controlled transition can fire based on a control policy, we claim that this policy allows control.

*Definition 20:* Let  $N$  be a CROTPN with  $N = (P, T, C, I, O, D, K, M_o, PR)$ . Let  $e_k^n$  be an interactive subnet in the  $N$ . A transition  $t_j$  is said to be an input transition of  $e_k^n$  if  $t_j \in P(e_k^n)$  and  $t_j \notin T(e_k^n)$ . A transition  $t_j$  is called an output transition of  $e_k^n$  if  $t_j \in P(e_k^n)$  and  $t_j \notin T(e_k^n)$ . Let  $T_I(e_k^n)$  and  $T_O(e_k^n)$  be respectively the sets of input transitions and output transitions of  $e_k^n$ .

*Definition 21:* Let  $N$  be a CROTPN with  $N = (P, T, C, I, O, D, K, M_o, PR)$ . Let the number of current spaces and free spaces in PPC  $e_k$  be respectively  $S'(e_k)$  and  $S(e_k)$  at marking  $M$ , expressed by

$$S(e_i) = \sum_{p_j \in P(e_k)} (K(p_j) - M(p_j)) \quad (11)$$

$$S'(e_i) = K(e_k) - M(e_k) \quad (12)$$

*Theorem 2:* Let  $N$  be a CROTPN with  $N = (P, T, C, I, O, D, K, M_o, PR)$ . Let  $R_{DF}(N, M_o)$  denote the set of reachable

markings under control in the  $N$ . For any marking  $M \in R_{DF}(N, M_o)$ , a PPC  $e_k$  is live if

$$S'(e_k) \geq 1. \quad (13)$$

*Proof:* Proved in [50].

*Theorem 3:* Let  $N$  be a CROTPN with  $N = (P, T, C, I, O, D, K, M_o, PR)$ . Let  $\eta(e_k^n, M)$  denote the enabled PPCs in  $e_k^n$  at marking  $M$ . For any marking  $M \in R_{DF}(N, M_o)$  reachable from  $M_o$ , a PPC  $e_k^n$  is live if

$$S'(e_k) \geq 1, \quad \text{for any } e_k, \quad (14)$$

and

$$\eta(e_k^n, M) \geq 1 \quad (15)$$

*Proof:* Proved in [50].

*Theorem 4:* Let  $N$  be a CROTPN with  $N = (P, T, C, I, O, D, K, M_o, PR)$ . If there is no PPC in the  $N$ , then it is always live.

*Proof:* Proved in [50].

*Definition 22:* Let  $N$  be a CROTPN with  $N = (P, T, C, I, O, D, K, M_o, PR)$ . Let a transition  $t_j$  be an input transition of a number of PPCs. Let  $V_{en}(t_j)$  and  $T_d$  be respectively the set of these PPCs and the set of transitions in the  $N$  such that if  $t_j \in T_d$ , then  $V_{en}(t_j) \neq \emptyset$ .

*Theorem 5:* Let  $N$  be a CROTPN with  $N = (P, T, C, I, O, D, K, M_o, PR)$ . At marking  $M$ , the  $e_k^n$  is live if (1) each  $t_j \in T_I(e_k^n)$  is controlled; (2) before  $t_j$  fires, for any  $e_k \in V_{en}(t_j)$ ,  $S'(e_k) \geq 2$ ; and (3) after  $t_j$  fires, the marking in the  $N$  is updated from  $M$  to  $M'$  with  $\eta(e_k^n, M') \geq 1$ .

*Proof:* Proved in [50].

Theorems 1–5 in [50] present the necessary and sufficient deadlock-free conditions for the CROTPN. Based on Definitions 15–22 and Theorems 1–5, the deadlock avoidance algorithm of the developed CROTPN is constructed in Algorithm 2.

#### IV. DESIGN OF UNRELIABLE CROTPN

A resource failure in an RAMS is a matter of temporal uncertainty. If a resource fails in an unreliable place  $p_i$ , we attempt to add a subnet that is capable of removing a token from  $p_i$  and repairing the failed resource. Additionally, this subnet will return a token to the unreliable place after the resource is repaired. The resource can then be reused. This subnet is called a recovery subnet. This section presents the formal definitions that are used to construct the recovery subnets for all failures in a CROTPN.

*Definition 23:* Let  $N$  be a CROTPN with  $N = (P, T, C, I, O, D, K, M_o)$ . Let  $r_u \in P_R$  be an unreliable resource in  $N$ . Let  $N_{RNi}$  be a recovery subnet of  $r_u$  with  $N_{RNi} = (\{p_i, p_{combined}\}, \{t_{fi}, t_{ri}\}, F_{mi}, c_{mi})$ , where  $p_i \in P_R$  and  $p_{combined}$ ,  $t_{fi}$ ,  $t_{ri}$  represent respectively the common recovery place of  $p_i$ , the failure transition, and the recovery transition.  $F_{mi} = (\{p_i, t_{fi}\}, \{t_{fi}, p_{combined}\}, (p_{combined}, t_{ri}), (t_{ri}, p_i)\}$ .  $c_{mi}$  is the color that maps  $p_i \in P$  into colors  $c_{mi} \in C$ .  $(N_{RNi}, M_{RNio})$  is called a marked recovery subnet, where  $M_{RNio}(p_i) \geq 0$  and  $M_{RNio}(p_{combined}) = 0$ .

**Algorithm 2** Deadlock Avoidance Policy of the CROTPN**Input:** A net CROTPN.**Output:** Controlled net CROTPN.**Initialization:**  $k = 0$  and  $j = 0$ .

1. Compute the set of PPCs =  $\{e_1, e_2, \dots, e_k\}$  for CROTPN.
2. Compute the set of  $R(N, M_o)$  for CROTPN.
3. **for** ( $l, |PPCs|, k++$ ), **do**
4.     **if**  $e_k$  is not an interactive subnet, **then**
5.         Check the liveness of  $e_k$ ;
6.         **for** ( $0, |R(N, M_o)|, j++$ ), **do**
7.              $K(e_k) = \Sigma K(p, e_k), p \in P(e_k)$ ;
8.              $M_j(e_k) = \Sigma M_j(p, e_k), p \in P(e_k)$ ;
9.              $S'(e_k) = K(e_k) - M_j(e_k)$ ;
10.         **if**  $S'(e_k) \geq 0$ , **then** /\* By using Theorems 1 and 2. \*/
11.              $e_k$  in a CROTPN is live;
12.              $R_{DF}(N, M_o) = R(N, M_o)$ ;
13.         **else if**
14.              $e_k$  in a CROTPN is not live;
15.         **end if**
16.     **else if** /\*  $e_k$  is an interactive subnet with  $n$  PPCs \*/.
17.         Check the liveness of  $e_k^n$ ;
18.         **for** ( $0, |R(N, M_o)|, j++$ ), **do**
19.              $K(e_k^n) = \Sigma K(p, e_k^n), p \in P(e_k^n)$ ;
20.              $M_j(e_k^n) = \Sigma M_j(p, e_k^n), p \in P(e_k^n)$ ;
21.              $S'(e_k^n) = K(e_k^n) - M_j(e_k^n)$ ;
22.             **if**  $S'(e_k^n) \geq 1$  and  $\eta(e_k^n, M_j) \geq 0$ , **then** /\* By using Theorems 3-5. \*/
23.                  $e_k^n$  in a CROTPN is live;
24.                  $R_{DF}(N, M_o) = R(N, M_o)$ ;
25.             **else if**
26.                  $e_k^n$  in a CROTPN is not live;
27.             **end if**
28.     Output a controlled net CROTPN.
29. **End**

**Definition 24:** Let  $N$  be a CROTPN with  $N = (P, T, C, I, O, D, K, M_o)$ . For all  $r_u \in P_R$ , designing a common recovery subnet results in an unreliable CROTPN, expressed by  $(N_U, M_{Uo}) = (N, M_o) \parallel (N_{RNi}, M_{RNio})$  that is the composition of  $(N, M_o)$  and  $(N_{RNi}, M_{RNio})$ , where  $\parallel$  means the net composition.

**Definition 25:** Let  $(N_U, M_{Uo})$  be an unreliable CROTPN with  $N_U = (P_U, T_U, C_U, I_U, O_U, D_U, K_U, M_{Uo})$ , and  $R_U(N_U, M_{Uo})$  be its reachable graph, where  $P_U = P_U \cup \{p_{combined}\}$ ,  $T_U = T \cup T_F \cup T_R$ .  $T_F$  and  $T_R$  represent respectively the sets of failure transitions and the recovery transitions of  $(N_U, M_{Uo})$  with  $T_F = \cup_{i \in \mathbf{NA}} \{t_{fi}\}$ ,  $T_R = \cup_{i \in \mathbf{NA}} \{t_{ri}\}$ , and  $\mathbf{NA} = \{i | p_i \in P_R\}$ .  $C_U = C \cup C_F$ ,  $C_F = \cup_{i \in \mathbf{NA}} \{c_{mi}\}$ .  $I_U(p_i, t_j): C_U(p_i) \times C_U(t_j) \rightarrow \mathbf{IN}$ ,  $O_U(p_i, t_j): C_U(p_i) \times C_U(t_j) \rightarrow \mathbf{IN}$ ,  $D_U: T_U \rightarrow \mathbf{TS}$ ,  $K_U: P_U \rightarrow \mathbf{IN}$ , and  $M_{Uo}: P_U \rightarrow \mathbf{IN}$  is an initial marking of  $N_U$ .

Based on Definitions 23–25, an algorithm for an unreliable CROTPN is constructed in Algorithm 3.

**Algorithm 3** Unreliable CROTPN Construction**Input:** A net CROTPN.**Output:** An unreliable CROTPN  $(N_U, M_{Uo})$ .**Initialization:**  $P_U = P \cup \{p_{combined}\}$ ,  $T_U = T$ ,  $F_U = F$ ,  $C_U = C$ ,  $M_{Uo} = M_o$ , and  $i = 0$ .

1. **for** ( $l, |P_R|, i++$ ), **do**
2.     Add a transition  $t_{fi}$ ;
3.     Define a color  $c_{rmi}$  for  $t_{fi}$ ;
4.     Add a transition  $t_{ri}$ ;
5.     Add an arc  $(p_i, t_{fi})$ ;
6.     Add an arc  $(t_{fi}, p_{combined})$ ;
7.     Add an arc  $(p_{combined}, t_{ri})$ ;
8.     Add an arc  $(t_{ri}, p_i)$ ;
9.      $T_U := T_U \cup \{t_{fi}, t_{ri}\}$ ;
10.      $F_U := F_U \cup ((P_U \times T_U) \cup (T_U \times P_U))$ ;
11.      $C_U := C_U \cup \{c_{rmi}\}$ .
12. **end for**
13. /\* Define the  $M_{Uo}^*$  \*/
14.      $M_{Uo} := M_o \cup M_{Uo}(p_{combined})$ .
15. **Output** an unreliable CROTPN net.
16. **End**

**V. NEURAL NETWORK AND CROTPN FOR FAULT DETECTION AND TREATMENT**

Recently, neural networks (NNs) have gained popularity since they can learn complex functions. Parallel and distributed processing systems comprising a large number of simple and highly-connected processors can be seen as neural networks. These networks can be trained offline for complicated mapping, for example to determine different faults and can then be effectively used in the online environment. This section presents the formal definitions that are used to construct the CROTPN model based on neural networks for fault detection and treatment.

**Definition 26:**  $N_{NP} = (P_{NP}, T_{NP}, F_{NP}, X_\zeta, Y_\zeta, W_{NP}, M_{NPo})$  is said to be a neural Petri net (NPN) if

1.  $P_{NP}$  is a set of places that represent the input neurons  $p_{xi}$  and outputs pattern  $p_{yj}$  of the neural network with  $P_{NP} = \cup_{i \in \theta} \{p_{xi}\} \cup (\cup_{j \in \alpha} \{p_{yj}\})$ ,  $\theta, \alpha > 0$ ;
2.  $T_{NP}$  is a set of transitions that represent fault detection  $t_{di}$  and fault treatment  $t_{ti}$  with  $T_{NP} = \cup_{i \in \beta} \{t_{di}\} \cup (\cup_{j \in \gamma} \{t_{ti}\})$  and  $\beta, \gamma > 0$ ;
3.  $F_N$  is the input and output function with  $F_N \subseteq (P_{NP} \times T_{NP}) \cup (T_{NP} \times P_{NP})$ ;
4.  $X_\zeta$  denotes the set of inputs neuron pattern  $k$  that represents the input factor of the neural model with  $X_\zeta = \cup_{i \in \theta} \{x_i^\zeta\}$ , where each  $x_i$  is mapped to the corresponding  $p_{xi}$  and  $\zeta = 1, 2, 3 \dots$ ;
5.  $Y_\zeta$  denotes the set of outputs of pattern  $\zeta$  that represents the output factor of the neural model with  $Y_\zeta = \cup_{j \in \alpha} \{y_j^\zeta\}$ , where each  $y_j$  is mapped to the corresponding  $p_{yj}$ ;
6.  $W_{NP} \rightarrow [0, 1]$  denotes the set of the connectivity matrix from  $p_{xi}$  to  $t_{di}$ ;

7.  $M_{NPo}$ :  $P_{NP} \rightarrow \mathbf{IN}$  denotes the initial marking of  $N_{NP}$ .

The major difference between the standard NN and the NPNs is that the Petri layer and transition layer proposed in NPNs represent the configuration of the NPNs model of the fault detection and treatment. The Petri layer input  $x_i^\zeta$  is the input of the NPNs and the output of the each node in this Petri layer is tokens with acquisition systems that collect signals from input sensors and connectivity matrix  $W_{NP}$ , which is defined as follows:

**Definition 27:** Let  $N_{NP} = (P_{NP}, T_{NP}, F_{NP}, X_\zeta, Y_\zeta, W_{NP}, M_{NPo})$  be a neural Petri net model. The connectivity matrix  $W_{NP}$  of  $N_{NP}$  can be represented as:

$$W_{NP} = \begin{bmatrix} \sum w_{ij} = 1 & j \in \beta \text{ and } i|p_{xi} \\ & \in t_{dj} \\ w_{ij} = 0 & \text{otherwise} \end{bmatrix} \quad (16)$$

**Definition 28:** Let  $N_{NP} = (P_{NP}, T_{NP}, F_{NP}, X_\zeta, Y_\zeta, W_{NP}, M_{NPo})$  be a neural Petri net model. Let  $Z_j$  be the input of all the fault detection neuron layers. If  $t_{dj}$  is enabled and fired, then the input  $Z_j$  is generated and represented as:

$$Z_j = \begin{bmatrix} \sum w_{ij} x_i^\zeta & j \in \beta \text{ and } i| \\ 0 & x_i \in X_\zeta \\ & \text{otherwise} \end{bmatrix} \quad (17)$$

The input of the transition layer is the output of the Petri layer and is connected to the neural network middle layer. This layer is designed to generate tokens using competition laws as follows:

**Definition 29:** Let  $N_{NP} = (P_{NP}, T_{NP}, F_{NP}, X_\zeta, Y_\zeta, W_{NP}, M_{NPo})$  be a neural Petri net model. The input  $Z_j \in Y_\zeta$  is called the winner if it has the largest value compared with others' input values and its output value  $y_j$  is stated as 1; otherwise, the other output values are stated as 0, denoted as

$$Y_\zeta = \begin{bmatrix} y_j = 1 & Z_j > Z_i \\ & i > 0 \\ & i \neq j \\ y_i = 0 & i \neq j \end{bmatrix} \quad (18)$$

We define the update law on the synaptic weight of the winner neuron  $w_{ij}$ , to guarantee the NPNs precisely online estimation as follows:

**Definition 30:** Let  $N_{NP} = (P_{NP}, T_{NP}, F_{NP}, X_\zeta, Y_\zeta, W_{NP}, M_{NPo})$  be a neural Petri net model. Let the winner  $j^{\text{th}}$  output neuron be  $y_j$ . Thus, the synaptic weight of the winner neuron's  $w_{ij} \in W_{NP}$  can be formulated as.

$$w_{ij} = \begin{bmatrix} w_{ij} + \Delta w_{ij} & i \in \theta \\ & j \in \beta \\ w_{ij} & \text{Otherwise} \end{bmatrix} \quad (19)$$

$$\Delta w_{ij} = \lambda \left( \frac{x_i^\zeta}{\delta} w_{ij} \right) \quad \begin{matrix} i \in \theta \\ j \in \beta \end{matrix} \quad (20)$$

where  $\delta$  denotes the number of items, which are equal to 1 in the input learning pattern  $X_\zeta$  and  $\lambda \rightarrow [0, 1]$  denotes a learning rate.

Finally, the neural unreliable CROTPN can be described as the following definition.

**Definition 31:** Let  $(N_U, M_{Uo})$  be an unreliable CROTPN with  $N_U = (P_U, T_U, C_U, F_U, W_U, D_U, K_U, M_{Uo})$  and let  $N_{NP} = (P_{NP}, T_{NP}, F_{NP}, X_\zeta, Y_\zeta, W_{NP}, M_{NPo})$  be a neural Petri net model. We call  $(N_{NU}, M_{NUo})$  a neural unreliable CROTPN, expressed as  $(N_{NU}, M_{NUo}) = (N_U, M_{Uo}) \parallel (N_{NP}, M_{NPo})$  that is the composition of  $(N_U, M_{Uo})$  and  $(N_{NP}, M_{NPo})$ , where  $N_{NU} = (P_{NU}, T_{NU}, C_{NU}, I_{NU}, O_{NU}, D_{NU}, K_{NU}, X_\zeta, Y_\zeta, W_{NP}, M_{NUo})$ , and

1.  $P_{NU} = P_U \cup P_{NP}$ ;
2.  $T_{NU} = T_U \cup T_{NP}$ ;
3.  $C_{NU} = C_U$ ;
4.  $I_{NU}(p_i, t_j): C_{NU}(p_i) \times C_{NU}(t_j) \rightarrow \mathbf{IN}$ ;
5.  $O_{NU}(p_i, t_j): C_{NU}(p_i) \times C_{NU}(t_j) \rightarrow \mathbf{IN}$ ;
6.  $D_{NU}: T_{NU} \rightarrow \mathbf{TS}$ ;
7.  $K_{NU}: P_{NU} \rightarrow \mathbf{IN}$ ;
8.  $M_{NUo}: P_{NU} \rightarrow \mathbf{IN}$  is the initial marking of  $N_{NU}$ .

Based on Definitions 36–31, the developed training and solution of a neural unreliable CROTPN algorithm is constructed in Algorithm 4.

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**Algorithm 4** Fault Type of a Neural Unreliable CROTPN

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**Input:** A neural unreliable CROTPN  $N_{NU}$  with  $N_{NU} = (P_{NU}, T_{NU}, C_{NU}, F_{NU}, W_{NU}, D_{NU}, K_{NU}, X_\zeta, Y_\zeta, W_{NP}, M_{NUo})$ .

**Output:** The fault type  $Y_\zeta$

**Initialization:**  $w_{ij} \rightarrow [0, 1]$ ,  $X_\zeta$ ,  $\mu$  (target weight),  $r = 0$ ,  $i = 0, j = 0$ , and  $k = 0$ .

1. **for** ( $1, |T_F|, r++$ ), **do**
  2.   **if**  $t_{fj}$  fires, **then**
  3.     **while**  $w_{ij} < \theta$ , **do**
  4.       **for** ( $1, |\zeta|, k++$ ), **do**;
  5.       **for** ( $1, |\theta|, i++$ ), **do**;
  6.       **for** ( $1, |\beta|, j++$ ), **do**;
  7.         Select a pattern  $X_\zeta$  from the input patterns  $\zeta$ ;
  8.         Compute the input  $Z_j$  of all the neurons;
  9.         Compute the winner output value  $y_j$  and Enable the winner transition  $t_{dj}$ ;
  10.        Update the weight  $w_{ij}$  of the winner neuron.
  11.     **end for**
  12.    **end for**
  13.    **end for**
  14.    **end while**
  15.    **else if**
  16.      Break.
  17.    **end if**
  18. **end for**
  19. Output a fault type  $Y_\zeta$ .
  20. **End**
-

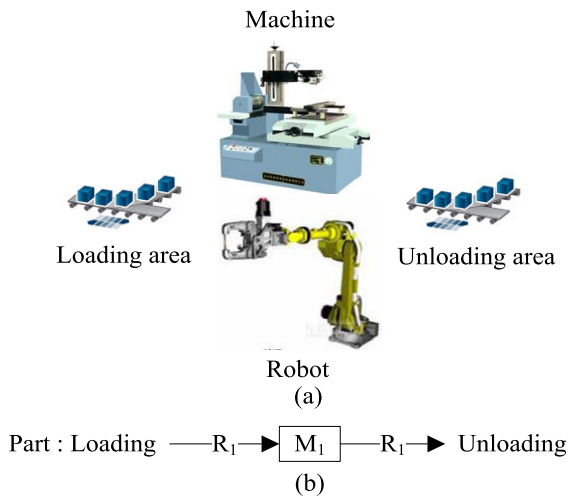


FIGURE 1. (a) Example of AMS and (b) The process route.

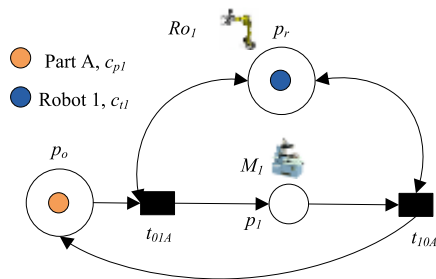


FIGURE 2. CROTPN of the system shown in Figure 1.

## VI. NUMERICAL EXAMPLE

### A. ALGORITHM 1 APPLICATION

Consider the AMS illustrated in Figure 1(a) to demonstrate the procedures of a CROTPN synthesis. The operation route of the system is presented in Figure 1(b). Figure 2 displays the transportation and operation resources of the system after implementing Algorithm 1, where resource place  $p_1$  represents machine 1 ( $M_1$ ), the operation sequence of part A is  $p_o \rightarrow t_{01A} \rightarrow p_1 \rightarrow t_{10A} \rightarrow p_o$ , and a transportation place  $p_r$  represents robot 1 ( $Ro_1$ ). To build the model of processes of transportations of part types, a place  $p_r$  is needed respectively for loading and unloading part A to and from  $p_1$  by transitions  $t_{01A}$  and  $t_{10A}$ . Thus, arcs  $(p_r, t_{01A})$ ,  $(t_{01A}, p_r)$ ,  $(p_r, t_{10A})$ , and  $(t_{10A}, p_r)$  are added into the CROTPN model. The CROTPN initial marking is defined as  $M_o(p_o) = \{c_{p1}\}$ ,  $M_o(p_r) = \{c_{t1}\}$ , and  $M_o(p_1) = 0$ , where  $c_{p1}$  and  $c_{t1}$  denote respectively part type A and robot 1 in the system.

Based on Definitions 5 and 6, the behavior of the CROTPN illustrated in Figure 2 is explained as follows. When transition  $t_{01A}$  fires, it selects respectively a token with color  $c_{p1}$  and color  $c_{t1}$  from input places  $p_o$  and  $p_r$ . If  $t_{01A}$  fires, it adds respectively a token  $c_{p1}$  and color  $c_{t1}$  to output places  $p_1$  and  $p_r$ . Finally, when  $t_{10A}$  fires, it selects respectively a token  $c_{p1}$  and color  $c_{t1}$  from input places  $p_1$  and  $p_r$ . If  $t_{10A}$  fires, it adds respectively a token with color  $c_{p1}$  and color  $c_{t1}$  to output places  $p_o$  and  $p_r$ .

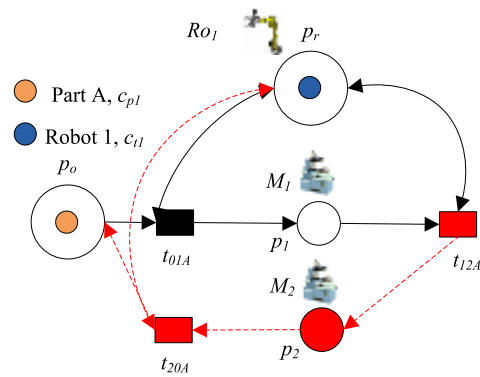


FIGURE 3. CROTPN after adding a new machine for the system shown in Figure 2.

To design and model the dynamic changes of the system shown in Figure 1(a) by using CROTPN synthesis, we assume that a system undergoes configurations including:

1. Adding a new machine;
2. Adding a new product;
3. Rework;
4. Adding a new transportation resource.

The first reconfiguration adds a new machine  $M_2$  to process part A after machine 1 in Figure 1(a), and robot 1 is required to load/unload part A to/from machine 2. To do this, consider the following steps to build the changed system by using the CROTPN synthesis:

- 1) Update the operation sequence of part A as:  $p_o \rightarrow t_{01A} \rightarrow p_1 \rightarrow t_{12A} \rightarrow p_2 \rightarrow t_{20A} \rightarrow p_o$ ;
- 2) Insert the new transitions  $t_{12A}$  and  $t_{20A}$  to the model;
- 3) Draw arcs  $(p_r, t_{12A})$ ,  $(t_{12A}, p_r)$ ,  $(p_r, t_{20A})$ , and  $(t_{20A}, p_r)$ .

The new reconfigured CROTPN model is shown in Figure 3.

The second dynamic change adds a new product part B to the model shown in Figure 3. Part B requires to be processed in machine 1 and robot 1.  $Ro_1$  is required to load/unload part B to/from machine 1. To build the newly added product, we apply the following steps to construct the changed system by using the CROTPN synthesis:

- 1) Add a new process sequence:  $p_o \rightarrow t_{01B} \rightarrow p_1 \rightarrow t_{10B} \rightarrow p_o$ ;
- 2) Insert the new transitions  $t_{01B}$  and  $t_{10B}$ ;
- 3) Draw arcs  $(p_r, t_{01B})$ ,  $(t_{01B}, p_r)$ ,  $(p_r, t_{10B})$ , and  $(t_{10B}, p_r)$ ;
- 4) Add the color  $c_{p2}$  as an initial token into  $p_o$  that represents part B in the system.

The new reconfigured CROTPN model is shown in Figure 4.

The third control specification is to add a rework sequence to part B by inserting an inspection machine 3 after machine 1 in Figure 4. If Part B is successfully produced after machine 1 operation, the system will continue according to its initial route. Otherwise, if defects occur in part B, then rework is necessary. To do this, consider the following steps to build the changed system by using the CROTPN synthesis:

- 1) Update the operation sequence of part B as
  - a.  $p_o \rightarrow t_{01B} \rightarrow p_1 \rightarrow t_{13B} \rightarrow p_3 \rightarrow t_{30B} \rightarrow p_o$ ;



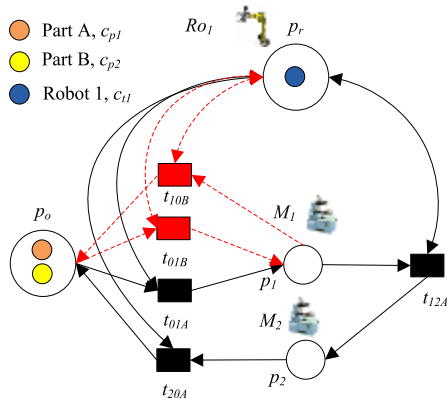


FIGURE 4. The CROTPN model after adding a new product for the system shown in Figure 3.

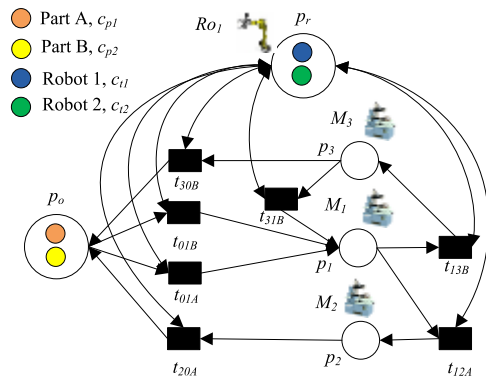


FIGURE 6. CROTPN model after adding a new transportation resource to the system shown in Figure 5.

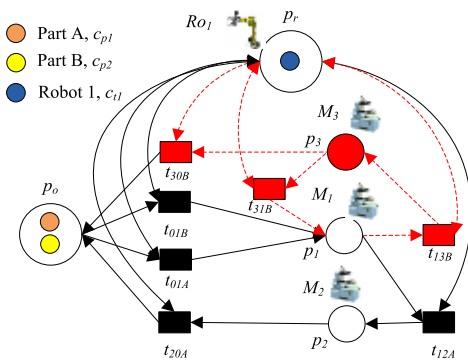


FIGURE 5. CROTPN after adding a rework for the system shown in Figure 4.

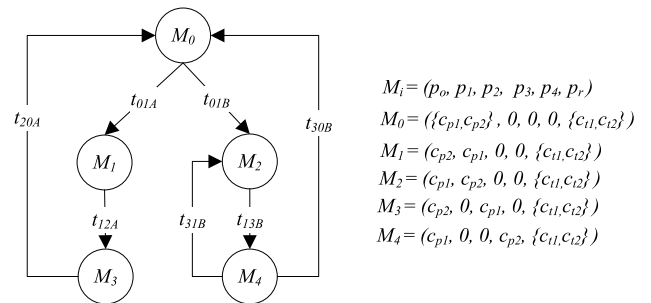


FIGURE 7. Reachable markings of the system shown in Figure 6.

TABLE 1. The available spaces in  $e_1$  for CROTPN shown in Figure 6.

Marking	$K(e_i)$ $= \sum K(p_i, e_i)$	$M(e_i)$ $= \sum M(p_i, e_i)$	$S'(e_i)$ $= K(e_i) - M(e_i)$	If $S'(e_i) \geq 1$
$M_o$	2	0	2	Yes
$M_1$	2	1	1	Yes
$M_2$	2	1	1	Yes
$M_3$	2	0	2	Yes
$M_4$	2	1	1	Yes

b.  $p_o \rightarrow t_{01B} \rightarrow p_1 \rightarrow t_{13B} \rightarrow p_3 \rightarrow t_{31B} \rightarrow p_1 \rightarrow t_{13B} \rightarrow p_3 \rightarrow t_{30B} \rightarrow p_o$

- 2) Insert the new transitions  $t_{13B}$ ,  $t_{31B}$ , and  $t_{30B}$ .
- 3) Draw arcs  $(p_r, t_{13B})$ ,  $(t_{13B}, p_r)$ ,  $(p_r, t_{31B})$ ,  $(t_{31B}, p_r)$ ,  $(p_r, t_{30B})$ ,  $(t_{30B}, p_r)$ .

The new reconfigured CROTPN model is shown in Figure 5.

Finally, suppose that a robot Ro2 (transportation resource) is inserted into the CROTPN shown in Figure 5 to load/unload part A to/from machine 1 and machine 2. To build the newly added robot Ro2, we apply the following steps to construct the changed system by using the CROTPN synthesis:

- 1) Add the initial token with color  $c_{r2}$  into place  $p_r$ , indicating that robot 2 in the system.
- 2) Update the transitions  $t_{01A}$ ,  $t_{12A}$ , and  $t_{20A}$ ;

The new reconfigured CROTPN model is shown in Figure 6.

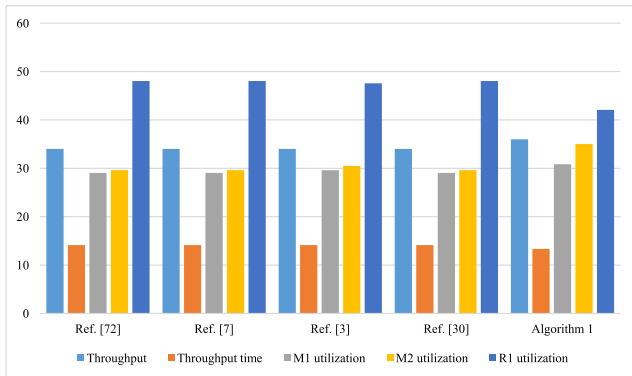
### B. ALGORITHM 2 APPLICATION

Let us reconsider the CROTPN of the changed model presented in Figure 6 to display the liveness of the CROTPN by using Algorithm 2. It has one PPC:  $e_1 = \{p_1, t_{13B}, p_3, t_{31B}\}$ . The CROTPN reachability graph in Figure 6 is illustrated in Figure 7. We assume that all places except  $p_r$

and  $p_o$  have a capacity of one with a buffer and a machine space. According to Theorem 2, the available spaces in  $e_1$  are calculated as shown in Table 1. We can see in Table 1 that for any marking, the condition in Theorem 2 is satisfied. Therefore, the deadlock in the reconfigured CROTPN shown in Figure 6 can be avoided when the condition illustrated in Theorem 2 is applied. The GPenSIM tool [3], [71] is employed to verify and validate Algorithms 1 and 2 and build a CROTPN model code. The proposed code is implemented on MATLAB R2015a. The simulation was done for 480 min. The time performance includes the total throughput time, total throughput, and utilization of machines and robots. The experimental results are compared with those in [3], [7], [30], [72]. Reconsider the CROTPN shown in Figure 3. Table 2 illustrates the MATLAB simulation results with regard to the above time performance criteria. It shows that Algorithm 1 can achieve less throughput time, greater throughput, and better utilization than the other methods, as presented in Figure 8. Thus, Algorithm 1 is accurate.

**TABLE 2.** The time performance of Algorithm 1 compared with the existing approaches for the model shown in Figure 3.

Parameters	Ref. [72]	Ref. [7]	Ref. [3]	Ref. [30]	Algorithm 1
Throughput	34	34	34	34	36
Throughput time	14.12	14.12	14.12	14.12	13.33
M1 utilization	29.05	29.05	29.60	29.05	30.83
M2 utilization	29.61	29.61	30.50	29.61	35.00
R1 utilization	48.04	48.04	47.56	48.04	42.08

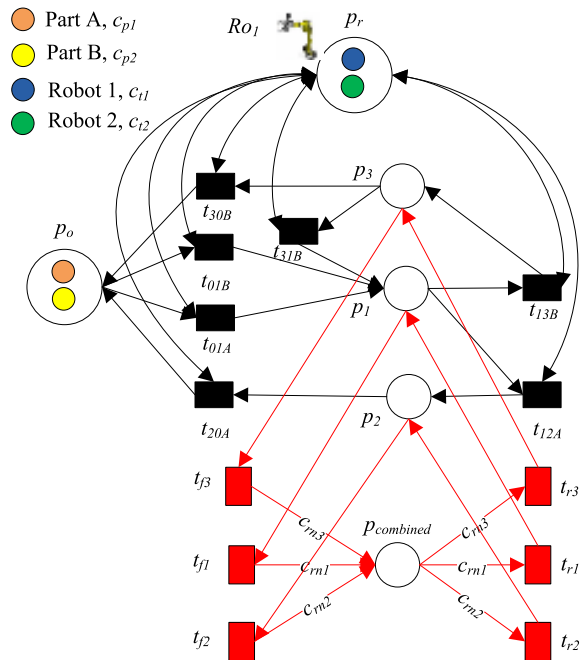


**FIGURE 8.** The time performance of Algorithm 1 compared with the current approaches for the net shown in Figure 3.

**C. ALGORITHM 3 APPLICATION**

To illustrate the common recovery subnet of an unreliable CROTPN by using Algorithm 3, consider the CROTPN model presented in Figure 6. We have three unreliable machines:  $p_1$ ,  $p_2$ , and  $p_3$ . Adding the recovery subnet by using Algorithm 3 results in an unreliable CROTPN, as shown in Figure 9, where  $NA = \{1, 2, 3\}$ ,  $T_F = \{t_{f1}, t_{f2}, t_{f3}\}$ , and  $T_R = \{t_{r1}, t_{r2}, t_{r3}\}$ , and  $C_F = \{c_{m1}, c_{m2}, c_{m3}\}$ . The behavior of the unreliable CROTPN illustrated in Figure 9 is explained as follows. When an unreliable machine 1 breaks down in  $p_1$ , the token in  $p_1$  moves into  $p_{combined}$  by firing  $t_{f1}$ . If  $t_{f1}$  fires, it generates a token  $c_{m1}$  and deposits it into a place  $p_{combined}$ . If the mean time of performing maintenance on machine 1 is elapsed, the token  $c_{m1}$  in  $p_{combined}$  moves into  $p_1$  by firing  $t_{r1}$ . If transition  $t_{r1}$  fires, it takes one token  $c_{m1}$  from  $p_{combined}$  and deposits it into  $p_1$ , denoting that a machine 1 recovery maintenance is finished.

If an unreliable machine 2 breaks down in  $p_2$ , then the token in  $p_2$  moves into  $p_{combined}$  by firing  $t_{f2}$ . If  $t_{f2}$  fires, it creates a token  $c_{m2}$  and deposits it into a place  $p_{combined}$ . If the mean time of performing maintenance on machine 2 is elapsed, the token  $c_{m2}$  in  $p_{combined}$  moves into  $p_2$  by firing  $t_{r2}$ . When transition  $t_{r2}$  fires, it takes one token  $c_{m2}$  from  $p_{combined}$  and deposits it into  $p_2$ , denoting that a machine 2 recovery maintenance is finished. Finally, when an unreliable machine 3 breaks down in  $p_3$ , the token in  $p_3$  moves into  $p_{combined}$  by firing  $t_{f3}$ . If  $t_{f3}$  fires, it creates a token  $c_{m3}$  and deposits it into place  $p_{combined}$ . If the mean time of performing maintenance on machine 3 is elapsed, the token



**FIGURE 9.** Unreliable CROTPN for the model shown in Figure 6.

**TABLE 3.** Input variables for the model shown in Figure 10.

Input	Description
$x_1$	The accelerometer
$x_2$	The current sensor
$x_3$	Strain gages
$x_4$	Coolant sensor
$x_5$	Acoustic emission sensor

$c_{m3}$  in  $p_{combined}$  moves into  $p_3$  by firing  $t_{r3}$ . When transition  $t_{r3}$  fires, it takes one token  $c_{m3}$  from  $p_{combined}$  and deposits it into  $p_3$ , denoting that a machine 3 recovery maintenance is finished.

**D. ALGORITHM 4 APPLICATION**

Finally, to illustrate the neural network and CROTPN for fault detection and treatment by using Algorithm 4, consider the unreliable CROTPN model presented in Figure 9. Algorithm 4 detects the types of various faults based on given parameters. The neural networks are used in two phases: training and testing. They learn how to identify the relation between inputs and outputs from the training phase. After training, the networks are tested using the test dataset. After the networks are tested and trained, they can diagnose faults under different operational conditions. The following concerns must be addressed when proposing models for system failure diagnosis: (a) data selection, (b) data normalization, and (c) structure network training and selection.

Using the CROTPN illustrated in Figure 9, we calculate the required data. The data consist of five input continuous factors [73]–[75] that are described in Table 3 and a single output is described in Table 4. The output variable from this

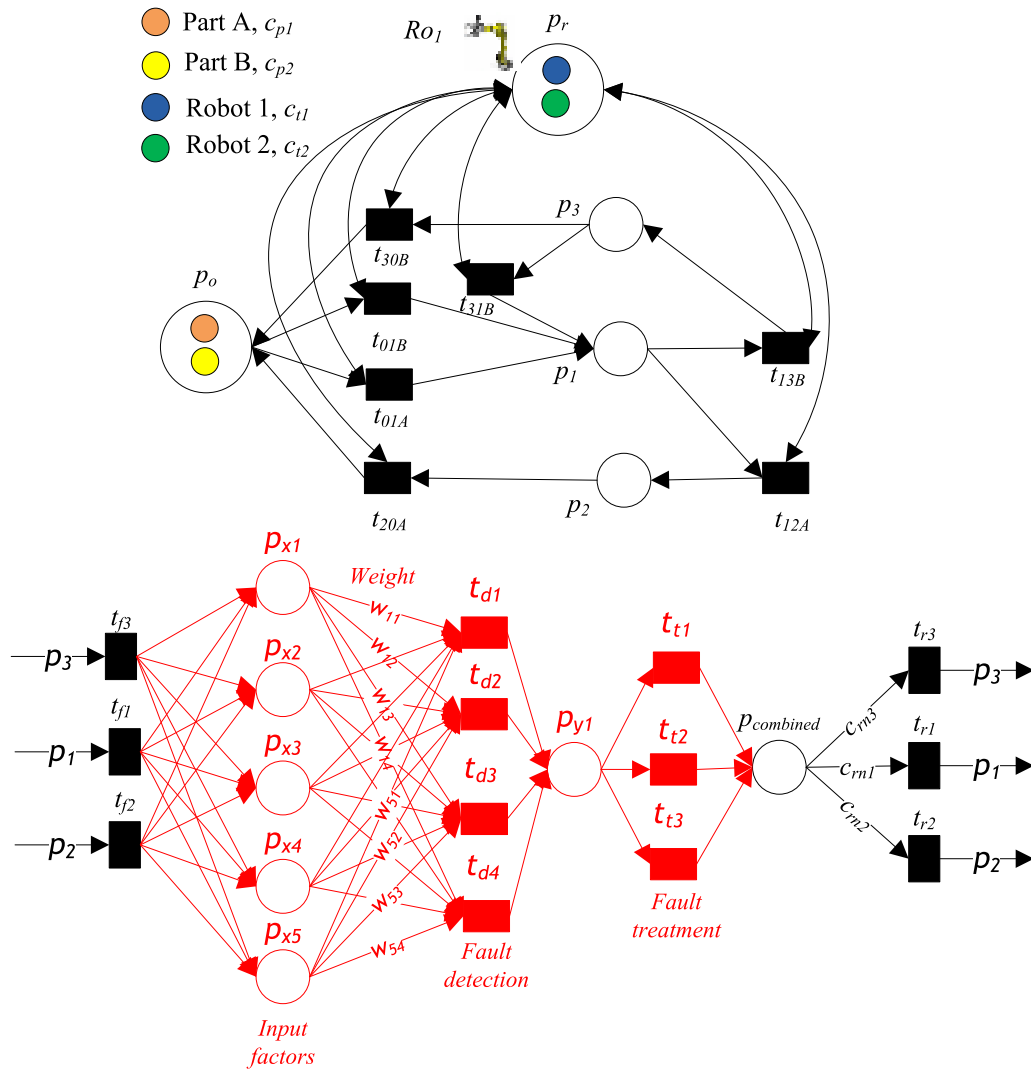


FIGURE 10. Neural unreliable CROTPN for the model shown in Figure 9.

TABLE 4. Output variables for the model shown in Figure 10.

Output	Description
$y_1$	Wearing the tool failure
$y_2$	Breaking the tool failure
$y_3$	Coolant failure
$y_4$	Programming errors

problem is obtained as [1 0 0 0] for fault type 1, [0 1 0 0] for fault type 2, [0 0 1 0] for fault type 3, and [0 0 0 1] for fault type 4. The GPenSIM code is employed to build the proposed neural unreliable CROTPN model. In Algorithm 4, a feature vector is obtained from the training dataset, the test dataset is used for fault diagnosis calculation, and the dataset for validation is used to interrupt iteration after a maximum capacity for generalization is reached. The collected datasets have 2250 patterns consisting of all five fault types. Moreover, the dataset includes 70% training patterns

(1575 patterns), 20% test patterns (450 patterns), and 10% validation patterns (225 patterns). The training data differs totally from the testing data. Figure 10 displays the fault detection of an unreliable CROTPN model shown in Figure 9. Only a single unreliable system can fail at one time.

As shown in Figure 10, in the input layer, the extraction system consists of an accelerometer ( $x_1$ ) that monitors mechanical vibrations, an electrical current sensor ( $x_2$ ) that monitors variations in electrical motor current consumption, a strain gage ( $x_3$ ) that monitors tool torsion or tool flexion, coolant sensor ( $x_4$ ) that monitors the coolant level, and an acoustic emission sensor ( $x_5$ ) that monitors acoustic effects of stress waves for tool break diagnosis. Acquisition systems collect signals from these sensors that identify machine tool states as being abnormal or normal. Random and uniform peaks are produced by the machine tool. Signals that exhibit peaks at the same wavelength signify slight tool-wear or erroneous programming of the machining parameters. The

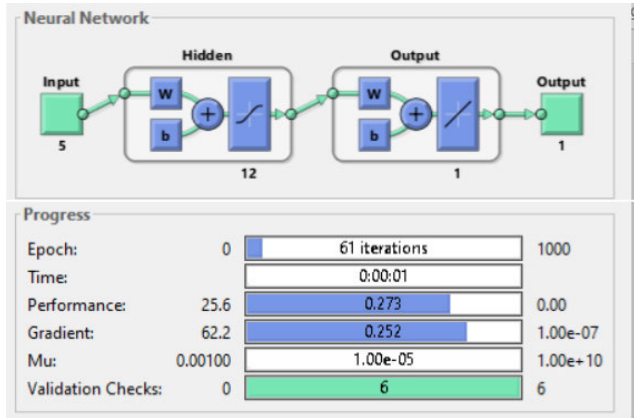


FIGURE 11. Performance of the neural unreliable CROTPN shown in Figure 10.

TABLE 5. Fault treatments for the model shown in Figure 10.

Fault treatment	Description
$t_{11}$	Changing the parameter
$t_{12}$	Changing the tool
$t_{13}$	Changing the coolant

signals exhibiting random peaks indicate that the tool is very worn or broken [76].

As shown in Figure 10, the failures in the output layer are a result of tool wear ( $y_1$ ), tool breaking ( $y_2$ ), cooling failure ( $y_3$ ), and programming mistakes ( $y_4$ ). Failures produced from the machine or programming mistakes such as an inappropriate setting of parameters or overuse of tools result in this kind of uniform peaks. Random peaks may be produced from failures caused by tool-break. Failures that identified through uniform peaks and oscillations are caused by tool wear. Finally, coolant failures result from insufficient coolant.

Suggested treatments are presented in Table 5 to recover a failed machine. The treatments include changing the parameter ( $t_{11}$ ), changing the tool ( $t_{12}$ ), or changing the coolant ( $t_{13}$ ). If the output from the neural network is a tool failure, the parameter change is needed. If the output from the neural network is a tool break failure, the tool change is needed. When the output from the neural network is coolant failure, the coolant change is needed. In addition, if the output from the neural network is a machining parameter or programming error failure, the parameter change is needed. Several training experiments are performed to identify the best network structures and the parameters that will lead to minimal training errors. In addition, many training tests with varying numbers of hidden neurons are employed. The number of hidden neural network layers used is 12.

Figures 11 and 12 present the performance of the neural unreliable CROTPN model shown in Figure 10. The model can identify faults as a time function. The mean square error (MSE) generated by a model at 61 iterations with a learning rate of 0.00001 is 0.273 and leads to a 95% accurate model

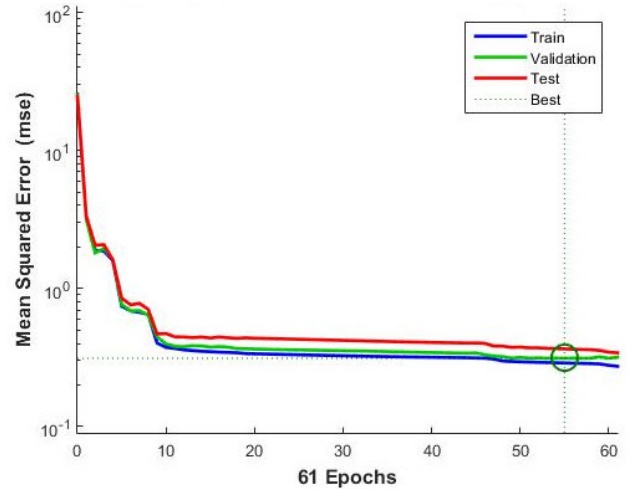


FIGURE 12. Learning performance of the neural unreliable CROTPN shown in Figure 10.

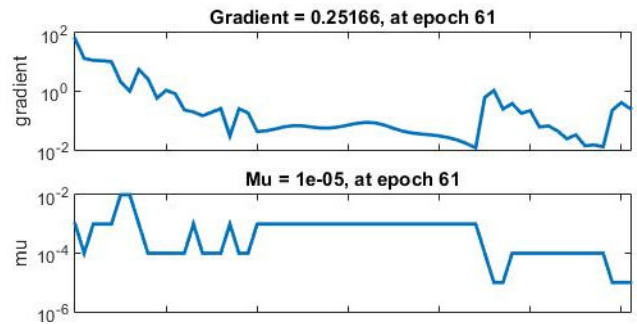


FIGURE 13. Validation check and learning rate of the neural unreliable CROTPN shown in Figure 10.

TABLE 6. Performance of the model shown in Figure 10.

Parameters	Value
Patterns of the training (%)	70
Patterns of the testing (%)	20
Patterns of the validation (%)	10
CPU time (s)	1
MSE	0.273
Value of learning rate	0.00001
Fault detection accuracy (%)	95

as shown in Table 6. Figure 13 indicates that the value of learning rate  $\gamma$  has a major impact on the convergence of the proposed model. Algorithm 4 converges slowly at low values of the learning rate, and it is very sensitive to the decreasing output if the learning rate is too high. The best solution for the coefficient of the correlation ( $R = 0.92031$ ), as shown in Figure 14, indicates the efficiency of Algorithm 4. Furthermore, the value of the correlation coefficient properly represents the efficiency of fault diagnosis. Based on these findings, it is suggested that Algorithm 4 can be significantly integrated with regression when fault detection and treatment issues are addressed.

TABLE 7. Comparison of Algorithm 4 with the existing methods.

Parameter	Ref. [36]	Ref. [44]	Algorithm 3	Algorithm 4
Throughput	60	61	63	65
Throughput time	8.00	7.87	7.62	7.38
M1 utilization	52.92	55.21	54.38	54.17
M2 utilization	22.53	23.75	23.13	23.75
R1 utilization	46.68	48.33	47.08	48.75
R2 utilization	38.50	39.58	40	41.67

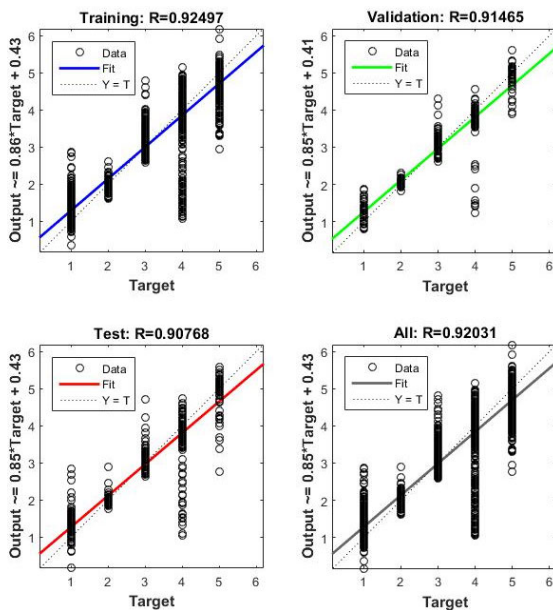


FIGURE 14. Regression results of the neural unreliable CROTPN model shown in Figure 10.

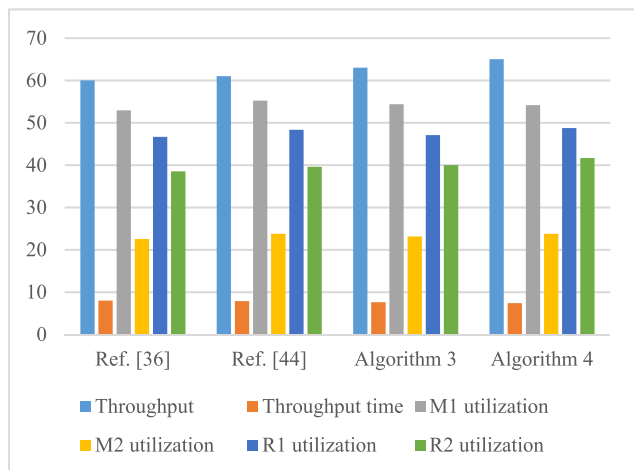


FIGURE 15. Time performance of Algorithm 4 compared with the current approaches for the model shown in Figure 10.

Finally, the GPenSIM code is employed to verify and validate Algorithm 4. The time performance criteria includes

the total throughput time (min/part), total throughput (parts), and utilization of machines and robots (%). The experimental results are compared with those in [44], [36] and Algorithm 3. Consider the CROTPN shown in Figure 10. Table 7 illustrates the results with regard to the above time performance criteria. Algorithm 4 can achieve less throughput time, greater throughput, and better utilization than the other methods, as presented in Figure 15. Thus, Algorithm 4 is accurate.

VII. CONCLUSION

This paper proposes a four-step deadlock control policy for the diagnosis and treatment of faults for an RMS with unreliable resources. The first step involves the development of a CROTPN for rapid and effective reconfiguration of the RMS without considering resource failure. The second step presents sufficient and necessary conditions for ensuring the liveness of the CROTPN to guarantee that the model is live. The third step solves the failures of all resources in the CROTPN model and guarantees that the net is reliable by developing and adding a single recovery subnet to the CROTPN model at the second step. The fourth step designs a new hybrid method, which combines the CROTPN with neural networks for fault detection and treatment. The GPenSIM tool is used to assess the proposed strategy under the RMS configuration changes and the results are compared with existing methods in the literature.

The advantages of the proposed policy are as follows. (1) A CROTPN has a very compact structure, and the part production operations can be represented by adding colors compared with the studies in [77]–[79]. (2) The developed CROTPN can perform any complex RMS configuration compared with those in [77], [78], [80]. (3) It is more powerful and has a simpler structure compared with the research findings in [44]. (4) One common transportation resource place is designed to transport all part types in RMS compared with [80]. (5) It is a modular Petri net that can combine the CROTPN with neural networks. (6) It is suitable for resources of RMSs that are complex and sequential. (7) It implements a combined approach to ensure that no deadlock can occur; faults are detected, and treated in RMSs. (8) The proposed fault detection and treatment mode is verified and validated by a simulation study.

The main limitations of this research are that the developed CROTPN is based on discrete data types. Therefore, the future research of this paper will improve the developed method to design the CROTPN based on continuous data types to handle continuous RMS data. In addition, an automatic interface based on the developed algorithms has to be designed for dynamic changes in RMSs.

## ACKNOWLEDGMENT

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