

Received March 10, 2021, accepted April 11, 2021, date of publication April 16, 2021, date of current version May 13, 2021. *Digital Object Identifier* 10.1109/ACCESS.2021.3073639

# Fault-Recovery and Robust Deadlock Control of Reconfigurable Multi-Unit Resource Allocation Systems Using Siphons

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This work was supported by the Deanship of Scientific Research at King Saud University under Grant RG-1441-425 and in part by the Natural Science Foundation of Shaanxi Province under Grant 2019JM-049.

**ABSTRACT** A multi-unit resource allocation system usually contains several processes and a number of resources with multiple units. Due to the competition for shared resources in these systems, deadlocks may occur. Recently, researchers have shown an increased awareness in deadlock control strategies for such a kind of systems without considering the dynamic changes such as processing failures and rework by using the Petri net paradigm. This article reports a new strategy for deadlock analysis and control in reconfigurable multi-unit resource systems (MRSs). We discuss a generalized class of Petri nets in which each stage of a process may require a number of units of different types of resources to perform a task. In this way, we can model more complex real systems. Thanks to a generalized class of Petri nets, i.e., the system of sequential systems with shared resources (S<sup>4</sup>R), this article proposes an effective integrated strategy for designing robust supervisors for reconfigurable MRSs, and improves an S<sup>4</sup>R model to achieve a new model, namely a system of sequential systems with shared resources and part-re-entry (S<sup>4</sup>RP), which represents the procedure that a flawed product re-enters a system and is re-processed. We use a siphon-based max-controllability deadlock prevention policy (DPP) to supervise the evolution of the S<sup>4</sup>RP, and present a comprehensive analysis to demonstrate that the controlled S<sup>4</sup>RP is free of deadlocks. A net analysis tool (INA) is used to test and validate the resulting S<sup>4</sup>RP.

**INDEX TERMS** Multi-unit resource system (MRS), Petri net, reconfiguration, robust deadlock control, max-controllability of siphon.

### I. INTRODUCTION

From the viewpoint of resource capacity, there are two distinct types of resource allocation systems: single-unit resource systems (SRSs) and multi-unit resource systems (MRSs). The two kinds of systems usually consist of several processes and a limited number of resources, where the difference between them is the capacity of resources. In a single-unit resource system, each resource has only one unit

The associate editor coordinating the review of this manuscript and approving it for publication was Yue Zhang<sup>10</sup>.

of that kind to be allocated to distinctive processes; on the other hand, in an MRS, a resource may equip with any number of units. The possibility of a system being in a deadlock state significantly depends on the competition for shared resources among different processes [1].

A deadlock is actually a status in a system where two or more processes wait for resources occupied by others to finish, and neither ever does. In an SRS, if a cycle is formed in its resource allocation graph that represents relationships among the processes and resources, a deadlock necessarily occurs. The issue of deadlock is increasingly challenging in an MRS since, for instance, the existence of a cycle in the resource allocation graph of an MRS does not necessarily imply the occurrence of a deadlock.

Many researchers and practitioners use Petri nets (PNs) for modelling and managing deadlocks in single or multi-unit resource systems [2]-[6]. PNs serve as a common formalism due to their inherent characteristics [7]–[17]. Deadlock control methods can be classified into three types: Deadlock detection and recovery [18], [19], deadlock avoidance [20], [21], and deadlock prevention [22], [23]. Deadlock prevention acts in an off-line way such that a group of constraints among the resources and processes in a system is imposed by an external agent, called a supervisor, thus making the resource requests that cause deadlocks be impossible. Deadlock avoidance offers an on-line computational mechanism. Whenever a deadlock state is recognized, a predefined mechanism helps the system return to a correct state. Deadlock prevention is usually thought of as being safer than other strategies [24]-[30]. For more details of Petri nets and their applications, readers are referred to [31]-[34].

The resources in manufacturing systems (a common example of MRSs) can have a multitude of forms, including a variety of equipment such as numerically controlled machine tools. The competitiveness of manufacturing companies depends not only by the high productivity of the manufacturing systems, but also by many factors from the market and customers. Reconfigurable manufacturing systems (RMSs) [35]–[37] offer the capability of an automatic and rapid response to the variation of the global market. Due to the complexity in its structure and configuration, the deadlock problem in an RMS remains a challenging issue for researchers and practitioners.

The existence of unreliable resources in an RMS is a significant factor contributing to deadlock occurrences. It is well-known that unreliable resources in RMSs may result in partial system collapse or even deadlocks due to the unavailability of some processing units in a resource [38]–[41]. Based on Petri nets, multiple strategies are introduced to make complex improvements in reconfigurable manufacturing systems [42]–[45]. However, most of them do not have a reconfiguration algorithm and cannot guarantee the behavioural properties of Petri nets (boundness, liveliness, and conservativeness).

To manage deadlocks within a reconfigurable MRS, we proposed in [46] a new net subclass, namely a simple sequential process with resources and part re-entry ( $S^2PRP$ ), which captures the dynamics of machine processing and part re-entry to a system by deciding whether a final product satisfies the desired quality. If not, a flawed part has to be sent to the system again for further processing. However, in [46] the process can acquire only one unit of resource at a time, implying that the developed technique in [46] has a limited application scope.

This paper aims to mitigate the technical issue in [46] by expanding the reported strategy in it. We first create a new net subclass called a system of sequential systems with shared

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resources and part-re-entry (S<sup>4</sup>RP). The major difference between the work in this paper and in [46] is that, this paper addresses a generalized class of Petri nets (S<sup>4</sup>R) [47] in which each stage of a process may require multiple units of multiple types of resources for executing a task. The well-known Petri nets (PNs) S<sup>3</sup>PR [48], [49] and WS<sup>3</sup>PR [50] are both proper subclasses of S<sup>4</sup>Rs.

In the literature, there are many net classes. Primarily, PNs can be either ordinary or generalized, depending on the weight of arcs. A PN is said to be ordinary when all arc-weights are one; a PN is said to be generalized if it has at least an arc with the weight being two or more. The structural approaches via siphon-control [11], [27], [51]–[53] are typical vehicles to derive deadlock prevention policies (DPPs) for generalized PNs. The occurrences of deadlocks in a generalized PN stem from the existence of siphons with insufficient tokens. It has been shown that deadlocks in a generalized PN could be managed or eliminated by the use of monitors (control places). However, the supervisors due to siphon control have several technical flaws such as structural complexity if the size of a plant is large. The notion of elementary siphons is introduced in [54], [55] and used for the design of liveness-enforcing-supervisors (LESs) with a simple structure.

For the modeling and analysis of manufacturing systems, a few PN subclasses have been reported, which are analyzed by means of siphons [56]–[62]. These findings could be traced to the seminal research in [48]. The proposed PN model (S<sup>4</sup>RP) in our research is a failure-safe model. A methodology for fault recovery and re-entry of a faulty part is presented, where a single working process is not in deadlock, which guarantees that the S<sup>4</sup>RP remains active even if an unreliable processing unit fails. Thus, the S<sup>4</sup>RP is always live.

This study introduces a new control technique in order to derive an LES for RMSs. It reports an improved class of generalized PNs, called an S<sup>4</sup>RP, which exposes how a failed part re-enters a system and is re-processed. We also employ a siphon-based max-controllability DPP to control the S<sup>4</sup>RP. A complete analysis is conducted, showing that the controlled S<sup>4</sup>RP is deadlock-free. Note that either inhibitor arcs or enumerating a reachability graph is necessary, which leads to less computational overheads and ensures that all predefined processing steps can be done continuously. We consider all unreliable resources in an MRS and the proposed method is applicable to a complex Petri net model for multiple unreliable resources.

This article is structured as follows. The deadlock problem in an MRS and deadlock control for an  $S^4R$  by max-controllability of siphons are reviewed in Section II. A novel generalized net subclass  $S^4RP$  is presented in Section III. The proposed model can well represent a part's failure and re-entry to a system when its quality test fails. Section IV introduces robust deadlock control for this net subclass via max-controllability of siphons, where an algorithm and a complete analysis for an illustrative example are given. Finally, conclusions are drawn in Section V. The basic definitions and properties of  $S^4R$  used throughout the paper can be found in [65], [66].

# **II. PRELIMINARIES**

# A. DEADLOCK IN AN MRS

A resource allocation graph (RAG) [63] is an effective tool to represent resource allocation relationships between processes and resources in an underlying system. An RAG is a digraph (V, E) with V and E being the sets of nodes and directed edges, respectively. Let  $V = P \cup Q$  with  $P \cap Q = \emptyset$ , where P is a set of processes and Q is the set of resources. In this sense, an RAG is a bipartite graph. An edge  $d_{ij} = (x_i, y_j)$ is a request edge if  $x_i \in P$  and  $y_j \in Q$ . An edge  $d_{ji} = (y_j, x_i)$  is a grant edge if  $y_j \in Q$  and  $x_i \in P$ . In a path  $(x_{i1}, y_{j1}), (y_{j1}, x_{i2}), \dots, (x_{ik}, y_{jk}), \dots, (y_{js}, x_{is+1})$ , each edge is distinct.

The reachable set of a node collects the nodes such that there exists a path from the node to every element in the reachable set. A knot is a non-empty set K of nodes satisfying the fact that the reachable set of each node in K is exactly K [64].

In an MRS, a process may request multiple units of a type of resource, which can be represented in the underlying RAG by multiple edges, each of which is labeled with an integer denoting the number of units assigned. This alternative representation is said to be a weighted RAG (WRAG). Fig. 1 depicts System-on-a-Chip (SoC) as an example of an MRS with five processors and four multi-unit resources. In this example, a process runs on a processor. Fig. 1(b) visualizes a current resource allocation status in a form of WRAG.

Fig. 2 depicts an RAG with knot  $K = \{p_1, p_2, p_3, q_1, q_2\}$  that represents a circular wait. A resource in an MRS can be requested and occupied as long as there are enough available units to be allocated. On the other hand, once a single-unit resource is occupied by a process, all the others that request it have to wait until it is released. We accordingly assume that (1) the capacity of a resource is fixed, i.e., it has a fixed number of processing units, and (2) a resource unit is granted without any time delay if it is available.

### B. DEADLOCK CONTROL FOR S<sup>4</sup>R

Here we first recall a DPP for an S<sup>4</sup>R [47], derived from the notion of siphon's max-controllability. Details regarding generalized PNs are taken from [65]. Given a place p, the maximal weight of its output arcs is denoted by  $max_p \bullet$ .

Definition 1 ([65]): Given a marked S<sup>4</sup>R net  $(N, M_0)$  and a siphon S in N, S is said to be max-marked at a marking  $M \in R(N, M_0)$  if there exists a place  $p \in S$  such that  $M(p) \ge max_p \bullet$  holds. S is said to be max-controlled if it is max-marked at any marking  $M \in R(N, M_0)$ . If all strict minimal siphons (SMSs) are max-controlled, a marked S<sup>4</sup>R is said to satisfy the max cs-property (controlled-siphon property).

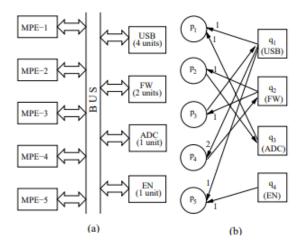


FIGURE 1. SoC example with its corresponding (WRAG).

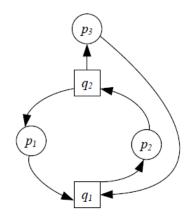


FIGURE 2. Resource allocation Graph (RAG) with a knot.

Theorem 1 ( [65]): A marked  $S^4R$  net  $(N, M_0)$  is live if it satisfies the max cs-property.

*Theorem 2* ( [65]): Let  $(N, M_0)$  be a marked S<sup>4</sup>R and S be a siphon. S is max-controlled if

 $\widehat{\exists} \operatorname{P-invariant} I, \forall p \in || I ||^{-} \cap S, max_{p} \bullet = 1, || I ||^{+} \subseteq S, \\ \sum_{p \in P} I(p) M_{0}(p) > \sum_{p \in S} I(p) (max_{p} \bullet - 1).$ 

In what follows, we write PI for a P-invariant. Let *S* be a siphon in an S<sup>4</sup>R that is composed of *n* state machines.  $\forall i \in \mathbb{N}_n = \{1, 2, ..., n\}, \forall S \in \Pi, \wp^s = \bigcup_{i=1}^n \wp_s^i, \text{ let } \wp_s^i = [S^i] \cup \{p \in P_A^i \mid p < \overline{N_l}[S^i]\}.$  For this *S*, a non-negative *P*-vector  $k_s$  for *S* is constructed, and it is assumed that  $\forall i \in \mathbb{N}_l, [S]^i \neq \emptyset; \forall j \in \mathbb{N}_n \setminus \mathbb{N}_l, [S]^i = \emptyset$ , where  $\mathbb{N}_l \subseteq \mathbb{N}_n$ . We define  $B_s^i = \{p \mid p \in [S]^i, \nexists p' \in [S]^i, p <_{\overline{N_l}} p'\}$  [66].

Note that  $\Pi$  denotes the set of all SMSs in *N*, and we use  $\overline{N_l}$  to represent the S<sup>2</sup>P of the *i*-th S<sup>2</sup>PR  $N_i$ .

*Definition 2 ( [66])*: A P-vector  $k_s$  for a siphon S in an S<sup>4</sup>R is constructed as follows:

$$\forall p \notin \wp^{s}, k_{s}(p) := 0$$
  

$$\forall p \in [S], k_{s}(p) := h_{s}(p)$$
  
*i*: =1  
*repeat*  

$$\forall p \in B^{i}, \varphi_{s} := max[h(p), h(p)]$$

$$\forall p \in B_s^i, \alpha_p := max\{h_s(p), h_s(p') \mid p' < \overline{N_l}p, p' \in [S]^i\}$$

 $\forall p_x \in \{p \mid p \in B_s^i\} \cup \{p' \mid p' < \overline{N_l}p, p' \in [S]^i\}, k_s(p_x) :=$  $\alpha_p$  $\forall p_y \in \{p'' \mid p'' < \overline{N_l}p, p \in B_s^i, p'' \in \wp^s \setminus [S]^i\}, k_s(p_y) :=$  $\alpha_p$  $\forall p_z \in \bigcap p_{w \in B_s^i} \{ p \mid p \in \mathcal{D}^s \setminus [S]^i, p < \overline{N_l} p_w \}, k_s(p_z) :=$  $max\{k_s(p) \mid p \in B_s^i\}$ i := i + 1until  $i \ge l+1$ To demonstrate Definition 2,  $k_s$  for the SMS in the net model in Fig. 3 is computed, where  $p_1^0 = p_7$ ,  $p_2^0 = p_{11}$ ,  $P_A^1 = \{p_1 - p_6\}$ ,  $P_A^2 = \{p_8 - p_{10}\}$ ,  $P_R^1 = \{p_{12} - p_{15}\}$ , and  $P_R^2 = \{p_{12} - p_{14}\}$ . It has three SMSs:  $S_1 = \{p_3, p_6, p_9, p_{13}, p_{14}\},\$  $S_2 = \{p_2, p_5, p_{10}, p_{12}, p_{13}\},$  and  $S_3 = \{p_3, p_6, p_{10}, p_{12}, p_{13}, p_{14}\}.$ We have  $\wp_s^1 = \{p_1, p_2, p_5, p_8\}, \wp_s^2 = \{p_1, p_8, p_9\}, \text{ and } \wp_s^3 =$  $\{p_1, p_2, p_5, p_8, p_9\}.$ For  $S_1$ ,  $[S_1] = p_2 + p_5 + p_8$ ,  $\forall p \notin \wp_s^1, k_s^1(p) = 0, B_s^1 =$  $\{p_2, p_5, p_8\}.$ For  $p_2 \in B_s^1$ , we have  $\alpha_{p_2} := 1,$  $k_s^1(p_2) := 1,$  $k_s^1(p_1) = k_s^1(p_2) = k_s^1(p_5) = 1.$ For  $p_8 \in B_s^1$ , we have  $\alpha_{p_8} := 1,$  $k_{s}^{1}(p_{8}) := 1,$ In summary, we have  $k_s^1(p_1) = k_s^1(p_2) = k_s^1(p_5) =$  $k_s^1(p_8) = 1.$ For  $S_2$ ,  $[S_2] = 2p_1 + p_9, \forall p \notin \wp_s^2, k_s^2(p) = 0, B_s^2 =$  $\{p_1, p_9\}.$ For  $p_1 \in B_s^2$ , we have  $\alpha_{p_1} := 2,$  $k_s^2(p_1) := 2.$ For  $p_9 \in B_s^2$ , we have  $\alpha_{p_9} := 1,$  $k_s^2(p_9) := 1,$ In summary, we have  $k_s^2(p_8) = k_s^2(p_9) = 1$ , and  $k_s^2(p_1) =$ 2. For  $S_3$ ,  $[S_3] = 2p_1 + p_2 + p_5 + p_8 + p_9$ ,  $\forall p \notin \wp_s^3$ ,  $k_s^3(p) =$  $0, B_s^3 = \{p_2, p_5, p_9\}.$ For  $p_2 \in B_s^3$ , we have  $\alpha_{p_2} := max(1, 2) = 2,$  $(p_2) := 2,$  $k_s^3(p_1) = k_s^3(p_2) = 2.$ For  $p_5 \in B_s^3$ , we have  $\alpha_{p_5} := max(1, 2) = 2,$  $k_s^3(p_5) := 2.$ For  $p_9 \in B_s^3$ , we have  $\alpha_{p_9} := 1,$  $(p_9) := 1,$  $k_s^3(p_8) = k_s^3(p_9) = 1$ . In summary, we have  $k_s^3(p_8) =$  $k_s^3(p_9) = 1$ , and  $k_s^3(p_1) = k_s^3(p_2) = k_s^3(p_5) = 2$ . Theorem 3 ([65]): Let S be an SMS in an S<sup>4</sup>R (N, M<sub>0</sub>)

Theorem 3 ([65]): Let S be an SMS in an S<sup>4</sup>R (N, M<sub>0</sub>) with  $N = (P_A \cup P^0 \cup P_R, T, F, W)$ . A monitor  $V_S$  is added to  $(N, M_0)$  such that  $g_S = k_S + V_S$  is a PI of the resulting

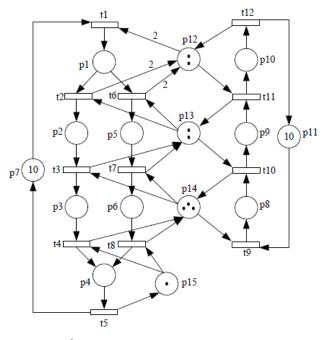


FIGURE 3. An S<sup>4</sup>R ( $N, M_0$ ).

net  $(N_V, M_0^V)$ , where  $N_V = (P_A \cup P^0 \cup P_R \cup \{V_S\}, T, F \cup F_V, W \cup W_V)$ ;  $\forall p \in P_A \cup P^0 \cup P_R, M_0^V(p) = M_0(p)$ . Let  $f_S = \sum_{\substack{r \in \mathcal{R} \\ S}} I_r - g_S$  and  $M_0^V(V_S) = M_0(S) - \xi_S(\xi_S \in \mathbb{N}^+)$ . Then, S is max-controlled if  $\xi_S > \sum_{p \in S} f_S(p)(max_p^{\bullet} - 1)$  and  $M_0^V(V_S) \ge max_{v_S}^{\bullet}$ .

Based on Theorem 3, for  $S_1 = \{p_3, p_6, p_9, p_{13}, p_{14}\}$  in the S<sup>4</sup>R net shown in Fig. 3, by Definition 2, we have  $k_S^1 = p_1 + p_2 + p_5 + p_8$ . As a result,  $g_S^1 = k_S^1 + V_S^1 = p_1 + p_2 + p_5 + p_8 + V_S^1$ . Notice that  $\sum_{r \in S_1^R} I_r = I_{p_{13}} + I_{p_{14}} = p_2 + p_3 + p_5 + p_6 + p_8 + p_9 + p_{13} + p_{14}, f_{S_1} = \sum_{r \in S_1^R} I_r - g_S^1 = p_3 + p_6 + p_9 + p_{13} + p_{14} - p_1 - V_S^1$ .

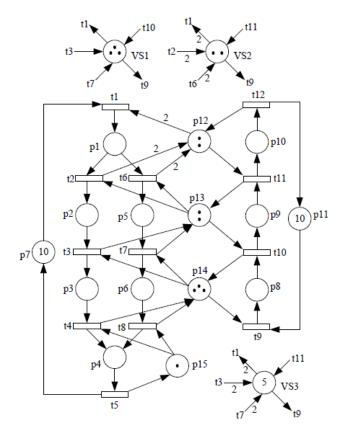
 $p_{13} + p_{14} - p_1 - V_S^1$ .  $f_{S_1}$  is a PI of  $N_V$ . Let  $\xi_S^1 = 2$ . As a result, it holds  $\xi_{S_1} > \sum_{p \in S_1} f_{S_1}(p)(max_{p^{\bullet}} - 1) = 0$ . We conclude that  $S_1$  is max-controlled by adding  $V_S^1$  with  $M_0^V(V_{S_1}) = 3$ . Similarly,  $S_2$  and  $S_3$  are max-controlled by adding monitors  $V_S^2$  and  $V_S^3$ , respectively, with  $\xi_S^2 = 2$ ,  $\xi_S^3 = 2$ ,  $M_0^V(V_{S_2}) = 2$ , and  $M_0^V(V_{S_3}) = 5$ . The resulting controlled net is shown in Fig. 4, which makes the net live.

Theorem 4 ( [67]):  $(N_V, M_0^V)$  is obtained by adding monitors for all SMSs in an S<sup>4</sup>R model  $(N, M_0)$  according to Theorem 3. Then, it is live.

# III. S<sup>4</sup>RP AS AN IMPROVED S<sup>4</sup>R

# A. S<sup>4</sup>RP

Previous studies [68]–[77] have not treated some changes in an RMS caused by a variety of reasons, such as processing failures and equipment breakdowns. In an MRS, these changes may consist of newly added machines as well as the newly released product orders, or shifts in processing routes triggered by market competition in much detail. To



**FIGURE 4.** The live  $S^4 R(N_V, M_0^V)$  with three siphons being max-controlled by monitors.

this end, an improved net model to S<sup>2</sup>PR, namely a simple sequential process with resources and part-re-entry (S<sup>2</sup>PRP), is proposed, which can deal with the dynamic changes in an RMS.

Since an S<sup>4</sup>R is a generalized class of Petri net consisting of two or more WS<sup>2</sup>PRs composed together through the shared resources, in this study, we extend our previous work [46] to an S<sup>4</sup>R.

Definition 3 ([46]): Termination place (transition)  $p_t(t_t)$  is defined as the last place in a simple sequential process  $(S^2P)$ (the last transition) in an S<sup>2</sup>P if  $P_A \cap {}^{\bullet}t_t = \{p_t\}$ .

Definition 4: A system of sequential systems with shared resources and part-re-entry (S<sup>4</sup>RP), denoted as  $(N, M_0) =$  $(P, T, F, W, M_0, C, \Psi(p_a, p_r, T_e, F_e))$ , is defined as follows:

- 1)  $P = P_A \cup \{p_a\} \cup P^0 \cup P_R \cup \{p_r\}$ , where  $P_A = \bigcup_{i=1}^n P_A^i$ is called the set of operation places such that  $P_A^i \cap P_A^j = \emptyset$ ,  $\forall i \neq j$ , and  $p_a$  is an additional operation place for the re-entry of failed parts and  $p_r$  is an additional resource for the failed operation.  $P^0 = \bigcup_{i=1}^n \{p_i^0\}$  is called the set of idle places with  $P^0 \cap (P_A \cup \{p_a\}) = \emptyset$ ,  $p_r$  is an additional resource place that represents a test machine TM, and  $P_R = \{r_1, r_2, \dots, r_m\}$  is called the set of resource places such that  $((P^0 \cup \{P_A \cup \{p_a\}) \cap (P_R \cup \{p_r\}) = \emptyset;$
- 2)  $T = \bigcup_{i=1}^{n} T_i$ , and  $\forall i \neq j, T_i \cap T_j = \emptyset$ ;
- 3)  $W = W_A \cup W_R$ , where  $W_A : (P_A \cup \{p_a\} \cup P^0) \times T) \cup (T \times (P_A \cup \{p_a\} \cup P^0)) \longrightarrow \{0, 1\}$  such that  $\forall j \neq i, ((P_A^j \cup P^0)) \longrightarrow \{0, 1\}$

- $\{p_a^j, p_j^0\} \times T_i) \cup (T_i \times (P_A^j \cup \{p_a^j, p_j^0\})) \longrightarrow \{0\}, \text{ and } W_R : (P_R \cup \{p_r\} \times T) \cup (T \times P_R \cup \{p_r\}) \longrightarrow \mathbb{N};$ 4)  $\forall j \in \mathbb{N}_n = \{1, 2, \dots, n\}, \text{ the subnet } N_j \text{ derived from } P_A^j \cup \{p_j^0\} \cup T_j \text{ is a strongly connected state machine } 0$ such that every circuit contains  $p_i^0$ ;
- 5)  $\forall r \in P_R$ , there exists a unique  $PI I_r$  such that  $|| I_r ||$  $\bigcap P_R = \{r\}, \parallel I_r \parallel \bigcap P^0 = \emptyset, \parallel I_r \parallel \bigcap P_A \neq \emptyset, \text{ and } I_r(r) = 1. \text{ Furthermore, } P_A = (\bigcup_{r \in P_R} \parallel I_r \parallel) \setminus P_R;$
- 6) *N* is pure and strongly connected;
- 7)  $M_0: P \longrightarrow \mathbb{N}$  is the initial marking of  $N. C: P \longrightarrow \mathbb{N}$ is a capacity function, where C(p) indicates the bound of the place p.
- 8)  $T_e = \{t_i, t_f\} \mid (T_e \cap \bullet p_a = \{t_i\}) \land (T_e \cap p_a^{\bullet} = \{t_f\});$
- 9)  $(\bullet p_r = \{t_i, t_i\}) \land (p_r^{\bullet} = \{t \in T \mid t^{\bullet} = p_t\});$  and
- 10)  $F_e \subseteq (P \cup \{p_a, p_r\} \times T \cup T_e) \cup (T \cup T_e \times P \cup \{p_a, p_r\}).$
- 11)  $\forall p \in P_A, M_0(p) = 0; \forall r \in P_R, M_0(r) \geq$  $max_{p \in ||I_r||}I_r(p); M_0(p_a) = 0; M_0(p_r) = 1; \forall p_i^0 \in P^{\overline{0}},$  $M_0(p_i^0) \ge 1.$

Definition 5: Let  $(N, M_0) = (P, T, F, W, M_0, C, \Psi(p_a, M_0))$  $p_r, T_e, F_e$ )) be an S<sup>4</sup>RP. N is self-loop-free if for all  $x, y \in$  $P_A \cup \{p_a\} \cup P^0 \cup P_R \cup \{p_r\} \cup T; W(x, y) > 0$  means W(y, x) = 0.

Definition 6: Let  $(N, M_0) = (P, T, F, W, M_0, C, \Psi(p_a, M_0))$  $p_r, T_e, F_e$ )) be an S<sup>4</sup>RP. The marking M' reachable by firing an enabled transition  $t \in T(M[t)M')$  satisfies

$$M'(p) = \begin{cases} M(p) - W(p, t) + W(t, p), & \forall p \in (^{\bullet}t \cap t^{\bullet}); \\ M(p) - W(p, t), & \forall p \in (^{\bullet}t \setminus t^{\bullet}); \\ M(p) + W(t, p), & \forall p \in (t^{\bullet} \setminus ^{\bullet}t); \\ M(p), & \text{otherwise} \end{cases}$$

Definition 7: Let  $(N, M_0) = (P, T, F, W, M_0, C, \Psi(p_a, M_0))$  $p_r, T_e, F_e$ )) be an S<sup>4</sup>RP. N is said to be ordinary if for all  $(p, t) \in F, W(p, t) = 1$ ; otherwise it is generalized.

Definition 8: Let  $(N, M_0) = (P, T, F, W, M_0, C, \Psi(p_a, M_0))$  $p_r, T_e, F_e$ ) be an S<sup>4</sup>RP. The reachability set of  $(N, M_0)$  is denoted by  $R(N, M_0)$ . A transition  $t \in T$  is live if for all  $M \in$ R(N, M), there exists a reachable marking  $M' \in R(N, M)$ such that M'[t) holds.  $(N, M_0)$  is said to be dead at  $M_0$  if there is no  $t \in T$  such that M'[t).

Definition 9: Let  $(N, M_0) = (P, T, F, W, M_0, C, \Psi(p_a, M_0))$  $p_r, T_e, F_e$ )) be an S<sup>4</sup>RP. A marking  $M_0$  is said to be reversible if for each marking  $M' \in R(N, M_0)$ ,  $M_0$  is reachable from M'.

Definition 10: Let  $(N, M_0) = (P, T, F, W, M_0, C, \Psi(p_a, M_0))$  $p_r, T_e, F_e$ )) be an S<sup>4</sup>RP. A marking M' is said to be coverable if for each  $p \in P$ , there exists a marking  $M'' \in R(N, M_0)$  such that  $M''(p) \ge M'(p)$ .

# B. BUILDING AN S<sup>4</sup>RP

To explain the construction of an S<sup>4</sup>RP, let us model an RMS (with four robots  $R_1 - R_4$  and three machine tools  $M_1 - M_3$ ) whose layout is shown in Fig. 5 and production routines are in Fig. 6. Each robot (except for  $R_4$ ) can hold one product at a time, while the capacity of  $R_4$  is 3. The capacities of  $M_1, M_2$ , and  $M_3$  are two, three, and three, respectively. There are three loading buffers  $I_1$ – $I_3$  and three unloading buffers  $O_1$ – $O_3$ . The

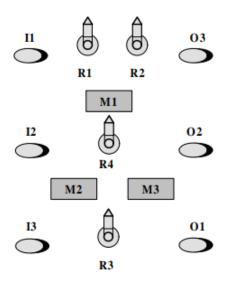


FIGURE 5. An RMS layout.

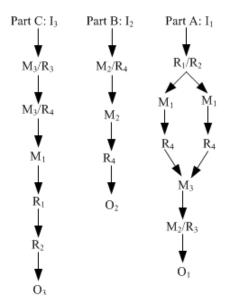
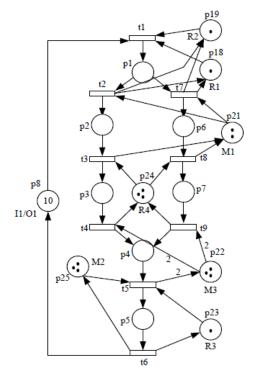


FIGURE 6. The production routings of an RMS.

system can produce three part types, namely A, B, and C. In Fig. 6, r/r' implies an alternative resource requirement for r and r' for a processing step. Fig. 7 represents the PN model  $(N, M_0)$  for working process of part A.

Now, we consider the case that the working process fails to produce a part A. According to the policy in [46], to take into account the processing failure and rework, a test machine TM is needed. Fig. 8 represents the Petri net model  $(N, M_0)$  that models the normal (as colored black) and re-entry operations (as colored red). Table 1 presents the physical meaning of the new improved part of the net model shown in Fig. 8.

The net model in Fig. 8 is a weighted simple sequential processes with resources and part-re-entry (WS<sup>2</sup>PRP), where  $p^0 = p_8$ ,  $P_A = \{p_i \mid i = 2, 3, ..., 7\}$ ,  $P_R = \{p_{18}, p_{19}, p_{21}, p_{22}, p_{23}, p_{24}, p_{25}\}$ ,

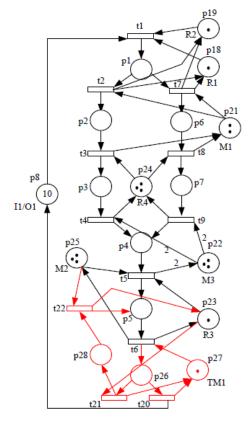


**FIGURE 7.** The petri net model  $(N, M_0)$  for working process 1.

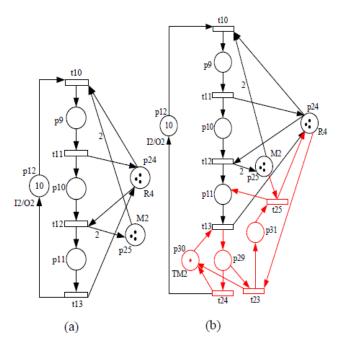
 $T = \{t_i \mid i = 1, 2, ..., 9\}$ . Places  $p_{18}, p_{19}, p_{21}, p_{22}, p_{23}, p_{24}$ and  $p_{25}$  represent  $R_1, R_2, M_1, M_3, R_3, R_4$  and  $M_2$ , respectively. Before a system starts, no parts are in it.  $M_0(p_8) = 10$ represents the number of instances that should be processed for part type  $P_1 \longrightarrow A$ ,  $p_a = p_{28}$ ,  $p_r = p_{27}$ ,  $p_t = p_{26}$ ,  $t_t = p_{26}$  $t_{20}, T_e = \{t_i, t_f\}$  with  $t_i = t_{21}$  and  $t_f = t_{22}$ , respectively; F = $\{(p_8, t_1), (t_1, p_1), (p_1, t_2), (t_2, p_2), (p_2, t_3), (t_3, p_3), (p_3, t_4), \}$  $(t_4, p_4), (p_1, t_7), (t_7, p_6), (p_6, t_8), (t_8, p_7), (p_7, t_9), (t_9, p_4),$  $(p_4, t_5), (t_5, p_5), (p_5, t_6), (t_6, p_8), (p_{18}, t_1), (p_{19}, t_1), (t_2, p_{18}),$  $(t_2, p_{19}), (t_7, p_{18}), (t_7, p_{19}), (p_{21}, t_7), (p_{21}, t_2), (t_3, p_{21}),$  $(t_8, p_{21}), (t_4, p_{24}), (t_9, p_{24}), (p_{24}, t_3), (p_{24}, t_8), (p_{22}, t_4),$  $(p_{22}, t_9), (t_5, p_{22}), (p_{23}, t_5), (t_6, p_{23}), (p_{25}, t_5), (t_6, p_{25})\}, F_e =$  $\{(t_6, p_{26}), (p_{26}, t_{20}), (p_{26}, t_{21}), (t_{21}, p_{28}), (p_{28}, t_{22}), (t_{22}, p_5), \}$  $(t_{22}, p_{23}), (p_{23}, t_{21}), (p_{25}, t_{22}), (t_{20}, p_{27}), (t_{21}, p_{27}), (p_{27}, t_6)\},\$ the weights of all arcs are equal to one, except that the weights of arcs in  $\{(p_{22}, t_4), (p_{22}, t_9), (t_5, p_{22})\}$  are equal to two. Finally, the capacities of the resources are  $C(R_1) =$  $C(R_2) = C(R_3) = 1, C(R_4) = 3, C(M_1) = 2,$  and  $C(M_2) = C(M_3) = 3.$ 

According to Fig. 6, the Petri net model  $(N, M_0)$  for the working process 2 can be established as shown in Fig. 9(a) and Fig. 9(b) represents the PN model  $(N, M_0)$  which explains the reconfiguration of the working process when it fails to produce a qualified product B. The part with black arcs of the PN models the normal process, while the part with red arcs models the re-entry case. Table 2 demonstrates the implications of the new improved part of the net model in Fig. 9(b).

The net model shown in Fig. 9(b) is a weighted simple sequential processes with resources and part-re-entry



**FIGURE 8.** The Petri net model  $(N, M_0)$  explaining the re-entry part for working process 1.



**FIGURE 9.** (a) The Petri net model  $(N, M_0)$  for working process 2, and (b) The petri net model  $(N, M_0)$  explaining the re-entry behaviour for working process 2.

(WS<sup>2</sup>PRP), where  $p^0 = p_{12}$ ,  $P_A = \{p_9, p_{10}, p_{11}\}$ ,  $P_R = \{p_{24}, p_{25}\}$ , and  $T = \{t_{10}, t_{11}, t_{12}, t_{13}\}$ . Places  $p_{24}$  and  $p_{25}$  represent  $R_4$  and  $M_2$ , respectively. At an initial stage, no parts

# TABLE 1. Physical meaning of the re-entry part in the net model shown in Figure 8.

	Meaning
_p/t	
$t_6$	When firing, robot $R_3$ is released and a finished part is dropped into place $p_{26}$ for test.
$p_{26}$	The final part is downloaded for testing by the test machine $p_{27}$ .
$t_{20}$	Its firing means that the test succeeds, and a final part is downloaded into output buffer $p_8$ .
$t_{21}$	Its firing means that a failed part re-enters the system and is re-uploaded by robot $R_3$ .
$p_{28}$	A failed part is downloaded.
$t_{22}$	When firing, a failed part is re-manufactured by machine $M_2$ and uploaded into $p_5$ .
$p_{18}$	Robot 1 $(R_1)$ with one unit available.
$p_{19}$	Robot 2 $(R_2)$ with one unit available.
$p_{21}$	Machine 1 $(M_1)$ with two units available.
$p_{22}$	Machine 3 $(M_3)$ with three units available.
$p_{23}$	Robot 3 $(R_3)$ with one unit available.
$p_{24}$	Robot 4 $(R_4)$ with three units available.
$p_{25}$	Machine 2 $(M_2)$ with three units available.
no7	Test machine 1 $TM_1$ available.

# **TABLE 2.** Physical meaning of the re-entry part in the net model shown in Figure 9(b).

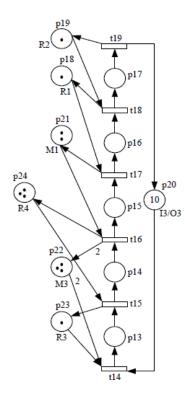
p/t	Meaning
$t_{13}$	When firing, robot $R_4$ is released and a finished part is dropped into place $p_{29}$ for test.

- $p_{29}$  A final part is unloaded for testing by the test machine  $p_{30}$ .
- $t_{24}$  Its firing means that the test succeeds, and a final part is loaded into output buffer  $p_{12}$ .  $t_{23}$  Its firing means that a failed part re-enters the system and is re-uploaded by robot  $R_4$ .
- $t_{23}$  Its firing means that a fai  $p_{31}$  A failed part is unloaded.
- $p_{31}$  A failed part is unloaded.  $t_{25}$  When firing, a failed part is re-manufactured by machine  $M_2$  and loaded into  $p_{11}$ .
- $p_{24}$  Robot 4  $(R_4)$  with three units available.
- $p_{30}$  Test machine 2  $TM_2$  available.

are present in a system.  $M_0(p_{12}) = 10$  represents the number of instances to be processed for part type  $P_2 \longrightarrow B$ ,  $p_a = p_{31}$ ,  $p_r = p_{30}$ ,  $p_t = p_{29}$ ,  $t_t = t_{24}$ ,  $T_e = \{t_i, t_f\}$  with  $t_i = t_{23}$  and  $t_f = t_{25}$ , respectively;  $F = \{(p_{12}, t_{10}), (t_{10}, p_9), (p_9, t_{11}), (t_{11}, p_{10}), (p_{10}, t_{12}), (t_{12}, p_{11}), (p_{11}, t_{13}), (t_{13}, p_{12}), (p_{24}, t_{10}), (p_{24}, t_{12}), (p_{25}, t_{10}), (t_{11}, p_{24}), (t_{12}, p_{25}), (t_{13}, p_{24})\}$ ,  $F_e = \{(t_{13}, p_{29}), (p_{29}, t_{24}), (p_{25}, t_{25}), (t_{23}, p_{30}), (p_{31}, t_{25}), (t_{25}, p_{11}), (t_{25}, p_{24}), (p_{24}, t_{23}), (p_{25}, t_{25}), (t_{24}, p_{30}), (t_{23}, p_{31}), (p_{30}, t_{13})\}$ , the weights of all arcs are equal to one, except that the weights of arcs  $\{(p_{25}, t_{10}), (t_{12}, p_{25})\}$  are equal to two. Finally, the capacity of the resources is  $C(R_4) = C(M_2) = 3$ .

According to the production cycles shown in Fig. 6, the Petri net model  $(N, M_0)$  for the working process 3 can be constructed, as visualized in Fig. 10 and Fig. 11 represents the Petri net model  $(N, M_0)$  that explains the reconfiguration of the working process when it fails to produce a qualified product C. The part with black arcs of the PN models the normal process, while the part with red arcs models the re-entry case. Table 3 presents the physical meaning of the new improved part of the net model shown in Fig. 11.

The net model shown in Fig. 11 is a weighted S<sup>2</sup>PRP, where  $p^0 = p_{20}$ ,  $P_A = \{p_i \mid i = 13, 14, ..., 17\}$ ,  $P_R = \{p_{18}, p_{19}, p_{21}, p_{22}, p_{23}, p_{24}\}$ , and  $T = \{t_i \mid i = 14, 15, ..., 19\}$ . Places  $p_{18}, p_{19}, p_{21}, p_{22}, p_{23}$  and  $p_{24}$  represent  $R_1, R_2, M_1$ ,  $M_3, R_3$ , and  $R_4$ , respectively. Suppose that no parts are processed at the initial state. Thus,  $M_0(p_{20}) = 10$  means the maximal number of instances to be processed for part type  $P_3 \longrightarrow C$ ,  $p_a = p_{34}, p_r = p_{33}, p_t = p_{32}, t_t = t_{26}, T_e = \{t_i, t_f\}$  with  $t_i = t_{27}$  and  $t_f = t_{28}$ , respectively;  $F = \{(p_{20}, t_{14}), (t_{14}, p_{13}), (p_{13}, t_{15}), (t_{15}, p_{14}), (p_{14}, t_{16}), (t_{16}, p_{15}), (p_{15}, t_{17}), (t_{17}, p_{16}), (p_{16}, t_{18}), (t_{18}, p_{17}), (p_{17}, t_{19}), (t_{19}, p_{19}), (p_{19}, t_{18}), (t_{18}, p_{18}), (p_{18}, t_{17}), (t_{17}, p_{21}), (p_{21}, t_{16}), (t_{16}, p_{24}), (t_{16}, p_{22}), (p_{24}, t_{15}), (p_{22}, t_{14}), (t_{15}, p_{23}), (p_{23}, t_{14})\}$ ,



**FIGURE 10.** A PN  $(N, M_0)$  for working process 3.

 TABLE 3. Physical meaning of the re-entry part in the net model shown in Figure 11.

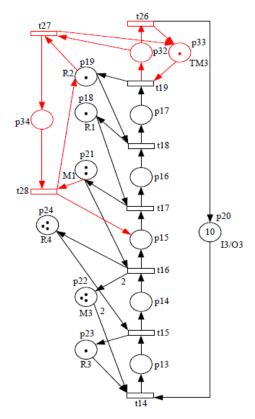
p/t	Meaning
$t_{19}$	When firing, robot $R_2$ is released and a finished part is dropped into place $p_{32}$ for test.
$p_{32}$	A final part is downloaded for testing by the test machine $p_{33}$ .
$t_{26}$	Its firing means that the test succeeds, and a final part is loaded into output buffer $p_{20}$ .
$t_{27}$	Its firing means that a failed part re-enters the system and is re-uploaded by robot $R_2$ .
$p_{34}$	A failed part is unloaded.
$t_{28}$	When firing, a failed part is re-manufactured by machine $M_1$ and uploaded into $p_{15}$ .
$p_{18}$	Robot 1 $(R_1)$ with one unit available.
$p_{19}$	Robot 2 $(R_2)$ with one unit available.
$p_{21}$	Machine 1 $(M_1)$ with two units available.
$p_{22}$	Machine 3 $(M_3)$ with three units available.
$p_{23}$	Robot 3 $(R_3)$ with one unit available.
$p_{24}$	Robot 4 $(R_4)$ with three units available.
$p_{33}$	Test machine 3 $TM_3$ available.

 $F_e = \{(t_{19}, p_{32}), (p_{32}, t_{26}), (t_{26}, p_{33}), (p_{33}, t_{19}), (p_{32}, t_{27}), (t_{27}, p_{33}), (t_{27}, p_{34}), (p_{34}, t_{28}), (t_{28}, p_{15}), (t_{28}, p_{19}), (p_{19}, t_{27}), (p_{21}, t_{28})\}$ , the weights of all arcs are equal to one, except that the weights of arcs  $\{(p_{22}, t_{14}), (t_{16}, p_{22})\}$  are equal to two. Finally, the capacities of resources are  $C(R_1) = C(R_2) = C(R_3) = 1, C(R_4) = 3, C(M_1) = 2, \text{ and } C(M_3) = 3.$ 

According to the concept of composition [66], [67], we can compose  $N_1$ ,  $N_2$ , and  $N_3$  shown in Figs. 7, 9(a), and 10 respectively to obtain an S<sup>4</sup>R that represents an RMS layout shown in Fig. 5. In the same way, we can compose  $N_1$ ,  $N_2$ , and  $N_3$ as shown in Figs. 8, 9(b), and 11 respectively to obtain an S<sup>4</sup>RP that includes the case of processing failures and rework. Fig. 12 shows the S<sup>4</sup>R and Fig. 13 illustrates its corresponding S<sup>4</sup>RP.

# **IV. ROBUST DEADLOCK CONTROL FOR S<sup>4</sup>RP**

Based on the classical deadlock prevention policy in [66], this section proposes a supervisor for an S<sup>4</sup>RP and a procedure to



**FIGURE 11.** A PN  $(N, M_0)$  that explains the re-entry part for working process 3.

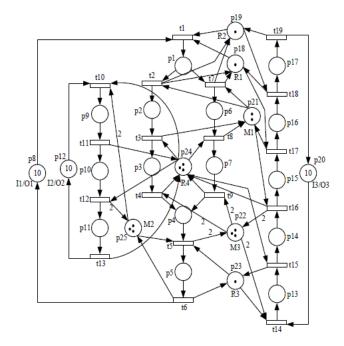


FIGURE 12. The S<sup>4</sup>R that represents an RMS layout shown in Fig. 5.

compute a robust LES and the controlled system  $(N_V, M_0^V)$  for S<sup>4</sup>RPs is developed. Here we make use of the notion of elementary siphons proposed in [65], [66] to simplify

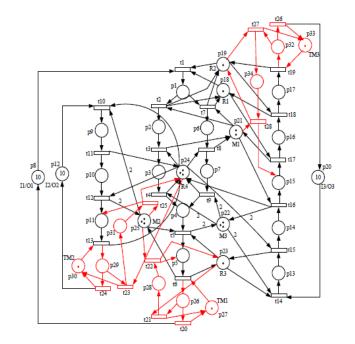


FIGURE 13. The S<sup>4</sup>RP that presents the case of processing failures and rework.

the structural complexity of the supervisor. For economy of space, the related definitions regarding elementary siphons are not presented.

Theorem 5: Let  $(N, M_0) = (P_A \cup P^0 \cup P_R, T, F, W, M_0, C, \Psi(p_a, p_r, T_e, F_e))$  be an S<sup>4</sup>RP and  $N_{ES}$  the number of its elementary siphons. Then,  $N_{ES} \leq |P_A|$ .

*Proof:* A similar proof can be found in [65].  $\Box$ In an S<sup>4</sup>RP, the control of a dependent siphon could be achieved through that of its elementary siphons. By Definition 4 and Theorem 3, we can formulate a DPP (as shown in Algorithm 1) for S<sup>4</sup>RP.

Assumption: Transitions in  $T_e = \{t_i, t_f\}$  in an S<sup>4</sup>RP  $(N, M_0) = (P, T, F, W, M_0, C, \Psi(p_a, p_r, T_e, F_e))$  are reliable (i.e., transitions that do not fail to fire whenever enabled).

Theorem 6: An S<sup>4</sup>RP ( $N, M_0$ ) = ( $P, T, F, W, M_0, C, \Psi(p_a, p_r, T_e, F_e)$ ) with an unreliable element that causes failed parts can be recovered by re-entering the failed parts and becomes live by applying Algorithm 1.

*Proof:* When a working process fails to produce a predefined product, the processing step modelled by  $P_A^i$  cannot be successfully finished such that the token in  $P_A^i$  is removed. Meanwhile, no token is in  $P_R^i$ , indicating the availability of the considered product. Thus, the transitions pertaining to the process that makes the considered product are disabled. At this state when this considered product fails to pass the test, the terminal place  $p_t$  receives a token, implying that the product is under testing by the test machine  $p_r$ . Then, transition  $t_i \in T_e$  is enabled. Enabling  $t_i \in T_e$  implies that the flawed product re-enters the system and is moved into the operation place  $p_a$ . Thus,  $t_f \in T_e$  is enabled and the flawed product re-enters the system and is re-produced by Algorithm 1 Computation of a robust LES for S<sup>4</sup>RP

**Input:**  $S^{4}RP(N, M_{0}) = (P, T, F, W, M_{0}, C, \Psi(p_{a}, p_{r}, T_{e}, F_{e})).$ 

**Output:** Robust controlled system  $(N_V, M_0^V)$  with its liveness ensured or "Undecided".

- 1. for  $i \leftarrow 1$  to n do
- 1.1 Find the possible routes  $RO_i$
- 1.2 Find the termination place  $p_t$  by Definition 3
- 1.3 Find the termination transition  $t_t$  such that  $P_A \cap {}^{\bullet}t_t = \{p_t\}$

1.4 Introduce a resource place  $p_r$  representing the test machine TM

1.5 Build the operation place  $p_a$  that receives a failed part 1.6 Build a set of extended transitions  $T_e$  and its corresponding extended arcs  $F_e$  such that

- 1.6.1  $T_e = \{t_i, t_f\} \mid (T_e \cap^{\bullet} p_a = \{t_i\}) \land (T_e \cap p_a^{\bullet} = \{t_f\})$
- 1.6.2 (• $p_r = \{t_i, t_t\}$ )  $\land$  ( $p_r^{\bullet} = \{t \in T \mid t^{\bullet} = p_t\}$ )
- $1.6.3 F_e \subseteq (P \cup \{p_a, p_r\} \times T \cup T_e) \cup (T \cup T_e \times P \cup \{p_a, p_r\}).$
- 1.7 Establish a  $WS^2$ PRP that models *RO*
- 1.8 end for

2. Construct an S<sup>4</sup>RP that models all possible routes  $RO_i$  that produce different part types by Definition 4

- 3. Compute  $\prod$  for the obtained S<sup>4</sup>RP
- 4. Compute  $\prod_E$
- 5. flag: = 0
- 6. for  $(i = 1; i < |\prod_{E} | +1; i + +)$  do
- 6.1 Compute  $k_S^i$  for  $S_i$  according to Definition 2

6.2 Add  $V_S^i$  to  $(N, M_0)$  to make  $S_i$  max-controlled based on Theorem 3 with  $M_0^V(V_S^i) = M_0(S_i) - \xi_S^i$ , where  $\xi_S^i >$ 

- $\sum_{p \in Si} f_{S_i}(p)(max_p \bullet 1)$
- $6.3 \text{ if } M_0^V(V_S) < \max_{v_{s_i^{\bullet}}} \text{ then }$
- 6.4 flag: = 1
- 6.5 end if
- 6.6 end for
- 7. **if** flag = 1 **then**
- 7.1 Output "Undecided"
- 7.2 **else**
- 7.3 **Output** a robust controlled system  $(N_V, M_0^V)$
- 7.4 end if

the machine. We infer that the PN S<sup>4</sup>RP always stays active when the unreliable element fails. Thus, the PN S<sup>4</sup>RP is live under the controlled fault recovery and re-entry process stated in Algorithm 1.  $\Box$ 

Now we explain, by Algorithm 1, how to design a robust LES by using the S<sup>4</sup>RP  $(N, M_0) = (P, T, F, W, M_0, C, \Psi(p_a, p_r, T_e, F_e))$  represented in Fig. 13 as an example.

Thanks to INA [78], 22 strict minimal siphons shown in Table 4 can be computed. It is clear that the set of elementary siphons  $\Pi_E = \{S_i \mid i = 1, 2, ..., 6\}$ , and we compute  $V_S^i$  for each siphon according to Definition 4 and Theorem 3.

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1. For elementary siphon  $S_1$ .  $S_1 = \{p_5, p_9, p_{11}, p_{14}, p_{22}, p_{24}, p_{25}\},\$  $I_{p_{22}} = 2p_4 + 2p_{13} + 2p_{14} + p_{22},$  $I_{p_{24}} = p_3 + p_7 + p_9 + p_{11} + p_{14} + p_{31} + p_{24},$  $I_{p_{25}} = p_5 + 2p_9 + 2p_{10} + p_{11} + p_{25},$  $\sum_{r \in S_1^R} I_r = p_3 + 2p_4 + p_5 + p_7 + 3p_9 + 2p_{10} + 2p_{11} + p_{11} + p$  $2p_{13} + 3p_{14} + p_{31} + p_{22} + p_{24} + p_{25}.$  $[S_1] = p_3 + 2p_4 + p_7 + 2p_{10} + 2p_{13} + p_{31},$  $\wp_s = \wp_s^1 \cup \wp_s^2 \cup \wp_s^3 = \{p_1, p_2, p_3, p_4, p_6, p_7\} \cup$  $\{p_9, p_{10}, p_{11}, p_{29}, p_{31}\} \cup \{p_{13}\},\$  $B_S^l = \{p_4, p_{31}, p_{13}\},\$  $h_s(p_3) := 1, h_s(p_4) := 2, h_s(p_7) := 1, h_s(p_{10}) :=$  $2, h_s(p_{13}) := 2, h_s(p_{31}) := 1.$ For  $p_4 \in B_S^l$ , we have  $\alpha_{p_4} := max\{2, 1\} = 2,$  $k_s(p_1) = k_s(p_2) = k_s(p_3) = k_s(p_4) = k_s(p_6) = k_s(p_7) = 2.$ For  $p_{31} \in B_S^i$ , we have  $\alpha_{p_{31}} := max\{1, 2\} = 2,$  $k_s(p_9) = k_s(p_{10}) = k_s(p_{11}) = k_s(p_{29}) = k_s(p_{31}) = 2.$ For  $p_{13} \in B_S^i$ , we have  $\alpha_{p_{13}} := 2,$  $k_s(p_{13}) := 2,$  $k_{s_1} = 2p_1 + 2p_2 + 2p_3 + 2p_4 + 2p_6 + 2p_7 + 2p_9 + 2p_{10} + 2p_{1$  $2p_{11} + 2p_{29} + 2p_{31} + 2p_{13},$  $g_{s_1} = 2p_1 + 2p_2 + 2p_3 + 2p_4 + 2p_6 + 2p_7 + 2p_9 + 2p_{10} + 2p_{1$  $2p_{11} + 2p_{29} + 2p_{31} + 2p_{13} + Vs_1,$  $f_{s_1} = \sum_{r \in S_1^R} I_r - g_{s_1} = p_5 + p_9 + p_{11} + 3p_{14} + p_{22} + p_{24} + p_$  $p_{25} - V_{s_1} - 2\dot{p}_1 - 2p_2 - p_3 - 2p_6 - p_7,$  $V_{s_1} = p_5 + p_9 + p_{11} + 3p_{14},$  $M_0^{\nu}(V_{s_1}) = 9 - \xi_{s_1},$  $2 < \xi_{s_1} \leq 8.$ 2. For elementary siphon  $S_2$ .  $S_2 = \{p_5, p_9, p_{11}, p_{14}, p_{22}, p_{23}, p_{24}, p_{28}, p_{31}\},\$  $I_{p_{22}} = 2p_4 + 2p_{13} + 2p_{14} + p_{22},$  $I_{p_{23}} = p_5 + p_{13} + p_{23} + p_{28},$  $I_{p_{24}} = p_3 + p_7 + p_9 + p_{11} + p_{14} + p_{31} + p_{24},$  $\sum_{r \in S_2^R} I_r = p_3 + 2p_4 + p_5 + p_7 + p_9 + p_{11} + 3p_{13} + 3p_{14} + p_{15} + p_{16} + p_$  $p_{31} + p_{22} + p_{23} + p_{24}.$ 
$$\begin{split} & [S_2] = p_3 + 2p_4 + p_7 + 3p_{13}, \\ & \wp_s = \wp_s^1 \cup \wp_s^2 = \{p_1, p_2, p_3, p_4, p_6, p_7\} \cup \{p_{13}\}, \end{split}$$
 $B_S^i = \{p_4, p_{13}\},\$  $h_s(p_3) := 1, h_s(p_4) := 2, h_s(p_7) := 1, h_s(p_{13}) := 3.$ For  $p_4 \in B_S^i$ , we have  $\alpha_{p_4} := max\{2, 1\} = 2,$  $k_s(p_1) = k_s(p_2) = k_s(p_3) = k_s(p_4) = k_s(p_6) = k_s(p_7) =$ 2. For  $p_{13} \in B_S^l$ , we have  $\alpha_{p_{13}} := 3,$  $k_s(p_{13}) := 3,$  $k_{s_2} = 2p_1 + 2p_2 + 2p_3 + 2p_4 + 2p_6 + 2p_7 + 3p_{13},$  $g_{s_2} = 2p_1 + 2p_2 + 2p_3 + 2p_4 + 2p_6 + 2p_7 + 3p_{13} + V_{s_2},$  $f_{s_2} = \sum_{r \in S_2^R} I_r - g_{s_2} = p_5 + p_9 + p_{11} + 3p_{14} + p_{31} + p_{22} + p_{31} + p_{32} + p_{31} + p_{32} + p_{31} + p_{32} + p_{33} + p_$  $p_{23} + p_{24} - V_{s_2} - 2p_1 - 2p_2 - p_3 - 2p_6 - p_7,$  $V_{s_2} = p_5 + p_9 + p_{11} + 3p_{14} + p_{31},$  $M_0^{\nu}(Vs_2) = 7 - \xi_{s_2},$ 

 $1 < \xi_{s_2} \le 6.$ 3. For elementary siphon  $S_3$ .  $S_3 = \{p_4, p_9, p_{11}, p_{14}, p_{22}, p_{24}, p_{31}\}, I_{p_{22}} = 2p_4 + 2p_{13} + 2p_{13$  $2p_{14} + p_{22}, I_{p_{24}} = p_3 + p_7 + p_9 + p_{11} + p_{14} + p_{31} + p_{24},$  $\sum_{r \in S_2^R} I_r = p_3 + 2p_4 + p_7 + p_9 + p_{11} + 2p_{13} + 3p_{14} + p_{14} +$  $p_{31} + p_{22} + p_{24}$ .  $[S_3] = p_3 + p_7 + 2p_{13},$  $\wp_s = \wp_s^1 \cup \wp_s^2 = \{p_1, p_2, p_3, p_6, p_7\} \cup \{p_{13}\},\$  $B_{S}^{i} = \{p_{3}, p_{7}, p_{13}\},\$  $h_s(p_3) := 1, h_s(p_7) := 1, h_s(p_{13}) := 2.$ For  $p_3 \in B_S^i$ , we have  $\alpha_{p_3} := max\{1, 1\} = 1,$  $k_s(p_1) = k_s(p_2) = k_s(p_3) = k_s(p_6) = k_s(p_7) = 1.$ For  $p_{13} \in B_{S}^{l}$ , we have  $\alpha_{p_{13}} := 2,$  $k_s(p_{13}) := 2,$  $k_{s_3} = p_1 + p_2 + p_3 + p_6 + p_7 + 2p_{13},$  $g_{s_3} = p_1 + p_2 + p_3 + p_6 + p_7 + 2p_{13} + V_{s_3},$  $f_{s_3} = \sum_{r \in S_3^R} I_r - g_{s_3} = 2p_4 + p_9 + p_{11} + 3p_{14} + p_{31} + p_{32} + p_{31} + p_{32} + p_{32} + p_{32} + p_{31} + p_{31} + p_{32} + p_{31} + p_{32} + p_{31} + p_{32} + p_{31} + p_{32} + p$  $p_{22} + p_{24} - V_{s_3} - p_1 - p_2 - p_6,$  $Vs_3 = 2p_4 + p_9 + p_{11} + 3p_{14} + p_{31},$  $M_0^{\nu}(Vs_3) = 6 - \xi s_3,$  $1 < \xi s_3 \le 5.$ 4. For elementary siphon  $S_4$ .  $S_4 = \{p_3, p_7, p_9, p_{11}, p_{15}, p_{21}, p_{24}, p_{31}\},\$  $I_{p_{21}} = p_2 + p_6 + p_{15} + p_{21},$  $I_{p_{24}} = p_3 + p_7 + p_9 + p_{11} + p_{14} + p_{31} + p_{24},$  $\sum_{r \in S_A^R} I_r = p_2 + p_3 + p_6 + p_7 + p_9 + p_{11} + p_{14} + p_{15} + p_{16} + p_{16$  $p_{31} + p_{21} + p_{24}$ .  $[S_4] = p_2 + p_6 + p_{14},$  $\wp_s = \wp_s^1 \cup \wp_s^2 = \{p_1, p_2, p_6\} \cup \{p_{13}, p_{14}\},\$  $B_S^l = \{p_2, p_6, p_{14}\},\$  $h_s(p_2) := 1, h_s(p_6) := 1, h_s(p_{14}) := 1.$ For  $p_2 \in B_S^i$ , we have  $\alpha_{p_2} := max\{1, 1\} = 1,$  $k_s(p_1) = k_s(p_2) = k_s(p_6) = 1.$ For  $p_{14} \in B_S^i$ , we have  $\alpha_{p_{14}} := 1,$  $k_s(p_{13}) = k_s(p_{14}) = 1,$  $k_{s_4} = p_1 + p_2 + p_6 + p_{13} + p_{14},$  $g_{s_4} = p_1 + p_2 + p_6 + p_{13} + p_{14} + Vs_4,$  $f_{s_4} = \sum_{r \in S_4^R} I_r - g_{s_4} = p_3 + p_7 + p_9 + p_{11} + p_{15} + p_{31} + p_{15} + p_{31} + p_{32} + p_{32}$  $p_{21} + p_{24} - V s_4 - p_1 - p_{13},$  $Vs_4 = p_3 + p_7 + p_9 + p_{11} + p_{15} + p_{31},$  $M_0^{\nu}(Vs_4) = 5 - \xi_{s_4},$  $0 < \xi_{s_4} \le 4.$ 5. For elementary siphon  $S_5$ .  $S_5 = \{p_2, p_6, p_{16}, p_{18}, p_{21}\},\$  $I_{p_{18}} = p_1 + p_{16} + p_{18},$  $I_{p_{21}} = p_2 + p_6 + p_{15} + p_{21},$  $\sum_{r \in S_{\varepsilon}^{R}} I_{r} = p_{1} + p_{2} + p_{6} + p_{15} + p_{16} + p_{18} + p_{21}.$  $[S_5] = p_1 + p_{15},$  $\wp_s = \wp_s^1 \cup \wp_s^2 = \{p_1\} \cup \{p_{13}, p_{14}, p_{15}\},\$  $B_S^i = \{p_1, p_{15}\},\$  $h_s(p_1) := 1, h_s(p_{15}) := 1.$ 

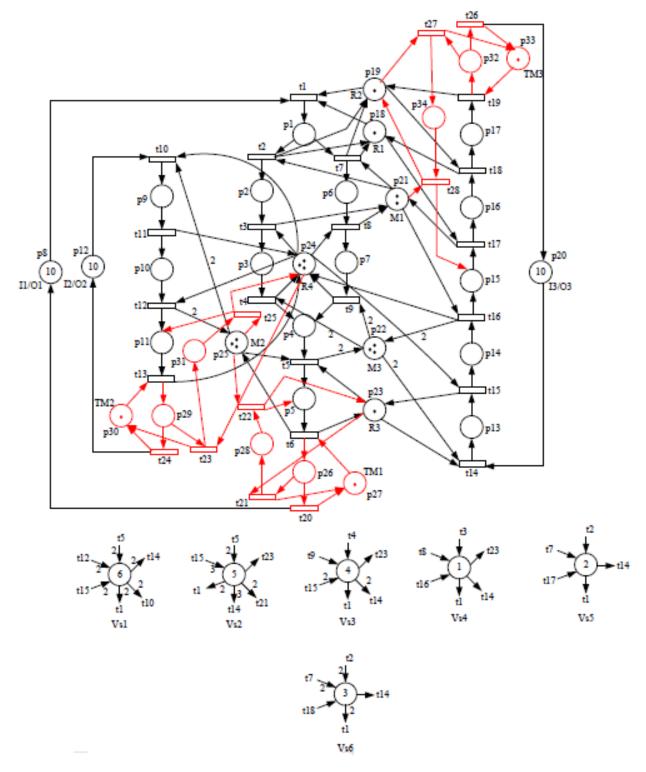


FIGURE 14. The controlled and live S<sup>4</sup>RP with processing failures and rework.

For  $p_1 \in B_S^i$ , we have $\alpha_{p_{15}} := 1$ , $\alpha_{p_1} := max\{1, 1\} = 1$ , $k_s(p_{13}) = k_s(p_{14}) = k_s(p_{15}) = 1$ , $k_s(p_1) := 1$ . $k_{s5} = p_1 + p_{13} + p_{14} + p_{15}$ ,For  $p_{15} \in B_S^i$ , we have $g_{s5} = p_1 + p_{13} + p_{14} + p_{15} + Vs_5$ ,

#### TABLE 4. SMSs in Figure 13.

Si	SMS
$S_1$	${p_5, p_9, p_{11}, p_{14}, p_{22}, p_{24}, p_{25}}.$
$S_2$	$\{p_5, p_9, p_{11}, p_{14}, p_{22}, p_{23}, p_{24}, p_{28}, p_{31}\}.$
$S_3$	$\{p_4, p_9, p_{11}, p_{14}, p_{22}, p_{24}, p_{31}\}.$
$S_4$	$\{p_3, p_7, p_9, p_{11}, p_{15}, p_{21}, p_{24}, p_{31}\}.$
$S_5$	$\{p_2, p_6, p_{16}, p_{18}, p_{21}\}.$
$S_6$	$\{p_2, p_6, p_{17}, p_{18}, p_{19}, p_{21}\}.$
$S_7$	$\{p_5, p_9, p_{11}, p_{15}, p_{21}, p_{22}, p_{23}, p_{24}, p_{28}, p_{31}\}.$
$S_8$	$\{p_5, p_9, p_{11}, p_{16}, p_{18}, p_{21}, p_{22}, p_{24}, p_{25}\}$
$S_9$	$\{p_5, p_9, p_{10}, p_{25}\}.$
$S_{10}$	$\{p_4, p_9, p_{11}, p_{17}, p_{18}, p_{19}, p_{21}, p_{22}, p_{24}, p_{31}\}.$
$S_{11}$	$\{p_4, p_9, p_{11}, p_{16}, p_{18}, p_{21}, p_{22}, p_{24}, p_{31}\}.$
$S_{12}$	$\{p_4, p_9, p_{11}, p_{15}, p_{21}, p_{22}, p_{24}, p_{31}\}.$
$S_{13}$	$\{p_5, p_9, p_{11}, p_{15}, p_{21}, p_{22}, p_{24}, p_{25}\}.$
$S_{14}$	$\{p_3, p_7, p_9, p_{11}, p_{17}, p_{18}, p_{19}, p_{21}, p_{24}, p_{31}\}.$
$S_{15}$	$\{p_3, p_5, p_7, p_9, p_{11}, p_{17}, p_{18}, p_{19}, p_{21}, p_{24}, p_{25}\}.$
$S_{16}$	$\{p_3, p_7, p_9, p_{11}, p_{16}, p_{18}, p_{21}, p_{24}, p_{31}\}.$
$S_{17}$	$\{p_3, p_5, p_7, p_9, p_{11}, p_{16}, p_{18}, p_{21}, p_{24}, p_{25}\}.$
$S_{18}$	$\{p_5, p_9, p_{11}, p_{17}, p_{18}, p_{19}, p_{21}, p_{22}, p_{24}, p_{25}\}.$
$S_{19}$	$\{p_3, p_5, p_7, p_9, p_{11}, p_{15}, p_{21}, p_{24}, p_{25}\}.$
$S_{20}$	$\{p_5, p_9, p_{11}, p_{17}, p_{18}, p_{19}, p_{21}, p_{22}, p_{23}, p_{24}, p_{28}, p_{31}\}.$
$S_{21}$	$\{p_3, p_5, p_7, p_9, p_{11}, p_{14}, p_{24}, p_{25}\}.$
$S_{22}$	$\{p_5, p_9, p_{11}, p_{16}, p_{18}, p_{21}, p_{22}, p_{23}, p_{24}, p_{28}, p_{31}\}.$

**TABLE 5.** Elementary siphons and monitors in Figure 13. Note that we use  $d_i$  to denote  $M_V O(V_S i)$ .

$S_i$	Elementary Siphon	• $V_{Si}$	$V_{S_i}$	di
$S_1$	$\{p_5, p_9, p_{11}, p_{14}, p_{22}, p_{24}, p_{25}\}$	$\{2t_5, 2t_{12}, 2t_{15}\}\$	$\{2t_1, 2t_{10}, 2t_{14}\}$	6
$S_2$	$\{p_5, p_9, p_{11}, p_{14}, p_{22}, p_{23}, p_{24}, p_{28}, p_{31}\}$	$\{2t_5, 3t_{15}\}$	$\{2t_1, 3t_{14}, 2t_{21}, t_{23}\}$	5
$S_3$	$\{p_4, p_9, p_{11}, p_{14}, p_{22}, p_{24}, p_{31}\}$	$\{t_4, t_9, 2t_{15}\}$	$\{t_1, 2t_{14}, t_{23}\}$	4
$S_4$	$\{p_3, p_7, p_9, p_{11}, p_{15}, p_{21}, p_{24}, p_{31}\}$	$\{t_3, t_8, t_{16}\}$	$\{t_1, t_{14}, t_{23}\}$	1
$S_5$	$\{p_2, p_6, p_{16}, p_{18}, p_{21}\}\$	$\{t_2, t_7, t_{17}\}$	$\{t_1, t_{14}\}$	2
$S_6$	$\{p_2, p_6, p_{17}, p_{18}, p_{19}, p_{21}\}$	$\{2t_2, 2t_7, t_{18}\}$	$\{2t_1, t_{14}\}$	3

```
f_{s_5} = \sum_{r \in S_s^R} I_r - g_{s_5} = p_2 + p_6 + p_{16} + p_{18} + p_{21} - V_{s_5} - p_{16} + p_{18} + p_{21} - V_{s_5} - p_{16} + p_{18} + p_{21} - V_{s_5} - p_{16} + p_{16} + p_{18} + p_{21} - V_{s_5} - p_{16} + p_{16} + p_{18} + p_{21} - V_{s_5} - p_{16} + p_{16} + p_{18} + p_{21} - V_{s_5} - p_{16} + p_{16} + p_{18} + p_{21} - V_{s_5} - p_{16} + p_{16} + p_{18} + p_{21} - V_{s_5} - p_{16} + p_{16} + p_{18} + p_{21} - V_{s_5} - p_{16} + p_{16} + p_{18} + p_{21} - V_{s_5} - p_{16} + p_{16} + p_{18} + p_{21} - V_{s_5} - p_{16} + p_{16} + p_{18} + p_{21} - V_{s_5} - p_{16} + p_{16} + p_{18} + p_{21} - V_{s_5} - p_{16} + p_{16} + p_{18} + p_{21} - V_{s_5} - p_{16} + p_{16} + p_{18} + p_{21} - V_{s_5} - p_{16} + p_{16}
p_{13} - p_{14},
                            Vs_5 = p_2 + p_6 + p_{16},
                            M_0^{\nu}(Vs_5) = 3 - \xi_{s_5},
                            0 < \xi_{s_5} \leq 2.
                            6. For elementary siphon S_6.
                            S_6 = \{p_2, p_6, p_{17}, p_{18}, p_{19}, p_{21}\},\
                            I_{p_{18}} = p_1 + p_{16} + p_{18},
                            I_{p_{19}} = p_1 + p_{17} + p_{19},
                            \bar{I}_{p_{21}} = p_2 + p_6 + p_{15} + p_{21},
\sum_{r \in S_6^R} \bar{I}_r = 2p_1 + p_2 + p_6 + p_{15} + p_{16} + p_{17} + p_{18} + p_{19} + p_{21}.
                             \begin{matrix} \overline{S_6} \\ \overline{S_6} \\ \overline{S_6} \\ \overline{S_7} \\ \overline{S_8} 
                            B_S^i = \{p_1, p_{16}\},\
                            h_s(p_1) := 2, h_s(p_{16}) := 1.
                            For p_1 \in B_s^i, we have
                            \alpha_{p_1} := 2,
                            k_s(p_1) := 2.
                            For p_{16} \in B_S^i, we have
                            \alpha_{p_{16}} := 1,
                            k_s(p_{13}) = k_s(p_{14}) = k_s(p_{15}) = k_s(p_{16}) = 1,
                            k_{s_6} = 2p_1 + p_{13} + p_{14} + p_{15} + p_{16},
                          g_{s_6} = 2p_1 + p_{13} + p_{14} + p_{15} + p_{16} + V_{s_6},
  f_{s_6} = \sum_{r \in S_6^R} I_r - g_{s_6} = p_2 + p_6 + p_{17} + p_{18} + p_{19} + p_{21} - V_{s_6} - p_{13} - p_{14},
                              V_{s_6} = p_2 + p_6 + p_{17},
```

Table 5 shows the elementary siphons in the S<sup>4</sup>RP in Fig. 13. Fig. 14 represents the live and controlled S<sup>4</sup>RP  $(N, M_0) = (P, T, F, W, M_0, C, \Psi(p_a, p_r, T_e, F_e))$  for the Net shown in Fig. 13.

### **V. CONCLUSION**

The main goal of the current study was to design a new DPP for preventing the occurrences of deadlocks in a reconfigurable MRS by excogitating a novel PN subclass,  $S^4RP$  for short, which addresses the case of processing failures and rework, and represents the process that a flawed part re-enters the underlying system to be re-processed. We apply a siphon-based max-controllability DPP to make the proposed  $S^4RP$  live through adding external control elements. We also use INA–a PN analyzer to validate the results.

The main results of the proposed strategy consist of the following contributions: (1) it can be extended to a generalized PN subclasses, such as ES<sup>3</sup>PR, S\*PR, S<sup>2</sup>LSPR, S<sup>3</sup>PGR<sup>2</sup> and S<sup>3</sup>PMR; (2) the proposed structural analysis techniques for S<sup>4</sup>RP do not need to generate reachability graphs; (3) it can manage failures efficiently in an MRS; (4) the developed S<sup>4</sup>RP can dynamically modify the arrangement of the PN without breaking its liveness property; (5) we include a representation of the configuration of reconfigurable manufacturing systems and provide an S<sup>4</sup>RP model for the architecture of the supervisor; and (6) an S<sup>4</sup>RP is applicable to a system with complicated resource requirements.

This research develops a generalized class of Petri nets, namely S<sup>4</sup>R that can simulate reconfigurable MRS. This means that the process can request and release more than one unit of single or multiple resources at a time. Moreover, elementary siphons are used for the case of re-entry parts in an MRS, which leads to expensive computing overheads.

In the future study, the behavioural permissiveness and structural complexity of a supervisor will be optimized and reduced. We will also focus on expanding and improving the proposed method to a system with uncontrollable and unobservable events.

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