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# A Detailed Analytical Model of SiC MOSFETs for Bridge-Leg Configuration by Considering Staged Critical Parameters

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**ABSTRACT** The high operating voltage and switching speed of silicon carbide (SiC) MOSFETs have significant impacts on parasitic elements. This leads to a limitation in the performance of the devices. Especially in the bridge-leg configuration, the coupling of the parasitic elements, in the upper and lower bridge-legs, produces knock-on effects, which complicates the modeling development to reveal the underlying mechanisms. This paper presents a detailed piecewise linear analytical model for bridge-leg configured SiC MOSFETs, which takes into account their characteristics and all parasitic elements. The novelty of the proposed model lies in the fact that the critical parameters in each stage are distinguished flexibly and emphatically according to their influence weights to the corresponding main variables. Therefore, the complexity of the model which considers all parasitic elements is reduced but the critical impacts on the switching processes are carefully kept. The turn-on and turn-off processes are analyzed stage-by-stage in detail with the derived critical parameters equivalent circuits, and the mechanism underlying how each critical parameter influences the model is revealed individually. Furthermore, based on this model, the impact mechanisms and trends of the switching rate variation, the power loop attenuation oscillation, and the driver loop crosstalk phenomenon for different critical parameters are analyzed emphatically. Double pulse measurements with a 600 V/20A SiC MOSFETs based bridge-leg test circuit are used for the experimental verification of the accuracy of the model and the trends of the critical parameters' impacts.

**INDEX TERMS** Analytical model, bridge-leg, SiC MOSFET, critical parameters, impact mechanisms, staged.

NOMENC	LATURE	$D_{bX}$	Antiparallel freewheeling diode of
$C_{gsX}$	Gate-source capacitance		SIC MOSFET
$C_{gdX}$	Gate-drain capacitance	$Q_{RS}$	Charge quantity of the minority carriers of
$C_{dsX}$	Drain-source capacitance		antiparallel freewheeling diode
$L_{gX\_in}$	Internal parasitic inductance of gate	$R_{gH\_eq1}$	Equivalent damping resistance of higher SiC
$L_{dX\_in}$	Internal parasitic inductance of drain		MOSFET in Stage 4
$L_{sX_in}$	Internal parasitic inductance of source	$R_{gL_eq1}$	Equivalent damping resistance of lower SiC
$L_{gX}_{ex}$	External parasitic inductance of gate		MOSFET in Stage 4
$L_{dX}_{ex}$	External parasitic inductance of drain	$R_{gL\_eq2}$	Equivalent damping resistance of lower SiC
$L_{sX}_{ex}$	External parasitic inductance of source		MOSFET in Stage 6
$L_{LOOP}$	Parasitic inductances of power loop	$R_{gH_eq2}$	Equivalent damping resistance of higher SiC
$R_{gX_{in}}$	Internal gate driver resistance		MOSFET in Stage 8
$R_{gX}_{ex}$	External gate driver resistance	$V_{DD}$	DC input voltage
<i>g</i> <sub>f</sub>	Transconductance of SiC MOSFET	$V_{GATE}$	Driver supply voltage
		$V_{th}$	Threshold voltage of SiC MOSFET
The asso	ciate editor coordinating the review of this manuscript and	$V_{miller}$	Miller platform voltage

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VgsX

Gate-source voltage

and SABER provide plentiful and accurate device models

$V_{dsX}$	Drain-source voltage
$V_{idsX}$	Induced voltage on $L_{sX}$
$V_{iddX}$	Induced voltage on $L_{dX}$
$i_{ch}$	Channel current
$i_{gX}$	Driver current
$i_{dX}$	Drain current
I <sub>RR_PEAK</sub>	Peak value of reverse recovery current
$I_{RR\_BV}$	Value of reverse recovery current when
	minority carriers elicited
ILOAD	Output load current

Note: the subscript "X" is represented as "H" and "L" refer to the higher SiC MOSFET and lower SiC MOSFET of bridge-leg configuration, respectively.

#### I. INTRODUCTION

Silicon carbide (SiC) MOSFETs are promising candidates for next-generation power devices. Compared with a siliconbased MOSFET, a SiC MOSFET has a number of advantages such as wider bandgap, lower on-state resistance, higher thermal conductivity, higher switching speed, and higher block voltage level [1]-[4]. However, along with these excellent characteristics comes, the impacts of its parasitic elements are significantly intensified during the fast switching process, which leads to many unfavorable factors that restrict the device's optimal performance. In a bridge-leg configuration, there are further knock-on effects such as switching oscillation of the power loop [5] and crosstalk phenomenon of the driver loop [6], [7] due to the coupling effects of the upper and lower devices [8]. Besides, the own characteristics of a SiC MOSFET can be also the key obstacles. A SiC MOSFET has a lower turn-on threshold voltage and negative breakdown voltage compared with a silicon-based MOSFET [9], and its gate-source parasitic capacitance is relatively small [10], which makes the driver loop more susceptible to the voltage coupling effects. These two factors contradict each other and reduce the reliability of the bridge-leg based on SiC MOSFETs, which could even result in misconducting [11]. Therefore, to take full advantage of SiC MOSFETs and avoid the obstacles, an accurate and detailed model is needed to evaluate the working processes and the impacts of different parameters for SiC MOSFETs operating in a bridge-leg configuration.

So far, there have been many studies summarizing various models, they can be classified into three categories: physicsbased model, behavioral model, and analytical model. The physics-based model based on the carrier drift-diffusion motion equations provides the most detailed descriptions of the physical parameters of the device [12], [13]. But this model is too complex to be used to describe the bridge-leg switching processes at the circuit level. With the development of simulation software, more and more complete behavioral models are employed to describe the switching processes of different kinds of devices. These models are more suitable to analyze the responses of devices nested in a circuit. The commonly used simulation software such as PSpice that could adjust a series of key parameters and peripheral parasitic elements [14]. Some device manufacturers such as CREE also provide specific SPACE model libraries for their products to close to reality. In [15], the influences of temperature are also taken into account. The perfect behavioral models make it realistic and precise to analyze the switching processes of devices working in a circuit. However, they can only provide the response results of switching processes, but cannot reveal the underlying mechanism and the influences' trends of the parameters. Additionally, the specific behavioral model cannot be easily transplanted to other devices, which makes the analysis tedious. Analytical models are set up based on the mathematical of the loop equations [16]-[18]. For a nonlinear variation switching process of the device, the piecewise linear model is the most convenient and widely used analytical model, which divides the switching process into several linear stages according to the different variable responses and the equivalent circuit models are established in each stage [17], [19]. However, in order to maintain the accuracy of the calculation results, the equations need to consider as many details of the parasitic elements as possible. This inevitably increases the circuit number and the order of equations, which makes the model too complex and can only be solved by iteration methods [20], [21]. Thus, the numerical solutions obtained by such a model cannot fundamentally reveal the physical impacts of the parameters, and a great deal of calculations and comparisons with changed parameters is needed to reveal the impact trends. In this way, the analytical method is analogous to the behavior model. However, in order to simplify the equations and obtain the analytical solutions of the responses, some insignificant parameters are uniformly omitted, such omissions may cause errors or even overlook the impacts of certain parameters [11], [17], [22]. These two aspects become a dilemma of analytical models to evaluate complex circuits.

For both the behavioral model and analytical model, the accuracy of them depends on the precise descriptions of the devices' actual characteristics and the correlations of parasitic elements. However, there is no consistent conclusion on such correlations in the reported literature. This could lead to inaccuracies, error simplifications, and even opposite conclusions. For example, the literatures [23] and [24] believe that common source parasitic inductance can suppress the driver crosstalk phenomenon, while [21] and [25] conferred an opposite conclusion. Another critical influence comes from the reverse recovery process of the freewheeling diode. Although the reverse recovery characteristics of SiC MOSFETs are better than Si MOSFETs, it still exists due to the capacitance effect of the drain-source junction, but it is ignored in some studies [22], [26]. Moreover, the descriptions of the occurrence interval of the reverse recovery process are not consistent. The authors, in [27] and [28], report that the current peak of the reverse recovery process occurs during the drain-source voltage decrease stage whereas [17] claims that it occurs before the drain-source voltage decrease.

Literatures [11] and [29] shown that the drain-source voltage does not change during the reverse recovery current rising time, while the drain-source voltage builds up when the reverse recovery current decreases. These differences will lead to cumulative irregularities in the calculation results. There are different judgments for the division of the nonlinear parasitic capacitances, and the linearization method adopted determines the accuracy of capacitance value restoration. In [19], only the nonlinear characteristic of the gate-drain capacitance is considered in detail. The authors of [17] consider both gate-drain capacitance and drain-source capacitance have nonlinear characteristics, but simply divide them into large and small values according to the drain-source voltage. The literatures [30] and [31] consider that all parasitic capacitances of SiC MOSFETs have nonlinear characteristics. Particularly, [31] presents a comprehensive behavior model of the nonlinear characteristics of parasitic capacitances. To sum up, although these special characteristics greatly increase the complexity of the model designing, they are related to the accuracy of the switching responses and cannot be ignored. Furthermore, the upper and lower devices have the same number of parasitic elements for a bridge-leg, which makes the analysis even more cumbersome.

This paper proposes a detailed and accurate analytical model for SiC MOSFETs applied to bridge-leg configuration. The model comprehensively considers all parasitic elements and the special characteristics of the switching devices, including the nonlinear characteristics of the interelectrode parasitic capacitance, the transconductance of the channel current versus the gate-source voltage, and the reverse recovery processes of antiparallel freewheeling diodes. Further, on the basis of the piecewise linear model, the dominant elements and key variables of each switching stage are identified independently, and they are selected separately according to their influence weights on different variables of the driver loop and power loop. Non-critical parasitic elements and variables are flexibly excluded. Through these staged parameter optimizations, the complexity of modeling can be reduced while ensuring its accuracy. The dominant elements, that affect the main switching responses, and the key coupling variables are summarized as the staged critical parameters. The equivalent circuits based on the critical parameters of each stage are derived individually and the switching processes are described in detail. Moreover, based on the proposed model, the influence mechanisms and trends of the critical parameters on the current and voltage switching rates, the coupling effects of the bridge-leg, the oscillation of the power loop, and the crosstalk of the driver loop, can be analyzed in detail. They are vital features of the bridge-arm. A double pulse test circuit composed of 600V, 20A SiC MOSFETs is set up and experimental results are obtained to verify the accuracy of the proposed analytical model and the tendencies of the critical parameters' effect.

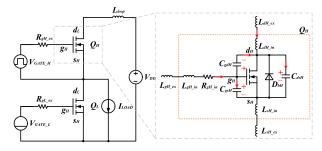


FIGURE 1. Equivalent circuit model of a bridge-leg configuration.

#### II. ANALYSIS OF STAGED SWITCHING PROCESS OF BRIDGE-LEG CONFIGURATION

In this section, the switching process of a bridge-leg configuration is introduced in detail. A double pulse test equivalent circuit based on SiC MOSFETs is established. Fig.1 displays the equivalent circuit model. The proposed model includes a DC input voltage  $V_{DD}$  modeled as a constant voltage source. The output current is considered as a constant current source. The SiC MOSFETs,  $Q_H$  and  $Q_L$ , are connected in series as the upper and lower switching devices of the bridge-leg, where their gates are connected to the gate drivers through the external driver resistances  $R_{gH\_ex}$  and  $R_{gL\_ex}$  respectively. The rise and fall times of the gate drivers' voltages are neglected in the analysis. In addition, the parasitic elements of the SiC MOSFETs are considered in the internal of the device packages and the external circuit traces. Taking  $Q_H$  as an example, the internal parasitic elements include interelectrode capacitances  $C_{gsH}$ ,  $C_{gdH}$ , and  $C_{dsH}$ , parasitic inductances  $L_{gH_in}$ ,  $L_{dH_{in}}$ , and  $L_{sH_{in}}$ , internal gate driver resistance  $R_{gH_{in}}$ , and the antiparallel freewheeling diode  $D_{bH}$ . The external parasitic elements are the stray inductances of the electrode pins and the circuit traces connected to the gate, source, and drain, which are represented by  $L_{gH\_ex}$ ,  $L_{dH\_ex}$ , and  $L_{sH\_ex}$ , respectively. As well,  $Q_L$  has the same structure. Indeed, there are extra stray inductances in the power loop lumped by  $L_{LOOP}$ , in order to facilitate the analysis,  $L_{LOOP}$  is lumped into  $L_{dH\_ex}$  in the subsequent discussion, and  $L_{gH} = L_{gH\_ex} +$  $L_{gH_{in}}, L_{dH} = L_{dH_{ex}} + L_{dH_{in}}, L_{sH} = L_{sH_{ex}} + L_{sH_{in}}$ , that respectively denote the total gate, the drain, and the source inductances of  $Q_H$ .  $Q_L$  is modeled in the same way.

To ensure the consistency of the variables' response expressions in each stage, the reference direction of each vector variable in the equivalent circuit is uniformly specified. The currents flow into the gates are in the positive direction in  $Q_H$  and  $Q_L$  driver loops, and the current direction from drain to source is positive in the power loop. Fig. 2 illustrates the staged analytical turn-on and turn-off switching waveforms of  $Q_H$  and  $Q_L$  in sequence. According to the period of major variables' response change, the turnon and turn-off switching processes are divided into eight stages. A thorough analysis of each stage is then presented stage-by-stage.

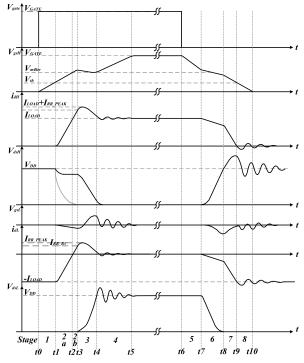


FIGURE 2. Analytical switching sequence of turn-on and turn-off stages.

#### A. TURN-ON SWITCHING TRANSITION

Before the gate signal of  $Q_H$  turns higher,  $Q_H$  and  $Q_L$  are in the cut-off state, the load current  $I_{LOAD}$  flows through the antiparallel freewheeling diode  $D_{bL}$  of  $Q_L$ ,  $D_{bL}$ .

#### 1) STAGE 1 (t0-t1) TURN-ON DELAY TIME

The gate signal of  $Q_H$  becomes high at  $V_{GATE}$ , and the gate current charges the input capacitances  $C_{gsH}$  and  $C_{gdH}$ . The gate-source voltage  $V_{gsH}$  starts to rise and the gate-drain voltage experiences a slight drop. Since  $V_{gsH}$  has not reached the threshold voltage  $V_{th}$ ,  $Q_H$  remains cut-off,  $I_{LOAD}$  still circulates through  $D_{bL}$  and the voltage distribution of the bridge-leg power loop remains unchanged.

Due to the nonlinear characteristics of the interelectrode capacitances with respect to the drain-source voltage. And there is a high voltage applied to the drain-source of  $Q_H$  in this stage. The value of  $C_{gdH}$  stays at a minimum, which is much smaller than that of  $C_{gsH}$ . In general, the value of  $C_{gsH}$  is a hundredfold or more than  $C_{gdH}$  for SiC MOSFETs. Thus, the current flowing through  $C_{gdH}$  and the small voltage drop on the drain parasitic inductance  $L_{dH}$  can be neglected (the neglected parasitic element and circuits are represented by dashed lines in Fig. 3). The equivalent circuit of this stage is shown in Fig. 3, the circuit equations are established as

$$V_{gsH} = V_{gdH} + V_{dsH} \tag{1}$$

$$i_{gH} = C_{gsH} \frac{dV_{gsH}}{dt} \tag{2}$$

$$V_{GATE} = R_{gH}i_{gH} + \left(L_{gH} + L_{sH}\right)\frac{di_{gH}}{dt} + V_{gsH} \qquad (3)$$



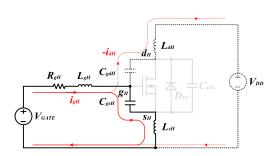


FIGURE 3. Equivalent circuit for Stage 1.

 $V_{gsH}$  is a step response of a second-order circuit, the equations can be obtained as shown in (4).

$$\left(L_{gH}+L_{sH}\right)C_{gsH}\frac{dV_{gsH}^{2}}{dt^{2}}+R_{gH}C_{gsH}\frac{dV_{gsH}}{dt}+V_{gsH}=V_{GATE}$$
(4)

And  $V_{gsH}$  can be solved as

$$V_{gsH} = V_{GATE} - \frac{V_{GATE}}{\tau_{bH1} - \tau_{aH1}} \times \left(\tau_{bH1}e^{-\tau_{aH1}\omega_{n\_H1}t} - \tau_{aH1}e^{-\tau_{bH1}\omega_{n\_H1}t}\right)$$
(5)

where  $\tau_{aH1} = \xi_{H1} - \sqrt{\xi_{H1}^2 - 1}$ ,  $\tau_{bH1} = \xi_{H1} + \sqrt{\xi_{H1}^2 - 1}$  and the characteristic parameters of the driver loop are

$$\omega_{n_H1} = \frac{1}{\sqrt{\left(L_{gH} + L_{sH}\right)C_{gsH}}} \tag{6}$$

$$\xi_{H1} = \frac{R_{gH}}{2} \sqrt{\frac{C_{gsH}}{L_{gH} + L_{sH}}} \tag{7}$$

where  $\omega_{n_{H1}}$  denote the natural frequency and  $\xi_{H1}$  denotes the damping coefficient.

## 2) STAGE 2 (t1-t3) $Q_H$ CHANNEL CURRENT RISE TIME AND $D_{bL}$ REVERSE RECOVERY CURRENT RISE TIME

When  $V_{gsH}$  exceeds  $V_{th}$ ,  $Q_H$  starts conducting and its channel current  $i_{ch}$  increases from zero. At the same time, the freewheeling current of  $D_{bL}$  decreases from  $I_{LOAD}$  and drops to zero when  $i_{ch}$  reaches  $I_{LOAD}$ . Nevertheless, due to the reverse recovery characteristic, the reverse recovery current through  $D_{bL}$  increases until it approaches the maximum  $I_{RR\_PEAK}$ , which is  $I_{RR\_BV}$ , and  $i_{dH}$  rises to  $I_{LOAD} + I_{RR\_BV}$ . So, according to the direction of  $i_{dL}$ , this stage can be divided into two sub-stages.

3) STAGE 2 (t1-t2)  $Q_H$  CHANNEL CURRENT RISE TIME In this stage,  $Q_H$  works in the saturation region and the channel current  $i_{ch}$  is controlled by  $V_{gsH}$ . Their relationship is given by:

$$i_{ch} = g_f \left( V_{gsH} - V_{th} \right) \tag{8}$$

where  $g_f$  is the transconductance coefficient of  $Q_H$ . The drain current  $i_{dH}$  can be expressed as follows:

$$i_{dH} = i_{ch} - C_{gdH} \frac{dV_{gdH}}{dt} + C_{dsH} \frac{dV_{dsH}}{dt}$$
(9)

 $g_f$  increases nonlinearly with the increase of  $V_{gsH}$  until it levels out slowly, and the rising rate of  $i_{ch}$  reaches the maximum. Correlatively, the freewheeling current through  $D_{bL}$  decreases. These rapid varying currents generate induced voltages on  $L_{dH}$ ,  $L_{sH}$ ,  $L_{dL}$ , and  $L_{sL}$  in the power loop, which cause a slight drop on  $V_{dsH}$ . Thereby, the equation of the power loop can be expressed as

$$V_{DD} = V_{dsH} + (L_{dH} + L_{sH}) \frac{di_{dH}}{dt} + L_{sH} \frac{di_{gH}}{dt} + (L_{dL} + L_{sL}) \frac{d (i_{dH} - I_{LOAD})}{dt}$$
(10)

Same as Stage 1,  $V_{dsH}$  does not decrease significantly and  $C_{gdH}$  still stay around its minimum. So, most of driver current of  $Q_H$  continues to charge  $C_{gsH}$  and the influence of the current flowing through  $C_{gdH}$  can still be neglected. The equivalent circuit of this sub-stage is shown in Fig. 4a.

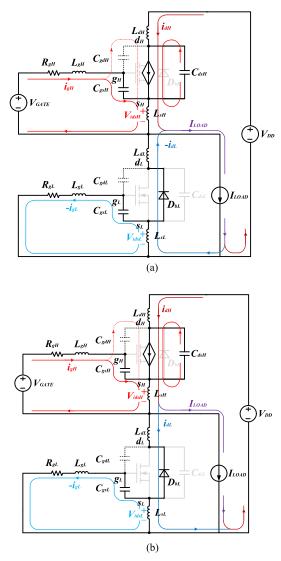


FIGURE 4. (a) Equivalent circuit for Stage 2a. (b) Equivalent circuit for Stage 2b.

The driver loop equation of  $Q_H$  can be expressed as

$$R_{gH}i_{gH} + \left(L_{gH} + L_{sH}\right)\frac{di_{gH}}{dt} + V_{idsH} + V_{gsH} = V_{GATE}$$
(11)

where  $V_{idsH}$  is the induced voltage on  $L_{sH}$  with  $i_{dH}$  increases.

$$V_{idsH} = L_{sH} \frac{di_{dH}}{dt} \tag{12}$$

When the rising rate of  $i_{dH}$  approaches its maximum, the induced voltages on  $L_{dH}$ ,  $L_{sH}$ ,  $L_{dL}$ , and  $L_{sL}$  remain constant. Thus, the power loop current can be considered as  $i_{dH} = i_{ch}$ . By combining (2) and (8)-(12), the driver loop equation of  $Q_H$  can be obtained as

$$V_{GATE} = (L_{gH} + L_{sH}) C_{gsH} \frac{d^2 V_{gsH}}{dt^2} + (R_{gH}C_{gsH} + L_{sH}g_f) \frac{dV_{gsH}}{dt} + V_{gsH}$$
(13)

The characteristic parameters of this equation can be deduced as given below:

$$\omega_{n\_H2} = \frac{1}{\sqrt{\left(L_{gH} + L_{sH}\right)C_{gsL}}} \tag{14}$$

$$\xi_{H2} = \frac{R_{gH}}{2} \sqrt{\frac{C_{gsH}}{L_{gH} + L_{sH}}} + \frac{L_{sH}g_f}{2\sqrt{(L_{gH} + L_{sH})C_{gsH}}}$$
(15)

Compared with Stage 1, the natural frequency of the driver loop is unaffected, but the damping coefficient increases with the influence of  $g_f$ .

At the same time, the induced voltage on  $L_{sL}$  increases, which will be superimposed on the driver loop of  $Q_L$  and causes a negative voltage response for  $V_{gsL}$ . The key equations can be listed as

$$V_{idsL} + V_{gsL} + R_{gL}i_{gL} + L_{gL}\frac{di_{gL}}{dt} = 0$$
(16)

$$i_{gL} = C_{gsL} \frac{dv_{gsL}}{dt}$$
(17)

$$V_{idsL} = L_{sL} \frac{dt_{dL}}{dt}$$
(18)

$$i_{dL} = i_{ch} - I_{LOAD} \tag{19}$$

where  $V_{idsL}$  is the induced voltage on  $L_{sL}$ . Combining with (8), (16)-(19), the driver loop equation of  $Q_L$  can be obtained as

$$L_{gL}C_{gsL}\frac{d^2V_{gsL}}{dt^2} + R_{gL}C_{gsL}\frac{dV_{gsL}}{dt} + V_{gsL} = -L_{sL}g_f\frac{dV_{gsH}}{dt}$$
(20)

#### 4) STAGE 2 (t2-t3) *D<sub>bL</sub>* REVERSE RECOVERY CURRENT RISE TIME

Once  $i_{dH}$  reaches  $I_{LOAD}$ , the current of  $D_{bL}$  drops to zero and the reverse recovery process starts.  $D_{bL}$  has a chargestorage effect and a great number of minority carriers accumulated at the interface of the PN junction during the previous freewheeling prosses. Thus, these minority carriers need to be elicited first and then a depletion layer can be formed. Thereafter,  $D_{bL}$  turns to the reverse-biased state and the blocking voltage starts to build up. In contrast to Stage 2a, the only difference is the direction of  $i_{dL}$ . The rising rate of  $i_{dL}$  keeps the same, the influences of  $i_{dH}$  and  $i_{dL}$  on the driver loop of upper and lower devices do not change, and the voltage distribution of the power loop keeps stable. The equivalent circuit of this sub-stage is shown in Fig. 4b. When  $i_{dL}$  increases to  $I_{RR_BV}$ , the elicitation of minority carriers is completed. The time at which this happens is denoted as t3.

The charge quantity of the minority carriers  $Q_{RS}$  is determined by the diffusion capacitance of  $D_{bL}$ , the minority carriers' lifetime, the forward current, and the junction temperature. The value of diffusion capacitance  $C_{dbL}$  can be expressed as

$$C_{dbL} = \left(\frac{1}{2V_t}\right) \left(I_{p0}\tau_{p0} + I_{n0}\tau_{n0}\right) \tag{21}$$

where  $V_t$  is the forward voltage drop and it is usually assumed to be a constant.  $\tau_{p0}$  and  $\tau_{n0}$  are the minority carriers' lifetime, and  $I_{p0}$  and  $I_{n0}$  are the equivalent current of the P zone and N zone, respectively. In the macroscopic view, the output current can be expressed as  $I_{LOAD} = I_{p0} + I_{n0}$ .  $I_{RR_BV}$  and  $Q_{RS}$  can be expressed as

$$I_{RR\_BV} = \left. \frac{di_{dL}}{dt} \right|_{t=t2} (t3 - t2) \tag{22}$$

$$Q_{RS} = \frac{1}{2} I_{RR_BV} (t3 - t2)$$
(23)

Therefore, the reverse recovery current can be obtained as

$$I_{RR\_BV} = \sqrt{2Q_{RS}g_f \left. \frac{dV_{gsH}}{dt} \right|_{t=t2}}$$
(24)

When  $i_{dL}$  reaches  $I_{RR_BV}$  at t3, it continues to rise at the same rate because of the parasitic inductances in the power loop, which can be considered as the initial condition of the blocking voltage building up in the next stage. The reverse recovery model of the independently packaged freewheeling diode applied in [17] and [20] is inadequate to describe the blocking voltage increase process. This is because the free-wheeling diode is inverse paralleled with the SiC MOSFET, hence, all the parasitic capacitances need to be considered to evaluate the response of the blocking voltage increase.

#### 5) STAGE 3 (t3-t4) VOLTAGE SWITCHING TIME

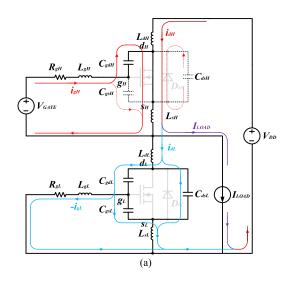
At t3, the blocking voltage of  $D_{bL}$  starts to increase, and the voltage of the bridge-leg begins to switch. The switching rate of the voltages is not only determined by the characteristic of the switching devices and the driver capability but also is restricted by the voltage dynamic equilibrium of the whole bridge-leg. This balance is maintained until  $V_{dsH}$  approaches zero and  $V_{dsL}$  increases to  $V_{DD}$ . The reverse recovery current of  $D_{bL}$  has the initial rising rate and continues to rise to  $I_{RR\_PEAK}$  and then begins to decrease. It can be regarded as the initial condition for the voltage switching process. In addition, the interelectrode capacitances values change due to the nonlinear characteristics related to the drain-source voltage, which makes the voltage switching process more complicated.

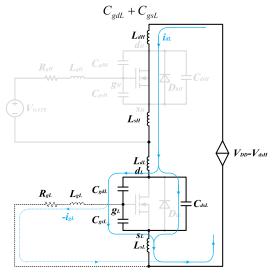
More concretely, the drop rate of  $V_{dsH}$  is determined by two key factors. The first on is the characteristics of the driver loop, which is reflected in the maximum discharge current of  $C_{gdH}$ . It is restricted by the pull-up current of the driver module, the resistances and the parasitic inductances of the driver loop, the clamp limiting factor caused by  $V_{gsH}$ , and the current carrying capacity of the channel. The second one is the characteristics of the power loop, which is reflected in the discharge rate of  $C_{dsH}$ . It is restricted by the dynamic equilibrium of the power loop. The parasitic inductances of the power loop, the parasitic capacitances of  $Q_L$ , the load characteristic, and the initial rising rate of the reverse recovery current are all associated with the discharge rate of  $C_{dsH}$ . Overall, the drop rate of  $V_{dsH}$  is determined by the slower one of the discharge rates of  $C_{gdH}$  and  $C_{dsH}$ . They keep an equilibrium state on the whole. Therefore, the power loop and driver loop are mutually coupled, their equilibrium point and the influences to the voltage switching processes are different under different operating situations that should be distinguished.

If a perfect condition is provided by the channel of  $Q_H$  and the power loop, it could satisfy the rapid discharge current of  $C_{dsH}$ . This usually occurs with SiC MOSFETs operating in high-voltage, high-current switching situations. However, the resistance conditions of the driver loop are relatively stable and it limits the maximum discharge current of  $C_{gdH}$ . Thus, the state of the driver loop reaches the limiting condition more easily, and the decrease rate of  $V_{dsH}$  is dominated by the driver loop. On the contrary, in the situations of low input voltage, low output current, or the parasitic inductances are extremely large that hinders the fast switching of the bridge-leg, the discharge process of  $C_{gdH}$  would spend less time. The decrease rate of  $V_{dsH}$  is dominated by the power loop. Besides,  $V_{dsH}$  may drop to the on-state voltage directly because of the low  $V_{DD}$  and it is all distributed by the parasitic inductances of the power loop in Stage 2. The operation enters Stage 4 directly, as shown by the gray line in Fig. 2. SiC MOSFETs work smoothly on these slow switching, light load, or low-voltage conditions. Therefore, only the former conditions will be discussed in the following.

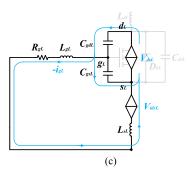
In this stage, most of  $i_{gH}$  turns to supply the discharge current of  $C_{gdH}$  and  $V_{gsH}$  remains stable basically due to the limitation of the saturation region. It causes a slight drop in  $V_{gsH}$  with  $i_{ch}$  declining from its maximum value. When  $i_{ch}$  closes to  $I_{LOAD}$ ,  $V_{gsH}$  keeps steady at the miller platform voltage  $V_{miller}$ , which can be expressed as  $V_{miller} = I_{LOAD}/$  $g_f + V_{th}$ . Thus, the current flowing through  $C_{gsH}$  decreases significantly and can be neglected. The reverse recovery current of  $D_{bL}$  starts to charge  $C_{dsL}$ ,  $C_{gdL}$ , and  $C_{gsL}$ , accompanied by the blocking voltage building up. The equivalent circuit of this stage is shown in Fig. 5a.

In the process of  $V_{dsH}$  decrease, the currents flow through the channel of  $Q_H$  include the discharge current of  $C_{gdH}$  and  $C_{dsH}$ , the reverse recovery current, and the output current  $I_{LOAD}$ . These four currents make the channel carrying current reach the maximum value. The channel keeps saturated state and the restriction of the channel to the current can be passed on to the  $V_{gsH}$  clamp limiting factor of the driver loop. The discharge current of  $C_{dsH}$  only flows through the









**FIGURE 5.** (a) Equivalent circuit for Stage 3. (b) Power loop equivalent circuit for Stage 3. (c) Driver loop of  $Q_L$  equivalent circuit for Stage 3.

channel, this process can be considered as an independent and passive response which is influenced by the decrease of  $V_{dsH}$ ,  $C_{dsH}$  is not a critical element. The driver current of  $Q_H$  turns to the following expression:

$$i_{gH} = C_{gdH} \frac{dV_{gdH}}{dt}$$
(25)

The driver loop equation of  $Q_H$  can be established as

$$R_{gH}i_{gH} + \left(L_{gH} + L_{sH}\right)\frac{di_{gH}}{dt} + V_{gdH} + V_{idsH} = V_{GATE}$$
(26-I)

This equation is only appropriate to describe the transitional process of the driver loop from Stage 2b. The initial states of  $i_{gH}$ ,  $di_{gH}/dt$ , and  $V_{idsH}$  should be considered. It is established based on  $i_{gH}$  supporting the discharge of  $C_{gdH}$ and the drain and source are regarded as an equipotential connection to avoid the voltage contradiction of  $C_{gdH}$  caused by the reference potential difference. When  $i_{gH}$  is clamped by the the driver loop saturation, it reaches the ceiling and the discharge rate of  $C_{gdH}$  reduces to zero, and the induced voltages on  $L_{gH}$  and  $L_{sH}$  caused by  $i_{gH}$  can be neglected. The driver loop equation is given by

$$R_{gH}i_{gH} + V_{miller} + V_{idsH} = V_{GATE}$$
(26-II)

where  $V_{idsH}$  is the induced voltage on  $L_{sH}$  caused by  $i_{dH}$ , it turns to negative when  $i_{dH}$  starts to decrease, and  $V_{idsH}$ gradually diminishes with  $i_{dH}$  dropping to  $i_{LOAD}$ .

The drain-source voltage of  $Q_L$  (the blocking voltage of  $D_{bL}$ ),  $V_{dsL}$ , increases. This process can be equivalent to a response of the whole parasitic capacitances of  $Q_L$  charged by the applied voltage  $V_{DD}$  -  $V_{dsH}$ , the charge current flowing through all the power loop parasitic inductances. The reverse recovery current only exists in the power loop initially. It is divided into two parts which flow through  $C_{gdL}$ and  $C_{dsL}$  respectively, and the  $C_{gdL}$  charging current is further divided by  $C_{gsL}$  and the driver loop of  $Q_L$ . The current flowing through the driver loop slowly increases from zero due to the relatively large impedance. It is too small and is not distributed naturally compared with the reverse recovery current that always exists in the power circuit. Therefore, the current in the driver loop of  $Q_L$  is not the dominant factor can be ignored when calculating the  $V_{dsL}$  response in this stage. The equivalent circuit of the power loop is shown in Fig. 5b and the power loop equations can be expressed as

$$(L_{dH} + L_{sH} + L_{dL} + L_{sL})\frac{di_{dL}}{dt} + V_{dsL} + V_{dsH} = V_{DD} \quad (27)$$
$$i_{dL} = C_{XL}\frac{dV_{dsL}}{dt} \qquad (28)$$

where

$$C_{XL} = \frac{C_{gdL}C_{gsL} + C_{gdL}C_{dsL} + C_{dsL}C_{gsL}}{C_{gdL} + C_{gsL}}$$
(29)

Combining (27)-(29) with (1), (12), (25), (26-II), the relationship between the power loop and the driver loop of  $Q_H$  can be linked by  $i_{dL}$ 

$$V_{GATE} = R_{gH}C_{gdH} \left(L_{dH} + L_{sH} + L_{dL} + L_{sL}\right) \frac{d^{2}i_{dL}}{dt^{2}} + L_{sH}\frac{di_{dL}}{dt} + \frac{R_{gH}C_{gdH}}{C_{XL}}i_{dL} + V_{miller} \quad (30)$$

 $i_{dL}$  can be deducted as

$$i_{dL} = \frac{C_{XL}}{C_{gdH}R_{gH}} (V_{GATE} - V_{miller}) - \frac{(\tau_p - \tau_q \tau_{aH3})}{\tau_r} e^{-\tau_{bH3}\omega_{n_{H3}}(t-t3)} - \frac{(\tau_p - \tau_q \tau_{bH3})}{\tau_r} \times e^{-\tau_{aH3}\omega_{n_{H3}}(t-t3)}$$
(31)

where

$$\begin{aligned} \tau_{aH3} &= \xi_{H3} - \sqrt{\xi_{H3}^2 - 1}, \quad \tau_{bH3} = \xi_{H3} + \sqrt{\xi_{H3}^2 - 1}, \\ \tau_{bH3} &= \xi_{H3} + \sqrt{\xi_{H3}^2 - 1}, \\ \tau_r &= C_{gdH} R_{gH} \omega_{n_{-}H3} \left( \tau_{bH3} - \tau_{aH3} \right), \\ \tau_p &= C_{gdH} R_{gH} \left. di_{dL} \left/ dt \right|_{t=t3}, \\ \tau_q &= \left( C_{XL} \left( V_{GATE} - V_{miller} \right) - C_{gdH} R_{gH} \left. i_{dL} \right|_{t=t3} \right) \omega_{n_{-}H3}. \end{aligned}$$

The characteristic parameters are

$$\omega_{n_H3} = \frac{1}{\sqrt{(L_{dH} + L_{sH} + L_{dL} + L_{sL})C_{XL}}}$$
(32)

$$\xi_{H3} = \frac{L_{sH}}{2C_{gdH}R_{gH}} \sqrt{\frac{C_{XL}}{L_{dH} + L_{sH} + L_{dL} + L_{sL}}}$$
(33)

And  $V_{dsL}$  can be deducted as

$$V_{dsL} = \frac{1}{C_{XL}} \int_{t_3}^{t} i_{dL} dt$$
  
=  $\frac{(V_{GATE} - V_{miller})}{C_{gdH}R_{gH}} (t - t_3) - \frac{e^{-\tau_{aH3}\omega_{n_{-}H3}(t - t_3)}}{C_{XL}\omega_{n_{-}H3}\tau_r\tau_{aH3}}$   
×  $(\tau_p - \tau_q\tau_{bH3})$   
+  $\frac{e^{-\tau_{bH3}\omega_{n_{-}H3}(t - t_3)}}{C_{XL}\omega_{n_{-}H3}\tau_r\tau_{bH3}} \cdot (\tau_p - \tau_q\tau_{aH3})$  (34)

It must be noted that this equivalent model can only be employed to calculate the response of the power loop variables, the shunted current flowing through the driver loop hardly affects the  $V_{dsL}$  response. However, it plays a key role in the crosstalk response of the driver loop. From the perspective of the driver loop of QL. The fast-rising rate of  $V_{dsL}$  results in an increase in the displacement current of  $C_{gdL}$ , the current of the driver loop to increase from zero and the voltages on  $R_{gL}$  and  $L_{gL}$  cannot be ignored. Besides, the reverse recovery current flows through  $L_{sL}$  and causes induced voltage,  $V_{idsL}$ . These two voltages responses maintain a dynamic equilibrium at  $C_{gsL}$ , which causes fluctuations in  $V_{gsL}$ , known as the crosstalk phenomenon. The equivalent circuit is shown in Fig. 5c and the equation can be expressed as

$$V_{gsL} = V_{gdL} + V_{dsL} \tag{35}$$

$$V_{idsL} = L_{sL} \frac{di_{dL}}{dt}$$
(36)

$$i_{gL} = C_{gdL} \frac{dV_{gdL}}{dt} + C_{gsL} \frac{dV_{gsL}}{dt}$$
(37)

$$R_{gL}i_{gL} + L_{gL}\frac{di_{gL}}{dt} + V_{gsL} + V_{idsL} = 0$$
(38)

Thus,  $V_{gsL}$  can be obtained as

$$L_{gL} \left( C_{gdL} + C_{gsL} \right) \frac{d^2 V_{gsL}}{dt^2} + R_{gL} \left( C_{gdL} + C_{gsL} \right) \frac{dV_{gsL}}{dt} + V_{gsL}$$
$$= \left( \frac{L_{gL} C_{gdL}}{C_{XL}} - L_{sL} \right) \frac{di_{dL}}{dt} + \frac{R_{gL} C_{gdL}}{C_{XL}} i_{dL} \quad (39)$$

The characteristic parameters of this equation can be deduced as

$$\omega_{n\_L3} = \frac{1}{\sqrt{L_{gL} \left( C_{gdL} + C_{gsL} \right)}} \tag{40}$$

$$\xi_{L3} = \frac{R_{gL}}{2} \sqrt{\frac{C_{gdL} + C_{gsL}}{L_{gL}}} \tag{41}$$

#### 6) STAGE 4 (t4-t5) GATE REMAINING CHARGING TIME

When  $V_{dsH}$  reaches the on-state voltage,  $Q_H$  works in the ohmic region and  $i_{ch}$  is separated from the relationship with  $V_{gsH}$ .  $C_{gsH}$  and  $C_{gdH}$  start charging and  $V_{gsH}$  continues to rise until it reaches  $V_{GATE}$ . The equations of the driver loop of  $Q_H$  are the same as (11) and (12) in Stage 2, and  $i_{gH}$  can be expressed as

$$i_{gH} = \left(C_{gsH} + C_{gdH}\right) \frac{dV_{gsH}}{dt} \tag{42}$$

In this stage,  $V_{dsL}$  keeps the rising rate at t4 and starts oscillating due to the parasitic inductances of the power loop and the parasitic capacitances of  $Q_L$ . The  $V_{gsH}$  increasing process for the driver loop of  $Q_H$  is a relatively independent response. But, when it is considered from the perspective of the power loop with  $Q_H$  turns on, the driver loop is equivalent to be in parallel with the common source parasitic inductance,  $L_{sH}$ . The equivalent circuit is shown in Fig. 6a.

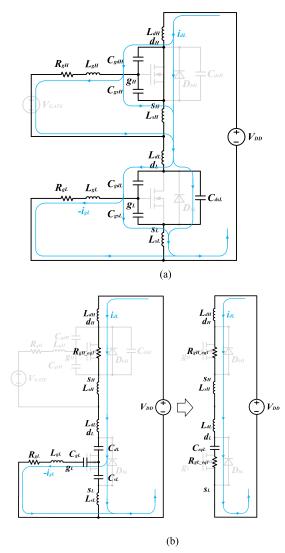
The power loop forms a serial RLC second-order circuit. Many studies consider that the resistance is composed of the stray resistance of the power loop and the on-state resistances of the SiC MOSFETs. The sums of these resistances, however, are generally in the milliohm range. Actually, the damping attenuation of the  $V_{dsL}$  oscillation is determined by the equivalent impedance of the whole poor loop which includes the paralleled drivel loop of  $Q_H$ , as described in [32] and [33]. However, it should be noted that this damping effect does not occur ideally after  $Q_H$  is fully turned-on. The power loop will start RLC oscillating once  $Q_H$  breaks away from the saturation region. Therefore, the impedance of the driver loop of  $Q_H$  in this stage is expressed as

$$X_{gH} = R_{gH} + j\omega_{n_{P4}}L_{gH} + \frac{1}{j\omega_{n_{P4}}\left(C_{gsH} + C_{gdH}\right)}$$
(43)

where  $\omega_{n_P4}$  is the oscillation frequency. The total equivalent impedance of the upper SiC MOSFET in the power loop is

$$X_H = \frac{X_{gH} \cdot j\omega_{n\_P4}L_{sH}}{X_{gH} + j\omega_{n\_P4}L_{sH}}$$
(44)

The equivalent damping resistance is determined by the ratio of the current that flows through  $R_{gH}$  and the total



**FIGURE 6.** (a) Equivalent circuit for Stage 4. (b) Simplified equivalent circuit for Stage 4.

current of the power loop, and can be expressed as

$$R_{gH\_eq1} = R_{gH} \left( \frac{|X_H|}{|X_{gH}|} \right)^2 = R_{gH} \left( \left| \frac{j\omega_{n\_P4}L_{sH}}{X_{gH} + j\omega_{n\_P4}L_{sH}} \right| \right)^2$$
  
=  $R_{gH} \frac{\omega_{n\_P4}^2 L_{sH}^2}{R_{gH}^2 + \left( \omega_{n\_P4}L_{gH} + \omega_{n\_P4}L_{sH} - \frac{1}{\omega_{n\_P4}(C_{gsH} + C_{gdH})} \right)^2}$   
(45)

As for the driver loop of  $Q_L$ ,  $C_{gsL}$ ,  $C_{gdL}$ , and  $C_{dsL}$  can be transformed into a Y connection, the driver loop is connected in parallel with the power loop from the central node as shown in Fig. 6b. The A-Y transformation is expressed as

$$C_{gL} = C_{gsL} + C_{gdL} + C_{gsL}C_{gdL}/C_{dsL}$$

$$C_{sL} = C_{gsL} + C_{dsL} + C_{gsL}C_{dsL}/C_{gdL}$$

$$C_{dL} = C_{gdL} + C_{dsL} + C_{gdL}C_{dsL}/C_{gsL}$$
(46)

 $\omega_{n_P4}$  is given by

$$\omega_{n\_P4} \approx \frac{1}{\sqrt{(L_{dH} + L_{sH} + L_{dL} + L_{sL}) C_{eqL}}} \qquad (47)$$

$$C_{eqL} = \frac{C_{dL}C_{sL}}{C_{dL} + C_{sL}}$$
(48)

The impedance of the driver loop of  $Q_L$  is expressed as

$$X_{gL} = R_{gL} + j\omega_{n\_P4}L_{gL} + \frac{1}{j\omega_{n\_P4}C_{gL}}$$
(49)

The impedance of the source branch is expressed as

$$X_{sL} = j\omega_{n\_P4}L_{sL} + \frac{1}{j\omega_{n\_P4}C_{sL}}$$
(50)

The total equivalent impedance of the lower SiC MOSFET in the power loop is

$$X_L = \frac{X_{gL} \cdot X_{sL}}{X_{gL} + X_{sL}} \tag{51}$$

The equivalent damping resistance is determined by the ratio of current flowing through  $R_{gL}$  and the total current of the power loop, which can be expressed as

$$R_{gL\_eq1} = R_{gL} \left( \frac{|X_L|}{|X_{gL}|} \right)^2$$
  
=  $R_{gL} \frac{\left( \omega_{n\_P4}L_{sL} - \frac{1}{\omega_{n\_P4}C_{sL}} \right)^2}{R_{gL}^2 + \left( \omega_{n\_P4}L_{gL} - \frac{1}{\omega_{n\_P4}C_{gL}} + \omega_{n\_P4}L_{sL} - \frac{1}{\omega_{n\_P4}C_{sL}} \right)^2}$   
(52)

Therefore, the power loop is equivalent to a second-order circuit, as shown in the right-hand side of Fig. 6b. The total equivalent resistance is then calculated by (53) and the power loop equations can be modeled as

$$R_{eq1} = R_{gH_eq1} + R_{dsH_on} + R_{gL_eq1}$$
(53)

$$V_{dsL} + R_{eq1}i_{dL} + (L_{dH} + L_{sH} + L_{dL} + L_{sL})\frac{di_{dL}}{dt} = V_{DD}$$
(54)

$$i_{dL} = C_{eqL} \frac{dV_{dsL}}{dt}$$
(55)

It is noteworthy that the A-Y transform for the driver loop of  $Q_L$  can be only applied in this full turn-on state because the currents of the driver loop and the power loop for  $Q_L$ transit into a natural distribution. While in Stage 3, the current distribution in the driver loop of  $Q_L$  builds up from zero, which is too small and not distributed naturally, it should be ignored.

The initial value of  $V_{dsL}$  is  $V_{DD}$  and the initial rising rate of  $V_{dsL}$  depends on the switching rate in Stage 3. The damping coefficient is obtained as

$$\xi_{P4} = \frac{R_{eq1}}{2} \sqrt{\frac{C_{eqL}}{L_{dH} + L_{sH} + L_{dL} + L_{sL}}}$$
(56)

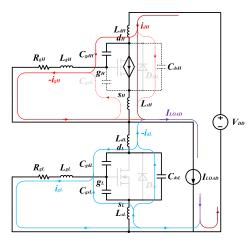


FIGURE 7. Equivalent circuit for Stage 6.

The response of  $V_{gsL}$  can still be described by the separate equivalent model for the driver loop of  $Q_L$  in stage 3.  $V_{gsL}$  will fluctuate due to the oscillations in the displacement current of  $C_{gdL}$  and the induced voltage over  $L_{sL}$ . The natural frequency and the damping coefficient of the driver loop of  $Q_L$  remain the same as those in Stage 3.

#### **B. TURN-OFF SWITCHING TRANSITION**

#### 1) STAGE 5 (t6-t7) TURN-OFF DELAY TIME

When the gate signal of  $Q_H$  is set to zero,  $C_{gsH}$  and  $C_{gdH}$  start discharging through the driver loop, and  $V_{gsH}$  decreases.  $Q_H$  operates in the ohmic region until  $V_{gsH}$  drops to  $V_{miller}$ .  $i_{dH}$  keeps flowing through the channel of  $Q_H$  and remains unchanged. The driver loop equation of  $Q_H$  is given by (57), and  $i_{gH}$  is still expressed by (42). The characteristic parameters of the driver loop of  $Q_H$  keep the same as Stage 4.

$$V_{gsH} + R_{gH}i_{gH} + (L_{gH} + L_{sH})\frac{di_{gH}}{dt} = 0$$
 (57)

#### STAGE 6 (t7-t8) VOLTAGE SWITCHING TIME

 $Q_H$  enters the saturation region at this stage and the channel resistance starts to increase. The load current continues to support through  $Q_H$  due to  $D_{bL}$  is still reverse-biased.  $V_{dsH}$  starts to rise and  $V_{dsL}$  decreases until it reaches the forward turn-on voltage of  $D_{bL}$ .  $C_{gdH}$  and  $C_{dsH}$  are charged,  $C_{gdL}$  and  $C_{dsL}$  are discharged, the displacement currents of these capacitances supply part of the load current and cause  $i_{ch}$  decreases to some extent.

Similar to the turn-on counterpart (Stage 3), almost all the current of the  $Q_H$  driver loop comes from the charging current of  $C_{gdH}$  and dominates the rising rate of  $V_{dsH}$ . The current flowing through  $C_{gsH}$  can be neglected. The equivalent circuit of this stage is shown in Fig. 7.

The charging process  $C_{gdH}$  can be established as

$$-R_{gH}i_{gH} - L_{gH}\frac{di_{gH}}{dt} - V_{gdH} + V_{iddH} = V_{DD}$$
(58)

$$V_{iddH} = L_{dH} \frac{di_{dL}}{dt} \quad (59)$$

where  $i_{gH}$  is same as (25), and  $V_{iddH}$  is the induced voltage of  $L_{dH}$  due to  $i_{dH}$  decreases.

When  $i_{gH}$  is clamped by the saturated state of the driver loop, the charge rate of  $C_{gdH}$  reaches the ceiling and the driver loop equation is given by

$$R_{gH}i_{gH} + V_{miller} + V_{idsH} = 0 \tag{60}$$

As for  $Q_L$ , the decrease of  $V_{dsL}$  is restricted by the dynamic equilibrium of the power loop. All the parasitic parameters of the power loop and the driver loop need to take into consideration. Same as Stage 4,  $C_{gsL}$ ,  $C_{gdL}$ , and  $C_{dsL}$  can be transformed to Y connection and then the driver loop can be simplified to a second-order circuit. The equivalent damping resistance can be deduced as

 $R_{gL_eq2}$ 

$$= R_{gL} \left(\frac{|X_L|}{|X_{gL}|}\right)^2$$
  
=  $R_{gL} \frac{\left(\omega_{n_P6}L_{sL} - \frac{1}{\omega_{n_P6}C_{sL}}\right)^2}{R_{gL}^2 + \left(\omega_{n_P6}L_{gL} - \frac{1}{\omega_{n_P6}C_{gL}} + \omega_{n_P6}L_{sL} - \frac{1}{\omega_{n_P6}C_{sL}}\right)^2}$   
(61)

where  $\omega_{n_P6} \approx 1/\sqrt{(L_{dL} + L_{sL}) C_{eqL}}$ , the equivalent power loop equation of  $Q_L$  can be modeled as

$$L_{dL}C_{eqL}\frac{d^2V_{dsL}}{dt^2} + R_{gL\_eq2}C_{eqL}\frac{dV_{dsL}}{dt} + V_{dsL}$$
  
=  $V_{DD} - V_{dsH} - V_{idsH} - V_{iddH}$  (62)  
 $i_{dL} = C_{eqL}\frac{dV_{dsL}}{dt}$  (63)

Combining (58)-(63) with (1), (12), (25), the relationship between the power loop and the driver loop of  $Q_H$  can be linked by  $i_{dL}$ 

$$R_{gH}C_{gdH} \left(L_{dH} + L_{sH} + L_{dL}\right) \frac{d^2 i_{dL}}{dt^2} + \left(R_{gH}R_{gL\_eq2}C_{gdH} + L_{sH}\right) \frac{d i_{dL}}{dt} + \frac{R_{gH}C_{gdH}}{C_{eqL}} i_{dL} + V_{miller} = 0$$
(64)

In this stage, the initial value and rate of  $i_{dL}$  are zero, the characteristic parameters are

$$\omega_{n_{H6}} = \frac{1}{\sqrt{(L_{dH} + L_{sH} + L_{dL}) C_{eqL}}}$$
(65)

$$\xi_{H6} = \frac{R_{gH}R_{gL\_eq2}C_{gdH} + L_{sH}}{2C_{gdH}R_{gH}} \sqrt{\frac{C_{eqL}}{L_{dH} + L_{sH} + L_{dL}}}$$
(66)

Correspondingly, the  $V_{gsL}$  crosstalk response can also be described by the separate equivalent model of the driver loop in Stage 3. There is a negative crosstalk voltage response of  $V_{gsL}$  due to the rapid drop of  $V_{dsL}$ .

#### 3) STAGE 7 (t8-t9) CURRENT SWITCHING TIME

After  $V_{dsL}$  reaches the forward voltage of  $D_{bL}$ , the current begins to divert from the channel of  $Q_H$  to  $D_{bL}$ .  $V_{dsH}$  keeps the rising rate at t8 and starts oscillating, which is coupled with the current switching process. When  $V_{dsH}$  reaches  $V_{DD}$ , the charge rate of  $C_{gdH}$  no longer dominants the rising rate of  $V_{dsH}$ ,  $C_{gdH}$  is paralleled with  $C_{dsH}$  and is involved in the oscillating of the power loop. However, similar to Stage 2,  $C_{gdH}$  stays at a minimum due to the nonlinear characteristic. The displacement current of  $C_{gdH}$  is much smaller than the charge current of  $C_{dsH}$  and the discharge current of  $C_{gsH}$ , which exerts little influence on the power loop and can be neglected in this stage. The equivalent circuit of this stage is shown in Fig. 8.

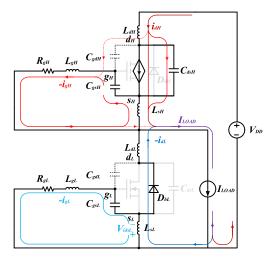


FIGURE 8. Equivalent circuit for Stage 7.

The driver loop of  $Q_H$  can be can be expressed as

$$R_{gH}i_{gH} + (L_{gH} + L_{sH})\frac{di_{gH}}{dt} + V_{idsH} + V_{gsH} = 0 \quad (67)$$

where  $i_{gH}$  and  $V_{idsH}$  can be obtained from (2) and (12). Part of the drain current flowing through  $C_{dsH}$  dominates the oscillation of  $V_{dsH}$ . The remaining current flows through the channel,  $i_{dH}$  can be expressed as

$$i_{dH} = i_{ch} + C_{dsH} \frac{dV_{dsH}}{dt}$$
(68)

where  $i_{ch}$  is controlled by  $V_{gsH}$  which is given by (8).

The power loop can be established as

$$(L_{dH} + L_{sH} + L_{dL} + L_{sL})\frac{di_{dH}}{dt} + L_{sH}\frac{di_{gH}}{dt} + V_{dsH} = V_{DD}$$
(69)

With the increase of the freewheeling current of  $D_{bL}$ , a negative induced voltage on  $L_{sL}$  is superimposed on the driver loop of  $Q_L$ . The equations of the driver loop are the same as Stage 2. Since the direction of the increasing freewheeling current is negative, a positive gate-source voltage fluctuation is induced in this stage.

4) STAGE 8 (t9-t10)  $V_{gsH}$  REMAINING DECREASING TIME When the load current flows entirely through  $D_{bL}$ ,  $Q_H$  is completely shut down and  $V_{gsH}$  decreases to zero, while the voltage and current of the power loop keep oscillation. Due to  $Q_H$  breaks away from the saturation region, all the parasitic capacitances of  $Q_H$  are involved in the oscillation in this stage. The equivalent circuit is shown in Fig. 9a.

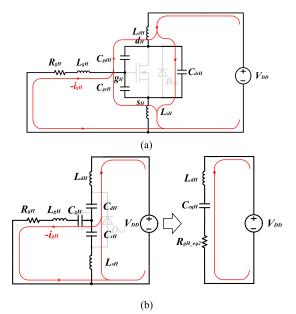


FIGURE 9. (a) Equivalent circuit for Stage 8. (b) Simplified equivalent circuit for Stage 8.

Similar to the state of  $Q_L$  in Stage 4, the paralleled driver loop of  $Q_H$  has a restrained effect on the oscillation.  $C_{gsH}$ ,  $C_{gdH}$ , and  $C_{dsH}$  could be transformed to Y connection, which is given by (70) and the simplified equivalent circuit is shown in Fig. 9b.

$$\begin{cases} C_{gH} = C_{gsH} + C_{gdH} + C_{gsH}C_{gdH} / C_{dsH} \\ C_{sH} = C_{gsH} + C_{dsH} + C_{gsH}C_{dsH} / C_{gdH} \\ C_{dH} = C_{gdH} + C_{dsH} + C_{gdH}C_{dsH} / C_{gsH} \end{cases}$$
(70)

The equivalent damping resistance can be deducted as

$$R_{gH\_eq2} = R_{gH} \left( \frac{|X_H|}{|X_{gH}|} \right)^2$$
  
=  $R_{gH} \frac{\left( \omega_{n\_P8} L_{sH} - \frac{1}{\omega_{n\_P8} C_{sH}} \right)^2}{R_{gH}^2 + \left( \omega_{n\_P8} L_{gH} - \frac{1}{\omega_{n\_P8} C_{gH}} + \omega_{n\_P8} L_{sH} - \frac{1}{\omega_{n\_P8} C_{sH}} \right)^2}$ (71)

where  $\omega_{n_P8} = 1/\sqrt{(L_{dH} + L_{sH}) C_{eqH}}$ , and  $C_{eqH} = C_{dL}C_{sL}/(C_{dL} + C_{sL})$ .

The power loop equations can be expressed as

$$V_{DD} = L_{dH}C_{eqH}\frac{d^{2}V_{dsH}}{dt^{2}} + R_{gH_{eq2}}C_{eqH}\frac{dV_{dsH}}{dt} + V_{dsH}$$
(72)

The characteristic parameters are

$$\omega_{n\_H8} = \frac{1}{\sqrt{C_{eqH}L_{dH}}} \tag{73}$$

$$\xi_{H8} = \frac{R_{gH\_eq2}}{2} \sqrt{\frac{C_{eqH}}{L_{dH}}}$$
(74)

This stage will extend until  $V_{dsH}$  stabilizes at  $V_{DD}$  and this process may spend more time than that  $V_{gsH}$  decreases to zero.

 TABLE 1. The critical parameters in each stage and their effects.

-	Main	Critical para	Critical parameter		
stage	variable	Parasitic element	Variable	parameter	
	$V_{gsH}$	$L_{sH}, R_{gH}, C_{gsH}$	di <sub>dH</sub> /dt	$C_{gdH}$	
	di <sub>dH</sub> /dt		$g_{f}, V_{gsH}$	$C_{gdH}$	
2	$V_{dsH}$	$L_{dH}, L_{sH}, L_{dL}, L_{sL}$	di <sub>dH</sub> /dt		
	$V_{gsL}$	$L_{sH}$	di <sub>dH</sub> /dt	$C_{gdL}$	
	$I_{RR\_BV}$	$Q_{SR}$	$di_{dH}/dt _{t=t2}$		
	$i_{dL}$	$C_{gdH}, R_{gH}, L_{sH}, C_{XL}$	$V_{miller}, I_{RR\_BV}, \ di_{dH}/dt _{t=t3}$	$C_{gsH}, C_{dsH}, \ L_{gH}, L_{sH}, \ di_{gH}/dt,$	
3	$dV_{dsL}/dt$	$C_{XL}$	$i_{dL}$	$R_{gL}, L_{gL}$	
	$V_{gsL}$	$R_{gL} = egin{smallmatrix} L_{sH} \ C_{gdL} \end{pmatrix}$	di <sub>dH</sub> /dt dV <sub>dsL</sub> /dt		
4	$V_{dsL}$	$R_{gH\_eql}, R_{gL\_eql}, C_{XL}$	$dV_{dsL}/dt _{t=t4}$		
	$i_{dL}$	$C_{gdH}, R_{gH}, L_{sH}, \ C_{eqL}, R_{gL\_eq2}$		$C_{gsH}, C_{dsH}, \ L_{gH}, L_{sH},$	
6	$dV_{dsL}/dt$	$C_{eqL}$	$i_{dL}$	di <sub>gH</sub> /dt	
	$V_{gsL}$	$R_{gL} = egin{matrix} L_{sH} \ C_{gdL} \end{pmatrix}$	di <sub>dH</sub> /dt dV <sub>dsL</sub> /dt		
	$V_{gsH}$	$L_{sH}, R_{gH}, C_{gsH}$	di <sub>dH</sub> /dt	$C_{gdH}$	
7	di <sub>dH</sub> /dt	$C_{dsH}$	$g_{\it f},V_{gsH}\ dV_{dsH}\!/dt$	$C_{gdH}$	
/	$V_{dsH}$	$L_{dH}, L_{sH}, L_{dL}, L_{sL}$	$di_{dH}/dt,\ dV_{dsH}/dt _{t=t8}$	$C_{gdH}$	
	$V_{gsL}$	$L_{sH}$	di <sub>dH</sub> /dt	$C_{gdL}$	
8	$V_{dsH}$	$C_{eqH}, R_{gH\_eq2}$	$dV_{dsL}/dt _{t=t9}$		

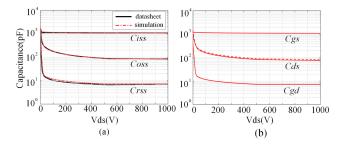
Summarily, based on the preceding discussion, the critical parameters separately discussed of each stage and their effects on the main variables are summarized in Table 1.

#### III. EFFECTS OF CRITICAL PARAMETERS ON THE SWITCHING PERFORMANCE

Based on the derived model, the correlations between the main variable responses and the parameters in each stage are thoroughly analyzed. The influence mechanism and coupling effects of the critical parameters are clarified. Therefore, the influence trends can undergo further analysis to distinguish the effect weights of the critical parameters in each stage. A 600V/20A double pulse test circuit is built. The bridge-configuration is composed of the SiC MOSFETs, C2M0080120D, from Wolfspeed corporation. All the analytical calculation circuit parameters and the value of parasitic elements are based on this real circuit configuration within reasonable ranges, the switching process can be simulated by

#### TABLE 2. Fixed parameter setup.

Component	Parameter	Value	Parameter	Value
	$V_{DD}$	600V	$L_{dH_{ex}} + L_{dL_{ex}}$	5.5nH
Power circuit	$I_{DD}$	20A	$L_{LOOP}$	50nH
	$V_{GATE}$	20V	$R_{LOOP}$	$120 \mathrm{m}\Omega$
	$V_{th}$	3.3V	$Q_{RS}$	26nC
	$R_{gH\_ex}$	$8.2\Omega$	$R_{gL\_ex}$	$8.2\Omega$
	$R_{gH\_in}$	3.9Ω	$R_{gL\_in}$	3.9Ω
Upper and lower	$L_{gH\_in}$	1.1nH	$L_{gL\_in}$	1.3nH
SiC MOSFET (C2M0080120D)	$L_{gH\_ex}$	2.6nH	$L_{gL\_ex}$	2.7nH
(C2100000120D)	$L_{sH\_in}$	1.3nH	$L_{sL\_in}$	1.3nH
	$L_{sH\_ex}$	3.7nH	$L_{sL\_ex}$	3.4nH
	$L_{dH\_in}$	1.2nH	$L_{dL\_in}$	1.1nH



**FIGURE 10.** Nonlinear capacitance curves. (a) Comparison between the data from datasheet and the simulation. (b) interelectrode capacitances calculated by the simulation.

MATLAB calculations stage-by-stage. The initial and fixed parameters of the circuit model are listed in Table 2.

To ensure the accuracy of calculations, the nonlinear parameters should be described accurately. The datasheet of SiC MOSFET provides the curves of the input capacitance  $C_{iss}$ , the output capacitance  $C_{oss}$ , and the reverse transfer capacitance  $C_{rss}$  versus the drain-source voltage  $V_{ds}$ . According to the method provided in [19], [30], and [34], the nonlinearity of the capacitance can be piecewise fitted by (75), and the interelectrode capacitances can be obtained by (76) based on the datasheet.

$$C = C_{jo} \left( 1 + \frac{V_{ds}}{V_j} \right)^{-m} \tag{75}$$

where  $C_{jo}$  is the capacitance value when  $V_{ds} = 0$ ,  $V_j$  is the built-in voltage, *m* is the capacitance gradient factor. They can be adjusted according to the range of  $V_{ds}$ .

$$C_{iss} = C_{gs} + C_{gd}$$

$$C_{oss} = C_{ds} + C_{gd}$$

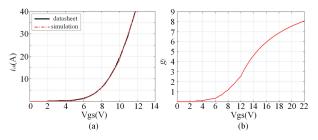
$$C_{rss} = C_{gd}$$
(76)

Fig.10(a) shows the fitted capacitance curves compared with the datasheet. The interelectrode capacitance curves are shown in Fig.10(b). Since  $C_{gs}$  and  $C_{ds}$  are much larger than  $C_{gd}$ , the interelectrode capacitances curves are almost same as the parasitic capacitances' curves provided in the datasheet.

The transconductance  $g_f$  represents the transfer current capability of the channel. The datasheet provides the curve of the transfer characteristic, the nonlinear increase of  $i_{ch}$  could be piecewise fitted by (77).

$$i_{ch} = k_1 \left( V_{gs} - V_{th} \right)^n + k_2 \tag{77}$$

where  $k_1$ ,  $k_2$ , and *n* are parameters of the transconductance and can be adjusted according to the value range of  $V_{gs}$ . Fig. 11(a) shows a comparison between the transconductance characteristic curve provided by the datasheet and the piecewise fitting result. Thus, the nonlinear curve of  $g_f$  can be obtained, which is shown in Fig.11(b). Notice that  $g_f$ becomes gentle when the rate of  $i_{ch}$  reaches the maximum.



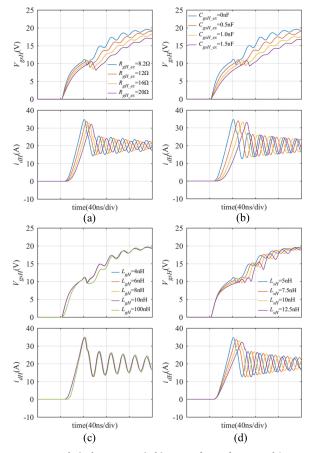
**FIGURE 11.** Nonlinear capacitance curves. (a) Comparison between the data from datasheet and the simulation. (b) interelectrode capacitances calculated by the simulation.

The piecewise fitting model of the interelectrode capacitances and  $g_f$  can be invoked as independent computing units based on the values of  $V_{dsH}$ ,  $V_{dsL}$ , and  $V_{gsH}$  to obtain the precise values in every discrete computing period of MATLAB.

In order to compare the importance of different parameters in terms of their influences in the same stage, the original parameters of the model are referred to as the basic values. These basic values are varied by uniformly multiplying themselves by 1.5, 2, and 2.5 in this paper. Because of the nonlinear characteristics of interelectrode capacitances, the minimum values of the capacitances are used as the basic values.

#### A. CURRENT SWITCHING RATE

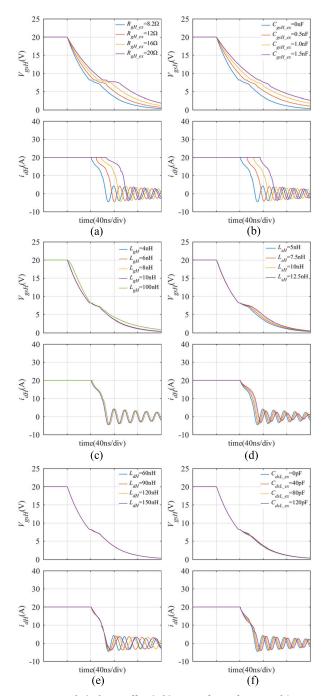
The current switching processes occur in Stage 2 and Stage 7, where  $Q_H$  works in the saturation region. In Stage 2a, the rising rate of  $i_{ch}$  is determined by the response of  $V_{gsH}$  and  $g_f$ . According to (15), the damping coefficient  $\xi_{H2}$  increases with the increases in  $R_{gH}$  and  $C_{gsH}$ , which reduces the slew rates of  $V_{gsH}$ . Fig. 12 (a) and (b) presents the turn-on analytical waveforms of  $V_{gsH}$  and  $i_{dH}$  with increased  $R_{gH}$  and  $C_{gsH}$ .  $L_{gH}$ also can reduce  $\xi_{H2}$ , but it has a lesser effect in comparison with  $C_{gsH}$ ,  $L_{sH}$ , and  $R_{gH}$ . The analytical waveforms of  $V_{gsH}$ and  $i_{dH}$  are shown in Fig.12(c). It emerges that, a significant difference in the rising response of  $V_{gsH}$  and  $i_{dH}$  appears when  $L_{gH}$  increases over twenty times. The nonlinear growth of  $g_f$  promotes the increase of  $i_{dH}$ . According to (8), (11), and (12), when the rising rate of  $i_{dH}$  increases, the induced voltage on  $L_{sH}$  provides a negative feedback to the driver loop, which weakens  $V_{gsH}$  build-up, and the driver loop keeps its equilibrium state (13). (15) reveals that  $L_{sH}$  and  $g_f$  could



**FIGURE 12.** Analytical turn-on switching waveform of  $V_{gsH}$  and  $i_{dH}$  showing the effect of (a)  $Q_H$  driver resistance. (b)  $Q_H$  gate-source capacitance. (c)  $Q_H$  gate inductance. (d)  $Q_H$  source inductance.

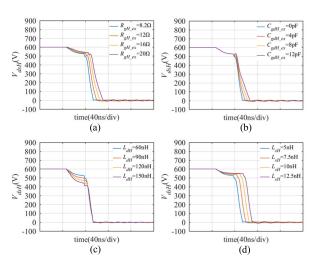
increase  $\xi_{H2}$ , which decreases the response speed of  $V_{gsH}$ . Thus, it is noteworthy that although  $g_f$  ostensibly increases the rising rate of  $i_{dH}$ , it strengthens the negative feedback that restricts the rising rate of  $V_{gsH}$ , which in turn restrains the growth of  $g_f$ . As a result, the rising rate of  $i_{dH}$  will reach and be limited at its maximum. This effect will be more obvious with a larger  $L_{sH}$ . The analytical switching waveforms with varying  $L_{sH}$  are shown in Fig. 12(d). In Stage 2b, the reverse recovery current flows through  $D_{bL}$ . The rising rate of  $i_{dH}$ stays the same as that in Stage 2a. It is because the equilibrium state of the driver loop remains unchanged.

Fig. 13(a), (b), and (c) show the turn-off analytical switching waveforms of  $V_{gsH}$  and  $i_{dH}$ . Similar to the turn-on counterpart, the slew rate of  $i_{dH}$  decreases with larger  $R_{gH}$ ,  $C_{gsH}$ , and  $L_{gH}$ .  $L_{sH}$  still provides a negative feedback to the driver loop. However, a portion of the drain current already starts switching in the voltage switching process (charging the parasitic capacitances  $C_{gdH}$  and  $C_{dsH}$  in Stage 6), which shunts the channel current  $i_{ch}$ . In Stage 7, this phenomenon will continue with the oscillation of  $V_{dsH}$ . The decrease rate of the shunted current through  $C_{dsH}$  depends on the characteristic of the power loop, which is determined by all the parasitic inductances of the bridge-leg according to (69), while  $L_{sH}$  hardly



**FIGURE 13.** Analytical turn-off switching waveform of  $V_{gsH}$  and  $i_{dH}$  showing the effect of (a)  $Q_H$  driver resistance. (b)  $Q_H$  gate-source capacitance. (c)  $Q_H$  gate inductance. (d)  $Q_H$  source inductance. (e) parasitic inductances of the power loop. (f)  $Q_L$  drain-source capacitance.

changes the rate of the current through  $C_{dsH}$ . Thus, it can be considered as the shunted current through  $C_{dsH}$  weakens the negative feedback effect of  $L_{sH}$ , and  $i_{dH}$  is less controlled by the driver loop. Further, because of the shunted current through  $C_{dsH}$ ,  $i_{ch}$  is smaller than  $I_{LOAD}$  at the beginning of Stage 7 and  $V_{gsH}$  has a lower value, which cause  $g_f$  to be smaller. The channel current  $i_{ch}$  decreases faster compared



**FIGURE 14.** Analytical turn-on switching waveform of  $V_{dsH}$  showing the effect of (a)  $Q_H$  driver resistance. (b)  $Q_H$  gate-drain capacitance. (c) parasitic inductances of the power loop. (d)  $Q_H$  source inductance.

with the turn-on process in Stage 2. The turn-off analytical switching waveforms of  $V_{gsH}$  and  $i_{dH}$  with varying  $L_{sH}$  are shown in Fig. 13 (d). To compare Fig. 13 (d) with Fig. 12(d), the maximum rate of  $i_{dH}$  in the turn-off stage is faster than that in the turn-on stage. When  $L_{sH}$  increases, the variation tendency of the decrease rate of  $i_{dH}$  is less noticeable than it is in the turn-on stage. With the increase of the parasitic inductances of the power loop, the oscillation frequency drops, which causes the slew rate of  $i_{dH}$  to decrease, as shown in Fig.13(e). The increase in  $C_{dsH}$  extends its discharging time and increases the  $i_{dH}$  drop in Stage 6, and it has a limited effect on the current switching rate in Stage 7, as shown in Fig.13(f).

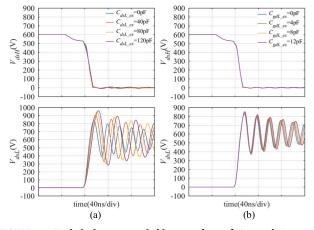
#### **B. VOLTAGE SWITCHING RATE**

The voltage switching processes occur in Stages 2, 3, and 6. In Stage 2, the rapid current switching of the power loop causes the induced voltages over the parasitic inductances and  $V_{dsH}$  to drop from  $V_{DD}$ . This voltage drop is determined by the value of the parasitic inductances and the rising rate of the drain currents. Fig. 14 (a), and (d) illustrate that the increase in  $R_{gH}$  and  $L_{sH}$  diminishes the amplitude of  $V_{dsH}$ drop, which is essentially because of the confined rising rate of  $i_{dH}$ . In Fig. 14 (c), the increase in  $L_{dH}$  raises the amplitude of  $V_{dsH}$  drop because voltage over it is higher.

In Stage 3, the decrease rate of  $V_{dsH}$  depends on the discharging speed of  $C_{gdH}$ . The discharging current is clamped by the state of the power loop, which is directly determined by  $R_{gH}$ ,  $C_{gdH}$  and the value of  $V_{miller}$ . Besides, the reverse recovery current (drain current of  $Q_L$ ) decreases in this stage, it charges the parasitic capacitances of  $Q_L$  depending on its initial state and influences the voltage switching responses indirectly.

It can be derived from the responses of the power loop, (31)-(34), that although the increases in  $R_{gH}$  and  $C_{gdH}$  could reduce the damping coefficient  $\xi_{H3}$ , however, they still exist

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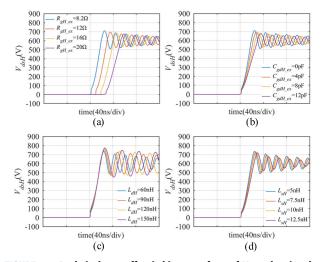


**FIGURE 15.** Analytical turn-on switching waveform of  $V_{dsL}$  and  $V_{dsL}$  showing the effect of (a)  $Q_L$  drain-source capacitance. (b)  $Q_L$  gate-drain capacitance.

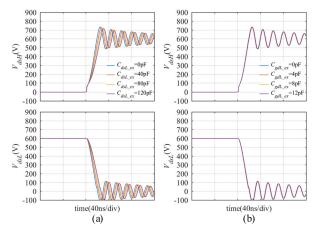
Similarly, the increase in the equivalent capacitance of  $Q_L$ ,  $C_{XL}$ , changes the characteristics of the power loop ( $\xi_{H3}$  increased and  $\omega_{n_H3}$  decreased), but does not affect the voltage switching rate. In (31), the increase in  $C_{XL}$  directly causes the steady-state components of  $i_{dL}$  to increase, whereas it does not exist in the steady-state components of  $V_{dsL}$  in (34).  $C_{XL}$  is definitively determined by  $C_{dsL}$ . It is because that  $C_{gdL}$  is in series with  $C_{gsL}$ , especially  $C_{gdL}$  is less than  $C_{gsL}$  and  $C_{dsL}$  in one or two orders of magnitude, which hardly changes the value of  $C_{XL}$ . As shown in Fig. 10,  $C_{XL}$  is depicted by a dotted line which is almost near  $C_{dsL}$  and  $V_{dsL}$  with varying  $C_{dsL}$  and  $C_{gdL}$ .

In the voltage switching process, a non-negligible factor is the nonlinear characteristics of the interelectrode capacitances, especially the gate-drain capacitances, which significantly increase with the decrease of the drain-source voltage. In Stage 3, these changes increase  $\omega_{n_H3}$  and decrease  $\xi_{H3}$ , which can accelerate the switching rate gradually.

To sum up, in the turn-on process, the voltage switching rate is determined by the clamped current of the driver loop of  $Q_H$ , the initial state of the reverse recovery current, the characteristics of the power loop, and the nonlinear characteristics of the interelectrode capacitances. It is the most complex switching process which involves numerous closely related parameters.



**FIGURE 16.** Analytical turn-off switching waveform of  $V_{dSH}$  showing the effect of (a)  $Q_H$  driver resistance. (b)  $Q_H$  gate-drain capacitance. (c) parasitic inductances of the power loop. (d)  $Q_H$  source inductance.



**FIGURE 17.** Analytical turn-off switching waveform of  $V_{dsL}$  and  $V_{dsL}$  showing the effect of (a)  $Q_L$  drain-source capacitance. (b)  $Q_L$  gate-drain capacitance.

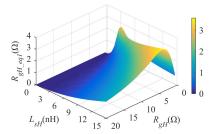
In Stage 6, the restrictive conditions are the same as those in Stage 3. Fig. 16 displays the turn-off analytical switching waveforms of  $V_{dsH}$  with varying  $R_{gH}$ ,  $C_{gdH}$ ,  $L_{dH}$ , and  $L_{sH}$ . However, the initial values and rates of the charging currents of  $Q_H$  and the discharging currents of  $Q_L$  are zero, which prolong the switching time. Therefore, the voltage switching rate in this stage is lower than that in Stage 3 even under the same parasitic element conditions.

The increase in the parasitic capacitances of  $Q_L$  also increases the damping coefficient  $\xi_{H6}$ . The difference in the voltage slew rate is more noticeable than in the turn-on process. Fig. 17 presents the turn-off analytical switching waveforms of  $V_{dsH}$  and  $V_{dsL}$  with varying  $C_{dsL}$  and  $C_{gdL}$ .

Based on the current and voltage switching, fast slew rates serve as critical parameters that further exert knock-on effects on the switching process of the bridge-leg. The most significant impacts are the oscillations of the power loop and crosstalk phenomenon of the driver loop.

#### C. OSCILLATIONS IN THE POWER LOOP

The oscillations in the power loop occur in Stage 4, 7 and 8. In Stage 4,  $V_{dsL}$  reaches  $V_{DD}$  and keeps the rising rate from Stage 3, which can be regarded as the initial state of the power loop oscillation. According to (47) and (56), the oscillation intensifies with the decrease in  $C_{eqL}$  and the increase in the parasitic inductances of the power loop. The literature [33] reveals that the equivalent resistance  $R_{gH\_eq1}$  has nonmonotonic relations with  $R_{gH}$  and  $L_{sH}$ , and the same trend is also true for  $R_{gL_eq1}$ . While it only considers the optimum value of driver resistance for taking the maximum of equivalent resistance to suppress the oscillation. The value of  $R_{gH}$  eal considered varying  $R_{gH}$  and  $L_{sH}$  is further presented in Fig. 18. It can be found that the maximum values of  $R_{gH}$  eal exist in the range of  $R_{gH}$  is less than 3.7 $\Omega$ . However, the internal gate resistance of a SiC MOSFET is usually beyond this range. Thus,  $R_{gH}$  eq1 only decreases with the increase in  $R_{gH}$ . While  $R_{gH_eq1}$  is positively correlated with  $L_{sH}$ . Equally, the same result can be derived for  $R_{gL eq1}$  according to (52).

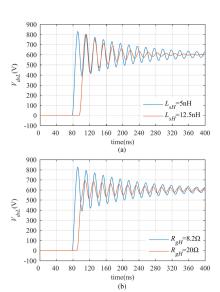


**FIGURE 18.** Equivalent resistance of  $Q_H$  with varied  $R_{gH}$  and  $L_{sH}$  in Stage 4.

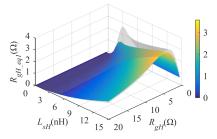
Therefore, to suppress the oscillation,  $R_{gH}$  should decrease and  $L_{sH}$  should increase. Combined with the analysis of part B, the increases in  $R_{gH}$  and  $L_{sH}$  can reduce the initial rising rate of  $V_{dsL}$ , which could restrict the oscillation fundamentally. Thus, the increase in  $L_{sH}$  suppresses oscillation amplitude and shortens the oscillation time, whereas the increase in  $R_{gH}$  prolong the oscillation time. Fig. 19 illustrates the turn-on analytical oscillation waveforms of  $V_{dsL}$ with various  $L_{sH}$  and  $R_{gH}$ .

In Stage 7, the oscillation of the power loop is accompanied by the current switching process. The decrease in the channel current  $i_{ch}$  causes negative induced voltages across  $L_{dH}$ and  $L_{sH}$ , which are superimposed on the oscillation circuit  $(L_{dH} \text{ and } L_{sH} - C_{dsH})$ . This factor increases the  $V_{dsH}$  amplitude of the initial oscillation. Combining the analyses of parts A and B, the increases in  $R_{gH}$ ,  $C_{gsH}$ ,  $C_{gdH}$ , and  $L_{sH}$  reduce the initial rising rate of  $V_{dsH}$  or the decrease rate of  $i_{ch}$ , which diminish the amplitude of  $V_{dsH}$ . While the increase in  $L_{dH}$  aggravates the oscillation amplitude. These trends are predicted by the analytical waveform in Fig. 16.

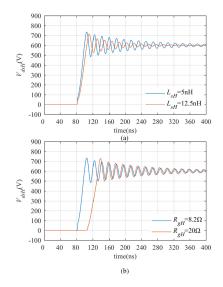
In Stage 8,  $Q_H$  is completely shut down. Similar to the state of  $Q_L$  in Stage 4, the trend of equivalent resistance  $R_{gH\_eq2}$  can be obtained as shown in Fig. 20, where the gray translucent surface is  $R_{gH\_eq1}$  in Stage 4. It shows that



**FIGURE 19.** Analytical turn-on oscillation waveform of  $V_{dsL}$  showing the effect of (a)  $Q_H$  source inductance. (b)  $Q_H$  driver resistance.



**FIGURE 20.** Equivalent resistance of  $Q_H$  with varied  $R_{gH}$  and  $L_{sH}$  in Stage 8.



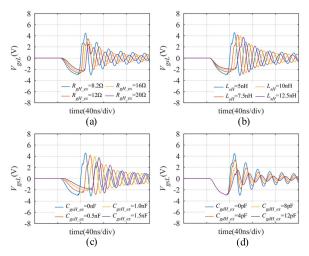
**FIGURE 21.** Analytical turn-off oscillation waveform of  $V_{dsH}$  showing the effect of (a)  $Q_H$  source inductance. (b)  $Q_H$  driver resistance.

 $R_{gH\_eq2}$  has the same variation trend as varying  $R_{gH}$  and  $L_{sH}$  in Stage 4. Fig. 21 illustrates the turn-off analytical oscillation waveforms of  $V_{dsH}$  with varying  $L_{sH}$  and  $R_{gH}$ .

#### D. CROSSTALK OF THE DRIVER LOOP

During the turn-on and turn-off processes of  $Q_H$ , the crosstalk phenomenon occurs at the driver loop of  $Q_L$  and lasts almost throughout the whole switching process.

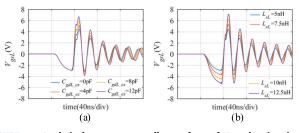
In Stage 2, a positive induced voltage of  $L_{sL}$  is superimposed on the driver loop of  $Q_L$  due to the rapid decrease of the current through  $L_{sL}$ , which induces a negative voltage fluctuation on  $V_{gsH}$ . In Stage 3, there are two factors impact the crosstalk, on the one hand, with the decrease of the reverse recovery current, the induced voltage over  $L_{sL}$  turns negative and induces a positive voltage fluctuation on  $V_{gsL}$ . On the other hand, the displacement current flows through  $C_{gdL}$  and is then shunted by  $C_{gsL}$  and the driver loop, which can also induce a positive pulse on  $V_{gsL}$ . The voltage on  $R_{gL}$  and  $L_{gL}$  achieves equilibrium with the sum of  $V_{gsL}$  and the induced voltage of  $L_{sL}$ , which satisfies equation (39). (39) illustrates that the fluctuation of  $V_{gsL}$  is positively correlated with the value and the slew rate of  $i_{dL}$ , where the value of  $i_{dL}$  reflects the rising rate of  $V_{dsL}$ .



**FIGURE 22.** Analytical turn-on crosstalk waveform of  $V_{gsL}$  showing the effect of (a)  $Q_H$  driver resistance. (b)  $Q_H$  source inductance. (c)  $Q_H$  gate-source capacitance. (d)  $Q_H$  gate-drain capacitance.

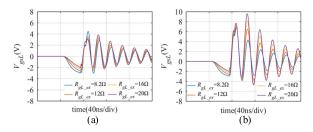
Fig. 22 presents the analytical turn-on waveforms of  $V_{gsL}$  with varied elements that have obvious effects on the voltage or current switching rate. It is discovered that the elements related to the voltage switching rate, such as  $R_{gH}$  and  $C_{gdH}$ , have much more effects on the  $V_{gsL}$  positive crosstalk voltage, and the elements related to the current switching rate, such as  $L_{sH}$  and  $C_{gsH}$ , have relatively fewer effects on the crosstalk voltage, as they can only indirectly affect the current slew rate by changing the initial rate of the reverse recovery current at t3.

For  $C_{gdL}$  and  $L_{sL}$ , their increase will aggravate the effects of the two factors and intensify the positive fluctuation of  $V_{gsL}$ . Fig. 23 presents the analytical waveforms of  $V_{gsL}$ with the effects of varying  $C_{gdL}$  and  $L_{sL}$ . Combined with the earlier analysis, larger  $L_{sL}$  causes greater negative voltage fluctuations of  $V_{gsL}$  in Stage 2, and the crosstalk phenomenon is more serious overall.

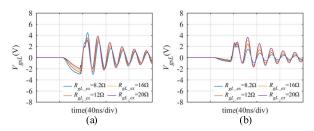


**FIGURE 23.** Analytical turn-on crosstalk waveform of  $V_{gsL}$  showing the effect of (a)  $Q_L$  gate-drain capacitance. (b)  $Q_L$  source inductance.

However, the impedance of the driver loop of  $Q_L$  itself has the opposite effects on these two factors. For the displacement current of  $C_{gdL}$ , the driver loop and  $C_{gsL}$  are equivalent to be in parallel. The increase in the impedance of the driver loop will promote a positive fluctuation of  $V_{gsL}$ . For the induced voltage of  $L_{sL}$ , the driver loop and  $C_{gsL}$  are equivalent to be in series. So, the increase in the impedance of the driver loop suppresses the positive fluctuation of  $V_{gsL}$ . According to (39), a larger  $R_{gL}$  increases the voltage formed by the displacement current of  $C_{gdL}$  flowing through the driver loop, which is shown in the right-hand side of the equation. Nevertheless, a larger  $R_{gL}$  also increases the damping coefficient  $\xi_{L3}$  of the driver loop in (41), which slows down the rising rate of  $V_{gsL}$ . Given the above reasoning, the influence of the driver loop impedance on the amplitude of the  $V_{gsL}$  is inconclusive.



**FIGURE 24.** Analytical turn-on crosstalk waveform of  $V_{gsL}$  showing the effect of  $R_{qL}$  with (a)  $C_{qdL_{ex}} = 0$  pF. (b)  $C_{qdL_{ex}} = 8$  pF.



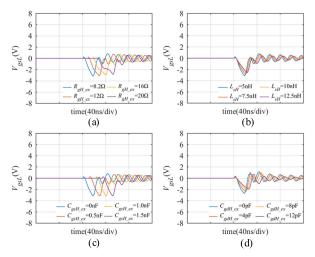
**FIGURE 25.** Analytical turn-on crosstalk waveform of  $V_{gsL}$  showing the effect of  $R_{qL}$  with (a)  $L_{sL} = 5$ nH. (b)  $L_{sL} = 2$ nH.

Fig. 24 presents the analytical waveforms of  $V_{gsL}$  with the effects of varied  $R_{gL}$  when external  $C_{gdL\_ex}$  is paralleled or not. It reveals that with an increase in  $R_{gL}$ , the positive fluctuation of  $V_{gsL}$  will decrease if no external  $C_{gdL\_ex}$  is paralleled, and will increase if  $C_{gdL\_ex} = 8$  pF. Fig. 25 presents the analytical waveforms of  $V_{gsL}$  with the effects of varied  $R_{gL}$ , whether  $L_{sL}$  is reduced or not. Fig. 25 reveals that with an increase in  $R_{gL}$ , the positive fluctuation of  $V_{gsL}$  will decrease if  $L_{sL}$  is reduced or not. Fig. 25 reveals that with an increase in  $R_{gL}$ , the positive fluctuation of  $V_{gsL}$  will decrease if  $L_{sL}$  is 25 reveals that with an increase in  $R_{gL}$ , the positive fluctuation of  $V_{gsL}$  will decrease if  $L_{sL}$  is 25 reveals that with an increase in  $R_{gL}$ , the positive fluctuation of  $V_{gsL}$  will decrease if  $L_{sL}$  is 25 reveals that with an increase in  $R_{gL}$ , the positive fluctuation of  $V_{gsL}$  will decrease if  $L_{sL}$  is 25 reveals that with an increase in  $R_{gL}$ , the positive fluctuation of  $V_{gsL}$  will decrease if  $L_{sL}$  is 25 reveals that with an increase in  $R_{gL}$ , the positive fluctuation of  $V_{gsL}$  will decrease if  $L_{sL}$  is 25 reveals that with an increase in  $R_{gL}$  will decrease if  $L_{sL}$  is 25 reveals that with an increase in  $R_{gL}$  will decrease if  $L_{sL}$  is 25 reveals that with an increase in  $R_{gL}$  will decrease in  $R_{gL}$  will decreas

It can be concluded, that the positive fluctuations of  $V_{gsL}$ essentially depend on the balance of the displacement current of  $C_{gdL}$  and the induced voltage on  $L_{sL}$  acting on the driver loop. The variation of the impedance of the driver loop will change the balance point. Besides, it is noteworthy that the nonlinear characteristics of parasitic capacitances aggravate the crosstalk due to  $\xi_{L3}$  decreases and  $\omega_{n \ L3}$  increases.

In Stage 4, the driver loop is affected by the same factors as in Stage 3. The oscillations of  $V_{dsL}$  cause the currents through  $C_{gdL}$  and  $L_{sL}$  to oscillate, which leads to the oscillations of  $V_{gsL}$ .

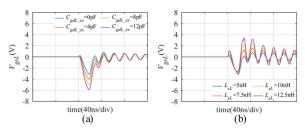
During the turn-off process, the voltage and current switching rates affect the negative fluctuation amplitude of  $V_{gsL}$ . Fig. 26 shows the analytical turn-off crosstalk waveforms of  $V_{gsL}$  with varied elements that have obvious effects on the voltage or current switching rate. Similar to the turn-on process, the elements related to the voltage switching rate have much more effects on the negative amplitude of  $V_{gsL}$ .



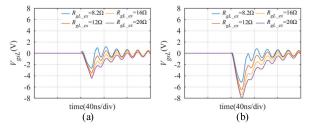
**FIGURE 26.** Analytical turn-off crosstalk waveform of  $V_{gsL}$  showing the effect of (a)  $Q_H$  driver resistance. (b)  $Q_H$  source inductance. (c)  $Q_H$  gate-drain capacitance. (d)  $Q_H$  gate-drain capacitance.

In the turn-off process, the voltage and current switching sequence is reversed. Therefore, the response of  $Q_L$  is different from that in the turn-on process. In Stage 6, the voltage starts to switch first,  $V_{dsL}$  decreases and the displacement current of  $C_{gdL}$  induces negative fluctuation in  $V_{gsL}$ . While there is no initial current when  $V_{dsL}$  decreases and  $i_{dL}$  starts to increase reversely from zero. It still causes negative induced voltage over  $L_{sL}$ , which could induce a positive fluctuation trend in  $V_{gsL}$ . These two factors produce opposite effects on the response of  $V_{gsL}$ . Thus, the increase in  $C_{gdL}$  promotes the negative fluctuation of  $V_{gsL}$ , while the increase in  $L_{sL}$ suppresses the fluctuation as shown in Fig. 27.

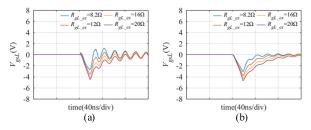
Therefore, the impedance of the driver loop of  $Q_L$  has the same effect on the two factors in Stage 6, which is different from the turn-on process. Fig.28 presents the analytical waveforms of  $V_{gsL}$  with the effects of varied  $R_{gL}$  when external  $C_{gdL\_ex}$  is paralleled or not. Fig. 29 shows the analytical waveforms of  $V_{gsL}$  with the effects of varied  $R_{gL}$  when  $L_{sL}$ 



**FIGURE 27.** Analytical turn-off crosstalk waveform of  $V_{gsL}$  showing the effect of (a)  $Q_L$  gate-drain capacitance. (b)  $Q_L$  source inductance.



**FIGURE 28.** Analytical turn-off crosstalk waveform of  $V_{gsL}$  showing the effect of  $R_{qL}$  with (a)  $C_{qdL_{ex}} = 0$  pF. (b)  $C_{qdL_{ex}} = 8$  pF.



**FIGURE 29.** Analytical turn-off crosstalk waveform of  $V_{gsL}$  showing the effect of  $R_{qL}$  with (a)  $L_{sL} = 5$ nH. (b)  $L_{sL} = 2$ nH.

is reduced or not. Combining Fig. 28 with Fig. 29, it can be deduced that the increase in  $R_{gL}$  aggravates the negative fluctuation amplitude of  $V_{gsL}$  no matter how  $C_{gdL}$  and  $L_{sL}$  change.

In Stage 7,  $D_{bL}$  starts to conduct, the displacement current of  $C_{gdL}$  drops to zero and the reverse rising rate of  $i_{dL}$ increases, which causes a larger negative induced voltage on  $L_{sL}$ . These factors induce a positive fluctuation in  $V_{gsL}$ based on Stage 6. If  $L_{sL}$  is large, a positive crosstalk voltage may appear, as the comparison shown in Fig. 29, while  $R_{gL}$ helps to suppress the upward voltage fluctuation.

#### **IV. EXPERIMENTAL VERIFICATION**

The bridge-leg test circuit has been designed for the experimental evaluation of the proposed analytical model. Fig. 30 shows the photograph of the test platform. Two SiC MOSFETs form the bridge-leg structure, and a 20  $\mu$ H ferrite-core inductor is connected in parallel with the lower SiC MOSFET as the load inductor. The test circuit is fed by 600 V DC supply voltage, multiple groups of capacitances are connected in parallel with the input end to ensure the stability of the support DC voltage. The DC loop was designed to minimize the parasitic inductances. The external pins of the devices and the connecting leads of the power loop is

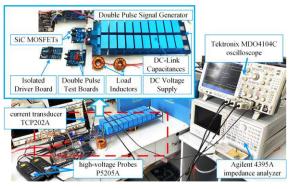


FIGURE 30. Photograph of the double pulse test platform.

measured by an Agilent 4395A impedance analyzer, the internal pins of the devices and the printed circuit board PCB layout is implemented by finite-element analysis of ANSYS Q3D [35]. The measurement and extraction results are listed in TABLE 2.

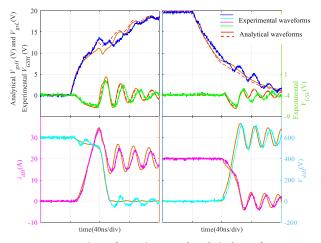
A high speed high current gate driver IXDN409 is selected to provide sufficient gate driver capability. The gate driver resistances of upper and lower transistors are chosen as  $8.2\Omega$ , which could maintain an appropriate switching speed to present the different switching stages of the bridge-leg. Since there is no any crosstalk suppression method in the experiment, in order to prevent spurious trigger of  $Q_L$ , the negative driver voltage level of the lower SiC MOSFET is set at -4V, this negative voltage bias does not have a significant effect on the responses of crosstalk voltage.

The measurement system should have enough bandwidth to acquire trustworthy experimental results. Power loop switching voltage is measured by high-voltage differential probes: P5205A (1300 V/100 MHz). The gate driver voltage of  $Q_L$  is measured by voltage probes: TPP0101 (300 V/100 MHz). The drain current is measured by a current transducer: TCP202A (30A peak/50MHz). These switching waveforms were carried out with the Tektronix MDO4104C, 1GHz oscilloscope. It should be noted that the delay time between the current probe and the voltage probe is 11.5ns displayed on the oscilloscope, which should set delay compensation to eliminate the deviation.

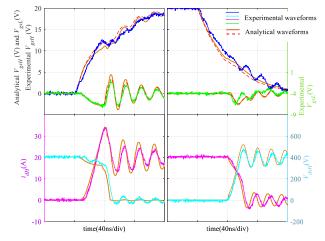
Double pulse test results are compared with the analytical results shown as follows. Particularly, in order to facilitate the comparison of crosstalk fluctuation amplitude, the -4V of the experimental  $V_{gsL}$  coordinates and the 0V of the analytical  $V_{gsL}$  coordinates are set as the same reference position. Fig. 31 shows the turn-on and turn off switch waveforms.

To verify the model under different voltages, double pulse test results when DC voltage is 400V while other test conditions remain unchanged are shown in Fig. 32.

To verify the model under different load currents, moving the double pulse trigger signal position to change the load current, double pulse test results when the load current is 10A while other test conditions are not changed are shown in Fig. 33.



**FIGURE 31.** Comparison of experiment and analytical waveforms @600V/20A. Left: turn-on waveforms, right: turn-off waveforms:  $V_{gsH}$ and  $V_{qsL}$  (5V/div),  $V_{dsH}$  (200V/div),  $I_{dH}$  (10A/div), and t (40ns/div).

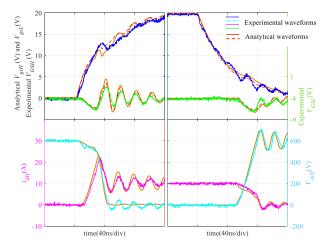


**FIGURE 32.** Comparison of experiment and analytical waveforms @400V/20A. Left: turn-on waveforms, right: turn-off waveforms: V<sub>gsH</sub> and V<sub>asL</sub> (5V/div), V<sub>dsH</sub> (200V/div), I<sub>dH</sub> (10A/div), and t (40ns/div).

It can be seen from Figs. 31 to 33 the analytical results match test results very well. The proposed analytical model can correctly represent the switching transient waveforms in terms of the voltage slope, the current slope, reverse recovery current, oscillation of the power loop, and the crosstalk of the driver loop.

In practice, the voltage measurement probes can only be connected between the external terminals, the internal voltages of parasitic elements are included in the measurement values. The gate-source voltages between the external package nodes are expressed by  $V_{GSH}$  and  $V_{GSL}$ , their relationships with the internal voltages are given by equations (78) and (79). The analytical waveforms of  $V_{GSH}$  and  $V_{GSL}$  are depicted in red dashed curves in Figs. 31 to 33.

$$V_{GSH} = V_{gsH} + R_{gH\_in}i_{gH} + \left(L_{gH\_in} + L_{sH\_in}\right)\frac{di_{gH}}{dt} + L_{sH\_in}\frac{di_{dH}}{dt}$$
(78)



**FIGURE 33.** Comparison of experiment and analytical waveforms @600V/10A. Left: turn-on waveforms, right: turn-off waveforms:  $V_{gsH}$  and  $V_{qsL}$  (5V/div),  $V_{dsH}$  (200V/div),  $I_{dH}$  (10A/div), and t (40ns/div).

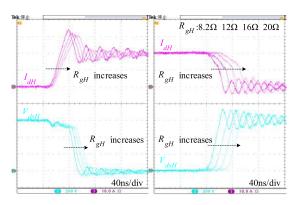
$$V_{GSL} = V_{gsL} + R_{gL\_in}i_{gL} + \left(L_{gL\_in} + L_{sL\_in}\right)\frac{di_{gL}}{dt} + L_{sL\_in}\frac{di_{dL}}{dt}$$
(79)

Thus, for the driver loop of  $Q_H$ , the measured value of the gate-source voltage is larger than the calculated values in the turn-on process, while smaller in the turn-off process. Similarly, since the gate and source internal parasitic elements of  $Q_L$  share part of the gate-source voltage, the measured value of gate-source voltage is smaller than the calculated value during the turn-on and turn-off process. The crosstalk phenomena by experimental measurements can therefore be compared with the analytical waveforms of  $V_{GSL}$ and  $V_{gsL}$  in Figs. 31 to 33.

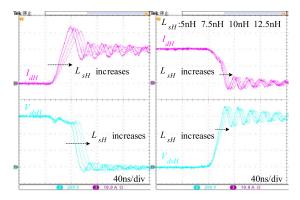
In the power loop, the measured  $V_{dsH}$  includes the induced voltages of  $L_{dH\_in}$  and  $L_{sH\_in}$ , this internal parasitic inductance forms an LC circuit with the drain-source capacitances, which causes the measured  $V_{dsH}$  has fluctuations with the voltage drop in Stage 2 and the more obvious oscillation in Stage 4.

The oscillation frequency and oscillation attenuation amplitude of the voltage and current provided by the experimental results are slightly larger than those of the proposed analytical model. During the voltage switching process (Stage 3 and Stage 6), there is a deviation between the calculation results and the actual response curve of drain current. It is because of the difference of the nonlinear capacitances model with the actual capacitances value and the measurement deviation of parasitic inductances of the power loop. These deviations are inevitable but the variation trend can still be correctly inferred.

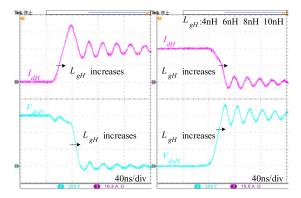
Next, a series of experimental results be provided to verify the trends of the switching speed, the duration and amplitude of power loop oscillation, and the magnitude of the crosstalk voltage under the influence of critical parameters. The adjustment rules of each element are the same as in section III.



**FIGURE 34.** Experimental switching waveform of  $i_{dH}$  and  $V_{dsH}$  showing the effect of  $R_{qH}$ . Left: turn-on, right: turn-off.



**FIGURE 35.** Experimental switching waveform of  $i_{dH}$  and  $V_{dsH}$  showing the effect of  $L_{sH}$ . Left: turn-on, right: turn-off.

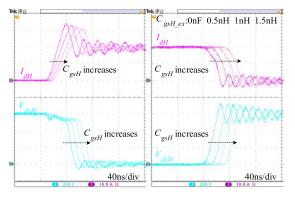


**FIGURE 36.** Experimental switching waveform of  $i_{dH}$  and  $V_{dsH}$  showing the effect of  $L_{qH}$ . Left: turn-on, right: turn-off.

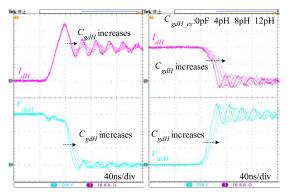
The switching waveforms with the varied elements are superimposed on one capture window of the oscilloscope.

Figs. 34-41 display the experimental switching waveforms of  $i_{dH}$  and  $V_{dsH}$  under the influence of the elements of the driver loop of  $Q_H$  and the power loop respectively.

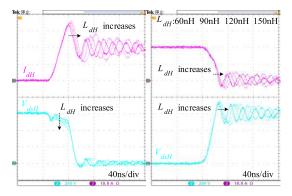
Fig. 34 and Fig. 35 show the experimental waveforms of  $i_{dH}$  and  $V_{dsH}$  with varying  $R_{gH}$  and  $L_{sH}$  respectively, both of them have influences on the current and voltage switching rate. The current slew rate decreases in the turn-on and turn-off processes with the increase in  $R_{gH}$ .  $L_{sH}$  has the same obvious influence on the current slew rate in the



**FIGURE 37.** Experimental switching waveform of  $i_{dH}$  and  $V_{dsH}$  showing the effect of  $C_{qsH}$ . Left: turn-on, right: turn-off.



**FIGURE 38.** Experimental switching waveform of  $i_{dH}$  and  $V_{dsH}$  showing the effect of  $C_{qdH}$ . Left: turn-on, right: turn-off.

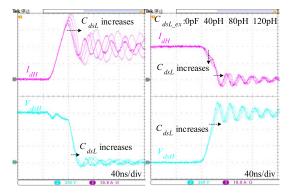


**FIGURE 39.** Experimental switching waveform of  $i_{dH}$  and  $V_{dsH}$  showing the effect of  $L_{dH}$ . Left: turn-on, right: turn-off.

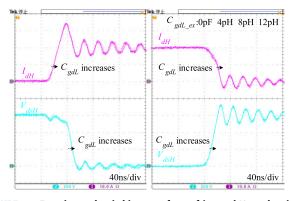
turn-on process, while its influence is smaller in the turn-off process, which shows the same characteristics as Fig. 12 and Fig. 13 predicted. The change range of the voltage slew rates with varied  $L_{sH}$  is relatively small, which confirms the explanation in section III.

As shown in Fig. 36, The turn-on and turn-off experimental switching waveforms with different  $L_{gH}$  are the same as the analytical model prediction, which shows little change in the switching rate.

The experimental current and voltage switching waveforms under the influence of  $C_{gsH}$  are shown in Fig. 37, the current slew rate decreases significantly with the increase



**FIGURE 40.** Experimental switching waveform of  $i_{dH}$  and  $V_{dsH}$  showing the effect of  $C_{dsL}$ . Left: turn-on, right: turn-off.

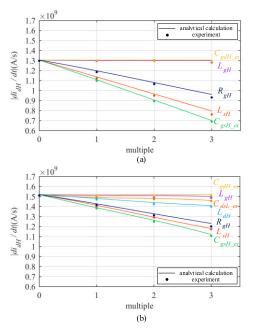


**FIGURE 41.** Experimental switching waveform of  $i_{dH}$  and  $V_{dsH}$  showing the effect of  $C_{gdL}$ . Left: turn-on, right: turn-off.

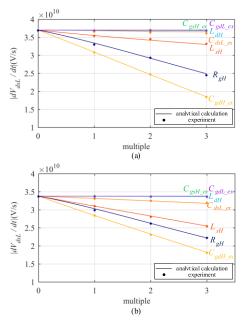
in  $C_{gsH}$  during both the turn-on and turn-off process, while the voltage slew rates are barely changed. Fig. 38 displays the experimental switching waveforms under the influence of  $C_{gdH}$ , which shows the voltage slew rate was reduced significantly with the increase of  $C_{gdH}$ , while the current slew rate has almost no change. These trends are consistent with the analytical model prediction for the impacts of critical elements in the different stages.

Same as the model setting rules, all the power loop parasitic inductances are denoted by  $L_{dH}$ . The experimental waveforms under the influence of the power loop parasitic inductances are depicted in Fig. 39, which illustrate that the increase in  $L_{dH}$  aggravates the amplitude of the reverse recovery current overshoot and the amplitude of the oscillation, but they have no significant effect on the current and voltage switching rate during the turn-on process, and it slightly restrains the current slew rate during the turn-off process, these phenomena confirm the analysis of section III.

Fig. 40 and Fig. 41 show the experimental waveforms under the influence of  $C_{dsL}$  and  $C_{gdL}$ . It can be seen that only  $C_{dsL}$  causes obvious changes in the current and voltage oscillation, which are consistent with the analytical results. Compare Fig. 39 and Fig 40, the increase in  $C_{dsL}$  has the same effect on current and voltage as  $L_{dH}$  during the turn-on process. However, in the turn-off process, the increase in  $C_{dsL}$ reduces the voltage switching rate and causes a greater current



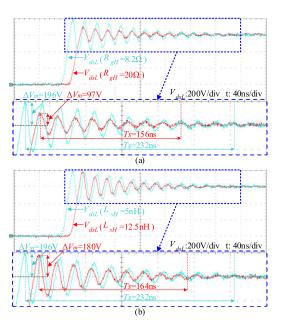
**FIGURE 42.** Variation trend of  $i_{dH}$  switching rate with different elements effect. (a) turn-on. (b) turn-off.



**FIGURE 43.** Variation trend of  $V_{dsH}$  switching rate with different elements effect. (a) turn-on. (b) turn-off.

drop in Stage 6. While after the voltage switching process,  $C_{dsL}$  is short-circuited and it does not affect the oscillating characteristics.

Summarizing the influence of all these key elements on the current and voltage switching rate, the comparisons of the influence trends with different elements obtained from experiments and analytical calculations are illustrated in Fig. 42 and Fig. 43 respectively. Fig. 42 illustrates that the elements that have obvious effects on the current switching



**FIGURE 44.** The turn-on oscillation experimental waveforms of  $V_{dsL}$  showing the effect of  $R_{qH}$  and  $L_{sH}$ .

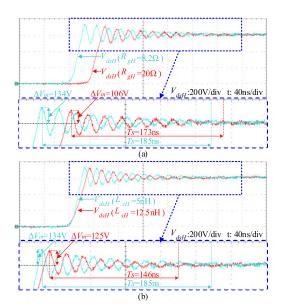
rate are  $C_{gsH}$ ,  $L_{sH}$ , and  $R_{gH}$  in sequence, the parasitic inductances of the power loop and  $C_{dsL}$  also have influences on the current slew rate in the turn-off process. Fig. 43 illustrates that the elements that have obvious effects on the voltage switching rate are  $C_{gdH}$ ,  $R_{gH}$ , and  $L_{sH}$  in sequence. Overall, the current switching rate in the turn-off process is generally faster than the turn-on process under the same conditions, while the voltage switching rate is just the opposite. Moreover, combining these two figures, it is shown that the effects of the driver loop elements on the variation ranges of current and voltage switching rate in the turn-on process are more obvious than those in the turn-off process.

With the transition of the stages, the parasitic inductances and the equivalent parasitic capacitances in the power loop cause oscillations, the increase in these elements aggravates the amplitude of the oscillation, which has been verified in the previous experimental waveforms as shown in Fig. 39 and Fig. 40.

Fig. 44 compares the turn-on experimental oscillation waveforms of  $V_{dsL}$  with  $R_{gH}$  and  $L_{sH}$  increases, and Fig. 45 compares the turn-off experimental oscillation waveforms of  $V_{dsH}$  with  $R_{gH}$  and  $L_{sH}$  increased.

In Fig. 44 and Fig. 45, the amplitude of the maximum peak value of  $V_{dsL}$  and  $V_{dsH}$  exceeding  $V_{DD}$  is marked as  $\Delta V_m$ , the duration from the maximum peak value of  $V_{dsL}$  and  $V_{dsH}$  to the oscillation amplitude within 5%  $V_{DD}$  is  $T_s$ . Since the increase in  $R_{gH}$  and  $L_{sH}$  slows down the initial rate of the voltage, introduce  $\lambda = T_s / \Delta V_m$  as the oscillation duration coefficient, the larger  $\lambda$  indicates the longer relative duration of the oscillation. The results are listed in Table 3.

As shown in Table 3, in the turn-on process, although the increase in  $R_{gH}$  can reduce the maximum peak value of  $V_{dsL}$  increases from 196V to 97V and the oscillation

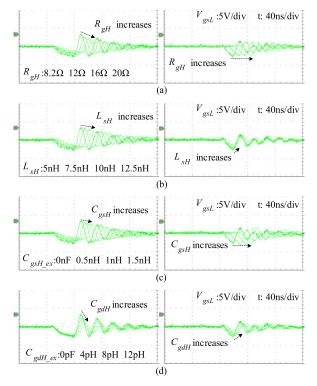


**FIGURE 45.** The turn-off oscillation experimental waveforms of  $V_{dsL}$  showing the effect of  $R_{qH}$  and  $L_{sH}$ .

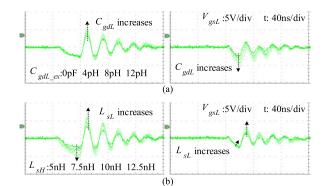
TABLE 3. Turn-on  $V_{dsL}$  and turn-off  $V_{dsH}$  oscillation characteristics with  $R_{gH}$  and  $L_{sH}$  regulated.

	Test cond	Initial state	R <sub>gH</sub> increased	L <sub>sH</sub> increased	
	Adjusted components	$R_{gH}(\Omega)$	8.2	20	8.2
		$L_{sH}$ (nH)	5	5	12.5
Turn on	Parameters	$R_{gH\_eql}\left(\Omega ight)$	0.432	0.179	2.126
		ξ	0.031	0.023	0.084
		$\Delta V_m(\mathbf{V})$	196	97	180
	$V_{dsL}$ Response	overshoot	32.7%	16.2%	30%
		$T_s$ (ns)	232	156	164
		$\lambda$ (ns/V)	1.18	1.61	0.91
Turn off	Parameters	$R_{gH\_eq2}\left(\Omega ight)$	0.431	0.181	2.215
		ξ	0.028	0.023	0.062
	V <sub>dsH</sub> Response	$\Delta V_m(\mathbf{V})$	134	106	125
		overshoot	22.3%	17.6%	21%
		$T_s$ (ns)	185	173	146
		$\lambda$ (ns/V)	1.38	1.63	1.17

duration drops from 219ns to 166ns, the damping coefficient  $\xi$  decreases from 0.031 to 0.023 and  $\lambda$  increases from 1.18 to 1.61, which indicates that the relative duration of the oscillation is prolonged with the increase in  $R_{gH}$ . The increase in  $L_{sH}$  reduces the maximum peak value of  $V_{dsL}$  and also causes  $\xi$  increase from 0.031 to 0.084,  $\lambda$  decreases to 0.91. Thus, the relative duration of the oscillation is shortened significantly. Similarly, in the turn-off process, the increase in  $R_{gH}$  prolongs the relative duration of the  $V_{dsH}$  oscillation,  $\lambda$  increases from 1.38 to 1.63; the increase in  $L_{sH}$  shortens the relative duration of the  $V_{dsH}$  oscillation with  $\lambda$  decreases



**FIGURE 46.** Experimental crosstalk waveform of  $V_{gsL}$  showing the effect of (a)  $Q_H$  driver resistance. (b)  $Q_H$  source inductance. (c)  $Q_H$  gate-source capacitance. (d)  $Q_H$  gate-drain capacitance. Left: turn-on, right: turn-off.

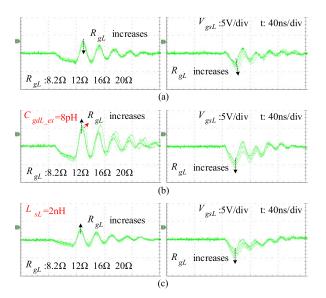


**FIGURE 47.** Experimental crosstalk waveform of  $V_{gsL}$  showing the effect of (a)  $Q_L$  gate-drain capacitance. (b)  $Q_L$  source inductance. Left: turn-on, right: turn-off.

to 1.17. This series of experiment results verify the analytical model prediction.

Fig. 46 displays the experimental waveforms of  $V_{gsL}$  under the influence of  $R_{gH}$ ,  $L_{sH}$ ,  $C_{gsH}$ , and  $C_{gdH}$ . Obviously, the increase in  $R_{gH}$  and  $C_{gdH}$  restrain the amplitude of the crosstalk voltage, while  $L_{sH}$  and  $C_{gsH}$  have relatively small impacts on the crosstalk voltage. These results are consistent with the analytical model shown in Fig. 22.

The experimental waveforms of  $V_{gsL}$  under the influence of  $C_{gdL}$  and  $L_{sL}$  are depicted in Fig. 47. In the turn-on process, both of them aggravate the amplitude of the crosstalk voltage. While in the turn-off process, it can be seen that the increase in  $C_{gdL}$  intensifies the negative crosstalk voltage,



**FIGURE 48.** Experimental crosstalk waveform of  $V_{gsL}$  showing the effect of  $Q_L$  gate resistance increase with (a)  $C_{gdL\_ex} = 0$  pF,  $L_{sL} = 5$  nH. (b)  $C_{gdL\_ex} = 8$  pF,  $L_{sL} = 5$  nH. (c)  $C_{gdL\_ex} = 0$  pF,  $L_{sL} = 2$  nH. Left: turn-on, right: turn-off.

the increase in  $L_{sL}$  restrains the negative crosstalk voltage, which agrees with the analytical switching waveforms shown in Fig. 23 and Fig. 27.

The experimental crosstalk waveforms under the influence of  $R_{gL}$  are depicted in Fig. 48. The crosstalk voltage waveforms with the default parasitic parameter settings are shown in Fig. 48(a), the increase in  $R_{gL}$  restrains the positive fluctuation of  $V_{gsL}$ . Fig. 48(b) shows the experimental waveforms of  $V_{gsL}$  with external  $C_{gdL\_ex}$  paralleled, instead, the increase in  $R_{gL}$  aggravates the amplitude of the crosstalk voltage. It should be noticed that when  $R_{gL}$  increases to  $12\Omega$ ,  $Q_L$  has a spurious turn-on phenomenon, the amplitude and the oscillation frequency of the crosstalk voltage are changed. Fig. 48(c) shows the experimental waveforms of  $V_{gsL}$  with  $L_{sL}$  decreases to 2nH, it is discovered that the crosstalk voltage is significantly reduced, but the increase in  $R_{gL}$  aggravates the amplitude of the crosstalk voltage. Fig. 48 also illustrates that the increase in  $R_{gL}$  aggravates the negative amplitude of  $V_{gsL}$  no matter how  $C_{gdL}$  and  $L_{sL}$ change in the turn-off process. All these results concluded from the combined comparison of the three experiments are consistent with the analytical model prediction.

#### **V. CONCLUSION**

A detailed and accurate circuit-level analytical model for a bridge-leg configuration based on SiC MOSFETs is proposed in this paper. Clear piecewise linear turn-on and turn-off switching processes are presented in detail and the critical parameters that have dominating effects on the variable switching responses in each switching stage are identified flexibly and independently. The influence mechanisms of these staged critical parameters on the main switching variables are analyzed in detail. Based on this model, the impacts of the critical parameters on the switching speed, the knock-on effects on the oscillation of the power loop, and the crosstalk of the driver loop are further studied, which are the important features of a bridge-leg. The influence degrees and trends of these staged critical parameters on the switching processes are derived and compared. The switching waveforms in a bridge-leg, which consists of 1200 V/ 20A SiC MOSFETs are measured and compared with the analytical results. The proposed model shows are successfully verified by experimental measurements and the influences of the critical parameters on the switching performance are successfully verified. The proposed model can be employed in the design and development of the power converters based on SiC MOSFETs bridge configurations to evaluate their operational performances, stability, and reliability for high power and/or high frequency applications.

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