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Design of a 7-Way Microstrip Divider for a Hexagonal Honeycomb Structure

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ABSTRACT This paper proposes a 7-way microstrip divider for hexagonal honeycomb structures. The honeycomb arrangement has advantages such as equidistant adjacent output ports and high space utilization. The structure comprises six output ports arranged hexagonally and one output port placed at the center of the hexagon in the same plane. To design such a divider considering the output ports' positions, this paper proposes the combination of a microstrip 6:1 unequal Wilkinson divider and a 6-way microstrip divider. To facilitate the implementation of the 6:1 unequal divider, including a transmission line with a high characteristic impedance, a microstrip coupler is used, and for the 6-way microstrip divider, a design scheme and analysis considering the impedance matching and isolation of the output ports are presented. Moreover, the ground layers of the two microstrip dividers are constructed in a back-to-back structure to minimize the size of the overall divider. For validation, a 5.8 GHz 7-way divider is designed, implemented, and measured. The measured S-parameters show that the proposed 7-way divider has appropriate return loss, insertion loss, isolation, and power distribution with a phase difference under 4.7◦ .

INDEX TERMS Microwave circuit, power divider, microstrip, 7-way divider, hexagonal honeycomb.

I. INTRODUCTION

Advanced microwave technologies, such as a phased array antenna are being employed not only in military radars but also in most wireless systems (communications [1], [2], wireless power charging [3]). A phased array antenna, depending on the arrangement of the elements, has different synthesized beam properties, and consequently, respective advantages and disadvantages [4]. Among the various arrangements, the hexagonal lattice arrangement has excellent advantages, such as optimum structural space utilization and few grating lobes, because all the adjacent antenna elements can be placed equidistantly [4]. To implement such an array structure, it is important to divide the microwave signal into *n*-ways by appropriately considering the location of the output ports.

Various studies have been conducted on *n*-way dividers [5]–[11]. An *n*-way divider can be implemented in two representative forms: a tree structure in which a reference signal is divided gradually through consecutive trees [5], [6]

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or, a scattering structure in which a reference signal is directly divided into *n*-ways [7], [8]. A tree structure divider requires a relatively large amount of space because it contains consecutive dividers connected up to *n*-way, while a scattering structure divider cannot easily accommodate one output port at the center of other output ports. Due to these issues, designers find it difficult to implement a space-efficient divider with a single scheme. To overcome these difficulties, we propose a novel method to design a 7-way divider that helps facilitate applications involving hexagonal honeycomb structures.

In the proposed design, a 6:1 unequal divider is combined with a 6-way scattering structure divider in the form of a consecutive tree [12] and a back-to-back microstrip structure for miniaturization [13]. However, a problem with the 6:1 unequal divider design is that one of the impedance transforming transmission lines (ITTLs) theoretically requires a considerably high characteristic impedance value. Moreover, even if an ITTL with a high characteristic impedance can be fabricated using an ordinary method, its electrical properties will not match the mathematically calculated values [14]. Various alternatives have been proposed, such as using a

defected ground structure (DGS) [15], [16] or a co-planar waveguide with an electronic bandgap (EBG CPW) [17], [18]. However, these have several drawbacks, such as requiring processes on the ground layer and a sufficient air gap (distance) from other conductors. To overcome these problems, the unequal divider requires other methods for implementing the space-efficient back-to-back structure. Furthermore, as previously reported dividers with scattering structures [7], [8] are also inappropriate for a planar back-to-back structure considering the arrangement of the resistors in [7] or the waveguide structure in [8], a new design method is desired for the scattering structure divider as well. We propose a novel design method for each divider. First, a microstrip unequal divider with a loosely coupled microstrip line coupler is proposed to avoid the problem of high characteristic impedance. We provide a mathematically analyzed design solution that uses ring-arrangement resistors for isolation and impedance matching for the 6-way microstrip scattering structure divider. Consequently, the two proposed dividers can be combined into a 7-way divider in a back-to-back structure. As a result, the proposed 7-way divider can be used for applications involving hexagonal honeycomb structures.

The rest of this paper is organized as follows. Section II presents the designs and analyses of the 6:1 uneven Wilkinson divider, 6-way scattering structure divider, and 7-way divider which is a combination of the two dividers. Section III discusses the implementation of the proposed divider and its performance with simulated and measured results. Finally, Section IV presents the conclusions of this study.

II. DESIGN OF THE 7-WAY DIVIDER

Fig. [1](#page-1-0) shows an example of a system with a hexagonal honeycomb structure. In this system, the seven antennae and the active microwave module are arranged equidistantly in the form of a hexagonal honeycomb.

To implement such a system, a 7-way divider is necessary. In this section, the design and analysis of the proposed 7-way divider is described. Before describing the detailed process, a brief guideline of the design process is given as follows.

- 1) Design and analyze the 6:1 unequal Wilkinson divider to divide the input power with a 6:1 ratio
- 2) Design and analyze a high impedance ITTL in the divider using a microstrip line coupler

FIGURE 1. Hexagonal honeycomb array antenna module.

- 3) Design and analyze a ring-type 6-way scattering structure divider
- 4) Determine the resistance between the output ports of the 6-way divider considering the output impedance and isolation
- 5) Combine the unequal Wilkinson divider and the 6-way scattering structure divider in back-to-back structure
- 6) Adjust the parameters and analyze the frequency responses of the divider by the performing a full-wave simulation

Steps 1 & 2 are described in section II-A, steps 3 & 4 in section II-B, step 5 in section II-C, and step 6 in Section III.

A. 6:1 UNEQUAL WILKINSON POWER DIVIDER

Fig. [2](#page-1-1) depicts a schematic of the *N*:1 unequal Wilkinson divider comprising several quarter-wavelength ITTLs. The power ratio (*K*) follows $\sqrt{P_B/P_A}$, where P_A and P_B are respectively the output power at Ports *A* and *B*, and its design values are obtained using the following equations [12]. In this section, analyses are made on the target frequency (f_0) , and the frequency responses of the designed divider are investigated through a full-wave simulation described in the next section.

$$
Z_1 = Z_0 \sqrt{K(1 + K^2)}
$$
 (1a)

$$
Z_2 = Z_0 \sqrt{\frac{1 + K^2}{K^3}}
$$
 (1b)

$$
Z_3 = \sqrt{Z_0^2 K} \tag{1c}
$$

$$
Z_4 = \sqrt{Z_0^2/K} \tag{1d}
$$

$$
R_x = Z_0(K + \frac{1}{K})
$$
 (1e)

The variables used in (1) are described in Fig. 2. Z_n ($n =$ 1, 2, 3, 4) is the characteristic impedance of the transmission line, and θ_n ($n = 1, 2, 3, 4$) is the electrical length of the transmission line for the given frequency. When the in/output port impedance is set to Z_0 , every characteristic impedance of the ITTL needs to be set based on the results of [\(1\)](#page-1-2). If the of the ITTL needs to be set based on the results of (1). If the output power ratio (K) is set to $\sqrt{6}$, Z_1 must be approximately 4.14*Z*0; therefore, a loosely coupled microstrip line coupler, which is available on a uni-surface, is adopted to replace *Z*1. Fig. 3(a) depicts such a microstrip coupler [19], comprising two ports with two other diagonal ports being shorted. *Y* in (2)

FIGURE 2. Schematic of N:1 unequal Wilkinson power divider.

FIGURE 3. (a) Microstrip coupler with two diagonal two ports shorted and (b) Equivalent circuit of Fig. 3(a), and (c) Input impedance of the circuit depicted in Fig. 3(b) terminated with $\boldsymbol{Z_{0}}.$

is the admittance matrix of the coupler depicted in Fig. 3(a).

$$
[Y] = -jY_{0e}\cot\theta_c \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}
$$

+ $j\frac{Y_{0o} - Y_{0e}}{2} \begin{bmatrix} -\cot(\pi + \theta_c) & \csc(\pi + \theta_c) \\ \csc(\pi + \theta_c) & -\cot(\pi + \theta_c) \end{bmatrix}$ (2)

Combining (2) and the structure shown in Fig. 3(a) results in a model equivalent to a double stub, as depicted in Fig. 3(b) [20]. Z_{0e} and Z_{0o} are the even- and odd mode impedances of the transmission line coupler, and Y_{0e} and Y_{0o} are their inverses, respectively. The first term in [\(2\)](#page-2-0) is identical to the two short stubs with a characteristic impedance of Z_{0e} and the second term with a $(\pi + \theta_c)$ length of transmission line with characteristic impedance $Z_c = [(Y_{0o} - Y_{0e})/2]^{-1}$. The conventional even- and odd-mode impedances using a coupling coefficient (C) gives the equation for Z_c [21].

$$
Z_{0e} = Z_0 \sqrt{\frac{1+C}{1-C}}
$$
 (3a)

$$
Z_{0o} = Z_0 \sqrt{\frac{1 - C}{1 + C}}
$$
 (3b)

$$
Z_c = (\frac{Y_{0o} - Y_{0e}}{2})^{-1} = Z_0 \sqrt{\frac{1}{C^2 - 1}}
$$
 (3c)

Given that one of the ports in Fig. $3(b)$ is terminated with Z_0 , as depicted in Fig. 3(c), an equation for the input impedance (*Zin*1) is obtained below.

$$
Z_{in1} = [-jY_{0e}cot\theta_c
$$

+
$$
Y_c \frac{-jY_{0e}cot\theta_c + Y_0 + jY_c tan\theta_c}{Y_c + j(-jY_{0e}cot\theta_c + Y_0)tan\theta_c}]^{-1}
$$
 (4)

Here, Y_c is Z_c^{-1} and Y_0 is Z_0^{-1} . For $\theta_c = \pi/2$, [\(4\)](#page-2-1) can be simplified as follows.

$$
Z_{in1} = \frac{Z_c^2}{Z_0}
$$
 (5)

Here, [\(5\)](#page-2-2) indicates that the input impedance (Z_{in1}) is equivalent to a $3\pi/2$ ITTL with a characteristic impedance of Z_c theoretically. Therefore, it implies that the characteristic impedance of Z_1 can be replaced with Z_c by adjusting the transmission line coupler, whose parameters are Z_{0e} and Z_{0o} . Once the issue of the characteristic impedance of Z_1 is solved, the other characteristic impedance values from [\(1\)](#page-1-2) are easily

available. However, as depicted in Fig. 3, as the $\pi/2$ length of the transmission line coupler is consistent with $3\pi/2$ length of the transmission line with a characteristic impedance of *Z^c* (Z_1) , the length of the transmission line with Z_2 should also be matched for the same phase delay.

B. PROPOSED 6-WAY MICROSTRIP SCATTERING STRUCTURE DIVIDER

When an *n*-way scattering structure divider is fabricated with a junction resistor node [7] or by using a waveguide format [8], the design provides good output port impedance and isolation between all the output ports. However, this is not implementable with an ordinary planar microstrip line. Therefore, we propose a planar ring resistor arrangement for output impedance matching and isolation as depicted in Fig. [4.](#page-2-3)

The arrangement in Fig. [4](#page-2-3) consists of several ITTLs whose characteristic impedance is Z_{α} or Z_{β} . The Z_{β} value and length are important to apply the resistors (R_v) without any impedance distortion. However, the length of the line with Z_β is assumed to be 0 to obtain an adequate R_ν value first. Every port in Fig. [4](#page-2-3) other than Port 2 is terminated with *Z*0, and an arbitrary source (V_s) is applied to Port 2, as depicted in Fig. [5.](#page-2-4)

The characteristic impedance Z_{α} is $\sqrt{6Z_0^2}$ [12], and by applying a transmission line equation when the physical length of every transmission line of Z_α is set to $\lambda/4$, we can obtain the correlations between the node voltages

FIGURE 4. Schematic of a 6-way microstrip scattering structure divider.

FIGURE 5. Microstrip scattering structure divider with Z_0 termination.

 V_n ($n = 2, 3, \ldots, 7$) and center node voltage V_B as follows:

$$
V(z) = (V_{\alpha}^+ + V_{\alpha}^-)\cos kz + j(V_{\alpha}^+ - V_{\alpha}^-)\sin kz
$$
 (6a)

$$
V(0) = (V_{\alpha}^{+} + V_{\alpha}^{-}) = V_{B}
$$
 (6b)

$$
V(-\lambda/4) = j(V_{\alpha}^{+} - V_{\alpha}^{-}) = V_{n}
$$
 (6c)

In (6), V_{α}^{+} and V_{α}^{-} are the wave voltages in the ITTL whose characteristic impedance is Z_{α} , and *k* is the wave-number which is $2\pi/\lambda$ under lossless conditions. Additional simultaneous equations can be obtained as follows:

$$
I_{nB}(z) = \frac{j}{Z_{\alpha}}(V_{\alpha}^{+} - V_{\alpha}^{-})\cos kz + \frac{j}{Z_{\alpha}}(V_{\alpha}^{+} + V_{\alpha}^{-})\sin kz
$$
 (7a)

$$
I_{nB}(0) = \frac{j}{Z_{\alpha}}(V_{\alpha}^{+} - V_{\alpha}^{-}) = \frac{jV_{n}}{Z_{\alpha}}
$$
 (7b)

$$
I_{nB}(-\lambda/4) = \frac{j}{Z_{\alpha}}(V_{\alpha}^{+} + V_{\alpha}^{-}) = \frac{jV_B}{Z_{\alpha}}
$$
(7c)

The current flowing from node $\#n$ to $\#B$, I_{nB} , and that in the opposite direction, *IBn*, can also be obtained in (7). A matrixvector equation between the node voltages and source voltage can be obtained in the form of (8), as shown at the bottom of the next page, using the Kirchhoff current law (KCL). The input impedance $(Z_{in2}$ shown in Fig. 5) is the ratio of the voltage at node #2 to the current I_s generated from V_s , and the isolation becomes perfect when the magnitude of the applied voltage at every node except #2 and #*B* becomes zero. *Zin*² and isolation are simultaneous dependent variables of the resistance *Ry*, as depicted in Figs. [6](#page-3-0) and [7](#page-3-1) respectively.

FIGURE 6. V_2 , I_s and Z_{in2} vs R_y .

Fig. [6](#page-3-0) shows that Z_{in2} is closest to Z_0 when R_y is approximately 2.08*Z*₀. Fig. [7](#page-3-1) shows that there is no specific resistance value that makes the voltage applied to every node except #2 and #*B* be zero. Thus, R_y is selected as 2.08 Z_0 such that every node voltage except V_2 and V_B are close to zero on average

FIGURE 7. Voltage magnitude at node #n (V_n) vs R_V .

and highly satisfies the output impedance matching, which affects the stability of the circuit.

As mentioned previously, additional transmission lines (Z_β, θ_β) should be considered to connect the resistor (R_v) , because its arbitrary value causes severe in/out impedance distortion owing to the extremely short wavelength of approximately a few centimeters. Fig. [8](#page-3-2) depicts the in/output port reflection with Z_β and θ_β .

FIGURE 8. In (S_{BB})/output (S_{nn}) port reflection for Z_β and θ_β variation $(n = 2, 3, \ldots, 7).$

As depicted in Fig. [8,](#page-3-2) when θ_{β} is $\pi/2$, it results in the worst reflection at the input (S_{BB}) and output (S_{nn}) ports $(n = 2, 3, \ldots, 7)$, whereas when it is 0 or π , it results in the best reflection. Furthermore, the best overall reflection is when the characteristic impedance of Z_β is approximately 1.8 Z_0 . Moreover, because, the length θ_β is not available with zero, the θ_{β} should be π .

C. PROPOSED 7-WAY DIVIDER

The next step is to design a 7-way divider by combining the two dividers designed in the previous Section II-A and B. Fig. 9 depicts a schematic of the proposed 7-way divider.

FIGURE 9. Schematic of proposed 7-way divider.

As shown in Fig. 9, the output port A of the unequal Wilkinson divider is connected to Port A' which supplies the smaller portion of the divided power to Port 8, and the output port B to Port B' directly supplies the larger portion to the scattering structure divider. The length of the transmission lines with Z_0 impedance in Fig. 9 can be adjusted considering the phase of the output signal and the size of the divider. From the previous subsections A and B, the parameters of the transmission line (Z_n, θ_n) and resistors (R_x, R_y) used in each divider can be acquired, and summarized in Table 1.

In the next section, we describe the implementation of the proposed 7-way divider and its performance. Unlike other *n*-way dividers [7], [8], [15]–[18], the two designed microstrip dividers contain an intact ground surface and have an appropriate shape to realize the back-to-back combination. To minimize the size of the 7-way divider, two dividers are constructed in a back-to-back structure.

III. FABRICATIONS AND VERIFICATION

Based on the theoretical values obtained in the previous section, the two dividers are fabricated and combined in this section. The network impedance (Z_0) is set to 50 Ω , and the target frequency is set to 5.8 GHz. Arlon TC-350 ($\epsilon_r = 3.5$, 20 mil, 1 oz) is used as a microstrip line substrate.

To implement the 7-way divider with a honeycomb structure, the seven output ports need to be placed at the center and six vertices of the hexagon. Thus, one output port is added at the center of the 6-way scattering structure divider as shown in Fig. 10, and it is connected to the output port A of the unequal Wilkinson divider by a ground etched via hole method which minimizes impedance distortions [22].

FIGURE 10. Fabricated 7-way divider and output port arrangement. (d is the diameter of the ring).

The additional output port 8 is at the center of the ring; thus, the input port of the 6-way scattering structure divider (Port B') is located slightly off-center and is also connected using the ground etched via hole method [22]. Considering the size of the divider and location of the output ports in this example, the electrical length (θ_{α}) of the Z_{α} transmission line is adjusted to $3\pi/2$ ($\theta_{\alpha} = \pi + \pi/2$) and the Z_{α} , Z_{β} transmission lines were implemented in a bent form, as shown in Fig. 10.

To verify the performance of the seven outputs, shown in Fig. 10, we conduct a full-wave simulation using an EM simulator (AWR Axiem from Cadence). Fig. 11(a) and (b) show the layout for EM simulation and frequency response. The circuit shown in Fig. 10 has two inputs, one of which is the input of the scattering structure divider (Port B) and the other is the input (Port A) via through from an output of the unequal Wilkinson divider. Fig. 11(b) shows the measured frequency response of $|S_{nB'}|$ $(n = 2, 3, \ldots, 7)$ for the fabricated 6-way divider and the center via through, $|S_{8A'}|$. A vector network analyzer P5007A (Agilent) is used for measurement. The simulation results using Fig. 11(a) are largely in agreement with the measured

FIGURE 11. (a) Layout for EM-simulation and (b) Measured frequency response of two types paths.

FIGURE 12. Parameters of the microstrip coupler for Z_1 .

results; therefore, only the measured results are presented. Because all the seven output ports of the proposed divider need to supply equally distributed power from the source, the frequency response, shown in Fig. 11(b) must be reflected in the design of the uneven Wilkinson divider. As depicted in Fig. 11(b), the measured frequency response of $|S_{nB'}|$ includes an additional insertion loss of approximately 0.8 dB in comparison with the theoretical 6-way divider (7.78 dB), and the center via through frequency response of $(|S_{8A'}|)$ has an insertion loss of approximately 0.3 dB. Thus, the ratio of the unequal divider is adjusted to 6.8:1 for equal power distribution. When the characteristic impedance is calculated with a power ratio of 6.8:1 using [\(1\)](#page-1-2), the highest characteristic value Z_1 is approximately 225.5 Ω . It is replaced with Z_{0e} = 62.33 Ω and $Z_{00} = 40.11 \Omega$ using [\(3\)](#page-2-5). A microstrip coupler that satisfies these conditions is determined using the AWR Axiem; Fig. [12](#page-5-0) depicts the coupler line converted from a high impedance line and its physical values.

The extracted characteristic impedances of the remaining microstrip lines for the unequal Wilkinson divider are Z_2 = 33.16 Ω , Z_3 = 80.74 Ω , and Z_4 = 30.96 Ω respectively. A microstrip line with these impedances can be easily implemented with the conventional method. Fig. 13 shows the fabricated unequal Wilkinson divider and its parameters.

The proposed 7-way divider is fabricated by connecting the two implemented dividers back-to-back; Fig. 14 depicts the fabricated 7-way honeycomb structure divider and its test environment.

Fig. 15 depicts the measured results of the frequency response; the order of the port numbers is the same as that depicted in Fig. 9. To verify the key indicators of the divider,

0.0.0.0.0 O Port B' 			
\circ Z_{4}	Param.	Width	Length
Z_{0} \bullet Port B \sim Port A' Z_2 , $3\pi/2$ \bullet Port A	Z_1, θ_1	Presented in Fig. 12	
	Z_2, θ_2	1.92 mm	7.61 mm
Z_3	Z_3, θ_3	0.46 mm	8.11 mm
Z_{1} (Microstrip Coupler)	Z_4, θ_4	2.13 mm	7.57 mm
000			

FIGURE 13. Fabricated 6:1 unequal divider using microstrip coupler.

FIGURE 14. Fabricated 7-way microstrip divider under test.

such as the insertion loss, phase delay, reflection, and isolation, the measurements are compared with the full-wave simulation using AWR Axiem. First, to validate the insertion loss and phase of each output port, the magnitude, and phase of S_{n1} $(n = 2, 3, ..., 8)$ are plotted in Figs. 15(a) and (b), respectively. To validate the reflection loss of the divider, S_{nn} ($n = 1, 2, \ldots, 8$) are plotted in Fig. 15(c), and finally, to check the isolation of the divider, that highly affects the stability of the circuit, we provide S_{2n} ($n = 3, 4, \ldots, 8$) in Fig. 15(d). Because the isolation between the other ports is measured similarly, only S_{2n} is presented in the figure. As a result, the four indicators of the proposed divider, namely the insertion loss, phase difference, reflection loss, and isolation, are 9.3 - 9.7 dB, under 4.7° , > 16 dB and > 18 dB at the target frequency of 5.8 GHz, respectively, The results are in good agreement with the simulation results.

Finally, the proposed divider is compared with several *n*-way dividers [6], [9]–[11] as listed in Table 2.

FIGURE 15. (a) Insertion loss, (b) Phase delay (c) Reflection and (d) Isolation between each port.

The comparison indicators include the number of ports, output port arrangement, substrate structure, operating frequency (BW) and insertion loss. To the best of our knowledge, the proposed divider is the only 7-way divider for the honeycomb structure, with an even power distribution and isolation value suitable for use as an *n*-way divider.

In this paper, a new 7-way RF divider for a hexagonal honeycomb structure is presented. The proposed divider comprises a 6:1 unequal Wilkinson divider and a 6-way scattering structure divider implemented in a back-to-back microstrip line structure with a common ground. A coupled line is used to replace the high impedance transmission line in the uneven Wilkinson divider, which is difficult to fabricate with the conventional microstrip line. To verify the proposed design, a divider was designed and implemented with a center frequency of 5.8 GHz. The simulated and measured results showed that the divider can distribute power to seven honeycomb output ports with equal power and a phase difference of less than 4.7◦ . The fabricated divider works properly, and the proposed design scheme is expected to be used in RF systems involving hexagonal honeycomb structures.

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