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Design of a New N-Shape Composite Ultra-Thin Deployable Boom in the Post-Buckling Range Using Response Surface Method and Optimization

HUI YANG¹, FENGSHUAI LU¹, HONGWEI GUO^{1,2}, AND RONGQIANG LIU²

¹College of Electrical Engineering and Automation, Anhui University, Hefei 230601, China

²China State Key Laboratory of Robotics and System, Harbin Institute of Technology, Harbin 150001, China

Corresponding author: Hongwei Guo (guohw@hit.edu.cn)

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ABSTRACT Composite ultra-thin boom can be folded elastically. Moreover, such booms are able to self-deploy by releasing stored strain energy, which can be applied in deployable antenna, solar sail, and optical telescopes. Surrogate models for imperfection-sensitive quantities of interest and multi-objective optimization are developed for the design of a new N-shape cross-section composite ultra-thin deployable boom. The proposed optimal design method integrates four general steps: (1) design of experiments, wherein the sampling designs of the N boom are created on the basis of the two-factor five-level full factorial design of experiments method; (2) efficient computational analyses of each design sample, wherein the post-buckling behavior of the N boom are analyzed under three different axial directions using nonlinear finite element ABAQUS/Explicit solver; (3) establishing the surrogate models of bending stiffness around the x - and y - axes and torsional stiffness around the z -axis by response surface method (RSM); (4) performing the multi-objective optimization design using modified non-dominated sorting genetic algorithm to realize the optimal design. The bending stiffness around the x - and y - axes and the torsional stiffness around the z -axis are set as the objectives, mass is set as the constraint, and the bonded web height and the central angle of the middle tape spring of the N boom are set as the variables. The typical surrogate modeling method can be applied to different problems in structural and material design.

INDEX TERMS Deployable structures, N boom, buckling, response surface method, optimization.

I. INTRODUCTION

Deployable structures, such as solar sails, antennae and optical telescopes, have been essential for space applications because of the limited volume of launching vehicles and the large-scale operating requirements in space. Different cross section wrapping deployable booms, such as the lenticular boom [1]–[3], triangular rollable and collapsible (TRAC) boom [4], [5], and storable tubular extendable member (STEM) [6], [7], have also been developed for spatial applications. All three booms can be wrapped around a hub,

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whereby the booms transitions from a flattened configuration to a structurally deployed shape.

Theoretical and experimental study on deployable truss structures were conducted [8]. An active-passive composite for driving a deployable lenticular boom for space probes was proposed and tested [9], and a geometrical optimal design of the lenticular boom was developed through modal and coiling analysis [10], [11]. A double-layer tape spring and integral tube hinge with double slots were investigated on basis of the response surface (RS) method [12]–[14]. A hinge that consists of three single tape springs was tested, and the finite element (FE) model was validated by the physics-based simulation results [15], [16]. The micro-mechanical behavior of two-ply plain weave laminates under small strains

for deployable booms was predicted [17]. The post-buckling characteristics of slender structures demonstrated an important relationship with loading capacity [18]. Stress concentration and material failure during the coiling of the TRAC boom were tested [19]. The bending and torsional behaviors of the TRAC booms were studied using numerical analysis and experimental testing [20]. The TRAC boom could carry significantly increased loads well into the post-buckling regime, and a data-driven computational framework improved their buckling and post-buckling behavior through [21], [22]. The STEM and lenticular booms were effectively derived, and their thickness was calculated under the assumption of a strain of 1.5%. The TRAC boom obtained 10 times more cross-section inertia than the lenticular boom and 34 times more than the STEM boom at the same packaged height [23]. However, the TRAC boom with open section demonstrated remarkably lower torsional stiffness than the closed section thin-walled boom.

This work aims to propose a new N-shape cross section (N) boom and to assess structural bending and torsional stiffness throughout the entire post-buckling process around the three axes. The N composite ultra-thin deployable boom, which has a configuration similar to that of the TRAC boom, consists of three tape springs. The middle tape spring has two circumscribed circles and two adjacent tape springs that bond along one longitudinal edge of the C shapes. Moreover, the torsional stiffness of the N boom is greater than that of the TRAC boom. The structural bending and torsional stiffness throughout the entire post-buckling process around the three axes should be analyzed to increase the capacity of the N boom in deploying state. Section 2 describes the behaviors of the N booms in detail. Section 3 presents a method using the RS theory to establish the surrogate model of the bending stiffness around the x - and y - axes and the torsional stiffness around the z -axis. The two-factor five-level full factorial design of experiment (DoE) is applied to obtain the sample points. Accuracy analysis validated the surrogate models. Section 4 presents the multi-objective optimization. Section 5 discusses the results and concludes the study.

II. BEHAVIOR OF THE N DEPLOYABLE BOOMS

The N boom is similar to the TRAC boom, which also consists of two tape springs that bond along one longitudinal edge of the C shapes. The difference between these two types of booms is that the N boom consists of three tape springs, in which the middle tape spring has two circumscribed circles. Coordinate system of the N boom cross-section is shown in Figure.1. The N boom is centrosymmetric with respect to the y -axis. The bonded web height is h , and the thickness of each tape spring is t_n . The radius and central angle of the outer side tape spring are R_1 and θ_1 , respectively; and those of the internal side tape spring are R_2 and θ_2 , respectively. The N boom is made by laying four plies [45° / -45° / 45° / -45°] of T800 carbon fiber reinforced polymer as shown in Figure.2. Each ply thickness is $t_0 = 0.125$ mm, each tape spring thickness is 0.5-mm, and the longitudinal length is $L_n = 1$ m.

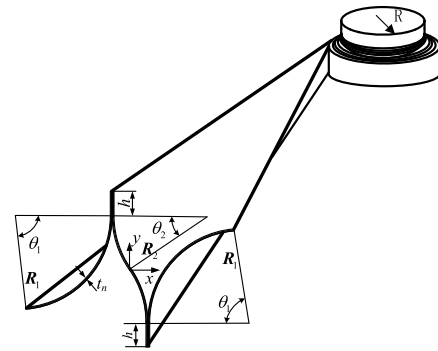


FIGURE 1. Cross section geometrical dimension of the N boom.

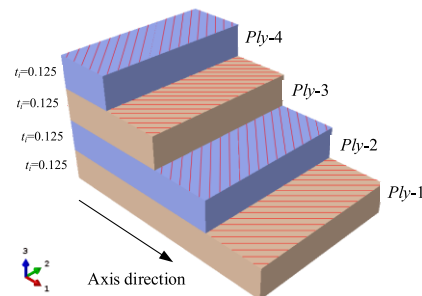


FIGURE 2. Material layout of the four plies [45° / -45° / 45° / -45°].

TABLE 1. Material properties of T800 and cohesive glue.

Material Properties	T800	Glue
Longitudinal stiffness E_1 /MPa	150 000	-
Transverse stiffness $E_2=E_3$ /MPa	7 000	60000
Shear stiffness $G_{12}=G_{13}$ /MPa	7 000	-
In-plane shear stiffness G_{23} /MPa	4 500	-
Poisson's ratio ν	0.3	0.3
Density ρ kg/m ³	2 500	1600

Two webs are bonded by cohesive glue. Material properties of T800 and glue are listed in Table 1.

The longitudinal length ($L_n = 1$ m) and thickness ($t_n = 0.5$ mm) are kept constant, and the same composite material described previously with the stacking sequence of [45° / -45° / 45° / -45°] is considered. The cross section width of the flattening tape springs is kept constant for all the three tape springs in each N boom to establish a fair comparison between different geometries. Figure.1 shows that the flattening width constant introduces a relationship among the one internal and two external tape springs and two independent parameters (e.g., h and θ_2) considered in this study:

$$\theta_1 = \frac{2R_2\theta_2 + h}{R_1} \tag{1}$$

N boom mass is presented as follows:

$$Mass(h, \theta_2) = 6\rho \cdot L_n \cdot t_n (R_2\theta_2 + h) \tag{2}$$

TABLE 2. Boundary conditions of RP2 under different circumstances.

	Bend around x -axis	Bend around y -axis	Torsion around z -axis
UX	0	Free	Free
UY	Free	0	Free
UZ	Free	Free	0
RX	Loading	0	0
RY	0	Loading	0
RZ	0	0	Loading

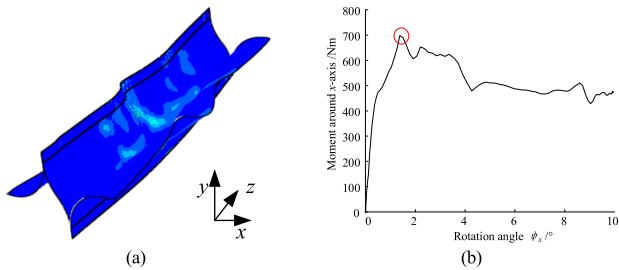


FIGURE 3. Predicted responses for the N boom: (a) bending moment around X ; (d) $M_x - \psi_x$.

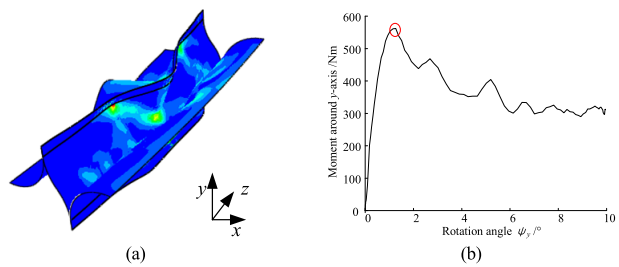


FIGURE 4. Predicted responses for the N boom: (a) bending moment around Y ; (d) $M_y - \psi_y$.

FE models are set up in the ABAQUS/Explicit software. Four nodes fully reduced integrated shell elements (S4R) and eight nodes three-dimensional cohesive elements (COH3D8) are applied. Two reference points (e.g., RP1 and RP2) are located on either end and set as the kinematic coupling constraints to either end surface. The degrees of freedom on RP1 are all restrained. The boundary conditions of RP2 under different circumstances are listed in Table 2. When buckling occurs in the N boom, the maximum moment around the three axes and the corresponding angle of rotation can be extracted. Figures 3-5 shows the predicted responses for the idealized N boom with $h = 35$ mm and $\theta_2 = 40^\circ$.

The ultimate buckling limit of the N boom is reached at the first bifurcation point, and the ultimate buckling limit is selected as the analytical maximum moment in the moment-angle response of the N boom. Thus, bending stiffness $EI_x(h, \theta_2)$, $EI_y(h, \theta_2)$ around the x -axis and y -axis, and torsional stiffness around the z -axis can be derived:

$$EI_x(h, \theta_2) = \left(\frac{dM_x}{d\theta_x} \right) \cdot L_n \quad (3)$$

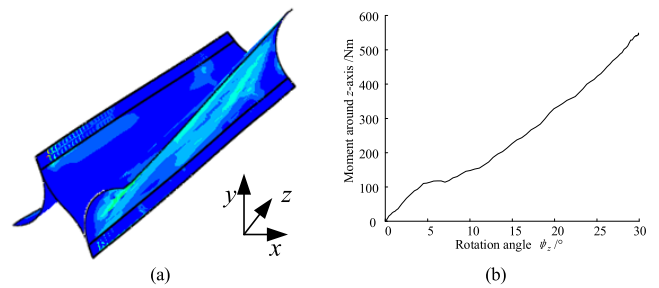


FIGURE 5. Predicted responses for the N boom: (a) bending moment around Z ; (d) $M_z - \psi_z$.

$$EI_y(h, \theta_2) = \left(\frac{dM_y}{d\theta_y} \right) \cdot L_n \quad (4)$$

$$GJ_z(h, \theta_2) = \left(\frac{dM_z}{d\theta} \right) \cdot L_n \quad (5)$$

where M_x is the moment around the x -axis, M_y is the moment around the y -axis; M_z is the moment around the z -axis; θ_x is the rotation angle around the x -axis; θ_y is the rotation angle around the y -axis; θ_z is the rotation angle around the z -axis.

III. RESPONSE SURFACE METHOD OF THE N BOOM

A. SAMPLE POINTS

To save computational time and cost in the buckling analysis, the RS method [24], [25] is used in the optimization study of the N boom. The RS method refers to a collection of mathematical and statistical procedures. The responses of the N booms includes the bending stiffness around the x -axis $EI_x(h, \theta_2)$, the bending stiffness around the y -axis $EI_y(h, \theta_2)$, and the torsional stiffness around the z -axis $GJ_z(h, \theta_2)$, which can be written in terms of a series of basic functions as follows:

$$\tilde{y}(h, \theta_2) = \sum_{i=1}^n \beta_i \phi_i(h, \theta_2) \quad (6)$$

where $\tilde{y}(h, \theta_2)$ represents the responses of $EI_x(h, \theta_2)$, $EI_y(h, \theta_2)$ and $GJ_z(h, \theta_2)$; n is the number of basic functions $\phi_i(h, \theta_2)$, i is the number of the design variables, and β_i is the coefficients of the basic functions. Polynomials are typical classes of basic functions, and a full n -order polynomial is given as

$$\begin{aligned} &1, x_1, x_2, \dots, x_n, \\ &x_1^2, x_1x_2, \dots, x_1x_n, \dots, x_n^2, \\ &x_1^3, x_1^2x_2, \dots, x_1^2x_n, x_1x_2^2, \dots, x_1x_n^2, \dots, x_n^3, \\ &x_1^4, x_1^3x_2, \dots, x_1^3x_n, x_1^2x_2^2, \dots, x_1^2x_n^2, \dots, x_1x_2^3, \\ &\dots, x_1x_n^3, \dots, x_n^4, \\ &\vdots \\ &x_1^n, x_1^{n-1}x_2, \dots, x_1x_n^{n-1}, x_1^2x_2^2, \dots, x_1^2x_n^{n-2}, \\ &\dots, x_1x_2^{n-1}, \dots, x_nx_2^{n-1}, \dots, x_n^n \end{aligned} \quad (7)$$

TABLE 3. Sample points and FE results of the bending stiffness around the x-axis.

No	h /mm	θ_2 /°	$EI_x(h, \theta_2)$ (N·m ² /rad)	$EI_y(h, \theta_2)$ (N·m ² /rad)	$GJ_z(h, \theta_2)$ (N·m ² /rad)
1	30	30	22902.76	13283.30	309.59
2	30	32.5	17009.73	14528.21	454.28
3	30	35	20018.65	18717.93	681.46
4	30	40	26844.00	25238.69	1284.93
5	30	45	27512.57	35923.76	1392.44
6	35	30	25031.26	14799.08	352.65
7	35	32.5	18859.77	15173.81	525.32
8	35	35	27639.15	17865.24	714.09
9	35	40	32029.18	24863.49	1266.72
10	35	45	32672.37	42408.89	1389.49
11	40	30	31419.65	14032.93	335.36
12	40	32.5	27368.94	14720.85	533.58
13	40	35	29041.04	18292.35	737.51
14	40	40	35532.41	28335.39	1198.68
15	40	45	28994.20	45166.06	1374.07
16	45	30	25720.40	14930.85	380.68
17	45	32.5	27704.56	16681.14	592.02
18	45	35	33645.25	19817.28	688.42
19	45	40	31339.98	33052.28	1323.39
20	45	45	29900.12	49859.45	1456.44
21	50	30	23809.02	16528.52	433.14
22	50	32.5	33120.92	15455.37	594.67
23	50	35	37684.79	21045.53	760.79
24	50	40	33419.45	30884.09	1255.94
25	50	45	38209.31	43478.15	1441.23

The quartic polynomials ($n = 15$) are selected to derive the basic functions in this study to ensure the accuracy and save computational time. Several design sample points $(h, \theta_2)^{(j)}$ ($j = 1, 2, \dots, m$) are needed ($m > n$) to determinate unknown parameters $\mathbf{b} = (\beta_1, \beta_2, \dots, \beta_n)$ in Eq.(6). The two-factor five level full-factorial DoE point is selected, and 25 sample points are obtained. The longitudinal length $L_n = 1$ m, thickness $t_n = 0.5$ mm, and radius of the external tape springs $R_1 = 153$ mm are kept constant. The bonded web height h changes from 30 mm to 50 mm, and the central angle θ_2 of the middle shell changes from 30° to 45°. Sample points and FE results of the N boom are listed in Table 3.

B. SURROGATE MODEL

From the simulation results (Table 3) and by combining Eqs. (6), (7), (8), and (9), the surrogate models of $EI_x(h, \theta_2)$, $EI_y(h, \theta_2)$, and $GJ_z(h, \theta_2)$ are derived from the DoE results,

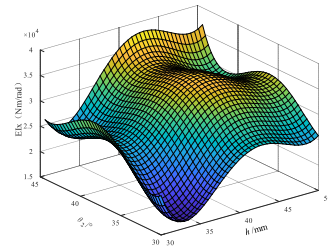


FIGURE 6. RS of $EI_x(h, \theta_2)$.

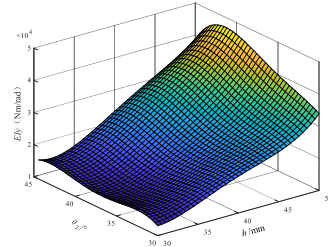


FIGURE 7. RS of $EI_y(h, \theta_2)$.

which are written as follows:

$$\begin{aligned}
 EI_x(h, \theta_2) &= 1.6955 \times 10^7 - 3.8366 \times 10^5 h - 1.4325 \times 10^6 \theta_2 \\
 &\quad + 12494h^2 + 5355.6h\theta - 186.3018h^3 \\
 &\quad + 54490\theta_2^2 - 92.1914h^2\theta_2 - 45.9468h\theta_2^2 \\
 &\quad - 944.2703\theta_2^3 + 0.9891h^4 + 0.8501h^3\theta_2 \\
 &\quad - 0.0939h^2\theta_2^2 + 0.4415h\theta_2^3 + 6.0864\theta_2^4 \tag{8}
 \end{aligned}$$

$$\begin{aligned}
 EI_y(h, \theta_2) &= -1.2496 \times 10^6 + 2.987 \times 10^5 h \\
 &\quad - 1.6571 \times 10^5 \theta_2 - 7.6665 \times 10^3 h^2 \\
 &\quad - 8.67 \times 103h\theta + 1.1161 \times 10^4 \theta_2^2 \\
 &\quad + 99.8632h^3 + 106.5774h^2\theta_2 + 124.1173h\theta_2^2 \\
 &\quad - 243.185\theta_2^3 - 0.5258h^4 - 0.4997h^3\theta_2 \\
 &\quad - 0.679h^2\theta_2^2 - 0.6149h\theta_2^3 + 1.7912\theta_2^4 \tag{9}
 \end{aligned}$$

$$\begin{aligned}
 GJ_z(h, \theta_2) &= -1.9112 \times 10^5 + 4213.3h + 17135\theta_2 \\
 &\quad - 170.7715h^2 + 22.7335h\theta - 744.0332\theta_2^2 \\
 &\quad + 2.6029h^3 + 0.8881h^2\theta_2 - 1.6326h\theta_2^2 \\
 &\quad + 14.6663\theta_2^3 - 0.0143h^4 - 0.0087h^3\theta_2 \\
 &\quad + 0.0022h^2\theta_2^2 + 0.0135h\theta_2^3 - 0.1067\theta_2^4 \tag{10}
 \end{aligned}$$

The derived RSs for $EI_x(h, \theta_2)$, $EI_y(h, \theta_2)$ and $GJ_z(h, \theta_2)$ of the N boom are plotted in Figures 6, 7 and 8, respectively. It can be seen that $EI_x(h, \theta_2)$ is sensitive to the central angle θ_2 and the bonded web height h , but $EI_y(h, \theta_2)$ and $GJ_z(h, \theta_2)$ are more sensitive to the bonded web height h than the central angle θ_2 of the middle tape spring.

C. ACCURACY ANALYSIS

The accuracy of the surrogate models must be evaluated using several criteria, i.e., coefficient of multiple

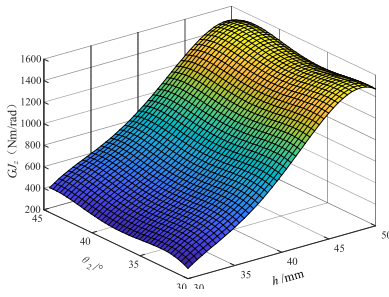


FIGURE 8. RS of $GJ_z(h, \theta_2)$.

determination (R^2), relative error (RE), root mean square error ($RMSE$), and adjusted coefficient of the multiple determination (R^2_{adj}). The criteria are written as follows:

$$RE = \frac{\tilde{y}_i(h, \theta_2) - y_i(h, \theta_2)}{y_i(h, \theta_2)} \quad (11)$$

$$R^2 = 1 - \frac{SSE}{SST} \quad (12)$$

$$R^2_{adj} = 1 - \frac{M - 1}{M - N} (1 - R^2) \quad (13)$$

$$RMSE = \left(\frac{SSE}{M - N - 1} \right)^{0.5} \quad (14)$$

where $y_i(h, \theta_2)$ is the simulation result, SSE is the total sum of the squares, and SST is the sum of squares of the following residuals:

$$SST = \sum_{i=1}^M [y_i(h, \theta_2) - \bar{y}(h, \theta_2)]^2 \quad (15)$$

$$SSE = \sum_{i=1}^M [y_i(h, \theta_2) - \tilde{y}(h, \theta_2)]^2 \quad (16)$$

For the surrogate models, the values of bending stiffness around the x -axis $EI_x(h, \theta_2)$, bending stiffness around the y -axis $EI_y(h, \theta_2)$, and torsional stiffness around the z -axis $GJ_z(h, \theta_2)$ vary from 0 to 1, which expresses the correlation level between the simulation results and responses. The enlarged R^2 and R^2_{adj} and small RE and $RMSE$ improve the RS fitting.

The buckling process simulation is highly nonlinear and needs high computation cost. The N boom longitudinal length is set to $L_n = 1$ m. The single flange thickness ($t_n = 0.5$ mm) and the flattening width of the three shells in each N boom are kept constant in the buckling process analysis. The RE errors between the FE and RS results of the 25 selected sample points are listed in Table 4.

The accuracies of the quartic polynomial functions are calculated by substituting the approximation of the responses derived from Eqs. (8) - (10) and the simulation results into Eqs. (11) - (14) with $m = 25$ and $n = 15$. The accuracies of the different RS models for the N booms are presented in Table 5. The values of RE s are no more than 8.81 %, meanwhile R^2 and R^2_{adj} are close to 1. These findings indicate

TABLE 4. RE errors between the FE models and RS results for the 25 sample points.

No	RS results			RE /%		
	$EI_x(h, \theta_2)$	$EI_y(h, \theta_2)$	$GJ_z(h, \theta_2)$	$EI_x(h, \theta_2)$	$EI_y(h, \theta_2)$	$GJ_z(h, \theta_2)$
1	22751.55	13101.43	295.40	-0.66	-1.37	-4.58
2	16443.57	15031.14	476.17	-3.33	3.46	4.82
3	20922.18	18544.28	675.02	4.51	-0.93	-0.94
4	26933.96	24565.99	1276.68	0.34	-2.67	-0.64
5	27236.22	36449.11	1399.44	-1.01	1.46	0.50
6	25274.60	14766.30	359.64	0.97	-0.22	1.98
7	20254.64	15039.62	532.38	7.34	-0.88	1.34
8	25458.43	18148.38	712.18	-7.89	1.58	-0.27
9	32059.88	25964.57	1267.86	0.096	4.43	0.089
10	33183.94	41191.70	1376.22	1.57	-2.87	-0.96
11	30523.61	14109.89	340.88	-2.85	0.555	1.65
12	25691.06	14185.39	520.21	-6.13	-3.64	-2.51
13	30460.72	17923.96	696.94	4.89	-2.01	-5.50
14	35157.04	28329.81	1242.78	-1.06	-0.019	3.68
15	30523.61	45998.58	1378.40	5.27	1.84	0.31
16	25022.61	15635.71	386.46	-2.71	4.73	1.52
17	29792.69	16035.00	570.73	7.54	-3.87	-3.59
18	33276.88	20500.60	744.15	-1.09	3.45	8.09
19	31043.42	32417.39	1283.78	-0.95	-1.92	-2.99
20	29174.47	49751.51	1455.85	-2.43	-0.22	-0.041
21	25355.79	15960.53	429.04	6.49	-3.44	-0.95
22	32154.75	16268.27	600.38	-2.92	5.26	0.96
23	38307.59	20621.17	753.98	1.65	-2.02	-0.89
24	32154.75	31096.25	1258.58	-3.78	0.67	0.21
25	38270.36	43445.50	1443.78	0.16	-0.08	0.18

TABLE 5. Accuracy of the different RS models for the N booms.

	R^2	R^2_{adj}	RE /%
EI_x (N·m ² /rad)	0.9623	0.9096	-6.13 ~ 7.54
EI_y (N·m ² /rad)	0.9974	0.9938	-3.87 ~ 5.26
GJ_z (N·m ² /rad)	0.9976	0.9942	-8.81 ~ 7.82

TABLE 6. Scale and weight factors of the objectives and constraint.

	S_j	W_j
EI_x	1	0.5
EI_y	1	0.8
GJ_z	1	100
Mass	1	20

that the accuracies of the surrogate models are sufficient for the selected sample points.

TABLE 7. Feasible designs of the N boom.

No.	h /mm	θ_2 /°	EI_x /(Nm ² /rad)	EI_y /(Nm ² /rad)	GJ_z /(Nm ² /rad)	Mass /g
1	37.153348	33.487733	24680.361	15471.024	586.52466	948.99081
2	35.711142	35.412321	27495.095	18590.685	744.52115	976.70178
3	33.436075	36.454169	26856.737	20644.978	859.3681	980.49189
4	31.567245	37.660292	26897.091	22370.263	996.695	990.61923
5	31.508465	37.738317	26947.85	22460.451	1005.9572	991.74025
6	30.780646	38.026215	26768.624	22670.973	1035.1694	992.0446
7	31.261411	38.026215	27080.448	22775.163	1040.16	995.65034
8	31.192997	38.139694	27141.391	22897.982	1053.9569	997.40882
9	30.832338	38.206982	26965.828	22894.456	1058.9004	996.05079
10	30.566525	38.302500	26909.063	22923.131	1067.7208	995.96924
11	30.622633	38.366159	26982.633	23014.313	1076.7212	997.66435
12	30.194766	38.576674	26957.814	23082.318	1097.3796	998.66932
13	30.091864	38.645529	26968.937	23109.213	1104.5003	999.27585
14	37.153348	33.487733	24680.361	15471.024	586.52466	948.99081

TABLE 8. Two optimal designs of the N boom with mass ≤ 1000 g.

No.	EI_x /(Nm ² /rad)		EI_y /(Nm ² /rad)		GJ_z /(Nm ² /rad)		RE /%		
	RS results	FE results	RS results	FE results	RS results	FE results	EI_x	EI_y	GJ_z
3	26856.737	24960.113	20644.978	22018.728	859.3681	819.268	7.60	-6.24	-5.25
6	26768.624	28722.362	22670.973	21242.741	1035.1694	1118.058	-6.80	6.72	-7.41

IV. MULTI-OBJECTIVE OPTIMIZATION DESIGN

The N boom should be designed for high stiffness deployment behavior to resist external disturbances. Bending stiffness around the x - and y -axis, and torsional stiffness around the z -axis are selected as the objectives. The mass of the N boom is directly related to the launch costs. Thus, mass is set as the constraint. The bonded web height h and central angle θ_2 of the middle tape spring are set as the design variables. Then, the multi-objective optimization design models of the N boom with three design objectives can be written as follows:

$$\begin{cases} \text{Opt. } \{EI_x|_{\max}; EI_y|_{\max}; GJ_z|_{\max}\} \\ \text{S.t. } Mass \leq 1000\text{g;} \\ 30\text{mm} \leq h \leq 50\text{mm;} \\ 30^\circ \leq \theta_2 \leq 45^\circ. \end{cases} \quad (17)$$

According to the analysis in Section 3.2, it is found that bending stiffness around the x - and y - axes, torsional stiffness around the z -axis favor different design variables. Non-dominated sorting genetic algorithm II is applied to realize the optimal design with a population size of 50 and generation number of 48. The value of the objective function T is equal to the sum of the objective components (O_j) with a corresponding weight factor (W_j) and scale factor (S_j) of the

j -th objective component [26], i.e.,

$$T = \sum_{j=1}^p \frac{O_j \cdot W_j}{S_j} \quad (18)$$

where j ($j = 1, 2, \dots, q$) is the number of optimization objectives, and q ($q = 4$) is the total number of objectives.

According to Eq.(18), the weight and scale factors of the objective component are equal, and the influences of the component with a small order of magnitude will be weaken. Given the significant bending stiffness around the x - and y -axes, both their scale factors are set to 1, and the weight factors are set to 0.5 and 0.8, respectively. Torsional stiffness GJ_z of the N boom with an open cross section is weak, and GJ_z is more important. Then, the scale and weight factors of the GJ_z are set to 1 and 100, respectively. The order of magnitude of mass is small; hence, the weight factor is set to 20. The scale and weight factors of the objectives and constraint are selected and listed in Table 6.

The feasible designs of the N boom are depicted in Table 7. The two optimal designs, namely, Nos.3 and 6. Then, the FE models of the two optimal designs are constructed. The bending and torsional stiffness are listed in Table 8. Notably, the REs between the RS and FE results are no more than 7.6 %. Thus, the accuracies of the surrogate model are

verified again. However, No.6 is selected as the optimal design with $h = 30.780646$ mm and $\theta_2 = 38.026215^\circ$ because the index of GJ_z is dominated.

V. CONCLUSIONS

The proposed N deployable boom concept consisted of three tape springs, wherein the middle tape spring had two circumscribed circles and two adjacent tape springs that bonded along one longitudinal edge of the C shapes. The post-buckling behaviors of the N boom under three different axial directions were analyzed using the nonlinear FE ABAQUS/Explicit solver.

The surrogate models for imperfection-sensitive quantities of interest of bending stiffness and torsional stiffness were derived from the quartic polynomials on the basis of RS method. A total of 25 sample points were created on the basis of the two-factor five-level full factorial DoE method. The precision of the surrogate models was validated by the absolute value of REs, which were no more than 8.81% in the entire design space.

The multi-objective optimization design was completed via the modified non-dominated sorting genetic algorithm II for the N boom. The optimal design configuration with the central angle $\theta_2 = 38.026215^\circ$ and bonded web height $h = 30.780646$ mm possessed high torsional and bending stiffness values. The FE model of the selected optimal design was established, and the RE between its FE and RS results was no more than 7.6%.

The bending stiffness around the x -axis was sensitively to both the central angle θ_2 and bonded web height h , but bending stiffness around the y -axis and torsional stiffness around z -axis were more sensitive to the bonded web height h than the central angle θ_2 of the middle tape spring. A large bonded web height of the N boom should be selected to improve the torsional behavior and disturbance resistance capacity in the fully deployed state.

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