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Auto-Diagnosis of COVID-19 Using Lung CT Images With Semi-Supervised Shallow Learning Network

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ABSTRACT In the current world pandemic situation, the contagious Novel Coronavirus Disease 2019 (COVID-19) has raised a real threat to human lives owing to infection on lung cells and human respiratory systems. It is a daunting task for the researchers to find suitable infection patterns on lung CT images for automated diagnosis of COVID-19. A novel integrated semi-supervised shallow neural network framework comprising a Parallel Quantum-Inspired Self-supervised Network (PQIS-Net) for automatic segmentation of lung CT images followed by Fully Connected (FC) layers, is proposed in this article. The proposed PQIS-Net model is aimed at providing fully automated segmentation of lung CT slices without incorporating pre-trained convolutional neural network based models. A parallel trinity of layered structure of quantum bits are interconnected using an $\mathcal N$ -connected second order neighborhood-based topology in the suggested PQIS-Net architecture for segmentation of lung CT slices with wide variations of local intensities. A random patch-based classification on PQIS-Net segmented slices is incorporated at the classification layers of the suggested semi-supervised shallow neural network framework. Intensive experiments have been conducted using three publicly available data sets, one for purely segmentation task and the other two for classification (COVID-19 diagnosis). The experimental outcome on segmentation of CT slices using self-supervised PQIS-Net and the diagnosis efficiency (Accuracy, Precision and AUC) of the integrated semi-supervised shallow framework is found to be promising. The proposed model is also found to be superior than the best state-of-the-art techniques and pre-trained convolutional neural network-based models, specially in COVID-19 and Mycoplasma Pneumonia (MP) screening.

INDEX TERMS COVID-19, QIS-Net, lung CT image segmentation, 3D-UNet and ResNet50.

I. INTRODUCTION

The world has suffered a lot in the recent pandemic due to the 2019 novel coronavirus disease (COVID-19) since its rapid outbreak from Wuhan, China. There have been sharp rises in infected and suspected cases in almost all the countries in the world from the beginning of January 2020 as reported by World Health Organization [1]. The severe effect

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of coronavirus disease has inflicted a SARS-CoV-2 acute respiratory syndrome and has resulted in a new febrile respiratory tract illness. Despite imposition of various strict measures and physical isolation guidelines, the number of positive test cases is rising rapidly and as of today (02/02/2021), the total number of confirmed cases reported in the entire world is over 102.1 million [2]. There are mainly three standard widely used diagnosis procedures viz. Reverse Transcription Polymerase Chain Reaction (RT-PCR) test from swab samples, Chest X-ray and Lung CT scan images for

COVID-19 detection [3]. However, the real-time RT-PRT test using detection of nucleotide has reported low sensitivity in China and hence it is not an effective tool for coronavirus infection detection [4] owing to lack of stability, quality and viral materials in specimens. In addition, lack of testing capabilities in the underdeveloped countries owing to insufficient test kits has spurred the demand for alternative COVID-19 diagnosis. The potential alternatives to RT-PRT test based COVID-19 detection include methods used on Lung CT scan image and Chest X-ray image segmentation. The captured lung CT scans of COVID-19 infected patients often show a bilateral patchy shadow. Moreover, Chest CT scan is a noninvasive and a fast diagnosis procedure and reported high sensitivity for pre-screening of COVID-19 infections [4]. However, with rise in the number of infections and suspected cases, it is a paramount and laborious task for the health experts to manually annotate the infected lesions and manually contour them in the current world-wide pandemic situation. In these circumstances, in order to maximize the diagnosis of the infected patients and to improve the treatment access, it is always preferred to have an automatic and robust segmentation technique followed by assessment of coronavirus infections.

A. RELATED WORKS

Recent years have witnessed the progress of deep learning technologies in the field of medical image segmentation which have become popular diagnostic tools due to key feature representation [5]–[10]. In this year, a plethora of deep learning networks have been employed for automatic detection of COVID-19 pneumonia lung CT volumes and have reported promising accuracy [11]–[15]. A multi-objective differential evolution assisted convolutional neural network (CNN) [12] is suggested for COVID-19 lung CT image classification by leveraging the hyper-parameters of the CNN. Wang *et al.* [16] proposed a weakly supervised deep learning model with the pre-trained U-Net for COVID-19 infection detection using lung CT volumes and reported high accuracy, sensitivity and specificity. Yan *et al.* [17] introduced a convolutional neural network introducing Progressive Atrous Spatial Pyramid Pooling to address the sophisticated infected lesions with overlapping and with wide variations of shape and orientation of lung CT volumes. However, owing to lack of sufficient annotated lung CT images and lack of image specific adaptability for unforeseen lung CT image classes (the infections on lung CT images vary with regions), the pre-trained CNN models fail to achieve desired accuracy. In addition to this, requirement of high computational resources to train the aforementioned deeply supervised networks is seldom a cost effective solution for COVID-19 diagnosis. To avoid the over-fitting during training of CNN based models with small data sets, a latent representation learning exploring multiple features prevalent to lung CT volumes, is suggested by Kang *et al.* [15]. In addition to this, a simple neural network model incorporating two coupled 3D Res-Nets with prior attention learning is proposed

In this article, we have proposed an integrated semisupervised shallow learning network model comprising a Parallel Quantum-Inspired Self-Supervised Neural Network (PQIS-Net) followed by fully connected classification layers for COVID-19 diagnosis. Of late, the authors have proposed quantum-inspired self-supervised networks referred to as QIS-Net [20] and QIBDS Net [21] for automatic brain lesion segmentation. Authors have also developed the optimized version of QIBDS Net referred to as Opti-QIBDS Net [22] which is found suitable for brain tumor segmentation. These self-supervised network architectures which are tailored and tested on brain MR images and efficient in brain MR image segmentation, serve as the inspiration behind the current work. In this manuscript, we aim to further investigate the parallel version of QIS-Net [20] on COVID-19 infected lung CT images without any sort of supervision or training for segmentation followed by classification using fully connected layers for feasibility analysis on COVID-19 diagnosis.

B. CONTRIBUTIONS

Eventually, in the current pandemic situation in the world, it is an uphill task for the health care professionals to acquire large volumes of lung CT images with annotations for deep supervision. Hence, the primary focus of the paper is to offer a potential alternative to deeply supervised networks using a semi-supervised shallow neural network model composed of a fully parallel self-supervised network (PQIS-Net) for appropriate segmentation for tiny COVID-19 infected lesions, and fully connected (FC) layers at the end for enabling training on weak data labels for suitable assessment of COVID-19 infections. The significant four-fold contributions of the article are highlighted as follows:

- 1) The convergence of the QIS-Net architecture is relatively slower than the Fully Connected (FC) layers and hence, there is an imbalance in the processing of segmentation using QIS-Net and classification at the FC layers. To obviate the problem, we have proposed a parallel version of the QIS-Net architecture referred to as PQIS-Net, which is found suitable for the segmentation of lung CT volumes with COVID-19 infections without any sort of supervision or training. PQIS-Net takes the CT volume (equal to batch size B) as inputs under parallel architecture, whereas QIS-Net takes brain MR image slices one at a time.
- 2) An N -connected neighborhood topology-based segmentation using PQIS-Net for taking into cognizance the wide variations of local intensities of lung CT images, is the key contribution of the proposed work.
- 3) We have also modified the loss or error function incorporated in QIS-Net which is based on the summation of

FIGURE 1. A Parallel Quantum-Inspired Self-Supervised Network (PQIS-Net) assisted semi-supervised shallow learning framework for COVID-19 diagnosis (only three inter-layer connections are shown for clarity and gray-scale segmented slices are color mapped for better visibility).

the differences of the interconnection weights between two successive iterations. Moreover, the inputs and weights of the PQIS-Net model are represented in terms of frequencies (*cos* and *sine* components) or spectral components in quantum formalism, thereby enabling faster convergence than QIS-Net which relies fully on quantum weights.

4) In addition, selections of *p*-random 2D patches from the PQIS-Net segmented images are allowed to augment the limited training data sets with high representation features to be fed to the constituent FC layers for processing training) thereby obviating over-fitting.

Rigorous experiments have been carried out considering three different publicly available data sets of COVID-19 lung CT images, one purely for segmentation task and the other two for segmentation followed by classification to facilitate an accurate diagnosis. The extensive experimental results validate our proposed semi-supervised shallow neural network model which outperforms the state of the art pre-trained CNN models with weak annotations, thus promoting auto-diagnosis with self-supervised neural network models.

The remaining portion of the manuscript is organized as follows: The proposed semi-supervised shallow neural network model comprising PQIS-Net architecture and its operation with the fully connected layers are discussed in Section [II.](#page-2-0) Experimental results and discussions including the data set details, experimental setup are provided in

Section [III.](#page-5-0) The limitations of the self-supervised PQIS-Net for lung CT image segmentation with the advantages of the proposed semi-supervised framework for COVID-19 diagnosis are highlighted in Section [IV.](#page-8-0) Finally, the concluding remarks are confabulated in Section [V.](#page-9-0)

II. PROPOSED SEMI-SUPERVISED SHALLOW NEURAL NETWORK MODEL

The Parallel Quantum-Inspired Self-Supervised Neural Network (PQIS-Net) architecture is the core of the proposed semi-supervised shallow neural learning model which is combined with fully connected layers at the end for classification and diagnosis of COVID-19 disease. The PQIS-Net is employed to segment lung CT image slices which are infected by COVID-19 or pneumonia in parallel fashion thereby reducing processing time. The PQIS-Net segmented images form highly representative features for classification. An integrated semi-supervised shallow learning model incorporating the self-supervised PQIS-Net with Fully Connected (FC) layers at the end is targeted to be developed which is appropriate for training at the FC layers with limited training data sets and can offer accurate diagnosis. The classification outcome is obtained using a majority voting scheme. A schematic outline of the proposed integrated self-supervised shallow neural network model with the fully connected layers is illustrated in Figure [1.](#page-2-1) The following subsection [II-A](#page-3-0) sheds light on the detailed description of our previously developed quantum-inspired fully self-supervised neural networks [20], [21]. A short description about the FC layers is also provided in subsection [II-C.](#page-4-0)

A. PARALLEL QUANTUM-INSPIRED SELF-SUPERVISED NEURAL NETWORK (PQIS-NET) FOR SEGMENTATION

The Parallel Quantum-Inspired Self-Supervised Neural Network architecture is the extended parallel version of our previous network architectures [20], [21]. Each one of the constituent network architectures in PQIS-Net comprises a trinity of layers of quantum neurons (represented as quantum bits or *qubits*). The incorporation of quantum-inspired computing in the suggested PQIS-Net stems from the fact that the classical self-supervised networks suffer from convergence problems [23]–[25]. The incorporation of quantum-inspired computing in the suggested parallel quantum-inspired self-supervised neural networks enables faster convergence by reducing the number of epochs with forceful termination and hence yields better accuracy in segmentation tasks [20]–[22], [26]–[28]. The network dynamics of PQIS-Net replicate the basic operation of the QIS-Net model [20] in parallel. The basis computation unit for the PQIS-Net is a quantum bit or a *qubit* designated by a quantum neuron in all the trinity of layers in the architecture in matrix notation. One such layer matrix comprising *qubits* is shown out of the identical parallel layers in the PQIS-Net as follows.

Here, each *qubit* is designated as ϕ_{ij}^l at the *l*th layer of the network architecture. The network layers are inter-connected through 8-connected spatial neighborhood neuron subsets and serve as the significant characteristic of the network architecture. In each layer of the PQIS-Net architecture, quantum neurons are also intra-linked among themselves with intra-connection strengths $\frac{\pi}{2}$ (quantum 1 logic). The N -connected neighborhood information of each candidate pixel is propagated to the subsequent layers for further computation in forward (input to hidden and hidden to output layer) and in counter-propagation fashions. The counter-propagation obviates the quantum back-propagation procedure thereby enabling faster convergence and reduced time complexity.

The principle of operation of the network is as follows. Each neuron of the network layers is designated as a *qubit* or a quantum bit and the inter-linked weights and its corresponding activation are mapped using rotation gates operating on the *qubits*. The classical input image pixels (x_i^l) at layer *l* are converted to quantum bits as

$$
|\phi_i^l\rangle = \begin{bmatrix} \cos(\frac{\pi}{2}x_i^l) \\ \sin(\frac{\pi}{2}x_i^l) \end{bmatrix} \quad i = 1, \dots m \times n \tag{1}
$$

The rotation gates are employed to update the *qubit* with rotation angle for inter-connection strength and activation as ω^l and γ^l (say) at layer *l*, respectively. The angle of rotation of an

interconnection strength, $\omega_{i,j}^l$ is decided by the adaptive and relative difference of fuzzy membership measures between the candidate pixel (*i*) and its corresponding neighborhood (j) located at its N -connected region in quantum formalism. The inspiration behind the adaptive and relative fuzzy membership measures in the evaluation of the rotation angle is to distinguish between the foreground and background image pixels. The angle of rotation is evaluated as

$$
\omega_{i,j}^l = 1 - (\mu_i^l - \mu_{i,j}^l); \quad i \in m \times n, \ j \in \{1, 2, \dots N\} \quad (2)
$$

Here, the fuzzy graded input at the *i th* candidate neuron and its corresponding spatially N-connected second-order neighborhood neuron at layer *l* are μ_i^l and $\mu_{i,j}^l$, respectively. It clearly describes the relative difference in the fuzzy membership measures between the foreground (μ_i^l) and the background regions $(\mu_{i,j}^l)$. Eg., if $\mu_i^l = 1$ and $\mu_{i,j}^l = 0$ then, $\omega_{i,j}^l$ $= 1 - (\mu_i^l - \mu_{i,j}^l) = 0$ suggests that there is no change in the rotation angle (activation remains same) and in this case, it is already segmented. On contrary, if $\mu_i^l = 1$ and $\mu_{i,j}^l = 1$, then $\omega_{i,j}^l = 1 - (\mu_i^l - \mu_{i,j}^l) = 1$ suggests that there is a significant change in the rotation angle (activation is high). A single *qubit* is updated using a rotation gate with an angle ω^l as

$$
\begin{bmatrix} \phi_{0'}^l \\ \phi_{1'}^l \end{bmatrix} = \begin{bmatrix} \cos(\frac{\pi}{2}\omega^l) & -\sin(\frac{\pi}{2}\omega^l) \\ \sin(\frac{\pi}{2}\omega^l) & \cos(\frac{\pi}{2}\omega^l) \end{bmatrix} \times \begin{bmatrix} \phi_0^l \\ \phi_1^l \end{bmatrix}
$$
 (3)

The fuzzy context sensitive activation in quantum formalism enables the bi-directional propagation (forward propagation and counter propagation). It is denoted at a layer *l* of a candidate neuron (pixel) *i* by ξ_i^l as

$$
|\xi_i^l\rangle = \begin{bmatrix} \cos \gamma_i^l \\ \sin \gamma_i^l \end{bmatrix}
$$
 (4)

where, the angle of rotation for activation ξ_i^l is γ_i^l measured as the contribution of its N -connected neighborhood neurons as

$$
\gamma_i^l = 2\pi \times (\sum_j \mu_{i,j}^l)
$$
 (5)

The network input-output dynamics of a basic quantum neuron (*i*) in the self-supervised PQIS-Net is defined at the layer *l* as

$$
|y_i^l\rangle = \sigma_{PQIS-Net}(\sum_j^8 f(y_i^{l-1}) \langle \varphi_j^l | \xi_j^l \rangle)
$$
 (6)

i.e.,

$$
|y_i^l\rangle = f(\frac{\pi}{2}\delta_i^{l-1} - \arg\{\sum_j^8 f(\omega_{j,i}^{l-1})f(y_i^{l-1}) - f(\xi_i^{l-1})\})
$$

= $\sigma_{POIS-Net}(\sum_j f(y_i^{l-1})\{\cos((\omega_{j,i}^{l-1}) - \gamma_i^{l-1})$
+ $\tau \sin((\omega_{j,i}^{l-1}) - \gamma_i^{l-1})\})$ (7)

Hence, the output at the ith quantum neuron is depicted as y_i^l and the phase transformation parameters are denoted as δ_i^{l-1} (τ is an imaginary number).

$$
|y_i^l\rangle = \sigma_{POIS-Net}(\sum_j^8 f(\frac{\pi}{2}y_j^l)\langle\varphi_{ji}^l|\xi_j^l\rangle)
$$

= $\sigma_{POIS-Net}(\sum_j^8 f(\frac{\pi}{2} \times \sigma_{POIS-Net}(\sum_l^8 f(\frac{\pi}{2}y_j^l)) \times \langle\varphi_{kj}^l|\xi_k^l\rangle)\langle\varphi_{ji}^l|\xi_j^l\rangle)$ (8)

Here, φ_{ji}^l and φ_{kj}^l are the interconnection weights between input to intermediate and intermediate to output layers, respectively.

$$
|y_i^l\rangle
$$

$$
= \sigma_{POIS-Net}(\sum_{j}^{8} f(\frac{\pi}{2} \times \sigma_{POIS-Net}(\sum_{k}^{8} f(\frac{\pi}{2} y_j^l) \cos(\omega_{kj}^l - \gamma_k^l))
$$

$$
\times s \cos(\omega_{ji}^l - \gamma_j^l) + \tau \sin(\omega_{kj}^l - \gamma_k^l) \sin(\omega_{ji}^l - \gamma_j^l)))) \quad (9)
$$

The σ*PQIS*−*Net* activation function [Quantum Multi-level Sigmoidal (QMSig)] employed in the above Equation is defined as [20], [21]

$$
\sigma_{PQIS-Net}(z; \lambda_{\theta}, \mathcal{S}_{\theta}, \gamma) = \sum_{\theta=1}^{L} \frac{1}{\lambda_{\theta} + e^{-\nu(z - (\theta - 1)\mathcal{S}_{\theta - 1} - \gamma)}} \tag{10}
$$

where,

$$
\lambda_{\theta} = \frac{\mathcal{N}_s}{\mathcal{S}_{\theta} - \mathcal{S}_{\theta - 1}}\tag{11}
$$

Hence, the outcome of two adjacent classes viz., θ and θ – 1 are S_θ and $S_{\theta-1}$, respectively and the sum of the contribution of the N -connected neighborhood pixels is designated as \mathcal{N}_s . ν denotes the steepness factor of the function and *L* is the number of gray levels in the segmented image.

A coherent network error cum loss function is introduced in PQIS-Net and is evaluated as [20] where, $\varphi(\omega_{i,j}^{i,k}, \gamma_i^{i,k})$ is the weighted inter-connection of the k^{th} parallel layer at a particular epoch *ι*, which is linearly dependent on ω and γ . B is the batch size of the constituent PQIS-Net and the semi-supervised model. The convergence analysis of the proposed PQIS-Net is demonstrated in *Appendix* section.

B. OPTIMIZATION PROCEDURE OF PQIS-NET

The activation parameter γ used in the QMSig activation function (σ) is appropriate for the uniform distribution of intensity and hence, gray-level segmentation accuracy degrades for lung CT slices due to wide variations of gray-scales having heterogeneous responses exhibited over the N -connected regions. In order to tackle this problem, we have entrusted on adaptive and optimal thresholding schemes using Quantum-inspired Differential Evolution [29] with Otsu's [30] multi-level thresholding as fitness function. There are four distinct adaptive activation schemes used for the activation parameter γ in the proposed QMSig activation function as provided below [20], [25].

(1) Activation based on β -distributed intensity of $\mathcal N$ -connected neighborhood image pixels (γ_B).

(2) Activation based on skewness (γ_{γ}).

(3) Activation based on fuzzy graded pixel heterogeneous intensity of 8-connected neighborhood (γ_{ξ}).

(4) Activation based on fuzzy cardinality estimation of 8-connected neighborhood (γ _ν).

The optimized multi-class level, (\mathcal{L}_{θ}) for fixed number of boundaries or class $\mathcal L$ is defined in a closed set $\mathcal F_{\lambda_\omega}$ as [20]

$$
\mathcal{F}_{\lambda_{\theta} \mathcal{L}} = \{ \{\lambda_{\theta \mathcal{L}}\}, \mathcal{L} = 4, 5, 6, 7, 8 \}
$$
 (12)

In order to obtain a number of optimal thresholds $\{\theta_1, \theta_2, \cdots, \theta_{C_l-1}\}$, Otsu's multi-level image thresholding [30] is incorporated to maximize the spread of the classes, and is defined as [30]

$$
\mathcal{O} = f_n\{\theta_1, \theta_2, \cdots, \theta_{C_l-1}\} = \sum_{k=1}^{C_l} w_k(r_k - r) \qquad (13)
$$

where, C_l represents the number of defined classes in $C =$ ${C_1, C_2, \ldots, C_{C_l}}$ and

$$
w_k = \sum_{i \in C_k} p_i, \quad r_k = \sum_{i \in C_k} i p_i / w_k \tag{14}
$$

where, p_i designates the i^{th} pixel and w_k represents the probability of class C_k with the mean value given by μ_k . The mean of the class C is given by m . In this work, for each multi-class level $\mathcal{L} = \{4, 6, 8\}$ four sets $\mathcal{F}_{\lambda_{\theta\mathcal{L}}} = \{S_1, S_2, S_3, S_4\}$ of class boundary are computed using Otsu's method [30] as fitness values in quantum formalism and are optimized using quantum-inspired differential evolution (QDE).

C. FULLY-CONNECTED (FC) LAYERS FOR PATCH-BASED **CLASSIFICATION**

The segmented lung CT images by PQIS-Net are targeted for classification using Fully Connected (FC) layers to enable the diagnosis of COVID-19 or pneumonia (Non-Covid). However, to avoid over-fitting in the FC layers due to the large size of segmented image features, patch-based classification [31], [32] is preferred incorporating *p*-number of random patches with relatively small fixed size window of $s \times s$. The patches extracted from the segmented lung CT images are augmented with the limited training data and hence avoids overfitting. In addition, patch-based training at the FC layers relatively reduces the network complexity. The center pixel x_p of an image patch \mathcal{R}_p is randomly chosen from the segmented lung region (the lung and the background pixels significantly differ in their intensities) to obviate the empty region of the segmented image without using any lung mask. The value of *p* is chosen judiciously such that each pixel of the segmented lung CT image is considered at least once. Each patch as a vector of*s* ² pixels is concatenated along a fixed lexicographic ordering [33]. It may be noted that each image pixel from the infected lung region of the *p*-random patches may be considered as the highest representative feature for classification. Some patches contain white and black pixels without any significant feature (infection region) or small section of an

infected lesion for classification. In what follows, each image patch as vector is fed to the FC layers for classification with a *Softmax* function and out of *p*-outcomes the final decision is made by a majority voting scheme [34]. For simplicity, in the experimental setup, maximum of 100 patches for classification are allowed with patch size of 32×32 . Here, we have employed cross entropy loss for COVID-19 diagnosis. The loss $(\mathcal{L}_{(\Theta)})$ is computed by leveraging the hyper-parameters Θ of the semi-supervised neural network model. It is defined as

$$
\underset{\Theta}{\text{argmin}} \mathcal{L}_{(\Theta)} = \sum_{i}^{C} [t_i \log y_i(\alpha_i) + (1 - t_i) \log\{1 - y_i(\alpha_i)\}] \tag{15}
$$

where, $y(\alpha_i)$ is the predicted outcome of the FC layers on input α_i with respect to the network hyper-parameter set Θ . *ti* is the target output.

III. RESULTS AND DISCUSSIONS

A. DATA SET

Publicly available lung CT images are collected from three data sources [35]–[37] and experiments are performed using the proposed semi-supervised neural network model on both the data sets. One of the data sets [35] contains total 2482 lung CT images with variable sizes and out of these, 1252 lung CT images are infected by COVID-19 and 1230 CT slices are not infected by COVID-19. It may be noted that non-COVID CT slices include few healthy slices which lack significant distinguishable features for diagnosis. We have augmented the COVID-19 infected and non-COVID lung slices using rotation, scaling, shearing, and flipping operations. The image slices are randomly rotated by an angle in the range $[-5^\circ, +5^\circ]$, randomly scaled with a scale factor in the range [0.5, 1.5], randomly sheared about *X* and *Y* in the slant angle in the range $[-0.15, +0.15]$, and vertical and horizontal flipping. The training-validation and testing splits of the randomly chosen images are provided in Table [1.](#page-5-1) The Brazilian data set [35] is acquired from the real patients of Sao Paulo, City hospitals, Brazil. Few samples (COVID-19 infected and non-COVID infected) from the Brazil data set [35] are provided in the *Supplementary Materials*. Another data set [36] comprises only 20 labelled COVID-19 lung CT volumes of fixed size of 512×512 which include infection masks, lung masks (left and right) and lung-infection pair masks. These labelled CT volumes are manually segmented and verified by radiologist experts. The data set [36] comprising the labelled CT volume masks is used in the experiment for the segmentation task. On the contrary, the other data sets [35], [37] are used for segmentation followed by classification tasks. The third data set employed in this experiment is the IEEE CCAP data set [37] collected from IEEE Data port which comprises five different sets of lung CT images (COVID-19, Viral Pneumonia (VP), Bacterial Pneumonia (BP), Mycoplasma Pneumonia (MP) and Normal lung). Details of the data sets used for diagnosis are provided in Table [1.](#page-5-1)

B. EXPERIMENTAL SETUP

In this current work, extensive experiments have been carried out on lung CT images of variable sizes using a high performance DL GPU (Nvidia RTX2070) System with MATLAB 2020a and Python 3.6.2 (Pytorch). However, the proposed semi-supervised shallow network framework is implemented without using any sort of GPU support. The Brazilian data set [35] and the IEEE CCAP data set [37] are divided into 7 : 3 ratio for training, validation and testing, respectively for segmentation followed by classification. In addition, experiments are carried out using 5-fold cross validation. The results for these three different scenario (data sets) are investigated by leveraging the set of hyper-parameters of the proposed semi-supervised shallow neural network.

The parallel quantum-inspired self-supervised network (PQIS-Net) is experimented with the pre-processed normalized gray-level CT scan images. Pre-processing of the input lung CT images from all three data sets [35]–[37] are performed using normalization of images. The PQIS-Net segmented CT volumes are processed though the 2D binary masks [20], [38] available in the labelled CT volumes in the data set [36] to obtain the infected lesion on lung CT scans in the suggested semi-supervised model. Lung masks are used to segment only the lung region from the segmented CT slices, whereas infection masks are considered in the evaluation. The predicted label of each pixel is evaluated based on the infection region labelled in the infection masks. Each PQIS-Net segmented image is binarized using Otsu's bi-level thresholding [30] and compared with the binary infection masks. The segmented output images resemble in size with the dimensions of the binary mask and a outcome 1 is considered as infected region and 0 as background (lung region) in diagnosis. Pixel by pixel comparison with the manually segmented regions of interest or lesion masks allows evaluating the dice similarity (DS) [39] which is considered as a standard evaluation procedure in automatic medical image segmentation. The evaluation process using the data set [36] involves the manually segmented lesion (infection regions) mask as ground truth and each 2D pixel is predicted as either True Positive (T_{RP}) or True Negative (T_{RN}) or False Positive (*TRN*) or False Negative (*FLN*). The PQIS-Net is experimented with gray-level CT scan images using with distinct classes $L = 4, 5, 6, 7$ and 8 in optimized fashion [22]. In this experiment, the steepness (ν) in the σ*PQIS*−*Net*

activation function, is varied in the range 0.230 to 0.240 with a step size 0.001. It has been observed that in majority of cases, $v = 0.239$ yields the optimal segmentation. In addition to this, the hyper-parameter $\mathcal N$ is chosen intuitively in the current experimental setup and it has been seen that the \mathcal{N} = 8-connected second order neighborhood pattern yields optimal segmentation using PQIS-Net. It captures the local intensity variations over the 8-connected neighborhood regions.

In addition to this segmentation, experiments are also set up for classification using the proposed semi-supervised shallow network model, ResNet50 [9], and 3D-UNet [10] model by replacing the last layer of 3D-UNet [10], ResNet50 [9] architectures with two fully connected layers and patch-based classification without segmentation using PQIS-Net (Pathc-FC). The FC layers in the proposed semi-supervised shallow neural network model, and the Patch-FC model are rigorously trained using the stochastic gradient descent algorithm with momentum (SGDM) with an initial learning rate of 0.01, momentum of 0.8, minimum batch size of 8 and weight decay of 0.0001, allowing maximum 10 epochs. The convergence of accuracy and loss during training using the proposed semi-supervised shallow neural network with 5-fold cross validation is shown in Figure [2.](#page-6-0) The convergence curves of the suggested self-supervised PQIS-Net are shown in the *Appendix*. Moreover, experiments have been performed on two recently developed CNN architectures suitable for medical image segmentation viz., convolutional 3D-UNet [10] and Residual U-Net (ResNet50) [9] available in GitHub. The ResNet50 [9] and 3D-UNet [10] are rigorously trained using the *adam* optimizer with an initial learning rate of 0.01, gradient decay factor of 0.9 and a minimum batch size of 8, allowing maximum 50 epochs to converge. The convergence of accuracy and loss during training using ResNet50 [9] with 5-fold cross validation is also demonstrated in Figure [3.](#page-6-1) The other state-of-the-art techniques include Kang *et al.* [15], Wang *et al.* [18], and Han *et al.* [19] for COVID-19 detection on the Brazilian data set [35] and the IEEE CCAP data set [37]. It may be noted that the PQIS-Net segmented slices from the IEEE CCAP data set [37] are further prepossessed before classification to remove the cavity regions from the slices in order to obtain lung region with uniform background.

C. EXPERIMENTAL RESULTS

Extensive experiments have been performed in the current setup and experimental outcomes are reported with the demonstration of numerical and statistical analysis on three

FIGURE 2. Convergence of the proposed semi-supervised shallow neural learning model allowing maximum 10 epochs during training with an initial learning rate = 0.01 using the IEEE CCAP data set [37].

FIGURE 3. Convergence of the ResNet50 [9] model allowing maximum 50 epochs during training with an initial learning rate $= 0.01$ and minimum batch size $= 8$.

different data sets [35]–[37]. Segmentation using the proposed semi-supervised shallow neural network, pre-trained ResNet50 [9] and 3D-UNet [10] models have been performed using all the three data sets and segmentation performance is measured on data set [36] using Dice Similarity (DS) [39]. The human expert (radiologist) segmented lung and infection masks lung CT image slices of size 512×512 are provided in Figure [4](#page-7-0) with the input and the PQIS-Net segmented slice. A randomly selected input lung CT image slice#001-171 [36] is shown in Figure [5](#page-8-1) using Lung Window (W/L: 4017/987) for better clarity. Table [2](#page-6-2) reports the segmentation results of the proposed PQIS-Net with ResNet50 [9] and 3D-UNet [10] models for three different tasks (infection, lung, infection and lung). Table [3](#page-7-1) presents the numerical results obtained using the proposed semi-supervised shallow neural network model, Han *et al.* [19], ResNet50 [9], 3D-UNet [10], Wang *et al.* [18], Kang *et al.* [15] and Patch-FC for COVID-19 detection on the Brazilian data set [35]. In addition, experimental results obtained using the IEEE CCAP data set [37] with the proposed semi-supervised shallow network, Han *et al.* [19], 3D-UNet [10], ResNet50 [9], Wang *et al.* [18] and Patch-FC are provided in Table [4.](#page-7-2) The standard evaluation metrics used in Tables [3](#page-7-1) and [4](#page-7-2) to measure the COVID-19 detection

TABLE 3. Performance analysis of the proposed semi-supervised model, ResNet50 [9], 3D-UNet [10], Han et al. [19], Wang et al. [18], Kang et al. [15] and Patch-FC for COVID-19 detection on the Brazilian data set [35] [One sided non-parametric two sample KS test [40] with $\alpha = 0.05$ significance level has been conducted and marked underlined].

Model	Accuracy	Precision	Recall	F1-score	AUC-
Patch-FC	$0.869 + 0.164$	$0.733 + 0.014$	$0.801 + 0.015$	0.779 ± 0.094	$0.862 + 0.015$
Kang et al. $[15]$	0.905 ± 0.028	0.920 ± 0.019	$0.901 + 0.017$	$0.910 + 0.041$	0.978 ± 0.065
Wang et al. $\lceil 18 \rceil$	0.919 ± 0.015	0.963 ± 0.003	0.882 ± 0.138	0.921 ± 0.146	0.980 ± 0.028
Han et al. $[19]$	0.945 ± 0.043	$0.961 + 0.081$	$0.921 + 0.017$	0.941 ± 0.093	0.981 ± 0.038
$3D$ -UNet [10]	0.920 ± 0.108	0.964 ± 0.038	0.880 ± 0.133	$0.922 + 0.012$	0.981 ± 0.039
ResNet50 [9]	0.943 ± 0.014	0.935 ± 0.018	0.945 ± 0.017	0.940 ± 0.029	0.982 ± 0.048
Proposed Model	0.944 ± 0.089	0.965 ± 0.085	0.935 ± 0.052	0.948 ± 0.051	0.983 ± 0.127

TABLE 4. Performance analysis of the proposed semi-supervised model, Han et al. [19], 3D-UNet [10], ResNet50 [9], Wang et al. [18] and Patch-FC for COVID-19 detection on the IEEE CCAP data set [37] [One sided non-parametric two sample KS test [40] with $\alpha = 0.05$ significance level has been conducted and marked underlined].

efficiency are accuracy, precision, recall, F1-score and AUC (Area under ROC curve) [39]. From Table [3,](#page-7-1) it is observed that after rigorous tuning of the hyper-parameters, the proposed semi-supervised shallow neural network model outperforms patch-based classification using fully connected layers (Patch-FC), Kang *et al.* [15] and Wang *et al.* [18] concerning evaluation metrics used in COVID-19 diagnosis on the Brazilian data set [35]. However, the proposed semi-supervised model has reported similar accuracy as ResNet50 [9] and Han *et al.* [19], and precision as 3D-UNet [10] while outperforming in terms of other evaluation metrics concerning the outcome of the statistical significance KS-test. It is noteworthy that the proposed semi-supervised model using PQIS-Net outperforms 3D-UNet [10] in terms of accuracy, recall, F1-score and AUC in COVID-19 diagnosis on the Brazilian data set [35]. Similarly, the results reported in Table [4](#page-7-2) show that the proposed model outperforms Patch-FC, Wang *et al.* [18] and 3D-UNet [10] in terms of the evaluation metrics and reports similar accuracy as ResNet50 [9] and Han *et al.* in COVID-19 diagnosis on the IEEE CCAP data set [37]. In addition to this, the suggested shallow framework also outperforms Han *et al.* [19] and ResNet50 [9] in terms of precision and AUC. It may be noted from the results reported in Tables [3](#page-7-1) and [4](#page-7-2) that PQIS-Net followed by patch-based classification using fully-connected (FC) layers is superior than only patch-based classification using fully-connected layers (Patch-FC) without prior segmentation. It is also interesting to note from the results reported in Tables [3](#page-7-1) and [4](#page-7-2) that with an increase in the training samples in the data set [37] the improvement of accuracy is phenomenal for all the methods especially 3D-UNet [10] and ResNet50 [9]. Thus, despite being a semi-supervised shallow learning framework, the suggested semi-supervised model has attained better stability on the outcome as is evident from the higher values of precision and AUC while compared with the state-of-the-art methods in COVID-19 screening.

FIGURE 4. PQIS-Net segmented lung CT slice#171 [36] with the three different masks.

In addition, the ROC curves and Confusion matrices are reported for quantitative representations of accuracy in COVID-19 detection using the Brazilian data set [35] and the IEEE CCAP data set [37] as shown in Figures [6,](#page-8-2) [7,](#page-8-3) [8,](#page-8-4) and [9,](#page-8-5) respectively. The confusion matrices for ResNet50 [9], 3D-UNet [10], Han *et al.* [19], and Wang *et al.* [18] in COVID-19 diagnosis on the IEEE CCAP data set [37] are also provided in the *Supplementary Materials*. For a good classifier, higher the number of predicted correct samples, the larger will be the values in the diagonal of the confusion matrix. Considering the confusion matrices, it is evident that the suggested shallow framework is superior to the models ResNet50 [9], 3D-UNet [10], Han *et al.* [19], Wang *et al.* [18] and Patch-FC in classifying COVID-19 and Mycoplasma Pneumonia (MP) categories. The suggested semi-supervised shallow framework predicts 520 and 237 correctly out of 520 COVID-19 and 240 MP target samples, respectively, whereas ResNet50 [9] has predicted 517 and 235, 3D-UNet [10] has predicted 518 and 235, Han *et al.* [19]

FIGURE 5. Randomly chosen input lung CT image slice#001 − 171 [36] is shown in Lung Window (W/L: 4017/987) and infections are shown red arrow.

FIGURE 6. ROC Curves for the COVID-19 detection rate vs. false positives using the proposed semi-supervised shallow neural network model, 3D-UNet [10], ResNet50 [9], Han et al. [19], Kang et al. [15], and Wang et al. [18] on Brazilian data set [35].

has predicted 519 and 236, Wang *et al.* [18] predicted 499 and 231, and Patch-FC has predicted 476 and 193. It further demonstrates that the random patch-based classification incorporated in the suggested semi-supervised framework significantly enhances the performance of COVID-19 screening as the severely infected features present in the COVID-19 slices are captured by these randomly chosen patches from the lung regions. However, the proposed semi-supervised model has maximum miss-classification in Viral Pneumonia (VP) class (4.8%) due to the fact that the majority of BP slices looks like Normal CT slices. Despite the remarkable success achieved in COVID-19 screening, ResNet50 [9] and 3D-UNet [10] architectures still suffer from some inherent challenges owing to deeper and complex network architectures. ResNet50 [9] and 3D-UNet [10] face slow convergence problems for COVID-19 diagnosis tasks during training. In addition, higher computational (GPU) and memory resources required for ResNet50 [9] and 3D-UNet [10] architectures pose a potential concern in COVID-19 automated diagnosis. On contrary, the proposed semi-supervised model is implemented without any support of Graphics Processing Unit and its convergence is also stabilized at epoch 10 as shown in Figure [2,](#page-6-0) whereas ResNet50 [9] requires 50 epochs to converge as shown in Figure [3.](#page-6-1) Hence, it can be concluded, that the performance of the semis-supervised model on lung CT image classifications is statistically significant and offers a potential alternative to the solution of deep learning networks and other time-intensive feature based learning paradigms in future.

FIGURE 7. Confusion matrix for the accuracy of prediction of COVID-19 using the proposed semi-supervised shallow neural network model on Brazilian data set [35].

FIGURE 8. ROC Curves for detection rate (in case of Bacterial Pneumonia (BP), COVID-19, Mycoplasma Pneumonia (MP), Normal lung, and Viral Pneumonia (VP)) vs false positive using the proposed semi-supervised shallow neural network model, ResNet50 [9], 3D-UNet [10], Kang et al. [19], and Wang et al. [18] on IEEE CCAP data set [37].

FIGURE 9. Confusion matrix for the accuracy of prediction of Bacterial Pneumonia (BP), COVID-19, Mycoplasma Pneumonia (MP), Normal lung, and Viral Pneumonia (VP) using the proposed semi-supervised shallow neural network model on IEEE CCAP data set [37].

IV. LIMITATIONS OF THE STUDY

It may be noted from the experimental studies that ResNet50 and 3D-UNet marginally outperform the proposed PQIS-Net in lung CT image segmentation tasks in terms of dice

FIGURE 10. Convergence of the proposed PQIS-Net for four different activation with four distinct class boundaries and using the data set [37].

similarity. This is due to the fact that the proposed PQIS-Net is a fully self-supervised neural network model based on pixel intensity based features. However, the performance of the proposed semi-supervised model is very close to ResNet50 and Han *et al.* (statistically similar) and outperforms all the best published works in terms of Precision and AUC for COVID-19 diagnosis. In addition to this, the lower computational complexity and lesser resources required to implement the proposed semi-supervised framework make it a notable significant contribution in the field of semi-supervised or weakly supervised learning paradigm. Thus, the proposed parallel semi-supervised shallow learning model serves as an inspiration for promoting a potential alternative to the deep supervised learning frameworks for lung CT image segmentation for automatic COVID-19 diagnosis as well as for automatic medical image segmentation in various applications with limited labelled data sets.

V. CONCLUSION

In this work, a novel attempt has been made using an integrated semi-supervised shallow neural network encompassing the parallel self-supervised neural network model (PQIS-Net) for fully automatic segmentation of lung CT images followed by fully connected (FL) layers for patch-based classification with majority voting. The proposed integrated framework is semi-supervised in the sense that the PQIS-Net is a fully self-supervised network for segmentation followed by fully connected layers for random patch-based classification of COVID-19 disease. The PQIS-Net model incorporates the frequency components of the weights and inputs in quantum formalism thereby enabling faster convergence of the network states owing to reduction in computation. This intrinsic property of the PQIS-Net model yields precise and time efficient segmentation in real-time, which is evident from the results demonstrated in the experimental section. In spite being a semi-supervised model, the suggested semi-supervised shallow neural network has attained better stability on the outcome as it is evident from the higher values of precision and AUC compared with the state-of-the-art methods specially in COVID-19 and Mycoplasma Pneumonia screening. Moreover, our light-weight semi-supervised model can be employed in any application setting (eg. medical IoT devices) right away where, the deep learning models face serious

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obstacles. However, it remains to investigate the performance of lung CT segmentation using the optimized version of PQIS-Net followed by classification with adaptive patch sizes. The authors are currently engaged in this direction.

APPENDIX

CONVERGENCE ANALYSIS OF THE PQIS-NET MODEL

The convergence of the network states in PQIS-Net is guided by the error or loss function and the segmented output is obtained once the network stabilizes. The coherent network error cum loss function is introduced in the PQIS-Net, is evaluated as follows.

$$
\zeta(\omega, \gamma)
$$

= $\frac{1}{2} \sum_{k}^{B} \sum_{i}^{m \times n} \sum_{j}^{N} [\varphi^{t+1,k}(\omega_{i,j}^{t+1,k}, \gamma_{i}^{t+1,k}) - \varphi^{t,k}(\omega_{i,j}^{t,k}, \gamma_{i}^{t,k})]^2$
(16)

where, $\varphi^{i,k}(\omega_{i,j}^{i,k}, \gamma_i^{i,k})$ is the weighted inter-connection at a particular epoch ι and is linearly dependent on ω and γ . β is the batch size of the constituent PQIS-Net. The loss function $\zeta(\omega, \gamma)$ is guided by the phase or angles ω and γ . Each entry in the weighted inter-connection matrix in between the successive constituent layers in the PQIS-Net architecture, is updated using rotation gate as follows.

$$
|\varphi^{l+1,k}\rangle = \begin{pmatrix} \cos \triangle \omega^{l,k} & -\sin \triangle \omega^{l,k} \\ \sin \triangle \omega^{l,k} & \cos \triangle \omega^{l,k} \end{pmatrix} |\varphi^{l,k}\rangle \quad (17)
$$

$$
|\xi^{l+1,k}\rangle = \begin{pmatrix} \cos \Delta \gamma^{l,k} & -\sin \Delta \gamma^{l,k} \\ \sin \Delta \gamma^{l,k} & \cos \Delta \gamma^{l,k} \end{pmatrix} |\xi^{l,k}\rangle \quad (18)
$$

where,

and

$$
\omega^{l+1,k} = \omega^{\iota,k} + \Delta \omega^{\iota,k} \tag{19}
$$

$$
\gamma^{l+1,k} = \gamma^{l,k} + \Delta \gamma^{l,k} \tag{20}
$$

Hence, Equations [19](#page-9-1) and [20](#page-9-2) measure the change in phase or angles $\Delta \omega^{t,k}$ and $\Delta \gamma^{l,k}$, respectively for the *k*th constituent parallel network in PQIS-Net at epoch ι. Consider

$$
\mathcal{W}^{i,k} = \omega^{i,k} - \overline{\omega^{i,k}} \tag{21}
$$

$$
\mathcal{A}^{i,k} = \gamma^{i,k} - \overline{\gamma^{i,k}} \tag{22}
$$

and

$$
\mathcal{V}^{\iota,k} = \omega^{\iota+1,k} - \omega^{\iota,k} = \mathcal{W}^{\iota+1,k} - \mathcal{W}^{\iota,k} \tag{23}
$$

$$
\mathcal{M}^{i,k} = \gamma^{i+1,k} - \gamma^{i,k} = \mathcal{A}^{i+1,k} - \mathcal{A}^{i,k} \tag{24}
$$

Hence, the optimal phase or angles for weighted interconnection and the corresponding activation are $\omega^{i,k}$ and $\gamma^{i,k}$, respectively. Differentiation of the loss function $\zeta(\omega, \gamma)$ with respect to $\omega_{ij}^{i,k}$, $\gamma_i^{i,k}$ gives

$$
\frac{\partial \zeta(\omega, \gamma)}{\partial \omega_{ij}^{i,k}} = \frac{2}{mn} \sum_{k=1}^{B} \sum_{i=1}^{m \times n} \sum_{j=1}^{N} \Delta \varphi_{ij}^{i,k}(\omega_{ij}^{i,k}, \gamma_{i}^{i,k})
$$
\n
$$
\times \left[\frac{\partial \varphi_{ij}^{i+1,k}(\omega_{ij}^{i+1,k}, \gamma_{i}^{i+1,k})}{\partial \omega_{ij}^{i,k}} - \frac{\partial \varphi_{ij}^{i,k}(\omega_{ij}^{i,k}, \gamma_{i}^{i,k})}{\partial \omega_{ij}^{i,k}} \right]
$$
\n(25)

$$
\frac{\partial \zeta(\omega, \gamma)}{\partial \gamma_i^{t,k}} = \frac{2}{mn} \sum_{k=1}^{B} \sum_{i=1}^{m \times n} \sum_{j=1}^{N} \Delta \varphi_{ij}^{t,k}(\omega_{ij}^{t,k}, \gamma_i^{t,k})
$$

$$
\times \left[\frac{\partial \varphi_{ij}^{t+1,k}(\omega_{ij}^{t+1,k}, \gamma_i^{t+1,k})}{\partial \gamma_i^{t,k}} - \frac{\partial \varphi_{ij}^{t,k}(\omega_{ij}^{t,k}, \gamma_i^{t,k})}{\partial \gamma_i^{t,k}} \right]
$$
(26)

where,

$$
\Delta \varphi_{ij}^{\iota,k}(\omega_{ij}^{\iota,k}, \gamma_i^{\iota,k}) = |\varphi_{ij}^{\iota+1,k}(\omega_{ij}^{\iota+1,k}, \gamma_i^{\iota+1,k}) - \varphi_{ij}^{\iota,k}(\omega_{ij}^{\iota,k}, \gamma_i^{\iota,k})|
$$
\n(27)

The changes in phase or angles are designated as $\Delta \omega_{ij}^{t,k}$ and $\Delta \gamma_{ij}^{i,k}$ for the rotation gate involved in updating the weighted matrix and its corresponding activation are given by

$$
\Delta \omega_{ij}^{i,k} = -\mathcal{X}_{ij}^{i,k} \left\{ \frac{\partial \zeta(\omega, \gamma)}{\partial \omega_{ij}^{i,k}} \zeta(\omega, \gamma) \right\}^{\frac{1}{i}} \tag{28}
$$

$$
\Delta \gamma_i^{i,k} = -\kappa_i^{i,k} \left\{ \frac{\partial \zeta(\omega, \gamma)}{\partial \gamma_i^{i,k}} \zeta(\omega, \gamma) \right\}^{\frac{1}{i}} \tag{29}
$$

Here, $\mathcal{X}_{ij}^{t,k}$ and $\kappa_i^{t,k}$ correspond to the learning rates in updating the angles of rotation in inter-connection matrix and its activation in the k^{th} parallel network in PQIS-Net at epoch ι . These are measured as follows.

$$
\mathcal{X}_{ij}^{i,k} = \mu_i^{i,k} - \mu_{ij}^{i,k} \quad \forall j = 1, 2... \mathcal{N}
$$
 (30)

and

$$
\kappa_i^{i,k} = (\sum_j \mu_{i,j}^{i,k}) \quad \forall j = 1, 2\mathcal{N} \tag{31}
$$

To show the super-linearly convergence of PQIS-Net, the following conditions on the sequences $\{\omega^{t,k}\}\$ and $\{\gamma^{t,k}\}\$ should be imposed [41].

$$
\lim_{t \to \infty} \frac{||\omega^{t+1,k} - \overline{\omega^{t,k}}||}{||\omega^{t,k} - \overline{\omega^{t,k}}||} \le 1
$$
\n(32)

and

$$
||\mathcal{W}^{t+1,k}|| = O||\mathcal{V}^{t,k}|| \tag{33}
$$

Also,

 \mathbf{L}

$$
\lim_{k \to \infty} \frac{||\gamma^{i+1,k} - \overline{\gamma^{i,k}}||}{||\gamma^{i,k} - \overline{\gamma^{i,k}}||} \le 1
$$
\n(34)

and

$$
||A^{t+1,k}|| = O||\mathcal{M}^{t,k}||
$$
\n(35)

TABLE 5. Description of the symbols used in the manuscript.

Now, according to Thaler formula

$$
\zeta(\omega^{t+1,k}, \gamma^{t+1,k}) - \zeta(\omega^{t,k}, \gamma^{t,k})
$$
\n(36)

$$
= \left[\begin{array}{cc}\Delta\omega_{ij}^{i,k} & \Delta\gamma_{i}^{i,k}\end{array}\right] \left[\begin{array}{c}\frac{\partial \zeta(\omega^{i,k}, \gamma^{i,k})}{\partial \omega_{ij}^{i,k}}\\\frac{\partial \zeta(\omega^{i,k}, \gamma^{i,k})}{\partial \gamma_{i}^{i,k}}\end{array}\right] \\
+ O\left[\begin{array}{cc}\|\Delta\omega_{ij}^{i,k} \Delta\gamma_{i}^{i,k}\|\\\vdots\\\frac{\partial \zeta(\omega^{i,k}, \gamma^{i,k})}{\partial \omega_{ij}^{i,k}}\end{array}\right]^{2} + \left\{-\kappa_{i}\frac{\partial \zeta(\omega^{i,k}, \gamma^{i,k})}{\partial \gamma_{ij}^{i,k}}\right\}^{2}\right]
$$
\n(37)

 $\times\{\zeta(\omega^{t,k},\gamma^{t,k})\}^{\frac{1}{t,k}}$ $\overline{\iota_{\cdot,k}}$ (38)

Here, it is evident that $(\zeta(\omega^{t+1,k}, \gamma^{t+1,k}) - \zeta(\omega^{t,k}, \gamma^{t,k})) \leq$ 0 and the monotonically decreasing behaviors of the given sequences $\{\omega^{i,k}\}\$ and $\{\gamma^{i,k}\}\$ are given by

$$
\lim_{l \to \infty} \zeta(\omega^{l,k}, \gamma^{l,k}) = (\overline{\omega^{l,k}}, \overline{\gamma^{l,k}})
$$
(39)

and

$$
\lim_{l\to\infty} \frac{||\zeta(\omega^{t+1,k}, \gamma^{t+1,k}) - (\overline{\omega^{t,k}}, \overline{\gamma^{t,k}})||}{||\zeta(\omega^{t,k}, \gamma^{t,k}) - (\overline{\omega^{t,k}}, \overline{\gamma^{t,k}})||} \le 1 \qquad (40)
$$

The loss curve of the suggested PQIS-Net is provided in Figure [10.](#page-9-3)

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