

Received April 14, 2019, accepted May 5, 2019, date of publication May 22, 2019, date of current version June 6, 2019.

Digital Object Identifier 10.1109/ACCESS.2019.2918345

# Power Control for Clustering Car-Following V2X Communication System With Non-Orthogonal Multiple Access

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This work was supported in part by the National Natural Science Foundation of China under Grant 61872406 and Grant 61472094, and in part by the Key Research and Development Plan Project of Zhejiang Province under Grant 2018C01059.

**ABSTRACT** Vehicle clustering has been utilized for reducing the complexity of vehicle-to-everything (V2X) communications that would ultimately improve road traffic efficiency. Using a car-following model in a V2X communication system, we propose a vehicle clustering method for dynamically classifying vehicles and adjusting cluster size in real time. The especially important issue for the selected cluster-head vehicles (CHVs) can achieve an optimal trade-off between the CHVs' relative speed and power allocation. Furthermore, in order to balance the power allocation among the CHVs to further increase the downlink throughput, a power control approach for non-orthogonal multiple access (NOMA) is proposed. In this approach, the power allocation coefficients are obtained by maximizing the achievable rate while meeting the predefined target rate of each NOMA user. Finally, numerical simulations are provided to confirm the theoretical results and demonstrate the superior performance of the proposed approach. Note that through the numerical simulations, we can find the critical point of maximizing the minimum achievable rate among the CHVs at low transmission power of base station (BS).

**INDEX TERMS** Power allocation, non-orthogonal multiple access, vehicular networks, cooperative communication, vehicle-to-everything communications.

## I. INTRODUCTION

Recently, vehicle-to-everything (V2X) communications have attracted widespread attention in academia and industry for their providing more efficient, smarter, and safer road traffic [1]–[3]. V2X communications typically include vehicle-to-vehicle (V2V), vehicle-to-infrastructure (V2I) and vehicle-to-pedestrian (V2P) transmissions to enable real-time traffic information exchange among vehicles, pedestrians and infrastructure [4]–[6]. The main present challenge in developing V2X communications is to address the issues of severe data congestion and low access efficiency caused by the ever-increasing number of connected vehicles in vehicular networks [7], [8]. Non-orthogonal

multiple access (NOMA) is a promising technique for the fifth-generation (5G) wireless systems, which not only meets growing traffic requirements but also enables large-scale device connectivity [9]–[11]. Therefore, the combination of NOMA technology in vehicular networks enables multiple vehicles to simultaneously transmit information on the same channel, thereby alleviating the resource conflicts such as limited transmission capacity and unpredictable propagation delays in V2X communications [12], [13].

It is well known that the vehicular networks are dynamic due to the real-time change of road traffic, thereby inevitably bringing about the problem of unstable network topology [14]–[16]. However, a clustering method has been proposed that makes the network topology hierarchical and scalable by establishing a connectivity graph between vehicular networks nodes [17], and supports data dissemination

The associate editor coordinating the review of this manuscript and approving it for publication was Fuhui Zhou.

through cluster head nodes to reduce the complexity of end-to-end communication [18], [19]. This clustering method has been widely employed in V2X communications to improve the performance of vehicular network [20]–[24]. The authors in [20] utilized a clustering method for predicting the movement of vehicle groups to increase the connection probability of V2V communications. Although the node with the largest link duration is selected as the cluster head in this method, the stability of the vehicle cluster may still not be maintained due to dynamic road traffic. In [21], a stable clustering method based on vehicular multi-hop communication was proposed, which adopts the relative mobility metric between vehicles to select out the cluster-head vehicles (CHVs). However, in order to increase the packet transmission rate among vehicles, this method causes a certain degree of propagation delay. For improving the end-to-end latency for vehicular network topology, a cluster-based protocol for selecting the optimal intersection CHV on the basis of real-time traffic was proposed in [22]. However, this protocol causes too much overhead for the vehicle cluster. In [23], an evolutionary game method for optimizing vehicle clustering was proposed to reduce the overhead of cluster recombination in vehicular networks. Although the method can automatically classify the vehicles and pick out CHVs, it just considers the average speed of vehicles rather than the dynamic speed of each vehicle. In [24], a dynamic clustering algorithm for considering real-time speed and position of vehicles was proposed. However, this algorithm needs as input the length of the cluster in order to create the vehicles clustering. In fact, pre-estimating the length of different vehicle clusters for dynamic road traffic is complicated as well as inconvenient. In this paper, we propose a clustering method that not only dynamically classifies vehicles but also adjusts cluster size according to real-time road traffic. Furthermore, the selected CHVs by this method can achieve an optimal trade-off between the CHVs' relative speed and power allocation.

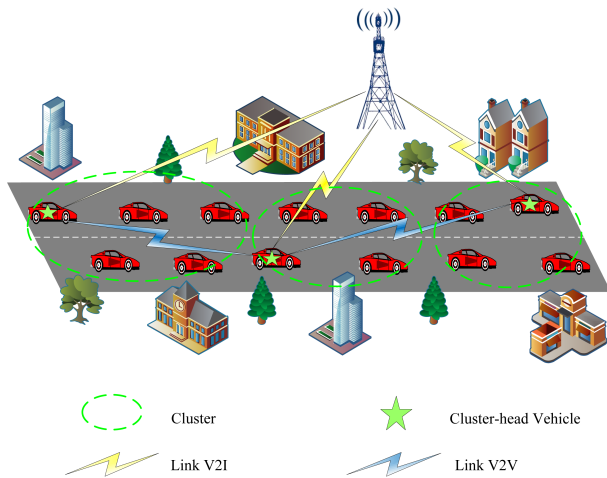
The expansion of vehicular networks has resulted in a tremendous increase in energy consumption, and power control is an effective way to reduce the power consumption without degrading both the connectivity and the coverage of vehicular networks [25], [26]. To balance the power allocation among CHVs to further increase the downlink throughput, the power control method is applied in V2X communications. As described above, NOMA has developed power-domain multiplexing to meet the requirements of high overload transmission [12]. Motivated by this, some researchers have studied power control schemes in V2X communications based on NOMA [13], [27]–[29]. In [27], a NOMA-based power allocation algorithm with opportunistic constraints is proposed to increase the throughput of V2X communications. For pursuing the robustness in vehicular communication, the algorithm only relies on the distance between the BS and vehicles to allocate the transmission power, thereby ignoring the dynamic power allocation issues of vehicles switching between different base stations. In [28], a NOMA-enabled hierarchical power control method was

proposed for dynamically power allocation from BSs to vehicles which optimizes the energy efficiency of the vehicular networks. Although this method exhibits excellent performance in terms of switching rate as well as spectrum efficiency, it inevitably has a certain degree of feedback delay. In order to avoid the access delay and matching instability caused by the mobility of vehicles, a hybrid power control scheme based on NOMA was proposed in [13]. This scheme autonomously allocates power-domain resources in a centralized and distributed manner through the BS and vehicles, respectively. Nevertheless, its multiplexing performance is inferior to the power control approach mentioned in [29]. The approach in [29] took full advantage of the cooperative performance of multiple-input multiple-output (MIMO) and NOMA, which maximizes bandwidth efficiency by multi-antenna spatial diversity and power-domain multiplexing. In recent years, NOMA-based cooperative transmission has been considered as a virtual MIMO scheme that can improve bandwidth efficiency of the system and reliability of users communication [30], [31]. In [32], a NOMA-based cooperative method is utilized to improve the performance of V2X communications with an emphasis on enhancing the throughput of remote transmission links. However, the corresponding throughput to the farthest transmission link is not always the smallest since the user in this link is assigned a maximum power allocation. Therefore, we propose a power control strategy based on NOMA cooperative transmission to maximize the achievable rates of CHVs, where the proposed power control strategy not only improves the throughput of the vehicular networks but also balances the power allocation among CHVs.

The rest of this paper is organized as follows. Section II describes the system model. Section III proposes a clustering algorithm and power allocation strategy. Section IV provides numerical simulation results and discussions. Finally, Section V concludes this paper.

## II. SYSTEM MODEL

Car-following model is a microscopic traffic flow model in which vehicles are traveling on a single line [33], [34]. Vehicles on the road have a certain degree of interaction due to their own mobility [21], thus the car-following model can capture the driving state of vehicles by variables such as speed and position [35]–[37]. Focusing on the impact of real-time traffic and road conditions for V2X communication system, a clustering car-following model is shown in Fig. 1, where each cluster includes the vehicles in green ellipsis area, and the CHVs are marked with a star symbol. The BS firstly uses a NOMA technique to send messages to the CHVs, and then the CHVs utilize a cooperative method to share inter-cluster information. Finally, other vehicles in each cluster only need to receive the broadcast messages from their CHVs. On the one hand, the hierarchical topology structure in vehicular network is established by the clustering method. On the other hand, the CHV acts as a local controller to support data dissemination between cluster members and clusters,



**FIGURE 1.** A clustering car-following model for V2X communications system.

which reduces the complexity of end-to-end communication in vehicular network. Therefore, the communication complexity of vehicular network topology can be reduced.

A downlink transmission scenario which contains a BS and three CHVs to preform NOMA is shown in Fig. 2. According to the near-far effect, the power-domain NOMA allocates less power resources to users with good channel gains. The tri-user mode not only representatively presents the power domain differences between users, but also facilitates the analysis and deployment of cooperative NOMA. Therefore, three CHVs' power allocation are enough to demonstrate the key aspects of power allocation among vehicles while avoiding unnecessary complications. Note that although we limit ourselves to three CHVs, the proposed approach can be extended to multiple CHVs. In Fig. 2, the BS and CHV-3 are regarded as the “source” node and the destination node; CHV-1 and CHV-2 are considered as the destination nodes or the relay nodes, respectively. The distance between the BS and the three CHVs satisfies  $d_{B1} < d_{B2} < d_{B3}$ . We assume

that the BS sends the message to three CHVs with a total transmission power  $P_B$ , and each CHV is equipped with an antenna and it operates in half-duplex mode. We divide the message transmission process into two phases. The first phase is the transmission of V2I links, where the BS sends the total superposition message to three CHVs, respectively. The second phase is the transmission of V2V links (i.e., links CHV-1→CHV-2 and CHV-2→CHV-3), where the amplify-and-forward (AF) protocol is employed by CHV-1 and CHV-2. For V2I communications where only the receivers are in motion, some theoretical analysis and experimental results demonstrate that the received signal amplitude of V2I links may follow the Rayleigh distribution [38], [39]. Note that the propagation channels of V2V communications are more dynamic than those in V2I, thus the envelope of the resulting narrowband impulse response should be modeled using the dual-Rayleigh distribution [40], [41]. Therefore, the channels of V2I communication scenarios can be modeled as Rayleigh fading, while the channels of V2V communication scenarios are modeled as dual-Rayleigh fading.

The total message sent by BS to the three NOMA-based CHVs is denoted as

$$x = \sqrt{P_B} \cdot \sum_{i=1}^3 a_i x_i, \tag{1}$$

where  $a_i^2$  ( $i = 1, 2, 3$ ) is the power allocation coefficient,  $x_1, x_2$  and  $x_3$  are the messages that satisfy  $E[|x_i|^2] = 1$ . According to the channel qualities, we assume  $0 < a_1^2 < a_2^2 < a_3^2$  and  $a_1^2 + a_2^2 + a_3^2 \leq 1$ . In the first phase, the signals received by CHV-1, CHV-2 and CHV-3 are respectively given by

$$y_{B \rightarrow 1}^1 = x h_{B1} + n_1, \tag{2}$$

$$y_{B \rightarrow 2}^1 = x h_{B2} + n_2, \tag{3}$$

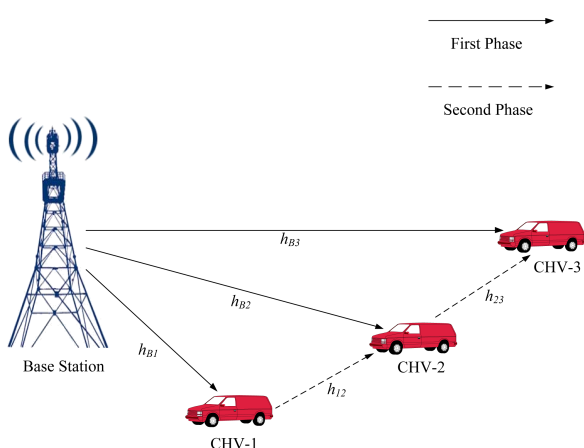
$$y_{B \rightarrow 3}^1 = x h_{B3} + n_3, \tag{4}$$

where  $h_{Bi}$  is the Rayleigh channel fading coefficient from BS to CHV, and follows the complex Gaussian distribution with the mean of zero and the variance of  $\Omega_{Bi}$ , i.e.,  $h_{Bi} \sim CN(0, \Omega_{Bi})$ . We assume that all channels are only affected by additive white Gaussian noise (AWGN),  $n_1, n_2$  and  $n_3$  are the AWGN with variance of  $N_0$  at CHV-1, CHV-2 and CHV-3, respectively.

To ensure that the received signals are successfully decoded and that there is successive interference cancellation (SIC) at CHVs [42], [43], we consider that the predefined target transmission rates of link BS CHV is lower than the corresponding achievable rates. In the case, for the transmission link BS CHV-1, we have

$$\begin{cases} R_{B \rightarrow 1}^{x_3} \leq \log_2(1 + \gamma_{B \rightarrow 1}^{x_3}) \\ R_{B \rightarrow 1}^{x_2} \leq \log_2(1 + \gamma_{B \rightarrow 1}^{x_2}) \end{cases}, \tag{5}$$

where  $R_{B \rightarrow 1}^{x_3}$  and  $R_{B \rightarrow 1}^{x_2}$  are the predefined target data rates of the messages  $x_3$  and  $x_2$  at CHV-1, respectively. The SINR for decoding the messages  $x_3$  and  $x_2$  at CHV-1 are respectively



**FIGURE 2.** Tri-CHV NOMA cooperative model.

denoted as

$$\gamma_{B \rightarrow 1}^{x_3} = \frac{\frac{P_B}{N_0} a_3^2 |h_{B1}|^2}{\frac{P_B}{N_0} (a_1^2 + a_2^2) |h_{B1}|^2 + 1}, \quad (6)$$

$$\gamma_{B \rightarrow 1}^{x_2} = \frac{\frac{P_B}{N_0} a_2^2 |h_{B1}|^2}{\frac{P_B}{N_0} a_1^2 |h_{B1}|^2 + 1}. \quad (7)$$

Therefore, the achievable data rates of the message  $x_1$  for the transmission link BS  $\rightarrow$  CHV-1 is given by

$$C_{B \rightarrow 1}^{x_1} = \log_2 (1 + \gamma_{B \rightarrow 1}^{x_1}), \quad (8)$$

where  $\gamma_{B \rightarrow 1}^{x_1}$  is the SINR for decoding the message  $x_1$  at CHV-1,

$$\gamma_{B \rightarrow 1}^{x_1} = \frac{P_B a_1^2 |h_{B1}|^2}{N_0}. \quad (9)$$

In order to realize SIC for the transmission link BS  $\rightarrow$  CHV-2, we have

$$R_{B \rightarrow 2}^{x_3} \leq \log_2 (1 + \gamma_{B \rightarrow 2}^{x_3}), \quad (10)$$

where  $R_{B \rightarrow 2}^{x_3}$  is the predefined target data rates of the message  $x_1$  at CHV-2, and  $\gamma_{B \rightarrow 2}^{x_3}$  is the SINR for decoding the message  $x_3$  at CHV-2,

$$\gamma_{B \rightarrow 2}^{x_3} = \frac{\frac{P_B}{N_0} a_3^2 |h_{B2}|^2}{\frac{P_B}{N_0} (a_1^2 + a_2^2) |h_{B2}|^2 + 1}. \quad (11)$$

After the message  $x_3$  are successfully decoded at CHV-2, the SINR for decoding the message  $x_2$  at CHV-2 is given by

$$\gamma_{B \rightarrow 2}^{x_2} = \frac{\frac{P_B}{N_0} a_2^2 |h_{B2}|^2}{\frac{P_B}{N_0} a_1^2 |h_{B2}|^2 + 1}, \quad (12)$$

and the achievable data rates of the message  $x_2$  for the transmission link BS  $\rightarrow$  CHV-2 is given by

$$C_{B \rightarrow 2}^{x_2} = \log_2 (1 + \gamma_{B \rightarrow 2}^{x_2}). \quad (13)$$

Since the signal power of the message  $x_3$  is stronger than messages  $x_2$  and  $x_1$ , the SINR for decoding the message  $x_3$  at CHV-3 is directly given by

$$\gamma_{B \rightarrow 3}^{x_3} = \frac{\frac{P_B}{N_0} a_3^2 |h_{B3}|^2}{\frac{P_B}{N_0} (a_1^2 + a_2^2) |h_{B3}|^2 + 1}, \quad (14)$$

and the achievable data rates for the transmission link BS CHV-3 is expressed as

$$C_{B \rightarrow 3}^{x_3} = \log_2 (1 + \gamma_{B \rightarrow 3}^{x_3}). \quad (15)$$

To ensure that the signals received by CHVs are successfully decoded in the first phase, we have

$$\begin{cases} R_{B \rightarrow 1}^{x_3} \leq \log_2 (1 + \gamma_{B \rightarrow 1}^{x_3}) \\ R_{B \rightarrow 1}^{x_2} \leq \log_2 (1 + \gamma_{B \rightarrow 1}^{x_2}) \\ R_{B \rightarrow 2}^{x_3} \leq \log_2 (1 + \gamma_{B \rightarrow 2}^{x_3}) \end{cases} \quad (16)$$

Under the constraints of predefined target rates and  $a_1^2 + a_2^2 + a_3^2 \leq 1$ , the power allocation coefficients are described as follows,

$$a_1^2 \in \left( 0, \frac{\gamma |h_{B1}|^2 - R_1 - R_2 (1 + R_1)}{\gamma |h_{B1}|^2 (1 + R_1) (1 + R_2)} \right], \quad (17)$$

$$a_2^2 \in \left( 0, \frac{\gamma |h_{B1}|^2 R_2 + R_2}{\gamma |h_{B1}|^2 (1 + R_1) (1 + R_2)} \right], \quad (18)$$

$$a_3^2 \in \left( 0, \frac{R_3 |h_{B2}|^2 (\gamma |h_{B1}|^2 - R_1)}{\gamma |h_{B1}|^2 |h_{B2}|^2 (1 + R_1)} + \frac{R_3 |h_{B1}|^2 (1 + R_1)}{\gamma |h_{B1}|^2 |h_{B2}|^2 (1 + R_1)} \right], \quad (19)$$

where  $\gamma = \frac{P_B}{N_0}$ ,  $R_1 = 2^{R_{B \rightarrow 1}^{x_3}} - 1$ ,  $R_2 = 2^{R_{B \rightarrow 1}^{x_2}} - 1$  and  $R_3 = 2^{R_{B \rightarrow 2}^{x_3}} - 1$ .

In the second phase (i.e., cooperative phase), CHV-1 transmits the decoded message  $y_{B \rightarrow 1}^1$  to CHV-2, while CHV-2 transmits the decoded message  $y_{B \rightarrow 2}^1$  to CHV-3. The cooperative transmission links CHV-1  $\rightarrow$  CHV-2 and CHV-2  $\rightarrow$  CHV-3 choose AF to forward the information. The corresponding amplify factors of links CHV-1  $\rightarrow$  CHV-2 and CHV-2  $\rightarrow$  CHV-3 are respectively given by [44]

$$\alpha = \sqrt{\frac{P_{V1}}{P_B |h_{B1}|^2 + N_0}}, \quad (20)$$

$$\beta = \sqrt{\frac{P_{V2}}{P_B |h_{B2}|^2 + N_0}}, \quad (21)$$

where  $P_{V1}$  and  $P_{V2}$  are the transmission power of CHV-2 and CHV-3, respectively. Therefore, the received signals by CHV-2 and CHV-3 can be expressed as

$$y_{1 \rightarrow 2}^2 = \alpha y_{B \rightarrow 1}^1 h_{12} + n_{12}, \quad (22)$$

$$y_{2 \rightarrow 3}^2 = \beta y_{B \rightarrow 2}^1 h_{23} + n_{23}. \quad (23)$$

The channels of links CHV-1  $\rightarrow$  CHV-2 and CHV-2  $\rightarrow$  CHV-3 are modeled as dual-Rayleigh fading,  $h_{12}$  and  $h_{23}$  are the products of two i.i.d (independent and identically distributed) complex Gaussian random variables [45], i.e.,  $h_{12} = h_{12}^x h_{12}^y$  and  $h_{23} = h_{23}^x h_{23}^y$ , where each of the random variable has zero mean and variance of  $\Omega_v$  per dimension. We make the following two realistic assumptions.

*Case I:* If  $a_3^2$  meets the following conditions

$$a_3^2 \in \left( 0, \frac{R_4 \gamma |h_{B1}|^2 \gamma_1 |h_{12}|^2}{\gamma |h_{B1}|^2 \gamma_1 |h_{12}|^2 (1 + R_4)} + \frac{R_4 (\gamma |h_{B1}|^2 + \gamma_1 |h_{12}|^2 + 1)}{\gamma |h_{B1}|^2 \gamma_1 |h_{12}|^2 (1 + R_4)} \right], \quad (24)$$

where we utilize  $Z = 0$  to describe the Case I. For the cooperative link CHV-1  $\rightarrow$  CHV-2, the message  $x_2$  failed to be decoded at CHV-2. In Case I, the information received at



CHV-2 does not obtain the cooperative gain, and the achievable data rates at CHV-2 is given by

$$C_2^{Z=0} = \log_2 (1 + \gamma_{B \rightarrow 2}^{x_2}). \quad (25)$$

Case II: If  $a_3^2$  meets the following conditions

$$a_3^2 \in \left( \begin{aligned} & \frac{R_4 \gamma |h_{B1}|^2 \gamma_1 |h_{12}|^2}{\gamma |h_{B1}|^2 \gamma_1 |h_{12}|^2 (1 + R_4)} \\ & + \frac{R_4 \gamma |h_{B1}|^2 \gamma_1 |h_{12}|^2}{\gamma |h_{B1}|^2 \gamma_1 |h_{12}|^2 (1 + R_4)}, \frac{R_3 |h_{B2}|^2 (\gamma |h_{B1}|^2 - R_1)}{\gamma |h_{B1}|^2 |h_{B2}|^2 (1 + R_1)} \\ & + \frac{R_3 |h_{B1}|^2 (1 + R_1)}{\gamma |h_{B1}|^2 |h_{B2}|^2 (1 + R_1)} \end{aligned} \right), \quad (26)$$

where  $\gamma_1 = \frac{P_{V1}}{N_0}$ ,  $R_4 = 2^{R_{1 \rightarrow 2}^{x_3}} - 1$ . We use  $Z = 1$  to depict the case II. At CHV-2, SIC will be realized for the cooperative link CHV-1  $\rightarrow$  CHV-2, i.e.,

$$R_{1 \rightarrow 2}^{x_3} \leq \log_2 (1 + \gamma_{1 \rightarrow 2}^{x_3}), \quad (27)$$

where  $R_{1 \rightarrow 2}^{x_3}$  is the predefined target data rates of cooperative link CHV-1  $\rightarrow$  CHV-2 with respect to the message  $x_3$ , and the corresponding SINR  $\gamma_{1 \rightarrow 2}^{x_3}$  for decoding the message  $x_3$  at CHV-2 is given by (28), as shown at the bottom of this page. After the message  $x_3$  are successfully decoded at CHV-2, the SINR for decoding the message  $x_2$  at CHV-2 can be expressed as

$$\gamma_{1 \rightarrow 2}^{x_2} = \frac{\frac{P_B}{N_0} a_2^2 |h_{B1}|^2 \frac{P_{V1}}{N_0} |h_{12}|^2}{\frac{P_B}{N_0} a_1^2 |h_{B1}|^2 \frac{P_{V1}}{N_0} |h_{12}|^2 + \frac{P_B}{N_0} |h_{B1}|^2 + \frac{P_{V1}}{N_0} |h_{12}|^2 + 1}, \quad (29)$$

and thus the achievable data rates at CHV-2 in Case II is denoted as

$$C_2^{Z=1} = \log_2 (1 + \gamma_{B \rightarrow 2}^{x_2} + \gamma_{1 \rightarrow 2}^{x_2}). \quad (30)$$

As for the cooperative transmission link CHV-2 CHV-3, the SINR for decoding the message  $x_3$  at CHV-3 is given by (31), as shown at the bottom of this page.

At the end of the second phase, maximum-ratio combining (MRC) [46], [47] is performed to detect the messages for CHV-2 and CHV-3. Consequently, the achievable data rates at CHV-1, CHV-2 and CHV-3 are respectively expressed as

$$C_1 = \frac{1}{2} \log_2 (1 + \gamma_{B \rightarrow 1}^{x_1}), \quad (32)$$

$$C_2 = \left[ \frac{1}{2} \log_2 (1 + \gamma_{B \rightarrow 2}^{x_2}) \right]^{1-Z}$$

$$\times \left[ \frac{1}{2} \log_2 (1 + \gamma_{B \rightarrow 2}^{x_2} + \gamma_{1 \rightarrow 2}^{x_2}) \right]^Z, \quad (33)$$

$$C_3 = \frac{1}{2} \log_2 (1 + \gamma_{B \rightarrow 3}^{x_3} + \gamma_{2 \rightarrow 3}^{x_3}). \quad (34)$$

### III. CLUSTERING ALGORITHM AND POWER ALLOCATION

#### A. VEHICLES CLUSTERING

There is a certain interaction between the vehicles on the road, and the car-following model as a microscopic traffic flow model can reflect the driving state of the vehicles on the road by speed and position. In this subsection, we can take the change of real-time traffic condition into account in the process of vehicles clustering, making the clustering algorithm more suitable for actual traffic scenarios. We firstly utilize the car-following distance to cluster the vehicles and adjust the cluster size according to the vehicle's relative speed and delay interval on the road. And then, joint vehicle relative speed and transmission power of vehicles are employed to select out CHVs.

We suppose that there are  $n$  ( $k = 1, 2, \dots, n$ ) vehicles near a BS in a single lane. The criterion for vehicles clustering is that the distance between the two adjacent cars is not farther than the minimum safety distance, and the coverage of the vehicle cluster is within the communication radius. According to the difference of the car-following distances between adjacent vehicles and the sum of the car-following distances in each cluster, we have

$$\begin{cases} |S_{k+1} - S_k| \leq d_{\min} \\ \sum_{k=1}^{w-1} S_k < D, \end{cases} \quad (35)$$

where  $w$  ( $j = 1, 2, \dots, w$ ) is the number of vehicles contained in a cluster,  $d_{\min}$  represents the minimum safe distance between the adjacent vehicles,  $D$  denotes the communication radius, and the car-following distance  $S_k$  is expressed as

$$S_k = d_{\min} + \Delta v \cdot \tau. \quad (36)$$

where  $\tau$  in formula (36) is the delay interval, and  $\Delta v$  represents the relative speed difference between adjacent vehicles, i.e.,

$$\Delta v = |v_k - v_{k-1}|, \quad (37)$$

where  $v_k$  denotes the speed of vehicle  $k$ .

After the vehicles on the road are clustered, we next proceed with the selection of CHVs. It is known that the transmission power assigned to each vehicle by BS is different, and there is also a difference in the speed of each vehicle within a cluster. Taking into account the above issues, in order to

$$\gamma_{1 \rightarrow 2}^{x_3} = \frac{\frac{P_B}{N_0} a_3^2 |h_{B1}|^2 \frac{P_{V1}}{N_0} |h_{12}|^2}{\frac{P_B}{N_0} (a_1^2 + a_2^2) |h_{B1}|^2 \frac{P_{V1}}{N_0} |h_{12}|^2 + \frac{P_B}{N_0} |h_{B1}|^2 + \frac{P_{V1}}{N_0} |h_{12}|^2 + 1} \quad (28)$$

$$\gamma_{2 \rightarrow 3}^{x_3} = \frac{\frac{P_B}{N_0} a_3^2 |h_{B2}|^2 \frac{P_{V2}}{N_0} |h_{23}|^2}{\frac{P_B}{N_0} (a_1^2 + a_2^2) |h_{B2}|^2 \frac{P_{V2}}{N_0} |h_{23}|^2 + \frac{P_B}{N_0} |h_{B2}|^2 + \frac{P_{V2}}{N_0} |h_{23}|^2 + 1} \quad (31)$$

select the vehicle with the lower relative speed and optimal transmission power as the CHV, we define the CHV selection parameter as

$$M_c = \max_c \left[ p_c \cdot \frac{P_V}{(w-1)} \cdot \sum_{j=1, c \neq j}^{w-1} |\bar{h}_{cj}|^2 (\bar{S}_{cj})^{-\alpha} \right], \quad (38)$$

where  $P_V$  is the transmission power of vehicle,  $\alpha$  is the path loss factor,  $\bar{h}_{cj}$  is the average channel gain between the CHV and its member vehicles, which follows dual-Rayleigh fading with zero mean and variance of  $\Omega_{cj}$  per dimension. We define  $p_c = P_c/P_T$ ,  $P_c$  is the transmission power required by BS to transmit the message to a certain vehicle in one cluster and  $P_T$  is the total transmit power of BS to send a message to all the vehicles inside the cluster. Here,  $\bar{S}_{cj}$  denotes the average normalized car-following distance between the CHV and its member vehicles,

$$\bar{S}_{cj} = \frac{d_{\min} + \Delta v_{cj} \cdot \bar{\tau}_{cj}}{\sum_{j=1, c \neq j}^{w-1} S_j}, \quad (39)$$

where  $S_j$  is the car-following distance among the member vehicles,  $\bar{\tau}_{cj}$  is the mean of the delay interval between the CHV and its member vehicles. The relative speed  $\Delta v_{cj}$  of CHV is given by

$$\Delta v_{cj} = \sqrt{\frac{1}{w-1} \sum_{j=1, c \neq j}^{w-1} \left( v_c - \frac{1}{w} \sum_{j=1}^w v_j \right)^2}, \quad (40)$$

where  $\Delta v_{cj}$  is obtained by calculating the standard deviation of the average speed between each vehicle and all the vehicles in the cluster.  $v_c$  and  $v_j$  represent the speeds of the CHV and the member vehicle, respectively.

## B. POWER ALLOCATION

Although we have already considered the transmission power ratio  $p_c$  as one of the significant factors affecting the selection of the CHV, there may be still a few CHVs with poor quality communication links due to being far away from the BS. We next propose an interval-based optimal power control scheme to maximize the achievable rates of CHVs while BS transmission power is limited, thereby improving the throughput of the vehicular network and balancing the power allocation among CHVs.

To simplify the analysis for the V2V communication process, we assume that CHVs have the same transmission power  $P_V$ , i.e.,  $P_{V1} = P_{V2} = P_V$ . In this case, the optimal power allocation problem (i.e., maximizing the minimum achievable rate of CHV at the limited transmission power of BS) can be given by

$$\begin{cases} \max_{P_i} \min [C_1(P_i), C_2(P_i), C_3(P_i)] \\ \text{s.t. } P_1 + P_2 + P_3 \leq P_B \\ P_i \geq 0, i = 1, 2, 3, \end{cases} \quad (41)$$

where  $P_1 = a_1^2 P_B$ ,  $P_2 = a_2^2 P_B$  and  $P_3 = a_3^2 P_B$ . We define  $P_B = P_i/a_i^2$ , then optimization problem (41) can be converted

into the following problem

$$\begin{cases} \max_{a_i^2} \min [C_1(a_i^2), C_2(a_i^2), C_3(a_i^2)] \\ \text{s.t. } a_1^2 + a_2^2 + a_3^2 \leq 1 \\ a_i^2 \geq 0, i = 1, 2, 3. \end{cases} \quad (42)$$

where  $a_i^2$  denotes the power allocation coefficient. Since the optimization problem formulated in (42) is non-convex, it's hard to directly obtain the solution. Therefore, we turn it into a series of linear optimization problems and adopt an interval-based dichotomy to solve them.

If the objective function is a quasi-concave function, the optimization problem is quasi-concave when its constraints are convex. The objective function in (42) is non-convex and its constraints are linear, which implies that the optimization problem is quasi-concave. As such, all the subsets of the objective function are concave. Here, we denote the subset of the objective function as [48]

$$\mathbb{C}_\theta = \left\{ \min [C_1(a_i^2), C_2(a_i^2), C_3(a_i^2)] \geq \theta, \theta \in \mathbb{R} \right\}, \quad (43)$$

and the constraints of  $\mathbb{C}$  can be expressed as

$$\begin{cases} a_1^2 \frac{P_B |h_{B1}|^2}{N_0} \geq 2^{2\theta} - 1 \\ a_2^2 \frac{P_B |h_{B2}|^2}{a_1^2 P_B |h_{B2}|^2 + N_0} \geq 2^{2\theta} - 1, (Z=0) \\ a_2^2 \left( \frac{P_B |h_{B1}|^2 \frac{P_V}{N_0} |h_{12}|^2}{a_1^2 P_B |h_{B1}|^2 N_0 \frac{P_V}{N_0} |h_{12}|^2 + P_B |h_{B1}|^2 + P_V |h_{12}|^2 + N_0} + \frac{P_B |h_{B2}|^2}{a_1^2 P_B |h_{B2}|^2 + N_0} \right) \geq 2^{2\theta} - 1, (Z=1) \\ a_3^2 \left[ \frac{P_B |h_{B2}|^2 \frac{P_V}{N_0} |h_{23}|^2}{(a_1^2 + a_2^2) P_B |h_{B2}|^2 \frac{P_V}{N_0} |h_{23}|^2 + P_B |h_{B2}|^2 + P_V |h_{23}|^2 + N_0} + \frac{P_B |h_{B3}|^2}{(a_1^2 + a_2^2) P_B |h_{B3}|^2 + N_0} \right] \geq 2^{2\theta} - 1, \end{cases} \quad (44)$$

Obviously, the inequalities in (44) are linear.

Here, we suppose  $\hat{\psi}$  is the optimal max-min value of (42). Finding the optimal value of  $a_i^2$  that satisfies the following conditions for a constant value  $\theta$  ( $\theta \geq 0$ ),

$$\begin{cases} C_i \geq \theta \\ a_1^2 + a_2^2 + a_3^2 \leq 1, \\ a_i^2 > 0 \end{cases}, \quad (45)$$

where  $C_i$  is the minimum achievable rate of CHVs. If the conditions (45) are feasible then we get  $\hat{\psi} \geq \theta$ , otherwise we

consider that  $\hat{\psi} \leq \theta$ . Equivalently, (45) can be re-formulated as

$$\begin{cases} \min a_1^2 + a_2^2 + a_3^2 \\ s.t. C_i \geq \theta, i = 1, 2, 3 \\ a_i^2 > 0. \end{cases} \quad (46)$$

In order to obtain the closed-form optimal solution of formula (46), we use the following proposition.

*Proposition 1:* For a constant value  $\theta$ , the optimization solution of formula (46) is given by

$$a_1^2 = \frac{(2^{2\theta} - 1)N_0}{P_B|h_{B1}|^2}, \quad (47)$$

$$a_2^2 = \left[ \frac{(2^{2\theta} - 1)|h_{B2}|^2 + |h_{B1}|^2}{P_B|h_{B1}|^2|h_{B2}|^2} \cdot (2^{2\theta} - 1)N_0 \right]^{1-Z} \times \left( \frac{2^{2\theta} - 1}{c + d} \right)^Z, \quad (48)$$

$$a_3^2 = \left( \frac{2^{2\theta} - 1}{m + n} \right)^{1-Z} \cdot \left( \frac{2^{2\theta} - 1}{p + q} \right)^Z, \quad (49)$$

where

$$c = \frac{P_B|h_{B1}|^2|h_{B2}|^2}{(2^{2\theta} - 1)|h_{B2}|^2N_0 + |h_{B1}|^2N_0}, \quad (50)$$

$$d = \frac{P_B|h_{B1}|^2P_V|h_{12}|^2}{(2^{2\theta} - 1)P_V|h_{12}|^2 + P_B|h_{B1}|^2 + P_V|h_{12}|^2 + N_0} \times \frac{1}{N_0}, \quad (51)$$

$$e = \frac{(2^{2\theta} - 1)N_0}{P_B|h_{B1}|^2} \cdot \left( 2^{2\theta} + \frac{|h_{B1}|^2}{|h_{B2}|^2} \right), \quad (52)$$

$$f = \frac{(2^{2\theta} - 1)N_0}{P_B|h_{B1}|^2} + \frac{2^{2\theta} - 1}{c + d}, \quad (53)$$

$$m = \frac{P_B|h_{B3}|^2}{e \cdot P_B|h_{B3}|^2 + N_0}, \quad (54)$$

$$n = \frac{P_B|h_{B2}|^2 \cdot \frac{P_V}{N_0}|h_{23}|^2}{e \cdot P_B|h_{B2}|^2 \cdot \frac{P_V}{N_0}|h_{23}|^2 + P_B|h_{B2}|^2 + P_V|h_{23}|^2 + N_0}, \quad (55)$$

$$p = \frac{P_B|h_{B3}|^2}{f \cdot P_B|h_{B3}|^2 + N_0}, \quad (56)$$

$$q = \frac{P_B|h_{B2}|^2 \cdot \frac{P_V}{N_0}|h_{23}|^2}{f \cdot P_B|h_{B2}|^2 \cdot \frac{P_V}{N_0}|h_{23}|^2 + P_B|h_{B2}|^2 + P_V|h_{23}|^2 + N_0}. \quad (57)$$

*Proof:* See Appendix.

To ensure the optimal values of satisfying conditions (17), (18), (19) and  $\sum_i^3 a_i^2 \leq 1$ , we design an interval-based optimal power control scheme as described in Algorithm 1. Here,  $\psi_L$  and  $\psi_U$  are the lower and upper limits of the initialized  $\mathbb{C}_\theta$ ,  $\hat{a}_i^2$  represents the optimal value of  $a_i^2$ ,  $\delta$  is a minimum value and denotes the accuracy range.

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**Algorithm 1** Interval-Based Optimal Power Control Scheme

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```

1 Input:  $\psi_L, \psi_U, \delta, Z, i = 1, 2, 3;$ 
2 While  $\psi_U - \psi_L \geq \delta$  do
3   Set  $\theta = \frac{\psi_U + \psi_L}{2}$ ;
4   Switch ( $Z$ )
5     Case I: Set  $Z = 0$  and solve the convex problem of
6       formula (46) to obtain the optimal  $a_i^2$ ;
7     if  $a_3^2 > \frac{R_4\gamma|h_{B1}|^2\gamma_1|h_{12}|^2 + R_4(\gamma|h_{B1}|^2 + \gamma_1|h_{12}|^2 + 1)}{\gamma|h_{B1}|^2\gamma_1|h_{12}|^2(1+R_4)}$ 
8       then
9          $\hat{a}_3^2 = \frac{R_4\gamma|h_{B1}|^2\gamma_1|h_{12}|^2 + R_4(\gamma|h_{B1}|^2 + \gamma_1|h_{12}|^2 + 1)}{\gamma|h_{B1}|^2\gamma_1|h_{12}|^2(1+R_4)}$ 
10        else  $\hat{a}_3^2 = a_3^2$ 
11        end if
12     break
13     Case II: Set  $Z = 1$  and solve the convex problem of
14       formula (46) to obtain the optimal  $a_i^2$ ;
15     if  $a_3^2 > \frac{R_3|h_{B2}|^2(\gamma|h_{B1}|^2 - R_1) + R_3|h_{B1}|^2(1+R_1)}{\gamma|h_{B1}|^2|h_{B2}|^2(1+R_1)}$ 
16       then
17          $\hat{a}_3^2 = \frac{R_3|h_{B2}|^2(\gamma|h_{B1}|^2 - R_1) + R_3|h_{B1}|^2(1+R_1)}{\gamma|h_{B1}|^2|h_{B2}|^2(1+R_1)}$ 
18        else  $\hat{a}_3^2 = a_3^2$ 
19        end if
20     break
21     if  $a_1^2 + a_2^2 + \hat{a}_3^2 \leq 1$  then
22       Set  $\psi_L = \theta, \hat{a}_1^2 = a_1^2, \hat{a}_2^2 = a_2^2, \hat{a}_3^2 = \hat{a}_3^2, \hat{\psi} = \theta;$ 
23     else  $\psi_U = \theta$ 
24     end if
25   end while
26   if  $\hat{a}_2^2 > \frac{\gamma|h_{B1}|^2R_2 + R_2}{\gamma|h_{B1}|^2(1+R_1)(1+R_2)}$  then
27      $\hat{a}_2^2 = \frac{\gamma|h_{B1}|^2R_2 + R_2}{\gamma|h_{B1}|^2(1+R_1)(1+R_2)}$ 
28   else  $\hat{a}_2^2 = a_2^2$ 
29   end if
30   if  $\hat{a}_1^2 > \frac{\gamma|h_{B1}|^2 - R_1 - R_2(1+R_1)}{\gamma|h_{B1}|^2(1+R_1)(1+R_2)}$  then
31      $\hat{a}_1^2 = \frac{\gamma|h_{B1}|^2 - R_1 - R_2(1+R_1)}{\gamma|h_{B1}|^2(1+R_1)(1+R_2)}$ 
32   else  $\hat{a}_1^2 = a_1^2$ 
33   end if
34 Output:  $\hat{a}_1^2, \hat{a}_2^2, \hat{a}_3^2.$ 

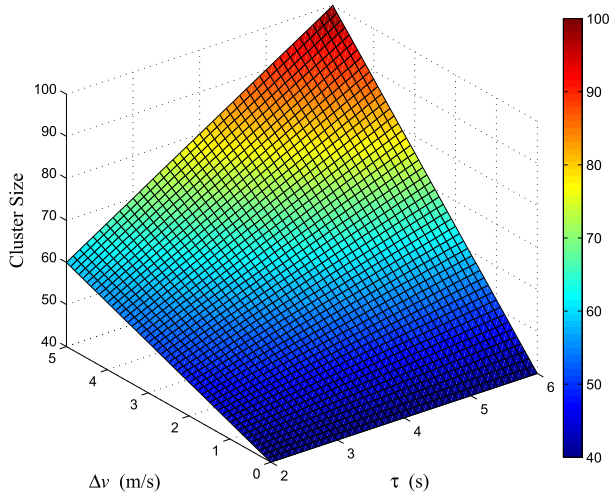
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**IV. NUMERICAL SIMULATION RESULTS**

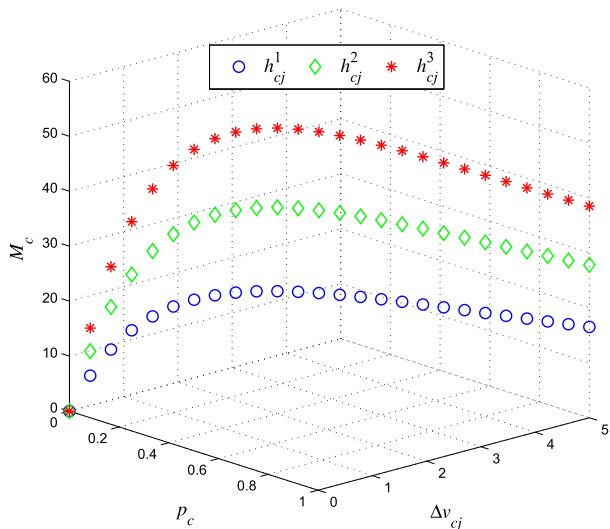
In this section, numerical simulation results are provided for evaluating the performance of the clustering algorithm and the proposed power allocation scheme. These results are compared with the conventional NOMA [31] as well as the fixed NOMA [49] algorithms. V2I and V2V transmission links are modeled as Rayleigh fading channel and dual-Rayleigh fading channel, respectively.

Fig. 3 shows the three-dimensional relationship among the size of vehicle cluster, the inter-vehicle speed difference and



**FIGURE 3.** The cluster size versus inter-vehicle speed difference ( $\Delta v$ ) and delay interval ( $\tau$ ).

delay interval. Here, we set  $d_{\min} = 20$  m and  $D = 100$  m. It is obvious that the coverage of vehicle cluster gradually expands as blue color turns red when the inter-vehicle speed difference and the delay interval are increasing, which implies that the algorithm dynamically adjusts the cluster size according to the actual traffic and road conditions. Moreover, it can be seen that the vehicle cluster size is maintained in the range of approximately 40-100 meters due to the limitation of the following distance between adjacent vehicles. Therefore, the adverse impact of the excessive size of cluster on communication quality of V2V links is reduced.



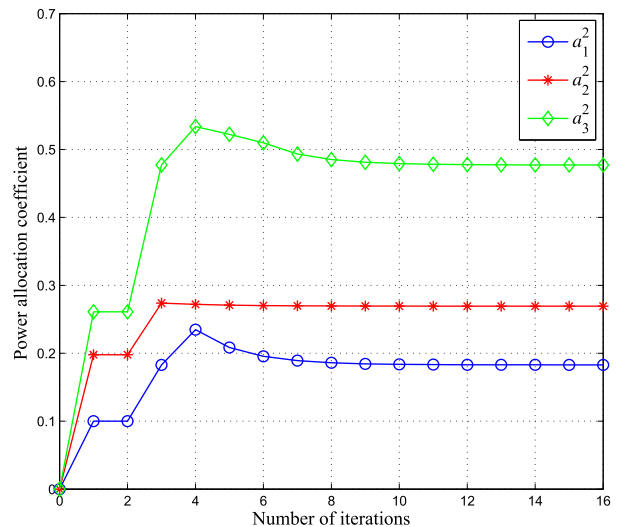
**FIGURE 4.** CHV selection parameter versus inter-vehicle speed difference ( $\Delta v_{cj}$ ) and transmission power ratio ( $p_c$ ) under different channel gains ( $\hat{h}_{cj}$ ).

Fig. 4 plots the relationship among CHV selection parameter, inter-vehicle speed difference and transmission power ratio under different channel gain conditions. Here, we set

the parameters as  $\bar{\tau}_{cj} = 5$  and  $P_V = 27$  dBm. The cluster size is set equal to 100 meters and the path loss factor is set as  $\alpha = 3$  [50]. The blue, green and red color curves correspond to different dual-Rayleigh fading channels coefficient  $\hat{h}_{cj}$  with per dimension variance  $\Omega_{cj}^1 = 3$ ,  $\Omega_{cj}^2 = 5$  and  $\Omega_{cj}^3 = 7$ , respectively. As we can be seen from Fig. 4, the CHV selection parameters of the blue curve are always larger than those of green and red under the same conditions of  $\Delta v_{cj}$  and  $p_c$ , i.e., the vehicle with bigger channel gain is easily selected as CHV. Furthermore, we can observe that  $M_c$  increases first and then decreases with the increase of  $\Delta v_{cj}$  and  $p_c$ . The corresponding extreme points of  $M_c$  are obtained when  $\Delta v_{cj} = 2$  and  $p_c = 0.4$ , which is favorable for selecting the CHV which can balance  $\Delta v_{cj}$  and  $p_c$  to maintain cluster stability and reduce overhead. As expected, the numerical simulation results are consistent with the analysis values.

As shown below in Fig. 5 to Fig. 9, we investigate the convergence of proposed power control algorithm and minimum achievable rate of CHV in two cases (Case I and Case II), respectively. We set some parameters as follows:  $\delta = 10^{-5}$ ,  $\psi_L = 0$  bit/s/Hz,  $N_0 = 1$ ,  $\psi_u = 1$  bit/s/Hz,  $P_B = 30$  dBm,  $P_V = 27$  dBm,  $\Omega_{B1} = 1$ ,  $\Omega_{B2} = 8$  and  $\Omega_{B3} = 9$ , respectively. Without loss of generality, the per dimension variance of dual-Rayleigh fading channels is set to  $\Omega_v = 3$ . We assume that the normalized distances between BS and CHVs are set as  $d_{B1} = 0.5$ ,  $d_{B2} = 0.7$  and  $d_{B3} = 1$ , respectively. The normalized distance between CHVs are set as  $d_{12} = 0.5$ ,  $d_{23} = 0.5$ , respectively. The path loss factor is set as  $\alpha = 3$ .

Fig. 5 and Fig. 6 illustrate the convergence of the proposed algorithm in Case I and Case II, respectively. As expected, it converges fast to the optimal power allocation coefficient about a few iterations, because power allocation coefficients  $a_1^2$ ,  $a_2^2$  and  $a_3^2$  only need the interval selection to be obtained quickly. Obviously, the numerical simulation results are consistent with the analysis values. Moreover, the



**FIGURE 5.** The convergence of the proposed algorithm in Case I.



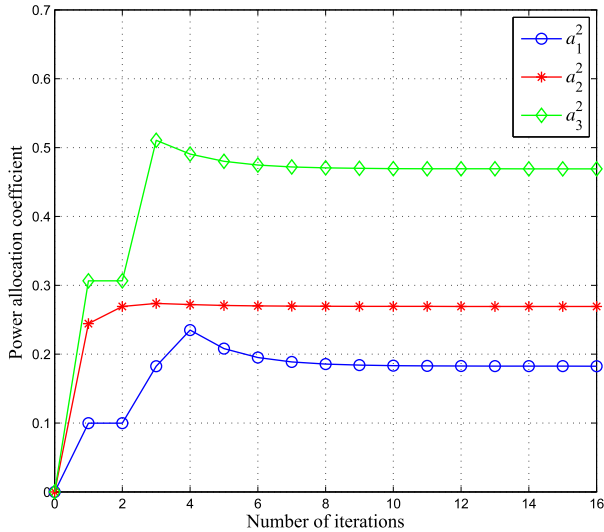


FIGURE 6. The convergence of the proposed algorithm in Case II.

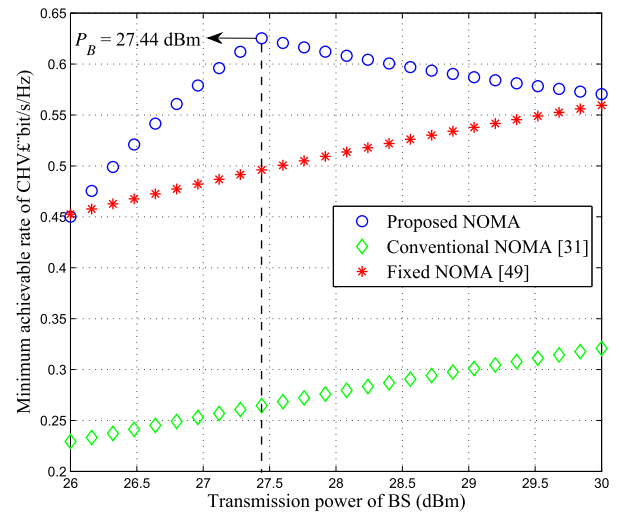


FIGURE 8. Minimum achievable rate of CHV under different transmission power of BS in Case II.

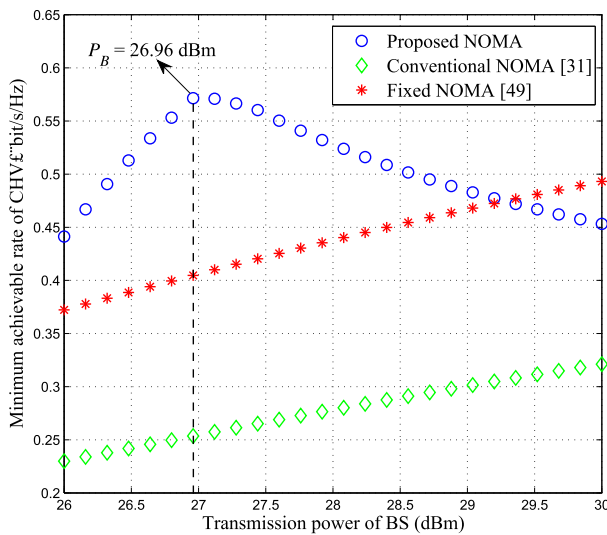


FIGURE 7. Minimum achievable rate of CHV under different transmission power of BS in Case I.

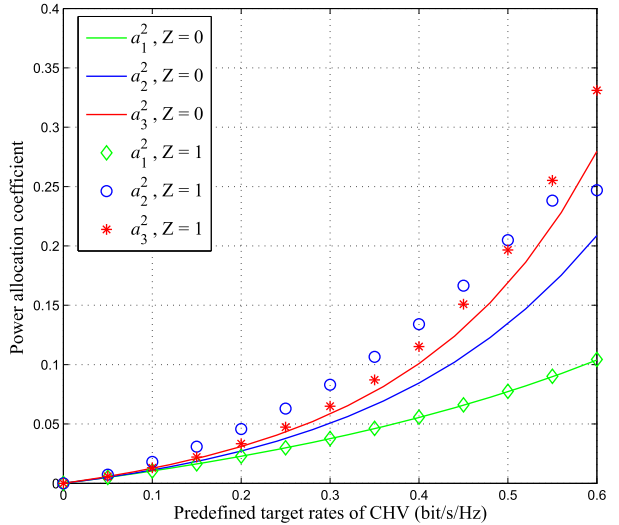


FIGURE 9. Power allocation coefficient versus different predefined target rates of CHV.

iterative calculation of the power allocation coefficient  $a_2^2$  always converges fastest compared to the iterative calculation of the power allocation coefficient  $a_1^2$  and  $a_3^2$  which implies that the proposed scheme gives priority to the power allocation of the relay CHV for achieving better cooperative gain performance.

Fig. 7 plots the minimum achievable rate of CHV among three NOMA schemes under different transmission power of BS in Case I, where CHV-2 receives only the directly transmitted information from BS. We can observe that the minimum achievable rate of the proposed scheme is higher than that of the conventional NOMA scheme [31] and fixed NOMA scheme [49]. Moreover, it can be seen that the minimum achievable rate of the proposed scheme increases first and then decreases as the transmission power of BS increases.

The reason is that the transmission power of the BS is increased to ensure that the CHV-2 was successful in receiving the information. Once the power allocation coefficient  $a_2^2$  no longer increases, his results in a reduction in its achievable transmission rate. It is worth noting that we can find the extreme point (i.e.,  $P_B = 26.96$  dBm,  $C_i = 0.5715$  bit/s/Hz) which maximizes the minimum achievable rate under low transmission power of BS.

Fig. 8 illustrates the minimum achievable rate of CHV under different transmission power of BS in Case II, where CHV-2 successfully receives the cooperative information from CHV-1. In this case, we can observe that the blue curve corresponding to the proposed scheme has also an extreme point (i.e.,  $P_B = 27.44$  dBm,  $C_i = 0.6253$  bit/s/Hz). It also confirms that the proposed scheme not only can save the BS transmission power but also maximize the minimum

achievable rate of CHV. Moreover, the minimum achievable rate of CHV has been increased compared to Case I. This highlights the cooperative performance gain of link CHV-1→CHV-2, with only a small quantity of transmission power of BS being sacrificed. Under the same conditions of  $P_B$ , the minimum achievable rate performance of the proposed NOMA scheme outperforms the conventional NOMA and fixed NOMA schemes.

Fig. 9 shows the variation of power allocation coefficient under different predefined target rates of CHV. In both cases, it can be seen that the three CHVs' power allocation coefficients gradually increase as the predefined target rates of CHV increase, where we must ensure that three CHVs' achievable rates are higher than their predefined target rates. In Case II, CHV-2 has obtained a cooperative gain from CHV-1. The power allocation coefficient  $a_2^2$  exhibits a slow growth and thus reduces the transmission power of BS, while the power allocation coefficient  $a_3^2$  keeps increasing due to poor channel quality of BS→CHV-3. Moreover, compared with Case I, the power allocation coefficients  $a_2^2$  and  $a_3^2$  are always larger than that of Case I, this is because the transmission power of BS is sacrificed in exchange for cooperative gain performance so as to increase the minimum transmission rate of CHV.

## V. CONCLUSION

In this paper, we have proposed the joint clustering method and power control scheme in V2X communications to reduce the communication complexity as well as the total power consumption of BS. The proposed clustering method can not only dynamically adjust the cluster size according to actual traffic and road conditions, but also select out the CHVs with an optimal trade-off between the vehicle's relative speed and the transmission power. Numerical simulation results have showed the consistency with the analytical values. Furthermore, a NOMA-based power control scheme has been proposed to maximize the minimum achievable rate among CHV for a given transmission power of BS. Numerical simulation results have illustrated that the proposed power control scheme can significantly improve the achievable rate of CHV compared with the other two schemes (conventional NOMA and fixed NOMA) under the same transmission power of BS. These results prove the superiority performance of the proposed scheme. It lays the foundation for the research on clustering car-following V2X communication system, and has great practical value in vehicular networks.

## APPENDIX

*Proof of proposition 1:* According to formula (46), using the Lagrange function is

$$\begin{aligned} L(a_i^2, \alpha_i, \beta_i) \\ = a_1^2 + a_2^2 + a_3^2 + \alpha_1 \left( 2^{2\theta} - 1 - a_1^2 \frac{P_B |h_{B1}|^2}{N_0} \right) \end{aligned}$$

$$\begin{aligned} + \alpha_2 \left[ 2^{2\theta} - 1 - a_2^2 \left( \frac{P_B |h_{B2}|^2}{a_1^2 P_B |h_{B2}|^2 + N_0} \right) \right]^{1-Z} \\ \times \left[ 2^{2\theta} - 1 - a_2^2 (c + d) \right]^Z \\ + \alpha_3 \left[ 2^{2\theta} - 1 - a_3^2 (m + n)^{1-Z} \cdot (p + q)^Z \right] \\ - \sum_{i=1}^3 \beta_i \cdot a_i^2, \end{aligned} \quad (58)$$

where  $\alpha_i \geq 0$  and  $\beta_i \geq 0$  are the Karush-Kuhn-Tucker (KKT) multipliers [51]. According to KKT conditions, we can obtain

$$\frac{\partial L}{\partial a_1^2} = 1 - \alpha_1 \frac{P_B |h_{B1}|^2}{N_0} - \beta_1 = 0, \quad (59)$$

$$\begin{aligned} \frac{\partial L}{\partial a_2^2} = 1 - \alpha_2 \left( \frac{P_B |h_{B2}|^2}{a_1^2 P_B |h_{B2}|^2 + N_0} \right)^{1-Z} \\ \times (c + d)^Z - \beta_2 = 0, \end{aligned} \quad (60)$$

$$\frac{\partial L}{\partial a_3^2} = 1 - \alpha_3 (m + n)^{1-Z} \cdot (p + q)^Z - \beta_3 = 0, \quad (61)$$

$$\beta_i \cdot a_i^2 = 0, \quad i = 1, 2, 3, \quad (62)$$

$$\alpha_1 \left( 2^{2\theta} - 1 - a_1^2 \frac{P_B |h_{B1}|^2}{N_0} \right) = 0, \quad (63)$$

$$\begin{aligned} \alpha_2 \left( 2^{2\theta} - 1 - a_2^2 \frac{P_B |h_{B2}|^2}{a_1^2 P_B |h_{B2}|^2 + N_0} \right)^{1-Z} \\ \times \left[ 2^{2\theta} - 1 - a_2^2 (c + d) \right]^Z = 0, \end{aligned} \quad (64)$$

$$\alpha_3 \left[ 2^{2\theta} - 1 - a_3^2 (m + n)^{1-Z} \cdot (p + q)^Z \right] = 0, \quad (65)$$

$$2^{2\theta} - 1 - a_1^2 \frac{P_B |h_{B1}|^2}{N_0} \leq 0, \quad (66)$$

$$\begin{aligned} \left( 2^{2\theta} - 1 - a_2^2 \frac{P_B |h_{B2}|^2}{a_1^2 P_B |h_{B2}|^2 + N_0} \right)^{1-Z} \\ \times \left[ 2^{2\theta} - 1 - a_2^2 (c + d) \right]^Z \leq 0, \end{aligned} \quad (67)$$

$$2^{2\theta} - 1 - a_3^2 (m + n)^{1-Z} \cdot (p + q)^Z \leq 0. \quad (68)$$

It's obvious that  $a_i^2 > 0$  ( $i = 1, 2, 3$ ), then we obtain  $\beta_i = 0$  in the formula (62). Due to  $\beta_i = 0$ ,  $\alpha_i > 0$  can be derived from the equalities (59), (60) and (61). According to constraints (63), (64), (65) and  $\alpha_i > 0$ , the non-strict inequalities (66), (67) and (68) should take equal conditions, i.e.,  $C_i = \theta$  ( $i = 1, 2, 3$ ). The proof of the proposition 1 follows from these results.

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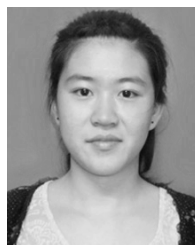
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