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# Joint Torque Closed-Loop Estimation Using NARX Neural Network Based on sEMG Signals

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**ABSTRACT** Joint torque estimation is of great significance for the research and clinical application of intelligent rehabilitation technology. This paper proposes a closed-loop model for joint torque estimation based on surface electromyography (sEMG). Combined with the physiological characteristics of muscle activation, a nonlinear autoregressive with exogenous inputs (NARX) neural network model for joint torque estimation based on sEMG signals is established. In order to solve the drift phenomenon of torque estimation, a state-space framework is constructed by regarding NARX neural network based torque estimation model as state model and developing a measurement model by the easily measured joint angle signals. With the built state-space model, the extended Kalman filter (EKF) is used to realize the closed-loop filtering of the estimated torque. In order to test the accuracy of the proposed closed-loop joint torque estimation, 8 volunteers were recruited to perform elbow joint isotonic motion experiments under four kinds of loads. The test results show that the average normalized root mean square error (NRMSE) between the estimated values of closed-loop model and measurement values of all subjects under load-dependent, multi-load and load-independent tests are  $0.1080 \pm 0.0411$ ,  $0.1326 \pm 0.0494$  and  $0.1674 \pm 0.0661$  respectively, which is significant better than the results of the open-loop model ( $0.2694 \pm 0.1584$  ( $p < 10^{-6}$ ),  $0.2499 \pm 0.1326$  ( $p < 10^{-6}$ ) and  $0.3435 \pm 0.2061$  ( $p < 10^{-4}$ )). The presented closed-loop model combines offline modeling and online filtering to achieve online estimation of joint torque, which ameliorates the problem that the estimated torque in the open-loop model deviates greatly from the actual values and improves the accuracy of joint torque estimation.

**INDEX TERMS** sEMG, neural network, NARX, EKF.

## I. INTRODUCTION

In recent years, the prevalence of paralysis caused by spinal cord injury and stroke have been increasing significantly. According to the heart disease and stroke statistics report from the American Heart Association, the stroke prevalence of adult in the United States is 2.9%, and it is estimated that by 2030, more than 3.4 million US adults over the age of 18 will have had a stroke, a 20.5% increase in prevalence from 2012 [1]. Stroke and spinal cord injury can easily lead to tissue damage, and different degrees of tissue damage at different positions can cause different degrees of sports injuries, so most of these patients have varying degrees of decline in mobility. For such a large group of

patients with motor dysfunction, it is very meaningful to help them recover and reconstruct their limb motor function. Human joint torque is one of the important parameters for quantitative analysis of human motion function, which is of great significance for realizing precise control of exoskeleton robots, quantitative evaluation of rehabilitation training [2]. The direct torque measurement system requires bulky equipment which requires complex mechanical structures and is limited by the environment. Therefore, estimation by other measurable parameters to achieve indirect measurement of joint torque has been widely studied. However, most of the existing researches on joint torque estimation are limited to isometric motion, which is a kind of static motion [3]. In fact, the torque estimation under motion state has much practical significance, for example, in the realization of motor control of rehabilitation robot.

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Electromyography (EMG) signal represents the sum of subcutaneous motor action potentials generated by muscle contraction, which can represent neuromuscular activity [4]. It is an alternative to reflect the patient's voluntary effort. The training involving the patient's voluntary effort can improve the therapeutic effect [5]. The surface electromyography (sEMG) is a non-invasive EMG signal collected by surface electrodes, which has the advantage of being more accessible than electroencephalography (EEG) and less likely to impede the user's normal activities. The EMG signals can not only be used for motor pattern recognition [6], but also for the estimation of motor signals such as joint torque and angle. Research on wearable EMG devices have shown that between 150-300 ms of window length is required to avoid significant delays for the user. The appearance of the EMG signals is ahead of the actual joint motion [7], which is called electromechanical delay between the EMG signals and the actual joint motion. This feature is very important for the implementation of real-time control. So, the sEMG signals are usually used as intelligent human-machine interface to estimate torque or angle for the control of rehabilitation robot [8].

The joint torque estimation model based on EMG signals mainly has two model structures, namely, the mechanism model based on neurophysiology, and the data-driven black-box model. The mechanism model uses EMG signals as the control signal, builds a model according to the physiological structure of the human body, and outputs joint torque or joint motion [9]. Among these model, the Hill-type muscle model is the most commonly used one. The mechanism model driven by EMG signals usually consists of muscle activation model, Hill-type muscle contraction dynamics and joint dynamics [10], [11]. Meyer *et al.* developed a novel EMG-driven modeling method based on the Hill-type model that automatically adjusts surrogate representations of the patient's musculoskeletal geometry, which improved the accuracy of walking joint torque estimation compared to results from previous EMG-driven studies [12]. The model structure based on the Hill-type mechanism model has shown its excellence when it comes to complex movements involving multiple joints and is a hot topic of research in the field of biomechanics. However, the model is very complex and involves a large number of unknown physiological parameters, making the analysis and application of the model very difficult.

In contrast to the development of complex physiological models, in the data-driven black-box model approach, functional relationships are established without the need for explicit equations to model underlying neural activation and joint motion. Thus, in the black-box model, all intermediate functional relationships between the observed experimental variables are not explicitly modeled. However, they are contained within a macroscopic transfer function. The NARX model is an effective method for solving nonlinear sequence problems that better combines the nonlinear spatiotemporal correlation structure of natural human movement with

muscle-driven control signals [13]. Dynamic recurrent neural networks based on the NARX model are widely used for joint angle estimation [14], decoding shoulder, elbow, and wrist movements [15], and prosthetic model control [16]. There are problems in the research of NARX model-based dynamic recurrent neural networks: firstly, the feature extraction of EMG signals by the existing models only considers the macroscopic characteristics of EMG signals, for instance, the amplitude characteristics such as mean absolute value, integrated EMG and root mean square, as well as waveform characteristics such as waveform length and zero crossing, without considering the microscopic physiological characteristics of muscle activation; secondly, the functional relationships obtained in specific conditions may not be applicable to the new conditions [17]. This is related to the fact that a single macroscopic nonlinear transfer function may not be sufficient to capture the complexity of the several intermediate nonlinear components that exist among the observables. EMG signals are typically non-stationary in real time [18], so the online application of the offline trained model may introduce estimation errors and even instability.

In this paper, considering the physiological characteristics of microscopic muscle activation, a second-order dynamic system was used to simulate the muscle activation dynamics, and then the muscle activation was used as the EMG signal feature as the input of the NARX neural network model. The NARX neural network simulated the process of muscle contraction dynamics and joint dynamics to generate the joint torque. Furthermore, in order to avoid the instability of the torque autoregressive signal in the NARX model, the torque signal was filtered to overcome the signal drift by forming a closed-loop model structure for joint torque estimation based on a nonlinear filtering algorithm with an easy-to-measure joint angle signal. Compared to the existing state of the art, the proposed method has the following advantages: (1) The physiological properties of muscle activation and the complex nonlinear mapping and learning capabilities of neural networks are combined to perform joint torque estimation based on sEMG signals; (2) We use easy-to-measure motion parameters to form a closed-loop model, filter the output torque of neural networks to improve the estimation accuracy of joint torque; (3) Only one pair of antagonistic muscle EMG signals are used to reduce the cost of EMG signal detection, which allows for online torque estimation of wearable devices.

## II. MATERIALS AND METHODS

### A. NARX NEURAL NETWORK TORQUE ESTIMATION MODEL BASED ON SEMG SIGNALS

#### 1) MUSCLE ACTIVATION DYNAMICS

The sEMG signal is the sum of the action potentials recruited to the muscle by surface electrodes and is used to reflect the level of muscle activation. The sEMG signal can be considered as the characterization of neuromotor control commands and is widely used to analyze musculoskeletal models. In order to reflect the microscopic physiological characteristics and reflect the relationship between EMG signal, neural

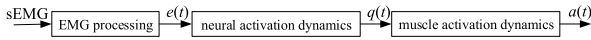


FIGURE 1. Muscle activation dynamics.

activation and muscle activation, this paper considered the physiological characteristics of microscopic muscle activation and established a muscle activation dynamics model to extract the EMG signal feature [19]. Muscle activation dynamics is mainly represented by the transformation process between EMG signal and muscle activation, as shown in Figure 1.

Raw sEMG signals was firstly high-pass filtered (4th order, cutoff frequency 20Hz) to eliminate low-frequency noise, then full-wave rectified and low-pass filtered (4th order, cutoff frequency 4Hz), and finally normalized to obtain the processed sEMG signal  $e(t)$ .

When a muscle fiber is activated by a single action potential, the muscle generated a twitch response. This response can be represented by a critically damped linear second-order differential system [20]. This type of response is the basis of different equations for determining the neural activation  $q(t)$  based on the sEMG signal  $e(t)$ :

$$q(t) = K_1 \frac{de^2(t)}{dt^2} + K_2 \frac{de(t)}{dt} + K_3 e(t) \quad (1)$$

where  $K_1, K_2$  and  $K_3$ , are the constants that define the dynamics of the second-order system.

Equation (1) is a continuous form of the second-order differential equation, however the data collected are discrete, resulting in discrete EMG signals time series. Thus, equation (1) is discretized to obtain a second-order discrete linear model [21], [22]:

$$q(t) = \alpha e(t - d) - \beta_1 q(t - 1) - \beta_2 q(t - 2) \quad (2)$$

where  $d$  is the electromechanical delay,  $\alpha$  the gain coefficient,  $\beta_1$  and  $\beta_2$  the recursive coefficients.

Equation (2) can be viewed as a recursive filter, where the current value of neural activation closely correlates with that of the approaching torque, consistent with the cumulative response of the muscular system. In order to ensure the stability of the second-order system, constraints are determined from the z transform of (2) as follows:

$$H(z) = \frac{q(z)}{e(z)} = \frac{\alpha}{1 + \beta_1 z^{-1} + \beta_2 z^{-2}} = \frac{\alpha}{(1 + \gamma_1 z^{-1})(1 + \gamma_2 z^{-1})}$$

$$\beta_1 = \gamma_1 + \gamma_2$$

$$\beta_2 = \gamma_1 \times \gamma_2 \quad (3)$$

Depending on the stability conditions of the system, the system parameters are constrained as shown in (4) [21], [22]:

$$|\gamma_1| < 1, |\gamma_2| < 1, \alpha - \beta_1 - \beta_2 = 1 \quad (4)$$

The value of  $\gamma_1$  and  $\gamma_2$  change the impulse response of the second-order filter. The recursive filter generates undamped response if both  $\gamma_1$  and  $\gamma_2$  are positive, and damped response if  $\gamma_1$  and  $\gamma_2$  are negative. The damped second-order response

lengthens the EMG signal processing time, while the electromechanical delay improves the synchronization between activation and force generation, ameliorating the problem of asynchrony between muscle activation and muscle force.

It has been shown that EMG signals are not necessarily linearly correlated with muscle force [23], and (5) was chosen to describe the nonlinear relationship between neural activation and muscle activation:

$$a(t) = \frac{e^{Aq(t)} - 1}{e^A - 1} \quad (5)$$

where  $a(t)$  is the muscle activation,  $q(t)$  the neural activation,  $A$  the non-linear shape factor, constrained to  $-3 < A < 0$ .

## 2) NARX NEURAL NETWORK MODEL

Nonlinear Auto-Regressive with eXogenous inputs (NARX) model is an effective method for solving nonlinear sequence problems that accommodates nonlinear discrete time processes and noisy models [24], [25]. NARX model predicts the current value of a system output by using a nonlinear function  $f$  with previous inputs and outputs, and there are two forms of prediction using the NARX model [26]. One is a NARX model based on the actual values of output:

$$\hat{y}_k = f(u_k, u_{k-1} \dots, u_{k-n_u}, y_{k-1}, y_{k-2}, \dots, y_{k-n_y}) \quad (6)$$

The other is a NARX model based on the estimated values of output:

$$\hat{y}_k = f(u_k, u_{k-1} \dots, u_{k-n_u}, \hat{y}_{k-1}, \hat{y}_{k-2}, \dots, \hat{y}_{k-n_y}), \quad (7)$$

where  $f(\cdot)$  is the nonlinear function between the input  $u_k$  and the estimated value  $\hat{y}_k$  of the actual output  $y_k$ ,  $k$  represents  $k$ th time step,  $n_u$  and  $n_y$  are the maximum lags for model input and output, respectively.

The multi-layer feedforward network has a highly nonlinear mapping capability, so in this paper it is used to implement the NARX model and form a dynamic recurrent neural network for joint torque estimation. In this paper, a single hidden layer feedforward neural network is adopted, with the  $tansig(\cdot)$  as the activation function at the hidden layer and a linear activation function at the output layer. The function relationship between input and output of the single hidden layer network is given as:

$$y = \sum_{j=1}^n (\delta_j tansig(\sum_{i=1}^m (\omega_{ij} u_i + \theta_i))) + \vartheta \quad (8)$$

where  $u_i$  and  $\theta_i$  represent the input and bias of the  $i$ th input unit respectively,  $\omega_{ij}$  represents the weight of the  $i$ th unit of the input layer to the  $j$ th unit of the hidden layer,  $\delta_j$  represents the weight of the  $j$ th unit of the hidden layer to the output unit,  $\vartheta$  represents the bias of the output layer,  $i = 1, 2, \dots, m$ ,  $j = 1, 2, \dots, n$ ,  $m$  is the number of input units, and  $n$  is the number of hidden layer units.

$tansig(\cdot)$  is the activation function of the hidden layer:

$$tansig(x) = tanh(x) = \frac{e^x - e^{-x}}{e^x + e^{-x}} \quad (9)$$

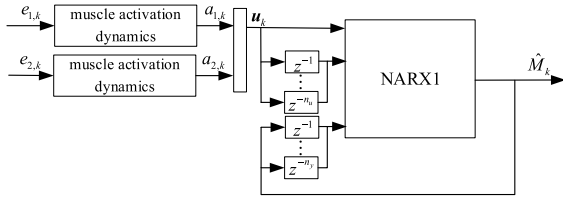


FIGURE 2. NARX neural network based torque estimation model.

To speed up the calculation, (9) is equated to

$$\text{tansig}(x) = \frac{2}{1 + e^{-2x}} - 1. \quad (10)$$

Substituting (6) and (7) into (8) respectively, we get two implementations of the NARX dynamic recurrent neural network as:

$$\hat{y}_k = \sum_{j=1}^n (\delta_j \text{tansig}(\sum_{i=1}^{n_u+1} (\omega_{ij} u_{k-i+1} + \theta_i) + \sum_{i=n_u+2}^{n_u+n_y+1} (\omega_{ij} y_{k-i+n_u+1} + \theta_i))) + \vartheta \quad (11)$$

$$\hat{y}_k = \sum_{j=1}^n (\delta_j \text{tansig}(\sum_{i=1}^{n_u+1} (\omega_{ij} u_{k-i+1} + \theta_i) + \sum_{i=n_u+2}^{n_u+n_y+1} (\omega_{ij} \hat{y}_{k-i+n_u+1} + \theta_i))) + \vartheta \quad (12)$$

Equation (11) is used to realize one-step ahead prediction in case of known actual output. Equation (12) is used when the actual output is unknown so as to realize estimation. The latter relies on autoregression of the estimated output, easily leading to some problems such as drift and instability of the estimated results. And its estimation accuracy is low.

### 3) NARX NEURAL NETWORK BASED TORQUE ESTIMATION MODEL

In this paper, a NARX neural network based torque estimation model was developed using sEMG signals from a pair of antagonist muscles (biceps brachii and triceps brachii) that control elbow joint motion, as shown in Figure 2. The  $e_{1,k}$  and  $e_{2,k}$  were the processed sEMG signals of the biceps brachii and triceps brachii, and the muscle activation  $a_{1,k}$  and  $a_{2,k}$  were then calculated through the muscle activation dynamics respectively to form the input  $u_k = [a_{1,k}, a_{2,k}]^T$ . The input and output of NARX dynamic recurrent neural network was  $u_k$  and joint torque, where  $k$  represents  $k$ th time step,  $\hat{M}_k$  was joint torque estimation,  $n_u$  and  $n_y$  were the maximum lags for model input and output of the model respectively.

Due to the bulky size of the direct torque measurement equipment, joint torque estimation by (12) is more meaningful. It allows for online real-time torque estimation. Therefore, in this paper, the open-loop model for joint torque estimation was established by NARX dynamic recurrent neural network based on the estimated values, denoted as

NARX1 in Figure 2. The output was estimated joint torque  $\hat{M}_k$  given as:

$$\hat{M}_k = \sum_{j=1}^{n_1} (\delta_{1,j} \text{tansig}(\sum_{i=1}^{n_{u1}+1} (\omega_{1,ij} u_{k-i+1} + \theta_{1,i}) + \sum_{i=n_{u1}+2}^{n_{u1}+n_{y1}+1} (\omega_{1,ij} \hat{M}_{k-i+n_{u1}+1} + \theta_{1,i}))) + \vartheta_1 \quad (13)$$

where the subscript 1 of  $\theta_{1,i}$ ,  $\omega_{1,ij}$ ,  $\delta_{1,j}$  and  $\vartheta_1$  was the parameter that represented NARX1, which was distinguished from other neural network models later on,  $n_{u1}$  and  $n_{y1}$  were the order of input and output, respectively. In order to improve the computational efficiency, the Levenberg-Marquardt algorithm was used to train the open-loop model. The effect of the number of hidden layer units on the estimation accuracy was pre-tested and found that increasing the number of hidden layer units within a certain range can improve the estimation accuracy, while continuing to increase the number of hidden layer units does not improve the estimation accuracy significantly, or even decreases it. Considering the model accuracy and the complexity of the model, the number of hidden layer units was determined to be  $n_1 = 5$ .

### B. CLOSED-LOOP MODEL FOR TORQUE ESTIMATION

The neural network model suffers from the problem that the functional relationships obtained in specific conditions may not be applicable to new conditions, and the NARX dynamic recurrent neural network model based on output estimation suffers from the problem of unstable estimation results and the influence of noise. To solve these problem, this paper established a closed-loop model for joint torque estimation, as shown in Figure 3.

#### 1) STATE SPACE MODEL

Since the joint angle can be easily measured by the inertial measurement unit, this paper established another NARX dynamic recurrent neural network model NARX2, which characterized the relationship between torque and angle based on the actual measurements of the joint angle, as the measurement model:

$$\hat{y}_k = \sum_{j=1}^{n_2} (\delta_{2,j} \text{tansig}(\sum_{i=1}^{n_{u2}+1} (\omega_{2,ij} M_{k-i+1} + \theta_{2,i}) + \sum_{i=n_{u2}+2}^{n_{u2}+n_{y2}+1} (\omega_{2,ij} y_{k-i+n_{u2}+1} + \theta_{2,i}))) + \vartheta_2 \quad (14)$$

where the subscript 2 of  $\theta_{2,i}$ ,  $\omega_{2,ij}$ ,  $\delta_{2,j}$  and  $\vartheta_2$  was the parameter that represented NARX2,  $n_{u2}$  and  $n_{y2}$  were the maximum lags for model input and output, respectively, and the number of hidden layer units  $n_2 = 5$ , output  $y_k$  was the joint angle.

Defining state vector to be joint torque vector. We assumed the process noise and the measurement noise to be the Gaussian white noise. State space model was developed for torque estimation based on state equation (13) and measurement

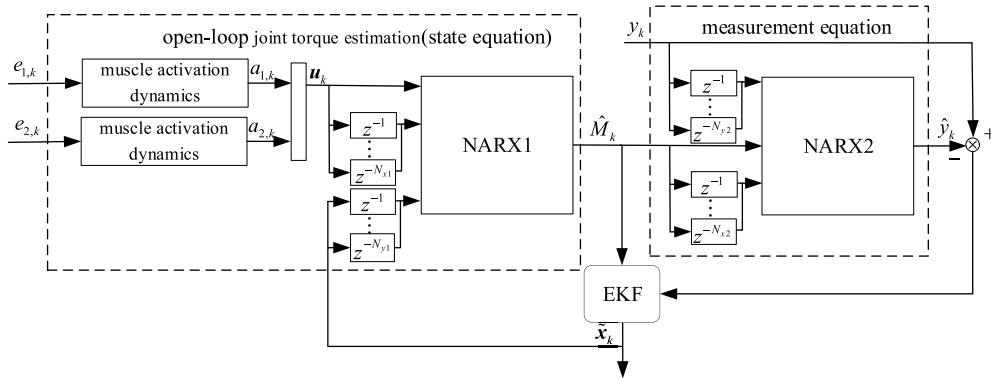


FIGURE 3. Closed-loop joint torque estimation model.

equation (14), as in (15) and (16), as shown at the bottom of the page.

In equation (15) and (16),  $N = \max(N_{y1}, N_{x2})$ ,  $N_{x1}$  and  $N_{y1}$  were the maximum lags for  $\mathbf{u}_k$  and  $\mathbf{x}_k$  of the state model,  $N_{x2}$  and  $N_{y2}$  were the maximum lags for  $\mathbf{x}_k$  and  $y_k$  of the output model.

### 2) TORQUE ESTIMATION BASED ON EXTENDED KALMAN FILTER

Extended Kalman filter (EKF) is widely used for online state estimation of discrete-time nonlinear systems because of its advantages in training efficiency and accuracy [27], so in this paper, EKF is utilized for closed-loop estimation of joint torque.

Muscle activation was first calculated using the sEMG signals, and then muscle activation and normalized joint torque and joint angle measurements were used to train NARX1 and NARX2 offline using the Levenberg-Marquardt algorithm, respectively.

The trained input and output models were then used to establish state space model, and a closed-loop model structure for joint torque estimation was formed based on EKF to perform state filtering.

Compute the Jacobian of the state and measurement function:

$$\mathbf{G}_k = \frac{\delta \mathbf{g}(\mathbf{x}_k)}{\delta \mathbf{x}_k} \tag{17}$$

$$\mathbf{H}_k = \frac{\delta h(\mathbf{x}_k)}{\delta \mathbf{x}_k} \tag{18}$$

The recursive estimation of the state space model by EKF consists of the following two stages [27]:

Time update (predict)

$$\hat{\mathbf{x}}_k = \mathbf{g}(\mathbf{x}_{k-1}, \mathbf{u}_k) \tag{19}$$

$$\mathbf{P}_k^- = \mathbf{G}_k \mathbf{P}_{k-1} \mathbf{G}_k^T + \mathbf{Q} \tag{20}$$

$$\hat{y}_k = h(\hat{\mathbf{x}}_k, \mathbf{u}_k) \tag{21}$$

Measurement update (correct)

$$\mathbf{K}_k = \mathbf{P}_k^- \mathbf{H}_k^T (\mathbf{H}_k \mathbf{P}_k^- \mathbf{H}_k^T + \mathbf{R})^{-1} \tag{22}$$

$$\tilde{\mathbf{x}}_k = \hat{\mathbf{x}}_k + \mathbf{K}_k (y_k - \hat{y}_k) \tag{23}$$

$$\mathbf{P}_k = (\mathbf{I} - \mathbf{K}_k \mathbf{H}_k) \mathbf{P}_k^- \tag{24}$$

where  $\tilde{\mathbf{x}}_k$  represented the filtered value of state vector,  $\tilde{M}_k = \tilde{x}_{1,k}$  was the closed-loop estimation of joint torque,  $\mathbf{Q}$  the process noise covariance,  $\mathbf{R}$  the measurement noise covariance,  $\mathbf{P}_k$  the estimation error covariance matrix,  $\mathbf{K}_k$  the Kalman gain.

### C. PERFORMANCE EVALUATION AND STATISTICAL ANALYSIS

Normalized root mean square error (NRMSE) and correlation coefficient (CC) were taken as indicators to evaluate the performance of joint torque estimation, as shown

$$\begin{aligned} \mathbf{x}_k &= \mathbf{g}(\mathbf{x}_{k-1}, \mathbf{u}_k, \mathbf{u}_{k-1}, \dots, \mathbf{u}_{k-N_{x1}}) + \boldsymbol{\omega}_k \\ y_k &= h(\mathbf{x}_k, y_{k-1}, y_{k-2}, \dots, y_{k-N_{y2}}) + v_k \end{aligned} \tag{15}$$

$$\mathbf{g}(\cdot) = \begin{pmatrix} \sum_{j=1}^{n_1} (\delta_{1,j} \text{tansig}(\sum_{i=1}^{N_{x1}+1} (\omega_{1,ij} \mathbf{u}_{k-i+1} + \theta_{1,i}) + \sum_{i=N_{x1}+2}^{N_{x1}+N_{y1}+1} (\omega_{1,ij} \mathbf{x}_{i-N_{x1}-1} + \theta_{1,i}))) + \vartheta_1 \\ x_{1,k} \\ \vdots \\ x_{N,k} \end{pmatrix} \tag{16}$$

$$h(\cdot) = \sum_{j=1}^{n_2} (\delta_{2,j} \text{tansig}(\sum_{i=1}^{N_{x2}+1} (\omega_{2,ij} \mathbf{x}_{i,k} + \theta_{2,i}) + \sum_{i=N_{x2}+2}^{N_{x2}+N_{y2}+1} (\omega_{2,ij} y_{k-i+N_{x2}+1} + \theta_{2,i}))) + \vartheta_2 \tag{16}$$

TABLE 1. Subject Information.

Subjects	Gender	Age (years)	Height (cm)	Weight (kg)
S1	male	25	167	50
S2	male	25	168	60
S3	male	23	168	70
S4	male	22	177	67
S5	female	21	160	40
S6	male	27	173	55
S7	male	24	170	56
S8	female	46	172	65

in (25) and (26):

$$NRMSE = \frac{1}{M_{real}^{max}} \sqrt{\frac{1}{num} \sum_{i=1}^{num} (M_{est} - M_{real})^2} \quad (25)$$

$$CC = \frac{cov(M_{est}, M_{real})}{\sigma_{M_{est}} \cdot \sigma_{M_{real}}} \quad (26)$$

where *num* was the number of test samples, *M<sub>est</sub>* the estimated values of joint torque, *M<sub>real</sub>* the measurements of joint torque, *M<sub>real</sub><sup>max</sup>* the maximum measurements of joint torque.

One-way analysis of variance (ANOVA) was conducted to assess the statistical difference of estimation errors obtained by different models [28]. The level of statistical significance was set to *p* < 0.05.

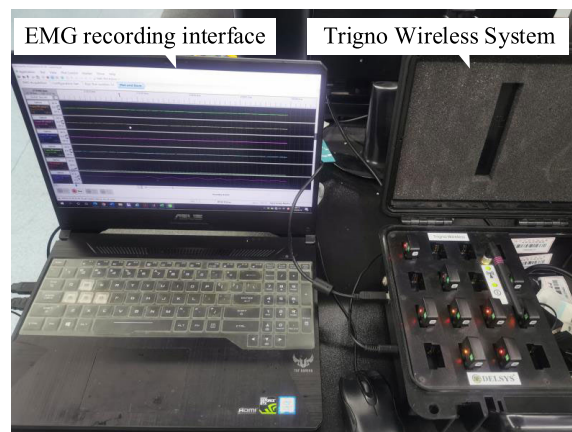
### III. EXPERIMENTS AND RESULTS

#### A. EXPERIMENTAL SETUP AND DATA ACQUISITION

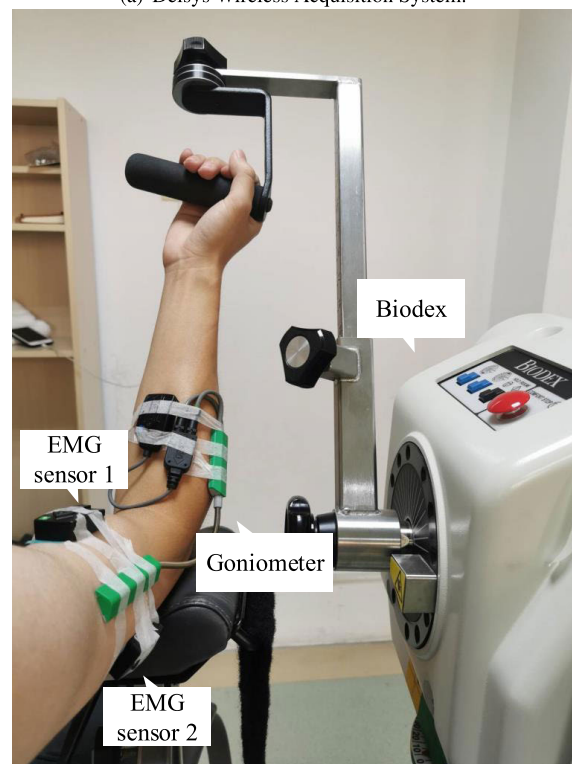
In this section, experiment was conducted to validate the proposed method. Eight healthy subjects volunteered to participate in the experiment (right-handed, age: 26.62 ± 7.53 years; height: 169.37 ± 4.68 cm; weight: 57.87 ± 9.21 kg, two of whom were female). The healthy subjects had no history of neuromuscular disorders, pain, or experience with regular upper extremity training. Subject information is shown in Table 1.

The sEMG signal was acquired using Delsys Trigno Lab Wireless Acquisition System (Trigno Wireless System, Delsys Inc., USA) with a sampling frequency of 2000 Hz, a bandwidth of 20-500 Hz, and a high common mode rejection ratio (CMRR > 80dB). The Goniometer sensor SG 150 (Biometrics Ltd., England) acquired angle signals at 148 Hz with an adapter for data transmission to the Trigno Wireless System. Torque measurement acquisition was performed using a Biodex Pro4 system (Biodex Medical Systems Inc., NY, USA). Using a custom synchronization system, the torque and sEMG signals were acquired synchronously via an adapter so that the torque signal acquisition frequency was the same as the sEMG signal acquisition frequency. Finally, all signals were resampled so that the frequency was the same as the angle signal frequency. The experimental environment is shown in Figure 4.

The sEMG signals, angle signals and torque signals of the isotonic motion of the elbow joint under different loads were collected for subsequent analysis. Isotonic motion is exercise when a contracting muscle shortens against a constant load. When the torque produced by the subject's muscle



(a) Delsys Wireless Acquisition System.



(b) Illustration of Sensor Wearing Position.

FIGURE 4. Experimental environment set-up.

contraction is greater than the load provided by the device, the trainer's joint accelerates; when the torque produced by the muscle contraction is less than the load provided by the device, the trainer's joint decelerates. In this experiment, the subject was asked to perform isometric motion of the elbow joint in the sagittal plane, and the wireless EMG signal sensors were placed on the muscle belly of the biceps and triceps respectively (EMG sensor 1 and EMG sensor 2), and the goniometer was placed at the elbow joint. The isometric motion was set up with loads of 2 N·m, 4 N·m, 6 N·m and 8 N·m for 5 cycles of isometric exercise under each load.

Using the muscle activation dynamics from Section II-A1 to achieve feature extraction of sEMG signals, the raw

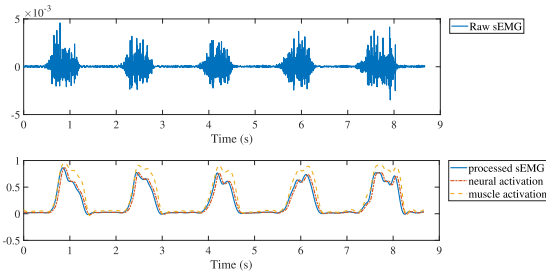


FIGURE 5. Feature extraction of sEMG signals.

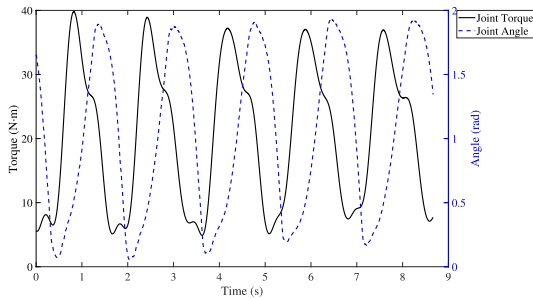


FIGURE 6. Joint angle and torque signals.

sEMGs, processed sEMG signals, neural activation and muscle activation of subject 4 (S4) for five cycles of isometric motion at a load of 6 N·m are shown in Figure 5, and joint angle and torque signals are shown in Figure 6.

**B. DATA ALLOCATION STRATEGY**

In order to investigate the influence of different loads of isometric motion on the joint torque estimation results, this paper analyzed the estimation results under three conditions: load-dependent, multi-load, and load-independent. Load-dependent took the first three cycles of each load as a training set, and the last two cycles at the corresponding load as test set; multi-load took the first three cycles of each load together as a training set, and the last two cycles of each load separately as a test set; the load-independent test took the last two cycles of one load in turn as test set, and the first three cycles of each unselected load together as training set.

**C. ESTIMATION RESULTS**

First, the model was trained offline according to the data allocation strategy. NARX1 was a NARX dynamic recurrent neural network model based on estimated values. Its input was the muscle activation extracted from the sEMG signals of the biceps and triceps with maximum lags  $N_{x1}=2$  for input,  $\gamma_1=\gamma_2=0.5$ ,  $A=-2$ , and the output was the normalized joint torque with maximum lags  $N_{y1}=2$  for output. NARX2 was another NARX dynamic recurrent neural network model based on measurement values with maximum lags  $N_{x2}=2$  for input and  $N_{y2}=2$  for output. The input was the normalized joint torque and the output was the normalized joint angle.

The trained model was then used to perform joint torque estimation. In order to verify the improvement of closed-loop model, we tested the joint estimation results of the NARX neural network based torque estimation model (denoted as NN) and the closed-loop model (denoted as EKFSS).

We tested the joint torque estimation from all subjects under the three conditions of load-dependent, multi-load, and load-independent, and the results for S4 are shown in Figure 7, 8, and 9, where ‘EKFSS’ was the joint torque estimation from the closed-loop model, ‘NN’ was the joint torque estimation based on the NARX neural network model, and ‘true’ was the measurements of the joint torque. From Figure 7 to 9, it can be concluded that the estimation of joint torque based on the NARX neural network model has a large error. After adding the EKF filtering algorithm, the error of closed-loop estimation using the state space model is significantly reduced, and the estimated joint torque can approximate to the ‘true’ values overall.

The mean value of NRMSE and CC under different loads for the three conditions are shown in Figure 10 and Figure 11. The joint torque estimation of the closed-loop state space model with EKF is significantly better than the joint torque estimation based on the NARX neural network model. The error between the measurement values and the closed-loop joint torque estimation is relatively small, and the closed-loop estimation of the joint moment is strongly correlated with the measurement values.

Table 2 and Table 3 show the NRMSE and CC between the estimated joint torque of different models and the measurements (‘true’ values) of all subjects (mean  $\pm$  standard deviation (std)). The mean CC between the EKFSS and ‘true’ values of all subjects were significantly larger than NN and the mean NRMSE were significantly smaller. The mean NRMSE of NN under load-dependent, multi-load and load-independent of all subjects are  $0.2694\pm 0.1584$ ,  $0.2499\pm 0.1326$  and  $0.3435\pm 0.2061$ , respectively, and EKFSS are  $0.1080\pm 0.0411$ ,  $0.1326\pm 0.0494$  and  $0.1674\pm 0.0661$ , respectively. ANOVA was used to evaluate NRMSE of NN and EKFSS, showing significant differences ( $p < 10^{-6}$ ,  $p < 10^{-6}$  and  $p < 10^{-4}$ ). It can also be found that the joint torque estimation results of the closed-loop model for the three cases are optimal for load-dependent estimation, with the smallest NRMSE (0.1080), followed by multi-load (0.1326), and worst for load-independent (0.1674). The variability of joint motion with different loads can affect the estimation of the model, and the experimental results also demonstrated that the load-dependent results were optimal and the load-independent results were the worst.

In this paper, in order to achieve joint torque estimation without torque measurement values, the estimation of NARX neural network model was based on estimated values. Thus, the error of joint torque estimation results has a great influence on the subsequent estimation results, which leads to the

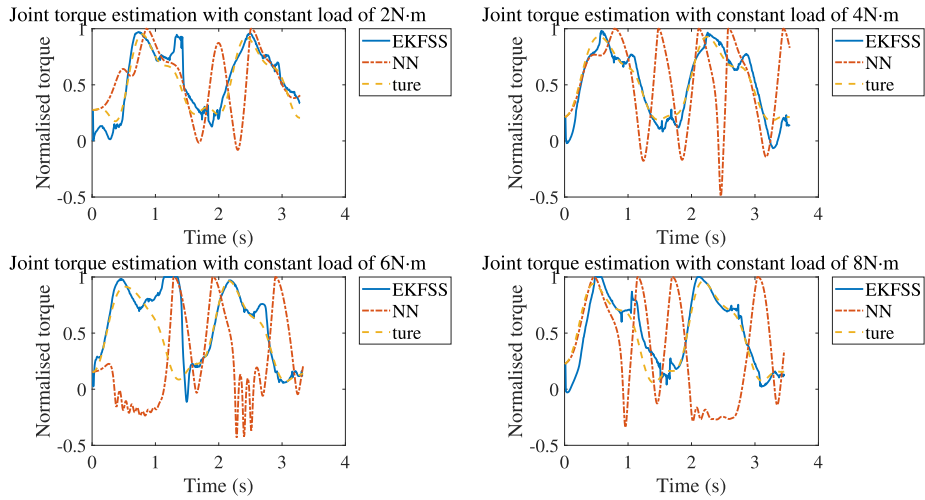


FIGURE 7. Joint torque estimation under load-dependent of S4.

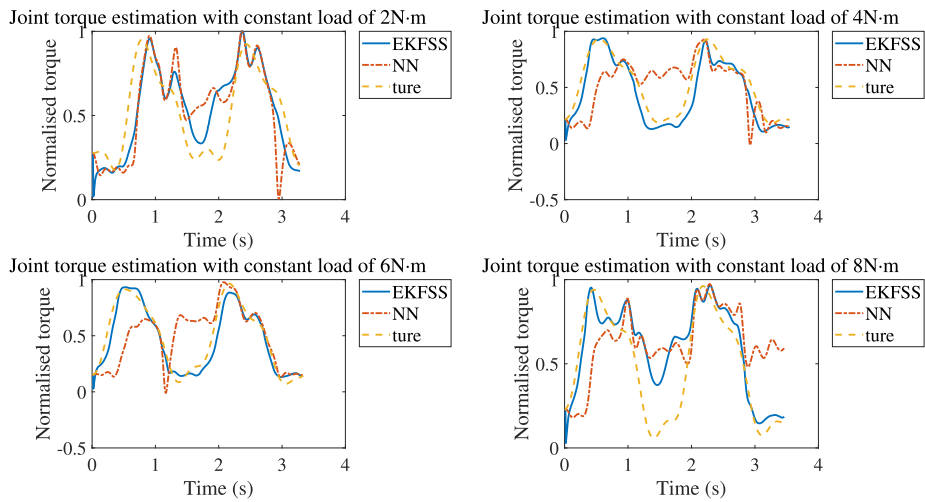


FIGURE 8. Joint torque estimation under multi-load of S4.

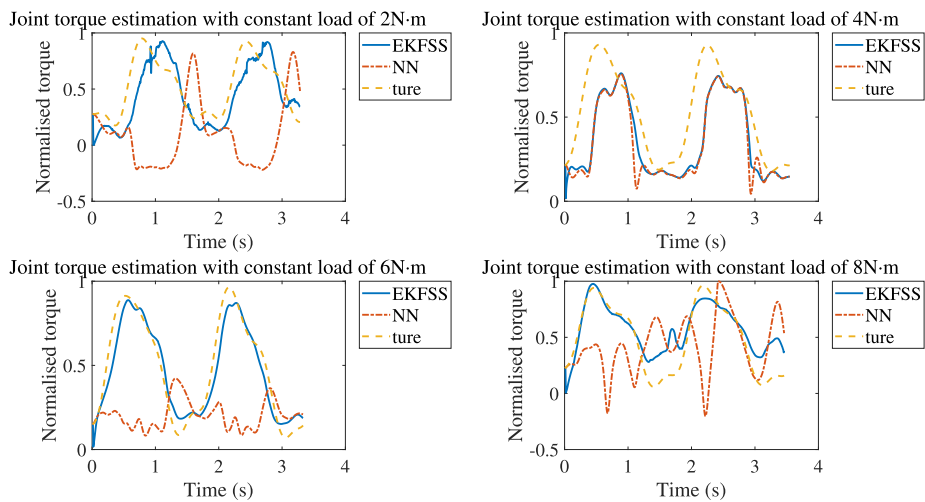


FIGURE 9. Joint torque estimation under load-independent of S4.

unstable performance of the torque estimation, with relatively large error and low correlation. Using joint angle signals

to establish a closed-loop estimation model for joint torque improves the accuracy of joint torque estimation.

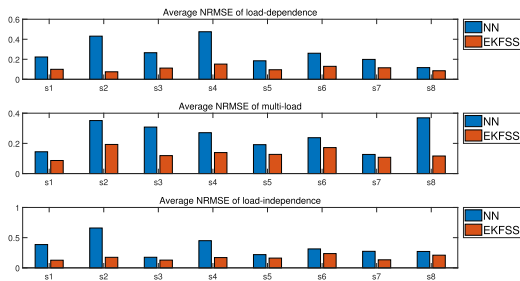


**TABLE 2.** NRMSE between the estimated joint torque of different models and the measurements ('true' values) of all subjects (mean ± std).

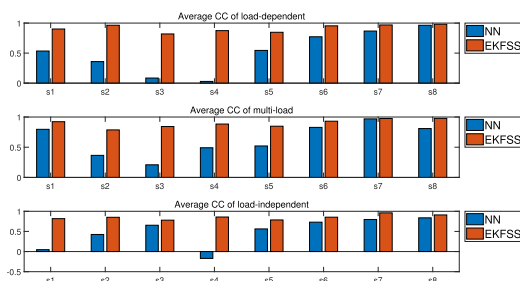
		2N.m	4N.m	6N.m	8N.m
load-dependent	NN	0.2129±0.1380	0.2181±0.0939	0.2874±0.1932	0.3591±0.1447
	EKFSS	0.0935±0.0176	0.0999±0.0189	0.1051±0.0654	0.1336±0.0298
multi-load	NN	0.2491±0.1151	0.2506±0.0949	0.2715±0.1023	0.2284±0.0701
	EKFSS	0.1486±0.0525	0.1042±0.0249	0.1166±0.0505	0.1610±0.0414
load-independent	NN	0.4181±0.2572	0.3624±0.2374	0.2783±0.1223	0.3150±0.1466
	EKFSS	0.1821±0.0682	0.1456±0.0532	0.1714±0.0680	0.1708±0.0684

**TABLE 3.** CC between the estimated joint torque of different models and the measurements ('true' values) of all subjects (mean ± std).

		2N.m	4N.m	6N.m	8N.m
load-dependent	NN	0.6108±0.2541	0.5648±0.3420	0.4634±0.4891	0.4381±0.3698
	EKFSS	0.8926±0.0990	0.9257±0.0562	0.9233±0.0930	0.9124±0.0532
multi-load	NN	0.5788±0.2510	0.6358±0.2492	0.5887±0.2994	0.6908±0.2586
	EKFSS	0.8457±0.0842	0.9254±0.0775	0.9258±0.0794	0.8862±0.0847
load-independent	NN	0.3040±0.5503	0.5945±0.2462	0.4689±0.5083	0.5732±0.3147
	EKFSS	0.7956±0.1430	0.8743±0.0602	0.8541±0.1261	0.8838±0.0632



**FIGURE 10.** Average NRMSE for estimation of joint torque under different loads.



**FIGURE 11.** Average CC for estimation of joint torque under different loads.

**IV. DISCUSSION AND CONCLUSION**

EMG signals are widely used in scientific research related to the development of intelligent rehabilitation technology and equipment [29]. The EMG signal contains a wealth of motion information that precedes actual joint motion and is often used as a control signal to predict joint motion. Previous studies have focused on feature extraction and classification of EMG signals for identifying movement patterns [30], gait analysis [31], and joint angle estimation [32], [33]. Joint torque measurements are more complicated relative to joint angles due to the complexity of the human joint structure. The closed-loop model designed in this paper uses the EKF filtering algorithm to optimize the closed-loop model, improve the joint torque estimation results, and provide a new strategy for real-time joint torque estimation.

Taking the elbow joint as the research object, this paper designs a closed-loop model of joint torque estimation based on sEMG signals. A series of processing of the sEMG signals of the biceps and triceps were performed, and the muscle activation was obtained from the muscle activation dynamics. A torque estimation model was developed using a dynamic recurrent neural network based on the NARX model. To address the instability of the NARX neural network model and the influence of interference, a state-space closed-loop model with EKF algorithm for joint torque estimation was further designed. Finally, an isotonic motion experiment of elbow joint was designed to verify the actual estimation effect of the joint torque estimation model. The designed closed-loop model estimation improved the stability, and the NRMSE was significantly lower than that of the open-loop model. The proposed method combined offline modeling and online filtering to achieve online estimation of joint torque.

Although this article takes the elbow joint as the research object for model research and verification, the closed-loop model for torque estimation proposed in this paper is not limited to elbow joint torque estimation. In further study, the proposed torque estimation model can be applied to the torque estimation of other joints for related testing and validation.

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