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The Optimal Investment Strategy of P2G Based on Real Option Theory

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ABSTRACT This paper initially proposes a real options model for the investment of the Power-to-gas (P2G) plant based on uncertain operating cost which mainly refers to the price of electricity. Through the analysis of the uncertainty parameters affecting the operation of the P2G project, the mathematical model expressing the relations between the parameters of P2G operation cost, electricity price, sunk cost, and other parameters are established. The Brownian motion is utilized to describe the operation cost, based on which, the option value and the project value models of P2G are derived in detail. According to these two models, the optimal investment timing of the P2G device and the corresponding optimal investment capacity can be determined. The above models are verified by numerical simulation. In addition, the influence of the change of parameters on the investment timing and investment capacity in the real options model is studied. The results show that the volatility of electricity price has a greater impact on the option value of P2G project than that of other parameters. When there is a high operating cost uncertainty, waiting is a better option, and the investment can be performed when the operating cost falls to the cost with reference to the optimal investment timing.

INDEX TERMS Power-to-gas, real option, investment opportunity, investment capacity, operation cost uncertainty.

I. INTRODUCTION

Energy storage device can effectively solve the unbalance matching between source and load at the aspect of the time and geographic location in power system. P2G device which can convert redundant power into hydrogen or natural gas, compared with batteries, compressed-air, flywheel and capacitors, has the characteristics of long-term energy storage [1]. The power system is facing the severe problem of volatility and intermittency especially with a high penetration of renewable energy in the future. Germany, for example, will generate 80% of its electricity from renewable sources by 2050. The UK aims to generate 30% of its energy from renewable sources by 2020 and reduce its greenhouse gas emissions by 80% by 2050 compared with 1990 [2]. While alleviating the pollution caused by energy use, the safety and stability of power grid with its volatility and uncertainty is threatened by renewable energies [3]. In addition, there is a situation that renewable energy has low load demand in its

peak output period, and the concomitant problems of wind, solar and water curtailment need to be solved urgently [4]. On the other hand, many industries need a lot of hydrogen, such as petroleum refining, metal smelting, food processing and other industries [5]. Natural gas needs to be imported in large quantities in many countries, such as Mexico, Korea, Japan, China, and India [6]. The redundant renewable energy can be transformed into hydrogen or natural gas by applying P2G technology for the above industries, which can effectively improve the utilization rate of renewable energy, and solve the pollution problem caused by energy use from the origin.

The operation economy of P2G has been discussed in many literatures. Before the advent of P2G technology, power grids and gas networks only relied on gas units as energy conversion devices, and the energy flow was one-way. After the emergence of P2G, the energy transmission between power and gas networks becomes bidirectional, thus increasing resources available to power network and gas network. Literature [7] establishes the heating value model of mixed hydrogen and natural gas, and studies the impact that

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injecting hydrogen into the natural gas pipelines on the wind abandoning, gas sources, gas pressure and carbon dioxide emission reduction of the power grid; Literature [8] proposes a robust optimization model considering the coordinated operation of P2G devices to coordinate the optimal operation of power and natural gas systems with uncertainties; Literature [9] establishes a scenario-based operation optimization model to analyze the micro-integrated power, natural gas and heating system with the consideration of the P2G and carbon capture technologies; Literature [10] analyzes the optimal Day-Ahead scheduling of power grid and gas network on the background of the transformation of redundant electricity power into natural gas for direct sales and combining the price information of power and natural gas market; Literature [11] studies the improvement of renewable energy utilization and carbon dioxide emission reduction effect of the system based on the carbon dioxide recycling system composed of gas turbine and electric gas; Literature [12] introduces the synergistic optimization of P2G device and fuel cells.

Some literatures have also studied the planning of the power network and gas network including the P2G device. A robust optimization programming model with uncertainty is proposed for long-term cooperation between power and gas systems in literature [13]. Based on this model, generators, transmission lines, gas transfer devices, natural gas suppliers, pipelines and compressor stations are simultaneously optimized in this work. In literature [14], electrolyzers as an effective means is taken to reduce the uncertainty of power grid dispatching. The control strategy of ensuring the minimum number of gas turbines is implemented in the running state under a given total output, and the optimal installation capacity of electrolyzers is determined.

Planning is the basis of operation, while it also needs to analyze the economy of investment. The above literatures mainly studied on the operation and planning of the electricity and gas networks with the P2G device, and few literatures investigated the investment economy of P2G. Literature [15] is one of the few to analyze the investment economy of P2G. The electricity is converted into hydrogen via electrolyzers in the P2G system. That work analyzes two scenarios, the hydrogen is converted back to power system and is directly sold. Based on the above scenarios, the economy of investing in electrolyzers as a wind farm energy storage system is analyzed. Further, Brownian motion is used to model the value of energy storage configuration system and a mathematical model between the benefits of energy storage system and various uncertain factors is established. Monte carlo method is used for simulation, discounted cash flow is calculated and taken as the premise of necessity of the real option analysis, and the sensitivity of related uncertain parameters is simulated to analyze its impact on option value. The analytical perspective is novel and the yield analysis of hydrogen is more comprehensive, that is, the hydrogen gains from various possible approaches are synthesized. However, it does not analyze the optimal investment capacity of hydrogen, and its hydrogen capacity is artificially set at 50MW. It can be

expected that the option value of the investment project will vary with the investment capacity. In addition, the value of the project is based on the benefits of the hydrogen storage system. The profit-based option investment model does not have a clear trace of the relationship among the operating and maintenance costs of hydrogen energy storage, the price, the capacity, etc., so it cannot conduct in-depth analysis of the basic variables.

The real option theory applied in literature [15] has been applied in various aspects of investment in power system:

In literature [16], the application of the path-dependent scenario tree technology in the real option theory is researched to evaluate wind power projects by solving the uncertainty of wind resource assessment, more accurate wind resource estimation is expected to enhance the value of the wind power investment. Based on the assumption that wind speed follows Weibull distribution and Gaussian distribution, the paper analyzes the potential of improving the value of wind power projects under different conditions and concludes that in most cases, the application of this method can increase the value of wind power investment projects.

Literature [17] applies real options to the carbon market to estimate the large incremental return of grid-connected renewable energy in the carbon market, namely the approved emission reduction-CER. The writing background of his thesis is based on whether the registration of clean development mechanism in Brazil has the value of investment. Incremental returns need to determine the carbon emission reduction under the baseline scenario, and the baseline measurement standard is the Brazilian document ACM0002. The present value of the proceeds from the sale of CER is considered as the value of the option, and the cost of registering CER with the United Nations commission for grid-connected power generation projects and the additional fees involved are considered as the strike price. In addition, the operation period of the project is regarded as the expiration date of the option. The price fluctuation of CER sold is taken as the volatility of the option, and the binomial option model is applied to determine the investment value of the CER project.

Literature [18] regards the portfolio contract of demand response as an investable project, evaluates the value of the demand response contract by applying the real option model, and takes the load aggregator and demand response user as both parties of the contract. Its essence is the power market trading based on the spot price of power and considering the option contract. Load aggregators of demand response (DR) can participate in the balancing market, use DR contracts to balance energy portfolios, reduce unbalanced costs, and thus hedge risks related to real-time price fluctuations. When the spot price exceeds the strike price, the option holder will exercise the option contract to purchase power from the demand response user at a lower strike price, thereby reducing the user load in the short term, and when the spot price is less than the strike price, the option will not be exercised and the option holder will purchase the power at the spot price. In addition, the situation that the aggregator's participation

in the day-ahead energy market as an energy retailer is also analyzed.

In literature [19], the option model is applied to determine the investment proportion of wind power and small hydropower, and the timing of investment is also determined. The optimization model in this paper is a two-layer model of Max-Min. The upper model is the investment option model of renewable energy projects considering the risks of energy purchase and sale, while the lower model is the purchase and sale costs of energy contracts in the worst case. The two-layer model is solved by robust optimization. The core idea of the work is to make portfolio project decisions based on the revenue level of energy contracts. Its innovation is reflected in the application of option model on the field of energy, which extends the application scenarios of investment decisions, namely, it is applied to the energy contracts of energy companies, and robust optimization is considered.

In literature [20], the optimal investment timing in irreversible engineering in which investment income and investment cost following continuous time stochastic process is studied, and the optimal investment rules and the formula of investment option value are derived. These formulas can be used to accurately calculate the investment time rules of a project and the loss value of investment in sub-optimal time.

With the increased confidence of countries in the application of P2G equipment, many countries have launched demonstration projects for P2G devices, and there is an urgent need to conduct research on the investment strategies of P2G project. Many countries in the world have built demonstration plants for P2G, including Germany, the United Kingdom, the United States, Spain, Canada, France, Denmark and so on. The power sources of P2G can be public power grid [21], photovoltaic power generation [22], [23], wind power [24], [25], hydropower [26], [27], etc.

The investment decision is of great importance on account of the irreversibility of the investment in the P2G equipment. Once invested, there will be sunk costs because of the specificity of the application of the P2G device. The P2G plants convert power into hydrogen, which has high conversion efficiency and economy compared to other forms. To this end, this paper mainly studies the investment optimization of electrolyzer plants. The most important factor affecting the economics of hydrogen investment via electrolyzers is the price of electricity. The price of electricity has a strong volatility, and it is the cost of hydrogen production. Therefore, the operating cost of hydrogen investment is uncertain. In the face of increasing uncertainty, real options are particularly suitable for investment analysis of P2G projects because a relatively complete analytical framework for uncertain environments can be provided. However, the uncertainty parameter of the investment model of traditional real options is generally the price of the output of the investment device. Under this circumstance, the idea of real option investment modeling in literature [28] is applied in this work and the model is also rewritten and expanded to fit the investment of P2G. An option investment model of the electrolyzer device based

on the uncertainty of operating cost is established, and the optimal investment timing and optimal investment capacity of the device are determined in this work. The main contributions of this paper are as follows:

(1) Instead of output price volatility consideration in traditional models, a real option investment model with production cost uncertainty is established, which is right fit the case of P2G.

(2) The proposed real option investment model is capable of determining the optimal investment timing and the associated optimal investment capacity simultaneously.

(3) In case study, sensitivity analysis is conducted with reference to different electricity price fluctuation rates, different investment costs, and prices of different output products. Furthermore, with minor adjustment, the application of the model can be expanded to other physical assets with high uncertainty in production cost and relatively stable output price.

The remainder of this paper is structured as follows. In section II, the operation cost model of the P2G and, based on the cost uncertainty, the option value and the project value are proposed so as to calculate the optimal investment opportunity and the optimal investment capacity of the project. In Section III, the solving steps of the mathematical model proposed in the second part are described. Numerical Simulation are introduced in Section IV to demonstrate the feasibility and effectiveness of the proposed real option mathematical model of the P2G project. Finally, a brief conclusion is given in Section V.

II. OPTION VALUE MODELING FOR P2G PLANT INVESTMENT

Real options can be used to adjust the project's investment decisions of the larger uncertainties currently facing by modeling the investment flexibility.

The P2G project investment has greater uncertainty since it takes the electricity price as a cost. However, traditional cash flow (NPV) investment methods are difficult to flexibly adjust to unforeseen market changes and correct subsequent decisions. For example, after starting an investment project, it will always operate according to the basic scale until the end of the project life. While the real option (ROA) theory can be used to model the uncertainty, and with the advent of new information, the relevant uncertainty gradually becomes clear. The real option theory can be utilized to change the initial business strategy and adapt to the changing market. The decision-makers can invest in opportunities that will be profitable in the future, and can delay, expand, shrink, abandon or even change projects at various stages of the project's business cycle [29]. It shows the difference between the NPV and ROA methods in FIGURE 1. The ROA method allows waiting for uncertain information about the project investment. The project is only invested when the uncertain information disappears and the investment environment shows a good signal. Thereby, the volatility σ of the uncertain information is decreased, and the expected value μ of the

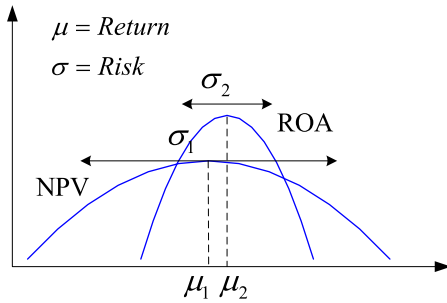


FIGURE 1. The risk and reward comparisons of NPV and ROA.

project is also increased. NPV method has lower returns and higher risks to an investment project, relatively speaking, ROA can achieve a win-win situation that avoids risks and gets higher returns.

The decision maker of the P2G project can choose to invest immediately or postpone the investment when the right to build the plant is obtained. When a P2G plant has been set up, the decision maker needs to make a decision on its operation in response to the changing power market: put it into operation immediately or wait for the operation opportunity. It needs to weigh the benefits and risks to make a choice between the two strategies. Postponing the investment is equivalent to holding an unlimited call option, but policy-makers face uncertain risks from electricity prices, hydrogen prices and so on. The historical price of hydrogen is relatively stable. Thus, the price of hydrogen is set at a constant value in this paper. It is assumed that the option to invest in the P2G project has been decided to be implemented. The project can be temporarily shut down costlessly if the sales price of hydrogen falls below the operating cost during production, and it can be restarted latter without any cost if the sales price of hydrogen rises above the operating cost thereafter. Based on the above situation, the investment decisions for electrolyzer plants is made in this paper. It is necessary to determine the investment strategy, including the investment capacity of the device and the timing of investment.

A. ABBREVIATIONS BROWNIAN MOTION MODEL OF P2G PROJECT OPERATION COST

In the power market environment, the power required for P2G operation is completely purchased from the electricity market. At this time, the mathematical model of $E(t)$ is described in equation (1).

$$E(t) = \frac{P_I}{\eta_{P2G}(t)} C_M(t) + C_F \quad (1)$$

where C_M is the market price of the electricity, P_I is the electricity energy consumption in theory of 1kg of hydrogen generated by the P2G device, η_{P2G} is the investment efficiency of P2G plant, C_F refers to other costs required by the operation of the P2G device.

Mean reversion model can be used for power price modeling, but geometric Brownian motion modeling will

not produce large errors in the results [30]. In particular, the Brownian motion model can be used to obtain satisfactory results compared with the model having slow mean recovery. For simplicity, electricity price $C_M(t)$ follows geometric Brownian motion. The model of Brownian motion of $C_M(t)$ is as follows:

$$dC_M(t) = \alpha_{C_M} C_M(t)dt + \sigma_{C_M} C_M(t)dz(t) \quad (2)$$

where, α_{C_M} is the expected relative drift of $C_M(t)$ per unit of time, σ_{C_M} is the standard deviation per unit of time.

For the convenience of analysis, let $C_F = 0$, when the electricity price $C_M(t)$ follows the Brownian motion, $E(t)$ also follows the Brownian motion with the same drift rate and volatility. The following is the derivation process.

Using Ito's Lemma according equation (1), expand dE in equation (3):

$$dE = \left(\frac{\partial E}{\partial C_M} \alpha_{C_M} C_M + \frac{\partial E}{\partial t} + \frac{1}{2} \frac{\partial^2 E}{\partial C_M^2} \sigma_{C_M}^2 C_M^2 \right) dt + \frac{\partial E}{\partial C_M} \sigma_{C_M} C_M dz \quad (3)$$

The equation(4) can be derived after inserting $\partial E/\partial C_M = P_I/\eta_{P2G}$, $\partial E/\partial t = 0$, $\partial^2 E/\partial C_M^2 = 0$ to equation(3):

$$dE = \frac{P_I}{\eta_{P2G}} C_M(t) \alpha_{C_M} dt + \frac{P_I}{\eta_{P2G}} C_M(t) \sigma_{C_M} dz \quad (4)$$

dE can be written as follows:

$$dE = \alpha_{C_M} E(t)dt + \sigma_{C_M} E(t)dz \quad (5)$$

Then, the equation (6) can be derived:

$$\left. \begin{aligned} \alpha_E &= \alpha_{C_M} \\ \sigma_E &= \sigma_{C_M} \end{aligned} \right\} \quad (6)$$

The model of Brownian motion of $E(t)$ is as follows:

$$dE(t) = \alpha_E E(t)dt + \sigma_E E(t)dZ(t) \quad (7)$$

where, α_E is the expected relative drift of $E(t)$ per unit of time, σ_E is the standard deviation per unit of time. And $dZ(t)$ is the increment of Wiener process. $dZ(t) = \varepsilon(t)\sqrt{dt}$, $\varepsilon(t) \sim N(0, 1)$, $E(0) = E_0$.

Since $dE(t)/E(t)$ follows normally distribution, thus $dE(t)$ follows logarithmically normally distributed. $G = \ln E$, $\partial G/\partial t = 0$, $\partial G/\partial E = 1/E$, $\partial^2 G/\partial E^2 = -1/E^2$.

The mathematical model of income and profit of P2G output is as follows.

$$Y(t) = R - E(t) \quad (8)$$

$$R = R_u * W_{P2G} \quad (9)$$

$Y(t)$ is the profit of the investment of P2G, and R is the overall income of the production. R_u is the unit price of the production. W_{P2G} is the installation capacity of P2G device.

The mathematical expression of the investment of P2G is as follows.

$$Q(t) = \eta(t)W_{P2G} \quad (10)$$

where $Q(t)$ is the annual output of P2G device. $\eta(t)$ is its utilization function, and it is assumed to be a constant here.

The capacity cost model of P2G plant adopts the exponential function model in literature [31]:

$$C_{P2G} = K_{P2G}e^{n_1 W_{P2G}} \quad (11)$$

C_{P2G} is the investment cost when the capacity of the P2G device is equal to W_{P2G} . n_1 is the exponential constant of the power function, and K_{P2G} is the constant coefficient.

B. MATHEMATICAL MODELING OF OPTIMAL INVESTMENT TIMING BASED ON ROA-INVESTMENT PROJECT VALUE $V(E)$

The decision maker who invests in the P2G device holds an option similar to a financial call option, which gives the right, but not the obligation, to invest in the device at a time of its choosing. When a company decides to invest in a P2G device, the investing entity executes the option but at the cost of abandoning the option, that is, the possibility of waiting for new information that may affect the willingness or timing of the investment is given up. The lost option value is the opportunity cost of investment, which must be included in the investment cost [32].

The value of P2G project is $V(E)$. It can determine the expected rate of return by constructing a risk-free portfolio and equating the expected rate of return to the risk-free interest rate.

Next an investment portfolio can be built. Let the option of holding a project with a value of $V(E)$ obtain a short position $n = V'(E)$. The dynamic investment value Φ of the P2G device can be expressed as follows.

$$\Phi = V(E) - V'(E)E \quad (12)$$

where $\pi(E)$ is the profit from an investment project during the dt period.

The short-term portfolio's return required during the dt period is $(r - \alpha_E)EV'(E)$, which is required to be paid by the short position in the portfolio, so the total return on holding the portfolio during the dt period is described as follows.

$$\varphi = \pi(E) + dV(E) - V'(E)dE - (r - \alpha_E)EV'(E)dt \quad (13)$$

The following equation can be obtained from Ito's lemma.

$$dV(E) = V'(E)dE + \frac{1}{2}V''(E)(dE)^2 \quad (14)$$

Equation (15) can be obtained from equation (13) and equation(14).

$$\varphi = \pi(E) + \frac{1}{2}V''(E)(dE)^2 - (r - \alpha_E)EV'(E)dt \quad (15)$$

Since $E(t)$ follows Brownian motion, equation (16) can be obtained from (7).

$$(dE)^2 = \sigma_E^2 E^2 dt \quad (16)$$

Equation (17) can be obtained from equation (15) and equation (16).

$$\varphi = \pi(E) + \frac{1}{2}\sigma_E^2 E^2 V''(E)dt - (r - \alpha_E)EV'(E)dt \quad (17)$$

According to the no arbitrage principle, equation (18) can be derived.

$$\varphi = r\Phi dt \quad (18)$$

Equation (19) can be obtained by solving the simultaneous equations (12), (17) and (18).

$$\frac{1}{2}\sigma_E^2 E^2 V''(E)dt + \alpha_E EV'(E) - rV(E) + \pi(E) = 0 \quad (19)$$

The solution form of the Equation (19) is as follows.

$$V(E) = A_1 E^{\beta_1} + A_2 E^{\beta_2} + M_C \quad (20)$$

M_C is a constant term here. After simple transformation, it can be known that the special solution of equation (19) is $(-\frac{E}{r-\alpha_R} + \frac{P}{r})$, and the equation has the following form:

$$V(E) = A_1 E^{\beta_1} + A_2 E^{\beta_2} - \frac{E}{r - \alpha_E} + \frac{R}{r} \quad (21)$$

where A_1, A_2 and β_1, β_2 are undetermined coefficients. The first two items of equation (21) can be seen as the option value, while the latter two items can be seen as the cash flow of the investment project.

The solution process of equation (19) is divided into two steps, namely, the situations of $E > R$ and $E < R$:

1) When $E > R, \pi(E) = 0$, that is, the operation of the project is postponed in this case, and the project does not have any profit flow.

The equation at this time is a homogeneous differential equation with the following form:

$$V(E) = K_1 E^{\beta_1} + K_2 E^{\beta_2} \quad (22)$$

where, K_1 and K_2 are undetermined coefficients, and β_1 and β_2 are solutions of the following equation:

$$\frac{1}{2}\sigma_E^2 \beta^2 + (\alpha_E - \frac{1}{2}\sigma_E^2)\beta - r = 0 \quad (23)$$

Solving Equation (23) can get the following solutions.

$$\beta_1 = \frac{1}{2} - \frac{\alpha_E}{\sigma_E^2} + \sqrt{(\frac{\alpha_E}{\sigma_E^2} - \frac{1}{2})^2 + \frac{2r}{\sigma_E^2}} \quad (24)$$

$$\beta_2 = \frac{1}{2} - \frac{\alpha_E}{\sigma_E^2} - \sqrt{(\frac{\alpha_E}{\sigma_E^2} - \frac{1}{2})^2 + \frac{2r}{\sigma_E^2}} \quad (25)$$

Since $\beta_1 > 1, E^{\beta_1} \rightarrow \infty$ when the operation cost $E \rightarrow \infty, E^{\beta_1} \rightarrow \infty$. So multiplied by this item equal to zero. This constant term is represented by the symbol K_1 . The value of the project can be described as follows.

$$V_1(E) = K_2 E^{\beta_2} \quad (26)$$

2) When $E < R$, $\pi(E) \neq 0$. Therefore, equation (19) has the following form of solution.

$$V(E) = B_1 E^{\beta_1} + B_2 E^{\beta_2} - \frac{E}{r - \alpha_E} + \frac{R}{r} \quad (27)$$

where, B_1 and B_2 are undetermined coefficients.

Since $\beta_2 < 0$, the value of the option cannot be increased indefinitely with the extension of time. Therefore, when $E \rightarrow 0$, R^{β_2} has no economic significance. The solution form in this case is as follows.

$$V_{\Pi}(E) = B_1 E^{\beta_1} - \frac{E}{r - \alpha_E} + \frac{R}{r} \quad (28)$$

where B_1 and β_1 are undetermined coefficients.

3) Determine the undetermined coefficients K_2 and B_1 in equations (26) and (28) at point $E = R$:

The solution to $V(R)$ must be a continuously differentiable value, so the following equation can be derived.

$$\begin{cases} V_1(E)|_{E=R} = V_{\Pi}(E)|_{E=R} \\ V'_1(E)|_{E=R} = V'_{\Pi}(E)|_{E=R} \end{cases} \quad (29)$$

Equations (30) and (31) can be obtained from (29).

$$K_2 = \frac{R^{1-\beta_2}}{\beta_1 - \beta_2} \left(\frac{\beta_1}{r} - \frac{\beta_1 - 1}{r - \alpha_E} \right) \quad (30)$$

$$B_1 = \frac{R^{1-\beta_1}}{\beta_1 - \beta_2} \left(\frac{\beta_2}{r} - \frac{\beta_2 - 1}{r - \alpha_E} \right) \quad (31)$$

1) MATHEMATICAL MODELING OF OPTIMAL INVESTMENT CAPACITY BASED ON ROA-OPTION VALUE F(E)

The net present value of the investment is shown in equation (32).

$$NPV = V(W_{P2G}|E^*) - C_{P2G}(W_{P2G}) \quad (32)$$

When investing in the P2G device, the maximum net present value can be used to find the optimal investment capacity. The schematic diagram of the principle is shown in FIGURE 2.

$$\frac{\partial V}{\partial W_{P2G}} = \frac{\partial C_{P2G}}{\partial W_{P2G}} \quad (33)$$

The project will be invested only when $E < R$. Equation (34) can be obtained from equation (9), (11) and (28).

$$B_1 \beta_1 E_u^{\beta_1} W_{P2G}^{*\beta_1-1} - \frac{E_u}{r - \alpha_E} + \frac{R_u}{r} = K_{P2G} e^{n_1 W_{P2G}^*} \quad (34)$$

It can be seen from the above equations that the optimal investment capacity W_{P2G}^* is a function of the operating cost E_u . Although W_{P2G}^* cannot write out an analytical expression about E_u , the numerical solution of the optimal investment capacity W_{P2G}^* can be derived if E_u is given.

$$Y_1(W_{P2G}^*|E_u^*) = B_1 \beta_1 E_u^{*\beta_1} W_{P2G}^{*\beta_1-1} - \frac{E_u^*}{r - \alpha_E} + \frac{R_u}{r} - K_{P2G} e^{n_1 W_{P2G}^*} \quad (35)$$

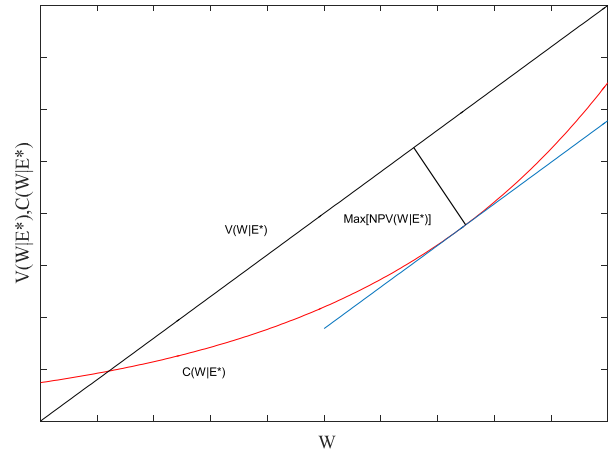


FIGURE 2. Schematic diagram of the solution of optimal capacity.

The expression of the optimal investment capacity W_{P2G}^* is as follows.

$$W_{P2G}^* = \text{Arg}\{Y_1(W_{P2G}^*)|_{E_u^*} = 0\} \quad (36)$$

The investment cost under the optimal investment capacity is described in equation (37).

$$C_{P2G}^* = K_{P2G} e^{n_1 W_{P2G}^*} \quad (37)$$

The operating cost E of P2G follows the geometric Brownian motion, so the option value of its investment satisfies the following form:

$$F(E) = M_1 E^{\beta_1} + M_2 E^{\beta_2} \quad (38)$$

$F(E)$ should satisfy the following three constraints:

$$\begin{cases} F(\infty) = 0 \\ F(E^*) = V(E^*) - C_{P2G}^*(E^*) \\ F'_E(E^*) = \frac{\partial(V(E^*), Q^*)}{\partial E} \end{cases} \quad (39)$$

In order to satisfy $F(E) = 0$ when $E \rightarrow \infty$, it is necessary to make $M_1 = 0$, and the following equations are obtained during the operation period ($E < R$).

$$M_2(E^*)^{\beta_2} = B_1(E^*)^{\beta_1} - \frac{E^*}{r - \alpha_E} + \frac{R}{r} - C_{P2G} \quad (40)$$

$$\beta_2 M_2(E^*)^{\beta_2-1} = \beta_1 B_1(E^*)^{\beta_1-1} - \frac{1}{r - \alpha_E} \quad (41)$$

Equation (42) is obtained from (40) and (41).

$$B_1(\beta_2 - \beta_1)(E_u^* W_{P2G}^*)^{\beta_1} + \frac{(1 - \beta_2)E_u^* W_{P2G}^*}{r - \alpha_E} + \beta_2 \left(\frac{R}{r} - C_{P2G}^* \right) = 0 \quad (42)$$

It can be seen from the above equation that the value of E_u^* of the optimal investment timing can be obtained if the optimal investment capacity W_{P2G}^* is given. Further, E_u^* has

no analytical expression, but the numerical solution can be obtained.

$$Y_2(E_u^* | W_{P2G}^*) = B_1(\beta_2 - \beta_1)(E_u^* W_{P2G}^*)^{\beta_1} + \frac{(1 - \beta_2)E_u^* W_{P2G}^*}{r - \alpha_E} + \beta_2\left(\frac{R}{r} - C_{P2G}^*\right) \quad (43)$$

Then, the optimal investment rule is described in equation (44).

$$E_u^* = Arg\{Y_2(E_u^*)|_{W_{P2G}^*} = 0\} \quad (44)$$

Equation (44) does not have an analytical solution, but there is a numerical solution.

Therefore, the optimal investment capacity W_{P2G}^* and the E_u^* value of the optimal investment timing can be derived from solving the equations (34) and (42).

M_2 can be obtained by substituting E_u^* into (40):

$$M_2 = (E^*)^{-\beta_2}(B_1(E^*)^{\beta_1} - \frac{E^*}{r - \alpha_E} + \frac{R}{r} - C_{P2G}) \quad (45)$$

$F(E)$ can be derived by substituting (25) and (45) into equation (38).

III. THE SOLUTION METHOD OF THE PROPOSED REAL OPTIONS MODEL OF P2G PROJECT

The operating cost sequence $E(t)$ of the P2G device is affected by the investment capacity W_{P2G} , and the investment capacity W_{P2G} is determined according to the drift rate α_E and the volatility σ_E of the running cost sequence. In the case that the power energy used by the P2G device is completely obtained from the power market, the optimal timing and capacity of the investment and operation of the P2G project are determined using the above option model. The drift rate α_E and the volatility σ_E can be obtained by equation (6).

The Brownian motion is used to model the electricity price, and the drift rate α_E and the volatility σ_E can be calculated by equations (46) and (47):

$$Y_3 = \alpha_E = \frac{1}{n} \sum_{i=1}^n [(E_{i+1} - E_i)/E_i] \quad (46)$$

$$Y_4 = \sigma_E = \sqrt{\frac{1}{n-1} \sum_{i=1}^n \{(E_{i+1} - E_i)/E_i - \frac{1}{n} \sum_{i=1}^n [(E_{i+1} - E_i)/E_i]\}^2} \quad (47)$$

The solving steps are summarized in FIGURE 3. The solution steps of this mode are as follows:

Applying the above mathematical model can get the value of $V(E)$ and $F(E)$. The $E(t)$ value of each moment can be obtained according the formula (1). $E(t)$ sequence can be described by Brownian motion. Through the analysis of massive data of electricity price, drift rate α_E and the volatility σ_E can be obtained through formula (6). Based on the historical data of sunk cost of P2G investment and the above mathematical model, relevant parameters are obtained, such

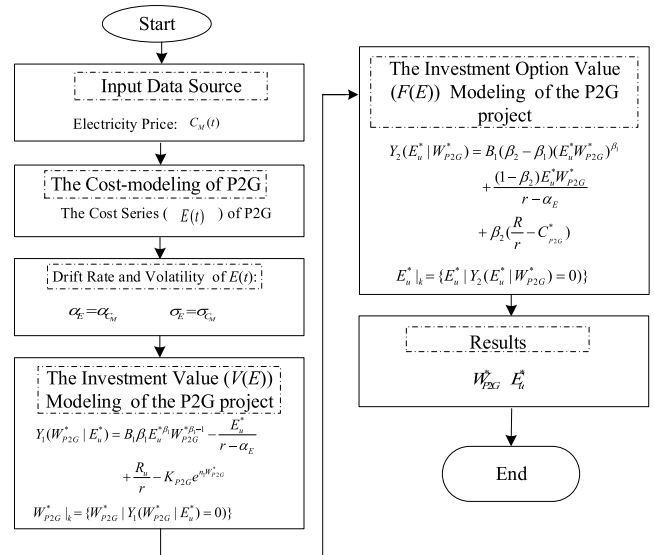


FIGURE 3. Flowchart for the optimal investment strategy modeling and solving of the P2G project (The electricity market model).

as K_{P2G} and n_1 . In combination with other parameters r and hydrogen price R_u etc., the optimal investment capacity and timing can be derived according to the derivation of the above mathematical models.

IV. NUMERICAL SIMULATION

This section takes the solution method and the solution process given in Part III to the application and analysis of the real option mathematical model of the P2G project established in Part II.

The energy conversion relationship between the power energy and the hydrogen in P2G is generally $48 \sim 60$ kWh/kg, which is 54 kWh/kg in the calculation, and the theoretical value is 39 kWh/kg. In actual operation, the operation efficiency of electrolyzers is generally between 67% and 76% , the efficiency is 72% used in this work, the operating cost of hydrogen is generally between 2.7 and 3.5 \$/kg in general, and the annual operating hours of P2G is 6000 [33]–[37]. Based on the data set above, the proposed mathematical model can be used to analyze the investment of the P2G project. It can be regressed of the historical data of the investment cost of the P2G, and the result is obtained, K_{P2G} is 51.77 , n_1 is 0.02084 . Assuming that the fitting functional relationship between the investment capacity and the cost is accurate, using the real option model established above, the operating options of the P2G project are analyzed as follows.

A. APPLYING THE REAL OPTION MODEL TO DERIVE THE OPTIMAL INVESTMENT TIMING AND OPTIMAL INVESTMENT CAPACITY OF THE P2G PROJECT

The flow chart shown in FIGURE 3 can be used to solve the problem. The parameters in the real option model are as follows: $r = 0.04$, $\alpha_E = 0$, $\sigma_E = 0.2$, $h = 6000$, $R_u = 5\$/kg$. In FIGURE 4, the black line is the option

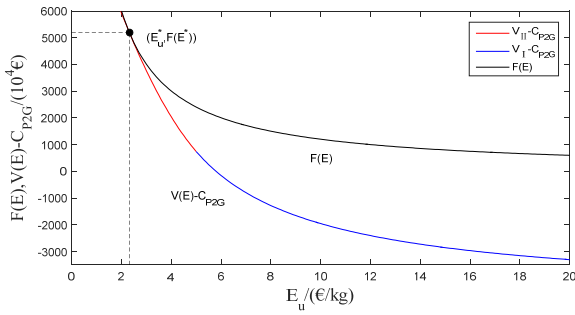


FIGURE 4. The value of investment opportunities in the base case.

value $F(E)$ of the P2G project, the red line represents $V_{II} - C_{P2G}$, and the blue line represents $V_I - C_{P2G}$. The optimal investment timing $E_u^* = 2.3202\text{€/kg}$ is derived at tangent point of the $F(E)$ curve and the $V(E) - C_{P2G}$ curve, and the corresponding optimal investment capacity is $W_{P2G}^* = 215.8241\text{kg/h}$, the total sunk cost is $C_{P2G}^* = 46.50$ million euros.

The option value $F(E)$ is greater than the net present value $V(E) - C_{P2G}$ of the immediate investment when $E_u > E_u^*$. The investment project encourages waiting before the operation cost value of the P2G investment project reaches E_u^* . In addition, the project arrives at the optimal investment timing when the net present value of the investment is equal to the value of waiting.

Then, the sensitivity of the parameters in the mathematical real option model of the P2G device is analyzed under full load operation to find the optimal investment timing and the optimal investment capacity W_{P2G}^* . The sensitivity analysis of the parameters affecting P2G project investment in the real option model is conducted in the following part. Therefore, the mathematical model proposed in this paper can be applied to invest in the P2G project in different situations.

B. THE SENSITIVITY ANALYSIS OF PARAMETERS IN REAL OPTION MODEL

1) THE CASE WITH THE CHANGE OF HYDROGEN PRICE R_u
 This part investigates the change of P2G device investment strategy when the sales price of P2G output changes. The parameters in the real option model are as follows: $r = 0.04$, $\alpha_E = 0$, $\sigma_E = 0.2$, $h = 6000$, $R_u = 5.5/6.5/7.5\text{€/kg}$. In this case, the optimal investment timing E_u^* are 2.58, 3.11 and 3.65 euro/kg respectively which can be seen from FIGURE 5. And the corresponding optimal investment capacities W_{P2G}^* are 220.41, 228.46 and 235.36 kg/h respectively.

It can be seen from FIGURE 5 that the optimal investment opportunity moves to the right, and the operation of P2G investment can be started at a higher cost as the sales price of hydrogen increasing, That is, when the sales price of hydrogen is high, it can engage in investment and operation activities even if the electricity price is high. On the other hand, if the high-end market for hydrogen can be found, the sales price of hydrogen can be kept high, and the investment and

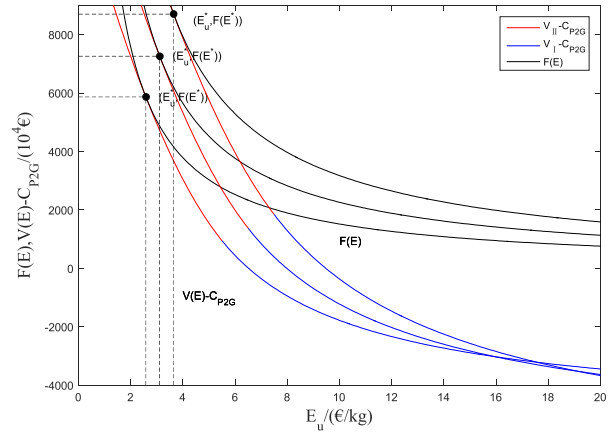


FIGURE 5. The value of investment opportunities with the change of hydrogen price R_u .

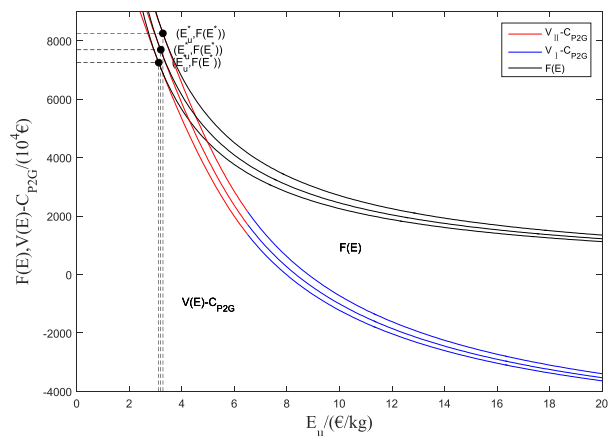


FIGURE 6. The value of investment opportunities with the change of sunk cost C_{P2G} .

operation can be carried out when the operation cost of P2G is high.

2) THE CASE WITH THE CHANGE OF SUNK COST C_{P2G}
 This part investigates the change of P2G device investment strategy when the sunk cost of P2G (C_{P2G}) changes. The parameters in the real option model are as follows: $r = 0.04$, $\alpha_E = 0$, $\sigma_E = 0.2$, $h = 6000$, $R_u = 6.5\text{€/kg}$. The sunk cost of investment C_{P2G} is going to be 100%, 80%, 60% of the base case. Through calculation, the optimal investment timing E_u^* is 3.1124, 3.1876 and 3.2768€/kg respectively which can be seen from FIGURE 6. It can be seen that the investment cost has little influence on the optimal investment timing. The optimal operation cost only increases by 5.28% even if the investment sunk cost decreases by 40%.

3) THE CASE WITH THE CHANGE OF VOLATILITY σ_E
 The change of P2G device investment strategy is investigated in this part when the volatility of investment cost (σ_E) changes. The parameters in the real option model are as follows: $r = 0.04$, $\alpha_E = 0$, $h = 6000$, $R_u = 6.5\text{€/kg}$, $\sigma_E = 0.1/0.2/0.3$. It can be seen from FIGURE 7 that

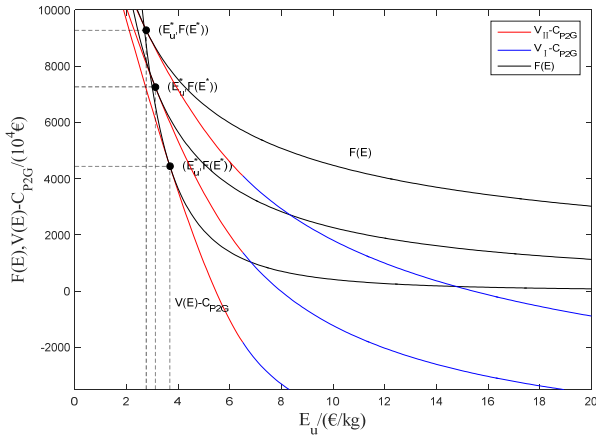


FIGURE 7. The value of investment opportunities with the change of volatility σ_E .

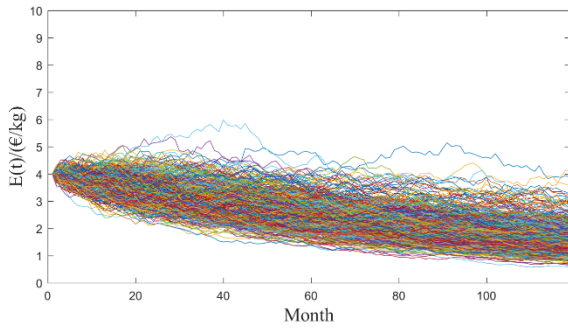


FIGURE 8. The sample sequences of $E(t)$ with $\sigma_E = 10\%$.

the project option value increases with the volatility σ_E , namely, it has greater incentives to wait for a period of time to investment under this kind of situation. In addition, the optimal investment cost E_u^* is 3.6803, 3.1124 and 2.7622 €/kg respectively, and it decreases with the volatility σ_E . The corresponding optimal investment capacity W_{P2G}^* , increasing with the volatility σ_E , is 225.09, 228.46 and 231.78 kg/h respectively.

As can be seen from FIGURE 7, the optimal investment opportunity moves to the left with the increase in volatility, that is, the higher uncertainty increases the option value of the investment in the P2G project and it encourages more waiting. The fluctuation range of operation cost increases with the volatility σ_E . This rule can also be directly reflected from the simulation path of $C_M(t)$ in FIGURE 8, FIGURE 9 and FIGURE 10. Due to the higher volatility of electricity price in the case of high uncertainty, the price sequence will have greater volatility in the future. As a result, there may be a possibility of sharp rise in electricity price in the future. Therefore, decision makers of P2G project are encouraged to wait for a longer time until lower investment cost can be determined. In this way, operation options can be exercised to carry out the investment and operation of P2G project. It can be used to explain why the option value of the P2G project will grow with the volatility. That is, the operation risk of P2G device is greater due to the higher volatility. Therefore,

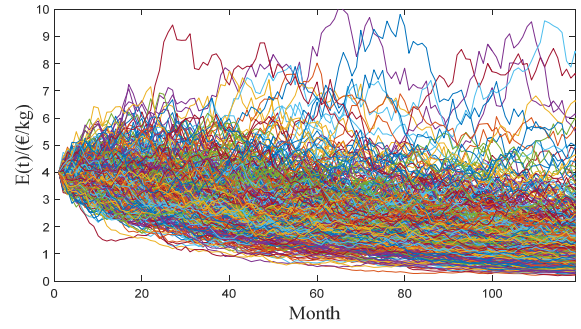


FIGURE 9. The sample sequences of $E(t)$ with $\sigma_E = 20\%$.

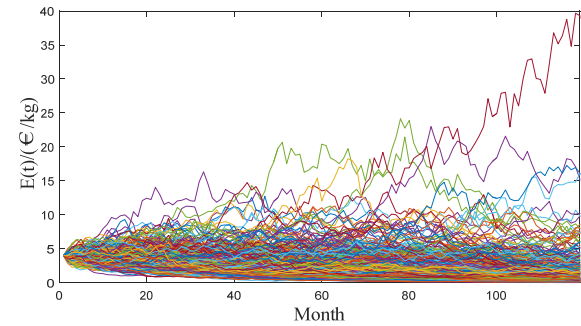


FIGURE 10. The sample sequences of $E(t)$ with $\sigma_E = 30\%$.

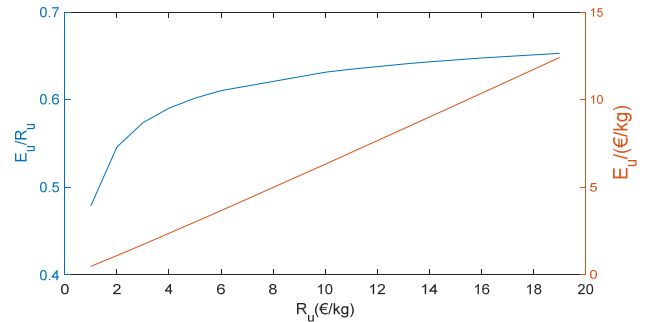


FIGURE 11. Schematic diagram of hydrogen price and optimal investment timing, the ration of operation cost, and hydrogen price.

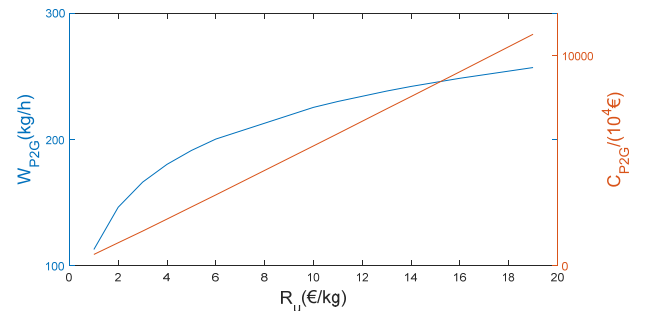


FIGURE 12. Schematic diagram of the relationship between hydrogen price and optimal investment capacity, and investment cost.

waiting has greater value to avoid future risks. The bigger the σ_E is, the option value is higher.

In FIGURE 8, FIGURE 9 and FIGURE 10, the initial value of $E(t)$ is 4€/kg. It can be seen from them that the greater

the volatility σ_E , the more possibility is that $E(t)$ sequences will decline under the same drift rate. The drift rate of $E(t)$ and $C_M(t)$ is set at 0.09, and the data trend is downward, the volatility is 10%, 20% and 30% respectively.

4) THE RELATIONSHIP BETWEEN HYDROGEN PRICE R_u AND OPTIMAL INVESTMENT COST E_u^*

The P2G operating cost (E_u) and the ratio of operation cost and hydrogen price (E_u/R_u) with different hydrogen prices at optimal investment timing are shown in FIGURE 11. It can be seen from the figure that the optimal investment timing of hydrogen is basically linear with the price of hydrogen, and the operating cost increases with the hydrogen price under the premise that other parameters are unchanged. The relationship between hydrogen price and the optimal investment capacity and investment sunk cost of P2G is shown in FIGURE 12. The optimal investment capacity of P2G gradually increases with the hydrogen price, but its increment gradually decreases, and its investment sunk cost is basically linear with the price.

V. CONCLUSIONS

The largest proportion of electricity costs in the operation of the P2G plant is the most important factor affecting the economics of the plant operation. In the electricity market environment, there is great uncertainty in electricity prices. A real option investment model based on the uncertainty of operating costs of P2G device is established in this work. Brownian motion model is used to describe the price of electricity in this work, and the economic efficiency of P2G in power market is modeled and analyzed. On this basis, the sensitivity analysis of the relevant parameters which affect the investment of P2G project is carried out.

From the analysis results, the P2G investment project is affected by the sales price of the output production, the cost of electricity price, while the sunken cost of the investment in P2G project is less affected. Especially when the operating cost volatility is high, the option has a greater value, that is, to encourage waiting rather than immediately investment operations. Therefore, there is a higher waiting incentive in this case, and investment will have greater value until the uncertainty is reduced, or the investment cost can be kept low.

The mathematical model of the real option applied in the P2G project in this paper is different from the traditional real option in terms of the price of the output product as the uncertainty variable, it is modeled by the cost as the uncertainty variable, and the valuation of optimal investment capacity suitable for the optimal production cost is also considered. The model proposed in this work can be used to determine the optimal investment timing and optimal investment capacity of the P2G device under different electricity price fluctuation rates, different investment costs, and sales prices of different output products. The mathematical model based on the real option theory established above can be adjusted to apply in physical assets that have high uncertainty in production

cost and relatively stable output price which will have broad applicability.

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