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Multi-Agent Bargaining Learning for Distributed Energy Hub Economic Dispatch

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ABSTRACT This paper proposes a novel multi-agent bargaining learning (MABL) for the distributed energy hub economic dispatch (EHED) of multiple energy carrier systems (MECS). Distributed EHED is developed by extending the conventional economic dispatch (ED) into MECS in a distributed manner, in which each energy hub is regarded as a learning agent for self-scheduling. The classical Q-learning with associative memory is employed for knowledge learning of each agent, while the non-uniform mutation operator is adopted for handling the continuous control variables. To maximize the total payoff of all the energy hubs, the bargaining game is presented for achieving an effective coordination between the buyer agents and a seller agent, where the slack energy hub is designed as the seller agent and the others are the buyer agents. MABL has been thoroughly evaluated for the distributed EHED on a high-complex 39-hub MECS with 29 energy hub structures and 76 energy production units. Case studies verify the superior performance of MABL for the distributed EHED compared with six centralized heuristic optimization algorithms.

INDEX TERMS Multi-agent bargaining learning, distributed energy hub economic dispatch, multiple energy carrier systems, knowledge learning, bargaining game.

I. INTRODUCTION

In recent years, multiple energy carrier systems (MECS) has intrigued many scholars as it is an inventible solution for the future energy network [1], which will lead to a high energy utilizing efficiency, a low CO₂ emission, a high operation economy and flexibility [2]. Accordingly, an attendant energy hub, i.e., a functional unit where multiple energy carriers [3] are converted, stored, and dissipated, is employed for achieving the interaction between different energy carriers.

Based on this intuition, a novel energy hub economic dispatch (EHED) was developed in [4], which aims to minimize the operation cost by optimizing the energy inputs of all the energy hubs to balance different types of energy demands (i.e., electricity, heat, cool, and compressed air) while satisfying various operation constraints. Consequently, EHED is essentially an extension version of the conventional economic dispatch (ED), however, it is more difficult to handle the highly nonlinear, non-convex, non-smooth, non-differential, and high-dimensional EHED with more equality and inequality constraints. To tackle this issue, the heuristic optimization algorithms are commonly considered as priority

techniques since they are highly independent on the mathematical model, compared with the conventional gradient-based algorithms (e.g., interior-point method [5]), which usually obtain a local optimum for the highly nonlinear and non-convex optimization.

To obtain a high-quality optimal solution with a lower objective function for EHED, a self-adoptive learning with time varying acceleration coefficient-gravitational search algorithm (SAL-TVAC-GSA) was proposed in [4] by designing three fundamental modifications based on the original GSA, which has been proven excellent performance on solution quality and computation efficiency compared that of GSA [6], enhanced GSA (EGSA) [6], particle swarm optimization (PSO) [7], and genetic algorithm (GA) [8]. No doubt it can be effectively addressed by other heuristic optimization algorithms, e.g., artificial bee colony (ABC) [9] and differential evolution (DE) [10]. Nevertheless, most of these algorithms essentially belong to the centralized optimization algorithms, which easily leads to a high computation burden and poor performance with a low-quality optimal solution as the scale and complexity of MECS increases [11], while



it is also difficult to satisfy the demand of high privacy and security [12].

Generally speaking, the distributed optimization algorithms can effectively handle these problems. In [13], an event-triggered communication-based method was presented for distributed ED. Based on the consensus theory, a distributed primal-dual dynamic multiagent system [14] was proposed for dynamical ED. Moreover, a bargaining-based alternating direction method of multipliers (ADMM) [15] was designed for distributed EHED. However, all of them are only available for convex and smooth ED, which cannot address the non-convex, non-smooth ED. On the other hand, the distributed heuristic optimization algorithms, including cooperative co-evolutionary differential evolution [16], distributed PSO [17], distributed multi-step $Q(\lambda)$ learning [18], and so on, are more suitable for the distributed EHED, but all of them can only search a local optimal solution in most cases.

Over the years, multi-agent reinforcement learning (MARL) has attracted extensive investigations and real-world applications due to its distributed nature of the multi-agent solution [19], in which each agent can maximize its payoff by competing or cooperating with other agents, e.g., a deep communication for obtaining a high-quality optimal solution of the multi-agent system (MAS). Motivated from this benefit, a novel MARL was developed for an optimal reactive power dispatch by combining the consensus theory with the distributed Q-learning [20]. Besides, a game theory based hierarchical correlated Q-learning was designed for multi-layer optimal generation command dispatch [21] and reactive power optimization [22], respectively. All of these algorithms can achieve a satisfactory optimal solution, but ineluctably suffer from three flaws, as follows:

- Slow convergence rate: each agent will consume a large amount of computation time to acquire the optimal Q-value matrix, especially for the equilibrium computation [23], e.g., the Nash equilibria computation is polynomial parity arguments on directed graphs (PPAD)-hard [24].
- *Curse of dimension*: the joint action space will increase exponentially with the growing controllable variables [25], thus they are incapable of solving EHED in a large-scale MECS.
- Weak disposal ability for the continuous controllable variables: action space needs to be discretized into a finite number of cells for each controllable variable, thus the control accuracy will be contradictory with the computation time [26], i.e., the higher the control accuracy, the longer computation time and vice versa.

In order to resolve these problems, this paper proposes a novel MARL called multi-agent bargaining learning (MABL) for rapidly searching a high-quality optimal solution of distributed EHED.

The remaining of this paper is organized as follows. The mathematical model of distributed EHED is presented in

Section II. Section III provides the basic principle of MABL. The detailed design of MABL for distributed EHED is given in Section IV. Simulation results and conclusion are given in Section V and Section VI, respectively.

II. MATHEMATICAL MODEL OF DISTRIBUTED EHED

A. GENERAL MODEL OF ENERGY HUB

As illustrated in Fig. 1, energy hub can be treated as an interface between energy infrastructures and loads [27], which usually consists of connection devices (e.g., transformer), converters (e.g., combined heat and power (CHP) units), and storage devices. In practice, CHP units, combined heat, cool, and power (CHCP) units, big building complexes, small isolated systems, and so on, can be regarded as different energy hubs [28]. For a general energy hub, the relation model between the output energy carriers and the input energy carriers can be written as follows [29]:

$$\begin{bmatrix}
E_{\alpha}^{\text{out}} \\
E_{\beta}^{\text{out}} \\
\vdots \\
E_{\zeta}^{\text{out}}
\end{bmatrix} = \begin{bmatrix}
C_{\alpha\alpha} & C_{\beta\alpha} & \cdots & C_{\zeta\alpha} \\
C_{\alpha\beta} & C_{\beta\beta} & \cdots & C_{\zeta\beta} \\
\vdots & \vdots & \ddots & \vdots \\
C_{\alpha\zeta} & C_{\beta\zeta} & \cdots & C_{\zeta\zeta}
\end{bmatrix} \begin{bmatrix}
E_{\alpha}^{\text{in}} \\
E_{\beta}^{\text{in}} \\
\vdots \\
E_{\zeta}^{\text{in}}
\end{bmatrix} (1)$$

where the subscripts $\{\alpha, \beta, ..., \zeta\}$ represents various energy carriers, including electricity, gas, heat, and so on; E^{out} , E^{in} denote the vectors of energy outputs and energy inputs, respectively; and C is the coupling matrix, in which each element (e.g., $C_{\alpha\alpha}$) denotes the coupling factor.

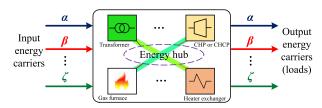


FIGURE 1. A general model of energy hub.

Note that the coupling matrix C is completely determined by the specific configuration of the corresponding energy hub, while each coupling factor C is equal to the product of the dispatch factor v and the converter efficiency η , i.e., $C = v\eta$ [30]. For an energy hub with multiple devices, the dispatch factors represent the distribution ratios of an input energy carrier to these devices, which can be considered as the controllable variables, while the converter efficiency is usually perceived as a constant.

B. DISTRIBUTED EHED

1) OBJECTIVE FUNCTION

To maximize the economic benefits of MECS, both the total energy costs f_C and the total energy losses f_L are taken as two basic objective functions for distributed EHED, respectively. In order to minimize the total energy costs and the total energy losses simultaneously, they can be transformed into a single



objective function $f_{\rm I}$, as follows [4]:

$$\min f_{\mathcal{C}}(\mathbf{x}) = \sum_{m=1}^{M} f_{\mathcal{C}}^{m}(\mathbf{x}_{m}), f_{\mathcal{L}}(\mathbf{x}) = \sum_{m=1}^{M} f_{\mathcal{L}}^{m}(\mathbf{x}_{m}),$$

$$f_{\mathcal{I}}(\mathbf{x}) = f_{\mathcal{C}}(\mathbf{x}) \left(1 + \frac{f_{\mathcal{L}}(\mathbf{x})}{\sum_{p \in P} E_{\text{demand}}^{p}} \right)$$
(2)

where x is the vector of the controllable variables of an entire system, including the energy production of each input energy carrier and each dispatch factor; x_m is the vector of the controllable variables for the mth energy hub; the subscript m and the superscript p represent the mth energy hub and the pth energy carrier, respectively; M is the number of energy hubs; **P** denotes the set of energy carriers, i.e., $P = {\alpha, \beta, ..., \zeta}$; E_{demand}^p denotes the energy demand of the pth output energy carrier of MECS; $f_{\rm C}^m$ and $f_{\rm L}^m$ represent the energy cost and the energy loss of the mth energy hub, respectively, which can be calculated as [4], [31]

$$f_{C}^{m}(\mathbf{x}_{m}) = \sum_{p \in \mathbf{P}} \sum_{j=1}^{n_{m}^{p}} \left(d_{mj}^{p} \left(E_{mj}^{p,\text{in}} \right)^{2} + b_{mj}^{p} E_{mj}^{p,\text{in}} + c_{mj}^{p} \right) + \sum_{j=1}^{n_{m}^{e}} \left| d_{mj}^{e} \sin \left(e_{mj}^{e} \left(E_{mj,\text{min}}^{e,\text{in}} - E_{mj}^{e,\text{in}} \right) \right) \right|$$
(3)

$$f_{\mathbf{L}}^{m}(\mathbf{x}_{m}) = \sum_{p \in \mathbf{P}} \left(E_{m}^{p, \text{in}} - E_{m}^{p, \text{out}} \right) \tag{4}$$

where n_m^p is the number of energy sources associated with the pth input energy carrier for the mth energy hub; n_m^e is the number of electrical generators with the valve-point effects of the *m*th energy hub; a_{mj}^p , b_{mj}^p , and c_{mj}^p are the cost coefficients of the *j*th energy source; d_{mj}^e and e_{mj}^e are the cost coefficients of the additional rectified sinusoidal component by considering the value-point effects of the electrical generators; $E_{mj}^{p,\text{in}}$ is the input energy production of the *j*th energy source; $E_{mj,\text{min}}^{\text{e,in}}$ is the minimum energy production of the *j*th electrical generator; $E_m^{p,\text{in}}$ and $E_m^{p,\text{out}}$ are the energy input and energy output of the pth input energy carrier for the mth energy hub, respectively.

2) CONSTRAINTS

In general, the renewable energy resources, e.g., solar or wind energy, are usually operated at the maximum power points (MPPs) at different weather conditions in a thermal power dominated system. Hence, no renewable energy resource is not considered for set points optimizations in this paper.

In the pursuit of different economic objective functions in (9), each energy hub needs to satisfy various constraints for an optimal operation, including energy balance constraints, capacity limits of all energy sources, prohibited operation zones (POZ) constraints of conventional thermal generators for faults prevention [32], and dispatch factor limits,

as follows:

$$E_{\text{demand}}^{p} = \sum_{m=1}^{M} E_{m}^{p, \text{out}}, p \in \mathbf{P}$$
 (5)

$$E_{mj,\min}^{p,\text{in}} \leq E_{mj}^{p,\text{in}} \leq E_{mj,\max}^{p,\text{in}}, p \in \mathbf{P};$$

$$m = 1, 2, \dots, M; j = 1, 2, \dots, n_m^p \quad (6)$$

$$m = 1, 2, \dots, M; j = 1, 2, \dots, n_{m}^{p}$$

$$m = 1, 2, \dots, M; j = 1, 2, \dots, n_{m}^{p}$$

$$\begin{cases} E_{mj,\min}^{e,in} \leq E_{mj}^{e,in} \leq E_{mj,\min_{1}}^{e,in} \\ \text{or } E_{mj,\max_{2}(z-1)} \leq E_{mj}^{e,in} \leq E_{mj,\min_{2}}^{e,in} \end{cases}$$

$$z = 2, \dots, Z_{mj}^{e}$$

$$\text{or } E_{mj,\max_{2}}^{e,in} \leq E_{mj}^{e,in} \leq E_{mj,\max_{2}}^{e,in}$$

$$m = 1, 2, \dots, M; j = 1, 2, \dots, n_{m}^{e}$$

$$(7)$$

where $E_{mj,\,{\rm min}\,_z}^{{\rm e},\,{\rm in}}$ and $E_{mj,\,{\rm max}\,_z}^{{\rm e},\,{\rm in}}$ are the low bound and upper bound of the zth POZ of jth electrical generator for the mth energy hub, respectively; and Z_{mi}^{e} is the POZ number of jth electrical generator for the *m*th energy hub.

III. MULTI-AGENT BARGAINING LEARNING

A. BARGAINING GAME

In a basic two-player bargaining game, the seller agent will firstly make an offer to the buyer agent, if the offer is accepted by the buyer agent, then an bargaining equilibrium (i.e., the strategy of the offer) can be determined, otherwise, the bargaining role will be shifted to be on the buyer agent in the next period until they reach an agreement on the offer [33]. Enlighted by this game, a novel cooperative one-seller and nbuyer bargaining game is proposed for achieving an efficient coordination between different players.

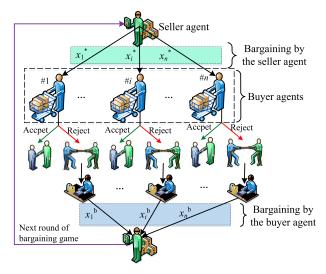


FIGURE 2. Principle of one-seller and n-buyer bargaining game.

As shown in Fig. 2, the one-seller and *n*-buyer bargaining game contains two bargaining process at each round, as

1) The seller agent firstly issues an current optimal joint action strategy $\mathbf{x}^* = (x_1^*, ..., x_i^*, ..., x_n^*)$ of the offers to all the buyer agents, which can be determined by comparing different bargaining strategies from the buyer agents,



as follows:

$$\mathbf{x}_{k}^{*} = \arg \max[U_{1}(\mathbf{x}_{1,k-1}^{b}, \mathbf{x}_{1,k-1}^{\text{other}}), \dots, U_{i}(\mathbf{x}_{i,k-1}^{b}, \mathbf{x}_{i,k-1}^{\text{other}}), \dots, U_{n}(\mathbf{x}_{n-1}^{b}, \mathbf{x}_{n-1}^{\text{other}}), U_{s}(\mathbf{x}_{k-1}^{b}), U_{s}(\mathbf{x}_{k-1}^{*})]$$
(8)

where the subscript k denotes the kth iteration; \boldsymbol{x}_k^* is the optimal joint action strategy at the kth iteration; $\boldsymbol{x}_{i,k-1}^{b}$ is the bargaining action strategy of the *i*th buyer agent; $x_{i,k-1}^{\text{other}}$ is the the optimal joint action strategy of all the buyer agents except the *i*th buyer agent at the (k-1) iteration; x_{k-1}^b is the joint bargaining action strategy; U_i is the utility function of the *i*th buyer agent, i = 1, 2, ..., n; n is the number of buyer agents; and U_s is the utility function of the seller agent.

2) If all the buyer agents accept that, the bargaining game is over, otherwise, the buyer agent will search a more optimal action strategy x_i^b to the seller agent if the following condition can be satisfied, as

$$\begin{cases} U_i(\mathbf{x}_{i,k}^{\mathrm{b}}, \mathbf{x}_{i,k}^{\mathrm{other}}) \ge U_{\mathrm{s}}(\mathbf{x}_k^*), & i = 1, 2, \dots, n \\ \text{or } U_{\mathrm{s}}(\mathbf{x}_k^{\mathrm{b}}) \ge U_{\mathrm{s}}(\mathbf{x}_k^*) \end{cases}$$
(9)

Note that all the utility functions in (16) and (9) represent the total payoff of all the agents, in which each buyer agent can only optimize its own action strategy to increase the total payoff. After a series of bargaining game between the seller agent and the buyer agents according to (16) and (9), a highquality bargaining equilibrium with a high total payoff of all the agents can be acquired. Hence, the key of bargaining game is to search a more optimal action strategy x_i^b for each buyer agent, which will be handled by the proposed learning method.

B. KNOWLEDGE LEARNING

As one of the most commonly used reinforcement learning, Q-learning is a model-free learning through continuous interactions with the environment [34], which can develop the knowledge for each action strategy at each state via a reward mechanism. Hence, it is adopted for knowledge learning of each buyer agent. To effectively avoid the curse of dimension and accelerate the learning rate of conventional learning, the associative memory is used for knowledge storage [35], while a cooperative swarm with multiple intelligent individuals is employed for implementing the exploration and exploitation in the environment, as illustrated in Fig. 3. Therefore, the knowledge matrices of each buyer agent can be updated as [35]

$$\begin{cases} \mathbf{Q}_{ih}^{k+1} \left(s_{ih}^{kj}, a_{ih}^{kj} \right) = \mathbf{Q}_{ih}^{k} \left(s_{ih}^{kj}, a_{ih}^{kj} \right) + \alpha \Delta \mathbf{Q}_{ih}^{k} \\ \Delta \mathbf{Q}_{ih}^{k} = R_{ih}^{j} \left(s_{ih}^{kj}, s_{ih}^{k+1,j}, a_{ih}^{kj} \right) \\ + \gamma \max_{a_{ih} \in A_{ih}} \mathbf{Q}_{ih}^{k} \left(s_{ih}^{k+1,j}, a_{ih} \right) - \mathbf{Q}_{ih}^{k} \left(s_{ih}^{kj}, a_{ih}^{kj} \right) \\ h = 1, 2, \dots, n_{i} : \quad j = 1, 2, \dots, J \end{cases}$$
(10)

where Q_{ih} is the knowledge matrix of the hth controllable variable for the *i*th buyer agent; ΔQ is the knowledge increment; α is the knowledge learning factor; γ is the discount factor; $(s_{ih}^{kj}, a_{ih}^{kj})$ represents the state-action pair executed by



FIGURE 3. Principle of knowledge learning with a cooperative swarm.

the *j*th individual for the controllable variable x_{ih} ; $R(s^k, s^{k+1}, s^{k+$ a^k) is the reward function of a transition from state s^k to s^{k+1} used under a selected action a^k ; a_{ih} represents any alternative action strategies; A_{ih} is the action space of x_{ih} ; n_i is the number of controllable variables for the ith buyer agent; and J is the population size of the cooperative swarm.

C. EXPLORATION AND EXPLOITATION

To achieve a high optimization accuracy, the exploration and exploitation of each individual is divided into two processes. For a controllable variable, each individual firstly choose an action strategy (i.e., interval of optimization) based on the corresponding knowledge matrix, then an accurate solution can be calculated by the non-uniform mutation operator [36] based on the local optimum of the corresponding interval. Aiming at a proper trade-off between exploration and exploitation, the ε -Greedy rule [37] is used for interval selection, as

$$a_{ih}^{kj} = \begin{cases} \arg\max_{a_{ih} \in A_{ih}} \mathbf{Q}_{ih}^{k}(s_{ih}^{kj}, a_{ih}), & \text{if } q_{0} \leq \varepsilon \\ a_{\text{rand}}, & \text{otherwise} \end{cases}$$

$$x_{ih}^{kj} = \begin{cases} x_{ih}^{d,\text{best}} + \Delta(k, x_{ih}^{d,\text{ub}} - x_{ih}^{d,\text{best}}), & \text{if } \text{rand}(0, 1) < 0.5 \\ x_{ih}^{d,\text{best}} - \Delta(k, x_{ih}^{d,\text{best}} - x_{ih}^{d,\text{lb}}), & \text{otherwise} \end{cases}$$
(11)

$$x_{ih}^{kj} = \begin{cases} x_{ih}^{d,\text{best}} + \Delta(k, x_{ih}^{d,\text{ub}} - x_{ih}^{d,\text{best}}), & \text{if } \text{rand}(0, 1) < 0.5\\ x_{ih}^{d,\text{best}} - \Delta(k, x_{ih}^{d,\text{best}} - x_{ih}^{d,\text{lb}}), & \text{otherwise} \end{cases}$$
(12)

$$\begin{cases} x_{ih}^{d,\text{ub}} = x_{ih}^{\text{lb}} + a_{ih}^{kj} \cdot (x_{ih}^{\text{ub}} - x_{ih}^{\text{lb}}) / |A_{ih}| \\ x_{ih}^{d,\text{lb}} = x_{ih}^{\text{lb}} + (a_{ih}^{kj} - 1) \cdot (x_{ih}^{\text{ub}} - x_{ih}^{\text{lb}}) / |A_{ih}| \end{cases}$$
(13)

$$\Delta(k, y) = y \cdot \left(1 - r^{(1-k/k_{\text{max}})^b}\right)$$
(14)

where q_0 is a uniform random value from [0, 1]; ε is the exploitation rate which represents the probability of exploitation; a_{rand} denotes a random action (exploration); $x_{ih}^{d,\text{best}}$ is the previous best optimal solution at the dth interval of the hth controllable variable for the *i*th buyer agent, and $d = a_{ih}^{kj}$; $x_{ih}^{d,\mathrm{ub}}$ and $x_{ih}^{d,\mathrm{lb}}$ are the upper and lower bounds of the *d*th interval, respectively; x_{ih}^{ub} and x_{ih}^{lb} are the upper and lower bounds for the hth controllable variable, respectively; $\Delta(k, y)$ is a decay function as the iteration k increases; r is a uniform random value from [0, 1]; b is the system parameter which determines the degree of non-uniformity; and k_{max} is the maximal iteration number.



MABL can escape from the local optimum via a proper trade-off between exploration and exploitation in (11). In fact, the exploration and exploitation represent the global search and local search, respectively. Therefore, the exploration can effectively escape from the local optimum, while the exploitation can accelerate the convergence and improve the optimum quality.

IV. DESIGN OF MABL FOR DISTRIBUTED EHED

A. DESIGN OF BARGARINING GAME

For the distributed EHED, each energy hub can be regarded as a player of bargaining game. Moreover, any one energy with the most diverse types of output energy carriers can be selected as a slack energy hub (i.e., the seller agent), while the others are regarded as different buyer agents. Note that the seller agent is only responsible for determining the joint action strategy by (8), in contrast, each buyer agent not only needs to bargain according to (9) but also needs to search a potential more optimal solution.

B. DESIGN OF STATE AND ACTION

For the distributed EHED, each energy hub consists of two types of controllable variables, including the input energy production of each energy source and the dispatch factor, where the value range of each controllable variable can be discretized into multiple the optimization intervals, i.e., the action space A_{ih} (i = 1, 2, ..., n; $h = 1, 2, ..., n_i$), while A_{ih} equals to the state space of the next controllable variables, i.e., $S_{i,h+1} = A_{ih}$. Besides, the state of the first controllable variable for each energy hub can be determined according to the current energy gap ΔE between the energy outputs and the energy demand, as follows:

$$\begin{cases} s_{i1}^{k}, & \text{if } E_{i,\min_{-v}}^{\text{in}} \leq \Delta E < E_{i,\max_{-v}}^{\text{in}} \\ \Delta E = \sum_{p \in p} E_{\text{demand}}^{p} - \sum_{m=1 \& m \neq i}^{M} \sum_{p \in p} \bar{E}_{m}^{p, \text{out}} \\ E_{i,\min_{-v}}^{\text{in}} = \sum_{p \in P} \sum_{j=1}^{n_{m}^{p}} E_{mj,\min}^{p, \text{in}} + (v - 1) \\ \cdot \left(\sum_{p \in P} \sum_{j=1}^{n_{m}^{p}} E_{mj,\max}^{p, \text{in}} - \sum_{p \in P} \sum_{j=1}^{n_{m}^{p}} E_{mj,\max}^{p, \text{in}} \right) \middle/ |S_{i1}| \end{cases}$$

$$(15)$$

$$E_{i,\max_{-v}}^{\text{in}} = \sum_{p \in P} \sum_{j=1}^{n_{m}^{p}} + v \\ \cdot \left(\sum_{p \in P} \sum_{j=1}^{n_{m}^{p}} E_{mj,\max}^{p, \text{in}} - \sum_{p \in P} \sum_{j=1}^{n_{m}^{p}} E_{mj,\max}^{p, \text{in}} \right) \middle/ |S_{i1}|$$

$$v = 1, 2, \quad |S_{i1}|$$

where $E_{i,\min_{\nu}}^{\mathrm{in}}$ and $E_{i,\max_{\nu}}^{\mathrm{in}}$ are the total low bound and upper bound at the ν th state of the ith energy hub, respectively; and $\bar{E}_{m}^{P,\mathrm{out}}$ is the current energy output of the pth input energy carrier for the mth energy hub, which can be provided from the seller agent based on the current optimal joint action strategy.

C. DESIGN OF REWARD FUNCTION

The reward function R in (10) represents the feedback from the environment after an exploration or exploitation, which can directly influence the optimization performance of MABL. Hence, it should be designed by fully integrating the mathematical model of distributed EHED (2)-(7), as [38]

$$R_{ih}^{j}\left(s_{ih}^{kj},s_{ih}^{k+1,j},a_{ih}^{kj}\right) = \begin{cases} \frac{p_{\text{m}}}{\min\limits_{j=1,2,...,J}F_{i}^{kj}}, & \text{if } \left(s_{ih}^{kj},a_{ih}^{kj}\right) \in \textbf{\textit{S}}\textbf{\textit{A}}_{i}^{\text{Best}} \\ 0, & \text{otherwise} \end{cases}$$
(16)

$$F_i^{kj} = f(x_i^{kj}, x_{i,k-1}^{\text{other}}) + \sum_{u=1}^{NC_i} PF_i^u$$
 (17)

$$PF_i^u = \begin{cases} \chi \left(Z_i^u - Z_i^{u, \lim} \right)^2, & \text{if violated} \\ 0, & \text{otherwise} \end{cases}$$
 (18)

where F_i^{kj} denotes the fitness function of the jth individual at the kth iteration, which is closely related to the utility function, i.e., $F_i = -U_i$; $p_{\rm m}$ is a positive multiplicator; $SA_i^{\rm Best}$ represents the state-action pairs set of the best individual at the kth iteration for the ith buyer agent; f is one of three objective functions in (2); NC_i is the number of constraints for the ith buyer agent based on (5)-(7); PF_i^u is the penalty function corresponding to the ith constraint for the ith buyer agent; ith buyer agent; ith buyer agent; ith buyer agent; and ith buyer agent; and ith buyer agent; is the constraint limit corresponding to ith buyer agent; and ith buyer agent agent; and ith buyer agent age

TABLE 1. Overall Execution Procedure of MABL for Distributed EHED

Determine the objective function from (2);

Initialize the parameters of MABL; 3: While $k \le k_{\text{max}}$ The seller agent determines the current joint action by (8); 5: The seller agent issues x_k^* to all the buyer agents; Determine the state of the first controllable variable by (15); Implement exploration and exploitation using (11)-(14); Calculate objective and constraints obtained by each solution 10: Calculation the reward function for each executed stateaction by (16)-(18); 11. Update the best optimal solution; 12: Update the knowledge matrix by (10); Implement the bargaining process of each buyer agent by (9); 13: **End For** 14. Set k:=k+1; 16. End While

TABLE 2. The Parameters Used in MABL for Distributed EHED.

Output the optimal solution of distributed EHED

α	γ	ε	b	p_{m}	J	$k_{\rm max}$
0.1	0.05	0.7	0.5	0.001	50	200

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1:



Algorithm		Minimization of total energy costs		Minimization of total energy losses			Minimization of total energy costs and losses simultaneously				
		$f_{\rm C}$ (mu)	$f_{\rm L}$ (pu)	$T_{\rm C}\left({ m s}\right)$	$f_{\rm C}$ (mu)	$f_{\rm L}$ (pu)	$T_{\rm C}\left({ m s}\right)$	$f_{\rm C}$ (mu)	$f_{\rm L}$ (pu)	$f_{\rm I}$ (mu)	$T_{\rm C}\left({ m s}\right)$
G	A	16384.4316	4.0788	27.3846	16622.8797	3.3902	17.2353	16388.6511	3.6722	18960.5487	29.6453
PS	О	16106.0947	3.7058	18.5038	16858.0050	2.9950	11.7354	16402.3627	3.1190	18588.6434	19.6453
GS	SA	15870.0549	4.5232	17.3926	17308.0887	2.9385	9.9919	15964.8911	3.3843	18273.8646	18.8789
EG	SA	15751.6029	3.6376	17.2627	16823.5307	2.8162	9.6391	15754.6403	3.6154	18188.8198	18.8837
TVAC	-GSA	15747.3098	3.6459	17.3030	16811.3114	2.8317	9.5825	15751.8705	3.6360	18199.4468	18.6678
SAL-TV	AC-GSA	15728.3913	3.6706	17.2354	16824.7134	2.8100	9.2078	15730.4677	3.6284	18169.6515	18.5632
	Worst	16275.4452	3.4500	2.0869	16877.4285	2.6500	1.7436	16347.2654	2.7939	18299.1442	2.1697
MABL	Mean	15901.7736	3.4538	2.0887	17552.4483	2.2348	1.7105	16057.4331	2.4959	17770.5560	2.1550
	Best	15667.9776	3.5503	2.0810	17940.7631	1.8879	1.6925	15734.9647	2.3374	17306.6931	2.1479

TABLE 3. Performance Results with Different Objective Functions Obtained by Different Algorithms in 30 Runs

D. OVERALL EXECUTION

In summary, the overall execution of MABL for distributed EHED is provided in Table I. Note that the implementation process of each buyer agent can be can be computed simultaneously, thus the computation time can be dramatically shorten.

V. CASE STUDIES

For evaluating the performance of MABL for distributed EHED, six centralized heuristic optimization algorithms including GA [8], PSO [7], GSA [6], EGSA [6], TVAC-GSA [6], and SAL-TVAC-GSA [4], are used for comparisons with different objective functions in (2), where the parameters of these algorithms can be referred from [4]. Through trial-and-error, the main parameters of MRBL for distributed EHED are given in Table II. Furthermore, all the simulations of the proposed algorithm are undertaken in Matlab R2016a by a personal computer with Intel(R) Xeon (R) E5-2670 v3 CPU at 2.3 GHz with 64 GB of RAM.

A. SIMULATION MODEL

The testing MECS is composed of 39 energy hubs with 29 different structures, in which the 34th energy hub is selected as the seller agent, while others are the buyer agents. This system consists of 76 energy sources, including 27 electrical sources with the value-point effects (8 of that consider the POZ constraints), 34 gas stations, and 15 heat sources, where the types of output energy carriers contain electricity, heat, cool and compressed air. All the parameters of this system are given in [4], which has 103 controllable variables (76 of that for energy sources and 27 for dispatch factors). Besides, the optimization interval of each controllable variable is equally divided into 5 smaller intervals, thus each action space contains 5 alternative action strategies, as well as for the state space.

B. STUDY OF CONVERGENCE

Fig. 4 illustrates the convergence process of MABL for minimizing the total energy costs $f_{\rm C}$ of distributed EHED, where the total energy demand of electricity, heat, cool, and compress air are 12.0, 9.5, 0.7, and 1.2 pu, respectively. It can be

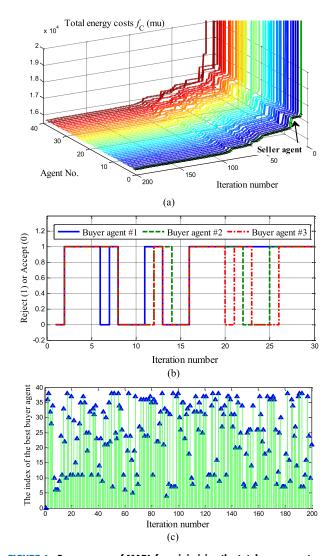


FIGURE 4. Convergence of MABL for minimizing the total energy costs. (a) Objective functions of different agents. (b) Bargaining processes of some agents. (c) Index of the best buyer agent with the largest payoff.

found from Fig. 4(a) that the seller agent and the buyer agents can constantly search a better optimal solution with a lower total energy costs via the continuous bargaining game from each other, more concretely, each of them can approximate an



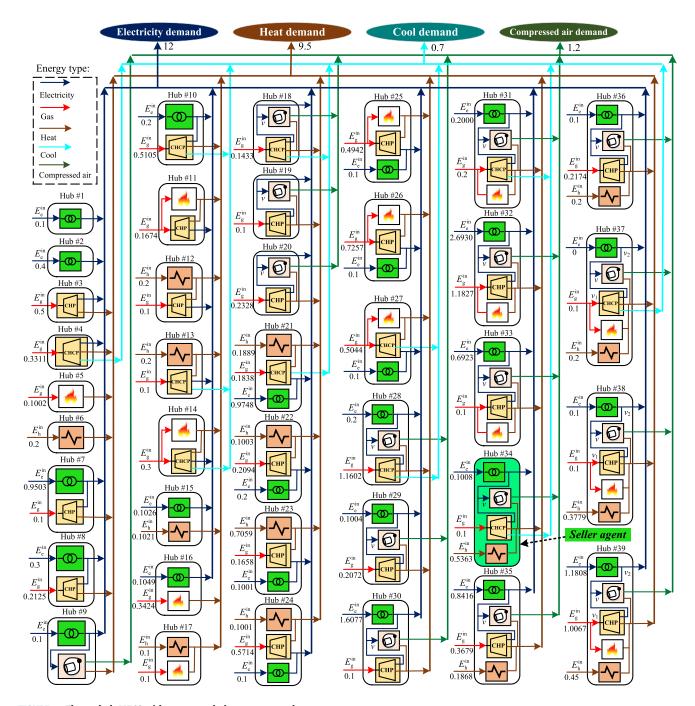


FIGURE 5. The 39-hub MECS with 29 energy hub structures and 76 energy sources.

optimal solution after 80 iterations, while the optimal input energy production of each energy source is given in Fig. 5. This obviously indicates that the bargaining game can effectively achieve an effective coordination between the buyer agents and a seller agent, thus the total payoff of all the energy hubs can be maximized.

Besides, to search a potential better optimal solution, each buyer agent can select an optimal action strategy for each controllable variable of the corresponding energy hub by selfscheduling based on knowledge learning, thus they can reject the seller agent (See Fig. 4(b)) and contribute to improving the total payoff of MECS (See Fig. 4(c)).

C. COMPARATIVE RESULTS AND DISCUSSIONS

Table III shows performance results with different objective functions in (2) obtained by different algorithms in 30 independent runs, where the performance results of the former six algorithms are the best optimal solutions with the smallest objective functions in 30 runs, respectively; all the performance results are in a per-unit (pu) system and the energy



costs are in monetary-unit (mu); T_C is the computation time in a run. Note that the obtained objective functions of MABL are much smaller than that of other algorithms, especially for the minimization of total energy losses. Particularly, the minimal total energy losses f_L obtained by MABL in the best case is only 55.69% of that of GA, in which the optimal operation points of all the energy hubs are provided in Table IV while the obtained optimal dispatch factors are given in Fig. 6, and the detailed operation illustration of energy hub #27 from the input energy carriers to the output energy carriers is given in Fig. 7. It verifies that the obtained optimum by MABL can not only satisfy all the constraints (5)-(7), but also significantly reduce the total energy losses. Even in the worst case, it is still only 94.31% of that of SAL-TVAC-GSA. These high-quality optimal solutions clearly demonstrate the beneficial effect of knowledge learning, and the effective coordination among the seller agent and the buyer agents via the continuous bargaining games.

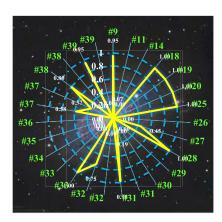


FIGURE 6. Dispatch factors distribution of all the energy hubs with minimization of total energy losses obtained by MABL in the best case.

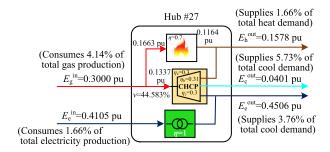


FIGURE 7. Best optimal results of energy hub #27 with minimization of total energy losses obtained by MABL.

Moreover, it is obviously that the computation time of MABL for distributed EHED is the shortest among all the algorithms, which is only 7.25% of that of GA for minimization of total energy costs and losses simultaneously in the best case, i.e., the computation rate can be up to 13.8 times against to GA, which is essentially benefited from the distributed optimization and associative memory based knowledge learning with a cooperative swarm.

TABLE 4. Optimization Results of the Best Optimal Solution with Minimization of Total Energy Losses Obtained by MABL.

	Input Ene	ergy (pu)		F			
Hub No.	Туре	Optimum	Electricity	Heat	Energy (pu) Cool	Compressed	Energy loss (pu)
#1	Electricity	0.1000	0.0990	0.0000	0.0000	air 0.0000	0,0010
#2	Electricity	0.4000	0.4000	0.0000	0.0000	0.0000	0.0000
#3	Gas	0.5000	0.1500	0.2000	0.0000	0.0000	0.1500
#4	Gas	0.3000	0.0750	0.1050	0.0600	0.0000	0.0600
#5	Gas Heat	0.1091 0.5000	0.0000	0.0818 0.4750	0.0000	0.0000	0.0273 0.0250
	Electricity	0.2000					
#7	Gas	0.1000	0.2270	0.0410	0.0000	0.0000	0.0320
#8	Electricity	0.3000	0.3250	0.0420	0,0000	0.0000	0.0330
	Gas	0.1000					
#9	Electricity Electricity	0.4186 0.2000	0.0192	0.0799	0.0000	0.2795	0.0399
#10	Gas	0.2000	0.2500	0.0740	0.0400	0.0000	0.0360
#11	Gas	0.1500	0.0030	0.1159	0.0000	0.0000	0.0311
#12	Gas	0.1000	0.0300	0.3961	0.0000	0.0000	0.0352
	Heat	0.3613	0.0500	0.5501	0.0000	0.0000	0.0002
#13	Electricity Gas	0.1000 0.2676	0.0250	0.2843	0.0300	0.0000	0.0284
#14	Gas	0.3000	0.0000	0.2100	0.0000	0.0000	0.0900
	Electricity	0.1001					
#15	Heat	0.1138	0.0981	0.1024	0.0000	0.0000	0.0134
#16	Electricity	0.1000	0.0950	0.1571	0.0000	0.0000	0.0631
	Gas	0.2152 0.1000					
#17	Gas Heat	0.1000	0.0000	0.1673	0.0000	0.0000	0.0353
#18	Gas	0.1023	0.0000	0.0370	0.0290	0.0210	0.0130
#19	Gas	0.1000	0.0000	0.0460	0.0000	0.0210	0.0330
#20	Gas	0.2000	0.0000	0.0861	0.0000	0.0455	0.0684
	Electricity	1.4677					
#21	Gas	0.1001	1.5038	0.4620	0.0240	0.0000	0.0040
	Heat Electricity	0.4259 0.2006					
#22	Gas	0.2000	0.2586	0.6323	0.0000	0.0000	0.0540
	Heat	0.5443		0.0323	0.0000	0.0000	
	Electricity	0.1022		0.1471	0.0000	0.0000	
#23	Gas	0.1000	0.1272				0.0407
	Heat	0.1128					
#24	Electricity Gas	1.3101 0.1000	1.3401	1.5400	0.0000	0.0000	0.0300
#24	Heat	1.5000	1.5401				
425	Electricity	0.1983	0.3109	0.1440	0.0000	0.0000	0.0644
#25	Gas	0.3218	0.3109	0.1448	0.0000	0.0000	0.0644
#26	Electricity	0.1000	0.0970	0.2250	0.0000	0.0000	0.0780
	Gas	0.3000 0.4105					
#27	Electricity Gas	0.3000	0.4506	0.1578	0.0401	0.0000	0.0619
	Electricity	0.6000					
#28	Gas	1.4200	0.0000	0.8491	0.4118	0.7013	0.0577
#29	Electricity	0.1000	0.1590	0.0640	0.0000	0.0000	0.0770
	Gas	0.2000	0.1570	0.0010	0.0000	0.0000	0.0170
#30	Electricity Gas	0.3013 0.1000	0.3343	0.0450	0.0000	0.0000	0.0220
	Electricity	0.1000		1			
#31	Gas	0.2211	0.0046	0.2067	0.0129	0.1237	0.0743
#32	Electricity	0.0000	0.0000	0.0740	0.0000	0.0000	0.0260
1152	Gas	0.1000	0.0000	0.0740	0.0000	0.0000	0.0200
#33	Electricity	0.0000	0.0350	0.0470	0.0000	0.0000	0.0180
	Gas Electricity	0.1000 1.9964		1			
#34	Gas	0.1405	2.0385	0.1294	0.0365	0.0000	0.0324
	Heat	0.1000					
	Electricity	0.2013					
#35	Gas	0.2000	0.2652	0.1568	0.0000	0.0000	0.0817
	Heat	0.1025					
#36	Electricity Gas	0.1000 0.2000	0.1478	0.4735	0.0000	0.0001	0.1999
#30	Heat	0.5213	0.1470	0.4/33	0.0000	0.0001	0.1999
#37	Electricity	0.0002		0.4888	0.0156	0.0031	0.0711
	Gas	0.1000	0.0096				
	Heat	0.4880					
#38	Electricity	2.7763	2 7000	0.4047	0.0000	0.0041	0.0350
	Gas Heat	0.1000 0.3681	2.7988	0.4047			0.0368
	Electricity	0.3681					
#39	Gas	0.1000	0.3225	0.5510	0.0000	0.0006	0.0430
	Heat	0.5294		<u> </u>	<u> </u>		
			12.0000	9.5000	0.7000	1.2000	1.8879

VI. CONCLUSION

This paper presents a novel MABL for distributed EHED of a large-scale MECS. The main observations are summarized as follows:



- 1) The one-seller and *n*-buyer bargaining game can effective achieve an effective coordination among the energy hub, thus the self-organized and distributed computation of each energy hub can be implemented for distributed EHED.
- 2) The associative memory and swarm intelligence can dramatically accelerate the convergence rate of knowledge learning, while the non-uniform mutation operator is conductive to a high optimization accuracy.
- 3) Simulation results on the complex testing system verify the superior performance of MABL compared with six centralized heuristic optimization algorithms, which can rapidly obtain a high-quality optimal solution for distributed EHED with different objective functions.
- 4) Compared with the gradient-based distributed methods (e.g., consensus algorithm or ADMM), MABL is more suitable for the non-convex and non-smooth EHED as it is fully independent on the mathematical model. Moreover, the performance of MABL is competitive to other distributed heuristic optimization algorithms due to its fast convergence and strong global search ability. Hence, it is adequate to be generalized to handle other distributed optimization of large-scale and complex smart energy systems.

In order to improve the applicability for the real-world system, our future works will consider both the environmental effects and the energy networks constraints.

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