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A Novel Zero-Watermarking Scheme Based on Variable Parameter Chaotic Mapping in NSPD-DCT Domain

RUI WANG¹, HAN SHAOCHENG¹, PENG ZHANG¹, MENG YUE¹, ZHENG CHENG², AND YUJIN ZHANG¹, (Member, IEEE)

¹College of Science, Civil Aviation University of China, Tianjin 300300, China

²Basic Experimental Center, Civil Aviation University of China, Tianjin 300300, China

Corresponding author: Rui Wang (r-wang@cauc.edu.cn)

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ABSTRACT In this paper, a novel image zero-watermarking scheme against rotation attacks is proposed based on nonsubsampled pyramid decomposition (NSPD) and discrete cosine transform (DCT). It utilizes the intrinsic characteristics of NSPD and DCT to extract the robust feature of an image as the original zero-watermark. To increase the security of the proposed scheme, a variable parameter chaotic mapping (VPCM) is designed for the processes of watermark encryption and robust feature extraction. Firstly, the host gray-scale image is decomposed by NSPD, and the low-frequency sub-band image is divided into non-overlapping blocks. After the blocks are transformed by DCT, the signs of the first AC coefficients from all the blocks are used to construct a binary feature image. Then an exclusive-or operation is performed between the binary feature image and the encrypted watermark image to obtain the verification zero-watermark image. Furthermore, a method against arbitrary rotation attacks is employed to improve the robustness of the scheme against geometric attacks. The experimental results demonstrate that the proposed scheme is highly robust against various image processing attacks such as filtering, JPEG compression, scaling, translation, rotation and Checkmark attacks.

INDEX TERMS Discrete cosine transform, nonsubsampled pyramid decomposition, rotation attacks, variable parameter chaotic mapping, zero-watermarking.

I. INTRODUCTION

With the rapid development of computer technology and the Internet, digital media such as image, audio and video, can be more easily tampered and distributed than ever before. Therefore, the protection of multimedia content is currently a serious issue. Digital watermarking has been proposed as a potential solution to address this problem. It embeds some special secret information into host data and the information can be retrieved to identify the ownership of these data when necessary [1]–[4]. Digital watermarking has been widely used in many applications, including copyright protection, authentication, transaction tracking, and broadcast monitoring [5], [6]. The characteristics of an effective watermarking scheme include imperceptibility, robustness, security, and

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embedding capacity [7]–[10]. Imperceptibility means that the original host data and watermarked data can not be differentiated by the human visual system [8]. Robustness refers to the ability of the watermarking scheme to extract the embedded watermark under various attacks [9]. Security ensures that the watermarking scheme is difficult to be cracked, and it depends mainly on the secret keys used in the process of watermark extraction [10]. Embedding capacity denotes the amount of watermark bits.

Depending on the various properties, the watermarking algorithms can be categorized in various ways [8]. According to the required information of original data in the process of watermark extraction, watermarking schemes are categorized into blind, non-blind and semi-blind algorithms [11]. Bind algorithms do not require the original data when extracting the watermark, while non-bind watermarking algorithms require the complete information of original data. On the

³College of Electronic Information and Automation, Civil Aviation University of China, Tianjin 300300, China

⁴School of Electronic and Electrical Engineering, Shanghai University of Engineering Science, Shanghai 201620, China



other hand, semi-blind watermarking algorithms only require the partial information of the original data to detect the watermark. According to their applications and purposes, watermarking algorithms can be categorized into fragile and robust watermarking algorithms [12]. Fragile algorithms [13] are used for image authentication and tamper detection, while robust watermarking algorithms are used for copyright protection. According to the domain in which the watermark will be embedded, watermarking algorithms can be categorized into spatial domain algorithms and transform domain algorithms [11]. In spatial domain algorithms [14]-[16], watermarks are usually embedded into the host images by modifying their pixels directly. In transform domain watermarking algorithms, one or more transforms are applied to the host images, then the watermarks are embedded by modifying the transformed coefficients in the frequency domain. Spatial domain algorithms usually have lower computational complexity than the transform domain watermarking algorithms. However, due to the limitations of watermarking in the spatial domain involving visualization and robustness [17], most image watermarking algorithms use the transforms such as Cosine transform [18]–[22], Fourier transform [23], [24], Wavelet transform [25], [26], Contourlet transform [27], [28], and Shearlet transform [29]-[31].

In the above-mentioned traditional watermarking algorithms, whether the original watermarks are embedded in the spatial domain or transform domain, the host images are distorted to some extent. Therefore, there is inevitably a contradiction between imperceptibility and robustness of the watermark. The traditional watermarking methods are usually limited for medical images [32]–[34] and remote-sensing images [35] which require low distortion and high resolution. In this case, the zero-watermarking was firstly proposed by Wen *et al.* [36], which has attracted wide attention of researchers in recent years. Zero-watermarking extracts the intrinsic features of original data without modifying the data. Hence it can address the contradiction between imperceptibility and robustness of the traditional watermarking methods.

Several zero-watermarking algorithms have been proposed in the past 15 years. In [36], Wen et al. constructed a zero-watermark by computing high-order cumulants. Their method is robust to common image processing attacks and slight scaling rotation, but it is fragile to large-scale rotations and requires a lot of time to compute the high-order cumulants. Ye [37] proposed a zero-watermarking algorithm based on singular value decomposition (SVD) and discrete cosine transform (DCT). In their algorithm, the host image is firstly divided into non-overlapping blocks. Then, the zerowatermark sequence is derived by comparing the numerical relationship between the direct current (DC) coefficients of two adjacent blocks after every block is performed with SVD and DCT. The algorithm gave out a new idea of zerowatermarking by combining matrix decomposition and traditional transforms, but the attacks used in the experiments were very slight. Based on [36] and [37], Zhang et al. [38] presented three improved zero-watermarking schemes

respectively named by DC-RE, CU-SVD and CU-SVD-RE. These schemes are more robust than the algorithms in [36] and [37], but the security of these schemes needs to be improved. Rani and Raman [39] also extracted the robust features of an image as the zero-watermark based on DCT and SVD. The scheme divided the host image into overlapping blocks of size 8 × 8 and performed DCT and SVD to every block. The zero-watermark is obtained by comparing the relationship between the two largest singular values, which are selected out randomly using four pseudo-random number sequences. The robustness and security of the algorithm are acceptable for the protection of images to some extent. However, dividing the host image into overlapping blocks generates a large number of image blocks, which increased the computational complexity of the algorithm. Ta Minhn Thanh et al. [40] extracted the robust feature as the master share from the host image by combining the QR decomposition and one-dimensional (1D) DCT. In their scheme, the host images are RGB images, and two zero-watermarking construction schemes were proposed utilizing the luminance Y-components of the host images. The Y-component is also divided into non-overlapping blocks, and the master share is generated by comparing the DC coefficients of two adjacent blocks after all the blocks have undergone QR decomposition and 1D-DCT.

Lin et al. [41] proposed a spatial domain zerowatermarking scheme based on generalized Arnold transform (GAT) and spread spectrum and despreading (SSD) techniques. In their method, the GAT is used to scramble the original watermark for security. Then, a binary feature matrix is obtained from the original host image in quantitative embedding rules. Finally, the zero-watermark is generated by performing an exclusive-or operation between the scrambled watermark and the feature matrix. Considering that better robustness of watermarking can be achieved in transform domain, some multi-scale transforms such as Contourlet [42] and Shearlet [43], [44], regarded as extension of the wavelet transform, have been applied to the zero-watermarkings. In [42], a robust zero-watermarking algorithm was proposed based on contourlet transform (CT) and DCT for medical images, Logistic Map is used to encrypt the original watermark to ensure the security of it. The experimental results show that the method is effective to against common and slightly geometric attacks. Nonsubsampled shearlet transform (NSST) is a new and very important multi-scale and multi-direction analysis tool that can provide nearly optimal approximation properties for image representation [45]. Han et al. [43] proposed a zero-watermarking method based on NSST and LU decomposition. In their method, after the host image is decomposed by NSST, a random sub-image of the low-frequency sub-band image is divided into nonoverlapping blocks. Then, every block undergoes LU decomposition to obtain the matrix U. The final zero-watermark is generated by comparing the numerical relationship between the sum of the first row elements from every matrix U and the mean of all the sums. In [44], a robust zero-watermarking



scheme was proposed that employed multi-resolution and multi-scale representation characteristics of NSST to analyze the direction features of the host image. In the algorithm, a sub-band image is firstly selected as the embedding position by calculating the direction feature information intensity. Then, the sub-band image is divided into non-overlapping blocks. The zero-watermark is constructed by comparing the 2-norms of every block with a threshold.

Although the above-mentioned zero-watermarking algorithms can resist conventional image processing operations, they are almost fragile to the geometrical distortions such as rotation and translation attacks. Gao and Jiang [46] developed a zero-watermarking algorithm against geometric attacks based on the Bessel-Fourier moment. In their algorithm, the image normalization is applied to the host image. Then, the magnitudes of the Bessel-Fourier moments of the normalized image are computed to construct a binary feature image. The final verification image is generated by performing an exclusive-or operation between the binary feature image and the original watermark image. Wang et al. [47] introduced a zero-watermarking algorithm against geometric attacks based on polar complex exponential transform (PCET) and logistic mapping (LM). Their algorithm computes the PCET of the original gray-scale image and randomly selects PCET coefficients based on LM. Then, the magnitudes of the PCET are computed to construct the binary feature image. These abovementioned zero-watermarking methods are summarized by Table 1.

TABLE 1. The performance of the related zero-watermarking methods.

Methods	Related techiques	Embedding domain	Robustness	Rotation attacks	Complexity
[36]	Cumulants	_	×	×	×
[37]	DCT	Single	×	×	\checkmark
[38]	DCT, SVD	Single	×	×	×
[39]	DCT, SVD	Single	\checkmark	×	×
[40]	QR, DCT	Single	×	×	\checkmark
[41]	GAT, SSD	_	×	×	\checkmark
[42]	CT, DCT	Hybrid	\checkmark	×	\checkmark
[43]	LU, NSST	Single	\checkmark	×	\checkmark
[44]	NSST, 2-norm	Single	\checkmark	×	\checkmark
[46]	Moments		\checkmark	\checkmark	×
[47]	PCET, LM	Single	\checkmark	\checkmark	×

In this paper, we propose a robust zero-watermarking scheme based on NSPD-DCT and VPCM. Our experimental results demonstrate that the proposed algorithm can effectively resist the conventional image processing operations and several geometrical distortions. The contributions of this paper are the following:

- A novel invariant feature of an image is found by combining the shift-invariant characteristic of NSPD and the robustness of the signs of some DCT coefficients against various attacks.
- (2) In order to improve the security of the proposed scheme, a VPCM system is designed for two processes: watermark encryption and robust feature extraction.

(3) To get better robustness of watermarking against geometrical attacks, a simple method for estimating the rotation angles of images is utilized by computing the normalized cross-correlation (NC) between the scaled down host image and the scaled down image to be detected.

The rest of this paper is organized as follows. Section II presents the preliminaries of the Arnold transform, DCT, and NSPD. This section also briefly describes VPCM. Section III explains the proposed zero-watermarking scheme. In this section, the zero-watermark generation and extraction are illustrated in different subsections. Section IV provides the results and discussions. Finally, Section V presents the conclusions drawn from this work.

II. PRELIMINARIES

A. ARNOLD TRANSFORM

Arnold transform is an image scrambling method also regarded as a two-dimensional (2D) chaotic mapping [19]. In many watermarking schemes, Arnold transform is applied to the watermark image to expand the robustness of the proposed algorithm and provide extra security for the embedded watermark [8]. The positions of different pixels in an image can be changed after the image undergoes the Arnold transform. The 2D Arnold transform is defined as:

$$\begin{pmatrix} x' \\ y' \end{pmatrix} = \begin{bmatrix} \begin{pmatrix} 1 & 1 \\ 1 & 2 \end{pmatrix} \begin{pmatrix} x \\ y \end{pmatrix} \end{bmatrix} \mod P, \tag{1}$$

where (x, y) are the location coordinates of the original image pixels, $x, y \in \{0, 1, 2, \dots, P-1\}$, (x', y') are the location coordinates of the scrambled image pixels, and P is the size of the watermark. When all of the pixels of the image are transformed, the scrambled image is obtained. Arnold scrambling is periodic. Considering that T is the transform period, the image can return to the original state after T iterations [48]. The number of iterations for image scrambling and T can be regarded as the private keys. Without the keys, the original image cannot be restored. In our method, the Arnold transform is also used to scramble the original watermark image.

B. DISCRETE COSINE TRANSFORM

Discrete cosine transform has been used in the field of various images and signal processing, including in image coding and watermarking. The DCT transforms an image from the spatial domain into the frequency domain [21], [49]. DCT has an excellent energy compactness property, which is why it is used in the JPEG compression technique to separate and remove the insignificant high frequency components in images [50]. The forward 2D-DCT formula is defined as:

$$F(u, v) = c(u)c(v)\frac{2}{N}$$

$$\cdot \sum_{x=0}^{N-1} \sum_{y=0}^{N-1} f(x, y) \cos\left(\frac{2x+1}{2N}u\pi\right) \cos\left(\frac{2y+1}{2N}v\pi\right)$$
(2)



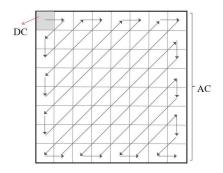


FIGURE 1. Zigzag scanning.

where x, y, u, v = 0, 1, 2, ..., N - 1, and

$$c(u) = c(v) = \begin{cases} \frac{1}{\sqrt{2}} & u = 0, v = 0\\ 1 & otherwise. \end{cases}$$
 (3)

The inverse 2D-DCT formula is described as

$$f(x,y) = \frac{2}{N} \cdot \sum_{u=0}^{N-1} \sum_{v=0}^{N-1} c(u)c(v)F(u,v)$$
$$\cos\left(\frac{2x+1}{2N}u\pi\right)\cos\left(\frac{2y+1}{2N}v\pi\right), \quad (4)$$

where f(x, y) is the gray value of a pixel, and F(u, v) is the DCT coefficient. After this transformation, an image consists of one DC coefficient and multiple alternate current (AC) coefficients. The DC and AC coefficients are arranged in the Zigzag scanning order, as shown in Fig. 1. The DC coefficient locating at the top-left corner of the coefficient matrix is a large positive number. It represents most of the energy of the image. Except for the DC coefficient, all the other coefficients are the AC coefficients. The AC coefficients represent the characteristics of different frequency bands, including low, middle and high frequency bands. Moreover, the AC coefficients are either positive or negative numbers, and their amplitudes are less than the DC coefficient [22], [51].

C. NONSUBSAMPLED PYRAMID DECOMPOSITION

Nonsubsampled pyramid decomposition was proposed by Cunha *et al.* when they designed the nonsubsampled contourlet transform (NSCT) [52]. The nonsubsampled pyramid (NSP) is achieved by replacing the Laplacian pyramid with two-channel nonsubsampled 2D filter banks as shown in Fig.2 (a). The decomposition filters $H_0(z)$, $H_1(z)$ and the composition filters $G_0(z)$, $G_1(z)$ satisfy the Bezout identical equation $H_0(z)G_0(z)+H_1(z)G_1(z)=1$. The equation ensures the NSP filter banks satisfying the perfect reconstruction condition, where $H_0(z)$ is a low-pass filter and $H_1(z)$ is a high-pass filter [53].

The frequency expansion of NSPD is conceptually similar to the one-dimensional nonsubsampled wavelet transform (NSWT) computed with the atrous algorithm. It has J+1 redundancy, where J denotes the number of decomposition stages [52]. The sketch map of

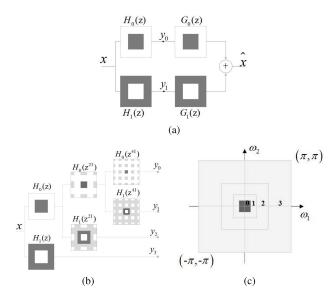


FIGURE 2. NSPD: (a) The two-channel NSP filter banks, (b) A 3-stages NSPD, (c) The sub-bands on the 2D frequency plane.

NSPD and the relevant frequency division with J=3 stages are shown in Fig. 2 (b) and (c) respectively. The ideal pass-band support of the low-pass filter at the j-th stage is the region $[(-\pi/2^j), (\pi/2^j)]^2$. Accordingly, the ideal support of the equivalent high-pass filter which is the complement of the low-pass filter is the region $[(-\pi/2^{j-1}), (\pi/2^{j-1})]^2 \setminus [(-\pi/2^j), (\pi/2^j)]^2$ [52]. By contrast, the 2D àtrous algorithm has 3J+1 redundancy. Besides having nice multi-resolution characteristics, NSPD can overcome the weakness of traditional DWT without shift-invariant characteristic and has less redundancy then NSWT [54]. Fig. 3 shows an example for NSPD of Man image at J=4. In Fig. 3, (a) is an original image, (b) is a low-pass image, and (c)-(e) are the band-pass images from coarse to fine stages.

D. VARIABLE PARAMETER CHAOTIC MAPPING

Chaotic mappings are widely used in most watermarking schemes to encrypt the original watermark. In this section, we propose a variable parameter chaotic mapping denoted by VPCM based on two typical chaotic systems: logistic mapping and piecewise linear chaotic mapping (PWLCM). The LM widely used in many watermarking algorithms [10], [47], [55] is defined as:

$$x_{n+1} = \mu x_n (1 - x_n), \tag{5}$$

where $\mu \in [0, 4]$ is the control parameter, and x_n is the chaos sequence of the map. Furthermore, because PWLCM has the properties, including uniform distribution, good ergodicity, confusion, and diffusion, it is also utilized for encrypting the watermarks [56]–[58]. PWLCM can be described as:

$$x_{n+1} = F(x_n, p) = \begin{cases} x_n/p, & x_n \in [0, p] \\ (x_n - p)/(0.5 - p), & x_n \in [p, 0.5] \\ F(1 - x_n, p), & x_n \in [0.5, 1], \end{cases}$$
(6)



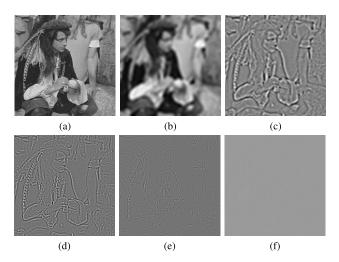


FIGURE 3. Original Man image and its NSPD: (a) Original image, (b) Low-pass image, (c) Band-pass image at the 1-th stage, (d) Band-pass image at the 2-th stage, (e) Band-pass image at the 3-th stage, (f) Band-pass image at the 4-th stage.

where $x_n \in (0, 1)$ and the control parameter $p \in (0, 0.5)$.

To enhance the robustness and security of the proposed scheme, we replace the control parameter p of the above PWLCM system with a variable parameter p_n . p_n depends on the random sequence x_n generated by the LM. To satisfy $p_n \in (0, 0.5)$, we make p_n to be a third of x_n . The proposed VPCM system can be presented as follows:

$$\begin{cases} x_{n+1} = \mu x_n (1 - x_n), p_n = x_n / 3 \\ y_n / p_n, & y_n \in [0, p_n] \\ (y_n - p_n) / (0.5 - p_n), & y_n \in [p_n, 0.5] \\ F(1 - y_n, p_n), & y_n \in [0.5, 1]. \end{cases}$$
(7)

The parameter μ and the initial state values of VPCM are regarded as private keys. In our watermarking scheme, we utilize the VPCM system to generate two random sequences to be used for watermark image encryption and robust feature extraction.

III. PROPOSED ZERO-WATERMARKING SCHEME BASED ON NSPD-DCT AND VPCM

In this section, we introduce a new robust feature extraction method for images. we performed experiments to show that the extracted feature of an image is highly robust to some image processing attacks. Finally, we explain the proposed zero-watermarking scheme based on NSPD-DCT and VPCM in detail. The zero-watermarking scheme mainly includes two procedures: zero-watermark generation and zero-watermark extraction [47]. Zero-watermark is usually generated from the important feature of an image [46]. In our scheme, after the host image undergoes NSPD and DCT, the signs of the first AC coefficients from the DCT blocks are used to construct the zero-watermark. Since the zero-watermarking does not need inverse transformation, the process of zero-watermark extraction is similar to that of zero-watermark generation. Furthermore, in order to improve the performance of the

proposed scheme against rotation attacks, we introduce a method of image rotation correction which is applied before the zero-watermark extraction.

A. ROBUST FEATURE EXTRACTION IN NSPD-DCT DOMAIN

Li *et al.* proposed a zero-watermarking algorithm for protecting medical images in the DCT domain [59]. In their algorithm, they pointed out that the signs of some DCT coefficients remain unchanged against some strong geometric attacks. Their method applies DCT to the host image, then the sign sequence of the low-frequency coefficients is extracted as the feature vector to construct the zero-watermark. The method has been extended to the DWT-DCT hybrid domain in [60]. However, the embedding capacities of watermarks in [59], [60] were limited.

Drawing inspiration from the methods in [59], [60], we here extract robust feature vector based on NSPD and DCT. To describe our method in detail, we performed several experiments as follows. Suppose the original test Man image shown in Fig. 3 (a) is denoted by H. We firstly performed the NSPD with J=5 stages on H to obtain the low-frequency subband image H_L . Then H_L was divided into non-overlapping blocks of size 8×8 , and every block was transformed by DCT. Finally we selected out eight coefficient blocks denoted by $D_i(i=1,2,\ldots,8)$ for test. The positions of them are shown in Fig. 4.

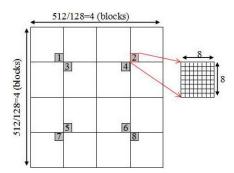


FIGURE 4. The positions of the selected blocks for test.

In these experiments, we tested the robustness of eight AC coefficients from each selected block. According to the Zigzag scanning order, the positions of the eight AC coefficients are (1, 2), (2, 1), (3, 1), (2, 2), (1, 3), (1, 4), (2, 3) and (3, 2). The host Man image was distorted via seven image processing attacks, such as (a) Gaussian noise (0.1), (b) Speckle noise (0.2), (c) Median filtering (7×7) , (d) JPEG compression (5%), (e) Scaling (1/8), (f)Translation (turn down by 5 pixels), (g) Rotation (2°). Table 2 shows the DCT coefficients of D_1 for the Man image under the above-mentioned different attacks. The coefficients shown in bold in Table 2 denote that their signs changed after the Man image was subjected to some attacks. The Peak Signal-to-Noise Ratio (PSNR) values of the Man image under different attacks are also shown in the Table 2. As seen from Table 2, all the attacks distort the Man image to have low PSNR values,



TABLE 2. The DCT coefficients of D_1 for the Man image under different attacks.

A tto also	DCNID	AC coefficients of matrix D_1 for Man image								
Attacks	PSNR	$D_1(1,2)$	$D_1(2,1)$	$D_1(3,1)$	$D_1(2,2)$	$D_1(1,3)$	$D_1(1,4)$	$D_1(2,3)$	$D_1(3,2)$	
No	Inf	25.8756	-6.9381	1.2278	0.0225	-1.2684	2.5842	0.0915	0.0463	
(a)	11.3686	19.7750	-8.0307	1.0601	0.0785	-1.1178	1.9533	0.0863	0.0961	
(b)	13.7787	26.4954	-8.6092	1.3148	0.0551	-1.3379	2.6470	0.0996	0.0233	
(c)	26.9180	25.9576	-8.7022	1.5331	0.1864	-1.1778	2.6016	0.1177	0.0912	
(d)	25.7431	28.8509	-5.7183	1.3863	-0.4789	-1.4461	2.7829	0.0657	0.0274	
(e)	23.8608	25.3355	-6.3649	1.3903	-0.1494	-1.2811	2.5380	0.0848	0.0484	
(f)	17.7057	28.0652	-0.3070	2.0964	-0.0548	0.0642	2.8152	0.0918	0.0291	
(g)	18.6144	25.8909	1.7006	2.0119	-0.0545	-1.1336	2.5676	0.0275	-0.0743	

TABLE 3. The constructed sign sequences for the Man image under JPEG compression attacks.

AC	NT	Ç	Numbers of				
coefficients	No attacks	1%	2%	3%	4%	5%	changed signs
$D_i(1,2)$	10101111	10101111	10101111	10101111	10101111	10101111	0
$D_{i}(2,1)$	00001111	00001111	00001111	00001111	00001111	00001111	0
$D_{i}(3,1)$	11100000	11100000	11100000	11100000	11100000	11100000	0
$D_{i}(2,2)$	11010011	11010001	11010001	11010001	01010011	01010011	5
$D_{i}(1,3)$	01110001	01110001	01110001	01110001	01110101	01110101	2
$D_{i}(1,4)$	10101111	10101111	10101111	10101111	10101111	10101111	0
$D_{i}(2,3)$	11000000	11000000	11000000	11000000	11000000	10000000	1
$D_{i}(3,2)$	10110000	10110000	10110000	10110000	10110000	10110000	0

TABLE 4. The constructed sign sequences for the Man image under scaling attacks.

AC	N 1		Se	caling facto	rs		_ Numbers of changed signs
coefficients	No attacks	1/32	1/16	1/8	1/4	1/2	
$D_i(1,2)$	10101111	10101111	10101111	10101111	10101111	10101111	0
$D_{i}(2,1)$	00001111	00001011	00001111	00001111	00001111	00001111	1
$D_{i}(3,1)$	11100000	11100000	11100000	11100000	11100000	11100000	0
$D_{i}(2,2)$	11010011	01010000	0101011	01010011	01010011	11010011	6
$D_{i}(1,3)$	01110001	00110001	01110101	01110001	01110101	01110101	2
$D_{i}(1,4)$	10101111	10101111	10101111	10101111	10101111	10101111	0
$D_{i}(2,3)$	11000000	11110000	11100000	10000000	11000000	10000000	4
$D_i(3,2)$	10110000	00010000	10110000	10110000	10110000	10110000	2

and the DCT coefficients of D_1 are changed greatly, but their signs almost did not change.

Moreover, we extracted the signs of the AC coefficients at the same positions for the eight selected blocks to construct a sign sequence of 8 bits, such as '10101111', where '1' represents a positive or zero coefficient, and '0' represents a negative coefficient. Eight sign sequences can be obtained according to the eight different positions of the selected AC coefficients in every block. Tables 3 to 6 show the sign sequences of the Man image and the number of changed signs after different attacks. The elements of the sign sequences shown in bold also denote that the signs of the coefficients have changed after the test image was subjected to some attacks. As seen in Tables 3 to 6, the signs of the selected AC coefficients are robust to the above attacks. We can utilize the polarities of the signs to construct the binary feature vector as the original zero-watermark. In our watermarking scheme, we used the sign of the first AC coefficient at (1, 2) of every block to construct the original zero-watermark because its robustness is the best to various attacks for all the selected coefficients in our experiments. Furthermore, if every block of size 8×8 can generate at least one bit of zero-watermark, the embedding capacity of the watermark will be increased compared with the methods in [59], [60].

B. ZERO-WATERMARK GENERATION

Let I be the original host image of size $N \times N$ and W be the original binary watermark image of size $M \times M$, where $N/M = 2^{l}$. The block diagram of the zero-watermark generation is illustrated in Fig. 5 and described as follows.

Step 1: Original watermark image scrambling

The original watermark W is scrambled by the Arnold transform to obtain W_1 with the private keys k_1 and T,

$$W_1 = \operatorname{Arnold}(W).$$
 (8)



TABLE 5. The constructed sign sequences for the Man image under rotation attacks.

AC	No attacks		Angles of rotation				
coefficients	No attacks	1	2	3	4	5	changed signs
$D_i(1,2)$	10101111	10101111	10101111	10101111	10101111	101011101	1
$D_{i}(2,1)$	00001111	00001111	00001111	10000111	10000111	10000101	7
$D_{i}(3,1)$	11100000	11100000	11100000	10100000	10100000	10100000	3
$D_{i}(2,2)$	11010011	11010001	0101000	11010000	11010000	11000000	11
$D_{i}(1,3)$	01110001	01110001	11110001	10110101	10100001	10100001	10
$D_{i}(1,4)$	10101111	10101111	10101111	10101111	10101111	10100101	2
$D_i(2,3)$	11000000	11000000	11010000	01010000	01010000	0111010	9
$D_i(3,2)$	10110000	11110000	11110000	11110100	11110101	11110101	10

TABLE 6. The constructed sign sequences for the Man image under translation attacks.

AC coefficients	NI++1	Distances of translation					Numbers of
	No attacks	2	4	6	8	10	changed signs
$D_i(1,2)$	10101111	10101111	10101111	10101111	10101111	10101111	0
$D_{i}(2,1)$	00001111	00001111	00001111	00001111	00001011	00001011	2
$D_{i}(3,1)$	11100000	11100000	11100000	11100000	11100000	11100000	0
$D_{i}(2,2)$	11010011	11010001	1101000	11010000	11010000	11010000	9
$D_i(1,3)$	01110001	01110001	01010001	01010001	01010001	01010001	4
$D_i(1,4)$	10101111	10101111	10101111	10101111	10101111	10101111	0
$D_i(2,3)$	11000000	10100000	10100000	10100000	10100000	0010100	12
$D_i(3,2)$	10110000	10110000	10110000	10110000	00110100	00100100	5

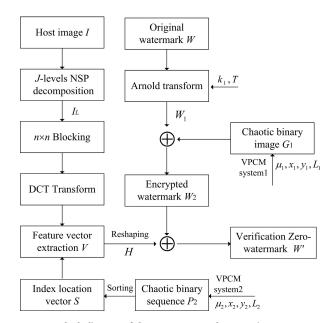


FIGURE 5. Block diagram of the zero-watermark generation process.

Step 2: Watermark encryption

A random sequence $Y_1 = \{y_n | n = 1, 2, ..., M^2 + L_1\}$ is generated by the VPCM system. Then, a new sequence $P_1 = \{y_n | n = L_1 + 1, L_1 + 2, ..., M^2 + L_1\}$ is defined. P_1 is converted into a binary image denoted by G_1 . Then an exclusive-or operation is performed between G_1 and W_1 to obtain the encrypted watermark W_2 ,

$$W_2 = XOR(W_1, G_1).$$
 (9)

Step 3: Robust feature extraction

NSPD is performed on the original host image I. Then, the low-frequency sub-band image I_L is divided into non-overlapping blocks of size $n_1 \times n_1$. Every block is decomposed by 2D-DCT, and the first AC coefficients in the order of Zigzag scanning for all blocks are selected out to construct the 1D feature vector U(k).

Step 4: Zero-watermark vector construction

As Step 2., the random sequences $Y_2 = \{z_n | n = 1, 2, ..., M^2 + L_2\}$ and $P_2 = \{z_n | n = L_2 + 1, L_2 + 2, ..., M^2 + L_2\}$ are generated. Then, the elements of P_2 are arranged in ascending order using the equation $[P_3, S] = \text{sort}(P_2)$ to obtain a new sequence P_3 and the index location vector S. The zero-watermark vector V(k) is constructed by judging whether every element of U(k) is larger than 0 or not as the order of S,

$$V(k) = \begin{cases} 1 & \text{if } U(S(k)) > 0 \\ 0 & \text{otherwise,} \end{cases} \quad k = 1, 2, \dots, M^2. \quad (10)$$

Step 5: Generation of the verification zero-watermark image

V(k) is reshaped into a binary image denoted by Q. Then, an exclusive-or operation is performed between the encrypted watermark W_2 and Q to generate the verification zero-watermark image W',

$$W' = XOR(W_2, Q). \tag{11}$$

C. ZERO-WATERMARK EXTRACTION

The procedure of zero-watermark extraction consists of two processes: image rotation correction and final



zero-watermark extraction. After doing a abundant of experiments, we found that the significant differences can exist among the NC values, which are used to assess the similarities between an image and its rotated images with different angles. In addition, when the original image and its rotated images are scaled down to the smaller size simultaneously, the differences among above NC values are not cut down. So this experimental conclusion can be utilized to estimate the angle of the rotated image. Based on the conclusion, the method of image rotation correction proposed in our previous work [61] is used again in this scheme. The block diagram of the zero-watermark extraction process is shown in Fig. 6. Suppose I_1 is the image to be verified, which may have undergone some attacks, the detailed steps of zero-watermark extraction are described as follows.

Step 1: Image rotation detection and correction

- (a) To decide whether I_1 undergoes rotation attacks or not, the means of four blocks of size $b_1 \times b_1$, which are located in the four corners of I_1 , are calculated. If I_1 has undergone rotation attacks, the processes from (b) to (e) are performed. Otherwise, Step 2 is performed immediately.
- (b) In order to reduce the computational cost, I and I_1 of size $N \times N$ are scaled down into two new images A and A_1 of size $b_2 \times b_2$ respectively.
- (c) A is rotated by 10m degrees sequentially, where m is a positive integer from 1 to 36. The NC value (described in Section 4) is calculated between every rotated A and A_1 for each m. The number m_1 is corresponds to the largest NC value.
- (d) A is rotated by $10m_1 + e$ degrees sequentially, where e is a positive integer from 1 to 10. The NC value is calculated between every rotated A and A_1 in turns again for each e.
- (e) I_1 is rotated by the angle corresponding to the largest NC value in (d) in the opposite direction to obtain the corrected image I_2 .

Step 2: Robust vector extraction

NSPD is performed on the image I_2 . Note that I_2 is the same with I_1 if I_1 does not undergo rotation attacks. The low-frequency sub-band image I_{2L} is divided into non-overlapping blocks of size $n_1 \times n_1$, and the 1D feature vector U'(k) is constructed by the process of zero-watermark generation.

Step 3: Zero-watermark vector construction

The random sequence P_3 and its index location vector S are generated by the same secret keys. Then, the zero-watermark vector V'(k) is obtained as follows:

$$V'(k) = \begin{cases} 1 & \text{if } U'(S(k)) > 0 \\ 0 & \text{otherwise,} \end{cases} \quad k = 1, 2, \dots, M^2.$$
 (12)

Step 4: Final watermark image extraction

V'(k) is reshaped into a binary image Q', and the chaotic binary image G_1 is also generated by the saved private keys. Then, an exclusive-or operations and the inverse Arnold transform are performed to extract the final

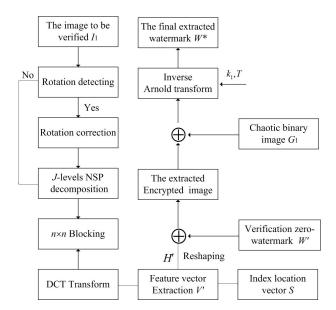


FIGURE 6. Block diagram of the zero-watermark extraction process.

watermark W^* by

$$W^* = \operatorname{Arnold}^{-1}(\operatorname{XOR}(\operatorname{XOR}(Q', W'), G_1)). \tag{13}$$

IV. EXPERIMENTAL RESULTS

To verify the validity and feasibility of the proposed scheme, we performed a series of experiments in this section. Eight well-known images of size 512×512 from the image database of USC-SIPI [62] were taken as the host images, i.e., Man, Tiffany, Elain, Lena, Goldhill, Boat, Bridge and Peppers, as shown in Fig. 7. Four binary watermark images with different sizes were used as the original watermark images, as shown in Fig. 8. The host images were decomposed by NSPD with J = 5 stages and 'maxflat' filter. The lowfrequency sub-band image of size 512×512 was divided into non-overlapping blocks according to the size of watermark. For the Arnold transform, the scrambling time k_1 was 12 and T = 24. The initial state values and control parameters of the VPCM system for the two random sequences were respectively assigned as $\mu_1 = 3.89999$, $x_1 = 0.65555$, $y_1 = 0.10000, \mu_2 = 3.98880, x_2 = 0.45550, y_2 = 0.22220,$ and $L_1 = L_2 = 500$. The parameters b_1 and b_2 in the process of image rotation correction were 2 and 20, respectively.

The objective criteria PSNR, NC and Bit error rate(BER) were used in our experiments. The PSNR was used to evaluate the quality of the host images under different attacks, defined as [63]:

PSNR =
$$10 \log_{10} \frac{255^2 \times N^2}{\sum_{x=1}^{N} \sum_{y=1}^{N} (I(x, y) - I'(x, y))^2}$$
 (14)

where I and I' represent the host and the attacked images of size $N \times N$, respectively.



TABLE 7. The similarity test of original zero-watermarks for different host images.

Images	Man	Tiffany	Elain	Lena	Goldhill	Boat	Bridge	Peppers
Man	1	0.4627	0.5602	0.4832	0.5305	0.4459	0.5107	0.4858
Tiffany	0.4627	1	0.4636	0.4355	0.5004	0.4726	0.4822	0.3834
Elain	0.5602	0.4636	1	0.5339	0.5627	0.5080	0.5701	0.5016
Lena	0.4832	0.4355	0.5339	1	0.4993	0.5182	0.5257	0.4344
Goldhill	0.5305	0.5004	0.5627	0.4993	1	0.5417	0.5336	0.4526
Boat	0.4459	0.4726	0.5080	0.5182	0.5417	1	0.5830	0.4312
Bridge	0.5107	0.4822	0.5701	0.5257	0.5336	0.5830	1	0.4639
Peppers	0.3834	0.3834	0.5016	0.4344	0.4526	0.4312	0.4639	1

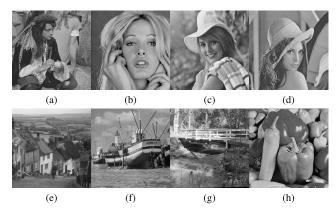


FIGURE 7. The host images used in the experiments: (a) Man, (b) Tiffany, (c) Elain, (d) Lena, (e) Goldhill, (f) Boat, (g) Bridge, (h) Peppers.

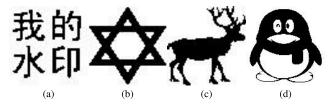


FIGURE 8. The original watermarks used in the experiments: (a) Watermark 1 of size 64×64 , (b) Watermark 2 of size 64×64 , (c) Watermark 3 of size 64×64 , (d) Watermark 4 of size 128×128 .

The NC and BER were used to evaluate the robustness of the proposed scheme. They are respectively defined as [3], [47]:

$$NC(W, W^*) = \frac{\sum_{i=1}^{M} \sum_{j=1}^{M} W(i, j) W^*(i, j)}{\sqrt{\sum_{i=1}^{M} \sum_{j=1}^{M} W^2(i, j)} \sqrt{\sum_{i=1}^{M} \sum_{j=1}^{M} W^{*2}(i, j)}}, \quad (15)$$

$$BER = \frac{B}{M \times M} \times 100. \quad (16)$$

where W and W^* represent the original and the extracted watermarks of size $M \times M$, respectively. B is the sum of inaccurate bits.

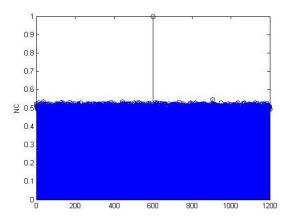


FIGURE 9. Similarities between the original zero-watermark and the random binary matrices.

A. UNIQUENESS VERIFICATION OF ZERO-WATERMARKS

In this subsection, we discuss the uniqueness verification of zero-watermarks similar to the method used in [37]. The zero-watermark constructed from an image should only be relevant to this image. In other words, the zero-watermarks constructed from different images should be different so that the zero-watermark constructed from an image just can uniquely identify this image [43]. The similarity between two different zero-watermark binary images constructed from different images is shown in Table 7. Table 7 shows that the maximum NC value of two different images is 0.5701, which is far less than 1. Therefore, the zero-watermark constructed from an image can be effectively distinguished from the zero-watermarks constructed from other different images.

To further verify the uniqueness of the zero-watermark constructed from an image in the proposed scheme, we produced 1200 random binary sequences from a uniform distribution and reshaped them into 2D images. Then, we calculated their respective NC values with the zero-watermark binary image constructed from the Man image. The results are shown in Fig. 9, where the 600th sequence corresponds to the zero-watermark of the Man image. Fig. 9 shows that all the NC values fluctuate around 0.5 in an extremely small range except the right zero-watermark of the Man image. Hence, it can be concluded that the zero-watermark constructed from an image in our proposed method can not be generated randomly and the image can be identified uniquely.



TABLE 8. The PSNR/NC values for different images under Gaussian noise attacks.

TY+:		Variances of Gaussian noise (Mean 0)							
Host image	0.01	0.05	0.1	0.15	0.2				
Man	20.07/0.9908	13.68/0.9817	11.38/0.9703	10.24/0.9649	9.53/0.9635				
Tiffany	20.04/0.9886	13.54/0.9776	11.26/0.9628	10.14/0.9608	9.50/0.9516				
Elain	20.07/0.9898	13.62/0.9764	11.31/0.9696	10.19/0.9656	9.51/0.9514				
Lena	20.02/0.9901	13.56/0.9750	11.24/0.9684	10.15/0.9591	9.49/0.9598				
Goldhill	20.12/0.9741	13.68/0.9458	11.40/0.9167	10.25/0.9082	9.55/0.9090				
Boat	20.11/0.9770	13.61/0.9413	11.29/0.9283	10.18/0.9140	9.52/0.8972				
Bridge	20.18/0.9873	13.79/0.9665	11.45/0.9547	10.31/0.9468	9.58/0.9336				
Peppers	20.16/0.9913	13.76/0.9804	11.44/0.9744	10.27/0.9679	9.56/0.9624				

TABLE 9. The PSNR/NC values for different images under Salt and Peppers noise attacks.

II4 5			Noise densities		
Host image	0.01	0.05	0.1	0.15	0.2
Man	25.18/0.9946	18.37/0.9869	15.37/0.9826	13.66/0.9759	12.40/0.9749
Tiffany	25.55/0.9944	18.56/0.9847	15.53/0.9791	13.75/0.9743	12.53/0.9714
Elain	25.42/0.9941	18.48/0.9887	15.47/0.9825	13.73/0.9744	12.44/0.9726
Lena	25.63/0.9957	18.59/0.9879	15.57/0.9815	13.84/0.9770	12.58/0.9643
Goldhill	25.28/0.9852	18.32/0.9680	15.32/0.9584	13.62/0.9459	12.43/0.9377
Boat	25.42/0.9885	18.45/0.9675	15.44/0.9583	13.69/0.9413	12.48/0.9359
Bridge	25.24/0.9925	18.28/0.9796	15.26/0.9726	13.48/0.9651	12.27/0.9532
Peppers	25.24/0.9954	18.27/0.9908	15.33/0.9865	13.51/0.9784	12.26/0.9755

TABLE 10. The PSNR/NC values for different images under Median filtering attacks.

**	Sizes of Median filter							
Host image	3×3	4×4	5×5	6×6	7×7			
Man	32.24/0.9978	27.50/0.9802	28.64/0.9927	26.30/0.9793	26.92/0.9871			
Tiffany	31.12/0.9956	26.96/0.9823	28.04/0.9913	25.88/0.9789	26.56/0.9898			
Elain	32.91/0.9989	29.38/0.9897	31.72/0.9973	28.96/0.9881	30.89/0.9957			
Lena	36.36/0.9986	29.65/0.9850	32.24/0.9964	28.59/0.9850	30.11/0.9951			
Goldhill	31.71/0.9956	28.30/0.9855	28.83/0.9893	27.08/0.9821	27.27/0.9852			
Boat	30.95/0.9940	26.51/0.9796	27.19/0.9841	25.04/0.9705	25.19/0.9733			
Bridge	26.73/0.9940	23.97/0.9812	24.02/0.9855	22.76/0.9739	22.68/0.9796			
Peppers	35.12 / 0.9992	$28.53 \not / 0.9847$	$32.35 \not / 0.9973$	27.85 / 0.9836	$30.36 \not/ 0.9933$			

B. ROBUSTNESS TESTS OF THE PROPOSED SCHEME

In this subsection, we present the experimental results for the robustness test of the proposed scheme under various attacks. The watermark image 1 was firstly used in this part. Several conventional image processing operations (adding noise, filtering, and JPEG compression) and the geometrical distortions (scaling, cropping, and rotation) were performed on the original host images. The robustness of the proposed scheme under the above-mentioned attacks was evaluated as follows.

1) ADDITION OF NOISE

Gaussian noise, Salt and Peppers noise are usually used to test the robustness of watermarking algorithms. For the Gaussian noise, we varied the amount of noise with respect to its variance while fixing its mean. For the Salt and Peppers noise, we degraded the quality by changing the noise densities. Table 8 shows the results of adding the Gaussian white noise with a mean of 0 and variances of 0.01 to 0.2 to the host images in terms of PSNR and NC values. Meanwhile, Table 9 shows the results of adding the Salt and Peppers noise with densities of 0.01 to 0.2 to the host images. As can be seen in the Tables, even though the test images are degraded greatly by the two types of noise with various noise variances or densities, the high NC values can be obtained. This means that the proposed scheme is robust against noise attacks.

2) FILTERING ATTACKS

Test images were filtered using Median filters and Wiener filters with size of 3×3 , 4×4 , 5×5 , 6×6 and 7×7 . Table 10 and 11 show the results in terms of PSNR and NC values for the Median and Wiener filters, respectively. The Tables show that the proposed scheme is highly robust to the Median filtering and Wiener filtering attacks. The NC values are very near to 1 in almost all of the cases, which demonstrates that the proposed scheme has



TABLE 11. The PSNR/NC values for different images under Wiener filtering attacks.

**		Sizes of Wiener filter							
Host image	3×3	4×4	5×5	6×6	7×7				
Man	35.14/0.9992	32.54/0.9948	31.72/0.9967	30.53/0.9929	29.92/0.9952				
Tiffany	34.76/0.9987	32.85/0.9946	32.41/0.9978	31.42/0.9938	31.10/0.9959				
Elain	33.66/0.9998	32.63/0.9935	32.53/0.9983	32.12/0.9935	31.96/0.9978				
Lena	38.85/0.9992	36.19/0.9946	35.74/0.9989	34.29/0.9948	33.73/0.9983				
Goldhill	34.12/0.9983	32.30/0.9933	31.35/0.9949	30.38/0.9906	29.67/0.9929				
Boat	34.10/0.9981	32.02/0.9930	31.18/0.9965	30.01/0.9917	29.29/0.9940				
Bridge	29.54/0.9986	27.44/0.9922	26.51/0.9956	$25.57^{'}/0.9905$	24.97/0.9924				
Peppers	36.62 / 0.9995	$34.85^{'}/0.9957$	34.69 / 0.9986	33.55/0.9948	33.18/0.9959				

TABLE 12. The PSNR/NC values for different images under JPEG compression attacks.

Host image			Quality factors(%)	•	
	1	5	10	20	40
Man	23.16/0.9960	25.74/0.9773	28.27/0.9929	30.55/0.9964	32.64/0.9981
Tiffany	23.49/0.9611	25.97/0.9727	28.40/0.9890	30.35/0.9960	32.25/0.9986
Elain	24.88/0.9592	27.50/0.9831	29.94/0.9906	31.60/0.9970	32.73/0.9976
Lena	24.78/0.9518	27.80/0.9744	30.99/0.9885	33.63/0.9952	35.87/0.9975
Goldhill	23.74/0.9243	26.16/0.9458	28.65/0.9746	$30.87^{'}/0.9887$	32.90/0.9897
Boat	22.99/0.9095	25.56/0.9515	28.13/0.9747	30.49/0.9882	32.75/0.9948
Bridge	21.08/0.9578	23.06/0.9780	25.13/0.9892	27.01/0.9952	28.85/0.998
Peppers	24.29/0.9699	27.18/0.9830	30.13/0.9909	32.42/0.9964	$34.20^{'}/0.9978$

TABLE 13. The PSNR/NC values for different images under cropping attacks attacks.

	Types of cropping							
Host image	Top-left 64×64	Top-left 128×128	$\begin{array}{c} \text{Center} \\ 128 \times 128 \end{array}$	Edge 64×512	Edge 128×512			
Man	24.47/0.9933	16.79/0.9770	15.45/0.9741	12.81/0.9335	9.88/0.9077			
Tiffany	21.46/0.9925	16.03/0.9749	17.99/0.9607	12.33/0.9347	10.53/0.8951			
Elain	28.08/0.9921	20.31/0.9783	17.29/0.9686	15.65/0.9553	12.52/0.9023			
Lena	26.74/0.9978	18.47/0.9709	18.33/0.9699	15.72/0.9813	11.56/0.8970			
Goldhill	29.67/0.9901	19.25/0.9741	15.90/0.9699	14.07/0.9560	11.03/0.8961			
Boat	24.73/0.9930	19.71/0.9792	18.34/0.9652	15.96/0.9553	12.70/0.9069			
Bridge	25.84/0.9976	19.84/0.9791	15.42/0.9627	16.21/0.9683	12.83/0.9210			
Peppers	24.39/0.9938	16.87/0.9713	$17.77^{'}/0.9774$	13.01/0.9311	10.76/0.8838			

superior performance against these two types of filtering attacks.

3) JPEG COMPRESSION

Any effective watermarking algorithm should be robust against compression attacks. We test our watermarking algorithm against JPEG compression, which is one of the most widely used common compression attacks. JPEG compression attacks with different quality factors of 1%, 5%, 10%, 20% and 40% were applied to the host images. The results in terms of PSNR and NC are summarized in Table 12. Table 12 shows that even though the quality factor is 1%, high NC values can be achieved. Therefore, the proposed scheme is highly robust against the JPEG compression attacks because the low-frequency components of the host images are used to construct the zero-watermarks.

4) CROPPING ATTACKS

To test the robustness against cropping attacks, the host images were cropped with different cropping windows. We used cropping window sizes of 64×64 , 128×128 , 64×512 , and 128×512 , and the cropping windows were black. The results in terms of PSNR and NC values are shown in Table 13. As seen in Table 13, even though the cropping window size is 128×512 , all the NC values are larger than 0.88 for the different test images. This verifies that the proposed scheme is robust against cropping attacks.

5) SCALING ATTACKS

For scaling attacks, we resized the original images by multiplying by a scaling factor, and then scaled back the images to their original sizes. If the scaling factor is less than 1, the images are scaled down, otherwise they are scaled up.



TABLE 14. The PSNR/NC values for different images under scaling attacks attacks.

II			Scaling factors		
Host image	1/16	1/8	1/4	1/2	2
Man	21.48/0.9776	23.86/0.9927	26.85/0.9987	31.04/0.9998	41.03/0.9998
Tiffany	21.46/0.9925	16.03/0.9749	17.99/0.9607	12.33/0.9347	10.53/0.8951
Elain	23.03/0.9809	27.01/0.9960	30.48/0.9992	33.09/1.0000	39.68/0.9998
Lena	23.18/0.9829	26.35/0.9952	30.01/0.9995	35.09/0.9995	45.09/0.9994
Goldhill	22.47/0.9711	24.93/0.9892	27.65/0.9967	31.44/0.9992	41.06/0.9994
Boat	20.81/0.9679	22.83/0.9870	25.53/0.9971	29.94/0.9986	39.53/0.9998
Bridge	18.98/0.9759	20.85/0.9909	23.06/0.9979	26.50/0.9995	35.83/0.9998
Peppers	21.22/0.9749	24.58/0.9954	27.92/0.9992	31.74/0.9995	40.98/0.9998

TABLE 15. The PSNR/NC values for different images under translation attacks.

TT	Distances of translation from left to right (pixels)						
Host image	1	2	3	4	5		
Man	24.96/0.9783	21.47/0.9570	19.89/0.9402	18.86/0.9232	18.10/0.9060		
Tiffany	24.76/0.9827	22.01/0.9665	20.79/0.9542	19.93/0.9389	19.21/0.924		
Elain	26.65/0.9734	23.71/0.9580	21.93/0.9440	20.34/0.9261	19.35/0.9113		
Lena	27.14/0.9853	23.23/0.9713	21.30/0.9598	20.03/0.9475	19.09/0.933		
Goldhill	26.08/0.9838	23.05/0.9693	21.57/0.9548	20.38/0.9434	19.67/0.9296		
Boat	23.40/0.9828	20.50/0.9651	19.18/0.9507	18.44/0.9329	17.92/0.917		
Bridge	22.17/0.9844	$19.34^{\prime}/0.9699$	18.19/0.9554	17.45/0.9419	16.88/0.929		
Peppers	26.79/0.9815	23.05/0.9624	20.81/0.9441	$19.33^{'}/0.9281$	18.24/0.912		

TABLE 16. The PSNR/NC values for different images under rotation attacks.

TT	Angles of rotation						
Host image	5°	10°	20°	40°	90°		
Man	14.86/0.9633	12.88/0.9474	11.14/0.9307	9.89/0.9189	11.64/1.0000		
Tiffany	15.56/0.9734	13.61/0.9664	12.03/0.9351	11.19/0.9182	13.13/1.0000		
Elain	14.53/0.9574	12.87/0.9412	11.17/0.9299	9.77/0.9149	10.90/1.0000		
Lena	15.33/0.9776	13.04/0.9646	11.66/0.9407	10.83/0.9125	12.42/1.0000		
Goldhill	15.12/0.9715	13.10/0.9623	11.43/0.9372	10.38/0.9196	10.65/1.0000		
Boat	23.40/0.9575	20.50/0.9419	19.18/0.9156	18.44/0.8974	17.92/1.0000		
Bridge	13.57/0.9691	12.09/0.9520	10.70/0.9153	9.67/0.9139	10.33/1.0000		
Peppers	13.56/0.9680	$11.47^{'}/0.9498$	9.99/0.9273	8.92/0.9176	10.48/1.0000		

Table 14 shows the results in terms of PSNR and NC values for the eight test images under scaling attacks with scaling factors of 1/16 to 2. From the Table 14, it can be demonstrated that the proposed watermarking scheme shows strong resistance to the scaling attacks.

6) TRANSLATION ATTACKS

For translation attacks, we translate the host images from left to right by 1, 2, 3, 4 and 5 pixels in turns before performing watermark extraction. The experimental results are shown in Table 15. As seen in Table 15, the NC values of the extracted zero-watermarks for translation attacks are not larger than those for other attacks, such as the addition of noise, filtering, and JPEG compression, but the minimum NC value is larger than 0.91. This means that the proposed scheme can effectively resist to the translation attacks.

7) ROTATION ATTACKS

The host images were also tested for geometric attacks of rotation. The images were respectively rotated by 5°, 10°, 20°, 40° and 90° before performing watermark detection. The results in terms of PSNR and NC values are shown in Table 16. Table 16 shows that the proposed scheme can successfully resist rotation attacks. Furthermore, the proposed scheme performs best against rotation attacks when the rotation angle is 90°. In fact, the same result can be obtained if the rotation angle is 180° or 270° because of the proposed method of image rotation correction. Since the proposed scheme can resist the rotation, scaling, and translation (RST) attacks, it can be considered as an RST-invariant watermarking algorithm. From the experimental results shown in Tables 8 to 16, we can conclude that the proposed scheme is highly robust against conventional image processing operations and some geometrical distortions.



TABLE 17. The PSNR/NC values for Lena image under different attacks.

A 441	DNCD		Watermark 1		Watermark 3	Watermark 4
Attacks	PNSR	32×32	64×64	128×128	64×64	128×128
Gaussian noise (0.05)	13.5306	0.9679/0.0459	0.9703/0.0452	0.9695/0.0464	0.9659/0.0454	0.9636/0.0457
Gaussian noise (0.15)	10.1598	0.9652/0.0498	0.9553/0.0667	0.9625/0.0569	0.9601/0.0530	0.9570/0.0540
Salt and Peppers noise (0.1)	15.6000	0.9864/0.0195	0.9831/0.0259	0.9827/0.0265	0.9786/0.0286	0.9725/0.0346
Salt and Peppers noise (0.2)	12.5448	0.9740/0.0371	0.9725/0.0420	0.9649/0.0466	0.9621/0.0505	0.9641/0.0451
Median filtering (5×5)	32.2413	0.9664/0.0479	0.9584/0.0630	0.9616/0.0583	0.9525/0.0630	0.9535/0.0583
Wiener filtering (5×5)	35.7395	0.9986/0.0020	0.9989/0.0017	0.9983/0.0026	0.9987/0.0017	0.9980/0.0026
JPEG compression (5%)	27.7996	0.9623/0.0537	0.9518/0.0728	0.9505/0.0749	0.9450/0.0728	0.9400/0.0749
JPEG compression (20%)	33.6275	0.9959/0.0059	0.9952/0.0073	0.9954/0.0071	0.9945/0.0073	0.9944/0.0071
Scaling (1/8)	26.3543	0.9857/0.0205	0.9829/0.0261	0.9825/0.0269	0.9805/0.0261	0.9787/0.0269
Cropping (center 128×128)	18.3265	0.9678/0.0459	0.9722/0.0425	0.9699/0.0459	0.9682/0.0425	0.9634/0.0459
Cropping (Edge 64×512)	15.7225	0.8947/0.0146	0.8906/0.1614	0.8902/0.1619	0.8748/0.1614	0.86800.1619/
Translation (5 pixels)	19.0941	0.8661/0.1855	0.8676/0.1936	0.8672/0.1943	0.8500/0.1936	08414/0.1943
Rotation(5°)	15.3284	0.9748/0.0361	0.9776/0.0342	0.9769/0.0353	0.9744/0.0342	0.9719/0.0353
Rotation(10°)	13.0434	0.9665/0.0479	0.9646/0.0537	0.9647/0.0536	0.9596/0.0537	0.9572/0.0536
Rotation(40°)	10.8319	0.9109/0.1250	0.9125/0.1299	0.9103/0.1335	0.9005/0.1299	0.8919/0.1335
Rotation(90°)	12.4175	1.0000/0.0000	1.0000/0.0000	1.0000/0.0000	1.0000/0.0000	1.0000/0.0000

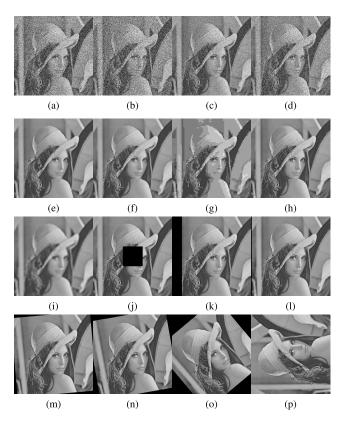


FIGURE 10. The attacked Lena image under different attacks (a) Gaussian noise (0.05), (b) Gaussian noise (0.15), (c) Salt and Peppers noise(0.1), (d) Salt and Peppers noise (0.2), (e) Median filtering (5×5), (f) Wiener filtering (5×5), (g) JPEG compression(5%), (h) JPEG compression (20%), (i) Scaling (1/8), (j) Cropping (center 128×128), (k) Cropping (Edge 64×512), (l) Translation (5 pixels), (m) Rotation (5°), (n) Rotation (10°), (o) Rotation(40°), (p) Rotation (90°).

To further demonstrate the robustness of the proposed scheme, more experiments for robustness test were completed. In this part, sixteen attacks were selected shown in Table 17, and Lena was used as host image. After above sixteen attacks, attacked Lena images are shown in Fig. 10.

TABLE 18. Robustness test of proposed scheme under Checkmark attacks.

Checkmark attacks	PSNR	NC	BER
Soft thresh(2)	33.9399	0.9968	0.0049
Hard thresh (2)	34.9442	0.9983	0.0027
Dither (2)	6.5338	0.9946	0.0083
Dprorr (1)	29.9750	0.9964	0.0056
Linear (5)	16.5825	0.9323	0.1016
Midpoint (2)	26.9431	0.9449	0.0078
Nulineremove (2)	35.3325	0.9960	0.0061
Projective (2)	19.9948	0.9557	0.0671
Ratio (4)	28.2486	0.9956	0.0068
Rotation scale(12)	19.3888	0.9122	0.1304
Row col (12)	31.7333	0.9927	0.0112
Sample down up (4)	33.2087	0.9944	0.0085
Scale (3)	36.0917	0.9949	0.0078
Sharpening (1)	23.3342	0.9818	0.0278
Shearing (4)	15.6781	0.8807	0.1758
Stimark (1)	25.5343	0.9801	0.0305
Template remove (1)	38.1953	0.9992	0.0012
Trimmed mean (2)	31.3160	0.9989	0.0071
Warp (1)	18.2210	0.9141	0.1279
Wavelet compression (10%)	30.5847	0.9895	0.0161

The PSNR values of attacked Lena images and the NC/BER values of watermarks extracted from them are also shown in Table 17. The PSNR values indicate that the host images are badly distorted under different attacks. The NC and BER values of the extracted watermarks prove that the extracted watermarks are very closely similar to the original watermark excepting for the cropping attacks with large areas. These data generally illustrate that the proposed scheme is robust to different attacks for multiple watermarks also with different sizes. For watermark image 1 of size 64×64 , watermark image 3 of size 64 × 64 and watermark image 4 of size 128×128 , the extracted watermarks from the corresponding attacked Lena images are shown in Fig. 11 to Fig. 13. In any case, it can be observed form the Fig. 10 to Fig. 13 that even though the host images are seriously degraded by different attacks, the corresponding extracted watermarks with different contents and sizes are basically clear enough. This





FIGURE 11. The extracted watermark image 1 for Lena image under different attacks: (a) Gaussian noise (0.05), (b) Gaussian noise (0.15), (c) Salt and Peppers noise(0.1), (d) Salt and Peppers noise (0.2), (e) Median filtering (5×5) , (f) Wiener filtering (5×5) , (g) JPEG compression(5%), (h) JPEG compression (20%), (i) Scaling (118), (j) Cropping (center 128 \times 128), (k) Cropping (Edge 64×512), (l) Translation (5 pixels), (m) Rotation (5°), (n) Rotation (10°), (o) Rotation(40°), (p) Rotation (90°).

demonstrates that the proposed scheme exhibits excellent performance against the attacks mentioned in Table 17. Table 18 shows the robustness test results of the proposed scheme against the standard benchmark software Checkmark [64]. In Table 18, twenty kinds of attacks in Checkmark, which are not almost mentioned in Table 17, are selected out to test the proposed scheme, and the PSNR, NC and BER values for different attacks are shown respectively. For these attacks, the NC and BER values are well accepted except the rotation scale, shearing and warp attacks, but the minimum NC value is 0.8807 while the maximum BER value is 0.1758. As can be seen from Table 18, the proposed scheme is robust to Checkmark attacks to some extent.

C. COMPARISON WITH OTHER ZERO-WATERMARKING ALGORITHMS

To evaluate the robustness of the proposed scheme in comparison with other methods, we have compared the results of our scheme with the three methods in [38], [40], [42]. We firstly embedded the 64×64 watermark image 2, shown in Fig. 8, into the host gray-scale images in all the algorithms. In the experiments, eight common attacks were adopted, including (1) Gaussian noise (0.05), (2) Salt and Peppers noise (0.1), (3) Median filtering (5 \times 5), (4) JPEG compression

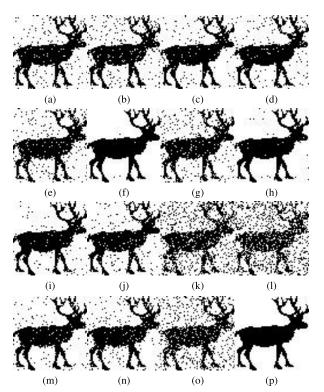


FIGURE 12. The extracted watermark image 3 for Lena image under different attacks: (a) Gaussian noise (0.05), (b) Gaussian noise (0.15), (c) Salt and Peppers noise(0.1), (d) Salt and Peppers noise (0.2), (e) Median filtering (5 × 5), (f) Wiener filtering (5 × 5), (g) JPEG compression(5%), (h) JPEG compression (20%), (i) Scaling (1/8), (j) Cropping (center 128 × 128), (k) Cropping (Edge 64 × 512), (l) Translation (5 pixels), (m) Rotation (5°), (n) Rotation (10°), (o) Rotation(40°), (p) Rotation (90°).

(10%), (5) Scaling (1/8), (6) Cropping (center 128×128), (7) Translation (5 pixels) and (8) Rotation (5°). Since several attacks can happen on an image simultaneously, it is also important to investigate the robustness of a watermarking scheme against combined attacks. Hence, we additionally tested four types of combined attacks, including (9) Gaussian noise (0.01)+ JPEG compression (10%), (10) Median filtering (3×3) + Scaling (1/8), (11) Salt and Peppers noise (0.02)+ Median filtering (5×5) + Rotation (1°) , and (12)Gaussian noise (0.01)+ Scaling (1/8)+ JPEG compression (5%). The Peppers image shown in Fig. 7 was used as the test image at this time. Table 19 shows the extracted watermarks from attacked Peppers images using the proposed scheme and the three methods in [38], [40], [42], and it can prove that the proposed scheme is more robust than other three methods. Because of the strong attack parameters used in the comparison experiments, some of the extracted watermarks in other three comparative methods are almost not clear enough in Table 19. For the watermark image 2 of size 32×32 , watermark image 3 of size 64×64 and watermark image 4 of size 128×128 , the same host image and attacks mentioned in Table 19 are used to test the robustness among the different methods. Fig. 14 to Fig. 16 show the comparison of the results in terms of average BER values of the extracted different



 $\begin{tabular}{ll} \textbf{TABLE 19.} & \textbf{The extracted watermarks for Peppers image using different methods.} \\ \end{tabular}$

	A., 1., 1.1		Extracted v	vatermarks	
No.	Attack types and the corresponding PSNR values	DC-RE in [38]	PVMF in [40]	Method in [42]	Proposed scheme
1	Gaussian noise (0.05) PSNR=13.7545		īΧ	X _X X	XX
2	Salt and Peppers noise (0.1) PSNR=15.3457		XX	XX	XX
3	Median filtering (5×5) PSNR=32.3463	XX	ХХ	XX	XX
4	JPEG compression (10%) PSNR=31.1288	XX	X,X	Χ̈́Х	XX
5	Scaling (1/8) PSNR=24.5768	XX	X	X	X
6	Cropping (center 128 × 128) PSNR=17.7666	XX	XX	XX	XX
7	Translation (5 pixels) PSNR=18.2372		Ý	XX	XX
8	Rotation (5°) PSNR=15.5551				ΧX
9	Gaussian noise (0.1) +JPEG compression (10%) PSNR=24.1970	X	XX	XX	XX
10	Gaussian noise (0.1) +Scaling (1/8), PSNR=24.5514	XX	ΧX	X	XX
11	Salt and Peppers noise (0.02) +Median filtering (5 \times 5) +Rotation (1°), PSNR=20.7589	XX	众	XX	XX
12	Salt and Peppers noise (0.01) +JPEG compression (10%) +Scaling (1/8), PSNR=23.3525			ΧÇΣ	X



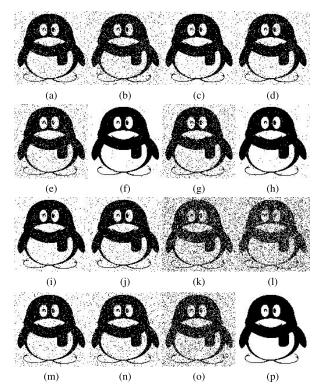


FIGURE 13. The extracted watermark image 4 for Lena image under different attacks: (a) Gaussian noise (0.05), (b) Gaussian noise (0.15), (c) Salt and Peppers noise (0.1), (d) Salt and Peppers noise (0.2), (e) Median filtering (5×5), (f) Wiener filtering (5×5), (g) JPEG compression(5%), (h) JPEG compression (20%), (i) Scaling (1/8), (j) Cropping (center 128×128), (k) Cropping (Edge 64×512), (l) Translation (5 pixels), (m) Rotation (5°), (n) Rotation (10°), (o) Rotation(40°), (p) Rotation (90°).

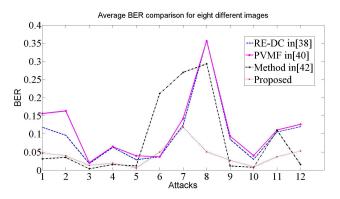


FIGURE 14. The average BER values in different methods with watermark image 2 of sizes 32×32 .

watermarks for eight test images shown in Fig. 7. As can be seen from Fig. 14 to Fig. 16, it is clear that the proposed scheme generally outperforms the other three watermarking methods in [38], [40], [42] for the above attacks. Especially, this advantage is more obvious when the size of watermark is large, for instance, the watermark image 4 used in Fig.16.

D. STATISTICAL ANALYSIS

In this section, a statistical analysis is performed between our proposed scheme and the each method in [38], [40], [42].

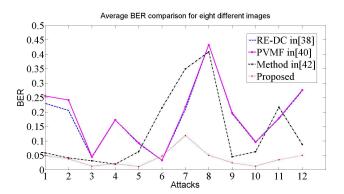


FIGURE 15. The average BER values in different methods with watermark image 3 of sizes 64×64 .

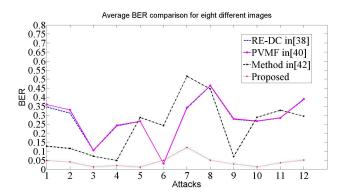


FIGURE 16. The average BER values in different methods with watermark image 4 of sizes 128×128 .

TABLE 20. The average PSNR/NC values under Gaussian noise attacks.

NT .		NC					
Noise variances	PSNR	Proposed scheme	Method in [38]	PVMF in [40]	Method in [42]		
0.01	20.0975	0.9861	0.9031	0.8978	0.9873		
0.02	17.2101	0.9793	0.8776	0.8688	0.9704		
0.05	13.6507	0.9686	0.8398	0.8213	0.9691		
0.1	11.3515	0.9563	0.8108	0.7873	0.9455		
0.15	10.2231	0.9493	0.7890	0.7644	0.9454		
0.2	9.5321	0.9415	0.7770	0.7475	0.9310		
0.25	9.0570	0.9365	0.7652	0.7395	0.9252		

According to the way mentioned in [65], Wilcoxon signed ranks test with a significance level of 0.05 is same to be used to assess the statistical significance of the difference between the proposed scheme and the each method in [38], [40], [42]. The robustness tests of the these compared algorithms against the attacks are shown in Tables 20 to 28. In the Tables 20 to 28, the average PSNR/NC values under different attacks for all the eight test images, shown in Fig. 7, are calculated. Furthermore, in order to satisfy the requirement for the number of statistical samples, the number of a certain type attacks in Tables 20 to 28 is increased form 5 to 7 comparing with that in the Tables 8 to 16.



TABLE 21. The average PSNR/NC values under Salt and Peppers noise attacks.

NI-:			NO	C	
Noise densities	PSNR	Proposed scheme	Method in [38]	PVMF in [40]	Method in [42]
0.01	25.4547	0.9925	0.9464	0.9403	0.9911
0.02	22.3985	0.9895	0.9229	0.9119	0.9872
0.05	18.4239	0.9817	0.8924	0.8683	0.9833
0.1	15.4139	0.9732	0.8613	0.8318	0.9637
0.15	13.6794	0.9667	0.8348	0.8087	0.9599
0.2	12.4090	0.9606	0.8169	0.7871	0.9520
0.25	11.4291	0.9527	0.8015	0.7760	0.9373

TABLE 22. The average PSNR/NC values under Median filtering attacks.

C: C		NC					
Sizes of filter	PSNR	Proposed scheme	Method in [38]	PVMF in [40]	Method in [42]		
3×3	32.1413	0.9967	0.9834	0.9824	0.9872		
4×4	27.5993	0.9835	0.9618	0.9608	0.9454		
5×5	29.1302	0.9917	0.9717	0.9708	0.9795		
6×6	26.5578	0.9802	0.9542	0.9526	0.9321		
7×7	27.4955	0.9874	0.9603	0.9592	0.9665		
9×9	26.3120	0.8558	0.9472	0.9461	0.9572		
11×11	25.4070	0.8549	0.9324	0.9314	0.9375		

TABLE 23. The average PSNR/NC values under Wiener filtering attacks.

C' C		NC					
Sizes of filter	PSNR	Proposed scheme	Method in [38]	PVMF in [40]	Method in [42]		
3×3	34.5984	0.9989	0.9894	0.9877	0.9924		
4×4	32.6026	0.9939	0.9751	0.9741	0.9898		
5×5	32.0164	0.9972	0.9796	0.9782	0.9834		
6×6	30.9845	0.9928	0.9678	0.9667	0.9860		
7×7	30.4787	0.9953	0.9677	0.9665	0.9783		
9×9	29.3087	0.9933	0.9547	0.9541	0.9704		
11×11	28.3664	0.9901	0.9400	0.9390	0.9652		

TABLE 24. The average PSNR/NC values under JPEG compression attacks.

Ovolity		NC					
Quality factors	PSNR	Proposed scheme	Method in [38]	PVMF in [40]	Method in [42]		
1%	23.5509	0.9500	0.7942	0.7922	0.9303		
5%	26.1208	0.9707	0.8286	0.8294	0.9678		
10%	28.7050	0.9863	0.8828	0.8822	0.9872		
20%	30.8657	0.9941	0.9287	0.9281	0.9936		
30%	32.0099	0.9955	0.9450	0.9455	0.9924		
40%	32.7744	0.9965	0.9571	0.9574	0.9962		
50%	33.4156	0.9976	0.9632	0.9654	0.9949		

In this part, IBM SPSS Statistics 26 was used to perform the statistical calculations. The null hypothesis H_0 indicates that there is no significant difference between the proposed scheme and the each method in [38], [40], [42]. In contrast, the alternative hypothesis H_1 indicates that a significant difference exists between the proposed scheme and the each

TABLE 25. The average PSNR/NC values under cropping attacks.

Tymas of		NC				
Types of croppping	PSNR	Proposed scheme	Method in [38]	PVMF in [40]	Method in [42]	
Top-left 32×32 Top-left 64×64	32.7752 25.6729	0.9960 0.9938	0.9985 0.9951	0.9985 0.9951	0.9691 0.9413	
Top-left 64×128	22.1912	0.9872	0.9906	0.9906	0.9455	
Top-left 128×128	18.4087	0.9756	0.9813	0.9813	0.8967	
Center 128×128	17.0610 14.4700	0.9686	0.9785 0.9605	0.9784 0.9607	0.8508 0.6732	
Edge 64×512 Edge 128×512	8.4867	$0.9519 \\ 0.7921$	0.9605 0.8361	0.9607 0.8364	0.6732 0.7224	

TABLE 26. The average PSNR/NC values under scaling attacks.

Scaling factors		NC				
	PSNR	Proposed scheme	Method in [38]	PVMF in [40]	Method in [42]	
1/32	32.7752	0.8831	0.7343	0.7333	0.7361	
1/16	25.6729	0.9765	0.8144	0.8139	0.8317	
1/8	22.1912	0.9927	0.9397	0.9382	0.9584	
1/4	18.4087	0.9985	0.9780	0.9758	0.9949	
1/2	17.0610	0.9994	0.9905	0.9887	0.9975	
$\dot{2}$	14.4700	0.9997	0.9959	0.9947	1.0000	
4	8.4867	0.9999	0.9967	0.9954	1.0000	

TABLE 27. The average PSNR/NC values under translation attacks.

Distances of translation		NC				
	PSNR	Proposed scheme	Method in [38]	PVMF in [40]	Method in [42]	
1 pixel	25.2435	0.9815	0.9659	0.9583	0.8913	
2 pixels	22.0444	0.9649	0.9362	0.9289	0.8076	
3 pixels	20.4578	0.9504	0.9076	0.9000	0.7789	
4 pixels	19.3440	0.9353	0.8803	0.8740	0.7671	
5 pixels	18.5579	0.9205	0.8561	0.8500	0.7472	
6 pixels	17.9150	0.9058	0.8323	0.8270	0.7264	
7 pixels	17.3867	0.8914	0.8095	0.8059	0.6955	

TABLE 28. The average PSNR/NC values under rotation attacks.

Angles of rotation		NC					
	PSNR	Proposed scheme	Method in [38]	PVMF in [40]	Method in [42]		
5°	14.6148	0.9672	0.6799	0.6808	0.7014		
10°	12.7213	0.9532	0.6488	0.6489	0.6840		
20°	11.1588	0.9290	0.6287	0.6276	0.6488		
30°	10.4677	0.9204	0.9294	0.6299	0.6360		
40°	10.0856	0.9141	0.6240	0.6239	0.5895		
50°	9.9846	0.9096	0.6256	0.6239	0.6401		
90°	11.4102	1.0000	0.6207	0.6193	0.6306		

method in [38], [40], [42]. With a 95% confidence level, H_0 is rejected if $\alpha \le 0.05$, and H_0 can not be rejected if $\alpha > 0.05$. In the case of rejecting H_0 ($\alpha \le 0.05$), the final decision is made according to the result whether the sum of the negative ranks w^- is smaller than or equal to the critical value for the Wilcoxon signed rank test. If the sum of the negative ranks



TABLE 29. Statistical comparison using the Wilcoxon signed-rank test.

Attacks	Proposed scheme vs method in [38]	Proposed scheme vs PVMF in [40]	Proposed scheme vs method in [42]
Gaussian noise (Table 18)	Reject H_0 , with $\alpha = 0.018$	Reject H_0 , with $\alpha = 0.018$	Reject H_0 , with $\alpha = 0.063$
	$w_{\alpha}^* = 3, w^- = 0, w^- \le w_{\alpha}^*$	$w_{\alpha}^* = 3, w^- = 0, w^- \le w_{\alpha}^*$	$w_{\alpha}^* = 3, w^- = 3, w^- \le w_{\alpha}^*$
Salt and Peppers noise (Table 19)	Reject H_0 , with $\alpha = 0.018$	Reject H_0 , with $\alpha = 0.018$	Reject H_0 , with $\alpha = 0.043$
	$w_{\alpha}^* = 3, w^- = 0, w^- \le w_{\alpha}^*$	$w_{\alpha}^* = 3, w^- = 0, w^- \le w_{\alpha}^*$	$w_{\alpha}^* = 3, w^- = 2, w^- \le w_{\alpha}^*$
Median filtering (Table 20)	Can not reject H_0 , with $\alpha = 0.866$	Can not reject H_0 , with $\alpha = 0.866$	Can not reject H_0 , with $\alpha = 0.866$
	$w_{\alpha}^* = 3, w^- = 13, w^- > w_{\alpha}^*$	$w_{\alpha}^* = 3, w^- = 13, w^- > w_{\alpha}^*$	$w_{\alpha}^* = 3, w^- = 13, w^- > w_{\alpha}^*$
Wiener filtering (Table 21)	Reject H_0 , with $\alpha = 0.018$	Reject H_0 , with $\alpha = 0.018$	Reject H_0 , with $\alpha = 0.018$
	$w_{\alpha}^* = 3, w^- = 0, w^- \le w_{\alpha}^*$	$w_{\alpha}^* = 3, w^- = 0, w^- \le w_{\alpha}^*$	$w_{\alpha}^* = 3, w^- = 0, w^- \le w_{\alpha}^*$
JPEG compression (Table 22)	Reject H_0 , with $\alpha = 0.018$	Reject H_0 , with $\alpha = 0.018$	Reject H_0 , with $\alpha = 0.018$
	$w_{\alpha}^* = 3, w^- = 0, w^- < w_{\alpha}^*$	$w_{\alpha}^* = 3, w^- = 0, w^- \le w_{\alpha}^*$	$w_{\alpha}^* = 3, w^- = 3, w^- < w_{\alpha}^*$
Cropping (Table 23)	Can not reject H_0 , with $\alpha = 0.018$	Can not reject H_0 , with $\alpha = 0.018$	Reject H_0 , with $\alpha = 0.018$
	$w_{\alpha}^* = 3, w^- = 28, w^- > w_{\alpha}^*$	$w_{\alpha}^* = 3, w^- = 28, w^- > w_{\alpha}^*$	$w_{\alpha}^* = 3, w^- = 0, w^- < w_{\alpha}^*$
Scaling (Table 24)	Reject H_0 , with $\alpha = 0.018$	Reject H_0 , with $\alpha = 0.018$	Reject H_0 , with $\alpha = 0.063$
	$w_{\alpha}^* = 3, w^- = 0, w^- < w_{\alpha}^*$	$w_{\alpha}^* = 3, w^- = 0, w^- < w_{\alpha}^*$	$w_{\alpha}^* = 3, w^- = 3, w^- < w_{\alpha}^*$
Translation (Table 25)	Reject H_0 , with $\alpha = 0.018$	Reject H_0 , with $\alpha = 0.018$	Reject H_0 , with $\alpha = 0.018$
	$w_{\alpha}^* = 3, w^- = 0, w^- < w_{\alpha}^*$	$w_{\alpha}^* = 3, w^- = 0, w^- < w_{\alpha}^*$	$w_{\alpha}^* = 3, w^- = 0, w^- < w_{\alpha}^*$
Rotation (Table 26)	Reject H_0 , with $\alpha = 0.018$	Reject H_0 , with $\alpha = 0.018$	Reject H_0 , with $\alpha = 0.018$
	$w_{\alpha}^* = 3, w^- = 0, w^- \le w_{\alpha}^*$	$w_{\alpha}^* = 3, w^- = 0, w^- \le w_{\alpha}^*$	$w_{\alpha}^* = 3, w^- = 0, w^- \le w_{\alpha}^*$

value is smaller than or equal to the critical value for the Wilcoxon signed rank test (i.e., $w^- \le w_{\alpha}^*$), the proposed scheme is more robust than the each method in [38], [40], [42]. Otherwise, the proposed scheme can not be obviously recognized as the better one [65].

The results of this statistical analysis is shown in Table 29. As can be seen from Table 29, the proposed scheme generally outperforms the each method in [38], [40], [42] except Median filtering and Cropping attacks. For Median filtering, the proposed scheme is better than the each method in [38], [40], [42] when the window sizes are 3×3 , 4×4 , 5×5 , 6×6 and 7×7 . But the nice average NC values are not obtained when the window sizes are 9×9 , 11×11 due to the three images, including Elain, Goldhill, and Bridge. Moreover, the each method in [38], [40] is more superior than the proposed scheme against Cropping attacks, but the superiority is not very significant. Finally, it is not difficult to find that the proposed scheme is more robust than the methods in [38], [40], [42] based on the Tables 20 to 29.

E. SECURITY ANALYSIS

The security of a watermarking scheme mainly depends on the encryption algorithms used in the watermarking scheme. In this paper, the secret keys from Arnold transform and the two random sequences produced by VPCM system together ensure the high security of the proposed scheme. Even though the algorithm of zero-watermark generation is open, the right zero-watermark image will not be extracted in the process of watermark detection if any one of the secret keys is incorrect. Due to the limited length of this paper, we only analyse how the secret key μ_1 affects the security of the proposed scheme in this subsection. In the previous experiments, we know that the correct μ_1 is 3.89999. To test the security of the scheme, we design the experiments as follows. Assuming that all the secret keys in the process of watermark extraction are correct except μ_1 , which is variable, we varied μ_1 from

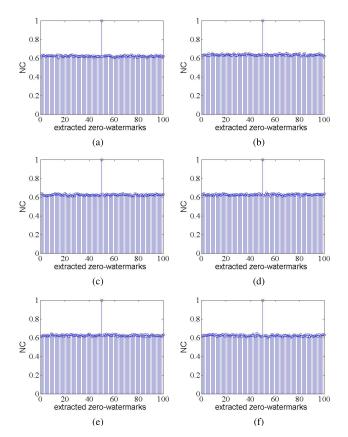


FIGURE 17. Security test of the proposed scheme for different images:
(a) Man, (b) Tiffany, (c) Elain, (d) Lena, (e) Goldhill, (f) Boat.

3.89950 to 3.90049 with 0.00001 steps to extract 100 zero-watermarks. The 100 NC values were respectively calculated between the 100 extracted zero-watermarks and the original zero-watermark generated with the correct μ_1 for different images. The experimental results are shown in Fig. 17. Fig. 17 shows that the NC value is 1 when μ_1 is correct. However, the NC value is just about 0.5 when μ_1 is incorrect, which



TABLE 30. Average computation time of the proposed scheme for all the test images.

	Zero-		Zero-watermark extraction under rotation attacks				
	watermar generatio		5°	10°	40°	90°	
Time (s)	1.3514	1.2500	1.3260	1.2636	1.3026	1.2792	

means that the watermark is extracted unsuccessfully. It is important to note that finding out the correct μ_1 randomly is very difficult. Therefore, all the secret keys perfectly ensure the security of the proposed scheme, and it is impossible to extract the correct zero-watermark without all the correct secret keys.

F. COMPUTATION TIME

The average computation time of the zero-watermark generation and extraction for the eight test images mentioned in Fig.7 are shown in Table 30. The computer used for our experiments had a 3.20 GHz Processor, 4-GB RAM, and a Microsoft Windows 7 operating system with 32 bits. The experiments were completed in the environment of MATLAB 2014. Table 30 illustrates that the computation time of the zero-watermark generation and extraction in the proposed scheme are acceptable.

V. CONCLUSION

In the proposed scheme for the copyright protection of digital images, NSPD and DCT were used to extract the robust feature of a host image as the original zero-watermark. Several experiments were performed to demonstrate that the signs of some AC coefficients of an image in the NSPD-DCT domain almost do not change under various attacks. To enhance the security of the proposed scheme, we combined PWLCM with LM to generate the VPCM system used for the watermark encryption and the robust feature vector extraction. Furthermore, an image rotation correction procedure was used before zero-watermark detection to improve the robustness of the scheme against rotation attacks. The experimental results have demonstrated that the NSPD-DCT based zerowatermarking scheme was highly robust to common image processing operations, several geometric attacks and some Checkmark attacks, and it had better performance than some existing algorithms. In the future, we will further improve the robustness of the proposed zero-watermarking scheme against combined attacks and extend this scheme to video watermarking.

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RUI WANG received the B.S. degree in applied mathematics from Tianjin University, in 2006, and the D.S. degree in applied mathematics from Nankai University, in 2011. She is currently a Lecturer with the College of Science, Civil Aviation University of China, Tianjin, China. Her research interests include image processing, information security, and coding theory.



HAN SHAOCHENG received the B.S. degree in information and communication engineering from the North University of China, in 2004, and the M.S. degree in signal and information processing from the Civil Aviation University of China, Tianjin, China, in 2009. He is currently an Associate Professor with the Basic Experimental Center, Civil Aviation University of China. His research interests include digital watermarking and information hiding.

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PENG ZHANG received the B.S. degree in electronic information science and technology from the Zhengzhou University of Light Industry, Henan, China, in 2018. He is currently pursuing the master's degree with the College of Electronic Information and Automation, Civil Aviation University of China, Tianjin. His research interests include image processing and information hiding.



ZHENG CHENG received the B.S. degree in electronic and communication engineering from the Civil Aviation University of China, Tianjin, China, in 2014. He is currently an Assistant Experimentalist with the Basic Experimental Center, Civil Aviation University of China. His research interests include SAR image processing and machine learning.



MENG YUE received the Ph.D. degree in information and communication engineering from Tianjin University, China, in 2017. He is currently a Lecturer with the School of Electronics, Information Engineering and Automation, Civil Aviation University of China. His current research interests include information security and cloud computing.



YUJIN ZHANG (Member, IEEE) received the Ph.D. degree in communication and information system from Shanghai Jiao Tong University, Shanghai, China, in 2014. Since 2015, he has been with the School of Electronic and Electrical Engineering, Shanghai University of Engineering Science. His research interests include multimedia forensics, signal processing, artificial intelligence, and pattern recognition.

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