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# Low-Cost Dual-Mechanical-Port Dual-Excitation Machine for Washing Machine Application

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**ABSTRACT** This paper proposes a low-cost dual-mechanical-port dual-excitation machine for washing machine application. The proposed machine artfully combines two machines (vernier and permanent magnet synchronous machine (PMSM)). An outer vernier rotor is used for the low-speed washing operations, and an inner PMSM rotor is used for the high-speed drying operations of the washing machine. The proposed machine is compared with a similar recently presented machine to verify its cost-effectiveness. Comparison using the finite element analysis (FEA) shows that the ferrite magnets used in the proposed topology are more cost-effective. Furthermore, compared to the existing machine, the power factor of the proposed machine is high during the drying operation; hence, a lower rating inverter is sufficient to drive the machine, which further reduces the overall cost. In addition, the proposed machine provides similar efficiencies as the existing machine for both washing and drying operations.

**INDEX TERMS** Dual excitation, dual mechanical port, low-cost, PMSM, vernier machine, washing machine.

## I. INTRODUCTION

The washing machine is an extensively used domestic appliance and the design of its motor is paramount to ensure its efficiency and cost-effectiveness. There are a few important characteristics a motor designed for a washing machine must possess: 1) wide driving range because it must operate at two speeds (washing and drying), 2) high efficiency at both operation points to minimize energy consumption, 3) low cost of the motor and drive to make the washing machine affordable. A direct drive motor with the abovementioned characteristics will have additional benefits.

Washing machines usually perform two operations: washing and drying. The washing operation is performed at low speeds, such as 50 rpm, and high torque values are required to enable fast start-up at full load; whereas, the drying operation is performed at high speeds, such as 1400 rpm, and requires low torque but high power. The speed required by the drying is typically approximately 28 times as much as that of washing. Different methods are used to achieve the

wide operating speed range of the washing machine motor, the commonest of them being the flux-weakening operation [1]–[3]. These operations are usually performed to run the machine at higher speeds. However, flux weakening increases the copper losses of the machine, and poses the risk of demagnetizing the permanent magnets (PMs) [4]. Furthermore, variable flux machines that combine the use of low coercive force (LCF) and constant magnets [5], [6] have been introduced for variable speed applications. The flux of the LCF magnets is weakened using either a negative d-axis current [7], [8] or a separate magnetizing winding [9]. The variable flux machines require complex control to vary the flux density of the LCF magnets. Moreover, there is the risk of permanently demagnetizing the LCF PMs.

The efficiency of the motor for washing machine application has been researched extensively, and many topologies have been proposed [11]–[14]. The efficiency of the washing machine motor is an important design consideration. However, due to the wide operating speed range, the designed machine does not demonstrate equal efficiencies during both operations. The efficiency of the machine is usually high for one operation and very low for the other operation [10].

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Furthermore, it is particularly desirable to consumers that a washing machine should be affordable, and the two important factors that impact the overall price of the washing machine are the prices of the motor and the inverter required for running the motor. The cost of the motor depends, to a great extent, on the. Recently, reasonably priced low-cost motors with ferrite magnets have been introduced [15]–[18]. However, the residual flux density ( $B_r$ ) of ferrite magnets is approximately three times lower than that of Neodymium-ferrite-boron (Nd-Fe-B) magnets. In addition, it is necessary to pay special attention to the power factor of the motor for drying operations. Low power factor machines inherently require a higher rating inverter, which increases the overall cost of the washing machine.

Direct drive motors have received extensive attention in recent years because, in addition to other advantages, they improve the reliability of the system by eliminating the backlash and simplifying the mechanical structures [19], [20]. In addition, direct drive motors reduce the noise and vibration of a system. They are incorporated into washing machines to make the machines more compact, according to the needs of user. The washing machine drum is connected directly to the motor shaft, thus eliminating the need for conveyor belts and gearboxes for coupling. Direct drive motors are characterized by high torque density. Therefore, various high torque-density machines, such as vernier machines and dual rotor machines, are the subjects of extensive research. Vernier machines have been recently acknowledged as a promising candidate for direct drive applications due to their high torque density [21], [22]. However, because of their high core losses and low power factor, they cannot be used for the drying operation of the machine.

Dual-rotor machines have been introduced in the literature [23]–[25]. These machines feature two rotors connected to a single shaft, which, compared to a single rotor topology, achieves a higher torque density. In [25], a dual-rotor hybrid permanent magnet machine is proposed for the traction application in which the outer rotor is a surface permanent magnet (SPM) rotor, and the inner rotor is a synchronous reluctance rotor. However, the two rotors are connected to a single shaft. Furthermore, dual mechanical port machines, with dual decoupled rotors, have been attracting scholarly attention [26], [27]. However, they have a single stator with two windings, which raises mutual coupling issues between two sets of windings [23]. Recently, a dual output stator-PM machine has been introduced to achieve high efficiency at the two operating points of a washing machine [28]. For comparison, the recently introduced machine will subsequently be referred to as the existing machine. Although the existing machine provides high efficiency for both washing and drying operations, it has a few shortcomings. Firstly, it deploys high-cost NdFeB magnets that increase the cost of the machine considerably. Secondly, the existing machine uses a flux-reversal machine for the drying operation. The flux-reversal machine is a type of flux-modulation machine. Hence, its operating frequency is high, and its core losses

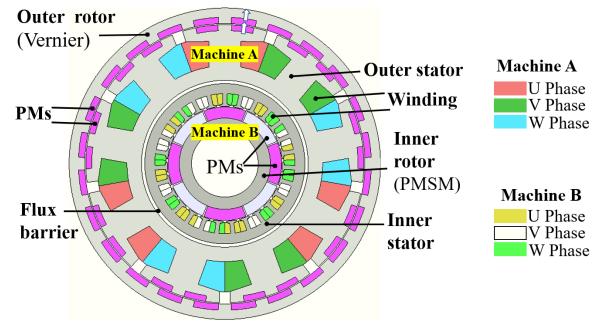


FIGURE 1. Configuration of proposed topology.

are correspondingly high. Thirdly, its power factor is low during drying operation. Therefore, A high rating inverter is required, which increases the overall cost of the system.

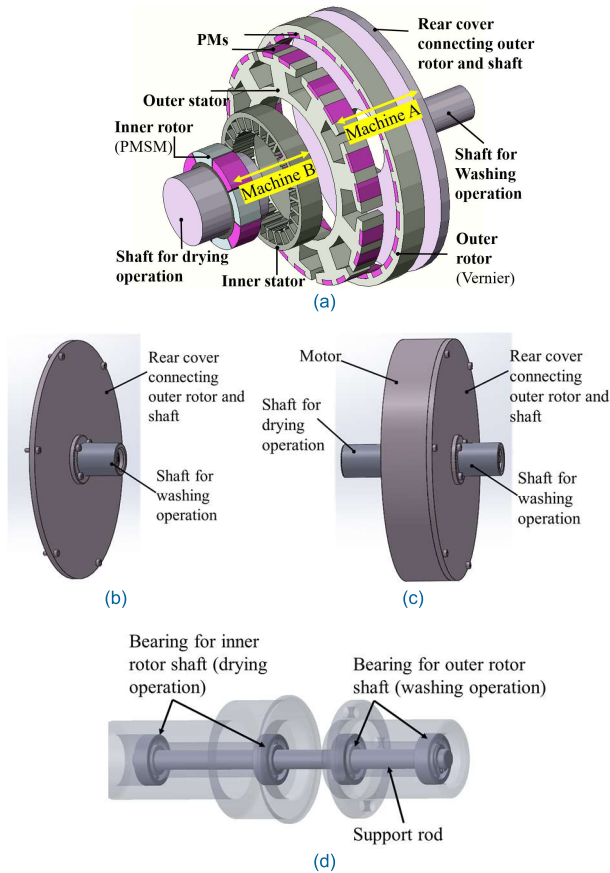
In this paper, a low-cost dual-mechanical-port dual-excitation machine is proposed for the washing machine application to circumvent the abovementioned demerits of the existing machine. The proposed motor is more cost-effective because of the cheaper PM and inverter. This is due to the alternate topologies proposed for the outer and inner rotors. Moreover, the proposed machine provides similar efficiencies as the existing machine. The proposed topology and its working principle are explained in Section II. The design considerations of the proposed topology are elaborated on in Section III. The performance analysis of the proposed machine using the finite element method is presented in Section IV. Finally, to verify the merits of the proposed machine, it is compared with the existing machine in terms of efficiency, power factor, and magnet price.

## II. TOPOLOGY AND WORKING PRINCIPLE

### A. TOPOLOGY

The configuration of the proposed topology is shown in Fig. 1. It is a combination of two machines, one nested into the other. The outer rotor and outer stator are referred to as Machine A, whereas the inner stator and inner rotor are referred to as Machine B.

Machine A is a dual-consequent-pole vernier machine [29]. It has an outer-rotor and inner-stator topology. It deploys one set of low-cost PMs (ferrite) on the rotor and another set of the PMs of the same grade on the stator. The stator of Machine A is comprised of the flux-modulation teeth with three-phase armature windings. Moreover, PMs are inserted between the flux-modulation teeth that are radially magnetized. The rotor of Machine A is composed of consequent-pole PMs along with iron teeth. The flux of the stator PMs and rotor PMs are both channeled outwards. It should be noted that the dual-consequent-pole vernier machine is selected for washing operation because of its high torque density. This is necessary because low-cost ferrite magnets with low  $B_r$  are desirable for their cost-effectiveness, which otherwise will reduce the torque density of the machine, which in turn will affect the efficiency of the machine. Hence, the dual-consequent-pole vernier machine



**FIGURE 2.** Exploded view of proposed topology (a) Exploded view (b) outer rotor and shaft connection method (c) motor with two shafts (d) bearings for shafts.

is desirable because its use of ferrite magnets ensures affordability and high efficiency for low-speed operations.

Machine B is a conventional surface-type PMSM. The stator is composed of 27 slots with four pole-pairs of armature windings, whereas the rotor consists of four pole-pairs of ferrite magnets. The number of slots and poles are selected to achieve the lowest possible torque ripple. A flux barrier is incorporated between the stators of Machines A and B (Fig. 1), which eliminates the magnetic coupling between the two machines. It is worth noting that the drying operation requires low torque. Therefore, a PMSM with ferrite magnets is the optimal choice for it because of its low-cost and high efficiency for high-speed operations.

The exploded view of the proposed topology is shown in Fig. 2(a). To perform washing and drying operations, two shafts are introduced to both sides of the machine. The inner rotor is directly connected to one side of the shaft, and it is used for the drying operation. The outer rotor is connected to a rear cover that is attached to the shaft on the other side, as shown in Fig. 2(b). It is connected such that when the outer rotor rotates, the connected cover rotates, which causes the shaft on the other side to rotate, thus enabling washing operations.

It should be noted that the washing drum and drying drum are not connected to each other. The outer rotor is connected

to the washing drum, and the inner rotor is connected to the drying drum. The two shafts are independent of each other, as shown in Fig. 2(c). When the outer rotor shaft rotates, the inner rotor may or may not rotate, depending on the requirement of the end user during the drying operation. To keep the two shafts independent of each other, bearing was installed on both sides of each shaft as shown in Fig. 2(d). Due to these bearings, both shafts can rotate independently of each other.

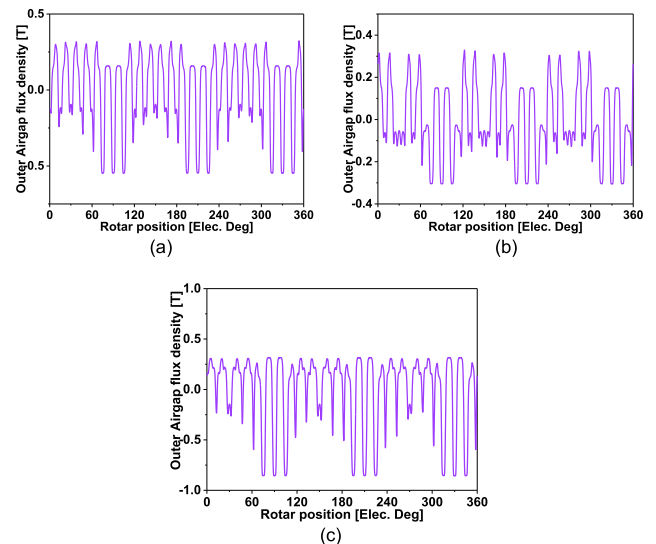
**B. WORKING PRINCIPLE**

Machine A is a dual-consequent-pole vernier machine. It is the combination of a stator consequent-pole PM vernier machine and a rotor consequent-pole PM vernier machine. Its working principle is based on the flux modulation principle [30], [31]. Machine A satisfies equation (1) to generate the flux modulation effect:

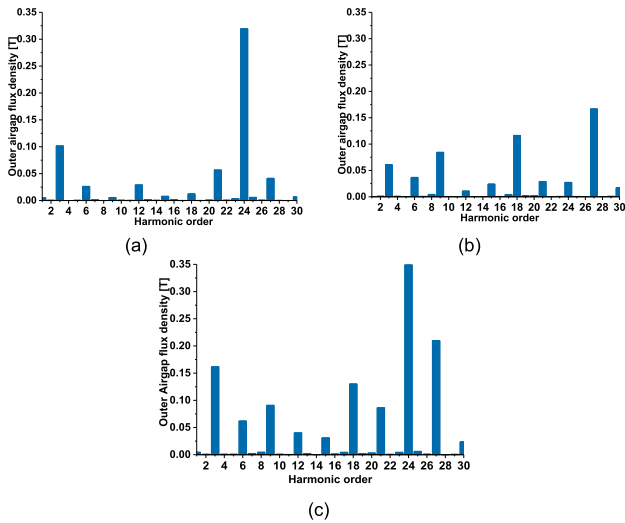
$$Z_r = Z_s - P \tag{1}$$

where  $Z_r$  is the number of rotor pole pairs,  $Z_s$  is the number of stator slots, and  $P$  is the number of armature pole pairs.

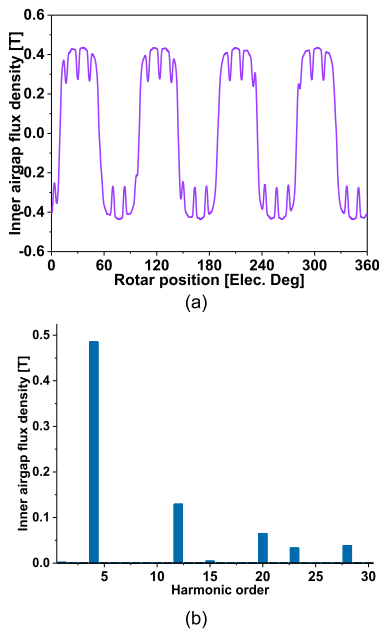
The flux from the rotor PMs is modulated by the stator flux-modulation teeth that produce a component equal to the stator-winding pole-pairs in the airgap flux density. The flux from the stator PMs is modulated by the rotor iron teeth, and produces a component equal to the winding pole pairs in the airgap. Therefore, the flux of both the rotor and stator PMs are modulated, and induce a back electromagnetic force (EMF) of the same frequency in the stator windings of Machine A. The working principle can be better explained by analyzing the airgap flux density in three conditions: with only rotor PMs, with only stator PMs, and with both stator and rotor PMs. The outer airgap flux-density of Machine A in these three conditions is shown in Fig. 3(a), 3(b), and 3(c), respectively.



**FIGURE 3.** Airgap flux density (a) only rotor PMs (b) only stator PMs (c) both stator and rotor PMs.



**FIGURE 4.** Airgap flux density harmonic spectra (a) only rotor PMs (b) only stator PMs (c) both stator and rotor PMs.



**FIGURE 5.** Airgap flux density Machine B (a) Waveform (b) Harmonic spectra.

The measurement of the airgap flux density reveals 24 pole pairs, because there are 24 pole pairs of rotor under all the three conditions. The harmonic spectra of the outer airgap flux density in the three conditions are shown in Fig. 4(a), 4(b), and 4(c), respectively. In Fig. 4(a), the harmonics of the airgap flux density with only rotor PMs are shown. The two working harmonics are the 3rd pole-pair-modulated component and the 24th pole-pair component, indicating the number of rotor PMs. The values of the 3rd and 24th harmonics are approximately 0.1 T and 0.33 T, respectively. The 3rd harmonic is the modulated component that is obtained under two conditions (with only stator PMs and only rotor PMs). When both stator and rotor PMs are

used, as shown in Fig. 4(c), the magnitude of this component is summed, which increases the back EMF, and consequently, the torque density in this topology. Moreover, additional working harmonics (such as 6, 12, 15, 21, and 30) are introduced in the airgap that produces the torque. This is because they are tooth harmonics of the 3rd harmonic (fundamental harmonic). The proposed Machine A has nine stator slots; thus, the 9k plus or minus 3 are tooth harmonics. Furthermore, some harmonics (such as 18 and 27) that result from the stator PM magneto-motive force (MMF) (18-pole pair) and air-gap permeance harmonic (9-pole pair), produce torque ripple. The 18th harmonic results from the stator PM MMF (18-pole pair) and the dc-term of the air-gap permeance; thus, it is stationary, and will not produce fundamental back EMF and average torque. The 27th harmonic is produced by the stator PM MMF (18-pole pair) and 9-pole-pair stator permeance; thus, it is also stationary and will not produce fundamental back-EMF. Machine A is utilized at the low speed of 50 rpm because of its higher torque density. It should be noted that the ferrite PMs are used to reduce the cost of the machine.

Machine B functions like a synchronous machine, because it is a conventional PMSM. The rotor PMs and stator windings have equal numbers of pole pairs. The airgap flux density and harmonic spectra of Machine B (inner airgap) are shown in Fig. 5(a) and 5(b), respectively. It can be observed that the airgap shows the 4-pole-pair main component, the number of the rotor pole pairs. The equal pole pairs of the stator and rotor interact to produce torque. Moreover, because Machine B is a conventional PMSM with few pole pairs, its armature frequency is not high, thus limiting the core losses of the machine. Machine B is used for the drying operation (1400 rpm). However, additional harmonics, such as the 12th and 20th, are present in the airgap flux density, thus producing torque ripple.

### III. DESIGN CONSIDERATIONS FOR THE PROPOSED TOPOLOGY

The design flow chart of the proposed topology is shown in Fig. 6. Initially, the topology of Machine A is selected. As we intend to use ferrite magnets at the low speed of 50 rpm, a machine with high torque density is required to compensate for the low residual flux-density of the ferrite magnets. Thus, for Machine A, the double-consequent-pole vernier machine was selected because of its higher torque density that was achieved based on the double flux modulation principle discussed earlier. To maintain the compactness of the washing machine, the outer diameter of the motor should not be very large, neither should the stack be very long. Therefore, the outer diameter of the machine was set to 280 mm, while the stack length was set to 25 mm. Moreover, natural cooling is selected for the machine.

Initially, an outer-rotor vernier machine is designed for the washing operation. Because high efficiency is required at 50 rpm, it is necessary to minimize the losses of the machine. At 50 rpm, the major losses of the machine are copper losses.

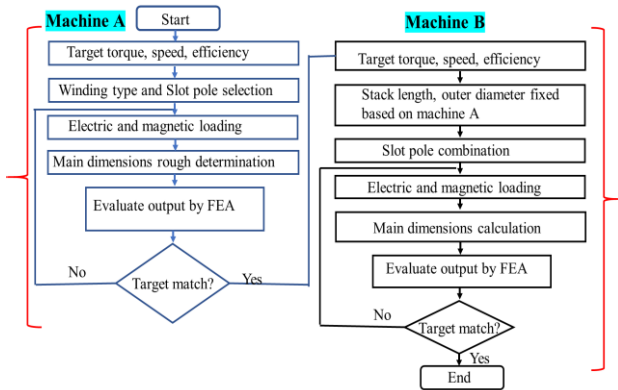


FIGURE 6. Design flow chart of Proposed topology.

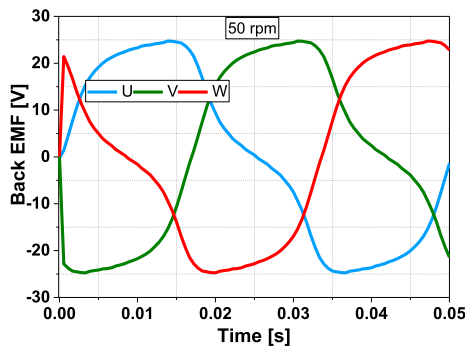


FIGURE 7. Back EMF of Machine A.

Hence, to minimize the copper losses, concentrated winding is employed in the stator of Machine A. The concentrated winding has a short end winding length, which corresponds to minimal copper losses. In addition, the pole ratio is also taken into consideration when selecting the pole-slot combination. The pole ratio is the ratio of the rotor pole pairs to the stator pole pairs; it affects the torque capability of the vernier machine. The pole-slot combination of Machine A is selected such that the pole ratio is 8. This pole ratio produces a high torque density with the employed fractional-slot concentrated winding. The initial main parameters, such as the airgap diameter, number of turns/phase, and stator current of the machine, are determined based on the design algorithm. Subsequently, finite element analysis (FEA) was performed to refine the parameters. Additional design considerations were made to select the optimal split ratio, which is defined as the ratio of the rotor’s inner diameter to the outer diameter. The higher split ratio provides a higher torque density; however, the resultant reduction in the width of the rotor core causes saturation that inevitably results in higher torque ripple and higher core losses. Following the FEA, the split ratio of 0.9 was determined to be the ideal. Furthermore, geometrical parameters, such as the auxiliary tooth width, slot depth, and slot opening, have a significant impact on the torque performance in vernier machines. These parameters were optimized using the genetic algorithm. All the results presented for Machine A are the final optimized results.

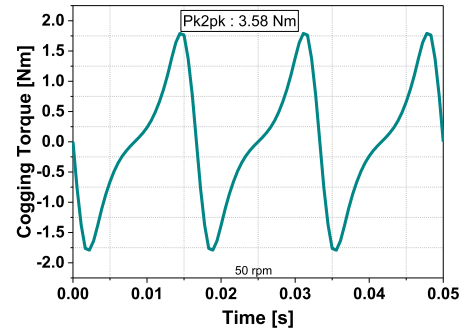


FIGURE 8. Cogging torque of Machine A.

After finalizing the parameters of Machine A, the thickness of the flux barrier was determined using iterative optimization to eliminate the magnetic coupling between Machines A and B. Because Machine B is to be nested inside the available space within Machine A, the outer diameter of Machine B cannot exceed the inner diameter of the flux barrier. Furthermore, the overall size of the machine remains unchanged because the stack length of Machine B is set to 25 mm, same as that of Machine A. The machine design algorithm is adhered to, and the main dimensions of Machine B are determined and refined using FEA. It should be noted that it was discovered that the slot area for coils was small in Machine B because of size restrictions. Hence, the coil diameter size was finally designed to be small to adjust the required number of turns, resulting in high copper losses in Machine B. Additionally, semi-closed slots were selected for Machine B to minimize the cogging torque. The width and height of the inner-rotor PMs were finalized based on iterative optimization. The main parameters of the proposed machine are shown in Table 1.

#### IV. PERFORMANCE ANALYSIS AND COMPARISON

In this section, the performance of the proposed machine is analyzed using 2D FEA. The commercial software, “JMAP version 17,” was used for the FEA.

##### A. PERFORMANCE OF MACHINE A

The back EMF of Machine A during the washing operation (50 rpm) is shown in Fig. 7. Distortions can be seen in the back EMF. This is because of the harmonics in the outer airgap flux density of Machine A due to the dual-consequent-pole structure of the machine.

The cogging torque of Machine A during the washing operation is shown in Fig. 8. It can be observed that a peak-to-peak cogging torque of 3.58 Nm is obtained in the proposed Machine A. This is attributable to the selected pole-slot combination for Machine A. The selected pole-slot combination and the dual-consequent-pole structure produce higher torque density; however, its drawback is the higher cogging torque.

The output torque of Machine A is shown in Fig. 9. An average torque of 17.4 Nm is obtained with a torque ripple of 15%. The torque ripple is mainly attributable to the additional harmonics in the airgap flux density. The flux

TABLE 1. Main parameters of conventional, existing, and proposed topology.

Parameters	Unit	Value				
		Conventional	Existing		Proposed	
Machine type	-		Machine I	Machine II	Machine A	Machine B
Sub-category	-	-				
Machine outer diameter	mm			280		
Stack length	mm			25		
Flux barrier length	mm	-			3	
Airgap length	mm	1	1	0.5	1	0.5
Stator outer diameter	mm	265	239	164	250	148
Stator inner diameter	mm	200	170	108.8	154	106
No. of turns / phase	-	396	400	900	480	540
No. of slots	-	36	12	6	9	27
PM pole pairs	-	24	24	6	24	4
PM volume	mm <sup>3</sup>	48000	22200	25475	124000	81625
PM grade	-		NdFeB (Neomax-50)		Ferrite (YBM_9BE)	
PM residual flux density	-		1.44		0.4	

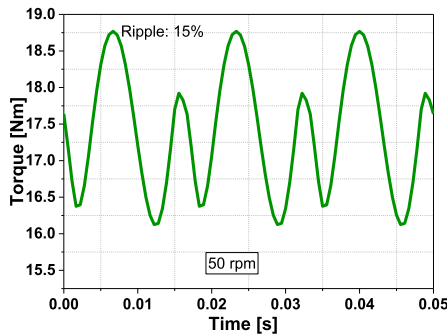


FIGURE 9. Output torque of Machine A.

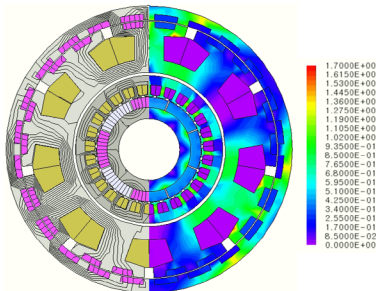


FIGURE 10. Flux lines and flux density distribution.

lines and flux density of the proposed machine at 50 rpm is shown in Fig. 10. It can be observed that there is no coupling between Machines A and B. Moreover, most components of the machine operate under the saturation limit of 1.8 T.

The copper and iron losses of the proposed machine were calculated to obtain the efficiency calculations. The efficiency of Machine A was calculated using equation (2):

$$\eta = \frac{P_{out}}{P_{out} + P_{cu} + P_{iron}} \times 100 \quad (2)$$

where  $P_{out}$ ,  $P_{cu}$ , and  $P_{iron}$  represent the output power, copper losses, and iron losses, respectively. The iron losses of the proposed machine were found to be 2.5 W. The copper losses

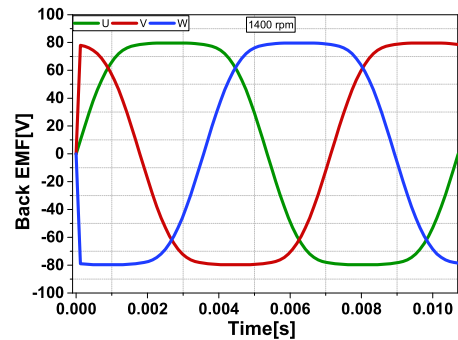


FIGURE 11. Back EMF of machine B.

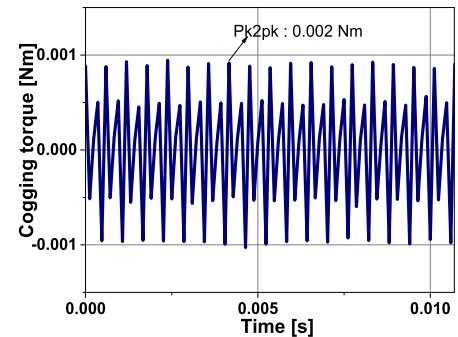


FIGURE 12. Cogging torque of machine B.

were higher. The efficiency of the proposed Machine A based on the copper and iron losses was 89.4%.

### B. PERFORMANCE OF MACHINE B

Machine B is used for the drying operations of the washing machine. The drying operation is performed at a high speed of 1400 rpm.

The back EMF of Machine B at 1400 rpm is shown in Fig. 11. It can be observed that smooth and sinusoidal back EMF is received. The cogging torque of Machine B is shown in Fig. 12. It can be observed that the peak-to-peak



higher magnet volume, the cost price of ferrite PMs per kg is much lower than that of NdFeB magnets. Therefore, overall, the PMs used in the proposed machine are cheaper. The proposed machine provides a similar efficiency as the existing machine at both speeds, even with the usage of low-cost ferrite magnets. This is owing to the better performance of the selected topologies for Machine A (washing operation) and B (drying operation). The power factor of the conventional machine is the same as the proposed drying operation; however, its efficiency is lower. The overall cost of the machine will be further low because of the high power factor of the proposed topology during drying operation.

## V. CONCLUSIONS

This paper proposed a topology to achieve high efficiency at the two operations points of a washing machine while ensuring low overall cost compared to an existing machine. The proposed topology was an integration of two machines, a dual-consequent-pole vernier machine and a permanent magnet synchronous machine (PMSM). The design considerations of the proposed machine were presented in detail in this paper. In addition, the proposed machine was compared with an existing dual-output machine to demonstrate the superiority of the proposed machine. The results showed that the proposed machine provided high efficiencies for both the washing and drying operations. The power factor for the drying operation of the proposed machine was high. Therefore, the inverter rating was reduced. Moreover, the PMs were also cheaper, because low-cost ferrite magnets were utilized. Therefore, the drive will be more affordable than the existing machine.

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