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# Super Twisting Fractional Order Energy Management Control for a Smart University System Integrated DC Micro-Grid

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**ABSTRACT** This paper designs an intelligent energy management control for a stand alone smart DC-micro-grid using super twisting fractional order method. Based on mathematical model of the micro-grid, controllers are derived for the source side converters such as photovoltaic (PV), wind, AC grid and battery management system, and load side converters. Based on the available measured input and consumed output power, an intelligent energy management algorithm decides the appropriate mode of operation for the source and load side converters controller. All DC loads connected to the micro-grid are treated as essential loads and no load shedding can be allowed by the energy management unit. The energy management unit prioritizes the renewable energy sources (PV and wind) in order to make the micro-grid as cost effective. The performance of the proposed control scheme is compared with the integer order controller and the system is simulated in MATLAB/SIMULINK environment for different test cases.

**INDEX TERMS** DC micro-grid, robust control, sliding mode control, fractional calculus, energy management.

## I. INTRODUCTION

In order to meet the raising power demands of the communities around the globe, generation from traditional power sources is no more a viable choice due to the emission of green house gases and the environmental problems [1]. In order to minimize the emission of green house gases and to reduce environmental pollution, the bulk power is now generated from the clean renewable energy sources such as photo voltaic (PV), wind, sea waves and fuel cells. The renewable energy sources are either integrated together to form standalone micro-grids or the available power from such sources is transferred to the existing power grids [2], [3]. Due to stochastic nature of renewable energy sources, auxiliary power sources such as energy storage system must be integrated to the system as a backup power sources [3], [4].

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Usually it is preferred to integrate different clean power sources such as PV, wind and fuel cells [5], [6], because the combination of several such power sources with stochastic nature may have a positive impact on the maximum capacity of the energy storage system [7]. The combination of battery and ultra capacitor is utilized as energy storage system when a fast response of the system is required to compensate the transients. [8], [9]. Such combination can extend the life time of the battery storage system, however where all connected loads are essential, then instead of ultra capacitor AC grid is utilized as a back power source [9]. The integration of all power sources with battery storage system forms a micro-grid. A micro-grid is further categorized as either direct current (DC) or alternating current (AC) or a combination of AC and DC types. In comparison to AC micro-grid, DC offers several advantages such as its simple structure, few parameters to control and ease of installation and integration [10], [11]. On the other hand, an AC micro-grid

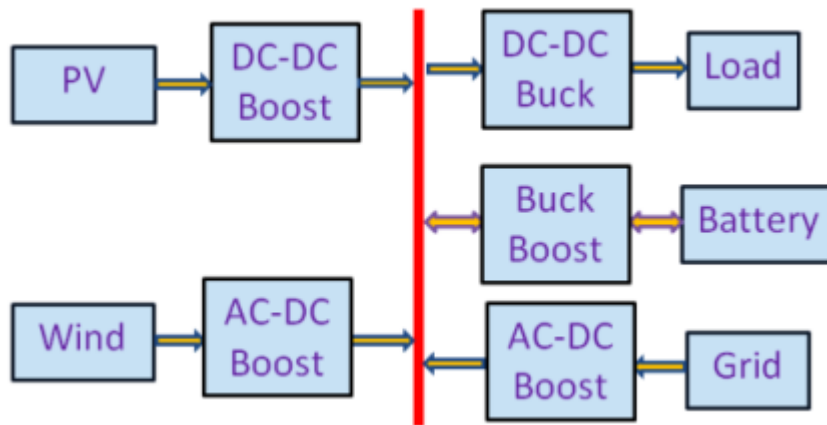


FIGURE 1. Block diagram of smart DC Micro-Grid.

requires additional parameters such as reactive power control and frequency synchronization, thus the control algorithm is computationally more complex [12], [13]. DC micro-grid can operate in several modes such as standalone, integrated with AC micro-grid or main AC grid. Due to the recent advances in power electronics switches, the standalone DC micro-grid can operate on maximum efficiency, however due to stochastic nature of the power sources, an additional energy management unit is required for the smooth operation and for the delivery of uninterrupted power to the loads. Several control methods integrated with energy management units have been reported for AC micro-grids [13]–[17], however since the dynamics of AC and DC quantities are different so the reported methods cannot be utilized for the DC micro-grids. In a typical DC micro-grid configuration, the source and load converters are connected in parallel to each other and energy is supplied or consumed from the main voltage bus referred as DC link. The mathematical dynamics of the system are non linear and coupled. The stabilization of DC link voltage is required for stable operation of the DC micro-grids [18]. Since the system dynamics are coupled, so the stabilization of DC link voltage is a difficult task to achieve and it requires sophisticated control methods [19], [21]. Linear control methods are often easy to implement. In [19], [22], [23], linear controllers are reported for the DC link voltage stabilization problem. However the utilized dynamic models are linear in nature and thus the proposed linear controllers can regulate the DC link voltage in a small operating envelop. Apart from linear controllers, several robust controllers have been reported in the literature such as Robust  $H_\infty$  control technique in [24], adaptive droop control method in [25], non-linear sliding mode control in [26], [27], feedback linearization method in [28] and Lyapunov based method in [29]. The literature reported in [24]–[29] offer several limitations such as lack of rigorous stability analysis in case of  $H_\infty$  method, poor performance of droop control based methods with several sources integrated together, chattering problem in sliding mode control method, small operating envelop in

case of general linearization method. The Lyapunov based method showed promising performance, however the energy management unit is not reported in subject work. In [30], [31], centralized robust and optimal controllers are reported for stability issues in DC micro-grid, however the effects of communication link such as network delays and its failure have not investigated. In [32]–[38] several other nonlinear control methods have been proposed with energy management units but all the presented methods are integer order. Fractional order controllers offer additional advantages over integer order controllers such as high degree of freedom, robust behavior to the measurement noise and oscillations. Several fractional order controllers have been reported in the literature such as DC-DC converters feeding constant power loads [31], robust non integer controller applied to nonlinear dynamic system [38], [39] and fuzzy fractional controller to servo systems [40], [41].

Based on the above literature survey, this paper proposes a decentralized super twisting fractional order control integrated with energy management unit for the proposed DC micro-grid shown in Figure 1. The proposed fractional order controllers will serve as low-level control. The high level control is managed by the energy management unit which monitors the generated and consumed power and generate appropriate references for the low level control. Major contributions of this research work are as following.

**1:** According to the author,s best knowledge, fractional order controllers have never been exploited for a DC- micro-grid integrated with several stochastic sources and essential DC loads.

**2:** The proposed fractional order controllers offer minimum oscillations in the DC link voltage, thus enhancing the stability of the system.

**3:** Large signal model of the DC micro-grid is utilized for controller formulation with power stage parameters uncertainty.

**4:**Global stability of the closed loop system is ensured using fractional order Lyapunov theorem.

5: In the reported back-stepping control methods for DC micro-grids, the inner loop current references are set by the outer voltage loops, while the proposed sliding surfaces offer flexibility in adjusting the reference currents from user input or from energy management unit in a convenient way.

The rest of the paper is organized as follows: Section II describes the system configuration of the DC micro-grid, mathematical modeling is performed in Section III, Controllers are derived in Section IV, the energy management unit is discussed in Section V, results are discussed in Section VI and finally the conclusion is made in Section VII.

## II. SYSTEM DESCRIPTION

Figure 1 shows the block diagram of a smart DC Micro-Grid. The sources include solar PV, wind and main ac grid. Apart from the sources, a battery storage system is also interfaced to the main DC bus. All sources are interfaced to the DC link via DC-DC converters. The battery storage system is connected through a bi directional buck-boost converter. As shown in the block diagram, the loads are driven by the load side converters. All loads are assumed to be priority loads that may include lighting, fans, and laboratory test benches for students experimentation. The power management unit calculates the total generated and consumed power and based on it, the appropriate control modes are utilized. The specifications of the system are tabulated in the results and discussion section.

## III. MATHEMATICAL MODELING

**1. Source Side Converters:** In this section, the mathematical models for source-side converters are presented. Based on the presented models, the controllers are derived using fractional calculus. Basic fractional mathematics is given in Appendix-I.

### A. PV CONVERTER SYSTEM MODEL

The PV converter system connected to the DC bus is shown in Figure 2. A boost converter is used to integrate the solar power to the main DC bus. The mathematical model for PV converter system can be written as:

$$\frac{dV_{pv}}{dt} = \frac{I_{pv}}{C_p} - \frac{I_{L_{pv}}}{C_p} \tag{1}$$

$$\frac{dI_{L_{pv}}}{dt} = \frac{V_{pv}}{L_{pv}} - (1 - U_1) \frac{V_{dc}}{L_{pv}} + D_1 \tag{2}$$

$$\frac{dV_{dc}}{dt} = (1 - U_1) \frac{I_{L_{pv}}}{C_{dc}} - \frac{I_{o_{pv}}}{C_{dc}} + D_2 \tag{3}$$

where  $V_{pv}$  represents the PV input voltage,  $I_{pv}$  is the PV current,  $I_{L_{pv}}$  represents inductor current,  $V_{dc}$  represents dc link voltage,  $L_{pv}$  represents the inductance and  $U_1$  is the control signal. The terms  $D_1$  and  $D_2$  represent the uncertainty dynamics in the power stage parameters.

### B. WIND CONVERTER SYSTEM MODEL

The wind converter system connected to the DC bus is shown in Figure 3. A rectifier is used to convert the alternating power

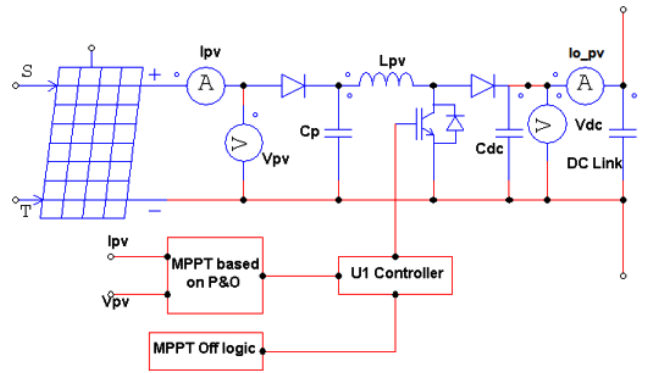


FIGURE 2. Block diagram of PV converter module.

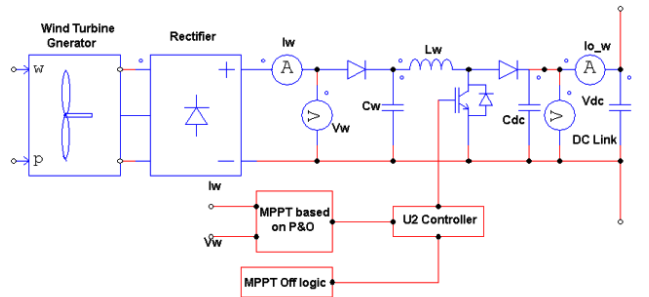


FIGURE 3. Block diagram of wind converter module.

to direct power and then a boost converter is used to integrate the wind power to the main DC bus. The mathematical model of the wind converter system is derived as following.

$$\frac{dV_w}{dt} = \frac{I_w}{C_w} - \frac{I_{L_w}}{C_w} \tag{4}$$

$$\frac{dI_{L_w}}{dt} = \frac{V_w}{L_w} - (1 - U_2) \frac{V_{dc}}{L_w} + D_3 \tag{5}$$

$$\frac{dV_{dc}}{dt} = (1 - U_2) \frac{I_{L_w}}{C_{dc}} - \frac{I_{o_w}}{C_{dc}} + D_4 \tag{6}$$

where  $V_w$  represents the wind rectified voltage input to the boost converter,  $I_w$  is the rectified wind current,  $I_{L_w}$  represents inductor current,  $V_{dc}$  represents dc link voltage,  $L_w$  represents the inductance and  $U_2$  is the control signal. The terms  $D_3$  and  $D_4$  represent the uncertainty dynamics in the power stage parameters.

### C. AC GRID CONVERTER SYSTEM MODEL

The AC grid converter system is similar to the wind converter system. A rectifier is used to convert the alternating power to direct power, then a boost converter is used to integrate the main AC grid into the DC bus. The mathematical model of the wind converter system is derived as follows:

$$\frac{dV_g}{dt} = \frac{I_g}{C_g} - \frac{I_{L_g}}{C_g} \tag{7}$$

$$\frac{dI_{L_g}}{dt} = \frac{V_g}{L_g} - (1 - U_3) \frac{V_{dc}}{L_g} + D_5 \tag{8}$$

$$\frac{dV_{dc}}{dt} = (1 - U_3) \frac{I_{L_g}}{C_{dc}} - \frac{I_{o_g}}{C_{dc}} + D_6 \tag{9}$$

where  $V_g$  represents the grid rectified voltage input to the grid boost converter,  $I_g$  is the rectified grid current,  $I_{L_g}$  represents inductor current,  $V_{dc}$  represents dc link voltage,  $L_g$  represents the inductance of the grid, s converter and  $U_3$  is the control signal. The terms  $D_5$  and  $D_6$  represent the uncertainty dynamics in the power stage parameters. Here it is worth to mention that the supply of the grid power is assumed to be constant so no MPPT will be employed for the grid converter system.

### D. BATTERY STORAGE CONVERTER SYSTEM MODEL

Block diagram of battery storage system is shown in Figure 4. A buck boost converter is used for the integration of battery storage system to the main DC bus of the micro-grid. Depending on the state of charge (SOC), source side power availability and load side power demand, battery storage system can work either in charging or discharging mode. In charging mode, power from the main bus is transferred to the batteries and, therefore, the converter works in buck mode. When power is supplied back to the micro-grid, the battery converter operates in boost mode. The mathematical model of the battery converter system is derived as following.

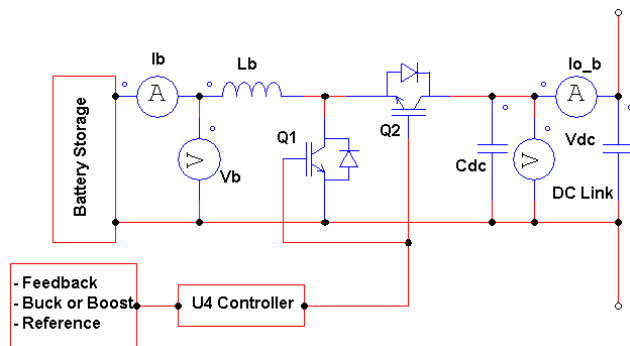


FIGURE 4. Battery storage converter module.

**1. Boost mode:** In boost mode, the reference battery current generated by the energy management system is positive. So the boost mode is modeled as follows:

$$\frac{dI_b}{dt} = \frac{V_b}{L_b} - (1 - U_{Q1}) \frac{V_{dc}}{L_b} + D_7 \quad (10)$$

$$\frac{dV_{dc}}{dt} = (1 - U_{Q1}) \frac{I_b}{C_{dc}} - \frac{I_{o_b}}{C_{dc}} + D_8 \quad (11)$$

where  $V_b$  represents the battery voltage,  $I_b$  is the battery current, and  $U_{Q1}$  is the control signal. The terms  $D_7$  and  $D_8$  represent the uncertainty dynamics in the power stage parameters.

**2. Buck mode:** In buck mode, the reference battery current generated by the energy management system is negative. So the buck mode is modeled as follows:

$$\frac{dI_b}{dt} = \frac{V_b}{L_b} - U_{Q2} \frac{V_{dc}}{L_b} + D_7 \quad (12)$$

$$\frac{dV_{dc}}{dt} = U_{Q2} \frac{I_b}{C_{dc}} - \frac{I_{o_b}}{C_{dc}} + D_8 \quad (13)$$

where  $U_{Q2}$  is the control signal in buck mode. The generalized model representing the buck and boost mode is expressed as follows:

$$\frac{dI_b}{dt} = \frac{V_b}{L_b} - U_4 \frac{V_{dc}}{L_b} + D_7 \quad (14)$$

$$\frac{dV_{dc}}{dt} = U_4 \frac{I_b}{C_{dc}} - \frac{I_{o_b}}{C_{dc}} + D_8 \quad (15)$$

where  $U_4 = sw(1 - U_{Q1}) + (1 - sw)U_{Q2}$ . When  $sw = 0$  the buck mode controller  $U_{Q2}$  is activated and with  $sw = 1$ , the boost mode control  $U_{Q1}$  is active.

### E. SOURCE SIDE CONVERTERS GENERALIZED MODEL

In order to avoid the derivation of controllers for each source side converter, the mathematical models presented in Eqs.(1)-(9) and Eqs (14)-(15) are expressed in generalized form as following:

$$\frac{dV_J}{dt} = \frac{I_J}{C_K} - \frac{I_{L_J}}{C_K} \quad (16)$$

$$\frac{dI_{L_J}}{dt} = \frac{V_J}{L_J} - (1 - U_i) \frac{V_{dc}}{L_J} + D_i \quad (17)$$

$$\frac{dV_{dc}}{dt} = (1 - U_i) \frac{I_{L_J}}{C_{dc}} - \frac{I_{o_J}}{C_{dc}} + D_{i+1} \quad (18)$$

In Eqs. (16)-(18), the subscript  $J$  represents the sub subscripts  $pv$ ,  $wind$ ,  $g$  and  $b$ , while subscript  $K$  represents the sub subscripts  $P$ ,  $w$  and  $g$ . The term  $i$  is 1 for  $pv$ , 2 for  $w$ , 3 for  $g$  and 4 for subscript  $b$ .

**2. Load Side Converters:** As shown in Figure 1, DC priority loads are connected through parallel DC/DC buck converters. Parallel converters are used to divide the load and reduce the stress on each converter. Moreover the DC loads are constant power loads.

The generalized model for  $p$  buck converters connected in parallel is expressed as following.

$$\frac{dI_{L_p}}{dt} = \frac{U_p V_{dc}}{L_p} - \frac{V_{load_p}}{L_p} + D_{I_{L_p}} \quad (19)$$

$$\frac{dV_{load_p}}{dt} = \frac{I_{L_p}}{C_p} - \frac{V_{load_p}}{R_{L_p} C_p} + D_{V_{load_p}} \quad (20)$$

where  $p = 1, 2, 3 - n$  which represents the number of buck converters,  $I_{L_p}$  represents inductor current,  $V_{load_p}$  is the load voltage,  $L_p$  represents the inductance,  $C_p$  represents the output capacitance and  $U_p$  is the generalized control law.  $D_{I_{L_p}}$  represents the uncertainty in the current dynamics while  $D_{V_{load_p}}$  is the uncertainty of voltage dynamics.

### IV. CONTROL SYSTEM FORMULATION

In this section the control system is derived for both source and load side converters of the proposed micro-grid based on fractional order super twisting method. Before going into the detailed derivations, the super twisting control is briefly explained. Referring to [31], [42], the super twisting control system consists of two parts. The first part is called the equivalent control which is derived based on system nominal model. The second part is the switching control part that is

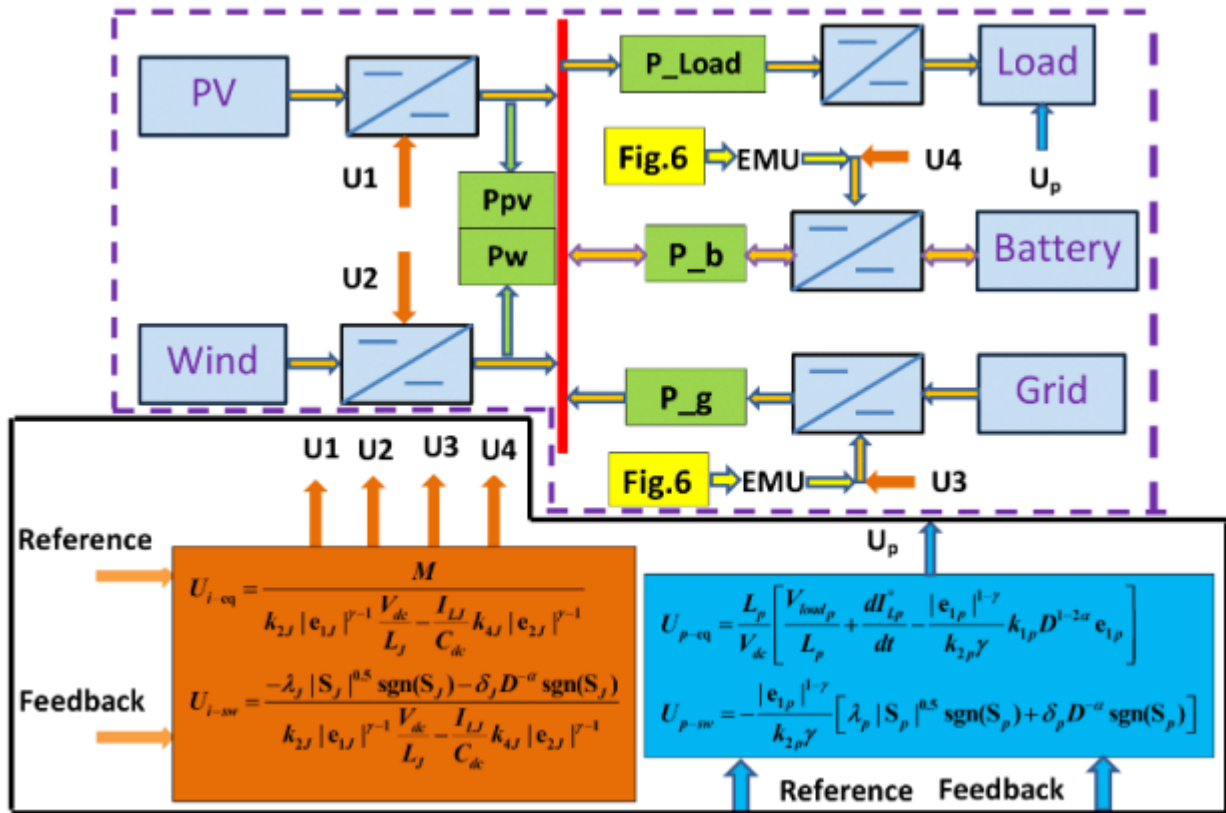


FIGURE 5. Control System block diagram.

based on the signum function and a nonlinear sliding surface. In comparison to the classical sliding mode control, the sliding surface is nonlinear in super twisting control system. As shown from Fig. 1-5, there are four source side and two load side converters, so the source side controllers [U1 – U4] are generalized in the system model of Eq. 16-18 as  $U_i$ . Similarly the load side controllers are generalized as  $U_p$  given in Eq. 19-20. So  $U_i$  is derived for source side and  $U_p$  for load side converters. A simplified diagram explaining the the overall control and energy management unit of the micro-grid is shown in Fig. 5

**1 Source side converters control:** In this section the control law is derived based on the generic mathematical model presented in Eqs. (16)-(18). Eq. (16) is used to generate reference current  $I_{Lj}$  for pv, w and g while for the battery storage system, this reference current is generated by the energy management system. To derive the control law, let a Lyapunov function is expressed as  $V_{J1} = 0.5 e_j^2$ . Where the error  $e_j$  and its first derivative are expressed as follows.

$$e_j = C_K (V_j - V_j^*) \tag{21}$$

$$\dot{e}_j = C_K (\dot{V}_j - \dot{V}_j^*) \tag{22}$$

Here  $V_j^*$  represents the reference voltage command. By combining Eq. (16) and (22), one obtains the following relation.

$$\dot{e}_j = (I_j - I_{Lj} - C_K \dot{V}_j^*) \tag{23}$$

The reference current  $I_{Lj}$  is calculated from Eq. (23) and it is expressed as follows:

$$I_{Lj}^* = -C_K \dot{V}_j^* + I_j + k_j e_j \tag{24}$$

By combining the first derivative of  $V_{J1}$  with Eq. (24), yields the following expression:

$$\dot{V}_{J1} = -k_j e_j^2 \tag{25}$$

where  $k_j$  represents the gain matrix and by choosing  $k_j > 0$ , Eq. (25) is always negative definite. The reference current for the battery storage system is generated by energy management system.  $I_{Lj}^*$  represents virtual control law. To derive the actual control system  $U_i$ , fractional order sliding manifold is chosen in the light of the concepts presented in [31] as follows:

$$S_j = k_{1j} D^{-\alpha} e_{1j} + k_{2j} D^{\alpha} |e_{1j}|^{\gamma} \text{Sgn}(e_{1j}) + k_{3j} D^{-\alpha} e_{2j} + k_{4j} D^{\alpha} |e_{2j}|^{\gamma} \text{Sgn}(e_{2j}) \tag{26}$$

In Eq. (26),  $k_{1j}$ ,  $k_{2j}$ ,  $k_{3j}$  and  $k_{4j}$  represent the gain matrix. The above sliding surface is chosen based on the concepts presented in [31]. The main difference of the proposed sliding surface in comparison with [31] is highlighted as follows: **a.** The proposed sliding surface of Eq. (26) has different dynamics in terms of fractional integration and derivative. **b.** The proposed sliding surface of Eq. (26) is proposed for  $J$  number of variables. Moreover the error  $e_{1j}$  and  $e_{2j}$  represent

the current and dc link voltage errors, respectively defined as follows:  $e_{1J} = I_{LJ} - I_{LJ}^*$ ,  $\dot{e}_{1J} = \dot{I}_{LJ} - \dot{I}_{LJ}^*$  and  $e_{2J} = V_{dc} - V_{dc}^*$ ,  $\dot{e}_{2J} = \dot{V}_{dc} - \dot{V}_{dc}^*$ . By taking the first derivative of Eq. (26) with respect to time, one obtains the following relation:

$$\dot{S}_J = k_{1J}D^{1-\alpha}e_{1J} + k_{2J}D^\alpha\gamma|e_{1J}|^{\gamma-1}\dot{e}_{1J} + k_{3J}D^{1-\alpha}e_{2J} + k_{4J}D^\alpha\gamma|e_{2J}|^{\gamma-1}\dot{e}_{2J} \quad (27)$$

By combining Eqs. (17) and (18) with Eq. (27) and multiply  $D^{-\alpha}$  to both hand sides of the resultant expression, we get the following relation:

$$D^{1-\alpha}S_J = k_{1J}D^{1-2\alpha}e_{1J} + k_{2J}\gamma|e_{1J}|^{\gamma-1}\left[\frac{V_J}{L_J} - (1-U_i)\frac{V_{dc}}{L_J} + D_i - \dot{I}_{LJ}^*\right] + k_{3J}D^{1-2\alpha}e_{2J} + k_{4J}\gamma|e_{2J}|^{\gamma-1}\left[(1-U_i)\frac{I_{LJ}}{C_{dc}} - \frac{I_{oJ}}{C_{dc}} + D_{i+1} - \dot{V}_{dc}^*\right] \quad (28)$$

After expanding Eq. (28) and separating the terms containing  $U_i$ , the resultant equation is expressed as follows:

$$D^{\bar{\alpha}}S_J = k_{1J}D^{1-2\alpha}e_{1J} + k_{2J}\gamma|e_{1J}|^{\gamma-1}\left[\frac{V_J}{L_J} - \frac{V_{dc}}{L_J} + D_i - \dot{I}_{LJ}^*\right] + k_{3J}D^{1-2\alpha}e_{2J} + k_{4J}\gamma|e_{2J}|^{\gamma-1}\left[\frac{I_{LJ}}{C_{dc}} - \frac{I_{oJ}}{C_{dc}} + D_{i+1} - \dot{V}_{dc}^*\right] + U_i\left[k_{2J}\gamma|e_{1J}|^{\gamma-1}\frac{V_{dc}}{L_J} - \frac{I_{LJ}}{C_{dc}}k_{4J}\gamma|e_{2J}|^{\gamma-1}\right] \quad (29)$$

In Eq. (29), the operator  $D^{\bar{\alpha}}$  is equal to  $D^{1-\alpha}$  and it represents a fractional order derivative term. Using Eq. (29), the control law  $U_i$  is simplified as follows:

$$U_i = \frac{M - \lambda_J|S_J|^{0.5}sgn(S_J) - \delta_J D^{-\alpha}sgn(S_J)}{[k_{2J}\gamma|e_{1J}|^{\gamma-1}\frac{V_{dc}}{L_J} - \frac{I_{LJ}}{C_{dc}}k_{4J}\gamma|e_{2J}|^{\gamma-1}]} \quad (30)$$

In Eq. (30),  $M$  is expressed as follows:

$$M = -k_{1J}D^{1-2\alpha}e_{1J} - k_{2J}\gamma|e_{1J}|^{\gamma-1}\left[\frac{V_J}{L_J} - \frac{V_{dc}}{L_J} - \dot{I}_{LJ}^*\right] - k_{3J}D^{1-2\alpha}e_{2J} - k_{4J}\gamma|e_{2J}|^{\gamma-1}\left[\frac{I_{LJ}}{C_{dc}} - \frac{I_{oJ}}{C_{dc}} - \dot{V}_{dc}^*\right] \quad (31)$$

In Eq. (31),  $\lambda_J$  and  $\delta_J$  represent gain of super-twisting sliding mode reaching law. The stability proof is given in Appendix III.

**2. Load converters control:** The generalized state space model for the load side converters is derived in Eqs. (19) and (20). To derive the control law  $U_p$ , let a Lyapunov function is expressed as  $V_p = 0.5 e_p^2$ . Therefore error  $e_p$  and its first derivative are expressed as follows:

$$e_p = C_p(V_{loadp} - V_{loadp}^*) \quad (32)$$

$$\dot{e}_p = C_p(\dot{V}_{loadp} - \dot{V}_{loadp}^*) \quad (33)$$

By combining Eq. (20) and (33), one obtains the following relation:

$$\dot{e}_p = (I_{Lp} - \frac{V_{loadp}}{R_{Lp}} + C_p D V_{loadp} - C_p \dot{V}_{loadp}^*) \quad (34)$$

The reference current  $I_{Lp}$  is calculated from Eq. (34) and it is expressed as follows:

$$I_{Lp}^* = \frac{V_{loadp}}{R_{Lp}} + C_p \dot{V}_{loadp}^* - k_p e_p - y_p sgn(e_p) \quad (35)$$

By combining the first derivative of  $V_p$  with Eq. (35) yields the following expression:

$$\dot{V}_p = -k_p e_p^2 - y_p |e_p| \quad (36)$$

where  $k_p$  and  $y_p$  represent the gain matrix and by choosing  $k_p > 0$  and  $y_p > D V_{loadp(max)}$ , Eq. (36) is always negative definite.

To derive the actual control law  $U_p$ , fractional order sliding manifold is chosen as follows:

$$S_p = k_{1p}D^{-\alpha}e_{1p} + k_{2p}D^\alpha|e_{1p}|^\gamma Sgn(e_{1p}) \quad (37)$$

In Eq. (37),  $k_{1p}$  and  $k_{2p}$  represent the gain matrix. Moreover, the error  $e_{1p}$  represents the current error defined as follows:  $e_{1p} = I_{Lp} - I_{Lp}^*$  and  $\dot{e}_{1p} = \dot{I}_{Lp} - \dot{I}_{Lp}^*$ . By taking the first derivative of Eq. (37), one obtains the following relation:

$$\dot{S}_p = k_{1p}D^{1-\alpha}e_{1p} + k_{2p}D^\alpha\gamma|e_{1p}|^{\gamma-1}\dot{e}_{1p} \quad (38)$$

By combining Eq. (19) and  $\dot{e}_{1p}$  with Eq. (38), and multiply  $D^{-\alpha}$  to both hand sides of the resultant expression, we get the following relation:

$$D^{\bar{\alpha}}S_p = D^{1-\alpha}S_p = k_{1p}D^{1-2\alpha}e_{1p} + k_{2p}\gamma|e_{1p}|^{\gamma-1}\left[\frac{U_p V_{dc}}{L_p} - \frac{V_{loadp}}{L_p} + D_{I_{Lp}} - \dot{I}_{Lp}^*\right] \quad (39)$$

where the operator  $D^{\bar{\alpha}}$  is equal to  $D^{1-\alpha}$  and it represents a fractional order derivative term. Using Eq. (39), the control system  $U_p$  is simplified as following.

$$U_p = \frac{L_p}{V_{dc}}\left[\frac{V_{loadp}}{L_p} + \dot{I}_{Lp}^* - \frac{|e_{1p}|^{1-\gamma}}{k_{2p}\gamma}\right] + [k_{1p}D^{1-2\alpha}e_{1p} + \lambda_p|S_p|^{0.5}sgn(S_p) + \delta_p D^{-\alpha}sgn(S_p)] \quad (40)$$

where  $\lambda_p$  and  $\delta_p$  represent gain of super-twisting sliding mode reaching law. To prove the stability of the closed loop system, the Lyapunov function can be expressed as:  $V_{U_p} = 0.5 S_p^2$ . By utilizing the concepts presented in the stability proof of the source converters control section, it is very to show that  $D^{\bar{\alpha}}S_p \leq 0$ .

## V. ENERGY MANAGEMENT UNIT

In this section the energy management algorithm is discussed briefly. The unit measures the input power available from the PV and wind sources. Similarly, the consumed power on the load side is also measured and then based on a power balance equation, the energy management algorithm is developed which is shown in Figure 6. Input sources such as PV and wind systems are utilized on priority to feed the loads. In the case of abundant power from input sources, the additional

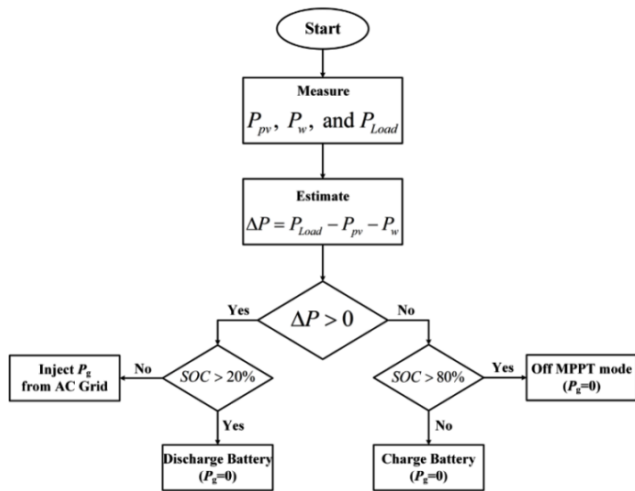


FIGURE 6. Energy management module.

power is used to charge the energy storage system. Usually in normal working conditions, no power is drawn from the AC grid. In a situation, when the power available from the PV, wind and battery storage system is not enough to drive the loads, then power from the AC grid is drawn to drive the loads. The power balance equation is expressed as follows:

$$P_w + P_{pv} + P_g = P_{Load} + P_{Battery} \quad (41)$$

When  $P_{Load} - (P_w + P_{pv}) > 0$  then  $P_g = 0$  and  $P_{Battery}$  is supplied to the loads until the state of charge (SOC) is above 20 percent. When the SOC is less than 20 percent, then  $P_g$  is adjusted as per the load demand and  $P_{Battery} = 0$ . In the second case when  $P_{Load} - (P_w + P_{pv}) < 0$  then  $P_g = 0$  and the  $P_{Battery}$  is absorbed from micro-grid to charge the battery storage system until the state of charge (SOC) is at maximum. The converters are operated on MPPT off mode when  $SOC > 80$  percent.

## VI. RESULTS AND DISCUSSION

In this section, the proposed controller is tested in simulation environment (MATLAB/Simulink) with the proposed DC micro-grid. All the parameters of the micro-grid subsystems and the controllers are tabulated in tables 1-4.

Overall the simulation results are focused on the verification of energy management unit (Figure 6) using the proposed control scheme. In the first case, fixed DC load of 8000 watts is connected through two load side converters to the DC voltage bus and state of charge (SOC) for battery storage system is initially set to 80 %. As shown in Figure 7a, the PV source is supplying fixed power of 2000 watts at a temperature of 25 degree Celsius and radiance of 600 watts/m<sup>2</sup>. The wind speed is varied between 8-13 m/s as shown in Fig. 7b and in response to it, the wind power is also varied between 4000 - 10000 watts which is shown in Figure 7c. Figure 8a shows the total power consumed by the load and it is around 8000 watts. The simulation results of the combined source power  $p_{dg}$

TABLE 1. Parameters of PV system.

PV panels	
Number of series strings	18
Number of parallel strings	5
Open circuit voltage	22V
Short circuit current	8.35A
Voltage at MPP	17.7V
Voltage at MPP	7.6A

TABLE 2. Parameters of wind energy system.

Wind Turbine	
Turbine output (Watts)	15000
Air density (Kg/m <sup>3</sup> )	1.225
Base wind speed(m/s)	15
PMSG(Generator)	
Generator (VA)	17000
Stator phase resistance (ohm)	1.36
Armature inductance (H)	0.0125
Flux linkage(wb)	1.44
Inertia ( kgm <sup>2</sup> )	0.1
Viscous damping( Nms)	0.0001
Pole pairs	4

TABLE 3. Parameters of battery storage system.

Lead acid battery	
Voltage (Volts)	261
Capacity (Ah)	208
Maximum Charge current(A)	25
Maximum discharge current(A)	40

TABLE 4. Converters and controllers parameters.

DC-DC converter parameters	
Inductance ( $[L_J]$ [ $L_p$ ])(mH)	([2.3, 5, 3.2, 4.1] [4.4, 4.4])
Capacitance ( $[C_K]$ [ $C_p]$ [ $C_{dc}$ ])(uF)	([3, 3, 200] [10, 10] [100])
Controller parameters	
Source side controller	
$\alpha$	0.25
$k_{1,J}$	[10, 5, 1.5, 15]
$k_{2,J}$	[5, 1.2, 10, 2.5]
$k_{3,J}$	[12, 3.5, 7.5, 10]
$k_{4,J}$	[12, 3.5, 7.5, 10]
$-\lambda_J$	[1.2, 1.2, 1.2, 1.2]
$-\delta_J$	[1.5, 1.5, 1.5, 1.5]
Load side controller	
$\alpha$	0.25
$k_{1,p}$	[1.5, 1.5]
$\gamma$	0.45
$k_{2,p}$	[1.2, 1.2]
$-\lambda_p$	[0.15, 0.15]
$-\delta_p$	[0.25, 0.25]

from both wind and PV sources are shown in Figure 8b. From the results presented, it is shown that  $p_{dg}$  increases from 6000-12000 watts during simulation time  $t = [3 - 6]s$ . Moreover since the consumed load power is fixed to 8000 watts (Figure 8a), while the combined source power  $p_{dg}$  is deficient in the time intervals  $[1 - 3]s$ ,  $[6 - 8]s$  and it is an excess amount for the time interval  $[3 - 6]s$ . With the above results presented,  $\Delta P = P_{Load} - (P_w + P_{pv}) > 0$  in the time intervals  $[0 - 3]s$ ,  $[6 - 8]s$  and  $\Delta P < 0$  for the time interval  $[3 - 6]s$ . As per the energy management algorithm of Figure 6, battery storage system will discharge to supply power to the

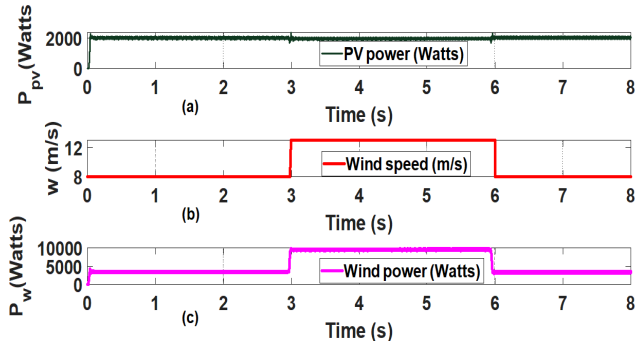


FIGURE 7. (a).PV power(Watts) (b). Wind speed (m/s) (c). Wind power (Watts).

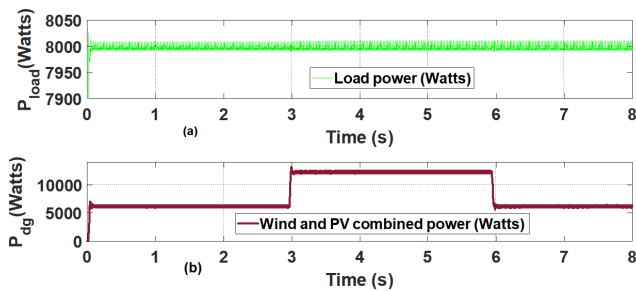


FIGURE 8. (a).Load power(Watts) (b). Wind and PV power (Watts).

micro-grid when  $\Delta P > 0$  and  $SOC > 20\%$ , and it will charge if  $\Delta P < 0$ .

Figure 9a, 9b and 9c show the battery power, SOC and grid power simulations with the available combined source power  $p_{dg}$  of Figure 8b. As shown in Figure 9a, the battery supplies approximately 2000 watts to the micro-grid in the time intervals  $[0 - 3]s$ ,  $[6 - 8]s$  when  $\Delta P > 0$  and  $SOC > 20\%$ , while in the time interval  $[3 - 6]s$  the micro-grid source power  $p_{dg}$  is more than the load power, so the battery is charged and it absorbs 4000 watts from the micro-grid. Figure 9b shows the SOC simulations. From the presented results it is noted that the SOC decreases in the time intervals  $[0 - 3]s$ ,  $[6 - 8]s$  and it increases in the time interval  $[3 - 6]s$ . Figure 9c shows the AC grid power supplied to the micro-grid. It is shown that  $p_g = 0$  in all time intervals. The reason is very obvious because the  $SOC > 20\%$ , so no power is drawn from the AC grid by the micro-grid. Load power is shared between the two load converters. Load converter-1 consumes 4600 watts and converter-2 draws the remaining power of 3400 watts from the micro-grid. Figure 10a, 10b and 10c show the current sharing, load 1 and load 2 output voltage regulations simulation results. Since the load is fixed, so the simulation results with the proposed control schemes are included in the paper. From the presented results, it is clear that under the action of the proposed control scheme, load power is appropriately shared between the two converters, while the output voltages of each converter are accurately regulated to the reference value of 220 volts.

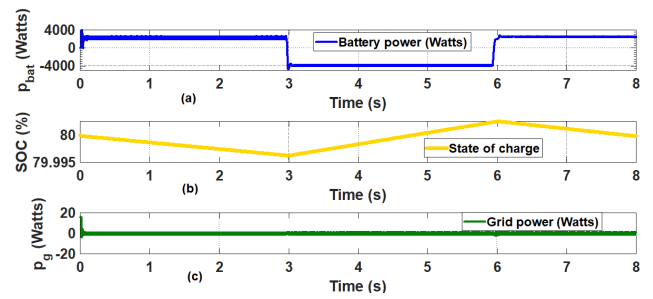


FIGURE 9. (a).Battery power(Watts) (b). SOC (%) c. Grid power (Watts).

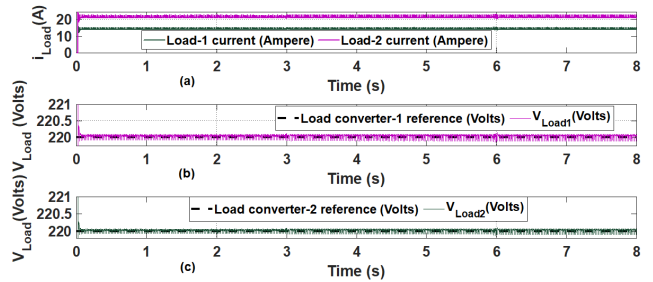


FIGURE 10. (a).Load sharing(Ampere) (b). Load-1 voltage c. Load-2 voltage.

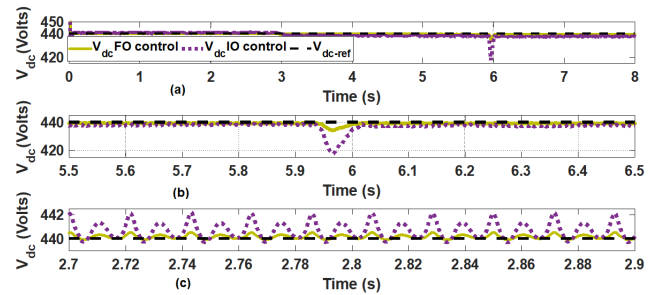


FIGURE 11. (a).Vdc regulation (b).Zoom in view1 c.Zoom in view2.

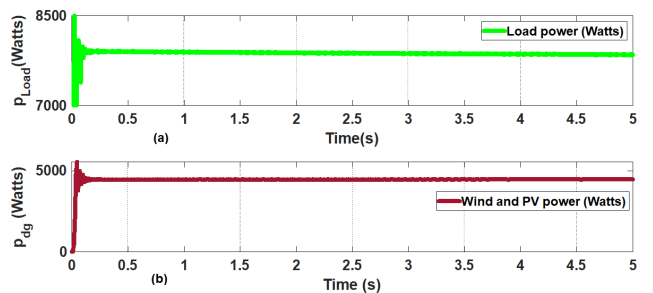


FIGURE 12. (a).Load power(Watts) (b). Wind and PV power (Watts).

It is also necessary to present a comparison of the proposed control system with its integer counter part. So an integer order controller is derived for the proposed micro-grid in Appendix-II. The stabilization of DC link voltage is very important because large fluctuations in it can cause system instabilities. Thus the results presented in Figure 11a, 11b and 11c give a fair performance comparison



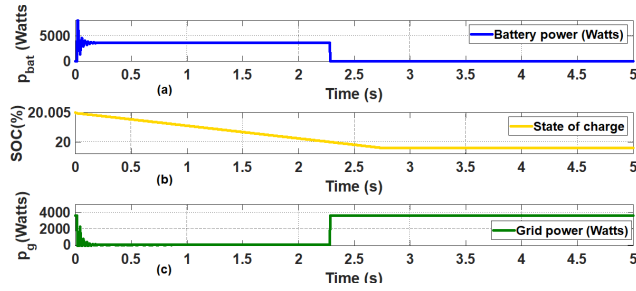


FIGURE 13. (a).Battery power(Watts) (b). SOC (%) c. Grid power (Watts).

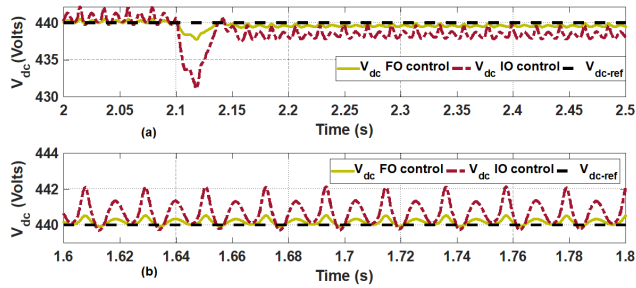


FIGURE 14. (a).Vdc regulation (b).Zoom in view1.

between the proposed and integer order control system given in Appendix-II. The load side converters are not considered as the loads are fixed. In the source side converters, the power stage parameters are subjected to uncertainty at time  $t = 6s$ . The uncertainty is introduced as following:  $L_J \pm 15\%L_J$ ,  $C_K \pm 15\%C_K$  and  $C_{dc} \pm 15\%C_{dc}$ . From the results presented in Figure 11, it is obvious that in the presence of the uncertainty and source side power variations, the proposed fractional order controller stabilizes the DC link voltage to its reference value (440 volts) with minimum oscillations and small steady state error.

The results presented in Figures 7-11 verify the proposed energy management system for all conditions when the state of charge of battery storage system, ( $SOC > 20\%$ ) and  $p_g = 0$ . In order to simulate the power injection mode from the main AC grid to the micro-grid, SOC of battery storage system is initially set to 20.005%. As shown in Fig. 12b, the combined source power  $p_{dg}$  is fixed at 4500 watts. Where out of 4500 watts, 2000 watts is contributed by PV sources as shown in Fig. 7a and the remaining 2500 watts is sourced from the wind power. Moreover fixed load of 8000 watts is connected to the micro-grid through two parallel load converters. The simulation results shown in Figure 12a and 12b show the available source power  $p_{dg}$  and load power. Now keeping in view this specific scenario,  $\Delta P > 0$  and hence the battery storage system will discharge and supply additional power to drive the loads until  $SOC > 20\%$ . Figure 13a, 13b and 13c show the simulation results of battery power, SOC and grid power. It is shown that in the time interval  $t = [0 - 2.4]s$ , the  $SOC > 20\%$  so the battery storage system is discharging and power is being supplied

to the micro-grid. In the same interval, the AC grid power  $p_g = 0$ . But when the  $SOC < 20\%$ , then the energy management disconnects the battery storage system and then power is supplied from the main AC grid. In order to compare the performance of the proposed controller with the integer order controller (Appendix-II), the source side converters are subject to the following uncertainty in its power stage parameters.  $L_J \pm 25\%L_J$ ,  $C_K \pm 10\%C_K$  and  $C_{dc} \pm 15\%C_{dc}$ . The uncertainty is introduced at time  $t = 2.1s$ . From the results presented in Figure 14a and 14b, it is obvious that in the presence of the uncertainty, the proposed fractional order controller stabilizes the DC link voltage to its reference value (440 volts) with minimum oscillations and small steady state error as compared to its integer order counter part controller.

## VII. CONCLUSION

In this work, a generalized nonlinear model of a DC micro-grid converters system is developed to formulate the proposed controller. All DC loads connected to the micro-grid are treated as essential loads and no load-shedding can be allowed by the energy management unit. An energy management unit is utilized to activate the appropriate mode of the controllers based on the measured source and load powers. The energy management unit prioritizes the renewable energy sources (PV and wind) in order to make the micro-grid as cost effective with essential loads and no load-shedding scheme. The proposed controller is successfully implemented and the energy management algorithm is verified. Moreover the performance of the proposed fractional order controller is compared with the integer order controller (Appendix-II) under system parameters uncertainty. The proposed controller showed superior performance over the integer control scheme.

## APPENDIX APPENDIX-I

Basics of the fractional mathematics is explained here.

*Definition 1:* The Riemann–Liouville fractional order integration and derivative of a function  $f(t)$  are expressed as following [39]–[41].

$${}_{t_0}I_t^\alpha f(t) = D_t^{-\alpha} f(t) = \frac{1}{\Gamma(\alpha)} \int_{t_0}^t \frac{f(\tau)}{(t-\tau)^{1-\alpha}} d\tau \quad (42)$$

$${}_{t_0}D_t^\alpha f(t) = \frac{d^\alpha}{dt^\alpha} f(t) = \frac{1}{\Gamma(m-\alpha)} \frac{d^m}{dt^m} \int_{t_0}^t \frac{f(\tau)}{(t-\tau)^{\alpha-m+1}} d\tau \quad (43)$$

where  $\Gamma(\cdot)$  represents the gamma function,  $m \in \mathbb{N}$  and  $m-1 < \alpha \leq m$

Using Eq. (42) and Eq. (43) the following relation holds:  ${}_{t_0}D_t^\alpha ({}_{t_0}I_t^\alpha f(t)) = f(t)$

**Definition 2:** The Caputo fractional order derivative of a function  $f(t)$  is given by [38], [39].

$${}_{t_0}D_t^\alpha f(t) = \begin{cases} \frac{1}{\Gamma(m-\alpha)} \int_{t_0}^t \frac{f^{(m)}(\tau)}{(t-\tau)^{\alpha-m+1}} d\tau; & m-1 < \alpha < m \\ \frac{d^m}{dt^m} f(t); & \alpha = m \end{cases} \quad (44)$$

The following relation also holds true for Caputo definitions:  ${}_{t_0}D_t^\alpha ({}_{t_0}I_t^\alpha f(t)) = f(t)$ . Rieman-Liouville and Caputo definitions are very much similar; the only difference lies in dealing with the initial conditions. In Rieman-Liouville definition, the initial conditions are non-integer while for Caputo definition they are of integer order.

**APPENDIX-II**

In this appendix the integer order controllers for source side converters are derived. Let an integer order sliding manifold is chosen as follows:

$$S_J = k_{1J} \int e_{1J} + k_{2J} |e_{1J}|^\gamma Sgn(e_{1J}) + k_{3J} \int e_{2J} + k_{4J} |e_{2J}|^\gamma Sgn(e_{2J}) \quad (45)$$

By taking the first derivative of Eq. (45), one obtains the following relation.

$$\dot{S}_J = k_{1J} e_{1J} + k_{2J} \gamma |e_{1J}|^{\gamma-1} \dot{e}_{1J} + k_{3J} e_{2J} + k_{4J} \gamma |e_{2J}|^{\gamma-1} \dot{e}_{2J} \quad (46)$$

By combining Eqs. (17) and (18) with Eq. (46), we get the following relation.

$$\begin{aligned} \dot{S}_J = & k_{1J} e_{1J} + k_{2J} \gamma |e_{1J}|^{\gamma-1} \left[ \frac{V_J}{L_J} - \frac{V_{dc}}{L_J} + D_i - \dot{I}_{L_J}^* \right] + k_{3J} e_{2J} \\ & + k_{4J} \gamma |e_{2J}|^{\gamma-1} \left[ \frac{I_{L_J}}{C_{dc}} - \frac{I_{oJ}}{C_{dc}} + D_{i+1} - \dot{V}_{dc}^* \right] \\ & + U_i [k_{2J} \gamma |e_{1J}|^{\gamma-1} \frac{V_{dc}}{L_J} - \frac{I_{L_J}}{C_{dc}} k_{4J} \gamma |e_{2J}|^{\gamma-1}] \end{aligned} \quad (47)$$

Using Eq. (47), the control system  $U_i$  is simplified as following.

$$U_i = \frac{M - \lambda_J |S_J|^{0.5} Sgn(S_J) - \delta_J \int Sgn(S_J)}{[k_{2J} \gamma |e_{1J}|^{\gamma-1} \frac{V_{dc}}{L_J} - \frac{I_{L_J}}{C_{dc}} k_{4J} \gamma |e_{2J}|^{\gamma-1}]} \quad (48)$$

In Eq. (48),  $M$  is expressed as following

$$\begin{aligned} M = & -k_{1J} e_{1J} - k_{2J} \gamma |e_{1J}|^{\gamma-1} \left[ \frac{V_J}{L_J} - \frac{V_{dc}}{L_J} - \dot{I}_{L_J}^* \right] \\ & - k_{3J} e_{2J} - k_{4J} \gamma |e_{2J}|^{\gamma-1} \left[ \frac{I_{L_J}}{C_{dc}} - \frac{I_{oJ}}{C_{dc}} - \dot{V}_{dc}^* \right] \end{aligned} \quad (49)$$

To prove the stability of the closed loop system, the Lyapunov function as expressed as:  $V_{U_i} = 0.5S_J^2$  By taking first derivative of the Lyapunov function and by combining it with Eq. (47), (48) and (49), it is easy to prove that  $\dot{V}_{U_i} \leq 0$

**APPENDIX III**

To prove the stability of the closed loop system, the Lyapunov function can be expressed as:  $V_{U_i} = 0.5S_J^2$  By applying fractional operator  $D^\alpha$  to the Lyapunov function:  $V_{U_i}$  yields the following expression [39]–[41].

$$D^{\bar{\alpha}} U_i \leq S_J D^{\bar{\alpha}} S_J + \sum_{l=1}^{\infty} \frac{\mathcal{T}(1+\bar{\alpha})}{\mathcal{T}(1+\bar{\alpha}-l)(1+l)} D^l S_J D^{\bar{\alpha}-l} S_J \quad (50)$$

Consider the following inequality:

$$\sum_{l=1}^{\infty} \frac{\mathcal{T}(1+\bar{\alpha})}{\mathcal{T}(1+\bar{\alpha}-l)(1+l)} D^l S_J D^{\bar{\alpha}-l} S_J \leq \zeta(S_J) \quad (51)$$

By combining Eqs. (29), (30), (50) and (51), the simplified equation can be expressed as follows:

$$\begin{aligned} D^{\bar{\alpha}} U_i \leq & S_J [-\lambda_J |S_J|^{0.5} Sgn(S_J) - \delta_J D^{-\alpha} Sgn(S_J) \\ & + k_{2J} \gamma |e_{1J}|^{\gamma-1} D_i + k_{4J} \gamma |e_{2J}|^{\gamma-1} D_{i+1}] + \zeta(S_J) \end{aligned} \quad (52)$$

Eq. (52) can be expressed as follows:

$$\begin{aligned} D^{\bar{\alpha}} U_i \leq & -\lambda_J |S_J|^{0.5} |S_J| - \delta_J D^{-\alpha} |S_J| \\ & + k_{2J} \gamma |e_{1J}|^{\gamma-1} S_J D_i + k_{4J} \gamma |e_{2J}|^{\gamma-1} S_J D_{i+1} + \zeta(S_J) \end{aligned} \quad (53)$$

In Eq. (53), by choosing  $\lambda_J$  and  $\delta_J$  such that the combined effect of the term  $-\lambda_J |S_J|^{0.5} |S_J| - \delta_J D^{-\alpha} |S_J|$  is more negative than the remaining terms  $k_{2J} \gamma |e_{1J}|^{\gamma-1} S_J D_i + k_{4J} \gamma |e_{2J}|^{\gamma-1} S_J D_{i+1} + \zeta(S_J)$ , then the fractional derivative of the Lyapunov function  $D^{\bar{\alpha}} U_i \leq 0$ . The condition is valid for both positive and negative values of sliding surface  $S_J$  subject to the condition that the maximum limits of disturbance terms  $|D_{i-max}|$  and  $|D_{i+1-max}|$  are known. With the above analysis, the reaching condition is achieved i.e.  $S_J = 0$ , then by multiplying Eq. (26) by  $D^{\alpha+1}$  the resultant expression can be written in the following form.

$$k_{1J} D^1 e_{1J} + k_{3J} D^1 e_{2J} = -D^{2\alpha} D^1 [k_{2J} |e_{1J}|^\gamma Sgn(e_{1J}) - k_{4J} |e_{2J}|^\gamma Sgn(e_{2J})] \quad (54)$$

In Eq. (54),  $D^1$  represents integer order derivative so the expression  $D^{2\alpha} D^1 [k_{2J} |e_{1J}|^\gamma Sgn(e_{1J}) - k_{4J} |e_{2J}|^\gamma Sgn(e_{2J})] = D^{2\alpha} [k_{2J} \gamma |e_{1J}|^{\gamma-1} \dot{e}_{1J} - k_{4J} \gamma |e_{2J}|^{\gamma-1} \dot{e}_{2J}]$ . By multiplying both hand sides of Eq. (54) by  $D^{-1}$ , the simplified equation is given as follows:

$$k_{1J} e_{1J} + k_{3J} e_{2J} = -D^{2\alpha-1} [k_{2J} \gamma |e_{1J}|^{\gamma-1} \dot{e}_{1J} - k_{4J} \gamma |e_{2J}|^{\gamma-1} \dot{e}_{2J}] \quad (55)$$

In Eq. (55), the left hand side terms are equated as:  $E_{surface} = k_{1J} e_{1J} + k_{3J} e_{2J}$ . Moreover, the term  $D^{2\alpha-1}$  represents the fractional integrator as long as  $\alpha < 0.5$ . With the condition specified on  $\alpha$ , Eq. (55) is simplified as follows:

$$\begin{aligned} E_{surface} = & -D^{2\alpha-1} [k_{2J} \gamma |e_{1J}|^{\gamma-1} \dot{e}_{1J} \\ & - k_{4J} \gamma |e_{2J}|^{\gamma-1} \dot{e}_{2J}] \end{aligned} \quad (56)$$

In Eq. (56),  $D^{-\bar{\alpha}} = D^{2\alpha-1}$  as long as  $\alpha < 0.5$ .

*Lemma 1.*: Fractional integral of a fractional derivative of a function  $f(t)$  is expressed as following [39]–[41]:

$${}_a D_t^{-\alpha} {}_a D_t^{\alpha} f(t) = f(t) - \sum_n^m [{}_a D_t^{\alpha-n} f(t)]_{t=a} \frac{[t-a]^{\alpha-n}}{\tau[\alpha-n+1]} \quad (57)$$

where  $\tau$  represents gamma function.

*Lemma 2.*: Fractional integral of a function  $f(t)$  is upper bounded such that following condition is true. [39]–[41]:

$$\|{}_a D_t^{-\alpha} f(t)\|_{\rho} \leq \psi_J \|f(t)\|_{\rho}; [1 \leq \psi_J \leq \infty; 1 \leq \rho \leq \infty] \quad (58)$$

All parameters of Eq. (57) and (58) are defined in [39]–[41]. *Lemma 1* is applied to the left hand side expression, while *Lemma 2* is applied to the right hand expression of Eq. (56). Mathematically the expression  $E_{surface} = D^{-\alpha} D^{\alpha} E_{surface}$  is valid. Therefore the application of *Lemma 1* to the above expression yields the following relations.

$$D^{-\alpha} D^{\alpha} E_{surface} = E_{surface} - [{}_t D_t^{\alpha-1} E_{surface}]_{t=t_r} \frac{(t-t_r)^{\alpha-1}}{\Gamma(\alpha)} \quad (59)$$

From Eq. (59), when  $t = t_r$  then  $D^{-\alpha} D^{\alpha} E_{surface} = E_{surface}$ . The expression  $E_{surface} = D^{-2} D^2 E_{surface}$  is also mathematically valid. So the application of *Lemma 1* to the above expression yields the following relation.

$$D^{-2} D^2 E_{surface} = E_{surface}(t) - [{}_t D_t^{2-1} E_{surface}]_{t=t_r} \frac{(t-t_r)^{2-1}}{2} - E_{surface}(t_r) \quad (60)$$

Therefore application of *Lemma 2* to the right hand terms of Eq. (56), yields the following relation:

$$-D^{2\alpha-1} [k_{2J} \gamma |e_{1J}|^{\gamma-1} \dot{e}_{1J} - k_{4J} \gamma |e_{2J}|^{\gamma-1} \dot{e}_{2J}] = -\psi_J [k_{2J} \gamma |e_{1J}|^{\gamma-1} \dot{e}_{1J} - k_{4J} \gamma |e_{2J}|^{\gamma-1} \dot{e}_{2J}] \quad (61)$$

By combining the terms in left hand side of Eq. (60) and (61), one obtains the following expression:

$$\|E_{surface}(t) - [{}_t D_t^{2-1} E_{surface}]_{t=t_r} \frac{(t-t_r)^{2-1}}{2} - [k_{2J} \gamma |e_{1J}|^{\gamma-1} \dot{e}_{1J} - k_{4J} \gamma |e_{2J}|^{\gamma-1} \dot{e}_{2J}]\| \leq -\|\psi_J [k_{2J} \gamma |e_{1J}|^{\gamma-1} \dot{e}_{1J} - k_{4J} \gamma |e_{2J}|^{\gamma-1} \dot{e}_{2J}]\| \quad (62)$$

In Eq. (62), by replacing  $t = t_{Sj}$ , the error terms  $e_{1J}$  and  $e_{2J}$  are zero. So the right hand side term and  $E_{surface}(t)$  are equal to zero. So the remaining expression is written as follows:

$$t_r \leq t_{Sj} - \frac{2E_{surface}(t_r)}{\dot{E}_{surface}(t_r)} \quad (63)$$

Eq. (63) shows that the convergence time of the proposed controller is finite.

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