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# An Improved IPM for Life Estimation of XLPE Under DC Stress Accounting for Space-Charge Effects

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**ABSTRACT** Inverse power model (IPM) is often used in the engineering field to estimate the electrical life of cross-linked polyethylene (XLPE) cable insulation and describe the relationship between applied voltage and insulation failure time. The voltage tolerance index *n* in IPM is also used as an important factor to select appropriate AC cable thickness and pre-evaluation test voltage. However, under the influence of DC electric field, space charge accumulation changes the internal field strength of XLPE. As a result, the actual electric field strength is quite different from the applied value. Hence, the existing IPM model exhibits a large error in evaluating the electrical life of DC cables. In this paper, an improved IPM is proposed. The correction parameters  $\alpha$  and  $\beta$  are introduced into the cumulative loss parameter *C* and voltage tolerance index *n* of the existing IPM to quantify the effect of space charge on distorting the electric field in electrical insulation life. Correlation between applied field strength (*E<sub>a</sub>*), maximum endurance field strength (*E<sub>rm</sub>*) and insulation failure time *t* of several XLPE with different thicknesses is obtained from DC voltage withstand test and pulsed electro acoustic test. In addition, the validity of the improved IPM is preliminarily verified.  $\alpha$  and  $\beta$  predicted by using the space charge characteristic parameter matrix [**P**] is proposed to efficiently obtain the actual parameters. According to experimental analysis, the improved IPM with a certain thickness is predicted by using the neural network fitting method.

**INDEX TERMS** Cross-linked polyethylene, space charge, inverse power model, voltage tolerance index, pulsed electro acoustic.

### I. INTRODUCTION

Cross-linked polyethylene (XLPE) is the most widely used insulating material in power cables. For HVAC cable, this material has abundant operation experience, and its design method has matured [1], [2]. However, the research and development of HVDC power cable lags far behind those of HVAC cable, and most of the designs refer to the calculation methods of parameters under AC working conditions. Under DC stress, the insulation characteristic of DC cable is essentially different from that of AC cable due the characteristic relationship between resistance coefficient, temperature and electric field distortion caused by space charge accumulation in XLPE insulation [3]–[5].

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The life model of XLPE under electric stress is an important factor for cable insulation design. The inverse power model (IPM)  $t = CE^{-n}$  is often used to describe the relationship between applied electric field (*E*) and failure time (*t*) of XLPE samples under an applied electric field. The power exponent *n* in the model is defined as the material voltage tolerance index and is an important basis for setting the insulation thickness and pre-qualification test voltage level during AC cable design. Therefore, XLPE may exhibit distinct lifetime characteristics due to the difference of space charge accumulation characteristics even under the same applied DC electric field.

The effect of space charge on the lifetime of XLPE under DC electric field has been widely studied [6], [7]. Various physical models i.e., Bulk, field limiting space charge (FLSC) and DMM are proposed to determine the effect of space charge accumulation on the lifetime of materials. Among them, the Bulk model constructs the correlation between space charge distortion field strength and material activation energy and calculates the insulation life of the material under electrical and thermal stresses by using the activation energy. The FLSC model introduces the threshold field strength to establish the relationship between space charge, dielectric breakdown, and insulation life [8]. The DMM model uses charge dynamics method to analyze the effect of local stress enhancement caused by charge accumulation on insulation deterioration [9]. However, this model is complex to construct. Up to eight hypotheses are proposed and more than 10 physical parameters are introduced. Compared with that in the phenomenological model IPM, each parameter in the physical model has a clear physical meaning. The physical model quantitatively describes the influence of various factors on insulation life according to material performance deterioration. However, many factors affect material deterioration, and physical models are often complex and have limited use. In addition, this model is only applicable for theoretical research but difficult to implement for engineering applications [10]-[12]. Considering the distorted effect of space charge accumulation on the internal field strength of XLPE under DC electric field, this paper proposes an electrical life model that reflects the effect of space charge on the electrical life of XLPE. The proposed model also has a simple form and is applicable to insulation life estimation.

## II. EFFECT OF SPACE CHARGE ACCUMULATION ON THE BREAKDOWN STRENGTH OF XLPE INSULATION

Short-term breakdown tests were conducted for XLPE samples with different thicknesses to study the correlation between space charge characteristics and breakdown strength of XLPE. The space charge characteristics of each sample were measured by pulsed electro acoustic (PEA) method.

The raw material of XLPE, namely, the product model LS4258DCE, used for DC cable production, was supplied by BOREALIS Company (Austria). Thin circular sheets with thickness of 50–170  $\mu$ m and diameter of 50 mm were prepared by hot pressing. AC and DC short-time breakdown tests were performed according to ASTM-149 standard [13]. The voltage increment rate was 1 kV/s, and more than 10 samples were tested at each point.

Two groups of samples labeled group A and B were prepared by two operators using the same preparation process to avoid the influence of sample difference on test results.

The test results in Fig. 1 indicate that with the increase in thickness d, the AC breakdown strength  $E_{b-ac}$  decreases continuously, whereas the DC breakdown strength  $E_{b-dc}$ increases first and then decreases. The  $E_{b-dc}$  of 100  $\mu$ m sample is approximately 1.3 times of that of 60  $\mu$ m sample. Some differences were found in the results of group A and group B, possibly due to the sample preparation of different operators. However, the variation rule of breakdown strength with thickness is consistent.



**FIGURE 1.** Variation of breakdown strength  $E_b$  with thickness d under (a) AC and (b) DC electric fields.

According to the "volume effect" of solid dielectrics, the breakdown strength of XLPE is strongly dependent to thickness and normally decrease with the increasing thickness. Breakdown always occurs at the weak points of the dielectric material that are caused by local defects. The increasing volume of material caused by increase in thickness or area will increase the probability of local defects occurrence but reduce the breakdown strength. This volume effect has been widely observed and recognized through the breakdown characteristics of various insulating materials, both under AC and DC [14]–[16].

In this study, the volume effect is valid for all film samples under AC. Hence, the  $E_{b-ac}$  decreases with increasing film thickness. However, the volume effect is not dominant for all thicknesses in the case of DC. The  $E_{b-dc}$  increases with the increasing thickness in the range of  $d < 100 \ \mu$ m but decreases in the range of  $d > 100 \ \mu$ m.

Similar phenomena were previously observed. Riechert *et al.* [17] investigated the DC breakdown characteristic of XLPE. Although the author claimed that insulation thickness between 50 and 200  $\mu$ m did not substantially influence the short-term electrical strength of XLPE, experimental



FIGURE 2. Space charge characteristic test platform.

results proved that the  $E_{b-dc}$  increased first, then decreased, and approached its maximum value at  $d = 160 \ \mu m$ . This value was approximately 105% of that at  $d = 100 \ \mu m$ . Khazaka et al. [18] investigated the parylene F (PA-F) film. The DC breakdown strength increased with the increasing thicknesses from 1.4  $\mu$ m to 5  $\mu$ m followed by a decrease for high thicknesses. Wang [19] studied the thickness dependence of the breakdown characteristics of polyester film for AC and DC. The results indicated that  $E_{b-dc}$  increased from 402.5 kV/mm at  $d = 40 \ \mu m$  to 417.5 kV/mm at  $d = 50 \ \mu m$ and then decreased to 318.2 kV/mm at  $d = 110 \ \mu$ m. The  $E_{h-ac}$  continued to decline with the increase in thickness. Li et al. [20] studied the breakdown characteristics of oilimpregnated insulation paper (OIIP) under AC, DC and pulsating DC voltages. The results revealed that breakdown strength decreased with the increasing thickness in the thickness range of 50  $\mu$ m to 200  $\mu$ m under AC. However, this parameter slightly increased with the increasing thickness of OIIPs under pulsating DC voltages (ripple factor of pulsating voltages = 1, 1/3 and strongly increased under DC voltages. The breakdown strength of 130.58 kV/mm at 50  $\mu$ m thickness remarkably increased to 161.76 kV/mm at 200  $\mu$ m.

Most reports only provided experimental results and revealed the difference in the thickness dependence of breakdown strength under AC and DC. Only a few investigated the reason and mechanism behind this phenomenon. Some scholars ascribed the increase in  $E_{b-dc}$  to the increase of crystallinity and the absence of spherulites within the sample film [18] or to the low free volume or electron mean free path in the thin film [21]. However, these analyses were only hypothesis and conjectures and have not been fully tested.

Nevertheless, one thing is certain that, in addition to volume effect, other factors may play a dominant role in DC breakdown, especially for thin samples and high electric fields. In this study, we assume that the distortion of electrical field caused by space charge accumulation contributes to this phenomenon.

For experimental verification, the space charge characteristics of XLPE samples were measured by PEA experiment. The composition of the test circuit is shown in Fig. 2. According to JB/T 12927-2016 standard for measuring space charge distribution in solid insulating materials [22], if the *x*-axis denotes the thickness direction of the sheet sample, then



**FIGURE 3.** Variation of maximum field strength in samples with different thicknesses.

the charge density along the thickness direction at voltage applying time *t* is  $\rho(x, t)$ . The actual electric field strength inside the sample,  $E_r(x, t)$ , can be determined by Poisson equation according to (1).

$$E_r(x,t) = \frac{1}{\varepsilon_0 \varepsilon_r} \int \rho(x,t) dx \tag{1}$$

where  $\varepsilon_0$  and  $\varepsilon_r$  are the vacuum dielectric constant and relative dielectric constant of the sample respectively.

Given that insulation failure is mainly attributed to the maximum electric field inside the sample,  $E_{r-max}$  is defined as the maximum of  $E_r(x, t_i)$  that is actually experienced by the sample at  $t_i$ , and Fig. 3 shows the relationship between  $E_{r-max}$  and d. The results of  $t_i = 5$ , 400, 900 s, and  $E_a = 10$ , 40, 60 kV/mm are presented to illustrate the influence of t and  $E_a$  on the relationship between  $E_{r-max}$  and d. When d increases,  $E_{r-max}$  decreases first and then increases. This tendency is observed at each value of t and  $E_a$ .

The space charge distorts the field strength inside the sample, making the actual value stronger than the applied one. The degree of distortion increases with the applied field strength. In the range of  $d = 50 - 100 \ \mu m$ , the  $E_{r-max}$ decreases with the increase in d. This finding indicates that the distortion of the field strength caused by space charge accumulation is weakened within this thickness range. This phenomenon occurs mainly because the injection of homogeneous space charge weakens the applied electric field strength and thus suppresses the injection of space charge. Moreover, the short-term breakdown strength of XLPE increases with the thickness.  $E_{r-max}$  increases slightly with d in the range of  $d > 100 \ \mu\text{m}$ . This result indicates that the effect of space charge accumulation on the field strength distortion is enhanced in this thickness range. This phenomenon mainly occurs because the increase in the thickness of the XLPE enhances the number of traps in bulk due to increase in amorphous regions in thicker samples, which leads to enhancement of the space charge accumulation and the increase



FIGURE 4. Charge density distribution with various thicknesses.

of  $E_{r-max}$ . As a result, the breakdown strength of XLPE decreases with *d* in range of  $d > 100 \,\mu$ m.

 $E_{r-max}$  is affected by space charge accumulation at various thicknesses. This phenomenon can also be explained by the space charge distribution curve. Fig. 4 shows the charge density distribution of the samples with different thicknesses of 60, 80, 100, 120, and 150  $\mu$ m. The distribution curve for every sample was measured under an applied electric field of 40 kV/mm at 400 s.

It can be seen from Fig. 4, in the range of  $d = 50-100 \,\mu$ m, the space charge accumulation of 60  $\mu$ m XLPE near the two electrodes is stronger than that of 80 and 100  $\mu$ m XLPE. This finding indicates the decreasing trend of  $E_r(x, t)$  in this thickness range. Similarly,  $E_{r-max}$  should have the same decrease trend. The minimum amount of charge accumulation near the electrode of the 100  $\mu$ m XLPE corresponds to the minimum  $E_{r-max}$ , which is consistent with the result in Fig. 3. In the range of  $d > 100 \,\mu$ m and near the two electrodes, 120  $\mu$ m XLPE accumulates more charge than 100 and 150  $\mu$ m XLPE. As shown in Fig. 3, the  $E_{r-max}$  of 120  $\mu$ m XLPE is higher than that of 100 and 150  $\mu$ m XLPE. In summary,  $E_{r-max}$ increases slightly with thickness in the range of  $d > 100 \,\mu$ m.

The variation in thickness shows the relationship between space charge accumulation and DC breakdown strength. The electric field distortion caused by space charge accumulation is closely related to the DC breakdown strength of XLPE.

## III. IMPROVED IPM ELECTRICAL LIFE MODEL WITH REGARD TO SPACE CHARGE EFFECTS

#### A. PROPOSED IMPROVED IPM

The inverse power model shown in (2) is often used as the electrical life model of XLPE.

$$t = CE^{-n} \tag{2}$$

where E is the electric field strength in kV/mm, t is the failure time or life in s. C is a constant representing the cumulative electrical damage required for material failure, and n is the voltage tolerance index representing the degree of influence



FIGURE 5. IPM life curve with regard to space charge distortion effect.



FIGURE 6. Internal electric field formed by space charge accumulation.

of electric field change on insulation life. The failure times  $t_1$ ,  $t_2$ , and  $t_3$  were recorded under at least three different applied field strengths  $E_{a1}$ ,  $E_{a2}$ , and  $E_{a3}$ . A line was drawn on the logarithmic coordinates of *lnt-lnE*, and the values of *n* and *C* were fitted as shown in line *a* in Fig. 5.

With regard to the field distortion effect caused by space charge, the actual field strength  $E_r$  is not equal to the applied field strength  $E_a$  but is determined by  $E_a$  and the field strength  $E_{sc}$  formed by the space charge inside the insulation. This finding satisfies (3) as shown in Fig. 6.

$$E_r = E_a + E_{sc} \tag{3}$$

Actually, the IPM of the samples should be a straight line *b* as shown in the Fig. 5. Space charge distorts the actual field strength  $(E_r)$  inside the sample. Moreover, line *a*  $(E_a$ -*t* curve) shifts and rotates on the basis of line *b*  $(E_r$ -*t* curve). Correction parameters  $\alpha$  and  $\beta$  can be added into the IPM of (2) as shown in (4) to describe the correlation between the two curves.

$$\mathbf{t} = C_r^{\alpha} E_r^{-\beta n_r} \tag{4}$$

which can be expressed as:

$$\ln t = \alpha \ln C_r - \beta n_r \ln E_r \tag{5}$$

where  $\alpha$ ,  $\beta$  are defined as shifting and rotation factor, respectively; and  $E_a$ -t curve represents double logarithmic coordinate system that can be obtained by multiplying the intercept and slope of  $E_r$ -t curve by  $\alpha$ ,  $\beta$  that is equivalent to the shift and rotation of  $E_r$ -t curve up and down, respectively. The difference between  $E_r$  and  $E_a$  is mainly caused by the field distortion due to the space charge accumulation. Hence, the values of  $\alpha$  and  $\beta$  are closely related to the space charge characteristics of the sample.

## B. ACQUISITION OF IMPROVED IPM MODEL PARAMETERS

1) ACQUISITION OF  $E_a - t$  AND  $E_{rm} - t$  CURVES

To obtain the parameters of the improved IPM proposed above, we proposed the following hypotheses:

- Under a uniform applied electric field  $(E_a)$ , the failure of XLPE sample depends mainly on the maximum of  $E_r$  inside the XLPE, namely,  $E_{r-max}$ .
- The relationship between  $E_r$  and failure time t satisfies the inverse power function shown in (6). At an evaluated temperature, the voltage tolerance index  $(n_r)$  and cumulative loss parameter  $(C_r)$  in the formula are constant and are only related to the physical and chemical properties of XLPE itself. Both constants have no relationship with the size of the sample.  $E_r$ -t curve is defined as the intrinsic life curve (ILC) of XLPE.

$$t = C_r E_r^{-n_r} \tag{6}$$

• The difference in  $E_a$  leads to the variation of space charge accumulation and field strength distortion at various degrees. The value of actual field strength  $E_r(x, t)$ inside XLPE is determined by  $E_a$  and the distribution characteristics of space charge e.g.,  $\rho(x, t)$ .

The above hypothesis states that although thickness does not affect the  $E_r$ -t curve of XLPE, it will change the space charge density  $\rho(x, t)$  in XLPE. Under the same applied field strength ( $E_a$ ), the actual field strength ( $E_r$ ) in the sample is quite different. Hence, the breakdown strength  $E_a$  and corresponding  $E_a$ -t curves at different thickness are also varying. Therefore, this hypothesis does not contradict the volume effect of solid dielectrics. Here we can define  $E_a$ -t curve as the apparent life curve (ALC) of XLPE.

XLPE samples with thicknesses of 60, 70, and 80  $\mu$ m were prepared for voltage withstanding tests at  $E_a$  of 180, 200, and 220 kV/mm to verify the above hypothesis. The setup in Fig. 2 was used to simultaneously launch voltage withstand and space charge tests. Space charge density  $\rho(x, t)$  was recorded at intervals of 60 s until sample breakdown. The corresponding  $E_r(x, t)$  was calculated according to (1). Fig.7 shows the variation of  $E_r(x)$  along the thickness direction at different voltage applying time. For brevity, only the result of 60 $\mu$ m sample at  $E_a$  of 180kV/mm was presented.  $E_{r-max}$  appears in the middle of the sample and is greater than the applied field strength  $E_a$ .  $E_{r-max}$  increases gradually over the first 420 s and then becomes relatively stable. In this case, the stable  $E_{r-max}$  in sample is 17% greater than that applied strength,  $E_a = 180$  kV/mm.

Fig. 8 shows the variation of  $E_{r-max}$  with endurance time of DC field, where  $t_b$  is the corresponding failure time in s. For brevity, only the result of 60  $\mu$ m sample was presented.  $E_{r-max}$  first increases with endurance time, then reaches a stable value, and fluctuates slightly up or down the value. Owing to  $E_{r-max}$  fluctuation over time, its root -mean -square (RMS) was used to calculate the relationship between  $E_r$  and



**FIGURE 7.** Distribution of  $E_r$  along the thickness direction at different voltage applying time.

failure time as shown in (7).

$$E_{rm} = \sqrt{\sum_{i=1}^{N} E_{r-\max}^2(t_i)/N}$$
 (7)

where  $t_i$  is the sampling point (at intervals of 60 s) and N is the total sampling times during the whole endurance test, until breakdown.

Considering the statistical characteristics of XLPE failure time, four to five life tests were conducted under each value of applied field strength  $E_a$ , where  $t_b$  is in s and  $E_{rm}$  is in kV/mm. The results are shown in Table 1.



**FIGURE 8.** Variation of  $E_{r-max}$  with endurance time of DC.

 TABLE 1. Parameter t<sub>b</sub> and E<sub>rm</sub> under different E<sub>a</sub> values.

$E_a$	180 kV/mm		200 kV/mm		220 kV/mm	
	$t_b$	$E_{rm}$	$t_b$	$E_{rm}$	$t_b$	$E_{rm}$
	14585	216.2	5740	249.9	1920	280.3
	12700	210.8	6960	239.9	2565	285.5
	16960	221.9	7500	245.1	4380	299.3
	18450	209.8	9480	235.7	7020	288.6
	_	—	10100	240.6	_	_

The data in Table 1 obey the two-parameter Weibull distribution model which is used to analyze the parameters  $t_b$  and  $E_{rm}$ . Furthermore, the parameters with a failure probability of 63.2% were obtained and are shown in Table 2.

Weibull statistical data in Table 2 can be plotted in a double logarithmic coordinate system as the ordinate and abscissa in the life curve (*lnt-lnE*) as shown in Fig. 9.

#### **TABLE 2.** Weibull statistics of parameters t<sub>b</sub> and E<sub>rm</sub>.

$E_a$	Weibull statistics			
180	$t_b$	16788		
kV/mm	$E_{rm}$	217.5		
200	$t_b$	9461.2		
kV/mm	$E_{rm}$	244.9		
220	$t_b$	5280		
kV/mm	$E_{rm}$	292.4		



FIGURE 9. Life curves of samples with different thicknesses.

Fig. 9 shows that among the samples with three different thicknesses, the ALC, which is the  $E_a$ -t curves, satisfies the IPM. The parameters of the model vary with the thickness of the samples. The parameters n and C increase with the thickness of the samples. However, the  $E_{rm}$ -t data corresponding to the three thickness samples can be fitted by one straight line (namely ILC) in the double logarithmic coordinate system. This finding indicates that the change of thickness does not affect the parameters of IPM obtained from ILC. In addition, experimental results validate the hypothesis that the relationship between  $E_r$  and failure time satisfies the inverse power function as shown in (6). At a certain temperature, the  $n_r$  and  $C_r$  in this equation are constant, are only related to the physical and chemical properties of the sample itself and are independent of the sample size.

2) CALCULATIONS OF CORRECTION PARAMETERS  $\alpha$  AND  $\beta$ Table 3 gives the improved IPM parameters.  $n_1 - n_3$  AND  $C_1-C_3$ , for three different thickness samples were determined by ALC.  $n_r$ , and  $C_r$  were determined by ILC.

According to the improved IPM proposed in (4), the parameters of shifting factor ( $\alpha$ ) and rotation factor ( $\beta$ ) can be calculated based on the correlation of  $n_i$ ,  $C_i$ , and  $n_r$ ,  $C_r$ , which are listed in Table 3. For the 60  $\mu$ m sample, its ALC parameter,  $C_1$ , can be obtained by taking exponent 1.092 from the ILC parameter,  $C_r = 5.92 \times 10^{15}$ , and  $n_1$ can be obtained by multiplying  $n_r = 4.89$  with 1.178. This value is equivalent to rotating the ILC at a certain angle and

#### TABLE 3. Improved IPM parameters.

d(µm)	n			С	α	β
-	n <sub>r</sub>	4.89	$C_{\mathrm{r}}$	$5.92 \times 10^{15}$	1	1
60	$n_1$	5.76	$C_1$	$1.65 \times 10^{17}$	1.092	1.178
70	$n_2$	6.49	$C_2$	$1.22 \times 10^{19}$	1.210	1.327
80	$n_3$	7.20	$C_3$	$8.20 \times 10^{20}$	1.326	1.472

translating it downward for a certain distance in logarithmic coordinates.

## IV. A METHOD OF OBTAINING IMPROVED IPM PARAMETERS BASED ON SPACE CHARGE CHARACTERISTICS

According to the above analysis, the ALC of a sample with different thicknesses can be obtained when the parameters of ILC are known. This method can also be used to describe the failure time of the sample under different applied field strengths.

In Section III, the parameters of the improved IPM,  $\alpha$ ,  $\beta$ ,  $C_r$  and  $n_r$ , were obtained. For practical application, the above methods have a heavy workload. For the improved IPM, its parameters are mainly caused by the difference between the applied field strength ( $E_a$ ) and the actual field strength ( $E_{r-max}$ ) due to space charge accumulation. Therefore, the space charge characteristics parameters are considered as closely related to  $\alpha$ ,  $\beta$ ,  $C_r$  and  $n_r$ . If the parameter **P** describing the space charge characteristics of the XLPE is used to quantitatively calculate  $\alpha$ ,  $\beta$ ,  $C_r$  and  $n_r$ , then the ALC of the sample can be obtained conveniently and efficiently.

## A. SELECTION OF SPACE CHARGE CHARACTERISTIC PARAMETER MATRIX [P]

Many parameters, including time- and field-varying ones, describe the characteristics of space charge. Montanari and Fabiani [23], [24] used space charge measurements and accelerated life tests to evaluate the performance of cable insulation under DC stress. By referring to the space charge parameters proposed by G. C. Montanari, this paper adopts the matrix  $[P] = [P_1, P_2, ..., P_k]$  to represent the space charge behavior of XLPE. Each parameter is defined as follows:

• Maximum field strength distortion rate  $(k_{max})$ 

The ratio of maximum field strength  $E_{r-max}$  to applied field strength  $(E_a)$  is defined as field strength distortion rate  $k = E_{r-max}/E_a$ . The maximum value of k in a certain pressure period is counted as parameter  $k_{max}$ .

• Mean field strength distortion rate (*k<sub>mean</sub>*)

Similarly, the average value of k in a certain pressure period is counted as the parameter  $k_{mean}$ .

• Average bulk density of space charge (Q)

If the charge density at time  $t_i$  is  $\rho(x, t)$ , then the average bulk density of the space charge can be calculated by (8) [22].

$$Q = \left(\sum_{i=1}^{N} \frac{1}{x_1 - x_0} \int_{x_0}^{x_1} |\rho(x, t_i)| dx\right) / N$$
(8)

where  $x_0$  and  $x_1$  are the positions of the electrodes,  $t_i$  represents the *i* test times within a certain pressure period, and N represents the total test times of space charge characteristics during the pressure period.

• Space charge accumulation rate (*b*)

When different  $E_a$  values are applied to the sample, the average bulk density Q increases with  $E_a$ . According to space charge limiting current theory, Q has different increasing rates corresponding to different applied field strength ranges. Q increases linearly with  $E_a$  in the space charge limited current region. The rate of space charge accumulation can be expressed by the slope b of Q growth curve [25].

Sample thickness d and applied field strength  $E_a$  can also be included in the parameter matrix [P] as two auxiliary parameters.

In conclusion, the parameters of space charge characteristics can be expressed by parameter matrix as follows:

$$[P] = [d, E_a, k_{\max}, k_{mean}, \mathbf{Q}, b]$$
(9)

According to Figs. 7 and 8,  $E_{r-max}$  takes approximately 400 s to stabilize after pressure. Therefore, in this part of PEA test, the sampling interval was set to 5 s, and the sample was continuously pressurized for 900 s. The test data between 400 s and 900 s were used to calculate the parameters  $k_{max}$ ,  $k_{mean}$ , Q and b. For the XLPE with three thicknesses of 60, 70, and 80  $\mu$ m, the data were extracted from Part III section B. PEA tests were conducted under five different applied field strengths of 80, 100, 120, 140, and 160 kV/mm, and space charge characteristic parameters were extracted to form matrix [**P**]. The results are shown in Table 4.

## B. ESTABLISHMENT OF THE RELATIONSHIP BETWEEN [P] AND $\alpha$ & $\beta$

In this part, the correction parameters  $\alpha$  and  $\beta$  of IPM were predicted by matrix [**P**]. When this function is realized, only the space charge characteristics of the sample can be tested, and the lifetime model parameters *n* and *C* can be calculated or predicted without tedious and time-consuming electrical lifetime tests. In this study, BP neural network fitting method was used to calculate the IPM correction parameters of samples with the space charge parameter matrix [**P**] as the input and [ $\alpha$ ,  $\beta$ ] as the output. A multi-layer feedforward neural network, which is based on error back propagation algorithm and has strong non-linear mapping ability, was selected. The number of nodes in the input, output and hidden layer are 6, 2, and 15, respectively. Fig. 10 shows the structure of the neural network.

First, we used teaching samples to train the network parameters. In the teaching samples, the parameters of

No.#	d (µm)	$E_a$ (kV/mm)	$k_{max}$	k <sub>mean</sub>	Q ( <i>C/m</i> <sup>3</sup> )	b
1	60	80	1.453	1.431	56.95	
2	60	100	1.540	1.511	74.09	
3	60	120	1.883	1.770	113.00	1.307
4	60	140	1.623	1.594	124.26	
5	60	160	1.690	1.664	133.16	
6	70	80	1.288	1.248	45.15	
7	70	100	1.506	1.463	67.06	
8	70	120	1.604	1.565	86.46	1.392
9	70	140	1.480	1.468	100.30	
10	70	160	1.345	1.332	121.19	
11	80	80	1.293	1.259	50.38	
12	80	100	1.262	1.224	57.59	
13	80	120	1.306	1.283	70.76	1.135
14	80	140	1.305	1.284	91.37	
15	80	160	1.248	1.230	108.06	

#### TABLE 4. Parameter matrix.



FIGURE 10. Structure of the neural network.

Train1–Train15 of 15 samples shown in Table 4 are selected as input  $[P]_{train}$ , and the correction coefficient matrix corresponding to each sample in Table 3 are used as output  $[\alpha, \beta]_{train}$ . Levenberg-Marquardt algorithm was used to train the hidden layer neurons, and mean square error was used to evaluate the effect of network training.

Another 20 samples of case 1–case 20 were selected as the test objects to verify the predictive effect of the network after training. The thickness of case 1–case 10 samples is 60  $\mu$ m, that of case 11–case 15 is 70  $\mu$ m, and the remaining samples' thickness is 80  $\mu$ m. The space charge parameter matrix [**P**]<sub>test</sub> of these 20 samples was used as the input of the network, and the IPM correction parameter of the test samples was applied as the output of the network [ $\alpha$ ,  $\beta$ ]<sub>test</sub>. This parameter, was also used to determine its electrical life model parameters.

Fig. 11 shows the comparison between the network prediction value "Netout" and the target value "Target". For the test samples of 60, 70, and 80  $\mu$ m, the prediction errors of parameters  $\alpha$  and  $\beta$  by the neural network are small (standard deviation < 5%), which preliminarily proves the validity of the method.

### **V. DISCUSSION**

Although the above research preliminarily confirms the effectiveness of the improved IPM proposed in this paper,



FIGURE 11. Prediction results of neural network for the correction parameters of test samples.

the neural network obtained in part B of section IV can only accurately predict the IPM model correction parameters of samples with thickness of 60–80  $\mu$ m due to the limited number of teaching samples participating in the training.

ALC and its corresponding space charge characteristic matrix [**P**] of additional samples with wide thickness range must be tested and trained to produce an abundant teaching sample and to improve the prediction ability of the neural network and predict the  $\alpha$  and  $\beta$  of thick samples. Admittedly, this process require a long testing time, especially through the use of constant DC withstand voltage method to obtain electrical life data.

The PEA test was used for the voltage withstand test on the thin sample to confirm the relationship between the distortion field caused by space charge and the apparent lifetime curve  $E_{a}$ -t of XLPE. This examination aims to obtain the  $E_{a}$ -t curve and the real field strength inside the dielectric material by measuring the space charge characteristics to consequently obtain the intrinsic life curve  $E_{r}$ -t. However, apply this method is not feasible to predict the life model parameters of thick samples and real cable insulation. The DC power supply of PEA space charge test platform is not designed for high voltage withstand test, and the maximum DC voltage output of this platform usually does not exceed 20 kV. The electrical life test is difficult to actualize with sample breakdown as the end of life for thick samples. Moreover, the frequent breakdown of test samples on PEA test platform will greatly damage the performance of the platform. This reason also explains why teaching sample data with thickness greater than 80  $\mu$ m were not obtained in this paper.

Given the importance of  $E_r$ -t curve for the determination of  $\alpha$  and  $\beta$ , this parameter requires simultaneous voltage withstand and space charge characteristic tests, which cannot be well achieved by current testing methods. So, how to apply this method to the lifetime model of real cables? As shown in Fig. 9, since  $E_r$ -t can be obtained from the apparent lifetime curve  $E_a$ -t of the sample with different thickness ( $d_1$ ,  $d_2$ ,  $d_3$  $\dots d_n$ ) by combining the shifting factor  $[\alpha_1, \alpha_2, \alpha_3 \dots \alpha_n]$ and the rotation factor  $[\beta_1, \beta_2, \beta_3...\beta_n]$ , then the  $E_r$ -t of any thickness sample can also be obtained from the  $E_a$ -t of other thickness samples by appropriate  $\alpha$  and  $\beta$  transformations. This finding indicates that instead of necessarily obtaining the  $E_r$ -t lifetime curve of the material, we can select a sample with a specific thickness (e.g. 0.5 mm or 1.0 mm) as the reference sample and measure its apparent life curve  $E_a^{ref}$ -t to replace the  $E_r$ -t mentioned above. Subsequently, we can test the life curve  $E_a^i$ -t of other samples with thickness  $d_i$ and calculate the rotation and shifting factor between the  $E_a^i$ -t and  $E_a^{ref}$ -t curves of the reference sample. We can also examine the space charge parameter matrix of these samples and obtain enough teaching samples based on the method in section IV to train the neural network. When the neural network has reliable prediction ability, we can only test the matrix [P] of the insulation of an unknown cable in practice and use it as the input of the neural network to predict the IPM electrical life model of the real cable. The predictive ability and accuracy of the neural network also depend on the abundance and sufficiency of the teaching samples. In addition, obtaining  $E_a - t$  and then the teaching samples by constant DC withstand voltage method is still time consuming and arduous. Fortunately, step stress test can be used to improve the efficiency of life test by setting reasonable test parameters [26]. We can easily obtain the  $E_a - t$  curve of the real cable insulation as long as the DC power supply meets the test requirements. For the measurement of space charge characteristics, full-scale real cable testing devices are already available [27], [28]. Therefore, the proposed method theoretically has the prospects of engineering application in real cables. That is also the research content we are carrying out.

#### **VI. CONCLUSION**

An improved IPM electrical life model is proposed based on the distortion effect of space charge accumulation on the internal field strength of XLPE insulation to quantify the effect of space charge accumulation on the electrical life characteristics of XLPE samples under DC electric field. In the existing IPM model, the correction coefficients  $\alpha$  and  $\beta$ are introduced to quantify the effect of space charge distortion field on insulation electrical life. The relationship between the intrinsic lifetime curve  $E_r - t$  and the apparent lifetime curve  $E_a - t$  of XLPE samples with different thickness are studied by DC withstand lifetime and space charge characteristic tests, and the rationality of the proposed model is preliminarily verified. Furthermore, correlation calculation and prediction method for correction coefficients  $\alpha$  and  $\beta$  are proposed by using the space charge parameter matrix. The validity of this method is preliminarily validated by using a thin sample ( $d = 60 - 80 \ \mu$ m), and the possible application of this method to real cables is discussed.

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