

# Development of Energy-Based Brittleness Index for Sandstone Subjected to Freeze-Thaw Cycles and Impact Loads

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**ABSTRACT** As one of the most important parameters of rock materials, brittleness is affected by external conditions such as temperature and dynamic disturbances. However, there is no universal criterion for brittleness. In this paper, the brittleness of sandstone subjected to rapid freeze–thaw (F–T) cycles and impact loads are investigated. The 25 specimens were subjected to different F–T cycles and impact loads and then investigated. It was found that the dynamic strength and Young’s modulus of the specimens decrease, whereas porosity increases after the application of F–T cycles. The dynamic stress–strain curves demonstrated that after the peak point, the rock sample first exhibited class I behavior and then class II behavior. Previous studies implied that the brittleness index based on the pre-peak stress–strain characteristics was not sufficient to describe the rock fracture. Two brittleness indices based on the pre-peak and post-peak strain energy were thus derived using the complete dynamic stress–strain characteristics of rock samples. The two brittleness indices were strongly correlated with the physical parameters, such as porosity and mechanical parameters, including peak stress and dynamic modulus.

**INDEX TERMS** Sandstone, energy, brittleness, freeze-thaw, impact load.

## I. INTRODUCTION

Rocks are often exposed to different external environments such as extreme temperature and impact loads. The behavior of rocks differs from each other owing to their external conditions. The mechanical and physical properties of different rocks subjected to F-T cycles have been studied by Altindag *et al.* [1], Fener and İnce [2], Karaca *et al.* [3], Momeni *et al.* [4], and Nicholson and Nicholson [5]. The results showed that with the increase in the number of F-T cycles, rocks exhibit deterioration and degradation to some extent in terms of the strength, P wave velocity and mass. Several studies have already focused on the mechanical properties of rocks under impact loads [6]–[8]. However, only a few studies have investigated the degradation of rocks under the combined effects of F-T cycles and impact loads.

Brittleness is an important mechanical property of intact rocks owing to its strong influence on the failure process of a rock mass, which is relevant to civil activities such as

tunneling and mining. The concept of brittleness corresponds to the fracture characteristics of hard and strong materials. Rock behavior (see Figure 1) can be divided into class I behavior or class II behavior based on the classification proposed by Wawersik and Fairhurst [9]. However, the concept of brittleness has not yet been defined by a universal criterion. Brittleness can be treated as an intrinsic material property or as the material behavior under an external loading system that contributes additional energy to the failure process [10]. In the past years, different brittleness criteria have been proposed to characterize rock behavior under compression. Table 1 summarizes the existing brittleness criteria.

Brittleness indices can be expressed using different formulae, based on which parameters have been adopted to define the brittleness index. However, a brittleness index may be suitable for a certain situation but not for another. For example, the brittleness indices based on elastic and plastic strain ( $B_1$ – $B_5$ ) are found to be insufficient to describe the

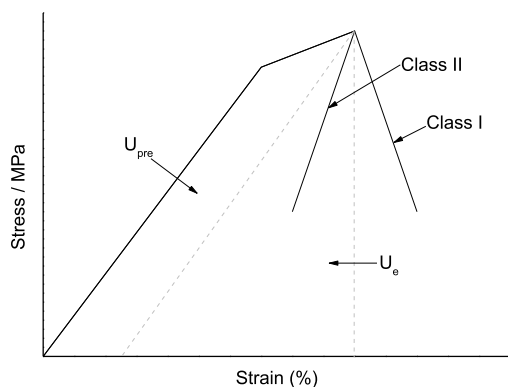


FIGURE 1. Scheme of representative stress-strain curves for two classes of rock failure behavior in uniaxial compression [9].

failure behavior of rock [10]. In some cases, it is necessary to also consider the pre-peak and post-peak characteristics. By extension, brittleness indices based on strength ( $B_6$ – $B_9$ ), mineral composition ( $B_{20}$ – $B_{23}$ ), Young’s modulus and Poisson’s ratio ( $B_{24}$ – $B_{29}$ ), Mohr’s envelope ( $B_{30}$ ), hardness ( $B_{31}$ ), porosity ( $B_{32}$ ) and percentage of fines ( $B_{33}$ – $B_{34}$ ), among others are not sufficient to describe the rock behavior precisely. Brittleness indices, i.e.  $B_{12}$ ,  $B_{13}$  and  $B_{14}$ , which based on pre-peak and post-peak strain energies, showed good correspondence with mechanical properties such as peak stress, crack damage stress and tangent Young’s modulus. The author also demonstrates that brittleness indices  $B_{10}$  and  $B_{11}$  were not able to correlate well with the three pre-peak parameters. From the discussion above, it can be seen that the brittleness indices based on both pre-peak and post-peak energy can characterize the rock behavior.

In this study, 25 sandstone samples under F-T cycles and impact load were analyzed. Porosity and dynamic stress-strain curves were investigated. Based on the classification of Wawersik and Fairhurst [9], two brittleness indices were proposed; these were defined as the ratio of the energy consumed during class I behavior and the elastic energy and that during class II behavior and the elastic energy. Finally, the correlations between the proposed brittleness indices and F-T cycles, porosity, peak stress and Young’s modulus were obtained.

## II. MATERIALS AND METHODS

### A. SPECIMEN PREPARATION

Porous sandstone formed underneath seabed or land contains a large amount of intergranular pore spaces. The mechanical behavior of sandstones has been investigated previously [37]. To perform this research, cylindrical sandstone samples were cored from a rock block. The diameter of each specimen was 50 mm, and their aspect ratio (i.e., length to diameter) was maintained at 1 [38] for dynamic tests. The diameter of sample was more than 20 times larger than the grain size, thereby satisfying the specimen size recommended by the International Society for Rock Mechanics (ISRM). The surface of the specimens was prepared to be smooth and straight.

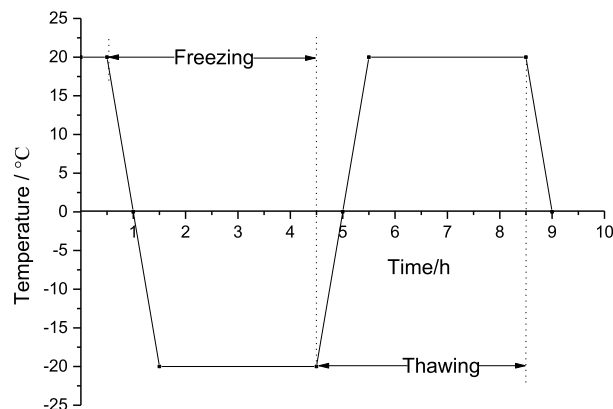


FIGURE 2. Temperature versus time curve.

In order to reduce the friction, surface roughness of the cylindrical samples is less than 0.02mm and the end surfaces perpendicular to its axis is less than 0.001 radians. The rock samples corresponded to fine grain-size rock having a dry density of  $2.21 \text{ g/cm}^3$ . Before the experiment, water-physical properties of the selected sandstones were determined, and the results are presented in Table 2.

### B. EXPERIMENTAL METHODS

In total, 25 specimens were used. These specimens were divided into 5 groups with each group comprising 5 specimens. For each group, rapid F-T tests were conducted, and the corresponding rate of change of temperature is shown in Figure 2. In this study for freezing and thawing, temperatures of  $-20^\circ\text{C}$  and  $20^\circ\text{C}$  were adopted respectively according to the average highest and lowest temperatures of the rock block location. A TDS-300 F-T machine with a lowest freezing temperature of  $-40^\circ\text{C}$  and a highest thawing temperature of  $20^\circ\text{C}$  was used to conduct the F-T treatment of the samples. The F-T cycles of each group were repeated 0, 20, 60, 100 and 140 times. Each F-T cycle lasted 8 h (i.e., 4 h freezing and 4 h thawing) according to the “Test Methods of Rock for Highway Engineering” proposed by the Ministry of Transport of the People’s Republic of China.

Nuclear Magnetic Resonance (NMR) is a non-destructive technology to measure the characteristics of a rock’s internal structure [39], such as pore size distribution and permeability [40]–[42], based on the measurement of signal decay of hydrogen atoms in a fully saturated rock sample. The NMR analysis system is suitable to measure the porosity of saturated specimens. In this study, a low field NMR analysis system (type AniMR-150) manufactured by Niumai Electric Technology Company was used. NMR tests were conducted after the F-T cycles for each specimen to measure the porosity. Figure 3 shows the  $T_2$  relaxation time and accumulative porosity curve based on the results of  $T_2$  relaxation time. A final porosity of 7.197% was obtained from the results shown in Figure 3.

TABLE 1. Summary of existing brittleness indices definitions.

Measurement methods	Formula	Description	References
Based on strain	$B_1 = \varepsilon_r / \varepsilon_e$	$\varepsilon_r$ and $\varepsilon_e$ are the reversible strain and total strain at the failure point, respectively	[12]
	$B_2 = \frac{\varepsilon_p}{\varepsilon_e}$	$\varepsilon_p$ , $\varepsilon_e$ and $\varepsilon_{tp}$ are the elastic strain, post-peak strain and total irreversible post-peak strain, respectively	[13]
	$B_3 = \frac{\varepsilon_{tp}}{\varepsilon_e}$		
	$B_4 = \frac{\varepsilon_f^p - \varepsilon_c^p}{\varepsilon_c^p}$	$\varepsilon_f^p$ is the plastic strain at which the friction strength is fully mobilized, $\varepsilon_c^p$ is the plastic strain at which cohesive strength reduces to its residual value	[14]
Based on strength	$B_5 = \varepsilon_{ir} * 100$	$\varepsilon_{ir}$ is the irreversible longitudinal strain	[15]
	$B_6 = \frac{\sigma_c - \sigma_t}{\sigma_c + \sigma_t}$	$\sigma_c$ and $\sigma_t$ are the compressive and tensile strengths, respectively	[12]
	$B_7 = \frac{\tau_p - \tau_r}{\tau_p}$	$\tau_p$ is the peak shear strength, $\tau_r$ is the residual shear strength	[16]
	$B_8 = \frac{\sigma_c \sigma_t}{2}$	$\sigma_c$ and $\sigma_t$ are the compressive and tensile strengths, respectively	[17, 18]
Based on energy	$B_9 = \sqrt{\sigma_c \sigma_t} / 2$	$U_e$ and $U_{peak}$ are the elastic energy and strain energy until peak stress, respectively	[12]
	$B_{10} = U^e / U^{peak}$		[12]
	$B_{11} = U_{pre} / U_e$	$U_e$ is the elastic energy, $U_{pre}$ is the pre-peak energy	[19]
	$B_{12} = U_e / U_{total}$	$U_e$ is the elastic energy, $U_{total}$ is the total fracture energy, $U_{post}$ is the post-peak energy	[11]
	$B_{13} = U_e / U_{post}$		
	$B_{14} = U_{peak} / U_{total}$	$E$ is the elastic modulus and $M$ is the post-peak modulus	[10]
	$B_{15} = M - E / M$		
	$B_{16} = E / M$	$E$ is the elastic modulus and $M$ is the post-peak modulus	[20-24]
	$B_{17} = M / E + M$		
	$B_{18} = M / E$	$H$ is the hardening modulus and $E$ is the Young's modulus	[25]
$B_{19} = \frac{H}{E}$			
Based on mineral composition	$B_{20} = \frac{F_{Qtz}}{F_{Qtz} + F_{Cb+Clty}}$	$F$ indicates fraction, mineral abbreviations are Qtz = quartz, Cb = carbonate, Clty = clay, Dol = dolomite, Cal = calcite	[26]
	$B_{21} = \frac{F_{Qtz+Dol}}{F_{Qtz+Dol} + F_{Cal+Clty+TOC}}$		[27]
	$B_{22} = \frac{F_{Qtz+Cb}}{F_{Qtz+Cb} + F_{Cal+TOC}}$	[28]	
	$B_{23} = \frac{w_{QFP} F_{QFP}}{w_{QFP} F_{QFP} + w_{Cb} F_{Cb} + w_{CltyTOC} F_{CltyTOC} + w_{\emptyset}}$	$w_{QFP}$ , $w_{Cb}$ , $w_{CltyTOC}$ , and $w_{\emptyset}$ are weighting factors that range between 0 and 1 and may be adapted to deformation conditions	[25]
		$E$ is the elastic modulus, $E_{min}$ and $E_{max}$ are the maximum and minimum Young's moduli, respectively	[29]
Based on Young's modulus and Poisson's ratio	$B_{24} = \frac{E - E_{min}}{E_{max} - E_{min}}$	$E_{min}$ and $E_{max}$ are the maximum and minimum Young's moduli, respectively; $v_{max}$ and $v_{min}$ are the maximum and minimum Poisson's ratio, respectively	[30]
	$B_{25} = \frac{1}{2} \left[ \frac{E - E_{min}}{E_{max} - E_{min}} + \frac{v_{max} - v}{v_{max} - v_{min}} \right]$		
	$B_{26} = \frac{E}{v}$	$E$ and $v$ are the Young's modulus and Poisson's ratio, respectively	[31]
	$B_{27} = \frac{E\rho}{v}$	$E$ and $v$ are the Young's modulus and Poisson's ratio, respectively; $\rho$ is the rock density	[32]
	$B_{28} = \frac{\lambda + 2\mu}{\lambda}$	$\lambda$ is Lamé's first parameter and $\mu$ is the shear modulus	[33]
Based on Mohr's envelope	$B_{29} = \frac{E}{\lambda}$	$E$ is Young's modulus and $\lambda$ is Lamé's first parameter	[34]
	$B_{30} = \sin\theta$	$\theta$ is the internal friction angle	[12]
		$H_{\mu}$ is the micro-indentation hardness, $H$ is the macro-indentation hardness and $K$ is a constant	[12]
Based on hardness	$B_{31} = \frac{H_{\mu} - H}{K}$		[12]
	$B_{32} = -1.8748 * \emptyset + 0.9679$	$\emptyset$ is the neutron porosity	[35]
Based on porosity		$F_{max}$ is the maximum applied force and $P$ is the corresponding penetration	[36]
	$B_{33} = \frac{F_{max}}{P}$		[36]
	$B_{34} = q\sigma_c$	$q$ is percentage of fines (-28 mesh) formed in protodyakonov impact test, $\sigma_c$ is uniaxial compression strength	[12]

TABLE 2. Water-physical properties of selected samples.

Specimen	Dry weight	Wet weight	Saturation weight	Water absorption	Saturation ratio	Saturation coefficient
1	428.77 g	449.18 g	460.31 g	4.76%	7.36%	0.65
2	417.67 g	438.08 g	448.51 g	4.89%	7.38%	0.66
3	429.65 g	449.88 g	461.00 g	4.71%	7.30%	0.65
Average	425.36 g	445.71 g	456.61 g	4.78%	7.35%	0.65

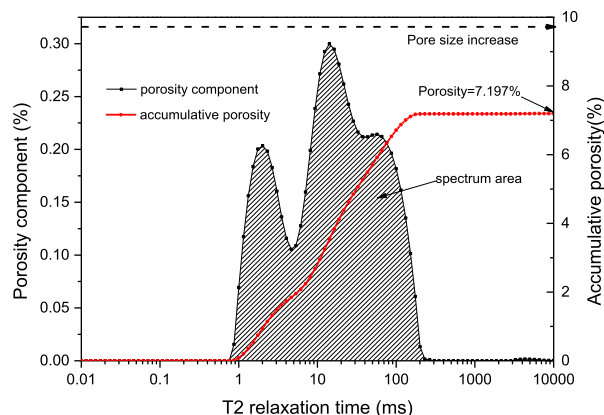


FIGURE 3. Method to calculate porosity.

The NMR tests were followed by dynamic compression tests conducted using a Splitting Hopkinson Pressure Bar (SHPB) to obtain the dynamic stress-strain curve for each specimen. The impact pressure of the SHPB test is 0.45MPa and the strain rate is about  $75s^{-1}$ .

C. TEST APPARATUS

A cyclic F-T testing machine (see Figure 4a), an NMR testing system (see Figure 4b) and an SHPB testing system (see Figure 4c) were used in this study.

III. PHYSICAL AND MECHANICAL RESULTS

A. POROSITY OF DETERIORATED SAMPLES

The porosity measured using the NMR system is shown in Figure 5. It was found that the porosity increases with the increase in the number of F-T cycles. The initial porosity of sandstone was 7.207%, and it increased to 11.4% when 140 F-T cycles were used. The main factor responsible for this increase in porosity is the temperature. During the F-T process, the frost heave force exceeds the bonding force between the mineral particles, which leads to the generation of new pores. The coefficient of correlation indicates good correspondence between the porosity and F-T cycles.

B. DYNAMIC STRESS-STRAIN CURVES

Figure 6a presents the stress equilibrium during the impact test. Figure 6b shows the dynamic stress-strain curves of specimens under different F-T cycles, and Table 3 lists the statistical dynamic strength, Young’s modulus and porosity. The data in Figure 6b and Table 3 demonstrates that the dynamic strength and Young’s modulus decrease with the

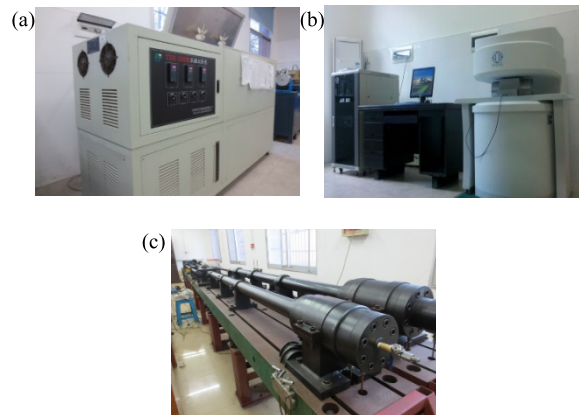


FIGURE 4. Test apparatus. (a) Cyclic F-T testing machine (b) NMR testing system (c) SHPB testing system.

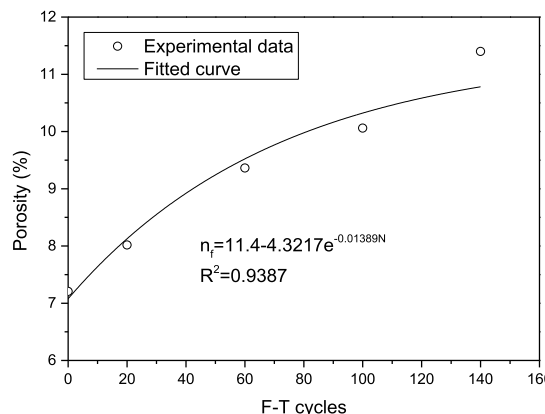


FIGURE 5. Correlation between F-T cycles and porosity.

increase in the number of F-T cycles. The results were similar to those obtained in other research [43], [44]. It also demonstrated that the post-peak stress-strain characteristics exhibit two different behaviors based on the classification proposed by Wawersik and Fairhurst [9]. After the peak point, the rock samples first exhibit class I behavior and then class II behavior. This means that during the fracturing process, the rock samples transition from being ductile to brittle.

IV. PRE-PEAK AND POST-PEAK ENERGY-BASED BRITTLENESS INDEX

Figure 1 shows the classification of class I and class II behaviors. It can be seen that brittleness indices  $B_{10}$  [12] and  $B_{11}$  [19], which are based on pre-peak stress-strain relations, may be equal, even though the post-peak behavior

TABLE 3. Statistical results of mechanical and physical parameters.

F-T cycles	Porosity (%)	Dynamic strength/MPa	Young's modulus/GPa
0	7.207	95.9	16.14
20	8.018	88.5	13.76
60	9.362	83.4	12.20
100	10.06	79.1	11.26
140	11.4	72.7	10.50

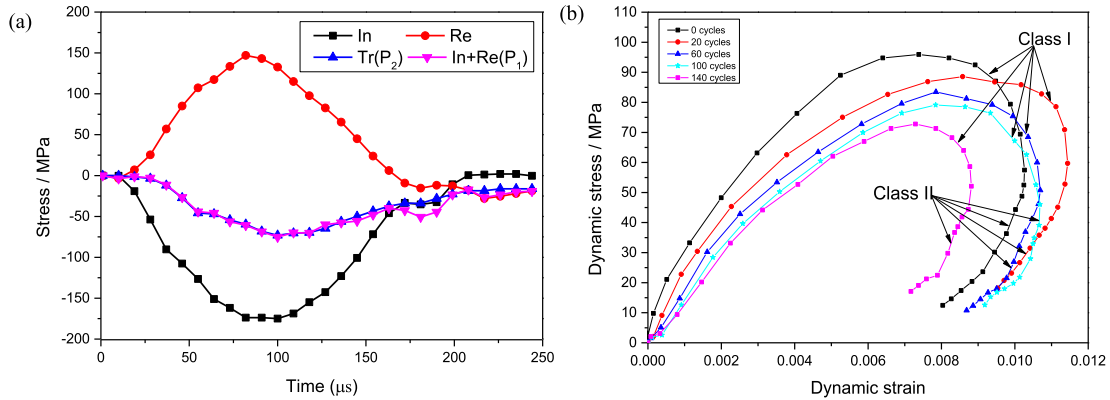


FIGURE 6. (a) stress equilibrium (b) dynamic stress-strain curves under different F-T cycles.

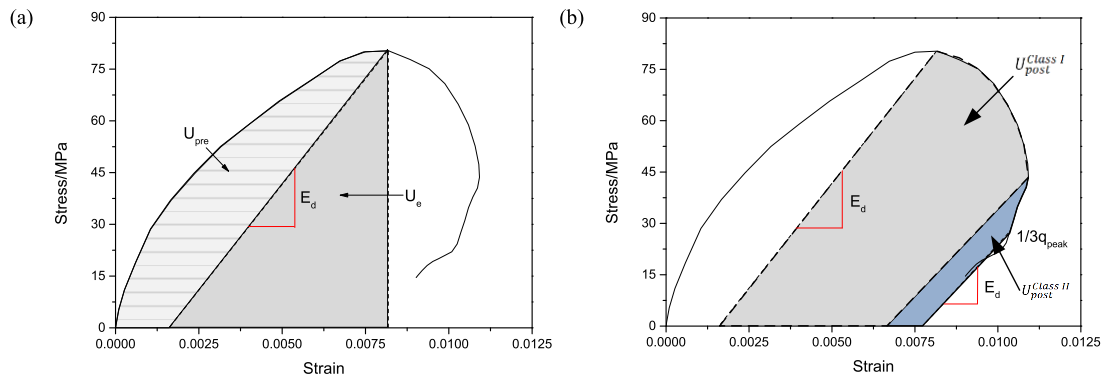


FIGURE 7. Strain energy of rock samples in dynamic compression.

was entirely different. Thus, it is necessary to take the post-peak stress-strain relations into consideration when defining a brittleness index.

The analysis described in the introduction shows that brittleness indices based on pre-peak behavior are not sufficient to describe the rock failure behavior. In addition, brittleness indices obtained from the static stress-strain relations are not sufficient to describe the rock failure behavior under impact load. As a result, two brittleness indices are proposed based on the pre-peak and post-peak dynamic stress-strain relations following energy balance to describe the rock behavior under impact load.

The elastic energy per unit volume of rock  $U_e^{peak}$  was evaluated by the area shown in Figure 7a. The post-peak energy was calculated using the unloaded pre-peak stress-strain curve and under the post-peak stress-strain as shown in Figure 7b. The post-peak energy is composed of

the fracture energies consumed during class I and class II behaviors, and it is expressed by the following equation:

$$U_{post} = U_{post}^{Class I} + U_{post}^{Class II} \quad (1)$$

As presented in Figure 7b, an increase in energy consumed during class I behavior (i.e.,  $U_{post}^{Class I}$ ) indicates the increase in brittleness. Conversely, an increase in the energy consumed during class II behavior (i.e.,  $U_{post}^{Class II}$ ) indicates the decrease in brittleness.

The following brittleness indices based on energy balance under impact load are proposed herein:

$$B_{U-1} = \frac{U_{post}^{Class I}}{U_e^{peak}} \quad (2)$$

$$B_{U-2} = \frac{U_{post}^{Class II}}{U_e^{peak}} \quad (3)$$

TABLE 4. Pre-peak and post-peak stress-strain quantities for the samples.

F-T cycles	$U_{total}$	$U_{peak}$	$U_e^{peak}$	$U_{pre}$	$U_{post}$	$U_{post}^{Class I}$	$U_{post}^{Class II}$	$B_{U-1}$	$B_{U-2}$
0	0.682	0.487	0.282	0.205	0.473	0.431	0.042	1.5445	0.1319
20	0.616	0.452	0.285	0.168	0.440	0.39	0.05	1.3995	0.147
60	0.579	0.432	0.285	0.147	0.427	0.371	0.056	1.3171	0.1811
100	0.554	0.382	0.256	0.125	0.422	0.361	0.061	1.1852	0.2142
140	0.380	0.323	0.217	0.107	0.266	0.192	0.075	0.9178	0.3124

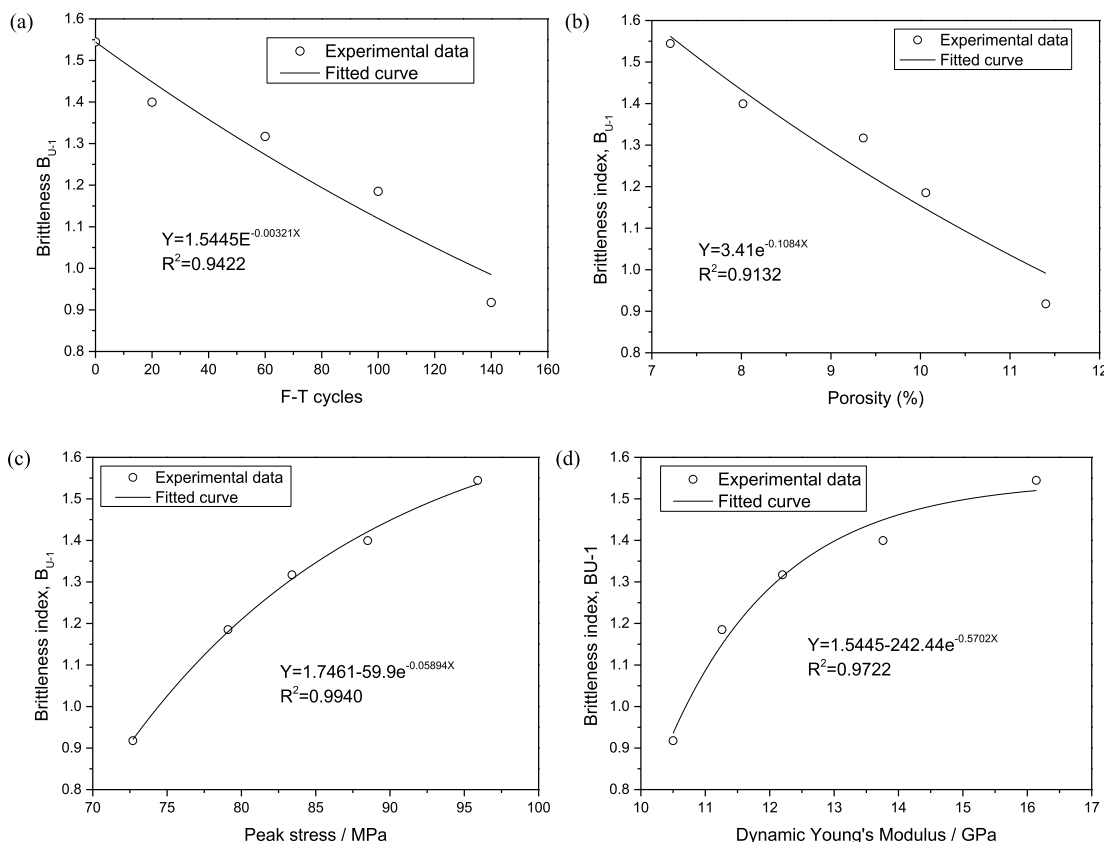


FIGURE 8. Correlation between brittleness index  $B_{U-1}$  and (a) F-T cycles, (b) porosity, (c) peak stress, (d) Young's modulus.

TABLE 5. Established relationships between brittleness indices and parameters.

Brittleness index	Parameter	Fitted curve	Decay constant	$R^2$
$B_{U-1}$	F-T cycles (N)	$B_{U-1} = 1.5445e^{-0.00321N}$	0.00321	0.9422
	Porosity ( $\rho$ )	$B_{U-1} = 3.41e^{-0.1084\rho}$	0.1084	0.9131
	Dynamic strength ( $q_{peak}$ )	$B_{U-1} = 1.7461-59.9e^{-0.05894q_{peak}}$	0.05894	0.9940
	Dynamic modulus ( $E_d$ )	$B_{U-1} = 1.5445-242.44e^{-0.5702E_d}$	0.5704	0.9722
$B_{U-2}$	F-T cycles (N)	$B_{U-2} = 0.1319e^{0.00583N}$	0.00583	0.9651
	Porosity ( $\rho$ )	$B_{U-2} = 0.02421e^{0.2218\rho}$	0.2218	0.9670
	Dynamic strength ( $q_{peak}$ )	$B_{U-2} = 6.74e^{-0.04279q_{peak}}$	0.04279	0.9429
	Dynamic modulus ( $E_d$ )	$B_{U-2} = 1.80e^{-0.1782E_d}$	0.1782	0.7693

where  $B_{U-1}$  and  $B_{U-2}$  are the two brittleness indices proposed in this paper,  $U_{post}^{Class I}$  is the energy consumed during class I behavior,  $U_{post}^{Class II}$  is the energy consumed during class II behavior.  $U_e^{peak}$  is the elastic energy stored in the specimen at the peak point. A larger value of  $B_{U-1}$  corresponds to a higher ductility of the rock. In contrast, a larger value of  $B_{U-2}$  indicates a more brittle rock.

Table 4 presents the pre-peak and post-peak stress-strain quantities for the samples, and the values of brittleness indices  $B_{U-1}$  and  $B_{U-2}$ . As shown in Table 4, the strain energy in both cases decreased to some extent with the increase in the number of F-T cycles, which means that the fracturing process required less energy if sandstone was deteriorated by the F-T cycles.

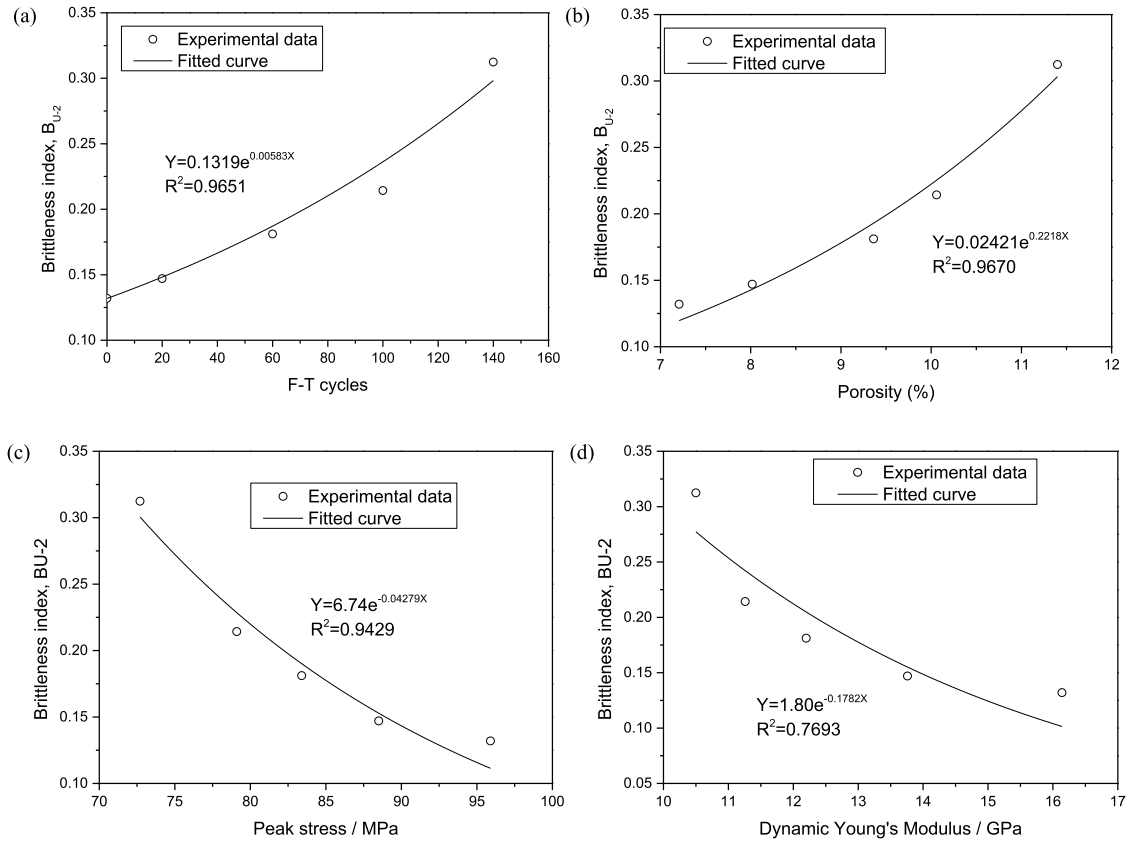


FIGURE 9. Correlation between brittleness index  $B_{U-2}$  and (a) F-T cycles, (b) porosity, (c) peak stress, (d) Young's modulus.

As demonstrated in Figures 8 and 9, the proposed brittleness indices  $B_{U-1}$  and  $B_{U-2}$  could describe the rock behavior properly. Brittleness  $B_{U-1}$  decreased in a nonlinear fashion with the increase in the number of F-T cycles and porosity, whereas  $B_{U-1}$  increased in a nonlinear manner with the increase in peak stress and Young's modulus. Brittleness  $B_{U-2}$  increased nonlinearly with increase in the number of F-T cycles and porosity, whereas  $B_{U-2}$  decreased nonlinearly with increase in peak stress and Young's modulus. This indicates that a larger number of F-T cycles lead to a lower brittleness  $B_{U-1}$  and a higher brittleness  $B_{U-2}$ , indicating a more brittle sandstone. From the results presented in Figures 8 and 9, a number of nonlinear relationships among the brittleness indices and F-T cycles, porosity, peak stress and Young's modulus were established and are presented in Table 5.

The results described above clearly demonstrate that the proposed brittleness indices are well correlated with F-T cycles, porosity, peak stress and Young's modulus. The results may thus be suitable for evaluating the drilling performance or the rock behavior under impact loads in cold regions.

## V. CONCLUSION

In this study, two brittleness indices based on pre-peak and post-peak energy were proposed to characterize the rock behavior under F-T cycles and impact load. The porosity and dynamic stress-strain curves were determined by using an NMR testing system and SHPB apparatus. Two brittleness indices were proposed to characterize the rock behavior under impact loads after F-T cycles. The following conclusions can be drawn from this study.

a) The porosity increases while the dynamic strength decreases when F-T cycles applied.

b) Stress-strain results demonstrated that the sandstone samples showed a combined class I and class II behavior under impact loads after F-T cycles. It was also found that with the increase in F-T cycles the sandstone became more brittle.

c) The two proposed brittleness indices were strongly correlated with porosity, peak stress and Young's modulus. The results of this study suggest that the pre-peak and post-peak energy-based brittleness indices could be used as indicators for evaluating the rock behavior under F-T cycles and impact loads.

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