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Current Prediction Error Reduction Method of Predictive Current Control for Permanent Magnet Synchronous Motors

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ABSTRACT Predictive current control (PCC) has been widely investigated in motor drive field. The PCC is a model-based control method and the motor prediction model is quite sensitive to motor parameters which may be inaccurately measured and change under different working conditions. In order to reduce the current prediction error of PCC caused by inductance mismatch, a current prediction error reduction method is proposed for permanent magnet synchronous motor (PMSM) by online inductance correction which is based on the relationship between inductance mismatch and current prediction error. Firstly, a proportional regulator is used to obtain the absolute correction value according to the relationship between inductance error and current prediction error. Secondly, the polarity of correction value is judged according to the fluctuation amplitudes of predicted current and actual current. Finally, an adaptive adjustment method for correction period is proposed to ensure the accuracy of inductance correction value. Experimental tests are carried out to verify the effectiveness of proposed method, and results show that the proposed method can obviously reduce current prediction error and improve control performance in practical applications. In addition, the proposed method is suitable for interior and surface mounted PMSMs.

INDEX TERMS Current prediction error reduction, online inductance correction, permanent magnet synchronous motor (PMSM), predictive current control (PCC).

I. INTRODUCTION

Permanent magnet synchronous motor (PMSM) is widely used in industrial products and electric vehicles due to its high power density and simple structure [1]–[4]. In motor control field, predictive current control (PCC) has been widely investigated and applied. The PCC is a model-based control method and it is quite sensitive to motor parameters [5]–[9]. However, the motor parameters cannot be measured accurately in actual applications, and they may vary under different working conditions [10]. Mismatch of motor parameters is the main reason causing current prediction error of PCC, and it may result in inaccurate prediction of motor motion behavior [11], [12].

In order to solve the above problem, scholars have proposed many methods to reduce the prediction error,

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including prediction error compensation methods, motor parameter identification methods, model-free prediction algorithms and so on.

For prediction error compensation methods, in [13], by adding discrete time integral term to current prediction stage, a discrete-time robust PCC method is proposed to compensate current prediction error. In [14], the prediction errors provided by each voltage vector are added to current prediction stage with a weighting factor, which can effectively improve the prediction accuracy. The current prediction errors are various under different switching states [15], so, a variable weighting factor is presented in [16] based on the position and magnitude of reference voltage. Although the error compensation method can effectively reduce the prediction error, it does not solve the fundamental problem that causes prediction error.

Parameter mismatch is the primary cause of current prediction error, so, some studies have focused on motor

parameter identification, such as parameter offline identification algorithm and parameter online identification algorithm. Among them, the offline parameter identification algorithms are mostly implemented by using high frequency voltage injection methods [17], adding low-pass filters [18] and so on.

Online parameter identification methods include particle swarm optimization algorithm [19], [20], current injection method [21], [22], novel affine projection algorithm [23], mean square identification algorithm [24] and recursive algorithm [25]. There are also some algorithms that consider inverter disturbance voltage and take advantage of motor parameter difference in dynamics when implementing online multi-parameter identification [26], [27]. Besides, many published references have constructed various observers to achieve online parameter identification. In [28], the extended state observer is proposed to enhance inductance robustness and to compensate errors caused by stator inductance mismatch. Some sliding-mode observers are applied to obtain the motor parameters [29]–[31]. For example, in [30], [31], an adaptive-gain sliding mode observer is designed for sensorless control, which can automatically adjust the gain to adapt to actual working condition.

In order to reduce the disturbance caused by parameter mismatch, many scholars have constructed disturbance observers to simultaneously predict stator current and track system disturbance [32], [33]. In [34], the lumped disturbances caused by unknown load torque and parameter variations are derived, and a generalized proportional integral observer based on feed-forward compensated controller is proposed to estimate the flux and current for next step current prediction. In [35], an incremental prediction model is used to predict flux linkage and an inductance disturbance observer is proposed to update inductance value. In [36], a terminal sliding mode control based on nonlinear disturbance observer is proposed to compensate the parameter uncertainty and it realizes the tracking control of speed and current.

In order to eliminate the effect of motor parameter mismatch, many published references have developed the model-free predictive current control (MFPC) algorithm. Unlike traditional model-based PCC, the MFPC algorithm uses stator current difference between two switching states to achieve prediction without using any motor parameters [37]. However, the switching action inside inverter may cause current spikes. In order to solve this problem, scholars have proposed a method that the current detection is performed immediately before power device turns on or turns off in each sampling period [15], [38]. In [39], a weighting factor is added in prediction process to eliminate current spikes. The prediction accuracy can be enhanced by adjusting weighting factor. In MFPC, prediction accuracy only depends on the measured current and current difference, which makes the current difference detection critical. To keep the current variation information up to date, scholars have made some improvements to MFPC method. In [40], a current reconstruction algorithm is presented based on the relationship

between voltage vectors. In [41], a continuous voltage vector MFPC is proposed to reduce the current fluctuation, and the optimal voltage vector is obtained by online optimization of vector's phase and amplitude.

However, the MFPC methods require a sufficiently short switching interval to ensure accuracy, which requires high hardware performance. And most of above mentioned parameter identification methods increase the computational burden of MPC, which makes control system more complex.

This paper aims to reduce the current prediction error of finite-control-set PCC strategy for PMSM, and improve the control performance of motor system. The main contributions of this paper are: a current prediction error reduction method based on online inductance correction is proposed, and it can directly correct the inductance value of prediction model only using one proportional regulator, which is simple and easy to implement. Compared with other methods, the proposed method can significantly reduce calculation burden, while the proposed method is suitable for both interior and surface mounted PMSMs. The paper is organized as follows. Section II presents the PMSM model and PCC algorithm, and the effect of parameter mismatch on current prediction error is analyzed. Based on the relationship between inductance error and current prediction error, the design of current prediction error reduction method is given in Section III. Section IV provides some experimental results to assess the performance of proposed method, and the paper is concluded in Section V.

II. PREDICTIVE CURRENT CONTROL

A. PMSM MODEL

The continuous state equations of PMSM in rotor reference frame are expressed as

$$\frac{di_d}{dt} = -\frac{R_s}{L_d}i_d + \frac{\omega_e L_q}{L_d}i_q + \frac{1}{L_d}u_d \quad (1)$$

$$\frac{di_q}{dt} = -\frac{\omega_e L_d}{L_q}i_d - \frac{R_s}{L_q}i_q + \frac{1}{L_q}u_q - \frac{\omega_e \psi_f}{L_q} \quad (2)$$

where i_d and i_q are d- and q-axes stator currents, u_d and u_q are d- and q-axes stator voltages, L_d and L_q are d- and q-axes inductances, R_s is stator resistance, ω_e and ψ_f are rotor electrical angular speed and flux linkage of permanent magnet, respectively. In order to predict d- and q-axes stator current for next sampling instant, the continuous state equations in (1) and (2) need to be discretized by the forward Euler approximation method. The discrete prediction model of PMSM is obtained as follows

$$i_d^p(k+1) = i_d(k) - \frac{T_s R_s i_d(k)}{L_d} + \frac{T_s \omega_e L_q i_q(k)}{L_d} + \frac{T_s u_d(k)}{L_d} \quad (3)$$

$$i_q^p(k+1) = i_q(k) - \frac{T_s R_s i_q(k)}{L_q} - \frac{T_s \omega_e L_d i_d(k)}{L_q} + \frac{T_s u_q(k)}{L_q} - \frac{T_s \omega_e \psi_f}{L_q} \quad (4)$$

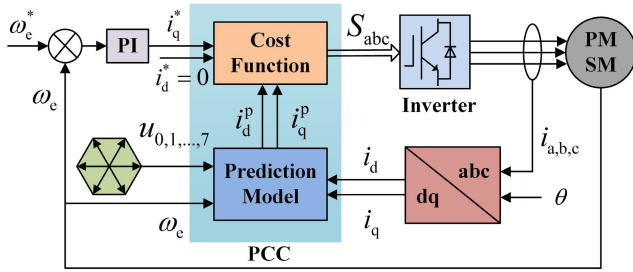


FIGURE 1. Block diagram of PCC for PMSM.

where the superscript p represents prediction value, T_s is the control period, $X(k)$ ($k = 1, 2, 3, \dots$) is the value of X at time kT_s and X represents predicted and actual values of d- and q-axis currents.

B. PREDICTIVE CURRENT CONTROL

The block diagram of PCC scheme for PMSM is shown in Fig. 1. For a two-level three-phase voltage-source inverter, there are eight switching states, which can provide eight voltage vectors including two zero vectors and six active vectors. The future states of motor system under these eight voltage vectors are predicted according to (3) and (4). Then, the prediction results are evaluated to select the optimal voltage vector according to cost function (CF) which is expressed as

$$CF = |i_d^p(k+1) - i_d^*(k+1)|^2 + |i_q^p(k+1) - i_q^*(k+1)|^2 \quad (5)$$

where the superscript * represents reference values. The voltage vector which can minimize CF is chosen as the optimal one and corresponding switching signals will drive inverter in next control period.

C. EFFECT OF PARAMETER MISMATCH ON PREDICTION ERROR

The PCC is sensitive to motor parameters, and the accuracy of model parameters will directly influence control performance of motor system. In actual applications, the motor parameters cannot be measured accurately, and they may change due to temperature, saturation effect and other environmental effects. For example, temperature increase will cause the increase of resistance and the decrease of permanent magnet flux linkage. The d- and q-axes inductances may vary due to magnetic saturation [21], [22]. The effect of model parameter mismatch on current prediction error of PCC is analyzed in this section. In this work, the current prediction error (PE) is defined as the difference between predicted value and actual value of d- and q-axes current, which is expressed as

$$PE = i_x^p(k+1) - i_x^a(k+1), \quad x \in \{d, q\} \quad (6)$$

where the superscript p represents predicted current values and superscript a represents actual current values.

In the PMSM prediction model, the d- and q-axes inductance, stator resistance and flux linkage are L_{dm} , L_{qm} , R_m and ψ_{fm} , respectively. According to (3) and (4),

the current prediction model can be expressed as

$$i_d^p(k+1) = i_d(k) - \frac{T_s R_m i_d(k)}{L_{dm}} + \frac{T_s \omega_e L_{qm} i_q(k)}{L_{dm}} + \frac{T_s u_d(k)}{L_{dm}} \quad (7)$$

$$i_q^p(k+1) = i_q(k) - \frac{T_s R_m i_q(k)}{L_{qm}} - \frac{T_s \omega_e L_{dm} i_d(k)}{L_{qm}} + \frac{T_s u_q(k)}{L_{qm}} - \frac{T_s \omega_e \psi_{fm}}{L_{qm}}. \quad (8)$$

For the actual motor, the d- and q-axes inductance, stator resistance and flux linkage are $L_{da} = L_{dm} + \Delta L_d$, $L_{qa} = L_{qm} + \Delta L_q$, $R_a = R_m + \Delta R$, and $\psi_{fa} = \psi_{fm} + \Delta \psi$, respectively, where ΔL_d , ΔL_q , ΔR , and $\Delta \psi$ are deviations between actual values and values in prediction model. So, actual current can be calculated by

$$\begin{aligned} i_d^a(k+1) &= i_d(k) - \frac{T_s R_a}{L_{da}} i_d(k) + \frac{T_s \omega_e L_{qa}}{L_{da}} i_q(k) + \frac{T_s}{L_{da}} u_d(k) \\ &= i_d(k) - \frac{T_s (R_m + \Delta R)}{L_{dm} + \Delta L_d} i_d(k) + \frac{T_s}{L_{dm} + \Delta L_d} u_d(k) \\ &\quad + \frac{T_s \omega_e (L_{qm} + \Delta L_q)}{L_{dm} + \Delta L_d} i_q(k) \end{aligned} \quad (9)$$

$$\begin{aligned} i_q^a(k+1) &= i_q(k) - \frac{T_s R_a}{L_{qa}} i_q(k) - \frac{T_s \omega_e L_{da}}{L_{qa}} i_d(k) + \frac{T_s}{L_{qa}} u_q(k) \\ &\quad - \frac{T_s \omega_e \psi_{fa}}{L_{qa}} \\ &= i_q(k) - \frac{T_s (R_m + \Delta R)}{L_{qm} + \Delta L_q} i_q(k) + \frac{T_s}{L_{qm} + \Delta L_q} u_q(k) \\ &\quad - \frac{T_s \omega_e (L_{dm} + \Delta L_d)}{L_{qm} + \Delta L_q} i_d(k) - \frac{T_s \omega_e (\psi_{fm} + \Delta \psi)}{L_{qm} + \Delta L_q}. \end{aligned} \quad (10)$$

According to (6)-(10), the current prediction errors of d- and q-axis, namely PE_{i_d} and PE_{i_q} , can be obtained

$$\begin{aligned} PE_{i_d} &= \frac{\Delta R L_{dm} - R_m \Delta L_d}{L_{dm} (L_{dm} + \Delta L_d)} T_s i_d(k) + \frac{\Delta L_d T_s u_d(k)}{L_{dm} (L_{dm} + \Delta L_d)} \\ &\quad + \frac{\Delta L_d L_{qm} - \Delta L_q L_{dm}}{L_{dm} (L_{dm} + \Delta L_d)} T_s \omega_e i_q(k) \end{aligned} \quad (11)$$

$$\begin{aligned} PE_{i_q} &= \frac{\Delta R L_{qm} - R_m \Delta L_q}{L_{qm} (L_{qm} + \Delta L_q)} T_s i_q(k) + \frac{\Delta L_q T_s u_q(k)}{L_{qm} (L_{qm} + \Delta L_q)} \\ &\quad + \frac{\Delta L_d L_{qm} - \Delta L_q L_{dm}}{L_{qm} (L_{qm} + \Delta L_q)} T_s \omega_e i_d(k) \\ &\quad + \frac{\Delta \psi L_{qm} - \psi_{fm} \Delta L_q}{L_{qm} (L_{qm} + \Delta L_q)} T_s \omega_e. \end{aligned} \quad (12)$$

It can be obviously seen from (11) and (12) that the mismatch of any motor parameter will lead to current prediction error. According to existing literature, stator inductance mismatch has the greatest effect on current prediction error [11]. It can be observed from (11) and (12) that the effect of resistance deviation ΔR is only reflected in first part of (11) and (12), and prediction errors are proportional to ΔR . The magnetic flux deviation $\Delta \psi$ only affects PE_{i_q} , and PE_{i_q} is proportional to $\Delta \psi$. The inductance deviation has an effect on each part of (11) and (12), which is more complicated

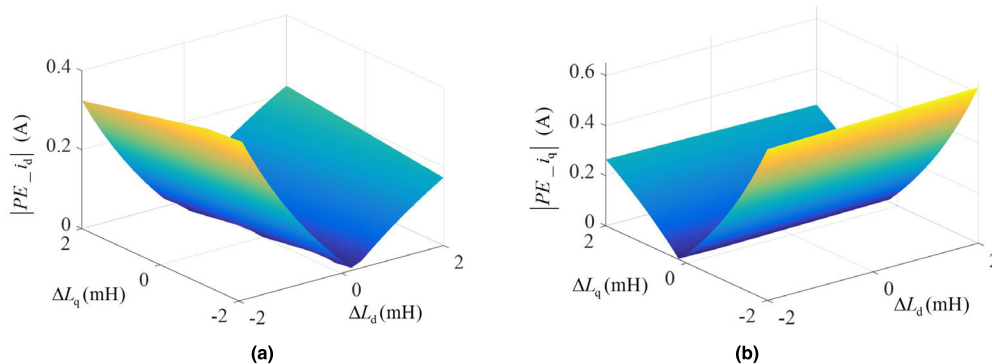


FIGURE 2. The absolute prediction error values under various mismatch degree of inductance parameters. (a) Relationship between absolute value of d-axis current prediction error and mismatch degree of d- and q-axes inductance values. (b) Relationship between absolute value of q-axis current prediction error and mismatch degree of d- and q-axes inductance values.

than that caused by other parameter mismatch. In this paper, the effect of inductance deviations on prediction errors are mainly considered.

To further analyze the impact of ΔL_d and ΔL_q on current prediction errors, the graphical illustrations of absolute current prediction error value with various mismatch degrees of L_d and L_q are shown in Fig. 2 under the working condition of 1 Nm load and 1000 r/min. It can be seen that ΔL_d can influence PE_{id} more obviously and same relationship also exists between ΔL_q and PE_{iq} . Besides, the effect of negative deviations of stator inductance is more obvious.

III. CURRENT PREDICTION ERROR REDUCTION METHOD

Based on the inherent relationship between parameter mismatch and prediction error, the prediction error feedback mechanism is introduced to realize online correction of prediction model parameter. In this section, the design of current prediction error reduction method based on online inductance correction is detailed illustrated.

A. RELATIONSHIP BETWEEN PREDICTION ERROR AND INDUCTANCE MISMATCH

The model predictive control is a nonlinear control scheme, which leads to a complex mapping relationship between prediction error and parameter mismatch. According to the analysis in last section, the current prediction errors are mostly affected by stator inductance mismatch. Therefore, the current prediction error reduction method proposed in this paper is based on the relationship between current prediction error and inductance parameter mismatch.

For interior PMSM (IPMSM) with different L_d and L_q , the d- and q-axes inductance deviations are defined as $\Delta L_d = L_{da} - L_{dm}$ and $\Delta L_q = L_{qa} - L_{qm}$, respectively, where the subscript m represents inductance values in motor prediction model and subscript a represents actual inductance values. Then the current prediction errors of d- and q-axis can be obtained

$$PE_{id} = \frac{\Delta L_d T_s}{L_{dm} (L_{dm} + \Delta L_d)} A_d + \frac{\Delta L_d L_{qm} - \Delta L_q L_{dm}}{L_{dm} (L_{dm} + \Delta L_d)} B_d \quad (13)$$

$$PE_{iq} = \frac{\Delta L_q T_s}{L_{qm} (L_{qm} + \Delta L_q)} A_q + \frac{\Delta L_d L_{qm} - \Delta L_q L_{dm}}{L_{qm} (L_{qm} + \Delta L_q)} B_q \quad (14)$$

where $A_d = -R_s i_d(k) + u_d(k)$, $A_q = -R_s i_q(k) + u_q(k) - \psi_f \omega_e$, $B_d = T_s \omega_e i_q(k)$ and $B_q = T_s \omega_e i_d(k)$. Solving (13) and (14), the relationships between inductance deviations and current prediction errors can be obtained as follow

$$\Delta L_d = \frac{-B_1 A_2 + C_1 B_2}{A_1 A_2 + C_1 C_2} \quad (15)$$

$$\Delta L_q = -\frac{B_2}{A_2} + \frac{C_2}{A_2} \frac{-B_1 A_2 + C_1 B_2}{A_1 A_2 + C_1 C_2} \quad (16)$$

where

$$\begin{cases} A_1 = PE_{id} \times L_{dm} - A_d T_s - L_{qm} B_d \\ B_1 = PE_{id} \times L_{dm}^2 \\ C_1 = L_{dm} B_d \end{cases} \quad (17)$$

$$\begin{cases} A_2 = PE_{iq} \times L_{qm} - A_q T_s + L_{dm} B_q \\ B_2 = PE_{iq} \times L_{qm}^2 \\ C_2 = L_{qm} B_q. \end{cases} \quad (18)$$

For (17) and (18), the orders of magnitude of A_x , B_x and C_x ($x \in \{1, 2\}$) are 10^{-2} , 10^{-7} and 10^{-6} , respectively. Then comparing the magnitude of each part of (15) and (16), and ignoring the smaller parts, the approximate relationship between inductance deviation and prediction error can be obtained

$$\begin{aligned} \Delta L_d &\approx -\frac{B_1}{A_1} \\ &= \frac{-PE_{id} \times L_{dm}^2}{PE_{id} L_{dm} + (R_s i_d(k) + u_d(k) - L_{qm} \omega_e i_q(k)) T_s} \end{aligned} \quad (19)$$

$$\begin{aligned} \Delta L_q &\approx -\frac{B_2}{A_2} \\ &= \frac{-PE_{iq} \times L_{qm}^2}{PE_{iq} L_{qm} + (R_s i_q(k) - u_q(k) + \psi_f \omega_e + L_{dm} \omega_e i_d(k)) T_s}. \end{aligned} \quad (20)$$

For the denominator of (19), the order of magnitude of $PE_{id} \times L_{dm}$ is 10^{-4} , and the order of magnitude of rest part is 10^{-2} . Therefore, the influence of $PE_{id} \times L_{dm}$ in (19) can be ignored. The case of (20) is similar to (19). Then by simplifying (19) and (20), the absolute values of inductance

deviations can be obtained

$$|\Delta L_d| \approx \left| \frac{L_{dm}^2}{(R_s i_d(k) + u_d(k) - L_{qm} \omega_e i_q(k)) T_s} \right| \times |PE_{-i_d}| \quad (21)$$

$$|\Delta L_q| \approx \left| \frac{L_{qm}^2}{(R_s i_q(k) - u_q(k) + \psi_f \omega_e + L_{dm} \omega_e i_d(k)) T_s} \right| \times |PE_{-i_q}|. \quad (22)$$

According to (21) and (22), there exists a proportional relationship between the absolute values of inductance deviations and that of current prediction errors.

Surface mounted PMSM (SPMSM, $L_d = L_q$) can be seen as a special case of IPMSM. In SPMSM control system, the $i_d = 0$ control is mostly used in practical applications, which makes the prediction error of q-axis current more obvious than that of d-axis. Therefore, the relationship between q-axis current prediction error and stator inductance parameter mismatch is mainly considered. For actual SPMSM, stator inductance is L_a . The stator inductance of SPMSM prediction model is L_m . Then PE_{-i_q} can be shown as

$$PE_{-i_q} = \frac{L_m - L_a}{L_m L_a} [R_s i_q(k) + \omega_e \psi_f - u_q(k)] T_s. \quad (23)$$

The stator inductance error ΔL is defined as $\Delta L = L_a - L_m$, and the relationship between ΔL and PE_{-i_q} is obtained as follows

$$\Delta L = \frac{-PE_{-i_q} \times L_m^2}{PE_{-i_q} \times L_m + [R_s i_q(k) + \omega_e \psi_f - u_q(k)] T_s}. \quad (24)$$

For the denominator of (24), the order of magnitude of $PE_{-i_q} \times L_m$ is 10^{-4} and the order of magnitude of rest part is 10^{-2} . Therefore, the influence of $PE_{-i_q} \times L_m$ in (24) can be ignored and the absolute value of ΔL can be obtained

$$|\Delta L| \approx \left| \frac{L_m^2}{[R_s i_q(k) + \omega_e \psi_f - u_q(k)] T_s} \right| \times |PE_{-i_q}|. \quad (25)$$

According to (25), there exists a proportional relationship between $|\Delta L|$ and $|PE_{-i_q}|$. So, the inductance online feedback correction can be realized through a proportional regulator. The input signal of proportional regulator is current prediction error, and the output signal is the absolute correction value of inductance parameter, while the order of magnitude of proportional coefficient is from 10^{-4} to 10^{-3} according to (25). In practical applications, the initial gain value of proportional regulator can be obtained by (25), and then fine tune the value according to different operating conditions.

B. INDUCTANCE ERROR POLARITY

In the last section, the absolute correction value of inductance parameter is obtained, and in this section, the polarity of correction value is judged according to the fluctuation amplitude of predicted current and actual current.

According to (7) and (8), the fluctuation amplitude of predicted current is inversely proportional to the polarity of inductance deviation. For example, if the inductance value in

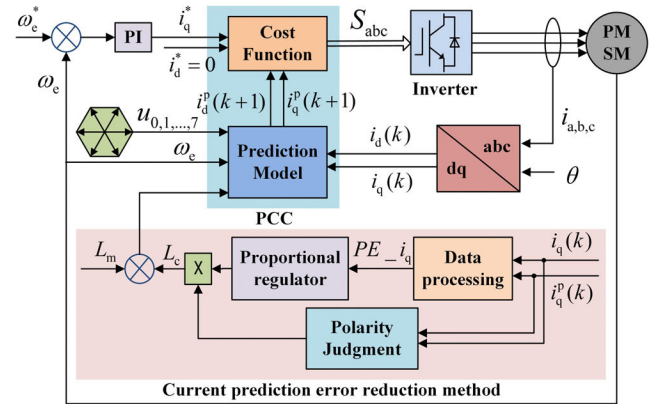


FIGURE 3. Block diagram of current prediction error reduction method.

prediction model is greater than the actual value, the fluctuation amplitude of predicted current will be smaller than that of actual current. On the contrary, the fluctuation amplitude of predicted current will be larger than that of actual current. Based on the above conclusion, the polarity of absolute correction value can be judged by

$$\begin{cases} \text{negative, } \sum |i_q^p(k) - \text{mean}(i_q^p(k))| \\ \quad < \sum |i_q(k) - \text{mean}(i_q(k))| \\ \text{positive, } \sum |i_q^p(k) - \text{mean}(i_q^p(k))| \\ \quad > \sum |i_q(k) - \text{mean}(i_q(k))| \end{cases} \quad (26)$$

where $\text{mean}(X)$ is the average value of current over a data window period T_d . The data window period T_d is related to inductance correction period T_c , which will be illustrated in the next section.

According to the absolute correction value and inductance error polarity, inductance correction value L_c can be calculated, and the block diagram of current prediction error reduction method is shown in Fig. 3.

C. CORRECTION PERIOD

According to the test results, the current prediction errors vary periodically and the variation period of prediction error changes under different motor speed. The higher the motor speed is, the shorter the variation period of current prediction error is. So, the determination of inductance correction period will affect the effectiveness of proposed method. If the correction period is too long, the inductance error cannot be corrected in time. Conversely, if the correction period is too short, the correction period cannot contain enough current prediction error variation periods, which may lead to the wrong correction value and its polarity according to (25) and (26). In addition, too frequent corrections may cause system instability.

Because the variation period of current prediction error is related to motor rotation speed, this paper proposes a correction period automatic adjustment method, in which the inductance correction period can be adaptively adjusted according to the motor speed. The principle of this method

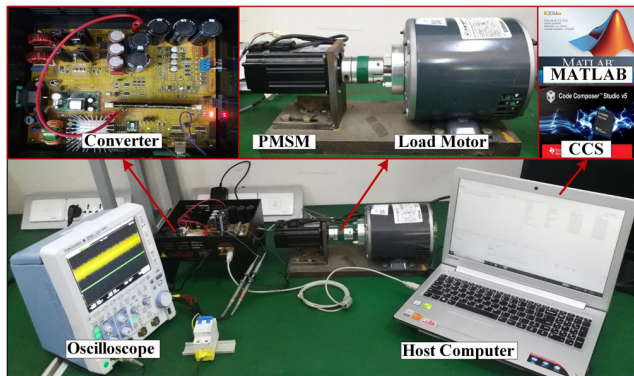


FIGURE 4. The experimental platform.

TABLE 1. Parameters of motor control system.

Symbol	Quantity	Value	Unit
P_n	rated power	400	W
I_n	rated current	2.8	A
ω_n	rated speed	3000	r/min
T_n	rated torque	1.27	Nm
R_s	stator resistance	2.35	Ω
L_s	stator inductance	6.5	mH
ψ_f	permanent magnet flux linkage	0.0755	Wb
n_p	number of pole pairs	4	pairs
U_{dc}	DC bus voltage	200	V
T_s	control period	100	μs

can be expressed by

$$T_c = T_d = \frac{2\pi n_p}{\omega_e} \times 20, \quad (27)$$

where n_p is the number of pole pairs. In (27), the inductance correction period T_c is equal to data window period T_d , and both of them contain fixed number of mechanical rotation cycles (fixed number of current prediction error periods).

IV. EXPERIMENTAL VERIFICATION

In order to verify the effectiveness of proposed current prediction error reduction method, the experimental platform is implemented as shown in Fig. 4, and the main parameters of motor control system are shown in Table 1. The PCC model is established using MATLAB/Simulink to generate C code, and the PCC algorithm is implemented using DSP TMS320F28335 processor.

In the experiment, the inductance value given by motor manufacturer L_s is regarded as actual inductance, and the inductance deviation is artificially designed by setting different inductance values in prediction model of PCC.

The experimental results of current prediction error reduction method are shown in Fig. 5(a) and Fig. 5(b). The waveforms from top to bottom are stator inductance of motor prediction model L_m , prediction errors of q- and d-axes currents, electromagnetic torque T_e and flux

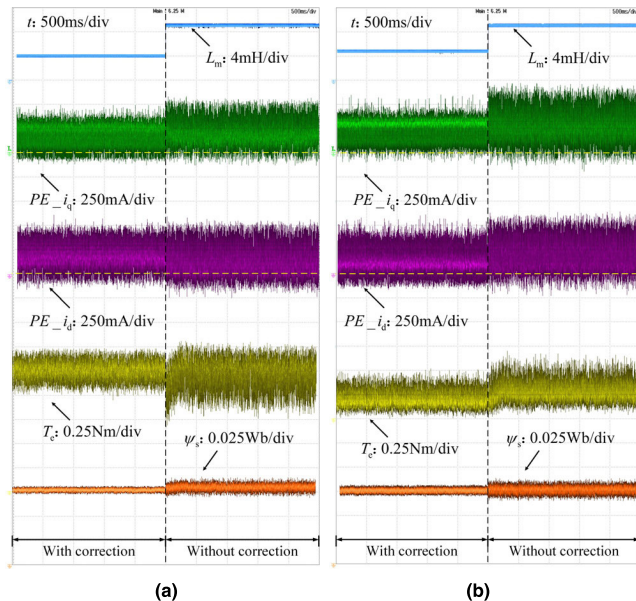


FIGURE 5. The experimental results of proposed method with 40% inductance mismatch ($L_m = 9.1$ mH, $L_s = 6.5$ mH). (a) Under 1.27 Nm load and 1500 r/min. (b) Under no load and 1500 r/min.

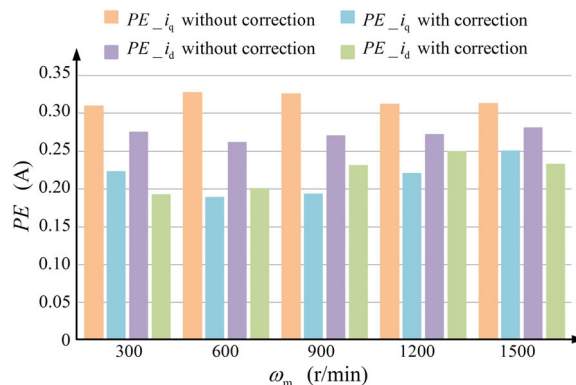


FIGURE 6. The results of d- and q-axes current prediction errors with 40% inductance mismatch ($L_m = 9.1$ mH, $L_s = 6.5$ mH) under different speeds.

linkage ψ_s , respectively. The results are obtained under the conditions of 40% inductance parameter mismatch ($L_m = 9.1$ mH, $L_s = 6.5$ mH), and the motor speed is 1500 r/min while load torque $T_L = 1.27$ Nm in Fig. 5(a) and no load in Fig. 5(b). It can be obviously seen that the proposed method can effectively correct the inductance value in motor prediction model, and the system control performance are improved. Under the condition of $T_L = 1.27$ Nm, after the proposed method is utilized, the PE_{i_q} and PE_{i_d} are reduced by 20.18% and 5.13%, respectively, and torque ripple T_{rip} and flux ripple ψ_{rip} are reduced by 30.13% and 48.01%, respectively. Similar results can be obtained under the condition of no load.

Fig. 6 shows the results of d- and q-axes current prediction errors with 40% inductance mismatch in cases where $T_L = 1.27$ Nm and ω_m is changed from 300 r/min to 1500 r/min by the step of 300 r/min. Fig. 7 shows the results of torque ripple T_{rip} and flux ripple ψ_{rip} . The results show

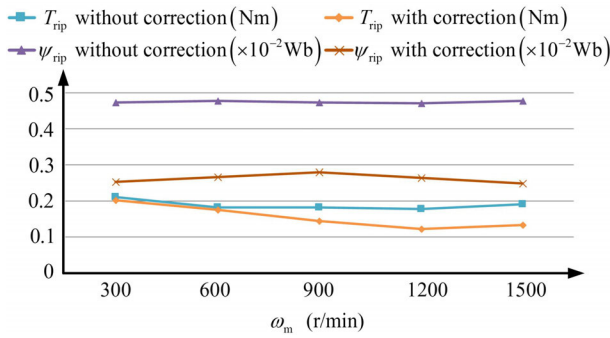


FIGURE 7. The results of torque ripple T_{rip} and flux ripple ψ_{rip} with 40% inductance mismatch under different speeds.

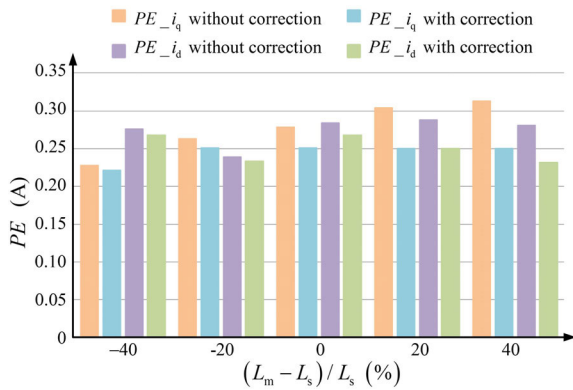


FIGURE 8. The results of d- and q-axes current prediction errors with different inductance mismatch degrees under 1.27 Nm load and 1500 r/min.

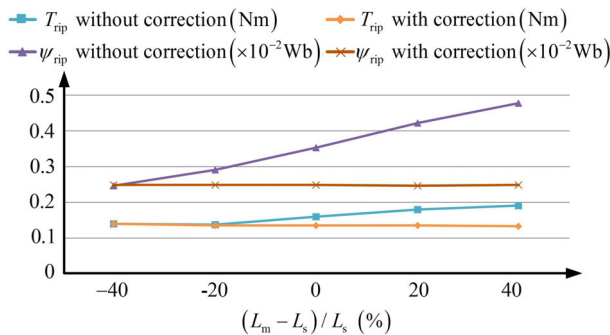


FIGURE 9. The results of torque ripple T_{rip} and flux ripple ψ_{rip} with different inductance mismatch degrees under 1.27 Nm load and 1500 r/min.

that the proposed method can significantly reduce current prediction errors under different speeds, while the control performance can be improved.

Fig. 8 shows the results of d- and q-axes current prediction errors in cases where $T_L = 1.27$ Nm, $\omega_m = 1500$ r/min and inductance mismatch is changed from -40% to 40% by the step of 20% . Fig. 9 shows the results of torque ripple T_{rip} and flux ripple ψ_{rip} . Table 2 shows the numerical results of current prediction error reduction and control performance. The results show that the proposed method can achieve significant reduction of current prediction error under different inductance mismatch degrees, while the control performance can be improved.

TABLE 2. Results under different inductance mismatch (%).

	(%)				
$(L_m - L_s) / L_s$	-40	-20	0	20	40
Reduction percentage of PE_{i_q}	2.96	4.43	9.59	17.61	20.18
Reduction percentage of PE_{i_d}	2.91	2.64	5.60	13.06	17.58
Reduction percentage of T_{rip}	-0.64	1.45	14.28	23.67	30.13
Reduction percentage of ψ_{rip}	-1.14	14.21	29.62	41.79	48.01

TABLE 3. Correction results of inductance.

$(L_m - L_s) / L_s$ (%)	-40	-20	0	20	40
L_m (mH)	3.9	5.2	6.5	7.8	9.1
L_m with correction (mH)	4.14	4.12	4.14	4.13	4.13

Table 3 shows the inductance values after correction under different inductance mismatch degrees. Two points need to be noted in the table: 1. In the case of no inductance mismatch, the proposed method still corrects inductance parameters to reduce prediction error. 2. The inductance value is corrected to approximately 4.13 mH for different mismatch degrees, while the inductance value given by motor manufacturer L_s is 6.5 mH. The reasons are as follows: 1. The inductance value provided by motor manufacturer L_s is a nominal value, but actual inductance value may vary during different operation conditions, resulting in a difference between actual and nominal inductance value. For example, magnetic saturation effect may lead to the result that actual inductance value is smaller than the given value. 2. Except inductance mismatch, the current prediction error may be caused by many other factors, such as resistance and magnetic flux mismatch, prediction step size, discretization order of motor prediction model and so on. Therefore, the influence of other factors on prediction error will be reflected in inductance correction value, and the corrected inductance value may differ from given value. The objective of proposed method is reducing prediction error and improving control performance, but not obtaining accurate inductance value.

Besides, the dynamic response of proposed method is fast during the experiments. The correction response is related to the proportional coefficient of regulator and correction period, which can be improved by increasing proportional coefficient and shortening correction period. However, large proportional coefficient will result in the oscillation of corrected inductance value, and short correction period will cause system instability. In the experiment, these two parameters can be fine-tuned according to (25) and (27) to give full play of proposed method.

V. CONCLUSION

In this paper, a current prediction error reduction method of PCC for PMSM based on online inductance correction is proposed and it has been experimentally applied to a SPMSM system. The major conclusions of this paper include: 1. The mismatch of motor parameters can lead to current prediction errors, and the deviation of stator

inductance is the most important factor causing current prediction error. 2. For $i_d = 0$ control of SPMSM, there exists a proportional relationship between inductance deviation and q-axis current prediction error, and the polarity of inductance deviation is opposite to the current prediction error. 3. The current prediction errors vary periodically and the variation period changes according to motor speed. 4. Experimental results show that the proposed method can achieve significant reduction of current prediction error, while the control performance can be improved. 5. The current prediction error reduction method based on online inductance correction is suitable for both IPMSM and SPMSM. Compared to other similar methods, the proposed method is simple and easy to implement in practical applications. Besides, it should be noted that current prediction error is difficult to completely eliminate, and the objective of proposed method is to reduce current prediction error as much as possible rather than eliminate it completely.

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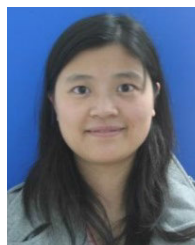
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