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# **Data-Driven Relay Selection for Physical-Layer Security: A Decision Tree Approach**

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**ABSTRACT** Conventional optimization-driven secure relay selection relies on maximization algorithm and accurate channel state information (CSI) of both legitimate and eavesdropper channels. Particularly, estimating and collecting accurate eavesdropper CSI is a difficult task. In this paper, we exploit the benefits of machine learning in solving secure relay selection problem from a data-driven perspective. We convert secure relay selection to a multiclass-classification problem and solve it by a decision-tree-based scheme, which is composed of three phases - preparing training data, building decision tree and predicting relay selection. To meet decision tree's requirement that input features must take discrete values, a feature extraction method is proposed to generate discrete input by quantizing the accurate CSI of legitimate and eavesdropper channels. By this means, the decision-tree-based relay selection only requires quantized CSI feedback which takes substantially fewer bits in predicting phase. For the purpose of optimizing quantization parameters and enhancing decision tree prediction, we further derive three splitting criteria, i.e. information gain, information gain ratio and Gini index. Simulation results show that if the quantization parameters are set properly, the proposed decision-tree-based scheme can achieve satisfactory performance in terms of average secrecy rate while reducing computational complexity and feedback amount.

**INDEX TERMS** Physical-layer security, relay selection, machine learning, decision tree, splitting criterion.

#### **I. INTRODUCTION**

Machine learning is an effective artificial intelligence technology which predicts the result of a task based on large amount of data. Machine learning has been widely investigated in the field of data mining, natural language processing, image processing, etc. Recently, research efforts have been devoted to using machine learning in next-generation wireless networks [1]–[9], covering channel estimation, information dissemination and network optimization. In [1], antenna selection of multiple-input-multiple-output (MIMO) systems, which is a conventional problem in wireless communications, was interpreted to multiclass-classification problem and solved by k-nearest neighbors (k-NN) and support vector machine (SVM) algorithms. More recently, authors in [2] considered antenna selection in wireless wiretap channels and proposed two machine-learning-based schemes: SVM-based scheme and naive-Bayes-based scheme.

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In recent years, physical-layer techniques for securing wireless transmissions against eavesdropping has been drawing great attention, including, resource allocation [10], [11], signal design [12], [13], etc. If active eavesdroppers exist [14], [15], more sophisticated techniques need to be designed. Relay technique, which has led to numerous theories and optimization methods, is also an effective tool enhancing physical-layer security. Relay selection for security was first investigated by Krikidis et al. in [16], which showed that relay selection tries to maximize the ratio of signal-to-noise ratio (SNR) of legitimate channel to SNR of eavesdropper channel. Then, researches on various relay protocols and selection requirements emerged [17]-[21]. Existing relay selection policies for physical-layer security all belong to optimization-driven schemes which strongly rely on maximization (or minimization) algorithms and accurate channel state information (CSI) feedback. Therefore, the cost of optimization computation and resource consumption of accurate CSI feedback cannot be neglected. Particularly, it is often difficult to acquire the accurate CSI of eavesdroppers,

so that designing efficient feedback strategy is also of importance [22], [23]. As long as optimization-driven selection schemes are adopted, these weak points cannot be overcome. This evokes our attempt to exploit brand new relay selection methods beyond conventional optimization theories.

Inspired by recent developments of machine learning and the bottleneck of conventional optimization-driven algorithms, we reconsider relay selection problem from datadriven perspective and propose a machine-learning-based relay selection scheme. Among the learning algorithms, decision tree has advantages of low computational complexity, discrete input and one-time initialization. [4] was our first attempt to solve relay selection by a supervised learning algorithm - decision tree learning. Massive samples of relay CSI were collected to generate training data, based on which a decision tree was constructed. The decision tree was then used to predict the best relay. The computation cost and communication overhead of the decision-treebased scheme are remarkably reduced while communication performance is comparable to the optimal selection policy.

In this paper, we design a decision-tree-based relay selection scheme for physical-layer security in dualhop wireless networks. To predict selection results with a decision tree, we first model relay selection as a multiclass-classification problem, where each class label represents the index of a candidate relay and the output label represents the index of the selected relay. Different from conventional optimizationdriven selection schemes which calculate maximization (or minimization) problems with accurate instantaneous CSI, data-driven selection scheme constructs a decision tree with large amount of sample data. The proposed scheme is composed of three phases - preparing training data, building decision tree and predicting relay selection. Decision tree requires the input features to be finite discrete values, so we design an extraction method which generates discrete features by quantizing continuous CSI of legitimate and eavesdropper channels. Using this quantization method, training data is generated from a large number of CSI samples. For each dualhop transmission, the scheme only requires quantized CSI feedback to predict selection results. To achieve high spectrum efficiency, quantization parameters should be set judiciously. Because splitting criteria play a key role in building an efficient decision tree, we derive splitting criteria of the input features and examine the quantization parameters maximizing the splitting criteria. The proposed decision-tree-based secure relay selection also has advantages in computation cost, communication overhead and feedback CSI requirement. Compared with our preliminary work in [4], this work is different in the following aspects.

(1) *Feature generating method*: In [4], a binary quantization method was proposed to generate one-bit features. In this paper, we propose a multi-level quantization method which divides the CSI region into multiple segments and generates a feature set with multiple discrete values.

- (2) Derivation of splitting criteria: As a result of the multilevel quantization method, the derivation of splitting criteria should cover all possible values of input features. Moreover, features representing legitimate CSI and eavesdropper CSI lead to different calculations.
- (3) Parameter optimization: In [4], splitting criteria are determined by only one parameter, i.e. quantization threshold, and are concave functions of the threshold. In this paper, multi-level quantization needs two parameters to define the quantization. Thus, analyzing the optimal values of the two parameters is intriguing.

The rest of this paper is organized as follows. In Section II, system model is introduced and conventional optimizationdriven selection schemes are described. Section III elaborates the decision-tree-based relay selection algorithm. In Section IV, three splitting criteria of input features are derived. Simulation results are presented in Section V, followed by conclusions in Section VI.

# II. SYSTEM MODEL AND OPTIMIZATION-DRIVEN RELAY SELECTION

## A. SYSTEM MODEL

Consider a dualhop network with one source (S), one destination (D), K decode-and-forward (DF) relays and a passive eavesdropper (E). The transmission from S to D is completed in two time slots aided by one of the relays. We assume coverage extension scenario where D is beyond the transmission range of S. The eavesdropper is located near D and is also beyond the coverage of S.

The wireless channel between each pair of nodes is assumed to experience independent and identically distributed (i.i.d.) Rayleigh fading. Large-scale fading is not considered in the system model. Suppose that the fading environment is not changing over time and the CSI is correctly estimated. The noise at each receiver is modeled as complex Gaussian random variable with zero mean and variance  $\sigma^2$ . For convenience, the *K* relays are denoted by  $\mathcal{R} = \{r_k | k =$ 1, 2, ..., *K*}. Let  $h_{Sk}$  denote the complex channel coefficient from S to  $r_k$ , and let  $h_{kD}$  and  $h_{kE}$  denote coefficients from  $r_k$ to D and E. If  $r_k$  is selected, the secrecy rate of the dualhop transmission is [24]

$$R_k^S = \frac{1}{2} \left[ \min\{R_{Sk}, R_{kD}\} - R_{kE} \right]^+$$
  
=  $\frac{1}{2} \left[ \min\left\{ \log_2 \left( 1 + \frac{Pg_{Sk}}{\sigma^2} \right), \log_2 \left( 1 + \frac{Pg_{kD}}{\sigma^2} \right) \right\} - \log_2 \left( 1 + \frac{Pg_{kE}}{\sigma^2} \right) \right]^+, \qquad (1)$ 

where  $R_{Sk}$ ,  $R_{kD}$  and  $R_{kE}$  represent the information rates of  $r_k$ , D and E. Moreover,  $[x]^+ = \max\{x, 0\}$ ,  $g_{Sk} = |h_{Sk}|^2$ ,  $g_{kD} = |h_{kD}|^2$  and  $g_{kE} = |h_{kE}|^2$ . Thus,  $g_{Sk}$ ,  $g_{kD}$  and  $g_{kE}$  are exponential distributed random variables with parameter  $\lambda_D$  for legitimate channels and  $\lambda_E$  for eavesdropper channels. To improve the readability of this paper, nomenclature is listed in Table 1.

#### TABLE 1. Nomenclature.

$h_{ij}$	complex channel coefficient from $i$ to $j$					
$g_{ij}$	channel gain from $i$ to $j$					
$g_k$	equivalent channel gain via relay k					
$g^q_{ij}$	quantized channel coefficient from $i$ to $j$					
$R_{ij}$	rate from $i$ to $j$					
$R_k^S$	instantaneous secrecy rate via relay $k$					
$\overline{R_S}$	average secrecy rate of the dualhop transmission					
$\sigma^2$	noise power					
$F_k$	the kth input feature					
$x_m^k$	the $k$ th element of the $m$ th input sample					
$y_m$	output of the <i>m</i> th training sample					
$T_D, N_D$	quantization parameters of legitimate channel					
$T_E, N_E$	quantization parameters of eavesdropper channel					
$[g_D^l(n), g_D^u(n)]$	the nth segment of quantized legitimate channel					
$[g_E^l(n), g_E^u(n)]$	the $n$ th segment of quantized eavesdropper channel					

## **B. OPTIMAL SELECTION**

In conventional optimization-driven relay selection, a central controller collects  $g_{Sk}$ ,  $g_{kD}$  and  $g_{kE}$  of all relays, and selects the relay maximizing  $R_k^S$ . This problem is to find from the cluster the index of the relay which yields maximum secrecy rate, as expressed by

$$k^* = \arg \max_{1 \le k \le K} R_k^S$$
  
=  $\arg \max_{1 \le k \le K} \min\{R_{Sk} - R_{kE}, R_{kD} - R_{kE}\}$   
=  $\arg \max_{1 \le k \le K} \min\left\{\frac{\sigma^2 + Pg_{Sk}}{\sigma^2 + Pg_{kE}}, \frac{\sigma^2 + Pg_{kD}}{\sigma^2 + Pg_{kE}}\right\}.$  (2)

To evaluate the communication performance of different relay selection schemes, average secrecy rate is computed as performance metric, which is given by

$$\overline{R_S} = \lim_{T \to \infty} \frac{1}{T} \sum_{t=1}^T R_{k^*}^S(2t).$$
(3)

## C. SUBOPTIMAL SELECTION

Optimal selection scheme requires full CSI of both legitimate and eavesdropper channel from all hops. Suboptimal selection schemes only take into account the CSI of a particular group of channels, ignoring the other channels with the purpose of simplifying calculation or reducing cost. One way to design suboptimal selection schemes is to consider only legitimate channel or eavesdropper channel [18], [25]. Another way to design suboptimal selection is to consider only one hop of the dualhop transmission [26]. These types of suboptimal selections are often referred to as partial selection.

Here, we give the following two partial selection schemes: the scheme that only considers legitimate CSI (Partial-D) and the scheme that only considers eavesdropper CSI (Partial-E). Partial-D is described by

$$k^{*} = \arg \max_{1 \le k \le K} \frac{1}{2} \min\{R_{Sk}, R_{kD}\}$$
  
=  $\arg \max_{1 \le k \le K} \min\left\{1 + \frac{Pg_{Sk}}{\sigma^{2}}, 1 + \frac{Pg_{kD}}{\sigma^{2}}\right\}$   
=  $\arg \max_{1 \le k \le K} \min\{g_{Sk}, g_{kD}\},$  (4)

and Partial-E is described by

$$k^* = \arg \min_{1 \le k \le K} R_{kE}$$
  
=  $\arg \min_{1 \le k \le K} \frac{1}{2} \log_2 \left( 1 + \frac{Pg_{kE}}{\sigma^2} \right)$   
=  $\arg \min_{1 \le k \le K} g_{kE}.$  (5)

These two partial selection schemes are simpler to implement and cost fewer resources, but compromise communication performance compared with optimal selection. Partial-D and Partial-E are proposed as comparison to the decision-treebased selection.

#### D. MULTICLASS-CLASSIFICATION PROBLEM

In machine learning, classification is the problem of deciding which class a sample belongs to. If each sample is labeled with single class and the class set contains multiple labels, this problem becomes multiclass classification. Let  $\mathcal{X}$  denote the input space and all elements in  $\mathcal{X}$  are i.i.d. Let  $\mathcal{Y}$  denote the output space where the classes are marked with numbers. The learner receives a set of labeled samples  $S = ((x_1, y_1), \ldots, (x_m, y_m)) \in (\mathcal{X} \times \mathcal{Y})^m$ , and trains a classifier which defines the target labeling function  $f : \mathcal{X} \to \mathcal{Y}$ .

To be solved by machine learning methods, relay selection problem needs to be converted to multiclass classification problem. To be specific, elements of  $\mathcal{X}$  are drawn from  $g_{Sk}$ ,  $g_{kD}$  and  $g_{kE}$ . The classes are labeled by the indices of candidate relays, i.e.  $\mathcal{Y} = \{1, \ldots, K\}$ . A decision tree is trained to simulate the labeling function  $f : \mathcal{X} \to \mathcal{Y}$ .

## **III. DECISION-TREE-BASED RELAY SELECTION**

To solve the multiclass-classification problem converted from relay selection problem, we adopt decision tree learning and build a classification tree. The entire relay selection scheme is composed of three phases: preparing training data, building decision tree and predicting relay selection. The first two phases are regarded as initialization and conducted before S transmits the first bit. After tree building is completed, no update or modification is needed to the decision tree. At the beginning of each dualhop transmission, the central controller collects CSI from all relays and uses the stored decision tree to compute selection result. System model and the decision-tree-based scheme are briefly illustrated in Fig. 1. Next, we elaborate the details of the decision-treebased scheme.

#### A. PREPARING TRAINING DATA

Training data demanded by decision tree is generated from CSI of the legitimate and eavesdropper channel, i.e.  $g_{Sk}$ ,  $g_{kD}$  and  $g_{kE}$ , and is denoted by  $D = \{(\mathbf{x}_1, y_1), (\mathbf{x}_2, y_2), \dots, (\mathbf{x}_M, y_M)\}$ .  $(\mathbf{x}_m, y_m)$  is the *m*th sample consisting of input  $\mathbf{x}_m$  and output  $y_m$ . *M* should be sufficiently large in order to train an accurate tree.  $y_m$  represents the index of optimal relay and is calculated by the optimizationdriven relay selection algorithm specified in (2) using the *m*th



FIGURE 1. System model of the decision-tree-based secure relay selection.

CSI samples. Input data is the values of 2K features describing the quality of all legitimate and eavesdropper channels. The features are denoted by  $\mathcal{F} = [F_1, F_2, \dots, F_{2K}]$ .  $\mathbf{x}_m$  is the input vector containing 2K values, and is given by

$$\mathbf{x}_m = [x_m^1, x_m^2, \dots, x_m^{2K}],$$
(6)

where  $x_m^k$  is the value of the *k*th feature.

The procedure of training data preparing is completed in the following steps.

- 1.1 Sensing fading characteristics. calculating splitting criterion and set up new quantization parameters.
- 1.2 Estimate and feedback  $g_{Sk}$ ,  $g_{kD}$  and  $g_{kE}$  for all k to the central controller. Generate input features. Compute  $\mathbf{x}_m = [x_m^1, x_m^2, \dots, x_m^{2K}]$  from  $g_{Sk}, g_{kD}$  and  $g_{kE}$ .

The input features required by decision tree are discrete values describing the object to be classified. Therefore, we need to transform  $g_{Sk}$ ,  $g_{kD}$  and  $g_{kE}$  to a set of values which are taken from finite discrete domain and can well characterize the relays.  $x_m^1, x_m^2, \ldots, x_m^K$  are generated from  $g_k$  which is given by  $g_k = \min\{g_{Sk}, g_{kD}\}, 1 \le k \le K$ . The entire CSI region is divided into  $N_D + 1$  segments by  $S_1, S_2, \ldots, S_{N_D}, 0 < S_1 < S_2 < \ldots < S_{N_D}$ . To clearly show the relations between quantization parameters and prediction performance, we consider uniform quantization. We set an upperbound  $T_D$  for  $g_k$ , and then evenly divide the  $[0, T_D]$  into  $N_D$  + 1 segments, each of which is denoted by  $[g_D^l(n), g_D^u(n)]$  with

$$g_D^l(n) = \begin{cases} \frac{(n-1)T_D}{N_D}, & 1 \le n \le N_D\\ T_D, & n = N_D + 1 \end{cases}$$
(7)

and

$$g_D^u(n) = \begin{cases} \frac{nT_D}{N_D}, & 1 \le n \le N_D\\ \infty, & n = N_D + 1. \end{cases}$$
(8)

Then, the value of  $x_m^k$  is an integer that lies between 1 and  $N_D + 1$ . To be specific, for  $1 \le k \le K$ ,

$$x_m^k = \begin{cases} n, & g_D^l(n) < g_k < g_D^u(n) \\ N_D + 1, & g_k > g_D^l(N_D + 1). \end{cases}$$
(9)

 $x_m^{K+1}, \ldots, x_m^{2K}$  represent channel features of the eavesdropper and are generated from  $g_{kE}$  following the same procedure as the first K features. An upperbound  $T_E$  is set to  $g_{kE}$ and  $[0, T_E]$  is divided evenly into  $N_E$  segments. The entire CSI region is divided into  $N_E + 1$  segments, each of which is denoted by  $[g_E^l(n), g_E^u(n)]$  with

$$g_{E}^{l}(n) = \begin{cases} \frac{(n-1)T_{E}}{N_{E}}, & 1 \le n \le N_{E} \\ T_{E}, & n = N_{E} + 1 \end{cases}$$
(10)

and

$$g_E^u(n) = \begin{cases} \frac{nT_E}{N_E}, & 1 \le n \le N_E\\ \infty, & n = N_E + 1. \end{cases}$$
(11)

For  $K + 1 \le k \le 2K$ , the *k*th feature is calculated as

$$x_m^k = \begin{cases} n, & g_E^l(n) < g_{(k-K)E} < g_E^u(n) \\ N_E + 1, & g_{(k-K)E} > g_E^l(N_E + 1). \end{cases}$$
(12)

The insight of the feature extraction method is to quantize  $g_k$  and  $g_{kE}$ , and assign the quantization results to input features. Quantization parameters for legitimate channels and eavesdropper channels can be set independently by different parameters.

- 1.3 Central controller calculates (2) with  $g_{Sk}$ ,  $g_{kD}$  and  $g_{kE}$ , and form  $(\mathbf{x}_m, y_m)$ , assigns  $k^*$  to  $y_m$  and forms  $(\mathbf{x}_m, y_m)$ .
- 1.4 Repeat 1.1-1.3 for another M-1 times to form a training data set containing totally M samples.

Collecting and preparing M samples of training data are completed offline before the transmissions are started. Once the decision tree is built, no training data are required as long as the network topology keeps stable.

## **B. BUILDING DECISION TREE**

After training data is prepared, the decision tree is built by selecting the *best* feature and splitting the data set into subsets based on feature value test. This process is repeated on each subset until stopping criterion is satisfied. Indices of all candidate relays are represented by the leaf nodes. Before we describe the building procedure, it is necessary to introduce the terminology of decision tree.

- *Splitting criterion*: The metric of evaluating a feature is called splitting criterion. It measures the decreased impurity after the current data set is split by a feature. Information gain, information gain ratio and Gini index are commonly adopted splitting criteria.
- *Stopping criterion*: Stopping criterion is the condition under which the current data set cannot be further split and the building of the current branch should stop. It is often defined that the number of samples in current data set is smaller than a threshold, or splitting criterion of current feature is smaller than a threshold, or no feature is left to choose.
- *Multi-branch tree*: As observed from feature extraction method, each feature has more than two possible values if  $N_D, N_E \ge 2$ , which means that the decision tree is a multi-branch tree and each interior node is split

into multiple branches. Multi-branch tree can also be converted to binary tree.

The decision tree building of the proposed scheme directly adopts the most widely-accepted decision tree algorithms. The details depend on the selection of splitting criterion, the selection between binary tree and multi-branch tree, etc. ID3 [27] and C4.5 [28] are two well-known multi-branch decision tree algorithms. ID3 adopts information gain as splitting criterion while C4.5 adopts information gain ratio. CART (Classification And Regression Tree) [29] is another widely used decision tree algorithm. It adopts Gini index as splitting criterion and is designed by binary tree. Here, we only briefly describe the steps of building phase.

- 2.1 Input sample data, set up parameters and stopping criterion.
- 2.2 Build a decision tree with sample data. From the root node, each node represents a test to one of the features which is selected for having the best splitting criterion. Then, the current data set is split according to the value of this feature.
- 2.3 Split subset of each branch according to the best feature in the remaining feature set. Build the decision tree recursively until stopping criterion is satisfied.

It is worth mentioning that the decision tree is converged if one of the stopping criteria is satisfied. The training data is generated from perfect CSI of all legitimate and eavesdropper channels. Thus, the decision tree is regarded to converge to optimal point. We only need to build the decision tree in the initialization phase of the dualhop transmission. After tree construction is completed, it is used to predict the best relay in each transmission, and requires no renewal.

## C. PREDICTING RELAY SELECTION

In each prediction, input features are generated from instantaneous CSI of legitimate and eavesdropper channels. As shown in feature extraction method, the values in  $\mathbf{x}_m$  are assigned by the quantization results of  $g_{Sk}$ ,  $g_{kD}$  and  $g_{kE}$ . Therefore, the central controller only needs to estimate and collect the quantized CSI of legitimate and eavesdropper channels.

3.1 Collect quantized CSI from all legitimate and eavesdroppers channels, and generate  $\mathbf{x}_m$ .

Let  $g_{Sk}^q$ ,  $g_{kD}^q$  and  $g_{kE}^q$  denote the quantization results of  $g_{Sk}$ ,  $g_{kD}$  and  $g_{kE}$ , the first two of which are generated by the quantization method (9) and the third one is generated by (12). Thus,  $g_{Sk}^q$ ,  $g_{kD}^q \in [1, 2, ..., N_D + 1]$  and  $g_{kE}^q \in [1, 2, ..., N_E + 1]$ . Transmitting them requires  $\log_2(N_D + 1)$  bits and  $\log_2(N_E + 1)$  bits, respectively. At the beginning of each odd time slot,  $g_{Sk}^q$ ,  $g_{kD}^q$  and  $g_{kE}^q$  are collected by the central controller. Then,  $\mathbf{x}_m$  is generated by

$$x_m^k = \begin{cases} \min\{g_{Sk}^q, g_{kD}^q\}, & 1 \le k \le K \\ g_{(k-K)E}^q, & K+1 \le k \le 2K. \end{cases}$$
(13)

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In each dualhop transmission, the feedback amount is reduced compared with the optimal selection scheme. Accurate instantaneous eavesdropper CSI is no longer required.

After input data is generated, it is input into the root node and tested by the rule that the current node defines. A leaf nodes will be reached following each branch representing test result. Relay selection prediction is elaborated as follows.

- 3.2 Input  $\mathbf{x}_m$  into the decision tree, test feature values from root to leaf. From root node, we examine the feature of  $\mathbf{x}_m$  that current node is testing and follow the right branch to the next node until a leaf node is reached.
- 3.3 Assign the leaf label to  $k^*$ . The central controller broadcasts the selection result to all nodes. The selected relay is ready to work.

Before next prediction starts, the network first senses the fading environment. If fading characteristics have not changed, only Step 3, i.e. relay prediction, is repeated. Else, new data will be collected and a new tree will be built. All three steps will be repeated. The entire algorithm is summarized as follows.

## Algorithm 1 Decision-Tree-Based Relay Selection

Step 1. Prepare training data.

- 1.1. Sensing fading characteristics. Calculate splitting criterion and set up new quantization parameters.
- 1.2. Estimate and feedback  $g_{Sk}$ ,  $g_{kD}$  and  $g_{kE}$  for all k to the central controller. Compute  $\mathbf{x}_m = [x_m^1, x_m^2, \dots, x_m^{2K}]$  using (9) and (12).
- 1.3. Solve problem (2) using  $g_{Sk}$ ,  $g_{kD}$  and  $g_{kE}$ , calculate  $k^*$  and assign it to  $y_m$ . Form  $(\mathbf{x}_m, y_m)$ .
- 1.4. Repeat 1.1-1.3 for M 1 times. Form training data D.

Step 2. Build decision tree.

- 2.1. Input training sample, define stopping criterion and set up parameters.
- 2.2. From the root node, split data set according to the feature with best splitting criterion.
- 2.3. Split subset of each branch according the best feature in the remaining feature set. Build the decision tree recursively until stopping criterion is satisfied.

Step 3. Predict relay selection

- 3.1. Collect  $g_{Sk}^q$ ,  $g_{kD}^q$  and  $g_{kE}^q$  from all *K* relays, and generate  $\mathbf{x}_m$ .
- 3.2. Input  $\mathbf{x}_m$  into the decision tree and test feature values from root to leaf.
- 3.3. Assign the leaf label to  $k^*$ .

Sense fading characteristics.

if fading has not changed

repeat Step 3;

else

repeat Step 1-Step 3;

end if

## D. CLOUD-ASSISTED STRUCTURE

The decision-tree-based scheme requires large amount of training data, which is generated or collected in different ways. In the considered network, training data can be collected by CSI estimation and feedback. If fading environment is changing fast, training data collection and tree building are repeated frequently, which leads to high overhead and long delay. Therefore, we consider to adopt the cloud-assisted structure proposed by [30] to save transmission overhead. Huge amount of historical data is collected and stored in cloud servers. Based on the data from same fading environment, the cloud server computes a number of different decision trees and stores them in the cloud. When it is uneconomical or impossible to collect CSI by real measurement, the dualhop network only estimates the fading characteristics and asks the cloud for the decision tree that best fits the current fading. The best tree will be used to predict relay selection.

The cloud-assisted structure provides a new way of generating training data, especially when fading environment is changing frequently. To efficiently use this structure, there are still many open issues to be solved, such as which features to be collected, how to compare the fading features with stored learning models, how to store and transmit learning model appropriately, etc.

#### **IV. ANALYSIS OF SPLITTING CRITERIA**

The input features are generated from continuous CSI and determined by quantization parameters, i.e.  $T_D$ ,  $T_E$  and  $N_D$ ,  $N_E$ . These parameters also affect the features' splitting criteria, which play a key role in building decision tree and enhancing prediction accuracy. Wisely setting up these parameters can promote the performance of decision-tree-based relay selection. Moreover, investigating the relation between quantization parameters and communication performance can help revealing the laws of relay selection.

In this section, we derive three commonly used splitting criteria, namely information gain, information gain ratio and Gini index. These splitting criteria describe the impurity of a data split. Large information gain means that this feature splits the current data set more efficiently. Information gain favors features with a large number of distinct values. Then, information gain ratio is defined as the ratio of information gain to intrinsic entropy to solve the weakness of information gain. Gini index measures the probability that a sample is incorrectly classified and takes value from 0 to 1. In the literature, it is not obvious which of the splitting criteria will produce the optimal decision tree for a given data set. Among all existing splitting criteria, no one is consistently superior to the others. As a result, it is necessary to derive these splitting criteria and analyze their relations with quantization parameters.

The optimal selection policy specified in (2) provides little insight and has to be simplified in order to derive the expressions of splitting criteria. Thus, approximation to (2) is made as

$$k^* = \arg \max_{1 \le k \le K} R_k^S$$
  

$$\approx \arg \max_{1 \le k \le K} \min \left\{ \frac{g_{Sk}}{g_{kE}}, \frac{g_{kD}}{g_{kE}} \right\}$$
  

$$\approx \arg \max_{1 \le k \le K} \frac{\min \left\{ g_{Sk}, g_{kD} \right\}}{g_{kE}}.$$
 (14)

For the convenience of derivation, we let  $\gamma_k = \frac{\min\{g_{Sk}, g_{kD}\}}{g_{kE}}$ .

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## A. INFORMATION GAIN

Information gain, which is adopted by ID3 algorithm, represents the entropy change after data set is split by a feature. To build a more efficient decision tree, information gain of the features need to be maximized. The information gain of the *k*th feature  $F_k$  is given by

$$IG(D, F_k) = H(D) - H(D|F_k).$$
 (15)

Here, H(D) is the entropy of the classification and given by

$$H(D) = -\sum_{i=1}^{K} \Pr(y_m = i) \log_2 \Pr(y_m = i) = \log_2 K.$$
 (16)

 $H(D|F_k)$  is the average entropy after the split caused by  $F_k$ . In the remaining part, we focus on the derivation of  $H(D|F_k)$ .

Since all wireless links experience i.i.d. Rayleigh fading, the first K features representing legitimate channels share identical information gain, and the other K features representing eavesdropper channels also share identical information gain. This means that information gain of the first Kfeatures can be maximized simultaneously. This conclusion also applies to the other K features and to other two splitting criteria. Next, we derive the expressions of information gain for the two cases.

1)  $1 \le K \le K$ 

The first *K* features are extracted from  $g_k$ , and quantized by  $T_D$ ,  $N_D$ . The entropy after splitting is calculated as

$$H(D|F_k) = \sum_{n=1}^{N_D+1} \Pr(x_m^k = n) H_n(T_D, N_D)$$
  
= 
$$\sum_{n=1}^{N_D+1} \Pr\left(g_D^l(n) < g_k < g_D^u(n)\right) H_n(T_D, N_D), \quad (17)$$

where

 $H_n(T_D, N_D)$ 

$$= -\sum_{i=1}^{K} \Pr(y_m = i | x_m^k = n) \log_2 \Pr(y_m = i | x_m^k = n).$$
(18)

In order to facilitate the derivation of  $Pr(y_m = i | x_m^k = n)$ , let  $\gamma_M = \max_{i \neq k} \gamma_i$  and its probability density function (PDF) is

given by 
$$f_M(z) = \frac{(K-1)\lambda_E(2\lambda_D)^{K-1}z^{K-2}}{(\lambda_E+2\lambda_D z)^K}$$
. When  $i = k$ ,  

$$\Pr(y_m = i|x_m^k = n)$$

$$= \Pr\left(\frac{g_k}{g_{kE}} > \gamma_M |g_D^l(n) < g_k < g_D^u(n)\right)$$

$$= \int_0^\infty \int_{g_D^l(n)}^{g_D^u(n)} \int_0^{\frac{x}{z}} f_X(x) f_Y(y) f_M(z) dx dy dz$$

$$= \int_0^\infty f_M(z) \left( (e^{-2g_D^l(n)\lambda_D} - e^{-2g_D^u(n)\lambda_D}) - \frac{2\lambda_D z}{\lambda_E + 2\lambda_D z} \times (e^{-g_D^l(n)(\lambda_E + 2\lambda_D z)/z} - e^{-g_D^u(n)(\lambda_E + 2\lambda_D z)/z}) \right) dz = q(n).$$
(19)

When  $i \neq k$ ,

$$\Pr(y_m = i | x_m^k = n) = \Pr(\gamma_M = \gamma_i, \gamma_M > \gamma_k | x_m^k = n)$$
$$= \frac{1 - q(n)}{K - 1}.$$
(20)

Calculating the summation in (18), we obtain

$$H_n(T_D, N_D) = -q(n) \log_2 q(n) - (1 - q(n)) \log_2 \frac{1 - q(n)}{K - 1}.$$
(21)

Combining all probabilities derived above, we can obtain the expression of information gain for k = 1, ..., K.

2)  $K + 1 \le K \le 2K$  $x_m^{K+1}, \ldots, x_m^{2K}$  are extracted from  $g_{kE}$  and determined by  $T_E$ ,  $N_E$ . The entropy after splitting is calculated as

$$H(D|F_k) = \sum_{n=1}^{N_E+1} \Pr(x_m^k = n) H_n(T_E, N_E)$$
  
= 
$$\sum_{n=1}^{N_E+1} \Pr(g_E^l(n) < g_{(k-K)E} < g_E^u(n)) H_n(T_E, N_E), \quad (22)$$

where

$$H_{n}(T_{E}, N_{E}) = -\sum_{i=1}^{K} \Pr(y_{m} = i | x_{m}^{k} = n) \log_{2} \Pr(y_{m} = i | x_{m}^{k} = n).$$
(23)  
When  $i = k - K$ ,

$$\Pr(y_m = i | x_m^k = n)$$

$$= \Pr\left(\frac{g_{k-K}}{g_{(k-K)E}} > \gamma_M | g_E^l(n) < g_{kE} < g_E^u(n)\right)$$

$$= \int_0^\infty \int_{g_E^l(n)}^{g_E^u(n)} \int_{y_Z}^\infty f_X(x) f_Y(y) f_M(z) dx dy dz$$

$$= \int_0^\infty f_M(z) \frac{\lambda_E}{\lambda_E + 2\lambda_D z}$$

$$\times \left(e^{-g_E^l(n)(\lambda_E + 2\lambda_D z)} - e^{-g_E^u(n)(\lambda_E + 2\lambda_D z)}\right) dz = p(n).$$
(24)

When  $i \neq k - K$ ,

$$\Pr(y_m = i | x_m^k = n) = \Pr(\gamma_M = \gamma_i, \gamma_M > \gamma_k | x_m^k = n)$$
$$= \frac{1 - p(n)}{K - 1}.$$
(25)

Substituting above results into (23), the entropy of the *n*th selection result is expressed as

$$H_n(T_E, N_E) = -p(n)\log_2 p(n) - (1 - p(n))\log_2 \frac{1 - p(n)}{K - 1}.$$
 (26)

Combining all probabilities derived above, we can obtain the expression of information gain for k = K + 1, ..., 2K.

## **B. INFORMATION GAIN RATIO**

Information gain ratio is a splitting criterion defined as the ratio of information gain to the intrinsic information gain. It is proposed to reduce information gain's bias towards multi-valued features by taking into account the number of branches. Information gain ratio of  $F_k$  is calculated by

$$\operatorname{IGR}(D, F_k) = \frac{\operatorname{IG}(D, F_k)}{H_{F_k}(D)}.$$
(27)

 $H_{F_k}(D)$  denotes the intrinsic entropy of  $F_k$  and is expressed by

$$H_{F_k}(D) = -\sum_{n=1}^{N_D+1} \Pr(x_m^k = n) \log_2 \Pr(x_m^k = n), \quad (28)$$

for  $1 \le k \le K$  and

$$H_{F_k}(D) = -\sum_{n=1}^{N_E+1} \Pr(x_m^k = n) \log_2 \Pr(x_m^k = n), \quad (29)$$

for  $K + 1 \le k \le 2K$ . Combining the results of information gain and intrinsic entropy, information gain ration can be obtained.

#### C. GINI INDEX

For the convenience of comparing the splitting criteria, Gini index is defined as the change of Gini impurity. As a result, it will be maximized to optimize the performance of the proposed scheme. Assume that feature  $F_k$  is considered, Gini index is given by

$$\operatorname{GINI}(D, F_k) = \operatorname{Gini}(D) - \operatorname{Gini}(D|F_k).$$
(30)

Gini(*D*) denotes the impurity of sample data and is irrelevant to quantization parameters. Then, we focus on the derivation of  $\text{Gini}(D|F_k)$ , which represents average Gini if  $F_k$  is considered.

1)  $1 \le K \le K$ Gini $(D|F_k)$  is calculated as

$$\operatorname{Gini}(D|F_k) = \sum_{n=1}^{N_D+1} \Pr(x_m^k = n) \operatorname{Gini}(n).$$
(31)

Gini(*n*) is the Gini of branch  $x_m^k = n$  and is expressed as

Gini(n) = 
$$1 - \left( \Pr(y_m = k | x_m^k = n) \right)^2$$
  
 $-\sum_{j \neq k} \left( \Pr(y_m = j | x_m^k = n) \right)^2$   
 $= 1 - q(n)^2 - \frac{(1 - q(n))^2}{K - 1}.$  (32)

Substituting above results into (31), the Gini index of feature  $F_k$  is expressed as

$$\operatorname{Gini}(D|F_k) = \sum_{n=1}^{N_D+1} \left( e^{-\frac{2(n-1)T_D\lambda_D}{N_D}} - e^{-\frac{2nT_D\lambda_D}{N_D}} \right) \times \left( 1 - q(n)^2 - \frac{(1-q(n))^2}{K-1} \right).$$
(33)

2) K + 1 < K < 2KIn this case, we calculate that

 $\operatorname{Gini}(D|F_k) = \sum_{n=1}^{N_E+1} \Pr(x_m^k = n)\operatorname{Gini}(n), \quad (34)$ 

where Gini(n) is the Gini of branch  $x_m^k = n$  and is expressed as

Gini(n) = 
$$1 - \left( \Pr(y_m = k | x_m^k = n) \right)^2$$
  
 $-\sum_{j \neq k} \left( \Pr(y_m = j | x_m^k = n) \right)^2$   
 $= 1 - p(n)^2 - \frac{(1 - p(n))^2}{K - 1}.$  (35)

Substituting above result into (34), we obtain the following expression

$$Gini(D|F_k) = \sum_{n=1}^{N_E+1} \left( e^{-\frac{(n-1)T_E\lambda_E}{N_E}} - e^{-\frac{nT_E\lambda_E}{N_E}} \right) \times \left( 1 - p(n)^2 - \frac{(1-p(n))^2}{K-1} \right).$$
(36)

#### **V. PERFORMANCE EVALUATION**

# A. NUMERICAL RESULTS

We provide experiments for the proposed decision-tree-based relay selection scheme.  $5 \times 10^3$  CSI samples that follow Rayleigh fading are generated to construct training samples. We use classregtree function from MATLAB Statistics and Machine Learning Toolbox to build the CART tree based on training samples. More  $5 \times 10^3$  Rayleigh distributed samples are generated to test the decision tree. Average secrecy rate over all testing sample output is considered as performance metric to evaluate the proposed decision-tree-based scheme. Comparison schemes are optimal selection given in (2), Partial-D in (4), Partial-E in (5) and random selection. We first demonstrate numerical results of splitting criteria,



FIGURE 2. Information gain of input features.



FIGURE 3. Information gain ratio of input features.



FIGURE 4. Gini index of input features.

i.e. information gain, information gain ratio and Gini index, with respect to quantization parameters. Then, we show how the performance of the proposed decision-tree-based scheme changes with quantization parameters.

In Fig. 2, Fig. 3 and Fig. 4, numerical results of splitting criteria are depicted by three-dimensional colored mesh with respect to quantization parameters. The range of  $T_D$  and  $T_E$  is from 0 to 10, and the range of  $N_D$  and  $N_E$  is from 1 to

20. These figures will show the intrinsic relation between splitting criteria and quantization parameters. Fig. 2 shows information gains of the two sets of features representing legitimate channels and eavesdropper channels. Information gain is regarded as a function of  $T_D(T_E)$  and  $N_D(N_E)$ , which is depicted three-dimensionally. We first observe that information gain of both feature sets is decreasing with  $T_D(T_E)$  when  $N_D(N_E)$  is fixed. The reason lies in that large  $T_D(T_E)$  yields longer segments and thus lowers accuracy of quantization. It can be concluded that the length of each segment plays an important role in the decision-tree-based scheme. Thus, we infer that information gain is also increasing with  $N_D(N_E)$ . However, the two surfs show no obvious rise along  $N_D(N_E)$ axis, except for large  $T_D(T_E)$  region. This suggests that when the length of each segment is small enough, it is no longer a significant factor that enhances the performance of the decision-tree-based scheme.

Information gain ratios of the 2K features are depicted in Fig. 3. It is clearly observed that both of the two surfs have a peak point at  $(T_E, N_E) = (0.5, 1)$ , the point closest to the origin. The reason lies in that information gain ratio favors partitions with fewer distinct values. Fig. 4 shows Gini indices of the two feature sets with respect to quantization parameters. We can easily observe that Gini indices of both feature sets are decreasing with  $T_D(T_E)$ . The change of the two surfs along  $N_D(N_E)$  axis is inconspicuous when  $T_D(T_E)$ is small. As  $T_D(T_E)$  grows larger, Gini indices of the two feature sets drop slightly with the decreasing of  $N_D(N_E)$ . Note that Gini index changes with quantization parameters in the similar pattern to information gain. However, information gain ratio shows evident bias towards quantization with two levels. Obviously, information gain and Gini index are more appropriate to the relay selection problem. Consequently, we adopt CART algorithm to build the decision tree in simulation experiments as CART uses Gini index as splitting criterion.

In our simulation experiments, average secrecy rate over the sample data is computed instead of the average secrecy rate defined in (3) owing to the ergodicity of Rayleigh fading channels. In practical wireless networks, CSI of legitimate channels can be precisely estimated, but to obtain full CSI of eavesdropper channels is a difficult task. Therefore, we fix the parameters of legitimate channels and depict average secrecy rate with respect to  $T_E$  and  $N_E$  in Fig. 5 and Fig. 6, respectively. Average secrecy rates of optimal selection, Partial-D, Partial-E and random selection are depicted as comparison. System parameters are K = 5,  $T_D = 5$ ,  $N_D = 20$ ,  $\lambda_D = \lambda_E = 1$ .

Fig. 5 shows how average secrecy rate is affected by  $T_E$ when  $N_E = 2, 8, 15$ . We observe that when  $T_E < 0.5$ , increasing  $T_E$  raises  $\overline{R}_S$  for  $N_E = 8, 15$ . This is because too small  $T_E$  cannot cover enough CSI samples. When  $T_E > 0.5$ , all curves drop with the growing of  $T_E$ , among which the curve with  $N_E = 2$  drops with largest slope, the curve with  $N_E = 15$  only drops slightly with smallest slope and the  $N_E = 8$  curve lies between the other two. It is concluded



FIGURE 5. Average secrecy rate vs.  $T_E$  when  $N_E = 2, 8, 15$ .



**FIGURE 6.** Average secrecy rate vs.  $N_E$  when  $T_E = 0.1, 1, 2$ .

that growing  $T_E$  leads to larger quantization segments and thus lower selection accuracy. If  $N_E$  is large enough, quantization segments can maintain a small length, and selection accuracy is guaranteed. Then, we compare the decision-treebased scheme with benchmark schemes. If  $T_E$  and  $N_E$  are set properly,  $\overline{R}_S$  of the decision-tree-based scheme can achieve a value close to optimal selection. Moreover, even if  $T_E$ and  $N_E$  are not set optimally,  $\overline{R}_S$  of the decision-tree-based scheme can still remarkably exceed random selection.  $\overline{R}_S$  for  $N_E = 8$  and  $N_E = 15$  always outperform Partial-D, which only outperforms the curve with  $N_E = 2$  in high  $T_E$  region. Although Partial-E is superior to Partial-D, it is still inferior to the decision-tree-based scheme if  $T_E$  and  $N_E$  are properly configured.

Fig. 6 shows how  $\overline{R}_S$  changes with  $N_E$  when  $T_E$  is fixed to 0.1, 1 and 2. The first observation is that when  $T_E = 0.1$ ,  $\overline{R}_S$  shows nearly zero fluctuation with  $N_E$  due to the severely incomplete sample set covered by  $T_E$ . When  $T_E = 1$  or 2, as  $N_E$  keeps growing,  $\overline{R}_S$  first rises with  $N_E$  and then stays around a certain value. This is also attributed to the length change of quantization segments, which can hardly influence selection accuracy when exceeding a certain threshold. We also notice that although the converged  $\overline{R}_S$  for  $T_E = 0.1$ 



**FIGURE 7.** Correct ratio vs.  $T_E$  when  $N_E = 2, 8, 15$ .



**FIGURE 8.** Correct ratio vs.  $N_E$  when  $T_E = 0.1, 1, 2$ .

is lower than  $T_E = 1$  and 2,  $\overline{R}_S$  for  $T_E = 0.1$  is higher than the curves with larger  $T_E$  if  $N_E$  is smaller than a threshold. This suggests that the length of quantization segments plays a more important role in the proposed decision-treebased scheme. Comparing decision-tree-based selection with benchmark schemes, we can draw similar conclusions to Fig. 5. It is worth mentioning that  $\overline{R}_S$  for  $T_E = 1$  and  $T_E = 2$ are higher than Partial-E if  $N_E$  is sufficiently large.

Accuracy is one of the metrics evaluating the performance of a decision tree. It is defined as correct ratio, the ratio of the number of correctly predicted samples to the total number of samples. In the simulation experiments, we calculate correct ratio of the decision-tree-based selection as a function of  $T_E$  and  $N_E$ . Fig. 7 depicts correct ratio versus  $T_E$  when  $N_E = 2, 8, 15$  and Fig. 8 depicts correct ratio versus  $N_E$  when  $T_E = 0.1, 1, 2$ . Both figures show that correct ratio can reach 70% if  $T_E$  and  $N_E$  are set optimally. The curves of correct ratio look similar to average secrecy rate. This means that communication metrics such as average rate can also evaluate the performance of decision-tree-based selection.

In Fig. 9, the decision-tree-based scheme is compared with SVM and *k*-NN. Relay selection problem is solved by SVM and *k*-NN with both accurate and quantized CSI.



FIGURE 9. Average secrecy rate comparison with SVM and k-NN.

Average secrecy rates with respect to K are depicted. It is observed that when quantized CSI is used, decision tree is superior to SVM and k-NN for any K. Even if accurate CSI is used, decision tree still outperforms k-NN as long as K > 2.

Summing up all observations described above, we draw the following conclusions. (1) The proposed decision-treebased scheme achieves satisfactory performance in terms of average secrecy rate if the learning parameters are set properly. (2) The length of quantization segments, i.e.  $\frac{T_E}{N_F}$ , plays the key role in deciding relay selection accuracy unless  $\frac{T_E}{N_P}$  is sufficiently small when the performance boost vanishes. Therefore,  $T_E$  should be large enough to cover sufficient CSI samples. (3) Increasing  $N_E$  is definitely beneficial to enhancing  $R_S$ , but also raises the difficulty of estimating eavesdropper channel. How to decide the value of  $N_E$  relies on performance requirement and system's ability to obtain eavesdropper CSI. Generally, in order to achieve high average rate,  $N_D/N_E$  and  $T_D/T_E$  should be set large simultaneously. However, large N costs more feedback bits and large T requires higher hardware quality. If resources are limited, tradeoff between performance and cost should be taken into account.

#### **B. COST ANALYSIS**

#### 1) COMPUTATIONAL COMPLEXITY

Computational complexity of optimization-driven relay selection schemes is O(K), the complexity of maximization algorithm. As comparison, the computational complexity of SVM and *k*-NN is  $O(K^2)$  and O(K), respectively.

The complexity of decision-tree-based prediction depends on the tree depth whose upperbound is K. Consequently, the average time complexity of prediction is lower than O(K). We take balanced decision tree as an example, whose complexity is  $O(\log_2 K)$ . Preparing data and building decision tree are only performed in the initialization part before the dualhop transmissions start. Preparing each sample includes generating M samples of  $\mathbf{x}_m$  and calculating  $y_m$ . Therefore, the complexity of preparing training data is O(KM).

TABLE 2.	Cost Com	parison o	f relay	selection	schemes.
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	optimal	Partial-D	Partial-E	random	decision tree
complexity	O(K)	O(K)	O(K)	O(1)	$O(\log_2 K)$
feedback amount (bits)	48K	32K	16K	0	$K \log_2(N_D + 1)^2(N_E + 1)$
eavesdropper CSI	accurate	none	accurate	none	quantized

Building decision tree includes selecting the best feature from 2K features and splitting the *M* samples into two subsets. Thus, the complexity of building a tree is  $O(KM \log_2 M)$ .

The decision tree needs no renewal in each dualhop transmission provided that fading environment stays stable. If one time slot is 0.5ms, the source transmits 1000 times per second. As transmissions continue, the decision-tree-based scheme shows its superiority to the optimization-driven scheme.

#### 2) FEEDBACK AMOUNT

In optimization-driven scheme,  $g_{Sk}$ ,  $g_{kD}$  and  $g_{kE}$  takes 3K real values. In practical systems, 16 bits are usually used to transmit one continuous real value. Thus, the feedback amount is 48K bits for each selection. In decision-tree-based prediction,  $g_{Sk}^q$ ,  $g_{kD}^q$  and  $g_{kE}^q$  are estimated and fed back to the central controller. Total feedback amount is  $K \log_2(N_D + 1)^2(N_E + 1)$  bits, which is much lower than 48K for practical values of  $N_D$  and  $N_E$ .

In decision-tree-based scheme, training data contains M samples of  $(\mathbf{x}_m, y_m)$ , leading to  $3K \times M$  real values, i.e. 48KM bits. In prediction phase, if one time slot is 0.5 ms, S transmits for 1000 times per second. For  $N_D = N_E = 15$ , the feedback amount of is 12K bits per second, economizing  $36K10^3$  bits per second compared with optimal selection. M is the order of  $10^3$ , so it takes only several seconds to compensate the delay caused by training data collection.

#### CSI ACCURACY

In secure relay selection design, acquiring eavesdropper's CSI is a difficult task. Optimization-driven schemes require accurate eavesdropper CSI while decision-tree-based scheme only requires quantized eavesdropper CSI. The costs of decision-tree-based selection and comparison schemes are compared in Table 2.

#### **VI. CONCLUSIONS AND DISCUSSIONS**

In this paper, we propose a decision-tree-based relay selection scheme for secure dualhop wireless networks. Input features are generated by quantization of legitimate and eavesdropper CSI. To analyze the influence of quantization parameters, we derive three splitting criteria - information gain, information gain ratio and Gini index. We evaluate the performance of the decision-tree-based scheme via simulation, and compare it with optimal selection and other comparison schemes. Simulation results show that if quantization parameters are set properly, the decision-tree-based scheme achieves comparable average secrecy rate to optimal selection results. Cost analysis reveals that the decision-tree-based scheme has advantages in lower computational complexity, smaller feedback amount and lower eavesdropper CSI requirement. In this paper, we have assumed that all channels in the

In this paper, we have assumed that all channels in the dualhop network experience i.i.d. Rayleigh fading, based on which expressions of splitting criteria are derived and simulation results are presented. The proposed scheme can be extended to other channel models, such as non-i.i.d. fading, imperfect CSI, etc. The key issue is how to design quantization parameters for new channel models.

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