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# **Tunable Frequency-Selective Rasorber Based on Varactor-Embedded Square-Loop Array**

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**ABSTRACT** This paper presents a varactor-based tunable frequency-selective rasorber (FSR) with embedded bias grid. The proposed structure consists of a lossy layer based on square-loop arrays and a lossless layer. Each layer has an embedded wire grid that provides the bias voltage for the varactors through metallic vias. This arrangement can avoid unnecessary effects associated with the additional biasing network. An equivalent circuit model is developed to explain how the structure can provide a tunable transmission window within the absorption band. Simple design guidelines for the tunable FSR are then provided. The performance of the proposed structure is measured in a parallel-plate waveguide setup. Both simulated and measured results show that by changing the bias voltage from 16 to 4 V, the center transmission frequency of the FSR can be tuned from 5.2 to 3.8 GHz continuously. The insertion loss of the FSR within the transmission window is only 0.59 dB at 5.2 GHz and a fractional bandwidth of 93.1% (2.4–6.58 GHz) for -10 dB reflectivity is achieved under the normal incidence.

**INDEX TERMS** Frequency-selective surface, rasorber, reconfigurable rasorber, tunable absorber.

### I. INTRODUCTION

Frequency-selective rasorber (FSR) has attracted growing attention due to its unique transmission and absorption characteristics [1]. Designed as a combination of frequency selective surface (FSS) and absorber, FSR can be transparent to incident electromagnetic (EM) waves in the passband and absorptive outside the passband, rather than reflective for conventional FSSs [2]. The key benefit of FSR is its suitability for stealthy radomes, which require a transmission window and a low radar cross section (RCS) over a desired frequency band. The rasorbers also have potential application in the protection and interference-mitigation of wireless local area network systems.

A conventional method of designing FSR structures is based on multi-layered frequency selective surfaces (FSSs) combined with lossy components or materials [4]–[12]. In the past, most of the existing configurations can only achieve one-sided absorption band (either lower or upper) [13]–[16]. To address this issue, a new concept of 3-D rasorbers was proposed in [17]–[20] to achieve a transmission window within a wide absorption band. In addition, the idea of bypassing the lossy components by adding resonators to improve the insertion loss within the transmission band was implemented in [21].

It is a challenging task to design a tunable and highly selective transmission window within a wide absorption band, or tunable FSR in short, though such tunable FSR can be very useful for many military systems. A tunable FSR based on 3-D structure was proposed in [22], though there were not experimental results reported. As for 2-D structures, based on existing tunable frequency-selective surfaces (FSSs), various methods of designing tunable FSRs can be proposed, such as using mechanical deformation [23], utilizing micro-electromechanical (MEMS) switches [24], magnetically tunable ferrite substrate [25], and liquid crystal [26]. However, the mechanical deformation method and MEMS switches have the disadvantages of being complicated structure and requiring large control voltage. It is also noted that the tuning ranges of the structures based on magnetically biased ferrite and liquid crystal are relatively limited.

A well-known technique of designing tunable FSSs is to use components such as varactors and PIN diodes [27]–[30]. They can provide electronic tuning with high-speed and

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exhibit wideband tuning range. Several designs of active FSR based on varactors and PIN diodes have been proposed so far, such as [31], [32]. However, the switchable FSR structure proposed in [31] can only provide one passband or none. Meanwhile, the insertion loss of the FSR reported in [32] is relatively large, and the filtering responses of the absorption band are not stable. In addition, it is desirable to avoid the use of complicated biasing network in these diode-based FSRs. According to [30], adding the extra biasing network and elements affects the frequency response of the original FSR. And the strategies for RF/DC isolation should also be considered.

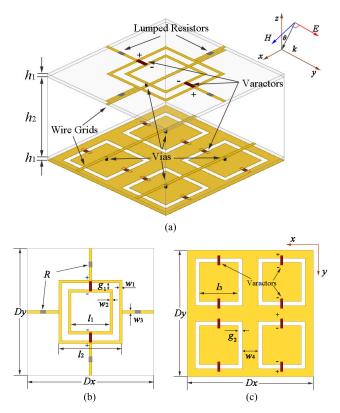
In order to overcome the above issues, we present a doublelayer varactor-based tunable FSR with two absorption bands at both sides of the transmission window in this paper. The lossy layer is achieved by utilizing a square-loop array combined with lumped resistors to provide the absorption band. A typical bandpass FSS layer is utilized to realize the transmission window within the absorption band. Both layers are constructed with varactors to achieve the coordinated tunable characteristic. The varactors in the front and back layers are connected to the ground through metallic vias and wire grids, which are incorporated with the biasing network and embedded in the FSS layers. Based on the presented equivalent circuit model (ECM), the tunable resonance and operating principle of the structure are analyzed in detail. This configuration can realize electronic tunability continuously with simple control of the bias voltage.

This paper is organized as follows. In Section II, we first describe the tunable FSR structure and its ECM to explain the operating principle. The detailed description of the tuning mechanism is also provided. Simple design guidelines are developed to implement the square-loop array-based tunable rasorber. After that, based on the method described above, an example of the tunable rasorber is designed. In Section III, the proposed tunable FSR is experimentally verified and discussed. A good agreement is observed between the measurement and simulation results. Finally, concluding remarks are given in Section IV.

#### **II. ANALYSIS AND DESIGN OF THE TUNABLE FSR**

#### A. DESCRIPTION OF THE TUNABLE RASORBE

In many FSR applications, the transmission window within the absorption band should can be adjusted according to the system requirements. A tunable rasorber can be designed by using varactors. Based on the reported designs [4], [6], [11], the unit cell configuration of our proposed tunable FSR is shown in Fig. 1. The structure contains one lossy FSS layer placed above a lossless FSS layer with a separation of a quarter-wavelength air spacer. It is well known that the lossy layer can be implemented by either resistive sheet or resistorloaded FSS. The incoming EM wave can propagate through the whole structure at the transmission band because both layers are band-pass within the transmission band, while it can be absorbed by the lossy material at the absorption band.



**FIGURE 1.** Geometry of the unit cell structure of the proposed FSR. (a) 3-D view of the FSR. (b) Top view of the lossy layer. (c) Top view of the bandpass layer.

In each unit cell of the tunable rasorber proposed in this paper, the lossy layer consists of a square-loop structure loaded with lumped resistors into four metallic strips. The lossless layer is a typical bandpass FSS. Copper patterns are printed on both layers that are separated by a dielectric spacer. The two FSS layers are separated by an intermediate air spacer. Furthermore, as shown in Fig. 1 (b) and (c), varactors on each layer are connected with the wire grid through metallic vias. Since all the varactors are biased in parallel, only a single RF choke is needed for RF/DC isolation. The dimensions of the unit cell along the x and y directions are specified by  $D_x = D_y = D$  for the tunable FSR. The thickness and relative permittivity of the substrate are  $h_1$  and  $\varepsilon_1$ , respectively.

#### **B. EQUIVALENT CIRCUIT MODEL**

In order to assist the design of our tunable FSR, an ECM is presented and analyzed in this subsection. Based on the ECM of a double square-loop and bandpass FSSs [33], the ECM of the proposed tunable FSR is constructed in Fig. 2. The lossy layer is mainly modeled by a series–parallel  $L_{c1}$ ,  $C_c$ , and  $L_{c2}$ resonator, corresponding to the square-loop array. The resonator is then connected by two *RC* parallel resonators with the inductors  $L_s$ , which represents the strip lines around the square-loop. The values of inductors  $L_{c1}$  and  $L_{c2}$  are related to the side length of inner and outer loops, respectively.  $C_c$ is determined by the gap width  $g_1$  between the two loops.

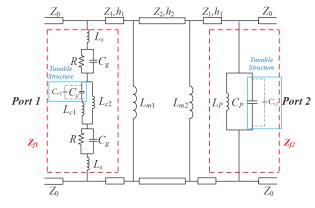


FIGURE 2. ECM of the proposed FSR.

 $C_g$  is associated with the distance of the outer loops on the neighboring two units. The bandpass layer is modeled by a parallel  $L_p C_p$  resonator. The parallel inductors  $L_{m1}$  and  $L_{m2}$  model the inductive effect of the wire grid at the back of each layer.  $Z_0$  and  $Z_1$  represent the wave impedances of free space and substrate, respectively.

The surface impedances of the first and second layers are represented by  $Z_{f1}$  and  $Z_{f2}$ , respectively. According to [2], the surface impedances of the lossy FSS layer and lossless layer are:

$$Z_{f1} = 1/[j\omega C_c/(1 - \omega^2 C_c L_{c1}) + 1/(j\omega L_{c2})]$$

$$+2^* j\omega L_s + 2/(j\omega C_g + 1/R)$$
 (1)

$$Z_{f2} = 1/[j\omega C_p + 1/(j\omega L_p)]$$
<sup>(2)</sup>

where  $\omega$  is the angular frequency.

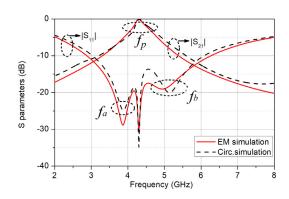
At the transmission frequency  $f_p$ , to achieve a good transmission characteristic with low insertion loss, both impedances  $Z_{f1}$  and  $Z_{f2}$  should approach  $\infty$ . In this case,  $|S_{11}| = 0$  and  $|S_{21}| = 1$ , which means that the incoming waves can propagate through the FSR from *Port 1* to *Port 2* with no absorption or loss. According to the ECM shown in Fig. 2, the resonant frequencies of the two FSSs are:

$$f_{p1} = \frac{1}{2\pi\sqrt{C_c(L_{c1} + L_{c2})}}$$
(3)  
$$f_{p2} = \frac{1}{2\pi\sqrt{C_pL_p}}$$
(4)

Both the first and second layers must satisfy a parallel resonance at the same frequency, which means that  $f_{p1} = f_{p2} = f_p$  for the center frequency of the transmission band.

At the absorption frequencies  $f_a$  and  $f_b$ , for an ideal FSR,  $|S_{11}| = 0$  and  $|S_{21}| = 0$ . Based on the matrix conversion, the *S* matrix of the equivalent circuit network of the bandpass FSS layer can be obtained. The ABCD matrix of the cascaded two-port network for the air spacer and bandpass FSS can be written as:

$$\begin{bmatrix} A & B \\ C & D \end{bmatrix} = \begin{bmatrix} \cos \theta_2 & jZ_2 \sin \theta_2 \\ jY_2 \sin \theta_2 & \cos \theta_2 \end{bmatrix} \begin{bmatrix} 1 & 0 \\ Y_{f2} & 1 \end{bmatrix}$$
(5)



**FIGURE 3.** Comparison between S parameters of the FSR calculated from HFSS using periodic boundaries for normal incidence and the equivalent circuit model. (Circuit parameters:  $Z_0 = Z_2 = 377 \ \Omega$ ,  $Z_1 = 236 \ \Omega$ ,  $R = 294 \ \Omega$ ,  $L_s = 3.2 \ nH$ ,  $L_{c1} = 1.85 \ nH$ ,  $L_{c2} = 2.05 \ nH$ ,  $L_p = 3.9 \ nH$ ,  $C_g = 0.06 \ pF$ ,  $C_c = 0.34 \ pF$ ,  $C_p = 0.35 \ pF$ ).

where  $\theta_2 = 2\pi fh_2/c$ , *c* is the speed of light,  $h_2$  is the spacing between two substrates, and  $Z_2 = 377 \ \Omega$  is the free-space wave impedance. We may set  $|S_{11}| = 0$  for an ideal FSR, and one can then solve:

$$\tan(\theta_2) = Z_2(\frac{1}{2\pi fL_p} - 2\pi fC_p) \tag{6}$$

for the designed frequencies  $f_a$  and  $f_b$  of the absorption bands. In addition, the series resonant frequency  $f_s$  for the lossy FSS layer can be expressed as:

$$f_s = \frac{1}{2\pi\sqrt{C_c L_{c1}}}\tag{7}$$

where the series resonant frequency  $f_s$  is very close to the upper absorption frequency  $f_b$ . Under this situation, the connected resistors are providing the necessary absorption. It can be seen from Fig. 3 that the ECM results are in good agreement with the simulated ones using ANSYS HFSS, which verifies the validity of our proposed equivalent circuit.

It should be mentioned that the parallel inductances  $L_{M1}$  and  $L_{M2}$  introduced by the wire grids can have negligible influence. According to [30], one obtains

$$L_{Mi} = \mu_0 \mu_{eff} \frac{P}{2\pi} \ln(\frac{1}{\sin(\pi W/(2D_i))}) \quad (i = 1, 2)$$
 (8)

where W is the width of the wire grid,  $D_i$  is the size of each unit cell (i = 1, 2),  $\mu_0$  is the permeability of the vacuum and  $\mu_{eff}$  is the effective relative permittivity of the substrate. The inductance embedded with wire grid can be calculated by:

$$L_{\text{lossless}} = 1/(1/L_P + 1/L_{M2}) = L_P/(1 + L_P/L_{M2})$$
(9)

For the lossless FSS layer, we can obtain  $L_{M2} = 57.3$  nH, which is much larger than the value of parameter  $L_P$ . When  $L_{M2} >> L_P$ ,  $L_{lossless}$  can be very close to  $L_P$ , indicating that the effect of  $L_{M2}$  can be ignored. The same conclusion applies to the lossy layer with  $L_{M1}$ .

### C. TUNING MECHANISM

The proposed FSR structure can be simply modified to achieve a tunable response by loading varactors on the lossy and bandpass layers, as shown in Fig. 1(a). For the lossy layer, a metallic via and two varactors are included in each unit cell for tuning the resonant frequency. The varactors are inserted across the gap between the two square loops of the resonator. As shown in Fig. 1(b), the negative electrode of the varactors is on the inside of the square-loop, while the positive electrode moves towards outside. The strip lines around the square-loop are used to connect the positive electrode of varactors to the ground. The metallic via is used to connect the inner square loop to the back-bias wire electrically, providing the forward current to the negative electrode of the varactors. Furthermore, this structure can also reduce any voltage drop caused by the loss of the lumped resistors because the positive electrode is connected to the ground. With this design, the reverse bias voltage can be provided to the varactors synchronously. The same structure is also applied to the bandpass layer, as shown in Fig. 1(c).

By applying a DC bias voltage (V<sub>b</sub>) between the two square loops, the equivalent capacitance between them can be varied electrically to realize a tunable frequency response on the lossy layer. With a proper design, the same tunable frequency response on the lossless layer can be supplied by the same bias voltage, resulting in a very simply tuning mechanism. As shown in Fig. 2, the equivalent capacitances of resonators on both layers can be defined as varactor capacitances  $C_{v1}$ and  $C_{v2}$ , respectively. The influence of the series resistance of the varactors we used will be discussed in the following sections. According to (1) and (2), we can obtain:

$$f_{p1}' = \frac{1}{2\pi\sqrt{(C_c + C_{v1})(L_{c1} + L_{c2})}} = f_{p2}'$$
$$= \frac{1}{2\pi\sqrt{(C_p + C_{v2})L_p}} = f_p'$$
(10)

where  $f_{p1}'$  and  $f_{p2}'$  are tunable resonator frequencies with varied capacitances.

In addition, the absorption rate of the tunable FSR is defined as the percentage of energy absorbed by the lossy layer, which is calculated as:

$$Absorption = 1 - |S_{11}|^2 - |S_{21}|^2 \tag{11}$$

# D. DESIGN OF THE TUNABLE RASORBER

According to the ECM and tuning mechanism discussed above, the transmission band  $f_p$  is mainly determined by the resonant frequencies of both FSSs. Based on the ECM and the conducted analysis, the design guidelines can be formulated and a tunable FSR can then be quickly designed as follows.

As shown in Fig. 3, the frequency f<sub>p</sub> is assumed to be the transmission frequency of the absorber to be designed. The thickness h<sub>2</sub> of the air spacer between the two FSSs can be evaluated similar to the Salisbury screen [4], which is 2β<sub>1</sub>h<sub>1</sub> + β<sub>2</sub>h<sub>2</sub> = π/2, β<sub>i</sub> = 2π/λ<sub>i</sub>, i = 1, 2. λis the wavelength of the EM wave propagating in

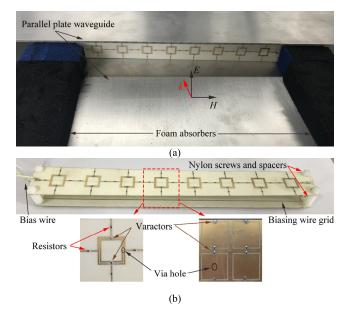
different dielectric media. Furthermore, the thickness of the air spacer can be reduced by selecting a substrate with higher dielectric constant for the spacer, although it may result in a narrower transmission bandwidth.

- 2) For the unit cell of the FSSs,  $D_x = D_y < \lambda_p/2$ . Based on the ECM, according to the desired transmission frequency ( $f_p$ ) and absorption frequencies ( $f_a$  and  $f_b$ ), a quick optimization can be carried out to determine the equivalent resistances, inductances, and capacitances of the square-loop as well as the bandpass structure.
- 3) The equivalent inductance L and capacitance C are determined by a function F given in [3]. It is clear that the values of the gaps  $(g_1 \text{ and } g_2)$  must be suitable for the size of varactors we used, which means that  $g_1$  and  $g_2$  can be decided based on the provided dimensions of the varactors. The physical dimensions of the two FSSs can then be estimated by the formulas provided in [30] and [34]. It should be mentioned that the functions are mainly related to frequency  $f_p$ . In order to obtain a quick design, the physical lengths  $l_2 \approx 0.25c/f_p$ .
- 4) Based on transmission line theory, the desirable frequency responses of the FSR can be obtained through a quick circuit simulation with the combination of selected resistors. It should be noted that a large absorption bandwidth can be realized by properly choosing the values of the inserted resistors.
- 5) Based on the estimated dimensions from the analysis of the tunable FSR, the full-wave simulators, ANSYS HFSS and CST Microwave Studio, can be used to further optimize the structure for better accuracy.

The guidelines above can provide considerable design flexibility and a fast optimization procedure.

In this paper, a design example is fabricated and tested. The original desirable transmission frequency is  $f_p = 5.2$  GHz. More specifically, the substrate material used for fabrication is Rogers 4003, with a dielectric constant  $\varepsilon_1 = 3.55$  and thickness  $h_1 = 0.508$  mm. Since the original center transmission frequency is 5.2 GHz, we obtain  $h_2 = 13.6$  mm for the ideal air spacer with  $\varepsilon_2 = 1$ . As shown in Fig. 1, the final dimensions are:  $l_1 = 7.6$  mm,  $l_2 = 10.2$  mm,  $l_3 = 9.7 \text{ mm}, w_1 = w_2 = w_3 = 0.5 \text{ mm}, w_4 = 1.7 \text{ mm},$  $g_1 = g_2 = 0.3 \text{ mm}, D_x = D_y = 24 \text{ mm}, R = 294 \Omega.$ The used varactor is MA46H120, which is a GaAs flip-chip diode and it can provide a tunable range of capacitance from 0.12 to 1.00 pF for a reverse bias voltage between 16 and 0 V. The fabricated sample of the lossy layer also consists of four lumped resisters in each unit cell with a value of 294  $\Omega$ . The resonators in the front and back layers of the tunable FSR are connected to the bias wire grid through vias of 0.3 mm diameter.

It should be mentioned that in this work, only a single polarization of the incident wave (TE polarization) is considered, as shown in the Fig. 1(a). We have designed the direction of the biasing wire grid along the *x*-axis, perpendicular to the E-field direction of the TE wave. The width of the bias



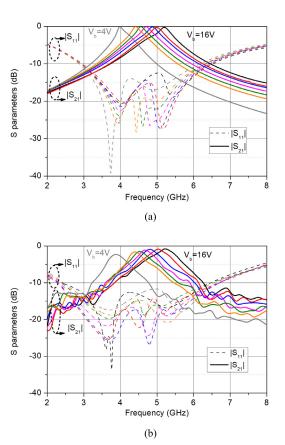
**FIGURE 4.** Measurement setup of proposed structure and assembly details. (a) FSR measurement setup inside the parallel-plate waveguide (PPW) testing platform. (b) 3-D view of the fabricated tunable FSR sample and details of the unit cell.

wire grid is 0.5 mm along the *y*-axis direction, which is relatively small. The effect of the biasing wire grid has been investigated and it is found to be negligible.

## **III. EXPERIMENTAL RESULTS AND DISCUSSION**

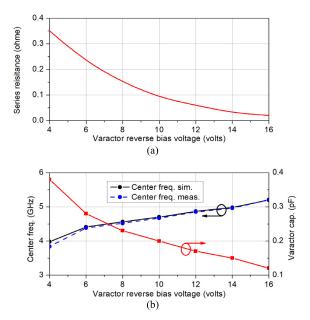
A photograph of our fabricated tunable FSR prototype consisting of eight cells in one direction with the size of  $24 \times 196 \text{ mm}^2$  is shown in Fig. 4, with several supporting plastic nylon screws and spacers, which maintains a uniform gap of 14 mm. The designed FSR has been measured inside a parallel-plate waveguide (PPW) setup [4], as shown in Fig. 4(a). The setup cell supports a TEM wave propagation, which can mimic a free-space environment approximately. The biasing wire grids on each layer are connected to a variable DC power supply. In this way, all the varactors are reverse-biased, and their capacitance can be tuned continuously by changing the DC bias voltage. A 40-k $\Omega$  resistor is connected to the wire grid to act as an RF choke [30]. In the measurements, the bias voltage is firstly set to 16 V to test the lowest capacitance value of 0.12 pF for each varactor, corresponding to a center transmission frequency of 5.2 GHz for the transmission band. The bias voltage is then decreased step-by-step from 16 to 4 V with a step size of 2 V, and the variation of the transmission responses is recorded for each step.

The comparison of the simulated and measured reflection and transmission coefficients of the tunable FSR under the normal incidence is shown in Fig. 5. It can be clearly noticed that the simulation and experiment results are in good agreement. The bias voltage in the measurement is decreased from 16 to 4 V gradually, while the capacitor value can be tuned from the lowest 0.12 pF to the highest 0.38 pF, corresponding to a change of the center transmission frequency from

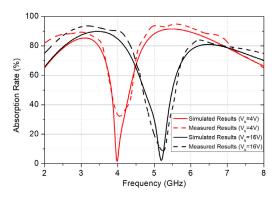


**FIGURE 5.** Reflection and transmission responses of the designed tunable FSR under normal incidence for different values of varactor bias voltage. The reverse bias voltage ( $V_b$ ) is varied from 16 to 4 V with a step size of 2 V. (a) Results obtained from EM simulations. (b) Measured reflection and transmission responses.

5.2 to 3.8 GHz simultaneously. The measured insertion loss is less than 0.59 dB at 5.2 GHz when the bias voltage equals to 16 V, while the fractional bandwidth for reflection less than -10 dB is 93.1% (2.4–6.58 GHz). When the bias voltage equals to 4 V, the fractional bandwidth for reflection less than -10 dB is 96.7% (2.26-6.49GHz). The intermediate performance have similar results. Meanwhile, a frequency shift of less than 0.1 GHz at the lower band is observed when comparing with the simulated results, which is probably caused by the variation of component values and the parasitic effects of the lumped elements. It should be mentioned that the measured insertion loss is less than 2.5 dB at the lower band, which is bigger than the simulated one. This is mostly due to the ohmic loss of the varactors. The passband is defined as the bandwidth with -3 dB from the peak of the transmission response. And the fractional bandwidth for this passband is 15.4% when the bias voltage is at 16 V. The insertion loss increases as the bias voltage is decreased because the varactor exhibits a larger series resistance at a lower bias voltage. Fig. 6(a) illustrates the variation of the series parasitic resistance of the varactor as a function of the reverse bias voltage. The center frequency of the FSR and the varactor capacitance versus the bias voltage are plotted in Fig. 6(b). The variation of the center frequency is not smooth



**FIGURE 6.** (a) Series resistance of the varactor as a function of the reverse bias voltage. (b) Variation of the varactor diode capacitance and the center frequency of the tunable FSR as a function of the reverse bias voltage.



**FIGURE 7.** Comparison of the EM simulated and measured absorption rate results.

when the voltages decreases due to the nonlinear relationship between the varactor capacitance and the bias voltage.

Fig. 7 illustrates the EM simulation and experiment results of the absorption rate at the upper and lower limits of the tuning band. It is shown that at the upper limit when the bias voltage equals to 16 V, the FSR has more than 90% absorption for an incident EM wave from 2.76 to 3.95 GHz, which represents a bandwidth of 35.5%. When the bias voltage equals to 4 V, the 90% absorption band is from 4.8 to 6.25 GHz with the fractional bandwidth of 26.2%. The absorption band shifts to the high frequency band as the voltage decreases. The measured absorption bandwidths are slightly larger than the simulated ones, which is mainly due to the ohmic loss of the varactors and the parasitic effect of the used lumped resistors.

The sensitivity of the tunable FSR's responses on the oblique incidences of the plane EM wave is further explained

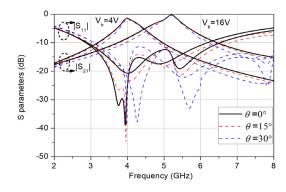


FIGURE 8. Simulated reflection coefficient and transmission coefficient of the proposed FSR unit cell under an oblique incidence.

TABLE 1. Comparisons between conventional FSR/FSS and proposed tunable FSR.

Refer ence	Insertion Loss (dB)	FBW ( S <sub>11</sub>   < - 10dB)	Tunable range	Thickn ess $(\lambda_L)$	FSR/ FSS
[17]	0.5	108%	N.A	0.19	FSR
[21]	0.68	92.3%	N.A	0.108	FSR
[22]	< 1	80%.	17.8%	N.A	FSR
[31]	3.3	95%	33%	N.A	FSR
[32]	0.64	99.6%	Switchable	0.09	FSR
[26]	< 1	N.A.	6%	N.A	FSS
Our work	0.59	93.1%	31%	0.107	FSR

in Fig. 8 through EM simulations. The scan plane of oblique incidence angle  $\theta$  is located in the *yz* plane for TE wave. The results provided for the upper and lower limits of the tuning band demonstrate that the designed FSR exhibits a stable response in the range of the incident angles up to 30°. This stability is mainly due to the relatively small dimension of the unit cell.

In order to better understand the advantages of our tunable structure, a comparison with other reported designs in the literature is made and provided in Table I. It can be obviously seen that a continuous tunable range has been obtained and developed while the thickness and insertion loss of our design are relatively small. The fractional bandwidth for reflection less than -10 dB is around 93%, which is relatively large. In addition, the topology of our design is polarization-sensitive for TE wave only because the varactors are only inserted along the *y*-axis, as we have discussed in Section II. The current design can be further generalized to suit dual polarizations (both TE and TM waves) if the varactors are assembled along both *x*-axis and *y*-axis. In this situation, the effect of the biasing networks should be more carefully characterized and compensated.

# **IV. CONCLUSION**

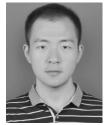
A tunable FSR based on square-loop array has been successfully designed and verified at the microwave band.

The tunability is achieved by integrating varactors on both lossy and lossless layers. An ECM is given to analyze the operating principle and design guidelines based on the ECM has then been developed. The unique feature of our proposed structure is that all the varactors are biased by embedded wire grid through metallic vias resulting in a low insertion loss, broadband, and high-selectivity rasorber. Measured results show that the designed rasorber has a continuous tuning range from 5.2 to 3.8 GHz for the center transmission frequency when the bias voltage changes from 16 to 4 V. Furthermore, the structure can be readily generalized to dual-polarized rasorber. Owing to the low insertion loss feature and tunable transmission band, the proposed FSR has potential applications in tunable and reconfigurable stealthy antenna-radome systems.

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