

Received May 3, 2019, accepted May 12, 2019, date of publication May 20, 2019, date of current version June 7, 2019. *Digital Object Identifier* 10.1109/ACCESS.2019.2917803

Hybrid Harmony Search Algorithm With Grey Wolf Optimizer and Modified Opposition-Based Learning

ALAA A. ALOMOUSH[®]¹, ABDULRAHMAN A. ALSEWARI^{®1,2}, (Senior Member, IEEE), HAMMOUDEH S. ALAMRI^{®1}, KHALID ALOUFI³, AND KAMAL Z. ZAMLI^{®1}

¹Faculty of Computer Systems and Software Engineering, Universiti Malaysia Pahang, Kuantan 26300, Malaysia
 ²IBM Centre of Excellence, Universiti Malaysia Pahang, Kuantan 26300, Malaysia
 ³College of Computer Science and Engineering, Taibah University, Medina 41477, Saudi Arabia

Corresponding author: Abdulrahman A. Alsewari (alsewari@ump.edu.my)

This work was supported by the UMP DSS, UMP, A Novel Hybrid Harmony Search Algorithm with Nomadic People Optimizer Algorithm for global optimization and feature selection under Grant RDU190334, and A novel Hybrid Kidney-inspired algorithm for Global Optimization Enhance Kidney Algorithm for IoT Combinatorial Testing Problem under Grant FRGS/1/2018/ICT05/UMP/02/1 and Grant RDU190102.

ABSTRACT Most metaheuristic algorithms, including harmony search (HS), suffer from parameter selection. Many variants have been developed to cope with this problem and improve algorithm performance. In this paper, a hybrid algorithm of HS with grey wolf optimizer (GWO) has been developed to solve the problem of HS parameter selection. Then, a modified version of opposition-based learning technique has been applied to the hybrid algorithm to improve the HS exploration because HS easily gets trapped into local optima. Two HS parameters were automatically updated using GWO, namely, pitch adjustment rate and bandwidth. The proposed hybrid algorithm for global optimization problems is called GWO-HS. The GWO-HS was evaluated using 24 classical benchmark functions with 30 state-of-the-art benchmark functions from CEC2014. Then, the GWO-HS has been compared with recent HS variants and other well-known metaheuristic algorithms. The results show that the GWO-HS is superior over the old HS variants and other well-known metaheuristics in terms of accuracy and speed process.

INDEX TERMS Computational intelligence, grey wolf optimizer, harmony search, hybrid algorithm, metaheuristic, optimization algorithm, CEC2014.

I. INTRODUCTION

Solving the NP-hard problem using an exhaustive search is an impractical technique because of long-time consumption and complex application. A well-known solution to solve the NP-hard problem with minimal time consumption is using a heuristic technique that can find a near-optimal solution. Heuristic algorithm sacrifices optimality or completeness to obtain quickly the best result.

Meta-heuristic algorithms are higher-level heuristic algorithms that can cover a wider range of problems, with a lack of information or high computation time [1]. The main functionality of meta-heuristic algorithms is obtained by merging rules and randomness to simulate natural phenomena, such as physical annealing in a simulated annealing (SA) algorithm [2], the human intelligence in the harmony search (HS)

The associate editor coordinating the review of this manuscript and approving it for publication was Chua Chin Heng Matthew.

algorithm [3], the biological evolutionary process in an evolutionary algorithm (EA) [4], and animal behavior in Tabu search [5].

The efficiency of metaheuristic algorithms depends on the utilization of explorative and exploitative ranges through the search process [6]. The exploitative process is accomplished by utilizing the information obtained to guide the search toward its goal. The explorative process is the capability of an algorithm to examine uncovered areas quickly within considerable search sizes. Overall performance develops if the balance between these two characteristics is established [7].

Harmony search (HS) algorithm is a well-known metaheuristic algorithm, introduced by Geem *et al.* [3] by mimicking the musician's process in creating a new musical harmony [8], [9]. The HS algorithm is used in different fields of optimization problems, such as engineering [10], [11], water distribution [12], structural optimization [6], music ensemble [13], and university timetable [14], Software

2169-3536 © 2019 IEEE. Translations and content mining are permitted for academic research only. Personal use is also permitted, but republication/redistribution requires IEEE permission. See http://www.ieee.org/publications_standards/publications/rights/index.html for more information. testing [15]–[18]. Many other applications and variants of the HS algorithm were made according to previous survey articles [19], [20].

The success of using HS in different research fields is attributed to its characteristics. The main advantage of HS is its capability to utilize exploration and exploitation simultaneously through the search process [14].

Most metaheuristic algorithms, including HS, suffer from parameter selection, and premature convergence. Many variants have been developed to cope with this problem and improve algorithm performance [21]–[26].

Generally, researchers have two ways of setting metaheuristic parameter values, namely, by using parameter tuning or by using parameter control.

A. PARAMETER TUNING

The use of parameter tuning is achieved by finding the best values for algorithm parameters before running the algorithm to fix the problem. Parameter tuning involves a number of difficulties, such as longtime consumption because of the need to cover all possibilities, which is practically impossible; another difficulty is high complexity because parameters are not independent; moreover, choosing a fixed parameter as optimal value through the search process is against the idea of EA of a dynamic and adaptive process [27].

B. PARAMETER CONTROL

The other way to modify algorithm parameter values is through the search process, which can be accomplished in three ways.

1: **First method:** The algorithm parameter values can be modified using a deterministic function to replace the static value of the parameters in the search process; an example of this process is the improved HS by Mahdavi *et al.* [21], who replaced the static values of pitch adjustment rate (PAR) and bandwidth (BW) with new functions to modify their values throughout the search process. The following equations present the dynamic BW:

$$C = \left(ln \left(\frac{BW_{min}}{BW_{max}} \right) \div \text{NI} \right) \tag{1}$$

$$BW(t) = BW_{max} \times e^{(c \times t)}.$$
 (2)

(*BWmin*; *BWmax*) are the minimum and maximum values of BW, t is the current number of iterations. The following equation present the dynamic PAR:

$$PAR(t) = PAR_{min} + \frac{(PAR_{max} - PAR_{min})}{NI} \times t.$$
(3)

(*PARmin; PARmax*) are minimum and maximum values of PAR, *t* is the current number of iterations, *NI* is the total number of iterations.

2: Second method: The algorithm can use feedback from the search process to improve the search parameter values, such as updating step size (by decreasing or increasing it) on the basis of the success rate of the search process.

3: **Third method**: The third method uses the self-adaptive values of the algorithm parameters. The adapted parameters can change in chromosomes and mutation processes on the basis of the previous results; an example of this approach is the self-adaptive global best HS algorithm by Pan *et al.* who constructed the mutated values of harmony memory consideration rate (HMCR) and PAR through the search process.

In the current article, we present a hybrid algorithm of HS and grey wolf optimizer (GWO). GWO is a newly developed algorithm inspired by the hunting and leadership of grey wolf packs [28]. Inspired by the idea of finding the best values using optimization algorithms, GWO was used in the current paper to modify the HS parameters as a self-adaptive process. Hence, instead of tuning the PAR and BW parameters before the search start, the GWO algorithm modifies the parameter values throughout the search process.

To improve HS exploration and avoid premature convergence, a modified version of the original opposition-based learning (OBL) [29] is implemented in the hybrid algorithm. This paper mainly aims to design, implement, and evaluate a new hybrid algorithm of HS and GWO with self-adaptive parameter selection. This paper also aims to improve HS algorithm exploration using a modified version of the OBL technique.

To evaluate the effectiveness of the suggested hybrid algorithm, the hybrid algorithm has been tested using 24 classical benchmark functions with 30 state-of-the-art benchmark functions from CEC and compared them with previous HS variants as well as with well-known metaheuristic algorithms. Parametric tests, namely, Wilcoxon's rank test and Friedman test, were used. The tests were used to provide an insight into the new hybrid algorithm in contrast to the previous variants and hybrid algorithm at $\alpha = 5\%$ significance level. The new hybrid algorithm shows highly competitive results in all experiments. To find the best values of harmony memory size (HMS) and HMCR for the hybrid algorithm, some experiments were conducted as presented in the experimental results and analysis section.

The remaining sections of this paper are organized as follows. The original HS and its variants. Then GWO algorithm and modified OBL are investigated. The proposed algorithm is described after that. Then, a section will provide the results and discussion. Finally, a conclusion is provided, and possible future improvements are provided.

II. HS AND ITS VARIANTS

In this part, we will comprehensively describe HS, and different variants were created to overcome the HS variable selection and improve its performance. Some researchers utilized fuzzy logic to automatically update the HS parameters [40]. Mahdavi *et al.* [21], created a modified variant of HS by adding new functions to modify the HMCR and PAR values throughout the search process. Other researchers, such as Omran and Mahdavi [22], modified the search process, which he borrowed from Particle Swarm Optimization [41].

A. HS ALGORITHM

The HS algorithm process contains five main steps, as shown in Figure 1:

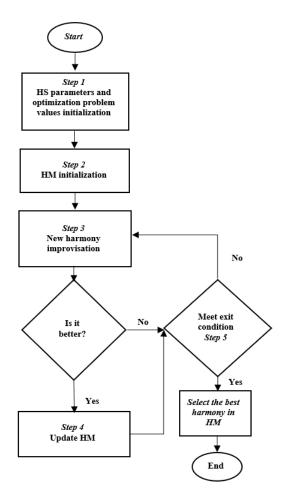


FIGURE 1. HS process.

Step 1: Creating initial values of HS parameters: BW, PAR, HMCR, number of iterations (NI), and HMS. The optimization objective function will be determined in this step either by using the maximum or minimum objective function f(x), which are the benchmark functions used in this paper. X_i is the prospect solution vector from N (all possible solution vectors of X_i , and the X_i value is within (lower and upper boundaries) for all the decision variables.

Step 2: In this step, HM will be initialized within the upper and lower boundary ranges, as shown in the next equation, and X_1 is a random value between 0 and 1.

$$X_i = LB + r_1 \times (UB - LB) \tag{4}$$

Step 3: In this step, the improvisation of new harmony will be performed using a combination of three major parameters, namely, HMCR, PAR, and BW, according to line 9 in Algorithm 1. First, random number X_2 generated between

0 and 1; if X_2 is larger than HMCR, then a new value X_j will be created using Equation 1; otherwise, a random value of X_i will be chosen from HM. Afterward, another random value r_3 will be generated between 0 and 1; if it is smaller than or equal to PAR, then X_i will be modified using Equation 2, as follows:

$$X_i' = X_i' \pm BW \times rnd \tag{5}$$

Step 4: If the newly generated vector X_i' is better than the worst vector in the harmony memory, then the worst vector will be replaced with the new vector X_i' because of the objective function.

Step 5: The stopping criteria, such as the maximum number of improvisations, should be checked after every improvisation. A detailed description of the HS algorithm is presented in the following pseudocode:

Algo	rithm 1 Harmony Search Algorithm Improvisation
1.	while $(t < Max number of iterations)$
2.	for $(j = 1 \text{ to } D) = \{D : number \text{ of dimensions}\}$
3.	If $(R2) \leq HMCR \{Memory \ consideration\}$
4.	$x'_i = x_{i,j} \{ i \text{ is a random integer } (1, \dots, HMS) \}$
5.	if $(R3 \leq PAR)$ {Pitch adjustment}
6.	$x'_{j} = x'_{j} \pm R4 \times bw$
	end if
8.	else
9.	$x'_{i} = LB + R5 \times (UB - LB))$
10.	end if
11.	end for
	Update HM :
13.	if $(x'_j \text{ better than worst } x_j \{x_j \in HM\})$
14.	$x_j = x'_i$
	t = t + 1
16.	End while
17.	return best harmony

B. EXPLORATORY POWER OF THE HARMONY SEARCH ALGORITHM: ANALYSIS AND IMPROVEMENTS FOR GLOBAL NUMERICAL OPTIMIZATION (EHS; 2011)

To improve HS performance, Das *et al.* [42] conducted a theoretical study of the HS algorithm; another variant of the HS algorithm was introduced. The new variant is compared with other variants of HS and other state-of-the-art optimization algorithms. The new variant shows competitive results. The new variant has the same steps as the original HS except for the BW value, which is updated based on the following equations:

$$BW = k\sqrt{Var(x)} \tag{6}$$

$$Var(x) = \frac{1}{m} \sum_{k=1}^{m} (x_i - \bar{x})^2 = x_i^2 - \bar{x}^2$$
(7)

For the benchmark function, the author suggests using (k = .17); meanwhile, m = HMS, and X is the population average.

C. AN IMPROVED GLOBAL-BEST HARMONY SEARCH ALGORITHM (IGHS; 2013)

El-Abd [24] developed as an improved variant of GHS [22] by focusing on the explorative range at the beginning, and then on the exploitative range at the end of a search. To accomplish this, the author used Gaussian distribution to select the random pitch adjustment, as described in the next Equation:

$$X'_{i} = HM'_{d} + Gauss(0, 1) \times BW$$
(8)

where HM_d^r is a randomly selected value from HM, and Gauss is a random number with a mean of 0 and a standard deviation of 1. For pitch adjustment, the next equation is used as follows:

$$X'_{j} = HM^{best}_{d} + \emptyset \times BW \tag{9}$$

where HM_d^{best} is the best value in HM based on the objective function evaluation f(x). The value φ is a random number that is uniformly distributed within the range "-1 to 1". PAR value is decreased within the iterations to achieve great exploitation, as described by [43]. For BW, the author borrowed its formula from the IHS [21] variant. The algorithm was compared with seven previous HS-variants using the CEC 2005 benchmark function.

D. DIFFERENTIAL-BASED HARMONY SEARCH ALGORITHM FOR THE OPTIMIZATION OF CONTINUOUS PROBLEMS (DH/BEST; 2016)

Hosein *et al.* [25] introduced a new HS-variant by modifying two aspects of the original HS. The first modification is applied to the initialization of HS by using a new method to initiate feasible solutions with less randomness. The second modification involves replacing pitch adjustment with the applied to the initialization of HS by using a new method to initiate feasible solutions with less randomness. The second modification involves replacing pitch adjustment with the updated version inspired by the differential evolution (DE) mutation strategy and excluding the BW parameter. The following algorithm describes the new initialization processes, which is implemented by replacing the random value with a new calculation based on HMS:

1. for $(j = 1 \text{ to } D) \{D = dimensions\}$ 2. for (i = 1 to HMS)3. temp_i = LB + $((i - \frac{0.5}{HMS}) \times (UB - LB)$ 4. end for 5. Shuffle the temporary array 6. for (i = 1 to HMS)7. HM = temp_i 8. end for 9. end for

where UB and LB are the upper and lower bounds of the decision variables. The new variant eliminates the requirement of setting BW, and pitches are adjusted based on the distances between the pitches in HM by using DE/best/1 mutation, as described in the following Pseudo-code:

Algo	rithm 3 DH/best Improvisation (Hosein 2016)
1:	$for(i = 1 \ to \ D)$
2:	if $(r(0 \sim 1) \leq HMCR)$
3:	$X'_i = X_{ij}$ (<i>i</i> is random integer from 1 HMS)
4:	$if(r(0 \sim 1) \leq PAR)$
5:	$X'_{i} = X_{best} + r (0 \sim 1) \times (X_{r1,J} - X_{r2,J})$
6:	$if(X'_i < LBorX'_i > UB)$
7:	$X'_{i} = r (0 \sim 1) \times (UB - LB) + LB$
8:	end if
9:	end if
10:	else
11:	$X'_i = r \left(0 \sim 1\right) \times \left(UB - LB\right) + LB$
12:	end if
13:	end for

where UB and LB are the upper and lower bounds of the decision variables, r(0 - 1) is the random value between 0 and 1, X_{best} is the best X_i in HM based on the objective function, and $X_{r1,J}$ and $X_{r2,J}$ are two random values in the *jth* dimension.

E. A HYBRID HARMONY SEARCH AND SIMULATED ANNEALING (HS-SA; 2018)

New hybrid HS algorithm and SA algorithm were presented by Assad and Deep [26], the temperature parameter in SA has been introduced inside the HS algorithm. The new hybrid algorithm adopts a similar process to the original HS, except that it has been updated to accept the poor results of the improvisation process via the probability of the temperature parameter. The temperature starts with a high value to provide high exploration, and it then decreases at each iteration to focus on exploitation through the search process. The new hybrid algorithm provided better results in comparison with the original HS and SA.

III. GWO ALGORITHM

GWO algorithm is a new metaheuristic algorithm developed by Mirjalili *et al.* [28], GWO has been presented as a swarmbased algorithm that simulates the natural driving life of grey wolves [30], [31]. The GWO algorithm shows high performance in many optimization problems [32]–[35].

The GWO algorithm divides the population into four groups, namely alpha α , beta β , Delta δ , and Omega ω .

Firstly, random populations of wolves are created. The wolves change their location through the optimization phase on the basis of the fittest wolves, which is α . Consequently, the second and third best solutions are named β , and δ , ω will be guided through the search by those wolves. In order to attack the prey, wolves will encircle the prey as described in the following equations:

$$\overrightarrow{D} = |\overrightarrow{C}.\overrightarrow{X}_{p}(t) - \overrightarrow{X}(t)|$$
(10)

$$\overrightarrow{X}(t+1) = \overrightarrow{X}_p(t) - \overrightarrow{A} \cdot \overrightarrow{D}$$
(11)

 \vec{X}_p marks the location vector of the prey, and \vec{X} marks the location vector of the grey wolf. \vec{C} and \vec{A} represent the coefficient vectors, whereas *t* indicates the current iteration value. \vec{C} and \vec{A} values are calculated using the following equations:

$$\overrightarrow{A} = 2\overrightarrow{A}.\overrightarrow{r}_1 - \overrightarrow{a} \tag{12}$$

$$\overrightarrow{C} = 2.\overrightarrow{r}_2 \tag{13}$$

where \vec{r}_1 and \vec{r}_2 are random vectors in (0,1), and \vec{d} decreased from 2 to 0 through iterations.

The α , β , and δ values will be the best solution acquired thus far. Then, all the other values (wolves) are considered as ω and will be relocated with respect to α , β , and δ . The updated value of the wolves is based on the following equations:

$$\overrightarrow{D}_{\alpha} = |\overrightarrow{C}_{1}, \overrightarrow{X}_{\alpha} - \overrightarrow{X}|$$
(14)

$$\overrightarrow{D}_{\beta} = |\overrightarrow{C}_{2}.\overrightarrow{X}_{\beta} - \overrightarrow{X}| \tag{15}$$

$$\overrightarrow{D}_{\delta} = |\overrightarrow{C}_{3}.\overrightarrow{X}_{\delta} - \overrightarrow{X}|$$
(16)

where \vec{X} is the location of the current solution; \vec{X}_{α} , \vec{X}_{β} , and \vec{X}_{δ} are the α , β , δ locations, respectively; \vec{C}_1 , \vec{C}_2 , and \vec{C}_3 are random vectors between (0 to 2); and \vec{X}_{α} , \vec{X}_{β} , and \vec{X}_{δ} , represent the distance between the current solution and α , β , and δ , respectively. Afterward, the final location of the current solution is calculated using the following equations:

$$\vec{X}_1 = \vec{X}_{\alpha} - \vec{A}_{1.}(\vec{D}_{\alpha}) \tag{17}$$

$$\vec{X}_2 = \vec{X}_\beta - \vec{A}_2.(\vec{D}_\beta) \tag{18}$$

$$\vec{X}_{3} = \vec{X}_{\delta} - \vec{A}_{3}.(\vec{D}_{\delta})$$
(19)

$$\vec{X}(t+1) = \frac{\vec{X}_1 + \vec{X}_2 + \vec{X}_3}{3}$$
 (20)

where \overrightarrow{A}_1 , \overrightarrow{A}_2 , \overrightarrow{A}_3 are random vectors between $\{-2a, 2a\}$, where a decreased from 2 to 0, within the course of iteration (t).

The final location will be calculated using Equations (10 to 12). Finally, \overrightarrow{A} and \overrightarrow{C} assist the exploration and exploitation as random and adaptive vectors, respectively. The entire process is described in algorithm 4.

IV. MODIFIED OPPOSITION-BASED LEARNING TECHNIQUE

The original OBL introduced by Tizhoosh [29], and many variants of OBL developed after that and used by different research areas [36]. Many HS variants and hybridizations utilized the OBL and its variants in the literature [37]–[39].

In this article we applied a modified version of the original OBL within the HS updating process, to improve the HS exploration, as described in Algorithm 5.

In algorithm 5, $x\{d\}$ represents the new improvisation vector, r is a random value between 0, and 1, d is the number of dimensions, and x_i is the modified opposition value. Once the improvisation process of HS creates a new value x_j , the modified opposition will be applied on the new improvisation

Algorithm 4 Grey Wolf Algorithm

- 1. Initialize grey wolf population within the boundaries $x_i (i = 1, 2, ..., n)$
- 2. Initialize A, a and C
- 3. Calculate the fitness of each search agent
- 4. $x_{\alpha} = best \ search \ agent$
- 5. $x_{\beta} = second best search agent$
- 6. $x_{\delta} = third best search agent$
- 7. while (t < Max number of iterations)do
- 8. for (each search agent)
- 9. update the current search agent possition by eq 18
- 10. End for
- 11. Update A, a, and C
- 12. Calculate the fitness of all search agents
- 13. Update x_{α} , x_{β} and x_{δ}
- 14. t = t + 1
- 15. return X_a

Algorithm 5 Modified Opposition

- 1. $x\{d\} = \{x_1, x_2, \dots, x_d\}$ 2. r = random value between (0, 1)
- 3. for (i = 1 to d)do
- 4. $\bar{X}_i = -1 \times x\{i\} \times r;$
- 5. $if(f(\bar{x}) < f(x))$
- 6. $x = \bar{x}$

Algorithm 6 Hybrid Algorithm GWO-HS

- 1: Define the objective function f(x)
- 2: Initialize HS and GWO Parameters (HMS, HMCR, GWO-Number-of-Agents, HS-NI, GWO-NI)
- 3: Initialize GWO population (PARi; BWi)
- 4: Initialize HS population (Xi)
- 5: while(it < GWO max iteration)do
- *6: while*(*i* < *search agents*)*do*
- 7: while(d < 2)do (for PAR and BW)
- 8: fitnes = HS()(HS-improvisation)
- 9: Improvise new PAR and BW(using GWO)
- 10: Update Alpha, Beta, andDelta
- 11: Improvise new PAR and BW (using GWO
- 12: *improvisation process*)
- 13: Return best harmony

value x_j in the update section and will replace it if it is better on the basis of the objective function f.

V. PROPOSED HYBRID ALGORITHM

A hybrid algorithm is an algorithm that merges two or more algorithms to solve a problem. The goal of this algorithm is to create a new algorithm that combines advantages from these algorithms. The main purpose of this paper is to design, implement, and evaluate a new hybrid algorithm of HS and GWO with a self-adaptive parameter selection, where the benchmark functions are the case studies to evaluate the new proposed algorithm.

IEEE Access

TABLE 1. Benchmark functions (GOV: global optimum value).

Function	Function Formula	Туре	Range	GOV
F1: Sphere	$\sum_{i=1}^n x_i^2$	UM	-100, 100	0
F2: Schwefel's 2.22	$\sum_{i=1}^{D} X_i + \Pi_{i=1}^{D} = X_i $	UM	-10, 10	0
F3: Step	$\sum_{i=1}^{D} (X_i + 0.5)^2$	UM	-100, 100	0
F4: Rosenbrock	$\sum_{i=1}^{D} 100 \times (X_i - X_{i-1}^2)^2 + (x_{i-1} - 1)^2$	UM	-30, 30	0
F5: Schwefel's 2.26	$-\sum_{i=1}^{n} \left[x_i \sin\left(\sqrt{ x_i }\right) \right]$	UM	-500, 500	-12569.5
F6: Rastrigin	$\sum_{i=1}^{D} (X_i^2 - 10\cos(2\pi x_i) + 10)$	М	-5.12, 5.12	0
F7: Ackleys	$-20 \exp\left(-0.2 \sqrt{\frac{1}{30} \sum_{i=1}^{D} x^2}\right) - \exp\left(\sqrt{\frac{1}{30} \sum_{i=1}^{D} \cos 2x^2}\right) + 20 + e$	М	-32, 32	0
F8: Griewank	$\frac{1}{4000} \sum_{i=1}^{D} x^2 - \Pi_{i=1}^{D} \cos \frac{x_i}{\sqrt{i}} + 1$	М	-600, 600	0
F9: Rotated hyper-ellipsoid	$\sum_{i=1}^{n} (\sum_{j=1}^{j=i} x_j)^2$	UM	-100, 100	0
F10: Schaffer	$0.5 + \frac{\sin^2\left(\sqrt{(x_1^2 + x_2^2)} - 0.5\right)}{ 1 + 0.001(x_1^2 + x_2^2) ^2}$	М	-100, 100	0
F11: Zakharov	$\sum_{i=1}^{n} x_i^2 + \left(\sum_{i=1}^{n} 0.5ix_i\right)^2 + \left(\sum_{i=1}^{n} 0.5ix_i\right)^4$	М	-5, 10	0
F12: Alpine	$\sum_{i=1}^{n} x_i. \ sin(x_i) + 0.1x_i $	М	-10, 10	0
F13: Inverted Cosine Wave	$-\sum_{i=1}^{n-1} e^{\left(\frac{-(x_i^2+x_{i+1}^2+0.5x_ix_{i+1})}{8}\right)} \cos 4 \times \sqrt{x_i^2+x_{i+1}^2+0.5x_ix_{i+1}}$	М	-1, 1	0
F14: Dixon price	$(x_1 - 1)^2 + \sum_{i=1}^n i(2x_i^2 - x_i - 1)^2$	UM	-10, 10	0
F15: Axis parallel hyper- ellipsoid 2.2	$\sum_{i=1}^{D} i \times X_i^2$	UM	-5.12, 5.12	0
F16: Sum of a different power 2.8	$\sum_{\{i=1\}}^{\{D\}} X_i^{\{1+i\}}$	UM	-1, 1	0

F17: Levy	$sin^{2}(\pi\omega_{1}) + \sum_{i=1}^{D-1} (\omega_{i} - 1)^{2} [1 + 10 \setminus sin^{2(\pi\omega_{l} + 1)}] \\ + (\omega_{D} - 1)^{2} [1 + (sin^{2(2\pi\omega_{D})})]$	М	-10, 10	0
F18: Salomon's 2.8	$\begin{aligned} & + (\omega_D - 1)^2 \left[1 + \sqrt{\sin^{2(2\pi\omega_D)}} \right] \\ & + \cos(2\pi x) + 0.1 x , \qquad x = \sqrt{\sum_{i=1}^n x_i^2} \end{aligned}$	М	-100, 100	0
F19: Pathologic	$\sum_{i=1}^{n-1} [0.5+] \frac{\sin^2 \left(\sqrt{\{100x_i^2 + x_{(i+1)}^2\}}\right) - 0.5}{1 + 0.001 \left(x_i^2 - 2x_{ix_{(i+1)}} + x_{(i+1)}^2\right)^2}$	М	-100, 100	0
F20: Whitley's	$\sum_{i=1}^{n} \sum_{i=1}^{n} \left(\frac{\left(100(x_i^2 - x_j)^2 + (1 - x_j)^2\right)^2}{4000} - \cos\left(100(x_i^2 - x_j)^2 + (1 - x_j)^2\right) + 1 \right)$	М	-10, 10	0
F21: Schwefel's problem 2.21	$max_i\{ x_i , 1 \le i \le n\}$	UM	-100, 100	0
F22: Quartic	$\sum_{i=0}^{n} i x_i^4 + random(0,1)$	UM	-1.28, 1.28	0
F23: Penalized 1	$ \frac{\pi}{n} \times \{10 \times sin^2(\pi y_1) +\} \sum_{i=1}^{n-1} (y_1 - 1)^2 [1 + 10 sin^2(\pi y_1 + 1)] + (y_n - 1)^2 + \sum_{i=1}^n u(x_i, a, k, m) $	UM	-50, 50	0
F24: Penalized 2	$\frac{\pi}{n} \times \{10 \times \sin^2(\pi y_1) + \} \sum_{i=1}^{n-1} (y_1 - 1)^2 [1 + 10 \sin^2(\pi y_1 + 1)] + (y_n - 1)^2 + \sum_{i=1}^n u(x_i, a, k, m)$	UM	-50, 50	0

TABLE 2. Parameters setting GWO-HS.

Algorithm	Parameters	Value
Harmony search	HMS	5
	HMCR	0.99
	PAR minimum value	0.1
	PAR maximum value	0.4
	BW minimum value	0.1
	BW maximum value	0.4
	HS iteration	100
Grey wolf optimizer	Number of search agents	10
	iteration	100
	number of dimensions	2

Given that the PAR and BW have a high effect on the efficiency of HS [22], [44], we utilize the GWO algorithm to find the right values of PAR and BW through the search process. We use a modified version of the original OBL technique [29] to improve improvisation results because HS suffers from bad exploration, especially if one or more of its vectors are near the local optimum. Meanwhile, we use the static values of 5 and 0.99 for HMS and HMCR, respectively. The new algorithm was tested on the benchmark function

TABLE 3. Parameters setting for compared algorithms.

Algorithm	Parameters	Value
ACS2013	N	5
	GLOBAL MINIMUM	1.0E+20
	РР	0.1
MULTIVERSE2016	Ν	5
	BEST UNIVERSE INFLATION RATE	1.0E+20
ABC2005	Ν	5
	LIMIT2	800
DE1997	Ν	5
	F	0.9
	CR	0.5

and proves the superior performance compared with the previous HS variants and other well-known metaheuristics. Figure 6 presents the general process of the hybrid algorithm, which is described as follows:

- 1. Hybrid algorithm parameter and population initialization:
 - a. Hybrid parameters will be initialized, as described in Table 2: HMCR, HMS, the minimum and maximum value of PAR and BW, number of iterations of HS (HS-NI), GWO number of iterations (GWO-NI), and the number of GWO search agents.

TABLE 4. Parameters setting for HS variants.

Algorithm	HMS	HMCR	PAR	BW	Other
EHS2011	5	0.99	PAR = 0.33	$BW = k.\sqrt{Var}(x)$	
IGHS2013	5	0.9	$PAR_{min} = 0.01$ $PAR_{max} = 0.99$	$\frac{BW_{min}}{BW_{max}} = 0.0001$	
DHBest2016	5	0.99	0.9	-	CR=0.5
HS-SA2018	5	0.9	0.3	0.001	<i>α</i> =0.99

TABLE 6. Effects of HMCR on the GWO-HS performance (HMS = 5).

F1	Mean	5 0.0	30	50	100
F1		00			100
			0.0	4.7E-147	2.1E-157
	SD	0.0	0.0	4.7E-147	2.1E-157
F2	Mean	0.0	0.0	6.3E-161	2.0E-74
	SD	0.0	0.0	6.3E-161	2.0E-74
F3	Mean	0.0	0.0	0.0	0.0
	SD	0.0	0.0	0.0	0.0
F4	Mean	27.6	27.729	27.738	27.73
	SD	27.6	27.729	27.738	27.73
F5	Mean	-12528	-12500	-12494	-12454
	SD	12528	12500	-2494	12454
F6	Mean	0.0	0.0	0.0	0.0
	SD	0.0	0.0	0.0	0.0
F7	Mean	4.4E-16	4.4e-16	4.4e-16	4.4e-16
	SD	4.4E-16	4.4e-16	4.4e-16	4.4e-16
F8	Mean	0.0	0.0	0.0	0.0
	SD	0.0	0.0	0.0	0.0
F9	Mean	0.0	0.0	0.0	0.0
	SD	0.0	0.0	0.0	0.0
F10	Mean	0.06	0.049	0.009	0.06
	SD	0.06	0.049	0.009	0.06
F11	Mean	3.8e-14	4.0e-8	4.0e-2	1.59
	SD	3.8e-14	4.0e-8	4.0e-2	1.59
F12	Mean	1.5e-53	3.2e-107	4.5e-145	0.45
	SD	1.5e-53	3.2e-107	4.5 e-145	0.45
F13	Mean	-26.836	-26.79	26.783	-26.87
	SD	26.836	26.79	26.783	-26.87
F14	Mean	0.666	0.667	0.666	0.67
	SD	0.666	0.667	0.666	0.67
F15	Mean	0.0	0.0	1.3E-241	1.3E-148
	SD	0.0	0.0	1.3E-241	1.3E-148

F	Index	HMCR 0.7	0.8	0.9	0.99
F1	Mean	7.0E-24	1.4E-37	3.9E-76	0.99
	SD	7.0E-24	1.4E-37	3.9E-76	0.0
F2	Mean	1.1E-1	9.6E-15	4.3E-70	0.0
	SD	1.1E-1	9.6E-15	4.3E-70	0.0
F3	Mean	0.0	0.0	0.0	0.0
	SD	0.0	0.0	0.0	0.0
F4	Mean	28.05	27.91	27.5	27.6
	SD	28.05	27.91	27.5	27.6
F5	Mean	-10081	-12091	-12552	-12528
	SD	-10081	-12091	-12552	12528
F6	Mean	0.0	0.0	0.0	0.0
	SD	0.0	0.0	0.0	0.0
F7	Mean	3.6E-12	8.3E-13	4.4E-16	4.4E-16
	SD	3.6E-12	8.3E-13	4.4E-16	4.4E-16
F8	Mean	0.0	0.0	0.0	0.0
	SD	0.0	0.0	0.0	0.0
F9	Mean	6.6E-20	4.0E-34	7.1E-15	0.0
	SD	6.6E-20	4.0E-34	7.1E-15	0.0
F10	Mean	8.4	0.79	0.029	0.009
	SD	8.4	0.79	0.029	0.009
F11	Mean	2.59	2.60	7.7E-6	3.8e-14
	SD	2.59	2.60	7.7E-6	3.8e-14
F12	Mean	0.49	0.45	0.062	1.5e-53
	SD	0.49	0.45	0.062	1.5e-53
F13	Mean	-26.44	-26.73	-26.87	-26.836
	SD	-26.44	-26.73	-26.87	26.836
F14	Mean	3.08	2.6	0.84	0.666
	SD	3.08	2.6	0.84	0.666
F15	Mean	1.1E-23	1.0E-30	0.0	0.0
	SD	1.1E-23	1.0E-30	0.0	0.0

- b. The GWO population will be initialized for PAR and BW within their upper and lower boundaries and represented as two dimensions.
- c. The HS population vectors (for the benchmark functions in this paper) will be initialized using HS initialization process. These vectors will be

used as HM through the whole process of the hybrid algorithm.

- 2. Improvisation process:
 - a. In the HS-improvisation process, the HM vectors will be optimized using the objective function (benchmark functions in this paper).

TABLE 7. Mean and SD of the errors of HS variants for (D = 30).

F	Index	Algorithms				CWO US
		EHS2011	IGHS 2013	DHBest 2016	HS-SA2018	GWO-HS
F1	Mean	2.235 e-60	14.613 14.61	0.0	10.242	0.0
F2	SD	2.235 e-60		0.0	10.242	0.0
ΓZ	Mean	3.484 e-35	0.179	0.0	0.851	0.0
F3	SD	3.484 e-35	0.179 20.0	0.0	0.851	0.0
Г3	Mean	0.0	20.0	0.0	11.766	0.0
F4	SD	0.0	20.0 393.048	0.0	11.766	0.0
Г4	Mean	28.712	393.048 393.048	28.767	553.709	27.766
F5	SD	28.712	-12539.117	28.767	553.709	27.766
гэ	Mean	-10238.560		-12565.425	-12542.17	-12540.709
F6	SD	10238.560	12539.117	12565.425	12542.17	12540.709
FO	Mean	0.0	3.152	0.335	1.449	0.0
57	SD	0.0	3.152	0.335	1.449	0.0
F7	Mean	5.417 e-15	1.841	4.440 e-16	1.610	4.440 e-16
70	SD	5.417 e-15	1.841	4.440 e-16	1.610	4.440 e-16
F8	Mean	8.924 e-4	1.050	0.0	1.103	0.0
-	SD	8.924 e-4	1.050	0.0	1.103	0.0
F9	Mean	11.881	70.978	0.0	92.409	0.0
	SD	11.881	70.978	0.0	92.409	0.0
F10	Mean	0.016	0.441	0.155	0.405	0.009
	SD	0.016	0.441	0.155	0.405	0.009
F11	Mean	9.206 e-5	975.251	57.17	24.633	1.002 e-5
	SD	9.206 e-5	975.251	57.17	24.633	1.002 e-5
F12	Mean	5.954 e-4	0.189	0.032	0.068	1.153 e-62
	SD	5.954 e-4	0.189	0.032	0.068	1.153 e-62
F13	Mean	-26.530	-26.875	-26.786	-26.842	-26.753
	SD	26.530	26.875	26.786	26.842	26.753
F14	Mean	0.697	4.555	10.520	7.625	0.666
	SD	0.697	4.555	10.520	7.625	0.666
F15	Mean	0.032	1.45 e-5	0.033	0.10	0.0
	SD	0.032	1.45 e-5	0.033	0.10	0.0
F16	Mean	3.250 e-10	4.692 e-14	1.785 e-8	1.70E-16	0.0
	SD	3.250 e-10	4.692 e-14	1.785 e-8	1.70E-16	0.0
F17	Mean	1.587	0.785	2.869	0.043	0.305
	SD	1.587	0.785	2.869	0.043	0.305
F18	Mean	0.103	3.506	0.0	1.867	0.0
	SD	0.103	3.506	0.0	1.867	0.0
F19	Mean	1.22	2.623	0.0	1.674	0.0
	SD	1.22	2.623	0.0	1.674	0.0
F20	Mean	372.07	947.823	411.16	394.573	362.217
	SD	372.07	947.823	411.16	394.573	362.217
F21	Mean	-2835.156	-2985.634	-2129.06	-3076.838	-2928.403
	SD	2835.156	2985.634	2129.06	3076.838	2928.403
F22	Mean	4.574	8.894	6.747	8.116	2.80
	SD	4.574	8.894 2	6.747	8.116	2.80
F23	Mean	0.330	2.175	1.592	0.054	0.398
	SD	0.330	2.175	1.592	0.054	0.398
F24	Mean	2.086	7.155	2.938	0.448	1.976
	SD	2.086	7.155	2.938	0.448	1.976

b. A modified OBL was used to improve the obtained result, from HS improvisation process, within the updating phase of HS, which is

described in Algorithm 6. The final result is sent as a fitness function value of GWO optimization process.

TABLE 8. Mean and standard deviation (SD) of the errors of HS variants for (D = 50).

F	Index	Algorithms				
		EHS2011	IGHS 2013	DHBest 2016	HS-SA 2018	GWO-HS
F1	Mean	3.958 e-6	382.791	0.0	524.218	0.0
	SD	3.958 e-6	382.791	0.0	524.218	0.0
F2	Mean	2.08 e-5	8.310	0.0	10.119	0.0
	SD	2.08 e-5	8.310	0.0	10.119	0.0
F3	Mean	0.0	280	0.0	535.9	0.0
	SD	0.0	280	0.0	535.9	0.0
F4	Mean	48.869	18234	48.644	30394	47.718
	SD	48.869	18234	48.644	30394	47.718
F5	Mean	-12372.787	-20216	-20929	-20093	-20750
	SD	12372.787	20216	20929	20093	20750
F6	Mean	2.677	41.536	1.519	45.022	0.0
	SD	2.677	41.536	1.519	45.022	0.0
F7	Mean	1.678 e-4	4.366	4.440 e-16	5.711	4.440 e-16
	SD	1.678 e-4	4.366	4.440 e-16	5.711	4.440 e-16
F8	Mean	0.054	2.476	0.0	5.788	0.0
	SD	0.054	2.476	0.0	5.788	0.0
F9	Mean	54.862	4507.177	0.0	8509	0.0
	SD	54.862	4507.177	0.0	8509	0.0
F10	Mean	0.057	0.471	0.306	0.488	0.037
	SD	0.057	0.471	0.306	0.488	0.037
F11	Mean	3.165	7410.696	175.885	131.789	0.036
	SD	3.165	7410.696	175.885	131.789	0.036
F12	Mean	0.103	1.08	0.051	2.329	2.528 e-68
	SD	0.103	1.08	0.051	2.329	2.528 e-68
F13	Mean	-42.985	-45.301	-45.144	-45.094	-45.370
	SD	42.985	45.301	45.144	45.094	45.370
F14	Mean	0.724	270.194	25.759	360.223	0.666
	SD	0.724	270.194	25.759	360.223	0.666
F15	Mean	0.195	17.166	0.169	23.059	0.0
	SD	0.195	17.166	0.169	23.059	0.0
F16	Mean	2.50 e-9	3.774 e-12	2.799 e-7	6.07 E-13	7.591 e-19
	SD	2.50 e-9	3.774 e-12	2.799 e-7	6.07 E-13	7.591 e-19
F17	Mean	3.319	7.999	1.813	1.729	2.954
	SD	3.319	7.999	1.813	1.729	2.954
F18	Mean	0.129	7.635	0.0	5.176	0.0
	SD	0.129	7.635	0.0	5.176	0.0
F19	Mean	3.835	5.289	0.0	4.437	0.0
	SD	3.835	5.289	0.0	4.437	0.0
F20	Mean	1051.242	682667.321	1096.557	4199.406	1032.046
	SD	1051.242	682667.321	1096.557	4199.406	1032.046
F21	Mean	-4094.937	4539.074	-4936.221	-4894.840	-4399.161
	SD	4094.937	4539.074	4936.221	4894.840	4399.1614
F22	Mean	11.247	23.853	12.479	21.414	8.30
	SD	11.247	23.8532	12.479	21.414	8.30
F23	Mean	0.527	25.025	0.652	2.710	0.579
	SD	0.527	25.025	0.652	2.710	0.579
F24	Mean	4.004	173.633	3.528	22.184	3.887
	SD	4.004	173.633	3.528	22.184	3.887

c. The GWO improvisation process, as described in Algorithm 4, will be used to improvise the PAR and BW values. The fitness function (as included

in line 3 in Algorithm 4) value will be the result of HS improvisation process in every GWO improvisation.

TABLE 9. Mean and standard deviation (SD) of the errors for the existing optimization algorithms for (D = 30).

F	Index	Algorithms ACS 2013	Multiverse 2016	ABC2005	DE 1997	GWO-HS
F1	Mean	3.356 e-34	0.0039	1.674	173.066	0.0
	SD	3.356 e-34	0.0039	1.674	173.066	0.0
F2	Mean	5.936 e-20	0.024	0.158	0.623	0.0
	SD	5.936 e-20	0.024	0.158	0.623	0.0
F3	Mean	0.0	0.666	0.0	775.266	0.0
	SD	0.0	0.666	0.0	775.266	0.0
F4	Mean	33.133	28.816	2232289.712	161316.322	27.766
	SD	33.133	28.816	2232289.712	161316.322	27.766
F5	Mean	-12542.508	-6745.606	-11701.463	-10417.237	-12540.709
	SD	12542.508	6745.606	11701.463	10417.237	12540.709
F6	Mean	0.8622	2.026	7.07	44.736	0.0
	SD	0.8622	2.026	7.07	44.736	0.0
F7	Mean	0.098	0.051	2.545	6.379	4.440 e-16
	SD	0.098	0.051	2.545	6.379	4.440 e-16
F8	Mean	0.001	0.009	0.348	3.338	0.0
	SD	0.001	0.009	0.348	3.338	0.0
F9	Mean	8.252 e-34	0.582	0.0	2137.225	0.0
	SD	8.252 e-34	0.582	0.0	2137.225	0.0
F10	Mean	0.195	0.009	0.459	0.347	0.009
	SD	0.195	0.009	0.459	0.347	0.009
F11	Mean	0.871	0.001	335.010	4.624	1.002 e-5
	SD	0.871	0.001	335.010	4.624	1.002 e-5
F12	Mean	1.221 e-6	0.017	0.014	0.567	1.153 e-62
	SD	1.221 e-6	0.017	0.014	0.567	1.153 e-62
F13	Mean	-26.864	-26.850	-26.553	-26.833	-26.753
110	SD	26.864	26.850	26.553	26.833	26.753
F14	Mean	0.746	0.741	3366.446	1036.294	0.666
	SD	0.746	0.741	3366.446	1036.294	0.666
F15	Mean	1.186 e-36	0.001	0.230	6.354	0.000
110	SD	1.186 e-36	0.001	0.230	6.354	0.0
F16	Mean	2.913 e-148	9.550 e-12	1.131 e-16	1.439 e-4	0.0
110	SD	2.913 e-148	9.550 e-12	1.131 e-16	1.439 e-4	0.0
F17	Mean	3.349	3.349	3.349	3.349	0.0
11/	SD	3.349	3.349	3.349	3.349	0.305
F18	Mean	0.0	0.0	0.0	0.0	0.303
110	SD	0.0	0.0	0.0	0.0	
F19	Mean	0.0	3.250 e-10	0.0	0.0	0.0 0.0
117	SD	0.0	3.250 e-10	0.0	0.0	0.0
F20	Mean	413.952	413.952	413.952	413.952	362.217
120	SD	413.952	413.952	413.952	413.952	
F21	Mean	-3099.99	-2971.234	-3088.953	-3075.226	362.217 -2928.403
1 2 1	SD	3099.99	2971.234	3088.953	3075.226	
EDD	Mean	7.013	3.324	13.676	17.238	-2928.403
F22	SD	7.013	3.324 2	13.676	17.238	2.80 2.80
E22			1.668			
F23	Mean	1.668		1.668	1.668	0.398
E74	SD Maan	1.668	1.668	1.668	1.668	0.398
F24	Mean	3.0	3.0	3.0	3.0	1.976
	SD	3.0	3.0	3.0	3.0	1.976

3. Results: The best results of the hybrid algorithm will be presented in this phase.

The values of *PARi*, *BWi* in Algorithm 6 are random values of *PAR* and *BW* within their lower and upper bounds.

Possible solutions for x_i for HS initialization are the random values between the objective function boundaries.

To conclude the whole process, the GOW-initialization will be used to create PAR and BW possible values

	Index	Algorithms ACS 2013	Multiverse 2016	ABC2005	DE 1997	GWO-HS
F1	Mean	5.212 e-19	0.027	1689.224	459.970	0.0
	SD	5.212 e-19	0.027	1689.224	459.970	0.0
F2	Mean	5.496 e-12	0.065	6.481	1.352	0.0
	SD	5.496 e-12	0.065	6.481	1.352	0.0
F3	Mean	1.4	1.633	0.3	2854.266	0.0
	SD	1.4	1.633	0.3	2854.266	0.0
F4	Mean	96.360	50.836	2050687.392	2232815.458	47.718
	SD	96.360	50.836	2050687.392	2232815.458	47.718
F5	Mean	-20842.549	-10662.148	-17807.783	-16560.174	-20750.237
	SD	20842.549	10662.148	17807.783	16560.174	20750.237
F6	Mean	4.123	5.1942	50.508	95.855	0.0
	SD	4.123	5.1942	50.508	95.855	0.0
F7	Mean	0.271	0.097	9.991	9.743	4.440 e-16
	SD	0.271	0.097	9.991	9.743	4.440 e-16
F8	Mean	0.004	0.057	13.013	10.318	0.0
	SD	0.004	0.057	13.013	10.318	0.0
F9	Mean	3.679 e-18	18.199	26232.197	14722.357	0.0
	SD	3.679 e-18	18.199	26232.197	14722.357	0.0
F10	Mean	0.384	0.042	0.497	0.477	0.037
	SD	0.384	0.042	0.497	0.477	0.037
F11	Mean	24.058	0.034	667.084	144.123	0.036
	SD	24.058	0.034	667.084	144.123	0.036
F12	Mean	1.573 e-4	0.114	0.619	1.804	2.528 e-68
	SD	1.573 e-4	0.114	0.619	1.804	2.528 e-68
F13	Mean	-45.313	-45.385	-44.409	-45.283	-45.370
	SD	45.313	45.385	44.409	45.283	45.370
F14	Mean	3.910	1.022	43610.849	23618.905	0.666
	SD	3.910	1.022	43610.849	23618.905	0.666
F15	Mean	7.768 e-21	0.016	88.173	41.068	0.0
	SD	7.768 e-21	0.016	88.173	41.068	0.0
F16	Mean	2.123 e-124	6.993 e-12	8.463 e-5	2.128 e-4	7.591 e-19
	SD	2.123 e-124	6.993 e-12	8.463 e-5	2.128 e-4	7.591 e-19
F17	Mean	5.166	5.166	5.166	5.166	2.954
	SD	5.166	5.166	5.166	5.166	2.954
F18	Mean	0.0	0.0	0.0	0.0	0.0
	SD	0.0	0.0	0.0	0.0	0.0
F19	Mean	0.0	0.0	0.0	0.0	0.0
	SD	0.0	0.0	0.0	0.0	0.0
F20	Mean	1149.869	1149.869	1149.869	1149.869	1032.046
	SD	1149.869	1149.869	1149.869	1149.869	1032.046
F21	Mean	-5099.996	-4682.634	-4891.577	-5011.839	-4399.161
	SD	5099.996	4682.634	4891.5774	5011.839	4399.161
F22	Mean	15.965	9.513	34.917	31.775	8.30
	SD	15.965	9.513	34.917	31.775	8.30
F23	Mean	1.472	1.472	1.472	1.472	0.579
	SD	1.472	1.472	1.472	1.472	0.579
F24	Mean	5.0	5.0	5.0	5.0	3.887
	SD	5.0	5.0	5.0	5.0	3.887

(as search agents). HS initialization will be used to initialize the benchmark functions possible solution vectors (as HM). In every iteration of GWO, the GWO-fitness function will be the result of HS optimization using the PAR and BW values from GWO-memory. HS improvisation will improvise HM values to find possible solutions to the benchmark functions.

F	Index	Algorithms				
		EHS2011	IGHS 2013	DHBest 2016	HS-SA 2018	GWO-HS
F1	Mean	4.78 E7	2.44 E7	2.17 E7	1.64 E7	413113
	SD	4.78 E7	2.44 E7	2.17 E7	1.64 E7	413113
	Time	35	36	402.25	32.483	60.163
F2	Mean	1.016 E9	2799924	1.62 E8	1180792	18904
	SD	1.016 E9	2799924	1.62 E8	1180792	18904
	Time	20	18	219.85	17.855	20.395
F3	Mean	9247	12394	15863.40	13003	5051
	SD	9247	12394	15863.40	13003	5051
	Time	20	21	239.87	20.542	25.632
F4	Mean	644	533	530.31	538	439
	SD	644	533	530.31	538	439
	Time	21	20.45	256.36	20.926	25.033
F5	Mean	520.67	519.99	520.08	520.04	520.00
	SD	520.67	519.99	520.08	520.04	520.00
	Time	33.023	31.048	405.066	32.749	49.116
F6	Mean	619.58	616.68	614.96	616	620.245
	SD	619.58	616.68	614.96	616	620.245
	Time	3305	3499.66	39014	4057.221	6312.374
F7	Mean	708.46	700.95	708.03	700.52	700.01
. /	SD	708.46	700.95	708.03	700.52	700.01
		41		485		
EQ	Time	863.71	40.83 800.20		41.882	52.229
F8	Mean			803.37	800.09	800
	SD	863.71	800.20	803.37	800.09	800
50	Time	29	27.35	335	27.826	27.31
F9	Mean	1047.49	977.72	989.04	971.87	1037
	SD	1047.49	977.72	989.04	971.87	1037
	Time	36	38.59	460	39.245	37.85
F10	Mean	1995.28	1001.11	1048.71	1001.26	1001
	SD	1995.28	1001.11	1048.71	1001.26	1001
	Time	58	56.51	13273	60.757	63.43
F11	Mean	4479.43	3333.98	3282.25	3220.57	3793.02
	SD	4479.43	3333.98	3282.25	3220.57	3793.02
	Time	67	82.37	726.23	69.857	97.10
F12	Mean	1200.71	1200.16	1200.17	1200.22	1200.18
	SD	1200.71	1200.16	1200.17	1200.22	1200.18
	Time	690	708.27	8221	739.323	1083.54
F13	Mean	1300.64	1300.57	1300.62	1300.59	1300.55
	SD	1300.64	1300.57	1300.62	1300.59	1300.55
	Time	28	26.45	360.72	26.858	17.811
F14	Mean	1686.38	1660.91	1686.04	1685.41	1685.40
	SD	1686.38	1660.91	1686.04	1685.41	1685.40
	Time	29	26.40	370	26.07	16.18
F15		1541.48	1519.03	2321.51	1515.24	1537.52
	Mean	1541.48	1519.03	2321.51	1515.24	
	SD T					1537.52
E14	Time	43	40.17	492	41.091	32.40
F16	Mean	1611.25	1610.12	1610.06	1610.07	1610.51
	SD	1611.25	1610.12	1610.06	1610.07	1610.51
	Time	42	39.22	497	41.409	31.95
F17	Mean	2699841	3011342	2894964	3716289.87	58210.62
	SD	2699841	3011342	2894964	3716289.87	58210.62
	Time	52	51.86	639	54.856	24.30

TABLE 11. Mean and standard deviation (SD) of the errors for HS variants using the CEC2014 (D = 30).

.ontinue	<i>a.)</i> iviean an	ia standara deviat	tion (SD) of the errors for	no variants using the Cr	$C_{2014} (D = 30).$	
F18	Mean	12719	7058.42	445339	5989.24	3523.70
	SD	12719	7058.42	445339	5989.24	3523.70
	Time	37	34.15	437	37.037	24.30
F19	Mean	2539.23	2296.31	2534	2538.38	2539
	SD	2539.23	2296.31	2534	2538.38	2539
	Time	834	798.49	9895	947.406	1046
F20	Mean	14549.12	15983.76	28188	17269.85	15049.83
	SD	14549.12	15983.76	28188	17269.85	15049.83
	Time	37	36.81	448	30.658	49.09
F21	Mean	748419	585489	1097997	774049.91	61828
	SD	748419	585489	1097997	774049.91	61828
	Time	49	47.32	856	40.798	63
F22	Mean	2758	2727.08	2844	2703.86	2813
	SD	2758	2727.08	2844	2703.86	2813
	Time	115	114.450	1696	109.921	139.4
F23	Mean	2617	2616.48	2620.21	2616.43	2500
	SD	2617	2616.48	2620.21	2616.43	2500
	Time	139	139.79	1976	134.524	173.45
F24	Mean	2600	2635.87	2603	2634.43	2600
	SD	2600	2635.87	2603	2634.43	2600
	Time	107	111.17	1503	118.136	127.97
F25	Mean	2707	2710.26	2700.32	2709.29	2700
	SD	2707	2710.26	2700.32	2709.29	2700
	Time	140	142.09	1846	155.969	172.26
F26	Mean	2782	2740.74	2800.04	2766.17	2798.04
	SD	2782	2740.74	2800.04	2766.17	2798.04
	Time	4118	4186.60	50167	3616.477	11220.31
F27	Mean	3443	3431.52	3273.93	3401.17	2900
	SD	3443	3431.52	3273.93	3401.17	2900
	Time	4382	4398	45428	2723.65	5419.98
F28	Mean	4495	3925.84	4050.87	3870.42	3000
	SD	4495	3925.84	4050.87	3870.42	3000
	Time	299	295.40	2768	186.109	344.37
F29	Mean	16215	4177.09	2015087	4362.35	3100
	SD	16215	4177.09	2015087	4362.35	3100
	Time	926	825	9245	646.452	1190.62
F30	Mean	14983	11741.60.0	17050.01	11977.69	3200
	SD	14983	11741.60	17050.01	11977.69	3200
	Time	208	178.75	1773	126.545	369.84

TABLE 11.	(Continued.,) Mean and	l standard	deviation	(SD) of	f the errors	for HS	variants us	sing the	e CEC2014 ((D =	30).
-----------	--------------	------------	------------	-----------	---------	--------------	--------	-------------	----------	-------------	------	------

Finally, we included a modified version of OBL technique as part of our hybrid algorithm through HS updating. The modified OBL will improve the exploration of HS and help the algorithm avoid falling in local optima. Figure 6 presents the general structure of the hybrid algorithm process. The pseudo code of Algorithm 6 describes the hybrid algorithm.

VI. EXPERIMENT RESULTS AND ANALYSIS

In the first section, we investigate HMCR and HMS parameter best values for the hybrid algorithm using the first 15 classical benchmark functions from Table 1. In the second and third sections, we apply the hybrid algorithm to minimize a set of 24 classical benchmark functions, as described in Table 1 and 30 state-of-the-art test cases from CEC2014 [45]. The classical test functions contain unimodal and multimodal functions to provide insight into the hybrid algorithm capabilities to cover different types of problems. The CEC2014 is also a well-known experimental test for single objective optimization problems that contain shifted, rotated, hybrid, and composition optimization test cases. Friedman test and Wilcoxon nonparametric test at $\alpha = 5\%$ significance level were conducted to evaluate the overall performance of the new hybrid algorithm. All experiments are performed on Microsoft Windows 10 Education in a computer with Intel Core i7 Quad CPU 4702MQ processor 2.2 GHz with 240 GB SSD hard drive and 16GB DDR3 RAM. All algorithms are coded in Java. The best results obtained from the experiments are highlighted in bold.

7	Index	Algorithms ACS 2013	MultiVerse 2016	ABC2005	DE 1997	GWO-HS
71	Mean	68849	2463618	2.34 E7	3889379	413113
	SD	68849	2463618	2.34 E7	3889379	413113
	Time	273	174	113	449	60.163
2	Mean	200	1908	993	4.76 E8	18904
	SD	200	1908	993	4.76 E8	18904
	Time	147	97	32	163	20.395
3	Mean	300	374	1600.05	5684	5051
	SD	300	374	1600.05	5684	5051
	Time	161	95	38	197	25.632
4	Mean	400.42	470	500.03	512	439
	SD	400.42	470	500.03	512	439
	Time	172	99	43	198	25.033
5	Mean	520.01	520	520.01	520.81	520.00
	SD	520.01	520	520.01	520.81	520.00
	Time	228	139	89	389	49.116
6	Mean	610.23	604.01	617.59	613	620.245
-	SD	610.23	604.01	617.59	613	620.245
	Time	37222		17323	84542	620.243 6312.374
7	Mean	700	16555 700.01	700.11		6312.374 700.01
/	SD	700		700.11	706.74	
	Time	235	700.01		706.74	700.01
8	Mean	800.91	207	110 800	451	52.229
>			868	800	856.48	800
	SD Time	800.91 162	868		856.48	800
9			165	12749	856.48	27.31
9	Mean	961 061	971	1039.01	993	1037
	SD	961	971	1039.01	993	1037
10	Time	231	192	85	527	37.85
10	Mean	1000.49	2649.50	1000.08	1743	1001
	SD	1000.49	2649.50	1000.08	1743	1001
	Time	337	316	158	881	63.43
11	Mean	2899.09	4168.99	3536.66	6115	3793.02
	SD	2899.09	4168.99	3536.66	6115	3793.02
	Time	423	360	221	1103	97.10
12	Mean	1200.10	1200.16	1200.14	1201.50	1200.18
	SD	1200.10	1200.16	1200.14	1201.50	1200.18
	Time	4105	3451	3011	11534	1083.54
13	Mean	1300.29	1300.26	1300.22	1300.40	1300.55
	SD	1300.29	1300.26	1300.22	1300.40	1300.55
	Time	160	167	56	215	17.811
14	Mean	1685.39	1691	1685.39	1686.15	1685.40
	SD	1685.39	1691	1685.39	1686.15	1685.40
	Time	169	169	67	227	16.18
15	Mean	1505.86	1508.67	1516.61	1612.67	1537.52
	SD	1505.86	1508.67	1516.61	1612.67	1537.52
	Time	243	216	116	476	32.40
16	Mean	1609.12	1610.97	1610.11	1611.78	1610.51
	SD	1609.12	1610.97	1610.11	1611.78	1610.51
	Time	247	218	127	497	31.95
17	Mean	15909.63	68155	3051313	440195.74	58210.62
	SD	15909.63	68155	3051313	440195.74	58210.62
	Time	348	267	203	701	24.30

TABLE 12. Mean and standard deviation (SD) of the errors existing optimization algorithms using the CEC20	14 (D = 30).
---	--------------

SD 1970.31 3693 7320 3.09 E7 3123.70 Time 277 205 112 406 24.30 F19 Mean 2538.04 2547.94 2538.38 2538.97 2539 SD 2538.04 2547.94 2538.38 2538.97 2539 Time 6847 3787 3944 14593 1046 F20 Mean 2799 2227 2185.48 5931 15049.83 SD 2799 2227 2185.48 5931 15049.83 SD 7125.01 34062 658713 125970 61828 Time 314 275 160 593 63 F22 Mean 2550.16 2475.32 2657.33 2486 2813 D 2550.16 2475.32 2617.83 2617.13 2500 SD 2615.24 2502 2617.83 2617.13 2500 SD 2627 2600.60 2630	F18	Mean	1970.31	3693	7320	3.09 E7	3523.70
Time 277 205 112 406 2430 F19 Mean 2538.04 2547.94 2538.38 2538.97 2539 SD 2538.04 2547.94 2538.38 2538.97 2539 Time 6847 3787 3944 14593 1046 F20 Mean 2799 2227 22185.48 5931 15049.83 Time 246 221 118 434 49.09 F21 Mean 7125.01 34062 658713 125970 61828 SD 7125.01 34062 658713 125970 61828 SD 7125.01 34062 2657.33 2486 2813 SD 2550.16 2475.32 2657.33 2486 2813 SD 2615.24 2502 2617.83 2617.13 2500 SD 2615.24 2502 2617.83 2617.13 2500 SD 2615.24 2502 2617.83							
F19 Mean 2538.04 2547.94 2538.38 2538.97 2539 SD 2538.04 2547.94 2538.38 2538.97 2539 Time 6847 3787 3944 14593 1046 F20 Mean 2799 2227 22185.48 5931 15049.83 Time 246 221 118 434 49.09 F21 Mean 7125.01 34062 658713 125970 61828 SD 2790 2227 2657.33 2486 2813 SD 2550.16 2475.32 2657.33 2486 2813 SD 2550.16 2475.32 2657.33 2486 2813 SD 2615.24 2502 2617.83 2617.13 2500 SD 2615.24 2502 2617.83 2617.13 2500 SD 2615.24 2502 2617.83 2617.13 2500 SD 2627 2600.60 2630 <td></td> <td>Time</td> <td></td> <td></td> <td></td> <td></td> <td></td>		Time					
SD 2538.04 2547.94 2538.38 2538.97 2539 Time 6847 3787 3944 14593 1046 F20 Mean 2799 2227 22185.48 5931 15049.83 SD 2799 2227 22185.48 5931 15049.83 SD 2799 2227 2185.48 5931 15049.83 Time 246 221 118 434 49.09 F21 Mean 7125.01 34062 658713 125970 61828 SD 7125.01 34062 2657.33 2486 2813 SD 2550.16 2475.32 2657.33 2486 2813 Time 721 611 503 1809 139.4 F23 Mean 2615.24 2502 2617.83 2617.13 2500 SD 2615.24 2502 2617.83 2646.36 2600 SD 2627 2600.60 2630 <	F19	Mean	2538.04				
Time 6847 3787 3944 14593 1046 F20 Mean 2799 2227 22185.48 5931 15049.83 SD 2799 2227 22185.48 5931 15049.83 SD 2799 2227 22185.48 5931 15049.83 Time 246 21 118 434 49.09 F21 Mean 7125.01 34062 658713 125970 61828 SD 7125.01 34062 658713 125970 61828 SD 2550.16 2475.32 2657.33 2486 2813 Time 721 611 503 1809 139.4 F23 Mean 2615.24 2502 2617.83 2617.13 2500 SD 2615.24 2502 2617.83 2617.13 2500 F24 Mean 2627 2600.60 2630 2646.36 2600 SD 2707.99 2700.88 <		SD	2538.04				
F20 Mean 2799 2227 22185.48 5931 15049.83 SD 2799 2227 22185.48 5931 15049.83 Time 246 221 118 434 49.09 F21 Mean 7125.01 34062 658713 125970 61828 SD 7125.01 34062 658713 125970 61828 Time 314 275 160 593 63 F22 Mean 2550.16 2475.32 2657.33 2486 2813 SD 2550.16 2475.32 2617.83 2617.13 2500 SD 2615.24 2502 2617.83 2617.13 2500 SD 2615.24 2502 2617.83 2646.36 2600 SD 2627 2600.60 2630 2646.36 2600 SD 2707.99 2700.08 2712 2711.38 2700 SD 2707.99 2700.34 2721		Time					
SD 2799 2227 21185.48 5931 15049.83 Time 246 221 118 434 49.09 F21 Mean 7125.01 34062 658713 125970 61828 SD 7125.01 34062 658713 125970 61828 Time 314 275 160 593 63 F22 Mean 2550.16 2475.32 2657.33 2486 2813 SD 2550.16 2475.32 2617.83 2617.13 2500 SD 2615.24 2502 2617.83 2617.13 2500 SD 2627 2600.60 2630 2646.36 2600 SD 2627 2600.60 2630 2646.36 2600 SD 2707.99 2700.08 2712 2711.38 2700 F25 Mean 2715 2700.34 2721 2725.87 2798.04 SD 2715 2700.34 2721	F20						
Time 246 221 111.1 434 49.09 F21 Mean 7125.01 34062 658713 125970 61828 SD 7125.01 34062 658713 125970 61828 Time 314 275 160 593 63 F22 Mean 2550.16 2475.32 2657.33 2486 2813 SD 2550.16 2475.32 2617.83 2617.13 2500 SD 2515.24 2502 2617.83 2617.13 2500 SD 2615.24 2502 2617.83 2617.13 2500 SD 2627 2600.60 2630 2646.36 2600 SD 2627 2600.60 2630 2646.36 2600 SD 2627 2600.60 2630 2646.36 2600 SD 2707.99 2700.08 2712 2711.38 2700 F25 Mean 2715 2700.34 2721							
F21 Mean 7125.01 34062 658713 125970 61828 SD 7125.01 34062 658713 125970 61828 Time 314 275 160 593 63 SD 2550.16 2475.32 2657.33 2486 2813 SD 2550.16 2475.32 2657.33 2486 2813 Time 721 611 503 1809 139.4 F23 Mean 2615.24 2502 2617.83 2617.13 2500 SD 2615.24 2502 2617.83 2617.13 2500 SD 2627 2600.60 2630 2646.36 2600 SD 2627 2600.60 2630 2646.36 2600 SD 2707.99 2700.08 2712 271.38 2700 F25 Mean 2715 2700.34 2721 2725.87 278.04 SD 2715 2700.34 2721 <td< td=""><td></td><td>Time</td><td>246</td><td>221</td><td></td><td></td><td>49.09</td></td<>		Time	246	221			49.09
SD 7125.01 34062 658713 125970 61828 Time 314 275 160 593 63 F22 Mean 2550.16 2475.32 2657.33 2486 2813 SD 2550.16 2475.32 2657.33 2486 2813 F23 Mean 2615.24 2502 2617.83 2617.13 2500 SD 2615.24 2502 2617.83 2617.13 2500 SD 2615.24 2600.60 2630 2646.36 2600 Time 999 715 662 2406 173.45 F24 Mean 2627 2600.60 2630 2646.36 2600 SD 2627 2600.60 2630 2711.38 2700 F25 Mean 2707.99 2700.88 2712 271.38 2700 F25 Mean 2715 2700.34 2721 2725.87 2798.04 SD 2715 <t< td=""><td>F21</td><td>Mean</td><td>7125.01</td><td></td><td></td><td></td><td></td></t<>	F21	Mean	7125.01				
Time 314 275 160 593 63 F22 Mean 2550.16 2475.32 2657.33 2486 2813 SD 2550.16 2475.32 2657.33 2486 2813 Time 721 611 503 1809 194 F23 Mean 2615.24 2502 2617.83 2617.13 2500 SD 2615.24 2502 2617.83 2617.13 2500 SD 2615.24 2502 2617.83 2617.13 2500 Time 999 715 662 2406 173.45 F24 Mean 2627 2600.60 2630 2646.36 2600 SD 2627 2600.08 2712 271.138 2700 F25 Mean 2707.99 2700.08 2712 271.38 2700 F26 Mean 2715 2700.34 2721 272.587 2798.04 SD 2715 2700.34 </td <td></td> <td></td> <td></td> <td></td> <td></td> <td></td> <td></td>							
F22 Mean 2550.16 2475.32 2657.33 2486 2813 F23 Mean 2615.24 2502 2617.83 2486 2813 F23 Mean 2615.24 2502 2617.83 2617.13 2500 SD 2615.24 2502 2617.83 2617.13 2500 Time 999 715 662 2406 173.45 F24 Mean 2627 2600.60 2630 2646.36 2600 SD 2627 2600.60 2630 2646.36 2600 F25 Mean 2707.99 2700.08 2712 271.38 2700 F25 Mean 2707.99 2700.08 2712 271.38 2700 F26 Mean 2715 2700.34 2721 2725.87 2798.04 SD 2715 2700.34 2721 2725.87 2798.04 F27 Mean 3124 2903.90 3168 3297.27 2900 </td <td></td> <td>Time</td> <td>314</td> <td></td> <td></td> <td></td> <td></td>		Time	314				
SD 2550.16 2475.32 2657.33 2486 2813 Time 721 611 503 1809 139.4 F23 Mean 2615.24 2502 2617.83 2617.13 2500 SD 2615.24 2502 2617.83 2617.13 2500 Time 999 715 662 2406 173.45 F24 Mean 2627 2600.60 2630 2646.36 2600 SD 2627 2600.60 2630 2646.36 2600 2630 2646.36 2600 Time 781 703 500 1761 127.97 F25 Mean 2707.99 2700.08 2712 2711.38 2700 F26 Mean 2715 2700.34 2721 2725.87 2798.04 SD 2715 2700.34 2721 2725.87 2798.04 F27 Mean 3124 2903.90 3168 3297.27 2900 <td>F22</td> <td>Mean</td> <td>2550.16</td> <td></td> <td></td> <td></td> <td></td>	F22	Mean	2550.16				
Time 721 611 503 1809 139.4 F23 Mean 2615.24 2502 2617.83 2617.13 2500 SD 2615.24 2502 2617.83 2617.13 2500 Time 999 715 662 2406 173.45 F24 Mean 2627 2600.60 2630 2646.36 2600 SD 2627 2600.60 2630 2646.36 2600 Time 781 703 500 1761 127.97 F25 Mean 2707.99 2700.08 2712 2711.38 2700 SD 2707.99 2700.08 2712 271.38 2700 F26 Mean 2715 2700.34 2721 2725.87 2798.04 SD 2715 2700.34 2721 2725.87 2798.04 F27 Mean 3124 2903.90 3168 3297.27 2900 SD 3124 2903.		SD		2475.32			
F23 Mean 2615.24 2502 2617.83 2617.13 2500 SD 2615.24 2502 2617.83 2617.13 2500 Time 999 715 662 2406 173.45 F24 Mean 2627 2600.60 2630 264.36 2600 SD 2627 2600.60 2630 264.36 2600 Time 781 703 500 1761 127.97 F25 Mean 2707.99 2700.08 2712 2711.38 2700 SD 2707.99 2700.34 2721 2725.87 2798.04 SD 2715 2700.34 2721 2725.87 2798.04 SD 2715 2700.34 2721 2725.87 2798.04 SD 2715 2700.34 2721 2725.87 2798.04 SD 3124 2903.90 3168 3297.27 2900 SD 3124 2903.90 3168 3297.27 2900 SD 3753 3017.05 4751		Time		611	503	1809	139.4
SD 2615.24 2502 2617.83 2617.13 2500 Time 999 715 662 2406 173.45 F24 Mean 2627 2600.60 2630 2646.36 2600 SD 2627 2600.60 2630 2646.36 2600 Time 781 703 500 1761 127.97 F25 Mean 2707.99 2700.08 2712 2711.38 2700 SD 2707.99 2700.08 2721 275.87 2798.04 SD 2715 2700.34 2721 275.87 2900 SD 3124 2903.90 3168 3297.27 2900 SD 3124 2903.90 3168 3297.27 <	F23	Mean		2502	2617.83	2617.13	2500
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$		SD	2615.24				
SD 2627 2600.60 2630 2646.36 2600 Time 781 703 500 1761 127.97 F25 Mean 2707.99 2700.08 2712 2711.38 2700 SD 2707.99 2700.08 2712 2711.38 2700 SD 2707.99 2700.34 2721 2725.87 2798.04 SD 2715 2700.34 2721 2725.87 2798.04 SD 2715 2700.34 2721 2725.87 2798.04 SD 2715 2700.34 2721 2725.87 2798.04 F27 Mean 3124 2903.90 3168 3297.27 2900 SD 3124 2903.90 3168 3297.27 2900 3168 3297.27 2900 SD 3124 2903.90 3168 3297.27 2900 3168 3297.27 2900 SD 3124 2903.90 3168 3297.27 2900		Time	999				
F25Time7817035001761127.97F25Mean2707.992700.0827122711.382700SD2707.992700.0827122711.382700SD2707.992700.0827122711.382700Time10599196332227172.26F26Mean27152700.3427212725.872798.04SD27152700.3427212725.872798.04F27Mean31242903.9031683297.272900SD31242903.9031683297.272900SD31242903.9031683297.272900SD31233017.0547513913.603000SD37533017.0547513913.603000SD3626.3819816.49493159318.7703100F29Mean3626.3819816.49493159318.7703100F30Mean550.635142.617907762.583200	F24	Mean	2627	2600.60	2630	2646.36	2600
F25 Mean 2707.99 2700.08 2712 2711.38 2700 SD 2707.99 2700.08 2712 2711.38 2700 Time 1059 919 633 2227 172.26 F26 Mean 2715 2700.34 2721 2725.87 2798.04 SD 2715 2700.34 2721 2725.87 2798.04 Time 26476 21762 21399 61044 11220.3 F27 Mean 3124 2903.90 3168 3297.27 2900 SD 3124 2903.90 3168 3297.27 2900 3168 F28 Mean 3753 3017.05 4751 3913.60 3000 SD 3626.38 19816.49 4931 59318.770 3100 SD 3626.38		SD	2627	2600.60	2630	2646.36	2600
SD 2707.99 2700.08 2712 2711.38 2700 Time 1059 919 633 2227 172.26 F26 Mean 2715 2700.34 2721 2725.87 2798.04 SD 2715 2700.34 2721 2725.87 2798.04 SD 2715 2700.34 2721 2725.87 2798.04 Time 26476 21762 21399 61044 11220.3 F27 Mean 3124 2903.90 3168 3297.27 2900 SD 3124 2903.90 3168 3297.27 2900 Time 25270 21615 20556 48621 5419.98 F28 Mean 3753 3017.05 4751 3913.60 3000 SD 3753 3017.05 4751 3913.60 3000 SD 3753 3017.05 4751 3913.60 3000 F29 Mean 3626.38 19816.49 <td></td> <td>Time</td> <td>781</td> <td>703</td> <td>500</td> <td>1761</td> <td>127.97</td>		Time	781	703	500	1761	127.97
Time 1059 919 633 2227 172.26 F26 Mean 2715 2700.34 2721 2725.87 2798.04 SD 2715 2700.34 2721 2725.87 2798.04 Time 26476 21762 21399 61044 11220.3 F27 Mean 3124 2903.90 3168 3297.27 2900 SD 3124 2903.90 3168 3297.27 2900 Time 25270 21615 20556 48621 5419.98 F28 Mean 3753 3017.05 4751 3913.60 3000 SD 3626.38 19816.49 4931 59318.770 3100 SD 3626.38 19816.49 4931	F25	Mean	2707.99	2700.08	2712	2711.38	2700
F26 Mean 2715 2700.34 2721 2725.87 2798.04 SD 2715 2700.34 2721 2725.87 2798.04 Time 26476 21762 21399 61044 11220.3 F27 Mean 3124 2903.90 3168 3297.27 2900 SD 3124 2903.90 3168 3297.27 2900 Time 25270 21615 20556 48621 5419.98 F28 Mean 3753 3017.05 4751 3913.60 3000 SD 3753 3017.05 4751 3913.60 3000 SD 3753 3017.05 4751 3913.60 3000 F29 Mean 3626.38 19816.49 4931 59318.770 3100 SD 3626.38 19816.49 4931 59318.770 3100 Time 6063 4775 4515 9249 1190.62 F30 Mean 5500.63 5142.61 7907 7762.58 3200		SD	2707.99	2700.08	2712	2711.38	2700
SD 2715 2700.34 2721 2725.87 2798.04 Time 26476 21762 21399 61044 11220.3 F27 Mean 3124 2903.90 3168 3297.27 2900 SD 3124 2903.90 3168 3297.27 2900 SD 3124 2903.90 3168 3297.27 2900 Time 25270 21615 20556 48621 5419.98 F28 Mean 3753 3017.05 4751 3913.60 3000 SD 3753 3017.05 4751 3913.60 3000 F29 Mean 3626.38 19816.49 4931 59318.770 3100 F29 Mean 3626.38 19816.49 4931 59318.770 3100 F29 Mean 3626.38 19816.49 4931 59318.770 3100 F30 Mean 5500.63 5142.61 7907 7762.58 3200		Time	1059	919	633	2227	172.26
Time 26476 21762 21399 61044 11220.3 F27 Mean 3124 2903.90 3168 3297.27 2900 SD 3124 2903.90 3168 3297.27 2900 Time 25270 21615 20556 48621 5419.98 F28 Mean 3753 3017.05 4751 3913.60 3000 SD 3753 3017.05 4751 3913.60 3000 Time 1776 1831 1339 2895 344.37 F29 Mean 3626.38 19816.49 4931 59318.770 3100 SD 3626.38 19816.49 4931 59318.770 3100 Time 6063 4775 4515 9249 1190.62 F30 Mean 5500.63 5142.61 7907 7762.58 3200	F26	Mean	2715	2700.34	2721	2725.87	2798.04
F27 Mean 3124 2903.90 3168 3297.27 2900 SD 3124 2903.90 3168 3297.27 2900 Time 25270 21615 20556 48621 5419.98 F28 Mean 3753 3017.05 4751 3913.60 3000 SD 3753 3017.05 4751 3913.60 3000 Time 1776 1831 1339 2895 344.37 F29 Mean 3626.38 19816.49 4931 59318.770 3100 SD 3626.38 19816.49 4931 59318.770 3100 Time 6063 4775 4515 9249 1190.62 F30 Mean 5500.63 5142.61 7907 7762.58 3200		SD	2715	2700.34	2721	2725.87	2798.04
SD 3124 2903.90 3168 3297.27 2900 Time 25270 21615 20556 48621 5419.98 F28 Mean 3753 3017.05 4751 3913.60 3000 SD 3753 3017.05 4751 3913.60 3000 SD 3753 3017.05 4751 3913.60 3000 F29 Mean 3626.38 19816.49 4931 59318.770 3100 SD 3626.38 19816.49 4931 59318.770 3100 Time 6063 4775 4515 9249 1190.62 F30 Mean 5500.63 5142.61 7907 7762.58 3200		Time	26476	21762	21399	61044	11220.31
Time 25270 21615 20556 48621 5419.98 F28 Mean 3753 3017.05 4751 3913.60 3000 SD 3753 3017.05 4751 3913.60 3000 Time 1776 1831 1339 2895 344.37 F29 Mean 3626.38 19816.49 4931 59318.770 3100 SD 3626.38 19816.49 4931 59318.770 3100 Time 6063 4775 4515 9249 1190.62 F30 Mean 5500.63 5142.61 7907 7762.58 3200	F27	Mean	3124	2903.90	3168	3297.27	2900
F28 Mean 3753 3017.05 4751 3913.60 3000 SD 3753 3017.05 4751 3913.60 3000 Time 1776 1831 1339 2895 344.37 F29 Mean 3626.38 19816.49 4931 59318.770 3100 SD 3626.38 19816.49 4931 59318.770 3100 Time 6063 4775 4515 9249 1190.62 F30 Mean 5500.63 5142.61 7907 7762.58 3200		SD	3124	2903.90	3168	3297.27	2900
SD 3753 3017.05 4751 3913.60 3000 Time 1776 1831 1339 2895 344.37 F29 Mean 3626.38 19816.49 4931 59318.770 3100 SD 3626.38 19816.49 4931 59318.770 3100 Time 6063 4775 4515 9249 1190.62 F30 Mean 5500.63 5142.61 7907 7762.58 3200		Time	25270	21615	20556	48621	5419.98
Time 1776 1831 1339 2895 344.37 F29 Mean 3626.38 19816.49 4931 59318.770 3100 SD 3626.38 19816.49 4931 59318.770 3100 Time 6063 4775 4515 9249 1190.62 F30 Mean 5500.63 5142.61 7907 7762.58 3200	F28	Mean	3753	3017.05	4751	3913.60	3000
F29 Mean 3626.38 19816.49 4931 59318.770 3100 SD 3626.38 19816.49 4931 59318.770 3100 Time 6063 4775 4515 9249 1190.62 F30 Mean 5500.63 5142.61 7907 7762.58 3200		SD	3753	3017.05	4751	3913.60	3000
SD 3626.38 19816.49 4931 59318.770 3100 Time 6063 4775 4515 9249 1190.62 F30 Mean 5500.63 5142.61 7907 7762.58 3200		Time	1776	1831	1339	2895	344.37
Time60634775451592491190.62F30Mean5500.635142.6179077762.583200	F29	Mean	3626.38	19816.49	4931	59318.770	3100
F30 Mean 5500.63 5142.61 7907 7762.58 3200		SD	3626.38	19816.49	4931	59318.770	3100
		Time	6063	4775	4515	9249	1190.62
SD 5500.63 5142.61 7007 7762.59 2200	F30	Mean	5500.63	5142.61	7907	7762.58	3200
~~ 5500.05 5172.01 /207 /702.38 5200		SD	5500.63	5142.61	7907	7762.58	3200
Time 1403 1232 916 1876 369.84		Time	1403	1232	916	1876	369.84

TABLE 12. (Continued.) Mean and standard deviation (SD) of the errors existing optimization algorithms using the CEC2014 (D = 30).

A. EFFECTS OF HMS AND HMCR ON THE HYBRID ALGORITHM

To determine the best values of the static parameters of the hybrid algorithm, we investigate the different values of the static parameters, namely, HMS and HMCR. Other parameters of the hybrid algorithm for these experiments are the same as those shown in Table 2. We used the first 15 benchmark functions as described in Table 1 to determine the best values of HMS and HMCR as static values in this article. The total number of improvisations is set to 10^4 for all experiments in this article, except for CEC2014 experiments in which we used 10^6 . The mean and SD are calculated for 30 runs of each function with 30 dimensions. Table 4 presents

the results of using different HMS values (i.e., 5, 30, 50, and 100). Meanwhile, *f* presents function.

Table 4 shows that the best results for the hybrid algorithm are obtained using HMS = 5 and shows the fastest results obtained in most functions. Table 4 shows that increasing HMS does not improve the performance in most algorithms. Thus, a small HMS improves the update rate in HM for most cases. Table 5 presents the results of running the hybrid algorithm with different HMCR values (i.e., 0.7, 0.8, 0.9, and 0.99). The obtained results show that the HMCR value has a high influence on the HS performance. A large HMCR value provides improved results. The best results are obtained using HMCR = 0.99 for most benchmark functions with the

TABLE 13. Wilcoxon signed-rank test results GWO-HS vs HS variants 30D.

Algorithms	P-value	R+	R-	n/h/l/s
GWO-HS vs EHS2011	0.0001	221	-52	24/21/1/2
GWO-HS vs IGHS 2013	0.00022	276	0	24/24/0/0
GWO-HS vs DHBest 2016	0.00782	217	-23	24/14/2/8
GWO-HS vs HS-SA 2018	0.00614	254	-22	24/21/3/0

TABLE 14. Wilcoxon signed-rank test results GWO-HS vs HS variants 50D.

Algorithms	P-value	R+	R-	n/h/l/s
GWO-HS vs EHS2011	0.0001	208	-2	24/20/3/1
GWO-HS vs IGHS 2013	0.0001	251	-21	24/22/2/0
GWO-HS vs DHBest 2016	0. 02642	188	-29	24/13/3/8
GWO-HS vs HS-SA 2018	0.0002	247	-6	24/21/3/0

TABLE 15. Wilcoxon signed-rank test results GWO-HS vs other metaheuristics 30D.

Algorithms	P-value	R+	R-	n/h/l/s
GWO-HS vs ACS 2013	0. 00374	225	0	24/21/0/3
GWO-HS vs MultiVerse 2016	0.00124	228	0	24/22/0/2
GWO-HS vs ABC2005	0. 00078	213	-8	24/19/1/4
GWO-HS vs DE 1997	0.00044	228	0	24/22/0/2

TABLE 16. Wilcoxon signed-rank test results GWO-HS vs other metaheuristics 50D.

Algorithms	P-value	R+	R-	n/h/l/s
GWO-HS vs ACS 2013	0.00214	231	-15	24/20/2/2
GWO-HS vs MultiVerse 2016	0. 00086	240	-4	24/21/1/2
GWO-HS vs ABC2005	0.00034	249	-8	24/20/2/2
GWO-HS vs DE 1997	0.00038	256	-4	24/20/2/2

TABLE 17. Wilcoxon signed-rank test results GWO-HS vs HS variants CEC2014 30D.

	P-value	R+	R-	n/h/l/s
GWO-HS vs EHS2011	0.0002	414	-50	30/25/4/1
GWO-HS vs IGHS 2013	0.01778	347	-117	30/19/-11/0
GWO-HS vs DHBest 2016	0.00044	403	-62	30/24/6/0
GWO-HS vs HS-SA 2018	0.00782	359	-103	30/22/8/0

TABLE 18. Wilcoxon signed-rank test results GWO-HS vs other metaheuristics CEC 2014 30D.

Algorithms	P-value	R+	R-	n/h/l/s
GWO-HS vs ACS 2013	0. 03662	362	-103	30/22/8/0
GWO-HS vs Multiverse 2016	0. 4965	267	-195	30/17/11/2
GWO-HS vs ABC2005	0. 14706	300	-163	30/16/13/1
GWO-HS vs DE 1997	0.00128	389	-76	30/23/7/0

fastest convergence rate. Through the experiment of HMS values, we use HMCR = 0.99 and HMS = 5 to run the HMCR value experiment.

B. EXPERIMENT 1

In this part, we will analyze the experiment of the new hybrid algorithm compared with four recent HS variants and one hybrid algorithm (i.e., EHS 2011, IGHS 2013, DH/best 2016 and HS-SA 2018). The parameter configurations for

these variants are described in Table 4. The parameter values for the hybrid algorithm are the same as those listed in Table 2. First, we examine the hybrid algorithm together with four HS variants using 24 benchmark functions with 30 and 50 dimensions, as described in Table 1.

For both dimensions, as presented in Tables 7 and 8, the hybrid algorithm provides better results than the other HS variants in most cases. Second, we compare the hybrid algorithm with the recent variants of HS using 30 state-of-the-art

Algorithms	Classical 30D	Classical 50D	CEC2014 30D
EHS2011	2.8542	2.9583	4.0833
IGHS 2013	4.1250	4.2083	2.6333
DHBest 2016	2.9792	2.1875	3.6000
HS-SA 2018	3.3750	4.1667	2.7000
GWO-HS	1.6667	1.4792	1.9833

TABLE 19. Friedman test results GWO-HS vs HS variants.

TABLE 20. Friedman test results GWO-HS vs other metaheuristics.

Algorithms	Classical 30D	Classical 50D	CEC2014 30D
ACS 2013	2.4792	2.5417	1.8667
Multiverse 2016	3.1458	2.8750	2.6667
ABC2005	3.6250	2.5417	3.4500
DE1997	4.1875	3.9583	4.2333
GWO-HS	1.5625	1.5000	2.7833

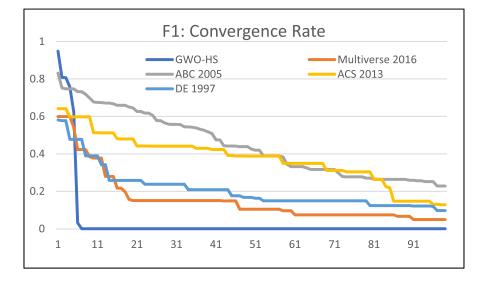


FIGURE 2. Convergence curve for f1.

CEC benchmark functions [45], with 30 dimensions. The results presented in Table 11 show that the new hybrid algorithm outperforms the recent variants in 20 out of the 30 test cases and provides highly competitive results. In terms of speed, the algorithm only outperforms the other variants in seven functions, but it provides high speed in all cases.

Wilcoxon's rank test was applied to the mean results of Tables 7, 8, and 11 presented in Tables 13, 14, and 17 respectively. The p-value shows the significance of the results and performance improvement in comparison with other variants. A low p-value means high improvement. R+ presents the total ranks whenever the hybrid algorithm provides better results than the other variants, whereas R- provides the total ranks of lower results than the other variants. N is the total number of benchmark functions, l, h, and s indicate the total number of functions with higher, lower, or similar results of the hybrid algorithm compared with other variants. As presented in Tables 13, 14, and 17, the new hybrid algorithm outperforms all variants of HS with improved performance. Finally, to establish a comparative assessment, Friedman statistical test has been conducted based on the mean results of Tables 7, 8, and 11. The results presented in Table 19 confirm that the new hybrid algorithm outperforms all previous variants of HS because it provides the highest ranking. These results obtained the lowest value on the Friedman test, which shows a high ranking. The results contain classical 30D as classical benchmark functions with 30 dimensions, and classical 50D as classical benchmark functions with 50 dimensions, and finally the CEC2014 test cases with 30 dimensions.

C. EXPERIMENT 2

To investigate the capability of the hybrid algorithm, we evaluate it with other state-of-the-art metaheuristic algorithms from different families, as follows: artificial cooperative search (ACS 2013) [46], (multi-verse 2016) [47], artificial bee colony (ABC 2005) [48], and differential evolution (DE 1997) [49]. The parameter characteristics of these algorithms are shown in Table 3 as used in this experiment.

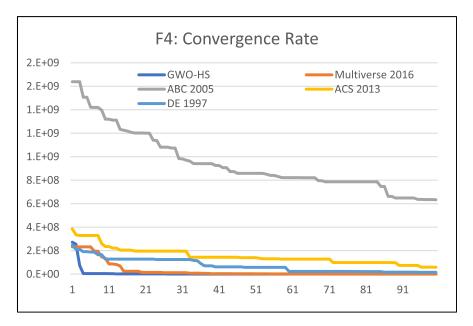


FIGURE 3. Convergence curve for f4.

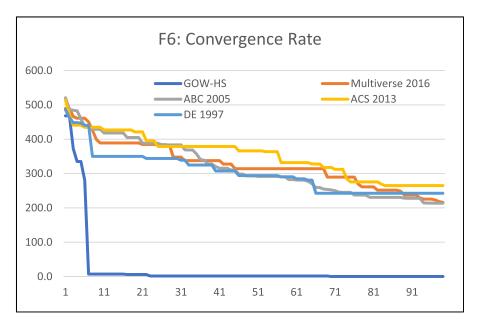


FIGURE 4. Convergence curve for f 6.

In Table 9, we compare the hybrid algorithm with other metaheuristics using classical benchmark functions as described in Table 1. These functions have 30 dimensions. The hybrid algorithm provides the best results in all test functions, except for F5 and F13. The hybrid algorithm provides the second-best results. Table 10 presents the mean, and the SD of the hybrid algorithm with other metaheuristics by using 50 dimensions for the classical benchmark functions. The hybrid algorithm outperforms other metaheuristics in all test functions, except for F5, F13, and F16; the hybrid algorithm provides the second-best result. Finally, we compare the hybrid algorithm with other metaheuristics in Table 12 using

30 state-of-the-art benchmark functions from CEC 2014. The results of mean and standard deviations and running time show that the hybrid algorithm provides the highest speed in all the 30 cases. Moreover, this algorithm outperforms all other metaheuristics in 12 cases, as presented in Table 12. Overall, according to the results shown in Tables 9 and 10, the hybrid algorithm provides a competitive result compared to other metaheuristic algorithms in terms of efficiency.

Similar to the previous section, we conducted Wilcoxon's rank test and Friedman statistical test based on the mean results of Tables 9, 10, and 12. The Wilcoxon's rank test results presented in Tables 15, 16, and 18 were derived from

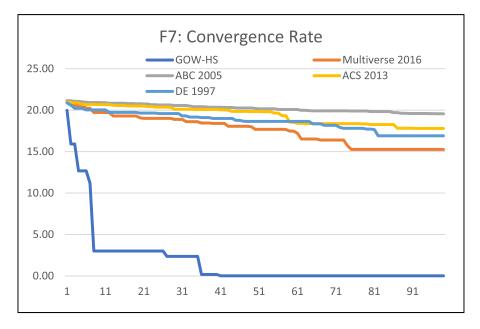


FIGURE 5. Convergence curve for f7.

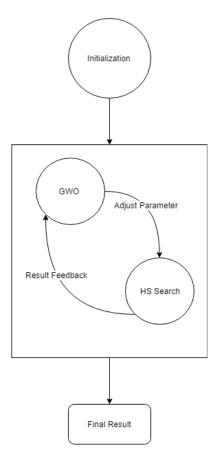


FIGURE 6. The general process of GWO/HS hybrid algorithm.

30, 50 dimensions of classical benchmark functions, and CEC2014 test cases, respectively.

As shown in Tables 15 and 16, the hybrid algorithm provides very small p-values. Therefore, it outperforms all

other metaheuristic algorithms and provides very high significant improvement. Table 18 shows the results based on CEC2014 experiment results presented in Table 12. The hybrid algorithm provides high significance results against two algorithms, namely, ACS and DE.

For the Friedman test, Table 20 presents a full overview of the classical benchmark functions with two dimensions, 30 and 50, and the CEC test cases. As seen in the classical experiments, the hybrid algorithm has the lowest value on Friedman test, which means it has the highest ranking among other metaheuristics. For the CEC2014 experiment, the hybrid algorithm has the second raking following ACS algorithm.

To provide insight into the hybrid algorithm convergence rate, we run experiment using four benchmark functions. Two functions with unimodal optimum (F1, F4), and two functions with multimodal optimum (F6, F7). Figures (2 - 5) illustrate the best score obtained so far of the hybrid algorithm and other HS variants versus the iteration.

VII. CONCLUSION

This paper presents a new hybrid algorithm of the HS algorithm with the GWO algorithm called GWO-HS algorithm for the global continuous optimization problem. The new hybrid algorithm solves the parameter selection problem of the HS algorithm by using another algorithm, namely, GWO, to modify the values of the PAR and BW parameters as a selfadaptive process. Another modification is performed to harmonize search by applying the modified opposition technique to the search result and improving the obtained results. The GWO-HS convergence is very high compared to the existing HS variants due to the opposition technique, and GWO-HS can reach the optimum results with less iterations. The new hybrid algorithm can cover different types of problems with

the same parameter setting, which makes it a better version of HS than the original one. Two groups of evaluation tests are used to examine the new algorithm performance. First, we compare the hybrid algorithm with the recent variants of the HS algorithm using different types of optimization functions, namely, 24 classical and 30 CEC2014 benchmark functions. The results show that the hybrid algorithm is better than the previous variants in terms of accuracy and provides competitive time consumption. Additionally, the algorithm has been evaluated with well-known metaheuristics from different families. The hybrid algorithm shows improved results and speed compared with these algorithms. The new hybrid algorithm shows high performance, which is essential in solving real-world optimization. Therefore, we recommend using a new algorithm to solve real-world problems. The current experiment focuses on continuous benchmark functions. Future work could utilize the new hybrid algorithm in discrete optimization problems.

REFERENCES

- K. Sörensen, "Metaheuristics—The metaphor exposed," Int. Trans. Oper. Res., vol. 22, no. 1, pp. 3–18, 2015.
- [2] S. Kirkpatrick, C. D. Gelatt, and M. P. Vecchi, "Optimization by simulated annealing," *Science*, vol. 220, no. 4598, pp. 671–680, 1983.
- [3] Z. W. Geem, J. H. Kim, and G. V. Loganathan, "A new heuristic optimization algorithm: Harmony search," *Simulation*, vol. 76, no. 2, pp. 60–68, Feb. 2001.
- [4] L. J. Fogel, A. J. Owens, and M. J. Walsh, Artificial Intelligence Through Simulated Evolution. Hoboken, NJ, USA: Wiley, 1966.
- [5] F. Glover, "Heuristics for integer programming using surrogate constraints," *Decis. Sci.*, vol. 8, no. 1, pp. 156–166, 1977.
- [6] K. S. Lee and Z. W. Geem, "A new structural optimization method based on the harmony search algorithm," *Comput. Struct.*, vol. 82, nos. 9–10, pp. 781–798, 2004.
- [7] A. E. Eiben and C. A. Schippers, "On evolutionary exploration and exploitation," *Fundam. Inform.*, vol. 35, nos. 1–4, pp. 35–50, 1998.
- [8] O. Castillo, P. Melin, F. Valdez, J. Soria, E. Ontiveros-Robles, C. Peraza, and P. Ochoa, "Shadowed type-2 fuzzy systems for dynamic parameter adaptation in harmony search and differential evolution algorithms," *Algorithms*, vol. 12, no. 1, p. 17, 2019.
- [9] C. Peraza, F. Valdez, J. R. Castro, and O. Castillo, "Fuzzy dynamic parameter adaptation in the harmony search algorithm for the optimization of the ball and beam controller," *Adv. Oper. Res.*, vol. 2018, Aug. 2018, Art. no. 3092872.
- [10] Z. W. Geem, J. H. Kim, and G. Loganathan, "Harmony search optimization: Application to pipe network design," *Int. J. Model. Simul.*, vol. 22, no. 3, pp. 125–133, 2002.
- [11] A. Vasebi, M. Fesanghary, and S. M. T. Bathaee, "Combined heat and power economic dispatch by harmony search algorithm," *Int. J. Elect. Power Energy Syst.*, vol. 29, no. 3, pp. 713–719, 2007.
- [12] Z. W. Geem, "Optimal cost design of water distribution networks using harmony search," *Eng. Optim.*, vol. 38, no. 3, pp. 259–277, 2006.
- [13] Z. W. Geem, "Improved harmony search from ensemble of music players," in *Knowledge-Based Intelligent Information and Engineering Systems*. Berlin, Germany: Springer, 2006.
- [14] M. A. Al-Betar and A. T. Khader, "A harmony search algorithm for University course timetabling," Ann. Oper. Res., vol. 194, no. 3, pp. 3–31, 2012.
- [15] A. K. Alazzawi, A. A. B. Homaid, A. A. Alomoush, and A. A. Alsewari, "Artificial bee colony algorithm for pairwise test generation," *J. Telecommun., Electron. Comput. Eng.*, vol. 9, nos. 1–2, pp. 103–108, 2017.
- [16] A. R. A. Alsewari and K. Z. Zamli, "A harmony search based pairwise sampling strategy for combinatorial testing," *Int. J. Phys. Sci.*, vol. 7, no. 7, pp. 1062–1072, 2012.
- [17] K. Z. Zamli, A. A. Al-Sewari, and M. H. M. Hassin, "On test case generation satisfying the MC/DC criterion," *Int. J. Adv. Soft Comput. Appl.*, vol. 5, no. 3, pp. 104–115, 2013.

- [18] A. A. Alsewari, K. Z. Zamli, and B. Al-Kazemi, "Generating t-way test suite in the presence of constraints," *J. Eng. Technol.*, vol. 6, no. 2, pp. 52–66, 2015.
- [19] D. Manjarres, I. Landa-Torres, S. Gil-Lopez, J. D. Ser, M. N. Bilbao, S. Salcedo-Sanz, and Z. W. Geem, "A survey on applications of the harmony search algorithm," *Eng. Appl. Artif. Intell.*, vol. 26, no. 8, pp. 1818–1831, 2013.
- [20] A. Ala'a, A. A. Alsewari, H. S. Alamri, and K. Z. Zamli, "Comprehensive review of the development of the harmony search algorithm and its applications," *IEEE Access*, vol. 7, pp. 14233–14245, 2019.
- [21] M. Mahdavi, M. Fesanghary, and E. Damangir, "An improved harmony search algorithm for solving optimization problems," *Appl. Math. Comput.*, vol. 188, no. 2, pp. 1567–1579, May 2007.
- [22] M. G. H. Omran and M. Mahdavi, "Global-best harmony search," Appl. Math. Comput., vol. 198, no. 2, pp. 643–656, 2008.
- [23] Q.-K. Pan, P. N. Suganthan, M. F. Tasgetiren, and J. J. Liang, "A selfadaptive global best harmony search algorithm for continuous optimization problems," *Appl. Math. Comput.*, vol. 216, no. 3, pp. 830–848, 2010.
- [24] M. El-Abd, "An improved global-best harmony search algorithm," Appl. Math. Comput., vol. 222, pp. 94–106, Oct. 2013.
- [25] H. Abedinpourshotorban, S. Hasan, S. M. Shamsuddin, and N. F. As'Sahra, "A differential-based harmony search algorithm for the optimization of continuous problems," *Expert Syst. Appl.*, vol. 62, pp. 317–332, Nov. 2016.
- [26] A. Assad and K. Deep, "A hybrid harmony search and simulated annealing algorithm for continuous optimization," *Inf. Sci.*, vol. 450, pp. 246–266, Jun. 2018.
- [27] Á. E. Eiben, R. Hinterding, and Z. Michalewicz, "Parameter control in evolutionary algorithms," *IEEE Trans. Evol. Comput.*, vol. 3, no. 2, pp. 124–141, Jul. 1999.
- [28] S. Mirjalili, S. M. Mirjalili, and A. Lewis, "Grey wolf optimizer," Adv. Eng. Softw., vol. 69, pp. 46–61, Mar. 2014.
- [29] H. R. Tizhoosh, "Opposition-based learning: A new scheme for machine intelligence," in Proc. Int. Conf. Comput. Intell. Modelling, Control Automat., Int. Conf. Intell. Agents, Web Technol. Internet Commerce, Nov. 2005, pp. 695–701.
- [30] L. Rodríguez, O. Castillo, J. Soria, P. Melin, F. Valdez, C. I. Gonzalez, G. E. Martinez, and J. Soto, "A fuzzy hierarchical operator in the grey wolf optimizer algorithm," *Appl. Soft Comput.*, vol. 57, pp. 315–328, Aug. 2017.
- [31] G. M. Komaki and V. Kayvanfar, "Grey wolf optimizer algorithm for the two-stage assembly flow shop scheduling problem with release time," *J. Comput. Sci.*, vol. 8, pp. 109–120, May 2015.
- [32] T. Jayabarathi, T. Raghunathan, B. R. Adarsh, and P. N. Suganthan, "Economic dispatch using hybrid grey wolf optimizer," *Energy*, vol. 111, pp. 630–641, Sep. 2016.
- [33] S. Zhang, Y. Zhou, Z. Li, and W. Pan, "Grey wolf optimizer for unmanned combat aerial vehicle path planning," *Adv. Eng. Softw.*, vol. 99, pp. 121–136, Sep. 2016.
- [34] X. Song, L. Tang, S. Zhao, X. Zhang, L. Li, J. Huang, and W. Cai, "Grey Wolf Optimizer for parameter estimation in surface waves," *Soil Dyn. Earthquake Eng.*, vol. 75, pp. 147–157, Aug. 2015.
- [35] Q. Xu, L. Wang, N. Wang, X. Hei, and L. Zhao, "A review of oppositionbased learning from 2005 to 2012," *Eng. Appl. Artif. Intell.*, vol. 29, pp. 1–12, Mar. 2014.
- [36] X. Z. Gao, X. Wang, S. J. Ovaska, and K. Zenger, "A hybrid optimization method of harmony search and opposition-based learning," *Eng. Optim.*, vol. 44, no. 8, pp. 895–914, 2012.
- [37] W.-L. Xiang, M.-Q. An, Y.-Z. Li, R.-C. He, and J.-F. Zhang, "An improved global-best harmony search algorithm for faster optimization," *Expert Syst. Appl.*, vol. 41, no. 13, pp. 5788–5803, Oct. 2014.
- [38] Z. Guo, S. Wang, X. Yue, and H. Yang, "Global harmony search with generalized opposition-based learning," *Soft Comput.*, vol. 21, no. 3, pp. 2129–2137, 2017.
- [39] C. Peraza, F. Valdez, M. Garcia, P. Melin, and O. Castillo, "A new fuzzy harmony search algorithm using fuzzy logic for dynamic parameter adaptation," *Algorithms*, vol. 9, no. 4, p. 69, 2016.
- [40] R. Eberhart and J. Kennedy, "A new optimizer using particle swarm theory," in *Proc. 6th Int. Symp. Micro Mach. Hum. Sci. (MHS)*, Oct. 1995, pp. 39–43.
- [41] S. Das, A. Mukhopadhyay, A. Roy, A. Abraham, and B. K. Panigrahi, "Exploratory power of the harmony search algorithm: Analysis and improvements for global numerical optimization," *IEEE Trans. Syst., Man, Cybern. B, Cybern.*, vol. 41, no. 1, pp. 89–106, Apr. 2011.

- [42] C.-M. Wang and Y.-F. Huang, "Self-adaptive harmony search algorithm for optimization," *Expert Syst. Appl.*, vol. 37, no. 3, pp. 2826–2837, 2010.
- [43] O. Castillo, F. Valdez, J. Soria, L. Amador-Angulo, P. Ochoa, and C. Peraza, "Comparative study in fuzzy controller optimization using bee colony, differential evolution, and harmony search algorithms," *Algorithms*, vol. 11, no. 4, p. 341, 1997.
- [44] J. Liang and B. P. Qu Suganthan, "Problem definitions and evaluation criteria for the CEC 2014 special session and competition on single objective real-parameter numerical optimization," Comput. Intell. Lab., Zhengzhou Univ., Zhengzhou, China, Tech. Rep., 2013.
- [45] P. Civicioglu, "Artificial cooperative search algorithm for numerical optimization problems," *Inf. Sci.*, vol. 229, pp. 58–76, Apr. 2013.
- [46] S. Mirjalili, S. M. Mirjalili, and A. Hatamlou, "Multi-verse optimizer: A nature-inspired algorithm for global optimization," *Neural Comput. Appl.*, vol. 27, no. 2, pp. 495–513, 2016.
- [47] D. Karaboga, "An idea based on honey bee swarm for numerical optimization," Comput. Eng. Fac., Erciyes Univ., Kayseri, Turkey, Tech. Rep. TR06, 2005,
- [48] R. Storn and K. Price, "Differential evolution-a simple and efficient heuristic for global optimization over continuous spaces," J. Global Optim., vol. 11, no. 4, pp. 341–359, 1997.



ALAA A. ALOMOUSH received the B.Sc. degree in computer science from Al Albayt University, in 2010, the M.Sc. degree from University Putra Malaysia, in 2013. He is currently pursuing the Ph.D. degree in computer science with the Faculty of Computer Systems and Software Engineering, Universiti Malaysia Pahang. His main research interests include artificial intelligence and computational intelligence.



ABDULRAHMAN A. ALSEWARI was born in Sana'a, Yemen, in 1980. He received the B.Eng. degree in computer engineering from the Military College of Engineering, Baghdad, Iraq, in 2002, and the M.Sc. degree in electronic system design engineering and the Ph.D. degree in software engineering from the Universiti Sains Malaysia, in 2008 and 2012, respectively. From 2012 to 2013, he was an Assistant Professor and a Head of the Information Technology Department,

Engineering College, DarAssalam International University for Science and Technology, Yemen. Since 2013, he has been a Senior Lecturer (Assistant Professor) and a Researcher with the Software Engineering Department, Faculty of Computer Systems and Software Engineering, Universiti Malaysia Pahang. He has authored and coauthored one book, more than 30 articles, and more than 10 inventions. His research interests include software engineering, software testing, optimization algorithms, artificial intelligence, soft computing, embedded systems, and image processing.



HAMMOUDEH S. ALAMRI received the B.Sc. degree in computer engineering from Yarmouk University, in 2008, and the M.Sc. degree from the University Malaysia Pahang, in 2016, where he is currently pursuing the Ph.D. degree in computer science with the Faculty of Computer Systems and Software Engineering. His main research interests include optimization algorithms, the IoT, and computational intelligence.



KHALID ALOUFI received the B.Sc. degree in computer engineering from the King Fahd University of Petroleum and Minerals (KFUPM), Saudi Arabia, in 1999, and the M.Sc. and Ph.D. degrees in informatics from Bradford University, U.K., in 2002 and 2006, respectively. From 2002 to 2006, he was part of the Networks and Performance Engineering Research Group at Bradford University. Since 2013, he has been the Dean of the College of Computer Science and Engineering,

Taibah University, Medina, Saudi Arabia, where he is currently an Associate Professor with the Department of Computer Engineering.



KAMAL Z. ZAMLI received the degree in electrical engineering from the Worcester Polytechnic Institute, USA, in 1992, the M.Sc. degree in real-time software engineering from the Universiti Teknologi Malaysia, in 2000, and the Ph.D. degree in software engineering from the University of Newcastle upon Tyne, U.K., in 2003. He is currently a Professor and the Dean of the Faculty of Computer Systems and Software Engineering, Universiti Malaysia Pahang. He has authored and

coauthored one book, more than 30 articles, and more than 350 papers in journals and conferences worldwide mainly in the area of (combinatorial t-way) software testing and search based software engineering.

. . .