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# Measurement of Potato Volume With Laser Triangulation and Three-Dimensional Reconstruction

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**ABSTRACT** Potato grading is related to weight. Three-dimensional (3D) reconstruction can provide highly accurate volume measurements of potatoes, which can help farmers to analyze their phenotypic characteristics and grade them. Considering their low cost and the required accuracy, a monocular camera and line laser were used to build a potato phenotype determination scanning device. The system obtains coordinates along the surface of a potato, collects laser light reflected from the surface in real time, and completes the coordinate calculation of the original points using the triangulation method. However, the original point clouds lose large areas of point clouds at the top and bottom of the potato. Point cloud repair is carried out by interpolation of points. In addition, the surface point cloud is smoothed. Finally, the generated point cloud is used for 3D reconstruction and volume calculation. In a volume error analysis test, potatoes are divided into calibration and verification groups. First, linear regression is used to relate the real and measured potato volume, and then the density of the potato is calculated. The volume and mass of potatoes in the verification group are measured by the device, and the standard volume and mass are measured manually. The results show that the average relative error in measured volume is  $-0.08\%$ , and the average relative error in estimated mass is  $0.48\%$ . These results indicate that the combination of a line laser and a single camera provides accurate measurements of potato volume that can be used for yield estimation and potato grading.

**INDEX TERMS** Line laser, volume estimation, feature prediction, weight estimation.

## I. INTRODUCTION

Non-destructive measurement methods are important for yield monitoring. Mechanical sensors, such as belt weights and impact measurements, can damage crops and are difficult to calibrate due to vibration. By measuring the volume of cultivated crops or agricultural products, yields can be accurately calculated [1], [2]. Geometric characteristics and yield monitoring of crops can give farmers feedback [3] that can help them grade fruits and vegetables for added value [4], [5]. However, the analysis of phenotypic features is mostly artificial [6], which is labor-intensive and inefficient, resulting in a so-called “phenotyping bottleneck” [7], [8]. Using computer

vision [9] or three-dimensional (3D) imaging [10], farmers can analyze the quality of crops, so they can estimate yields and grades [11].

The potato (*Solanum tuberosum* L.) is one of the most important crops around the world, totaling 17.6 million hectares (FAO, 2018). In many cases, it is difficult to measure and grade potatoes due to their uneven surface and vulnerability to damage [12]. In the last decade, with the development of machine vision, images have been widely used to analyze the quality and weight of fruits and vegetables [13]–[15], including potatoes [16], [17]. However, the thickness of the potato cannot be obtained without the depth of field in a two-dimensional image. 3D reconstruction technology allows for precise measurements of potato volume [18], and phenotypic reconstruction has become possible.

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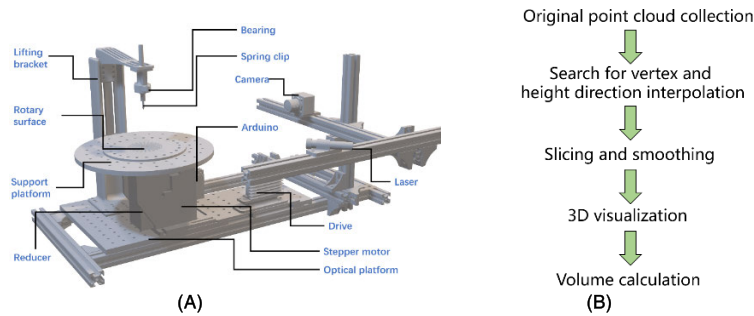


FIGURE 1. (A) Device structure. (B) Reconstruction process.

3D reconstruction has long been used to measure forest canopy parameters [19]–[21] and to monitor crop phenotypes [22], [23] and poultry [24]–[26]. It also has been used to measure the volume of crops, such as the fresh weight of lettuce [27], volume of onion fruit [28], or volume of cauliflower [29]. 3D laser scanning provides fast measurements with moderate accuracy and low cost [30]. Common methods include the use of structured light [31], [32] and time-of-flight measurements using the phase of received light [33], where the former is most used in 3D modeling, such as with the Microsoft Kinect sensor. However, due to the complexity of crop phenotypes, it is difficult to complete scanning from one angle at a time. There have been studies using multi-view stereovision [34]–[36] and structure from motion [37]–[39].

This study aims to use a single camera and line laser to build a 3D reconstruction system for potato volume measurements, through which potato surface information can be collected and stored. By analyzing point cloud data, the appearance of a potato can be reconstructed, and the exact volume calculated. Due to the limitations of a low-cost device and the influence of the camera angle, the camera cannot move and collect color information from the surface, resulting in point cloud measurements with missing information, especially at the bottom and top of a potato's rotation axis. To remedy this problem, we process the original point cloud data and reconstruct a 3D model of the potato from a grid. The potato volume measurement error from the device is determined by comparing the exact volume to the standard volume container. A non-destructive method is used to predict the weight of potatoes.

## II. MATERIALS AND METHODS

### A. POTATO SAMPLES AND MANUAL ASSESSMENT

The sampling standard refers to GB/T 8855-2008, and the minimum sampling quantity is 3 kg. Fresh potatoes were purchased in the afternoon from Qixia Agricultural Market of Nanjing on the day before the experiment. The total weight of 35 fresh potatoes was 6.056 kg; potatoes were randomly selected and did not have deformities. All potatoes were manually cleaned and washed to remove dirt and clay clouds before testing. The potatoes were separated into groups for calibration and verification. The weight of five potatoes used for calibration was 0.835 kg, and the weight of 30 potatoes used for verification was 5.221 kg.

The volume of potatoes was measured manually by a metrologist at Jiangsu Institute of Metrology at a constant temperature of 20°C and 50% RH. The standard device used for volume measurement is a standard glass gauge, which has an error of  $-0.07\%$  in 500 mL. An electronic counting balance (Sartorius, Germany) with an error of 0.04% within 1000 g was used for mass measurement.

### B. HARDWARE AND SYSTEMS

The hardware system is shown in Fig. 1A. The motion mechanism is composed of a reducer with a deceleration ratio of 2.5:1, a stepping motor (57 steps, SNOWIT, Changzhou), a two-phase DC synchronous subdivision step driver (LiChuan, Shenzhen), and an Arduino UNO R3 microcontroller board (Arduino, Italy). The data acquisition system consists of a 532-nm linear laser with 10 mW output power, and a  $2048 \times 1536$  pixel CCD camera with a focal length of 21 mm. The system is controlled by a computer (Intel i5 CPU, Windows 7 operating system, 16 GB RAM, Hewlett Packard, USA). Both the camera and laser were placed 300 mm from the rotation axis, and the angle between the camera and laser was set to  $50^\circ$ .

A program for controlling the system was written in LabVIEW 2019 SP1 (National Instruments, USA); the data acquisition process is shown in Fig. 1B. Access 2016 (Microsoft, USA) was used for data storage, and MATLAB R2019a (MathWorks, USA) for 3D visualization.

### C. ORIGINAL POINT CLOUD COLLECTION

A flowchart of the process for acquiring original point cloud coordinates is shown in Fig. 2A. The potato is placed on a rotating surface, and the compression force of a spring clip is used to fix the potato to the surface. The stepping motor drives the reducer and rotates the surface. Data are gathered by rotating the potato  $1^\circ$  in 0.5 s.

The camera is used to gather successive images as the motor moves through each step. The coordinates of points on the potato surface are calculated by image processing. A schematic diagram is shown in Fig. 2B. The actual radius  $r$  of the potato surface point and the imaging distance  $\Delta d$  in the image are related by the formula

$$\frac{r \cdot \sin \gamma}{\Delta d \cdot \sin \beta} = \frac{f - r \cdot \cos \gamma}{f' + \Delta d \cdot \cos \beta} \quad (1)$$

where  $r$  is the distance to the center of rotation for the potato surface point;  $\Delta d$  is the distance between the light contour

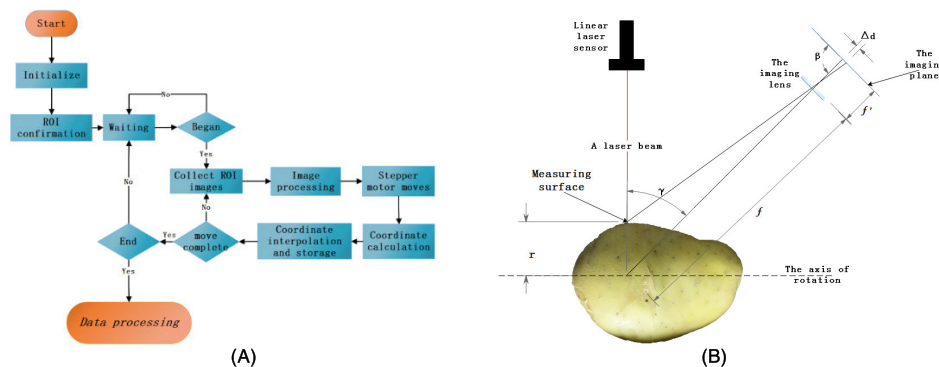


FIGURE 2. (A) Flowchart of the process for acquiring original point cloud coordinates. (B) Schematic diagram of radius coordinate calculation.

and the axis of rotation on the imaging surface;  $\gamma$  is the angle between the laser beam axis and the optical axis of the imaging lens;  $\beta$  is the angle between the imaging surface and the optical axis of the imaging lens;  $f$  is the object distance on the optical axis of the imaging lens; and  $f'$  is the image distance on the optical axis of the imaging lens. The missing point coordinates in the original coordinate data are interpolated, and all coordinates are stored in the database. The ratio of the pixel coordinates of the ROI area in the image to the actual coordinates is stored in the computer memory, and the ROI area is determined manually. Images collected by the camera are converted to 32-bit RGB format. The green component in the image is converted to an 8-bit grayscale image, which is transformed to a matrix. The program traverses each column of the matrix, calculates its brightness value using a threshold method [40], [41], and coordinates of the laser centerline in the picture are obtained. The centerline coordinates of the potato contour are compared to the axis coordinates to obtain the coordinates of the points at  $\theta_i$ . A small number of noise points in the point cloud cause the centerline to be discontinuous. These isolated points can be removed by threshold judgment. Cubic interpolation is carried out to make discontinuous coordinate points continuous within the original range, and all coordinates are stored in an Access database. This process is repeated until the potato has rotated through a full revolution.

#### D. SEARCH FOR VERTEX AND HEIGHT DIRECTION INTERPOLATION

In the process of collecting the original point cloud coordinates, a large region of data will be missing from the bottom and top of the potato due to the camera angle, occlusion of the fixed device, and self-occlusion of the potato, as shown in Fig. 3A. Methods to repair 3D point clouds include implicit surface reconstruction with radial basis functions [42], surface hole filling with a context sampling model [43], and point cloud repair using Poisson’s equation [44] or partial differential equations [45]. These methods are computationally intensive and may lose some detail. This study is based on the original data-acquisition device in potato fixation. There are two fixed points along the Z-axis direction, so all points in the missing area will intersect at one point. Finally, the missing

points can be repaired by interpolating the intersection point and the point at each angle.

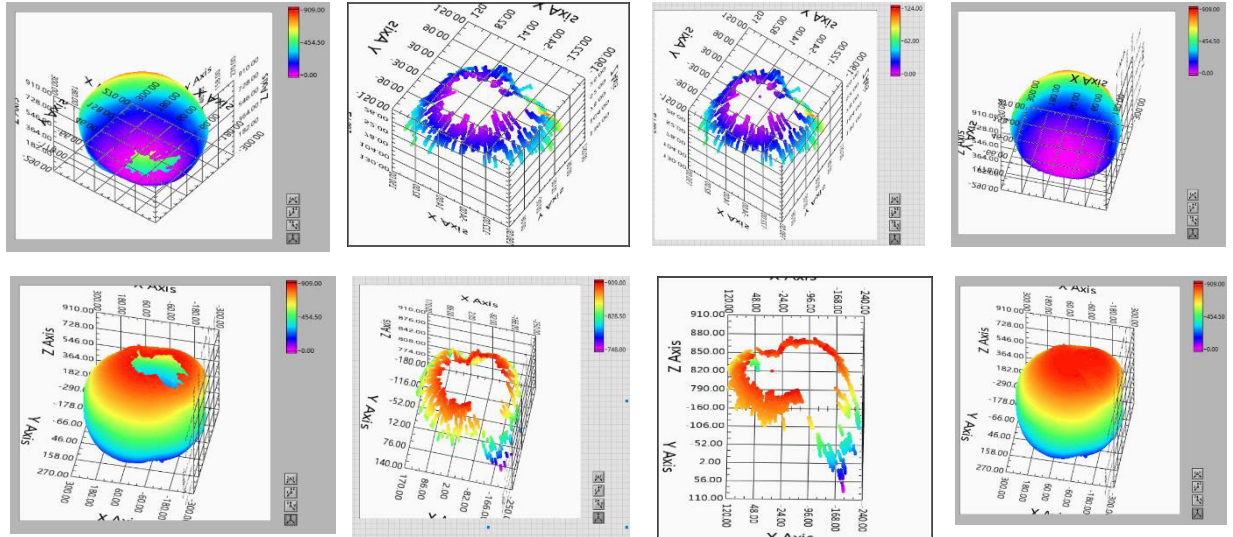
In the program, the missing regions of the point cloud at the top and bottom of the potato are first extracted, and points from 15 layers outside the missing regions are taken as the interpolation regions, as shown in Fig. 3B. The top and bottom interpolation regions are searched to find the point closest to the Z-axis and the point with the lowest height at the bottom. Points on the angles of the two search points are fitted to obtain the points intersecting the Z-axis, as shown in Fig. 3C. Various angles on the potato are traversed, and the coordinates of all the points at each angle are interpolated to obtain filled point cloud coordinates. The repaired point cloud is shown in Fig. 3D.

#### E. SLICING AND SMOOTHING

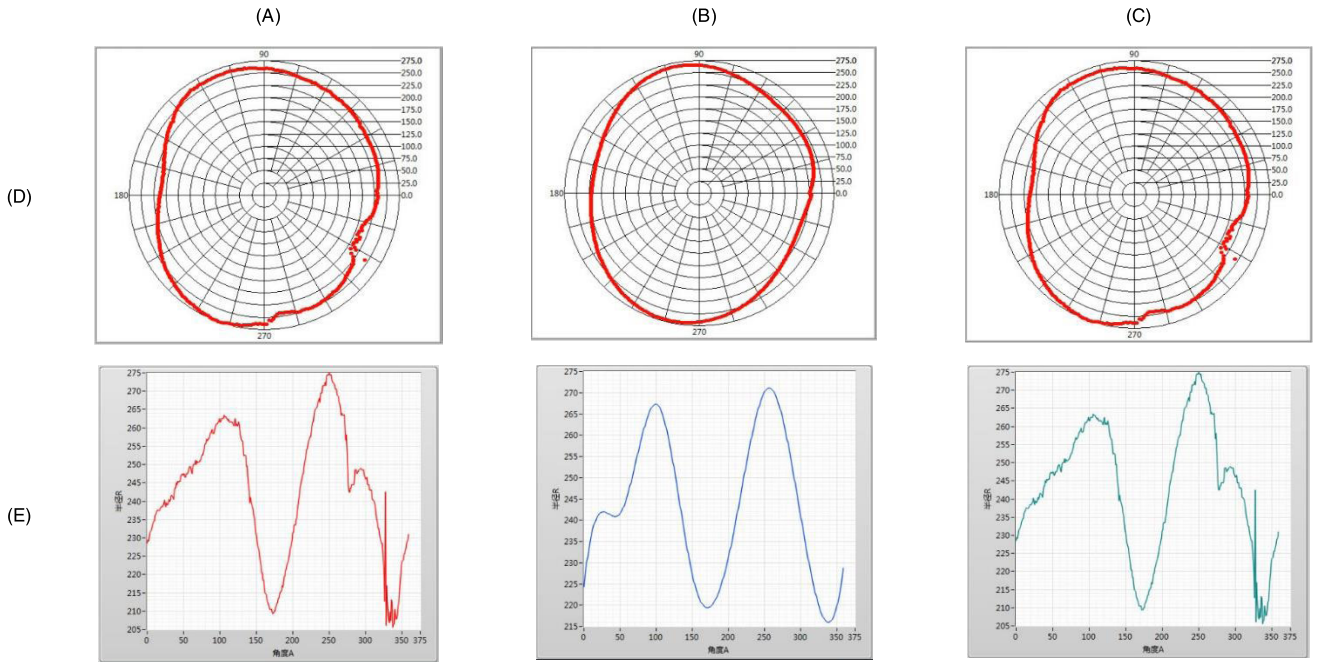
Point clouds on the surfaces of potatoes can be divided into two categories. The first contains unprocessed raw data, and the second contains data obtained through interpolation. Each layer is sliced according to the Z-axis, and one finds that coordinate points with no interpolation in the cross section are smooth in polar and x-y coordinates, as shown in Fig. 4A. The coordinates of the points on the interpolated cross section are too scattered, as shown in Fig. 5A. To reduce variance in the interpolation region of the point cloud, the data are fitted to a B-spline curve, which is often used for modeling in mechanical 3D design software [46], to obtain a smooth contour. All points on each slice are fitted to B-spline curves to obtain a smooth contour, as shown in Figs. 4B and 5B. By controlling the RMSE threshold of the distance between the original point and the B-spline curve, a small fluctuation is obtained and superimposed on the B-spline fitting curve. The optimized point cloud coordinates are shown in Figs. 4C and 5C.

#### F. VOLUME CALCULATION

The volume of the potato is calculated using the point cloud in cylindrical coordinates, as shown in Fig. 6A. The system reads all point cloud coordinates from the Access database, with coordinates formatted as shown in eq. (2). The area of the slice at height  $h_{\theta_i}^j$  is integrated, as shown in eq. (3). Finally, the total volume of potatoes can be obtained by integrating the



**FIGURE 3.** Point cloud interpolation process. (1) Point cloud from the bottom of a potato. (2) Point cloud from the top of a potato. (A) Original point cloud. (B) Point cloud interpolation region. (C) Region used to search for the intersection point. (D) Repaired point cloud.



**FIGURE 4.** Slice graph of a point cloud region without interpolation. (A) Original point cloud. (B) B-spline fitting curve. (C) Processed point cloud in: (D) polar coordinates; and (E) Cartesian coordinates.

height of area  $S^j$ , as shown in eq. (4):

$$\vec{P}_{\theta_i}^j = (\theta_i, h_{\theta_i}^j, r_{\theta_i}^j) \quad (2)$$

$$S^j = \sum_0^n \frac{\Delta\theta_i \cdot \pi \cdot (r_{\theta_i}^j)^2}{360} \quad (3)$$

$$V = \sum_0^m \left( \sum_0^n \frac{\Delta\theta_i \cdot \pi \cdot (r_{\theta_i}^j)^2}{360} \right) \cdot \Delta h^j. \quad (4)$$

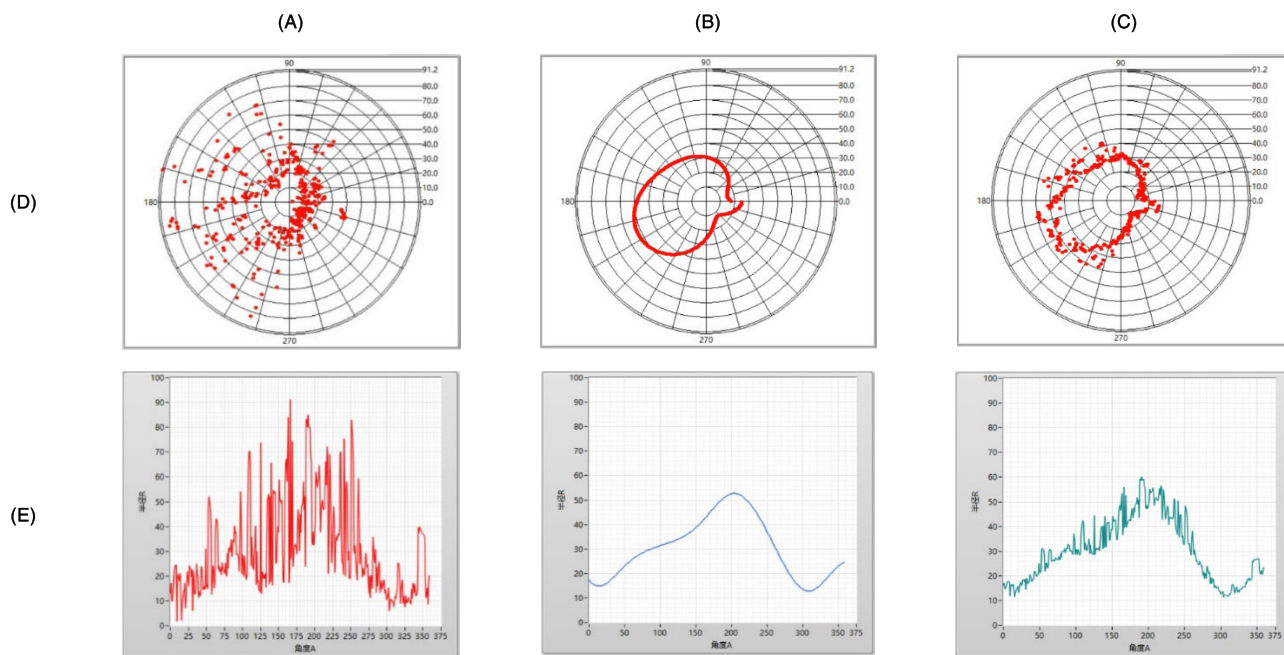
$\theta_{\theta_i}^j, h_{\theta_i}^j, r_{\theta_i}^j$  are respectively the measurement angle, height, and radius of the surface point in cylindrical coordinates;  $S^j$  is

the area of the section corresponding to height  $\Delta h^j$  at height  $h_{\theta_i}^j$ ;  $\Delta\theta_i$  is the stepping angle;  $n$  is the number of measurement angles; and  $m$  is the total number of potato slices along the Z-axis.

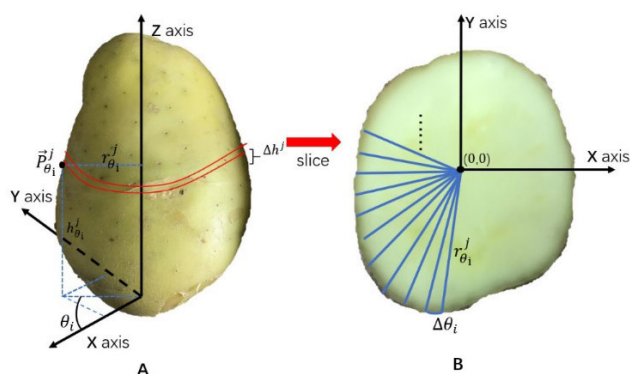
### III. RESULTS

#### A. SYSTEM CALIBRATION RESULTS

The potatoes used for calibration were measured, and the measured volume, standard volume, and standard mass were determined. Relationships between the measured volume and standard volume, and between the standard volume and standard mass, were determined using linear regression, as shown in Figs. 7A and B, respectively.



**FIGURE 5.** Slice graph of a point cloud region with interpolation. (A) Original point cloud. (B) B-spline fitting curve. (C) Processed point cloud in: (D) polar coordinates; and (E) Cartesian coordinates.



**FIGURE 6.** Potato volume calculation results. (A) Potatoes in Cartesian and cylindrical coordinates. (B) Potato slice area integration region.

SPSS version 23.0 (IBM Corp., Armonk, NY, USA) was used to perform linear regression between the measured volume and standard volume; the resulting model is shown in eq. (5):

$$V = V_0 * 0.992 + 13.171, \tag{5}$$

where  $V$  is the corrected volume and  $V_0$  is the measured volume. The coefficient of determination is 1.000 and  $RMSE = 1.02 \text{ cm}^3$ . The average density of potatoes used for calibration was calculated to be  $1.0805 \text{ g/cm}^3$ .

**B. VERIFICATION OF POTATO VOLUME**

For the point cloud used for verification, the volume was calculated using eq. (3), and the volume and mass were determined using eq. (4) and the potato density. The standard volume and standard mass were measured manually, as shown in Fig. 8.

**C. CHANGE OF POTATO VOLUME DURING ALGORITHM PROCESSING**

In processing the potato point cloud, the steps to change the computational value of potato volume include interpolation and smoothing. The volume of a potato is obtained in two processing steps. The volumes of the unprocessed potato point cloud, interpolated potato, and smooth potato are shown in Figure 9.

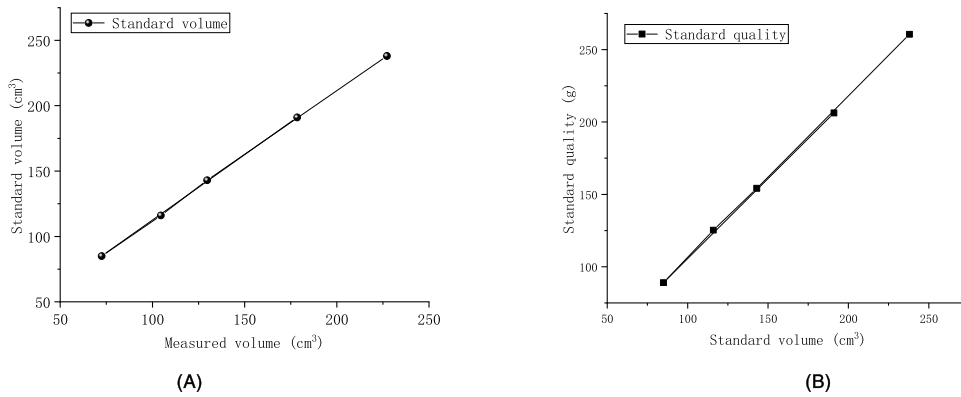
**D. 3D RECONSTRUCTION**

3D reconstruction of potatoes was accomplished using the alphaShape [47] toolbox in MATLAB. The surface mesh effect of the potato based on the original point cloud and the treated post-point cloud is shown in Figs. 10A–C. The maximum alpha radii of the original and processed point clouds are respectively 12 and 3 mm. For the potato in the figure, the relative error between the original point cloud volume and the standard volume is  $-2.12\%$ , and the relative error between the treated point cloud volume and the standard volume is  $-0.98\%$ , where the uncertainty of the standard volume measurement is  $0.96\%$ .

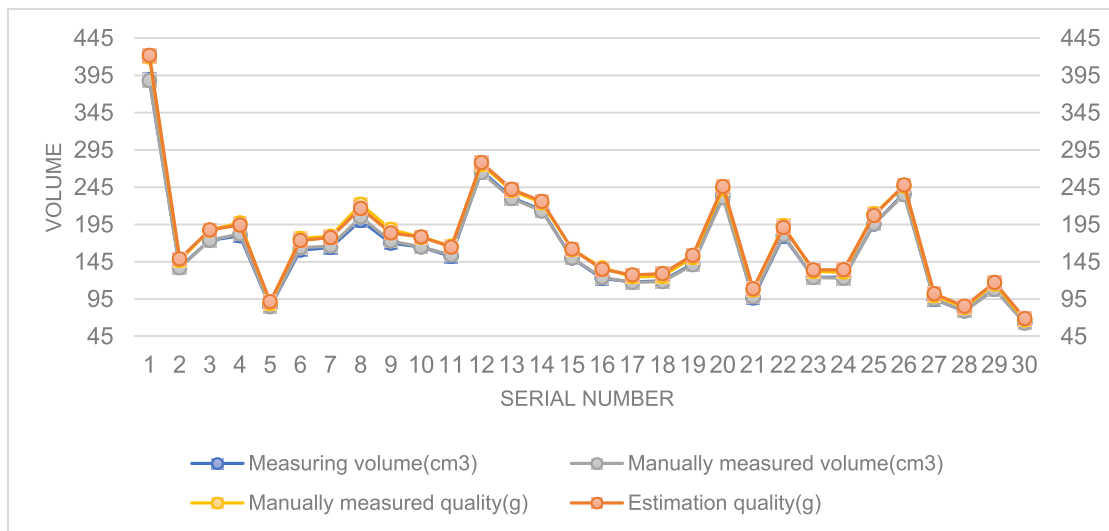
We materialized the surface mesh of the potato using Geomagic Wrap 2017 (3D Systems, USA) and printed a materialized model using a 3D printer with a precision of 0.2 mm from polylactic acid material. The models of real potatoes and 3D printed potatoes are shown in Figs. 11A–C.

**IV. DISCUSSION**

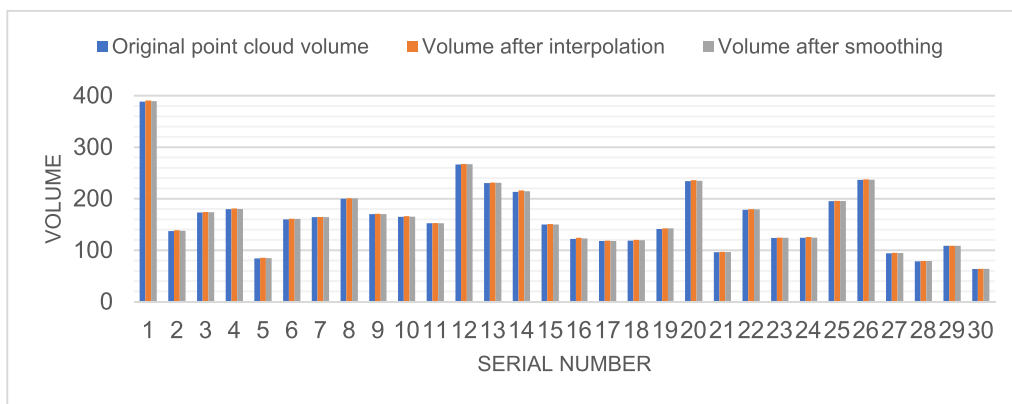
A fixed wire laser and camera were used to complete a full revolution surface scan by rotating a potato. The device can also be used to measure the volumes of vegetables and fruits, such as sweet potatoes, corn, oranges, and avocados. However, this device is not suitable for apples, pears, and



**FIGURE 7. Linear regression results between: (A) measured volume and standard volume; and (B) standard volume and standard mass.**



**FIGURE 8. Volume and mass measurements.**



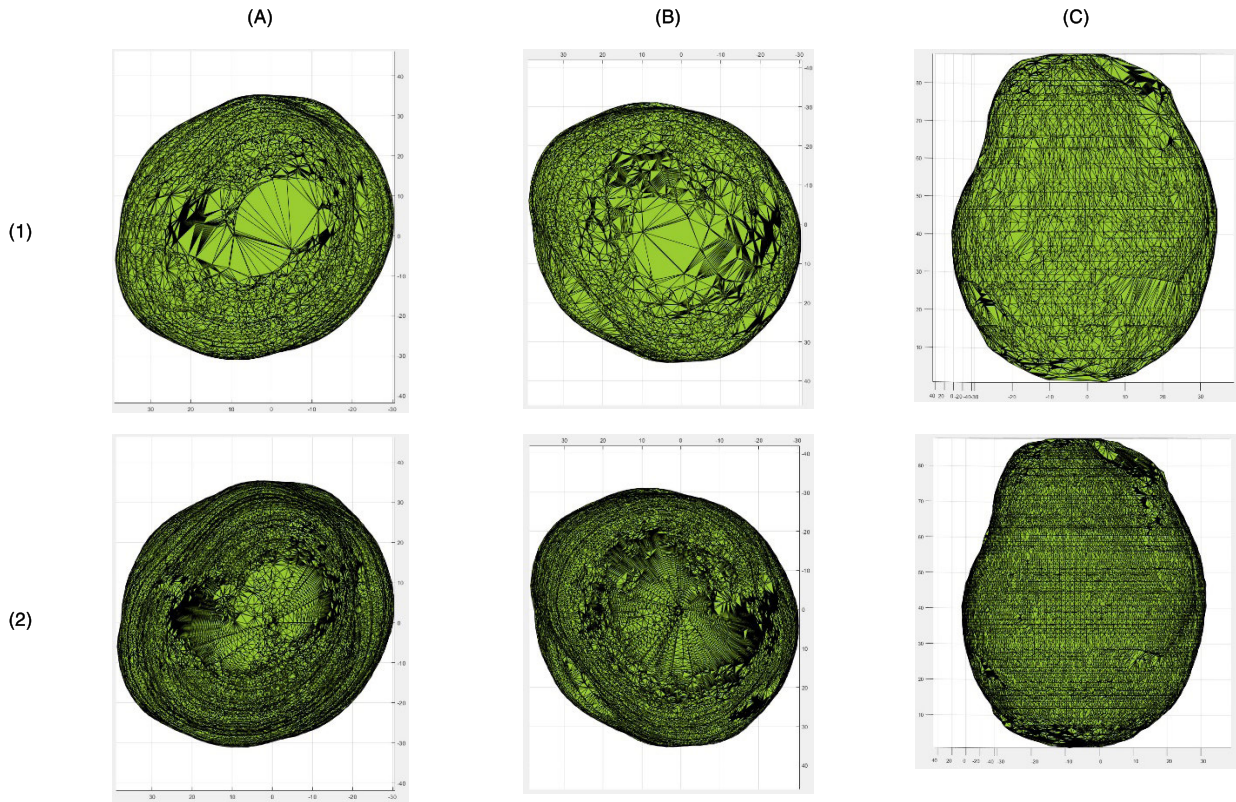
**FIGURE 9. Potato volume change during point cloud processing.**

other fruits with large depressions at the top, which cause large distortions in the local area. This can be solved by gathering data from multiple azimuths or by using a point cloud registration method [48], [49].

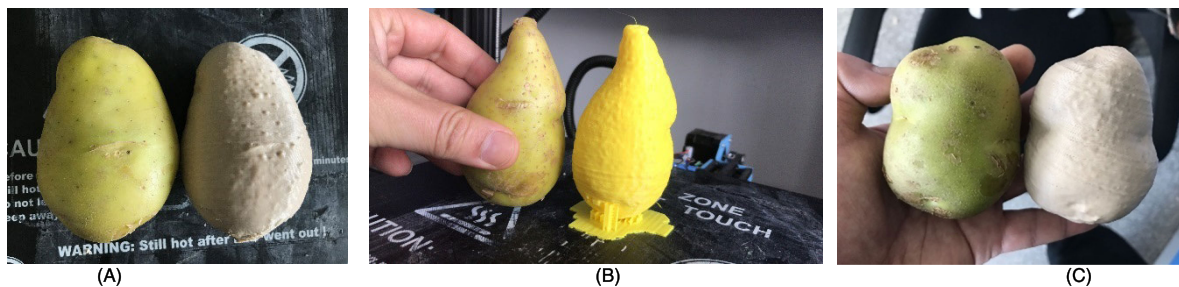
Local vertex search, interpolation, slicing, and smoothing are used in data processing to improve the detail effect of

the 3D model, reducing the alpha radius after point cloud processing from 12 to 3 mm. The relative error of volume measurement after different processing steps of potatoes is shown in Fig. 12.

From the relative error of potato volume after different treatments, the calculated average relative error of the original



**FIGURE 10.** Point clouds of potatoes. (1) Grid diagram of an original point cloud. (2) Grid diagram of a processed point cloud. (A) Top of a potato. (B) Bottom of a potato. (C) Side of a potato.



**FIGURE 11.** Real potatoes and 3D printed potatoes.

point cloud is  $-0.4\%$ , the average relative error after interpolation is  $0.29\%$ , and the average relative error after smoothing is  $-0.08\%$ . In addition, the volume of the potato in Fig. 10 was studied using 3D point cloud repair, after which the measurement error could be reduced by  $1.14\%$ . This means that point cloud repair has a small impact on the measurement of volume, but a large impact on 3D visualization. By changing the potato's volume, we can see that our processing methods are beneficial and useful in correcting the volume of the potato.

The relative error between the measured volume and estimated mass of potatoes is shown in Fig. 13.

The average relative error of potato volume in the verification group is  $-0.08\%$ , the maximum relative error is  $2.17\%$ , and the minimum relative error is  $0.03\%$ . The volume, mass, and surface point cloud of the potato can be obtained

simultaneously with structured light and camera. The volume of the potato can be accurately measured, and a fixed density can be used to estimate its mass. The average relative error of the estimated mass is  $0.48\%$ , and the maximum and minimum relative errors are  $2.92\%$  and  $0.12\%$ , respectively. In comparison, the average error of cauliflower volume measured by Kinect was  $0.58\%$  [29], the average error of grape volume measured by air displacement techniques was  $3.8\%$  [51], and the average error of potato volume measured by RGB-D camera was  $9\%$  [52]. Our device has obvious advantages in accuracy, at a much lower cost.

The linear correlation equation between the measured and standard volume of potatoes was analyzed using SPSS. The  $R^2$  value was found to be  $1.000$  with an RMSE of  $1.80 \text{ cm}^3$ ; thus the measured surface volume was in good agreement with the actual volume. It is believed that the point cloud

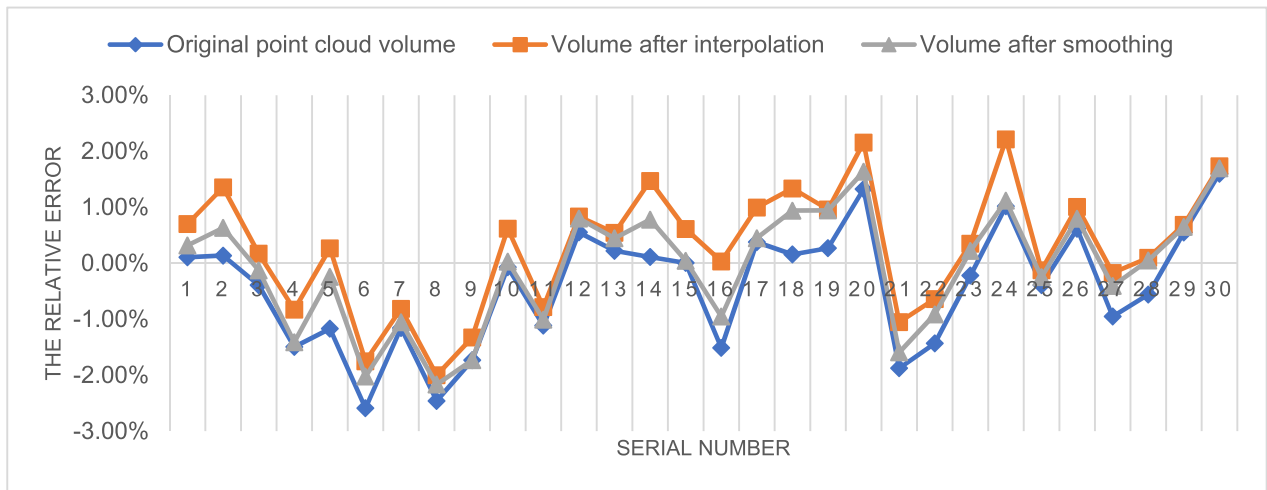


FIGURE 12. Relative error of potato volume during point cloud processing.

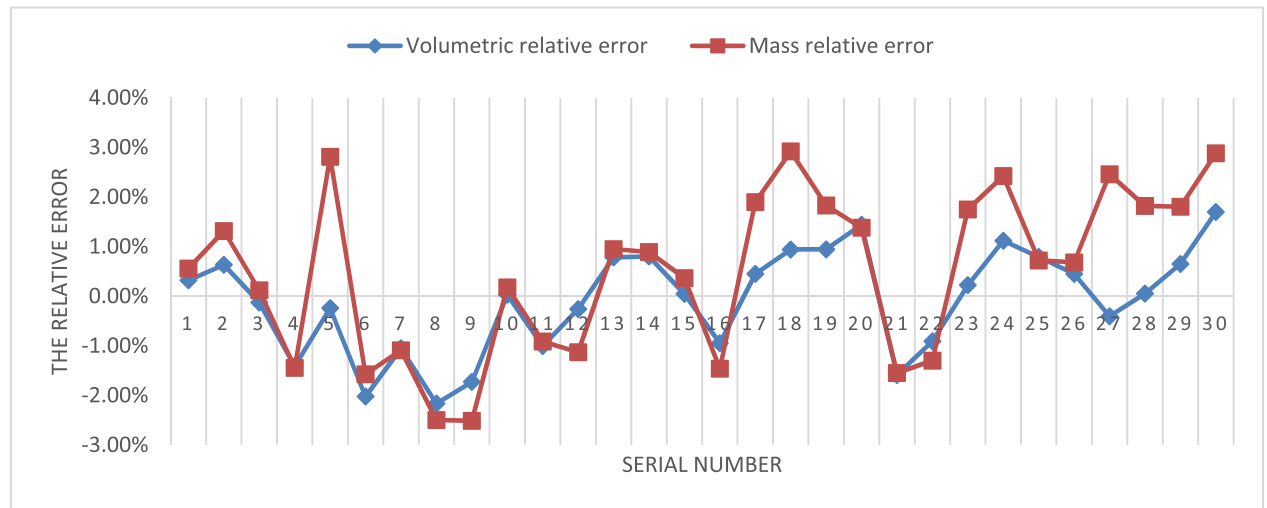


FIGURE 13. Relative error of measuring volume and estimating mass of potatoes.

coordinates obtained with the device for this paper and the reconstructed 3D model are strongly correlated with the potato surface, whose pits and buds can be visualized.

## V. CONCLUSION

In this paper, a monocular camera and line laser were used to build a rotary phenotype scanning mechanism, which can be used to acquire point cloud data from the surface of a potato. We searched the point closest to the Z-axis and the intersection with the Z-axis through the point cloud at the angle of the nearest point and completed the repair of the point cloud through the intersection point and the original point cloud. Then the potatoes were sliced along the Z-axis, and the points in each section were fit to B-spline curves. The entire point cloud was used to calculate the volume and mass of a calibrated potato. The standard volume and mass of a calibrated potato were measured manually. A linear relationship between the measured and standard volume was determined using linear regression, and the density of the potato was obtained by manually measuring the mass and volume of potatoes in a modified group. The regression

model of volume was used for potato verification, and the volume and mass of the potato obtained using the point cloud were compared with those that were manually measured. The coefficient of determination between potato mass and volume was 1.000, with an average relative error of  $-0.08\%$  and RMSE of  $1.80 \text{ cm}^3$ . The potato mass could be accurately estimated with an average relative error of  $0.48\%$ . The results show that the error in potato mass estimation is very small. According to the NY/T 1066-2006 standard, the grading error rate of a potato is  $0\%$ . This result showed better accuracy than the  $91\%$  accuracy based on color image processing [50] and the  $93\%$  accuracy based on depth image processing [18]. This device and treatment can be used for potato grading and yield estimation. The results illustrate the usefulness of 3D point cloud reconstruction for potato phenotype reconstruction.

3D reconstruction has potential use in potato yield estimation, phenotypic studies, and quality grading. In the future, we hope to improve the performance of the system and reduce the measurement time by using depth cameras or coding structured light.



## VI. ACKNOWLEDGMENT

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