

Novel Scheme of Reversible Watermarking With a Complementary Embedding Strategy

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ABSTRACT In this paper, a new scheme of reversible watermarking is proposed using a complementary embedding strategy in the spatial domain. The proposed scheme consists of two stages: horizontal direction embedding and vertical direction embedding. A complementary embedding strategy is designed to increase the embedding capacity and decrease the distortion of the watermarked image in the vertical direction embedding. Specifically, in the horizontal direction, the proposed scheme embeds one secret data bit by increasing values of pixels in even rows and decreasing values of pixels in odd rows by one. In the vertical direction, it embeds another secret data bit by decreasing values of pixels in even rows and increasing values of pixels in odd rows by one. In addition, a histogram shrinkage technique is adopted to prevent overflow and underflow problems. Experimental results demonstrate that the proposed reversible watermarking scheme outperforms state-of-the-art methods in terms of both embedding capacity and watermarked image quality.

INDEX TERMS Complementary embedding strategy, prediction error, reversible watermarking.

I. INTRODUCTION

Reversible watermarking (also called reversible information hiding or reversible data hiding) aims to hide secret data in digital multimedia and can restore the original signal completely: the embedded secret data can be correctly extracted from the watermarked digital multimedia [1]. In recent years, many reversible watermarking algorithms have been presented. For digital images, three major approaches have been proposed: lossless compression [2]–[3], difference expansion (DE) [4]–[12], and histogram shifting (HS) [13]–[29].

For compression-based reversible watermarking schemes [2]–[3], the original cover image is first compressed by a lossless compression technique (such as arithmetic coding or run-length coding), and then the compressed image is encoded to hide secret data. Generally, the compression ratio is poor. Hence, the embedding capacity of the schemes based on lossless compression is rather low.

Later, more efficient schemes based on DE have been presented [4]–[12]. In 2003, Tian [4] first proposed a novel reversible watermarking algorithm based on DE. The basic idea of this algorithm is to use the difference of pair pixels

instead of the pixel itself to hide secret data. Tian's scheme offers a higher embedding capacity while keeping a lower distortion compared with the compression-based reversible watermarking schemes [2]–[3]. However, this scheme needs a location map to distinguish which pixel pair is expanded. The generated location map has to be compressed first, and then the compressed location map is embedded into the cover image. Hence, the pure embedding capacity of this scheme is reduced significantly because of the large size of the compressed location map. Afterwards, the DE technique has been improved by researchers. Alattar [5] generalized Tian's scheme using a vector instead of a pixel pair. In this scheme, $n - 1$ secret data bits can be hidden in a vector with n cover pixels. Studies [6]–[9] extended the DE method by reducing the size of the location map. Thodi and Rodriguez [10] improved DE by a prediction error expansion (PEE). Their scheme embedded secret data using each pixel's prediction value instead of the pixel difference. Subsequently, this scheme was improved in various ways: for example, using generalized prediction-error expansion and adaptive embedding [11]–[12] and context embedding [13].

Besides the DE technique, the HS-based reversible watermarking scheme was first proposed by Ni *et al.* [14] in 2006, where the peak point of the cover pixel histogram was used

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to embed the secret data. In this scheme, each pixel value of the original cover image is changed by one at most. Hence, watermarked images have an exceptionally good visual quality. However, the embedding capacity of this scheme is limited. Several schemes have been proposed to improve performance, such as using prediction error [15]–[17], pixel difference [18]–[19], interpolation technique [20]–[22], interpolation error [23], generalized HS [24]–[25], two-dimensional HS [26], pixel-value ordering [27]–[28], multi-predictor sorting [29], combinatorial strategy [30], human visual system characteristics [31], and pixel location [32].

Unlike DE-based and HS-based schemes, Kieu and Chang [33] proposed a novel high-quality reversible watermarking scheme based on multiple embedding strategies in 2009. It includes two phases: horizontal embedding phase and vertical embedding phase. The basic idea of this scheme is to use the pixel odd-even value instead of the pixel difference to embed secret data; here, horizontal and vertical embedding phases are complementary. For the horizontal embedding phase, if the cover pixel is an odd value and the to-be-embedded bit is 0, then this pixel is modified by subtracting one. If the cover pixel is an even value or the to-be-embedded bit is 1, then this pixel is unchanged. For the vertical embedding phase, if the cover pixel is an even value and the to-be-embedded bit is 1, then this pixel is modified by adding one. If the cover pixel is an odd value or the to-be-embedded bit is 0, then this pixel is untouched. Later on, this scheme was improved by Chang and Kieu [34] and Jia *et al.* [35]. All three schemes have a much larger embedding capacity while keeping a low distortion (compared with most previous schemes). However, their pure embedding capacity is rather limited because the size of the location map is very large (even if the location map has been compressed by a lossless compression technique). Hence, this paper presents a new high-fidelity reversible watermarking scheme based on a complementary embedding strategy. In the proposed scheme, the data embedding procedure consists of horizontal direction embedding and vertical direction embedding. Specifically, for the horizontal direction embedding, the prediction value of each pixel is first obtained by computing the average value of its two neighboring pixels, and then the to-be-embedded data bit is embedded into the cover pixel by increasing or decreasing the pixel value by one when the prediction error of the current pixel is 0. Similarly, for the vertical direction embedding, the secret data bit is embedded by decreasing or increasing the pixel value by one. The horizontal and vertical direction embeddings are complementary. This property enables the proposed scheme to obtain a particularly good visual quality of the watermarked image. Moreover, the histogram shrinkage technique is used to prevent overflow and underflow problems. Experimental results demonstrate that the proposed scheme outperforms similar reversible watermarking schemes. The main contributions of this paper are summarized as the following three aspects:

1. We point out that the Kieu *et al.*'s scheme [33], Chang *et al.*' scheme [34] and Jia *et al.*'s scheme [35] cannot embed the secret data into a cover image if the compressed location map needs to be embedded. The reason is that for natural image the number of "1" almost equals to the number of "0" in location map, and lossless compression cannot significantly reduce the size of the original location map.
2. We propose a complementary embedding strategy to embed watermarking signal. The horizontal and vertical direction embedding are complementary. This property enables the proposed scheme to obtain a better visual quality of the watermarked image.
3. We verify its effectiveness by experiments and comparisons with the state of the art.

The rest of this paper is organized as follows. The reversible watermarking scheme based on a complementary embedding method is briefly reviewed in Section 2. The details of the proposed scheme are introduced in Section 3. Experimental results are shown in Section 4. Finally, conclusions are given in Section 5.

II. RELATED WORK

In 2009, Kieu *et al.* [33] proposed a novel high-quality reversible watermarking scheme using multiple embedding strategies. Their scheme can horizontally and vertically embed one secret data bit into one pixel pair of a cover image. Experimental results demonstrate that this scheme achieves a good image quality and ideal embedding capacity. Later, Kieu *et al.*'s work has been improved by Chang and Kieu [34] and Jia *et al.* [35]. Jia *et al.*'s scheme also horizontally and vertically embeds one secret bit into one pixel pair of a cover image. Unlike Kieu *et al.*'s scheme and Jia *et al.*'s scheme, Chang *et al.*'s scheme horizontally and vertically embeds one secret bit into one pixel of a cover image. However, in essence, the embedding procedure used by Jia *et al.* and Chang *et al.* is the same as in Kieu *et al.* Therefore, this section mainly reviews the Kieu *et al.*'s method. More details about the schemes by Jia *et al.* and Chang *et al.* can be found in their papers.

The embedding steps of Kieu *et al.*'s scheme are described as follows.

Step 1: Horizontally scan the original cover image I by a raster scan to group two neighboring pixels $I(i, j)$ and $I(i, j + 1)$ into a pixel pair, where $1 \leq i \leq M$, $1 \leq j \leq N - 1$. If $I(i, j + 1)$ is an odd value, then this pixel pair is defined as a horizontal embeddable pixel pair. The first pixel of each pixel pair always remains unchanged.

Step 2: Create a location map LM_1 sized $M \times (N/2)$ to record the positions of the horizontal embeddable pixel pairs and identify the value of LE_1 , where LE_1 is the number of the horizontal embeddable pixel pairs. Initially, all the elements of LM_1 are set to 0. If the pixel pair is the horizontal embeddable pixel pair, then the corresponding element of LM_1 is set to be 1. Note that location map LM_1 is a binary sequence.

TABLE 1. Results of Kieu et al.'s scheme [33], Chang et al.'s scheme [34], and Jia et al.'s scheme [35].

Schemes	Images	Horizontal direction embedding			Vertical direction embedding		
		L_e	L_m	L_c	L_e	L_m	L_c
[33]	Aerial	65403	131072	131120	82118	131072	123928
	Airplane	65374	131072	131104	82115	131072	123928
	Elaine	66843	131072	131080	81045	131072	124560
	Lena	65732	131072	131112	81648	131072	124532
[34]	Aerial	130518	262144	262184	196746	262144	212496
	Airplane	130490	262144	262168	197119	262144	211904
	Elaine	133498	262144	262128	195329	262144	214720
	Lena	131522	262144	262176	196507	262144	212880
[35]	Aerial	65669	131072	131120	98328	131072	106344
	Airplane	65698	131072	131104	98200	131072	106544
	Elaine	64229	131072	131080	99008	131072	105248
	Lena	65340	131072	131112	98494	131072	106080

Step 3: Losslessly compress LM_1 using arithmetic coding to obtain a compressed location map C_1 whose length is LC_1 .

Step 4: Let B_1 be the first LB_1 bits of B , where $LB_1 = LE_1 - LC_1$.

Step 5: For the first LC_1 pixels in I , when each pixel has been embedded using (1), its least significant bit (LSB) is taken as auxiliary information bit of A_1 and needs to be appended to the end of B_1 . This step will be repeated until all secret bits in B_1 are completely embedded and image X can be obtained.

$$X(i, j + 1) = \begin{cases} I(i, j + 1), & \text{if } b = 1 \text{ and } LM_1 = 1 \\ I(i, j + 1) - 1, & \text{if } b = 0 \text{ and } LM_1 = 1 \end{cases} \quad (1)$$

Step 6: Replace LSB of the first LC_1 image pixels in X by C_1 to obtain image H .

Step 7: As in Steps 1–3, obtain LE_2 and compressed location map C_2 whose length is LC_2 , where LE_2 is the number of the vertical embeddable pixel pairs.

Step 8: Let B_2 be the remaining LC_2 bits of B , where $LB_2 = LE_2 - LC_2$.

Step 9: As in Step 5, for the first LC_2 pixels in H , when each pixel has been embedded using (2), its LSB is taken as auxiliary information bit of A_2 and needs to be appended to the end of B_2 . This step will be repeated until all secret bits in B_2 are completely embedded and image Y can be obtained.

$$Y(i, j + 1) = \begin{cases} H(i, j + 1), & \text{if } b = 0 \text{ and } LM_2 = 1 \\ H(i, j + 1) + 1, & \text{if } b = 1 \text{ and } LM_2 = 1 \end{cases} \quad (2)$$

Step 10: Replace LSB of the first LC_2 pixels in Y by C_2 to obtain the final watermarked image V .

This data embedding procedure has a big problem: although it achieves a high visual quality and hiding capacity in the experiments, this scheme almost cannot embed the secret data into a cover image if the compressed location map needs to be embedded. In fact, for natural images, the number of pixel values with odd values and even values are roughly the same. That is, the number of “1” almost equals to the number of “0” in location maps LM_1 or LM_2 . Consequently, lossless compression cannot significantly reduce the size of the original location map. For schemes by Kieu and Chang [33], Chang and Kieu [34], and Jia *et al.* [35],

location maps LM_1 and LM_2 first need to be compressed using arithmetic coding [36] and then are embedded into the cover image. The performance comparison results of the schemes by Kieu *et al.*, Jia *et al.*, and Chang *et al.* for four standard test images (see Fig. 7) are shown in Table 1. In Table 1, L_e , L_m , and L_c represent the number of embeddable secret data bits, length of the original location map, and length of the compressed location map, respectively.

For schemes by Kieu *et al.*, Jia *et al.*, and Chang *et al.*, Table 1 shows that, if location maps LM_1 and LM_2 are directly sent to the expected receivers, these three schemes can embed ideal secret data. However, if compressed location maps LM_1 and LM_2 need to be embedded into the cover image with the to-be-embedded secret data, these three schemes cannot embed any secret data because L_c is much larger than L_e for all test images.

Taking “Aerial” image as an example, consider the horizontal direction embedding in the Kieu *et al.*'s scheme. Here, the number of embeddable secret data bits, length of the original location map, and length of the compressed location map are 65403, 131072, and 131120, respectively. It can be clearly seen that the number of embeddable secret data bits is much less than the length of the compressed location map. That is, in the horizontal direction, their scheme cannot really embed any secret data into “Aerial” image. Similarly, in the vertical direction, their scheme also cannot really embed any secret data.

III. PROPOSED SCHEME

This section describes image preprocessing, data embedding, and data extraction in the proposed scheme.

A. PREVENT OVERFLOW AND UNDERFLOW PROBLEMS

For the proposed scheme, the pixel values of the original cover image may be increased or decreased by one at most. Hence, for an eight-bit gray-scale cover image, if the pixel value is equal to 0 or 255, then the pixel value of the watermarked image may be outside of [0, 255]. That is, these pixels may cause an overflow or underflow problem after the secret data bit has been embedded. To solve this problem, the histogram shrinkage technique is used. The original cover image is processed as follows.

Step 1: The original cover image I is scanned from left to right and from top to bottom. If the pixel value is equal to 0 or 1, then it is changed to 1 and generates one bit, 1 or 0. That is, if the pixel value is 0, then 1 is added to L . Otherwise, if the pixel value is 1, then 0 is added to L .

Step 2: As in Step 1, if a pixel value is equal to 254 or 255, then it is changed to 254 and generates one bit, 0 or 1. That is, if the pixel value is 254, then 0 is added to R . Otherwise, if the value is 255, then 1 is added to R .

Note that L and R are one-dimensional binary sequences. For most test images, the length of L and R is exceedingly small. Hence, L and R do not require a lossless compression.

Similarly, the original image is restored as follows.

Step 1: Obtain L and R from the extraction bit stream.

Step 2: Recovery image I is scanned from left to right and from top to bottom. If the pixel value of the recovery image is 1 and the extracted auxiliary data bit is 0, then it is restored to 1. If the pixel value is 1 and the extracted auxiliary data bit is 1, then it is modified to 0.

Step 3: As in Step 2, if the pixel value of the recovery image is 254 and the extracted auxiliary data bit is 0, then it is recovered to 254. If the pixel value is 254 and the extracted auxiliary data bit is 1, then it is changed to 255.

For example, in the data embedding procedure, if a pixel $I(i, j)$ equals to 0, then this pixel is changed to 1 and is encoded by “1” in L . Assume that the current prediction error $d(i, j) = 0$, which means that this pixel can embed a secret data bit. If the to-be-embedded secret data bit is above auxiliary information bit $b = 1$, the watermarked pixel $H(i, j) = I(i, j) + 1 = 2$ according to the data embedding method based on histogram shifting. In data extraction and image recovery procedure, the embedded auxiliary information bit $b = 1$ can be extracted correctly, and the recovery pixel is $I(i, j) = H(i, j) - 1 = 1$. Finally, original cover pixel can be restored by $I(i, j) = I(i, j) - 1 = 0$.

B. DATA EMBEDDING PROCEDURE

Assume that I and V with size $M \times N$ represent an eight-bit original gray-scale cover image and its watermarked image, respectively. $I(i, j)$ and $\bar{I}(i, j)$ represent cover pixel value and its predicted value, respectively. The to-be-embedded secret data bits $B = \{b|b \in \{0, 1\}\}$ are a binary sequence.

The data embedding procedure of the proposed scheme is composed of two stages: the horizontal direction embedding and vertical direction embedding. When a secret data bit has to be embedded, the cover image is processed from left to right and from top to bottom, as shown in Fig. 1.

Fig. 2 presents a relationship between cover pixel $I(i, j)$ and its neighboring pixels. In horizontal direction embedding, for each pixel $I(i, j)$, its predicted value $\bar{I}(i, j)$ can be calculated as follows.

$$\bar{I}(i, j) = \begin{cases} \lfloor (H(i, j-1) + I(i, j+1)) / 2 \rfloor, & \text{if } 1 \leq i \leq M \text{ and } 1 < j < N \\ I(i, j+1), & \text{if } 1 \leq i \leq M \text{ and } j = 1 \\ H(i, j-1), & \text{if } 1 \leq i \leq M \text{ and } j = N \end{cases} \quad (3)$$

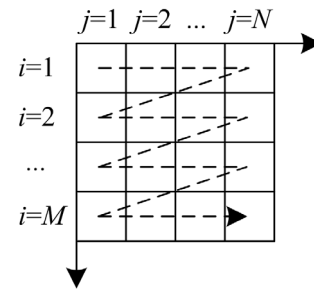


FIGURE 1. Order of the data embedding procedure.

$I(i-1, j-1)$	$I(i-1, j)$	$I(i-1, j+1)$
$I(i, j-1)$	$I(i, j)$	$I(i, j+1)$
$I(i+1, j-1)$	$I(i+1, j)$	$I(i+1, j+1)$

FIGURE 2. Cover pixel $I(i, j)$ and its neighboring pixels.

where $\lfloor \cdot \rfloor$ is the floor function and $H(i, j)$ is an embedded pixel.

After predicted value $\bar{I}(i, j)$ is obtained, prediction error $d_1(i, j)$ between current pixel $I(i, j)$ and its predicted value $\bar{I}(i, j)$ is computed using (4).

$$d_1(i, j) = I(i, j) - \bar{I}(i, j) \quad (4)$$

In the horizontal embedding, the pixel is shifted by (5) and a secret data bit $b \in \{0, 1\}$ is embedded by (6), respectively.

$$H(i, j) = \begin{cases} I(i, j) + 1, & \text{if } d_1(i, j) > 0 \text{ and } \text{mod}(i, 2) = 1 \\ I(i, j) - 1, & \text{if } d_1(i, j) < 0 \text{ and } \text{mod}(i, 2) = 0 \end{cases} \quad (5)$$

$$H(i, j) = \begin{cases} I(i, j) + b, & \text{if } d_1(i, j) = 0 \text{ and } \text{mod}(i, 2) = 1 \\ I(i, j) - b, & \text{if } d_1(i, j) = 0 \text{ and } \text{mod}(i, 2) = 0 \end{cases} \quad (6)$$

In the vertical embedding, for each pixel $H(i, j)$, its predicted value $\bar{H}(i, j)$ can be calculated as follows.

$$\bar{H}(i, j) = \begin{cases} \lfloor (V(i-1, j) + H(i+1, j)) / 2 \rfloor, & \text{if } 1 \leq j \leq N \text{ and } 1 < i < M \\ H(i+1, j), & \text{if } 1 \leq j \leq N \text{ and } i = 1 \\ V(i-1, j), & \text{if } 1 \leq j \leq N \text{ and } i = M \end{cases} \quad (7)$$

where $V(i, j)$ is a new embedded pixel.

After predicted value $\bar{H}(i, j)$ is obtained, prediction error $d_2(i, j)$ between current $H(i, j)$ and its predicted value $\bar{H}(i, j)$ is computed using (8).

$$d_2(i, j) = H(i, j) - \bar{H}(i, j) \quad (8)$$

In the vertical embedding, shift the pixel by (9) and embed another secret data bit $b \in \{0, 1\}$ by (10), respectively.

$$V(i, j) = \begin{cases} H(i, j) - 1, & \text{if } d_2(i, j) < 0 \text{ and } \text{mod}(i, 2) = 1 \\ H(i, j) + 1, & \text{if } d_2(i, j) > 0 \text{ and } \text{mod}(i, 2) = 0 \end{cases} \quad (9)$$

$$V(i, j) = \begin{cases} H(i, j) - b, & \text{if } d_2(i, j) = 0 \text{ and } \text{mod}(i, 2) = 1 \\ H(i, j) + b, & \text{if } d_2(i, j) = 0 \text{ and } \text{mod}(i, 2) = 0 \end{cases} \quad (10)$$

The flowchart of the data embedding procedure of the proposed scheme is shown in Fig. 3. Next, the details are described step by step.

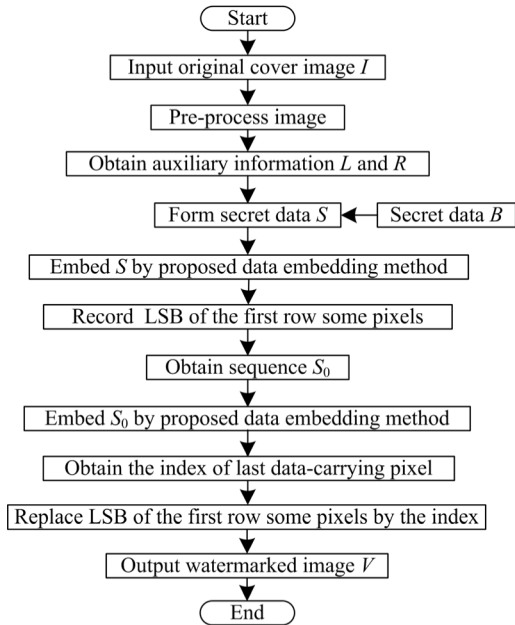


FIGURE 3. Flowchart of data embedding procedure.

Step 1: Preprocess the original cover image I by a raster scan to obtain the auxiliary information $A_1 = L||R$, where the notation “||” represents the concatenation operation. The size of L and R is L_1 and L_2 , respectively. If the original cover image has no pixels with values 0 or 255, then it does not require image preprocessing and the size of auxiliary information A_1 is 0. Hence, we have to use one bit to record whether auxiliary information A_1 exists. That is, the length of auxiliary information A_1 is at least 1. After image preprocessing, embed the secret data bits into the processed image without overflow and underflow problems.

Step 2: Final to-be-embedded secret data bits S are created by $S = F||Len_1||Len_2||L||R||B$, where F (1 bit) is a flag that is used to record whether auxiliary information exists; Len_1 ($\lceil \log_2(L_1 + 1) \rceil$ bits) and Len_2 ($\lceil \log_2(L_2 + 1) \rceil$ bits) represent the size of auxiliary information L and R , and B denotes real embeddable data.

Step 3: Embed the secret data bits into the cover image as follows.

- In the horizontal direction embedding, calculate prediction error $d_1(i, j)$ by (4). The pixel is modified, and the secret data bit is embedded by (5) and (6), respectively.
- In the vertical direction embedding, calculate prediction error $d_2(i, j)$ by (8). The pixel is modified, and the secret data bit is embedded by (9) and (10), respectively.

Step 4: Repeat Step 3 until all secret data bits in S have been embedded.

Step 5: Take the LSBs of the first $\lceil \log_2(M + 1) \rceil + \lceil \log_2(N + 1) \rceil$ watermarked image pixels in the first row to obtain a binary sequence S_0 , where $\lceil \cdot \rceil$ is a ceiling function.

Step 6: As in Step 3, embed binary sequence S_0 defined in Step 5 into the remaining pixels of the cover image, and denote i_{end} and j_{end} as the index of the last data-carrying pixel.

Step 7: Replace the LSB of the first image pixels by auxiliary information A_2 to obtain the final watermarked image, where A_2 is the index of end position i_{end} ($\lceil \log_2(M + 1) \rceil$ bits) and j_{end} ($\lceil \log_2(N + 1) \rceil$ bits).

Here, the procedures of horizontal and vertical embedding are inverse. That is, in the horizontal direction embedding, the proposed scheme increases or decreases pixel values by one. In the vertical direction embedding, it decreases or increases pixel values by one to balance out the embedded secret bits that were produced in the horizontal embedding. Thanks to this inverse property, the proposed scheme has an ideal embedding capacity and a good image quality.

Fig. 4 shows a simple example of the data embedding procedure. Note that auxiliary information is not embedded into the cover image. Assume that the to-be-embedded secret data B is 011010101110. Fig. 4(a) is an original cover image sized $M \times N$, where $M = N = 3$. The pixel $I(1, 1) = 3$ is first processed in the horizontal direction according to the data embedding rule, and its predicted value is calculated as $\bar{I}(1, 1) = H(1, 2) = 3$. Prediction error $d_1(1, 1)$ is obtained by $d_1(1, 1) = I(1, 1) - \bar{I}(1, 1) = 0$, which means that this pixel can embed a secret data bit. Because the first bit of B is 0 and $\text{mod}(1, 2) = 1$, this pixel is modified by $H(1, 1) = I(1, 1) + 0 = 3$. In vertical direction, its predicted value is calculated as $\bar{H}(1, 1) = I(2, 1) = 3$. Prediction error $d_2(1, 1)$ is 0. Because the second bit of B is 1, the final watermarked pixel is obtained by $V(1, 1) = H(1, 1) - 1 = 2$. For the next pixel $I(1, 2) = 3$, in the horizontal direction, its predicted value is computed as $\bar{I}(1, 2) = \lfloor (V(1, 1) + I(1, 3))/2 \rfloor = 3$ and the prediction error $d_1(1, 2)$ is 0. Hence, this pixel is modified by $H(1, 2) = I(1, 2) + 1 = 4$ because the to-be-embedded secret data bit is 1 and $\text{mod}(1, 2) = 1$. In the vertical direction, its predicted value is calculated as $\bar{H}(1, 2) = I(2, 2) = 3$, and prediction error $d_2(1, 2) = 1$, which means that this pixel cannot embed a secret data bit and remains unchanged. Hence, final watermarked pixel $V(1, 2)$ is 4. A similar operation can be performed for the remaining pixels of this image. When all secret data bits in B have been embedded completely, watermarked image V is obtained, as shown in Fig. 4(b). Table 2 presents the detailed data embedding procedure.

C. DATA EXTRACTION PROCEDURE

The data extraction procedure is actually the reverse process of the data embedding procedure. The data extraction procedure of the proposed scheme also includes two stages: the vertical direction extraction and horizontal direction extraction.

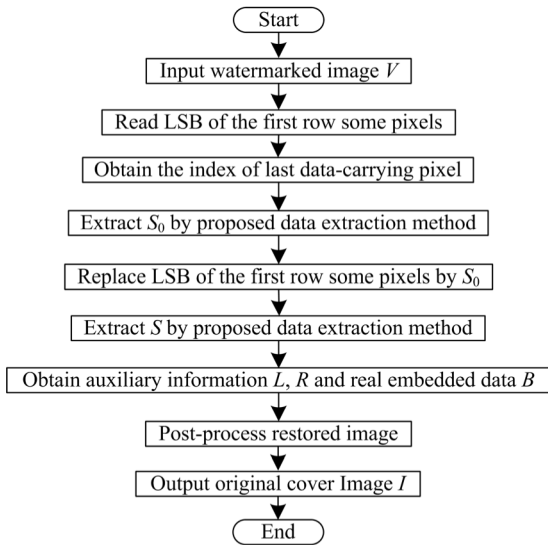


FIGURE 6. Flowchart of the data extraction procedure.

Step 2: Based on indexes i_{end} and j_{end} , extract binary sequence S_0 defined in Step 5 of the data embedding procedure. Meanwhile, do the original cover image restoration. For each pixel $V(i, j)$, the data extraction and image restoration procedures are defined as follows.

- In the vertical direction extraction, calculate its prediction error $d_2(i, j)$ by (12). Next, extract the embedded secret data bits and recover the image using (13) and (14), respectively.
- In the horizontal direction extraction, calculate its prediction error $d_1(i, j)$ by (16). Next, extract the embedded secret data bits and recover the image using (17) and (18), respectively.

Step 3: Repeat Step 2 until sequence S_0 has been extracted.

Step 4: Replace the LSB of the first $\lceil \log_2(M + 1) \rceil + \lceil \log_2(N + 1) \rceil$ image pixels by S_0 extracted in Step 2.

Step 5: As in Step 2, extract the embedded secret data bits from the remaining pixels. Meanwhile, restore those pixels. Finally, embedded secret data S are extracted correctly and a secondary image can be obtained.

Step 6: Extracted secret data S are separated into auxiliary information A_1 and secret data B . If the first bit of A_1 is 1, the original cover image can be recovered exactly from the secondary image without any distortion according to auxiliary information A_1 . If the first bit is 0, it means that the overflow and underflow problems did not occur in the data embedding, and the secondary image is the final recovered original cover image.

The following example illustrates the data extraction and image restoration procedure. Suppose that the input watermarked image is shown in Fig. 4(b). Note that the extraction procedure should be processed first in vertical direction, and then in horizontal direction. For the vertical extraction, pixel $V(3, 3) = 3$ is first processed to predict its predicted value, which is computed as $\bar{V}(3, 3) = V(2, 3) = 1$. Prediction error

$d_2(3, 3)$ is obtained by $d_2(3, 3) = V(3, 3) - \bar{V}(3, 3) = 2$, which means this pixel does not contain the secret data bit and remains unchanged because $d_2(3, 3)$ is larger than 1 and $\text{mod}(3, 2) = 1$. For horizontal direction, its predicted value is obtained by $\bar{H}(3, 3) = V(3, 2) = 3$. Prediction error $d_1(3, 3) = H(3, 3) - \bar{H}(3, 3) = 0$, which means this pixel contains the secret data bit. According to the data extraction and image restoration methods, the embedded secret bit 0 can be extracted and this pixel is unchanged. For the next pixel, $V(3, 2) = 3$, in vertical direction, its predicted value is obtained as $\bar{V}(3, 2) = V(2, 2) = 4$ and the prediction error $d_2(3, 2)$ is -1 , which means this pixel contains the secret data bit. According to the proposed method, the bit 1 is extracted, and this pixel will be modified to 4. In horizontal direction, its predicted value is obtained as $\bar{H}(3, 2) = \lfloor (V(3, 1) + I(3, 3)) / 2 \rfloor = 3$ and the prediction error $d_1(3, 2)$ is 1. The bit 1 is extracted and this pixel will be changed to 3. Similar method can be used for other pixels. Finally, the embedded secret data bits can be extracted correctly and the original cover image I can be restored perfectly, as shown in Fig. 4(a). Table 3 presents the data extraction and image restoration procedure.

IV. EXPERIMENTAL RESULTS

In this section, in order to validate the performance of the proposed scheme in terms of embedding capacity and visual quality of the embedded image, the Matlab language is used to perform experiments with the proposed scheme and six baseline schemes. The experiments are performed in Windows 7, SP1, using Matlab 2010a software running on the AMD Sempron X2 180 Processor, 2.4 GHz CPU, and 2.0 GB RAM. Four 8-bit standard test gray-scale images sized 512×512 (namely, “Aerial”, “Airplane”, “Elaine” and “Lena”) are selected as original cover images, as shown in Fig. 7. All images are obtained from USC SIPI image dataset [37]. The to-be-embedded secret data bits are generated using the random function.

In the experiments, the visual quality of the watermarked image is measured using the peak signal-to-noise ratio (PSNR), which is defined as follows.

$$PSNR = 10 \times \log_{10} \left(\frac{255^2}{MSE} \right) \quad (19)$$

where the mean square error (MSE) is defined as below.

$$MSE = \frac{1}{M \times N} \sum_{i=1}^M \sum_{j=1}^N (I(i, j) - V(i, j))^2 \quad (20)$$

where $I(i, j)$ and $V(i, j)$ are the pixel values of the original cover image and watermarked image. M and N are the width and height of original cover image, respectively.

In addition, the embedding capacity is estimated using the number of secret data bits that can really be embedded into a cover image. That is, the embedding capacity is a pure payload. For the proposed scheme, to ensure the embedded pixel value within the allowable range $[0, 255]$, the auxiliary

TABLE 3. An example of the data extraction and image restoration procedure.

Vertical direction extraction					Horizontal direction extraction				
Location	$V(i, j)$	d_2	b	$H(i, j)$	Location	$H(i, j)$	d_1	b	$I(i, j)$
(3, 3)	3	2	-	3	(3, 3)	3	0	0	3
(3, 2)	3	-1	1	4	(3, 2)	4	1	1	3
(3, 1)	3	1	-	3	(3, 1)	3	0	0	3
(2, 3)	1	-2	-	1	(2, 3)	1	-3	-	2
(2, 2)	4	1	1	3	(2, 2)	3	1	-	3
(2, 1)	2	0	0	2	(2, 1)	2	-1	1	3
(1, 3)	4	2	-	4	(1, 3)	4	0	0	4
(1, 2)	4	1	-	4	(1, 2)	4	1	1	3
(1, 1)	2	-1	1	3	(1, 1)	3	0	0	3

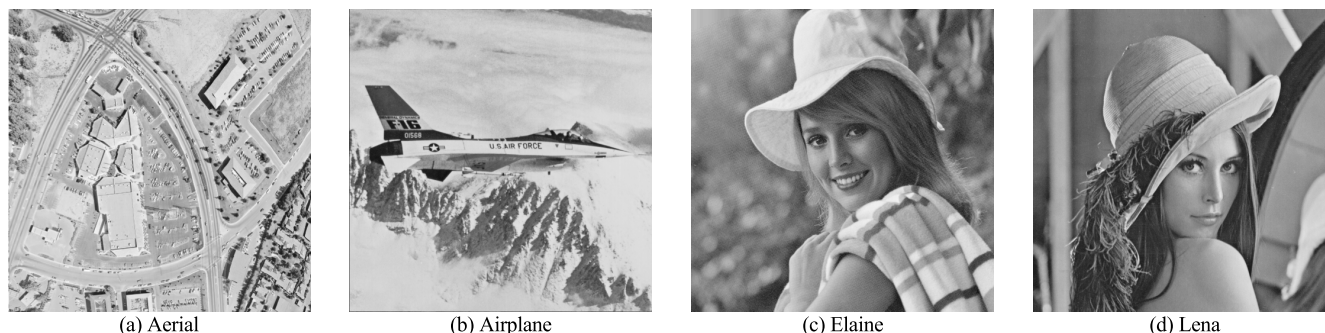


FIGURE 7. Four standard gray-scale test images.

TABLE 4. Performance results of the proposed scheme and other schemes.

Scheme	Metric	Aerial	Airplane	Elaine	Lena	Average
Propose scheme	Payload	58298	82738	33774	58038	58212
	PSNR	49.705	49.7011	49.2102	49.5042	49.5301
Non-complementary	Payload	55948	79710	32658	56372	56172
	PSNR	45.7419	45.716	45.5758	45.5744	45.6520
[9]	Payload	31797	50033	18379	33566	33444
	PSNR	48.4249	48.6026	48.3099	48.4544	48.4480
[15]	Payload	44935	66158	26291	46797	46045
	PSNR	48.5332	48.7332	48.3719	48.5546	48.5482
[16]	Payload	26974	47599	16502	29469	30136
	PSNR	51.1867	51.2398	51.2416	51.3257	51.2485
[17]	Payload	62909	84231	36196	55000	59584
	PSNR	48.6982	48.9207	48.4688	48.6395	48.6818
[18]	Payload	23219	39331	16039	22045	25159
	PSNR	48.3404	48.487	48.2832	48.3345	48.3613
[19]	Payload	43394	71140	30066	42844	46861
	PSNR	48.5109	48.7804	48.4057	48.5195	48.5541

information is needed. Thus, in the following experiments, the auxiliary information bits are excluded from computing embedding capacity.

For a comparison with similar reversible watermarking schemes, the maximum embeddable secret data bits of each scheme are embedded into each test image using schemes by Tai *et al.* [18], Hong *et al.* [15], Lee and Chen [9], Fallahpour [16], Yang and Tsai [17], Li *et al.* [19], and non-complementary scheme. For Tai *et al.*'s scheme [18], the difference of two adjacent pixels is used to embed the secret data. For Hong *et al.*'s scheme [15], the difference between the original pixel and its predicted value obtained by median edge detector is used to embed the secret data. For Lee *et al.*'s

scheme [9], the difference between the original pixel and the average of its neighboring pixels is used to embed the secret data. For Fallahpour's scheme [16], the difference between the original pixel and its predicted value calculated by gradient adjusted predictor is used to embed the secret data. For Li *et al.*'s scheme [19], the difference of two adjacent pixels is computed first and then two peak points are selected to embed the secret data. For Yang *et al.*'s scheme [17], the interleaving predictor is used to predict the pixel value. For non-complementary scheme, the embedding procedure is similar to the proposed scheme, but the embedding rule in vertical and horizontal embedding direction is the same. The performance comparison results are shown in Table 4.

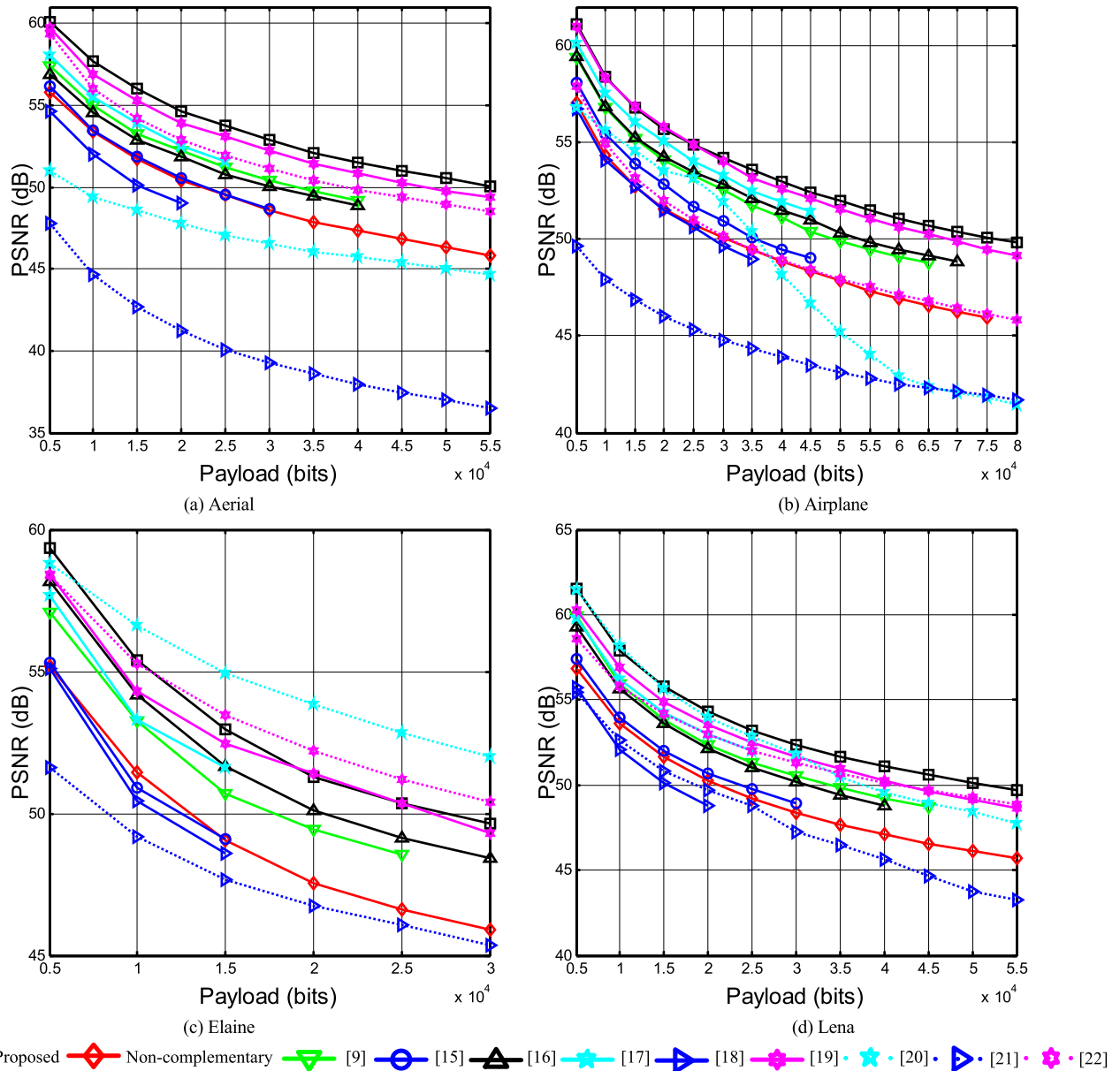


FIGURE 8. Performance comparison of the proposed scheme and other schemes.

From Table 4, it can be clearly seen that the proposed scheme has a better performance in terms of the average PSNR value and pure embedding capacity compared with similar schemes [9, 15, 18–19] and non-complementary scheme. The average pure embedding capacity of the proposed scheme is 58212 bits, which is 28076 bits, 12167 bits, 33054 bits, 11351 bits, 24768 bits, and 2040 bits larger than that of Fallahpour’s scheme [16], Hong et al.’s scheme [15], Tai et al.’s scheme [18], Li et al.’s scheme [19], Lee et al.’s scheme [9], and non-complementary scheme. The average PSNR value of the proposed scheme is 49.5301 dB, which is 0.8483 dB, 0.9819 dB, 1.1689 dB, 0.9760 dB, 1.0822 dB, and 3.8781 dB larger than that of Yang et al.’s scheme [17], Hong et al.’s scheme [15], Tai et al.’s scheme [18], Li et al.’s scheme [19], Lee et al.’s scheme [9] and non-complementary scheme.

It is noted that although the average PSNR value of Fallahpour’s scheme is 51.2485 dB, which is larger than that of the proposed scheme, its average payload is 28076 bits less than that of the proposed scheme. For Yang et al.’s scheme, the embedding capacity is 59584 bits larger than that of the proposed scheme, but its average PSNR value is 48.6818 dB less than that of the proposed scheme.

Fig. 8 shows the performance comparison results of the proposed scheme and other similar schemes which are Yang et al.’s scheme [17], Tai et al.’s scheme [18], Hong et al.’s scheme [15], Lee et al.’s scheme [9], Fallahpour’s scheme [16], Li et al.’s scheme [19], Yang et al.’s scheme [20], Hu et al.’s scheme [21], Wahed et al.’s scheme [22] and non-complementary scheme. For these schemes, we vary the embedding capacity from 5000 bits to

TABLE 5. Performance comparison results of Kodak image data set in terms of PSNR value for [9], [15]–[22] and the proposed scheme with the pure embedding capacity of 20000 bits.

Images	Proposed	[9]	[15]	[16]	[17]	[18]	[19]	[20]	[21]	[22]
kodim01	53.8745	49.7996	51.3780	52.7862	53.1809	50.1608	51.2721	50.3858	42.3703	56.0153
kodim02	56.1054	52.3535	53.7939	54.5318	55.6194	52.3783	54.0755	52.9948	46.9836	58.4495
kodim03	59.1136	56.1139	57.1410	58.5497	59.6009	56.7946	58.8186	50.7278	44.7300	56.5595
kodim04	57.1918	52.7738	54.5147	55.1972	56.0767	51.8361	53.9365	50.5180	41.9879	53.9905
kodim05	56.7201	52.0596	54.1800	54.0324	55.3086	51.2003	53.8940	47.8853	41.5865	57.3390
kodim06	59.9354	57.7963	58.0369	60.2150	60.5976	58.4603	59.8299	46.0502	38.4505	54.5520
kodim07	58.7837	55.3215	56.6866	57.3934	59.1594	55.6547	58.0540	53.1371	47.4874	56.8902
kodim08	53.0701	48.3823	51.2092	51.8771	51.6272	48.7515	50.5958	48.4247	38.9502	54.5835
kodim09	57.1872	53.7254	55.5593	56.0798	57.0522	54.3308	56.8126	56.6413	50.7580	57.2703
kodim10	56.7879	53.1316	55.2754	55.6615	56.1891	53.3393	55.6305	50.7584	44.9601	57.4946
kodim11	59.3271	54.4605	57.3745	57.1513	58.1366	57.0398	59.3782	51.8820	46.8093	58.8445
kodim12	59.0262	54.4931	56.5024	56.4143	58.0098	55.3119	58.2252	49.3984	39.9662	54.0508
kodim13	53.6196	48.3108	50.0920	—	51.3629	48.2744	50.7455	48.4523	39.9364	54.1864
kodim14	56.0184	50.4995	53.5336	52.8428	54.8729	50.8001	53.8578	50.5830	44.0418	57.8767
kodim15	55.9349	52.9663	54.4864	55.4667	55.9894	53.4353	55.0440	50.3288	47.8892	56.1292
kodim16	59.3387	56.3963	57.4990	58.3836	60.0066	57.2386	59.2912	52.0742	48.6720	58.1636
kodim17	58.3758	54.3621	56.2129	56.8209	57.8973	54.9086	57.7328	48.4081	43.4113	58.5436
kodim18	54.5317	50.6140	52.4419	52.7028	53.4713	49.5976	52.3916	52.8637	46.2570	59.1639
kodim19	57.7977	54.6272	56.0811	56.5372	57.9099	54.3470	56.8598	59.4410	57.1470	57.0437
kodim20	55.3322	57.7547	56.4468	57.8644	53.1994	59.4436	52.6949	44.7204	34.9949	51.2037
kodim21	57.3555	54.2413	55.8976	56.5723	57.5698	54.7025	57.2256	54.3289	60.3961	58.4927
kodim22	56.1571	51.5090	54.1739	53.7564	54.2871	50.9320	55.1306	53.8160	49.9046	53.8000
kodim23	58.0532	55.3902	56.5170	57.5548	58.5169	55.0934	57.3709	60.7231	56.6181	57.0741
kodim24	55.9227	53.4533	53.7130	56.0425	53.8893	54.0016	53.5242	47.0231	40.1938	51.6310
Average	56.8983	53.3557	54.9478	55.8450	56.2305	53.6680	55.3484	51.3153	45.3918	56.2229

their maximum with a step size of 5000 bits. From Fig. 8, it is clearly found that the proposed scheme outperforms these schemes [9], [15]–[22] in terms of the PSNR value under the same embedding capacity for most cases. For example, the proposed scheme can improve by 5.6517 dB compared with Tai et al.’s scheme [18], 2.5280 dB compared with Hong et al.’s scheme [15], 4.1258 dB compared with Lee et al.’s scheme [9], 2.8979 dB compared with Li et al.’s scheme [19], 0.6742 dB compared with Li et al.’s scheme [17], 2.1370 dB compared with Fallahpour’s scheme [16], 4.2387 dB compared with non-complementary scheme, 6.6340 dB compared with Yang et al.’s scheme [20], 13.3603 dB compared with Hu et al.’s scheme [21], and 1.6010 dB compared with Wahed et al.’s scheme [22] for the image “Aerial.”

In addition, although the embedding procedure of the non-complementary scheme is similar to the proposed scheme, the proposed scheme has better performance with a same embedding capacity. The reason can be explained as follows. In the horizontal embedding procedure, the proposed scheme embeds the secret data bits by increasing or decreasing the pixel values by one, while in the vertical embedding procedure, the proposed scheme embeds the secret data bits by decreasing or increasing the pixel values by one. Hence, according to the vertical embedding procedure, among the pixel values modified by the horizontal embedding procedure, many have a chance to return to their original pixels value. This means that the horizontal and vertical embedding procedures of the proposed scheme are complementary. This property enables the proposed scheme to obtain a particularly good visual quality of the watermarked image.

The Kodak image data set [38] is selected as test image to further compare the proposed scheme with these nine schemes, which contains 24 color images sized 512×768 or 768×512 . In experiments, all color images are first transformed into gray-scale image, and then embed with 20000 and 30000 secret data bits into each gray-scale image, respectively. Because the size of auxiliary information A_1 is very large for some images (e.g., for image kodim20, the length of A_1 is 90027, for image kodim24, the length of A_1 is 20768, etc.) in Kodak image set, the auxiliary information A_1 is first compressed by arithmetic coding [34] and then is embedded into the cover image with secret data B . Tables 5 and 6 show the performance comparison results. Note that the embedding capacity is pure capacity. The average PSNR value of the proposed scheme is 3.5427 dB, 1.9506 dB, 1.0534 dB, 0.6679 dB, 3.2303 dB, 1.5499 dB, 5.5831 dB, 11.5066 dB, and 0.6755 dB larger than that of Lee et al.’s scheme [9], Hong et al.’s scheme [15], Fallahpour’s scheme [16], Yang et al.’s scheme [17], Tai et al.’s scheme [18], Li et al.’s scheme [19], Yang et al.’s scheme [20], Hu et al.’s scheme [21], and Wahed et al.’s scheme [22], respectively, when the pure embedding capacity is 20000 bits. The average PSNR value of the proposed scheme is 2.8689 dB, 1.9861 dB, 0.7885 dB, 0.6558 dB, 2.8616 dB, 1.3654 dB, 6.1747 dB, 11.0579 dB and 0.6749 dB larger than that of Lee et al.’s scheme [9], Hong et al.’s scheme [15], Fallahpour’s scheme [16], Yang et al.’s scheme [17], Tai et al.’s scheme [18], Li et al.’s scheme [19], Yang et al.’s scheme [20], Hu et al.’s scheme [21], and Wahed et al.’s scheme [22], respectively, when the payload is 30000 bits. These results show that the proposed scheme outperforms nine

TABLE 6. Performance comparison results of Kodak image data set in terms of PSNR value for [9], [15]–[22] and the proposed scheme with the pure embedding capacity of 30000 bits.

Images	Proposed	[9]	[15]	[16]	[17]	[18]	[19]	[20]	[21]	[22]
kodim01	52.2959	—	50.4266	51.2073	51.6321	48.5875	50.3778	47.3665	40.5227	53.3899
kodim02	54.3170	50.8657	52.3653	53.1956	54.1495	50.8720	52.7678	51.2495	45.2383	56.7655
kodim03	57.2181	54.1298	55.1091	56.6645	57.5689	54.6394	56.8184	48.1877	43.4133	54.8446
kodim04	54.9052	51.0863	52.6107	53.5588	54.2580	50.3465	52.3079	48.6195	40.9479	52.2864
kodim05	54.3859	49.9140	52.0451	51.9686	53.4338	49.1237	51.7606	45.6954	39.9903	55.5589
kodim06	58.2658	55.9930	56.2324	58.5470	57.4635	56.7478	58.2100	43.9294	38.1768	52.5960
kodim07	56.8830	53.2429	54.7846	55.2287	57.2452	53.4903	55.9154	50.7966	45.4427	54.7184
kodim08	51.9491	—	49.9693	51.2096	49.9143	48.3205	49.3666	46.7856	37.9303	52.9210
kodim09	55.3468	51.8038	53.6817	54.3293	55.0885	52.1903	54.9489	52.0286	50.3558	54.7022
kodim10	55.0519	51.4149	53.4783	53.9502	54.4459	51.5444	53.9102	48.9295	43.2751	55.7438
kodim11	57.0155	52.4497	54.3926	55.0963	55.8792	53.5448	56.7322	48.6685	45.0744	57.0435
kodim12	56.7206	51.5439	53.8004	53.9889	55.5933	52.3606	55.7170	47.0276	39.7519	52.1662
kodim13	50.7106	—	48.3305	—	49.5127	—	48.5430	46.6910	39.1366	52.4139
kodim14	53.7185	49.1863	51.1071	51.5217	53.0315	49.2509	51.3486	49.2799	42.0084	55.9105
kodim15	54.6280	51.7366	53.1060	54.3064	54.8403	52.0906	53.7393	48.9915	41.5032	54.3856
kodim16	57.5072	54.1787	55.4802	56.2210	57.7042	55.1016	57.4098	50.4266	47.3475	56.3419
kodim17	56.0587	52.1193	53.9419	54.1182	55.5784	52.2809	55.3358	46.0879	43.0160	56.7109
kodim18	52.7248	48.9868	50.5623	—	51.7264	—	50.4577	50.9331	44.2985	57.4373
kodim19	55.9403	52.5382	54.2026	54.2740	55.7769	52.3299	55.0635	52.6711	55.0883	55.7460
kodim20	55.1350	57.7668	55.4947	57.9826	52.9519	58.6097	52.3295	43.9391	34.6423	49.3229
kodim21	55.5335	52.2829	54.0467	54.4882	55.6224	52.6592	55.3512	51.8352	58.3449	56.7221
kodim22	53.8981	49.7114	51.5627	52.2460	52.6712	49.2655	52.2160	50.3458	47.4917	52.0387
kodim23	56.3887	53.4745	54.7149	55.6291	56.5624	53.0857	55.5898	57.1935	54.5841	55.2145
kodim24	54.6610	51.4304	52.1461	54.0749	52.8682	51.7569	52.2730	45.3868	38.2884	50.0820
Average	55.0525	52.1836	53.0663	54.2640	54.3966	52.1909	53.6871	48.8777	43.9946	54.3776

similar state-of-the-art schemes with the same embedding capacity.

V. CONCLUSION

In this paper, a new, simple reversible watermarking scheme based on complementary embedding strategy is proposed for high-fidelity images in spatial domain. To achieve high image quality, the complementary embedding method is used in the vertical direction embedding. The distortion which produced in the horizontal direction embedding can be balanced out in vertical direction embedding. This property enables the proposed scheme to obtain an exceptionally good quality of watermarked image. Experimental results show that the watermarked image quality of the proposed scheme is superior to some similar reversible watermarking schemes under the same embedding capacity. However, at the current stage, the performance of the proposed scheme is not very well. In our future work, we will try to further improve the embedding capacity and visual quality of watermarked image by designing more accurate predictor and the proposed complementary embedding strategy.

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