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# Bandpass Impedance Transformers With Extremely High Transforming Ratios Using II-Tapped Feeds

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**ABSTRACT** Bandpass impedance transformers (BPIMTs) with extremely high transforming ratios by adopting the proposed  $\Pi$ -tapped feeds are realized in this paper.  $\Pi$ -tapped feeds composed of two shunt stubs and one-section line performing the impedance transforming function are introduced. To validate the generality of the proposed approach, two different types of bandpass transformers, i.e., type-A and type-B adopting a short-ended parallel coupled-line and a via-inductive coupling as their interstage couplings, respectively, originating from two coupled-resonator filter topologies are designed. The synthesis procedures and design formulas of the two transformer types are provided, and the auxiliary graphs for different impedance transforming ratios are thoroughly investigated. The circuit-level simulated results of the proposed BPIMTs agree well with the theoretical results calculated from the coupling matrix, thus validating the design approach. Specifically, two type-A prototypes with the transforming ratios of 20 (200  $\Omega/10 \Omega$ ) and 95 (475  $\Omega$ /5  $\Omega$ ), respectively, and one type-B prototype with a transforming ratio of 104 (520  $\Omega/5 \Omega$ ) were demonstrated. The proposed transformer is capable of satisfactorily matching the low and high impedances, and it also possesses the highest impedance transforming ratio ever reported in the literature.

**INDEX TERMS** Impedance transformer, bandpass function,  $\Pi$ -tapped feed, parallel-coupled line, inductive coupling.

#### I. INTRODUCTION

In microwave systems, impedance transformers (IMT) play a critical role in impedance matching or maximum power transfer, and they are also widely utilized in power dividers/combiners [1]-[3], baluns [4], [5], power amplifiers [6]-[8], and low-noise amplifiers. Generally, if the IMT is just serving as an impedance transforming connection between components, it is designed for wideband performance [9], [10]. On the other hand, in most microwave communication systems, the filters are usually inserted between the antennas and transceivers and both their I/O ports are commonly matched with system impedance  $Z_0$ . The conventional approach of designing antennas is to adjust the dimensions to achieve radiation resistance equal to  $Z_0$ . However, different types of antennas may provide significantly different impedance levels resulting from their radiation nature, which is not easy to control to the demanded level, and thus, the IMTs are needed. Therefore, from a system viewpoint,

it would be beneficial to combine the impedance transforming and filtering functions into a single component to save circuit size and reduce loss.

Quite a few research studies have been carried out to design IMTs that can be roughly classified into three categories: multi-section IMTs using cascading quarter-wave transmission lines ( $\lambda/4$  TLs) [10]–[12], TL-IMT [13], [14], and one-/multi-section parallel coupled-line IMTs [15]–[19]. Concerning [10], through the derivation of the transmission coefficient of a two-port network and equating it with the transfer function of the Chebyshev response, the required electrical parameters can be derived. Once the required impedance ratio is high, the multi-section IMTs [11], [12] using  $\lambda/4$  TLs suffer from very wide/narrow line widths that may not be practical in common applications. A single-section coupled line was employed as the impedance-transforming DC block with  $r_z = 2$  (50 $\Omega/25\Omega$ ) [15]. In addition, the IMT using open-ended parallel-coupled

lines (PCLs) with a transforming ratio of  $2(50\Omega/25\Omega)$  [17] or based on short-ended PCLs with transforming ratios up to 20 (1000 $\Omega/50\Omega$ ) [18] were presented. The open-ended two-section coupled-line IMT proposed in [19] achieved an ultra-high impedance ratio of 10 (50 $\Omega/5\Omega$ ). According to these works, it is observed that the IMTs utilizing open-ended PCLs seem more suitable for transforming relatively low source/load impedances [19]. Once the source/load impedances are both relatively high, the strong coupling required may be not achievable due to process limitation. In contrast, the IMT using short-ended PCLs is preferable in transforming relatively high source/load impedances [18]. Finding an approach for dealing with wide-range source/load impedance transformation is an attractive research topic.

The tapped-line feed structure can be traced back to [20], 1979. Due to the simple structure and tight coupling, the tapped-line has been widely adopted in many different types of filters as a feeding structure [21]–[23]. In [24] and [25], efforts are made to improve the feeding characteristics of conventional tapped-line feeds. From the theoretical viewpoint, the conventional tapped feed can be further modified to possess impedance-transforming capability.



**FIGURE 1.** Dual functions of the proposed bandpass impedance transformer.

This study was intended to design a dual-function microwave component possessing filtering capability and impedance transformation as shown in Fig. 1. By adopting the proposed  $\Pi$ -tapped feed structures as the I/O feeds of the coupled-resonator structure, impedance transformation and a filtering function can be simultaneously accomplished. In addition, two transmission zeros contributed by the inherent stubs of the  $\Pi$ -tapped feeds can potentially be used to suppress the spurious passbands. Two different types of BPIMT, type-A and type-B, based on the  $\Pi$ -tapped feeds are discussed to show the generality of the proposed design. The circuit-level simulated results and calculations from the coupling matrix show significant agreement in terms of bandwidth, passband ripple, and impedance-matching. Theoretically speaking, the proposed method of designing BPIMT can be used in those coupled-resonator filters using different coupling mechanisms. The BPIMTs are implemented and measured showing satisfactory electrical performance.

#### II. II-TAPPED FEEDS WITH IMPEDANCE-TRANSFORMATION FUNCTION

A bandpass impedance transformer (BPIMT) that possesses both the impedance transforming capability and the filtering



**FIGURE 2.** Schematic of the proposed type-A filtering impedance transformer with spurious suppression  $(Y_{0e} = 1/Z_{0e}, Y_{0o} = 1/Z_{0o})$ .

function can be designed using the inverter-based coupledresonator filter [25] through appropriate modification. Fig. 2 depicts the equivalent-circuit of the proposed type-A 2ndorder BPIMT composed of two  $\Pi$ -tapped feeds and one short-ended parallel-coupled line (SE-PCL). The transformer is specified with center frequency  $f_0$ , transforming ratio  $r_Z = R_L / R_S$ , fractional bandwidth  $\Delta$ , and order N = 2 to minimize the insertion loss. The corresponding element values of the lowpass prototype filter are  $[g_0, g_1, g_2, g_3]$ . The two attached open-ended stubs associated with the I/O  $\Pi$ -tapped feeds can be used for spurious suppression or interference rejection by contributing two transmission zeros.



**FIGURE 3.** Singly loaded resonator fed by the proposed  $\Pi$ -tapped feed for evaluating the external quality factor. ( $G_S = 1/R_S$ ,  $Y_{mi} = 1/Z_{mi}$ ,  $Y_h = 1/Z_h$ ,  $Y_2 = 1/Z_2$ ).

Redrawing the singly loaded resonator composed of the  $\Pi$ -tapped feed and the  $\lambda/4$  stepped-impedance resonator (SIR) adjacent to the input port in Fig. 3 for the following discussion, the  $\Pi$ -tapped feed exploited in the loaded resonator consists of a shunt short-ended stub  $T_{M2}$ , a cascading line section  $T_{M1}$  and a shunt open-ended stub  $T_{sb}$ . With regard to the SIR, its design parameters are  $(Y_h, \theta_C)$  and  $(Y_2, \theta_2)$ . As shown in Fig. 3, the input admittance  $Y_{TI} = G_{TI} + jB_{TI}$  of the  $\Pi$ -tapped feed must be purely resistive exactly at the operation frequency, whereas its reactive component behaves as a shunt resonator. The derived  $B_{TI}$  is expressed as

$$B_{TI} = \frac{Y_{mi}[G_S^2(\sin 2\theta_{A1} - 2\sin 2\theta_{m1}) + (G_S^2 - 4Y_{mi}^2)\sin 2\theta_{A2}]}{8[(G_S \sin \theta_{m1i} \sin \theta_{m2i})^2 + (Y_{mi} \sin \theta_{A2})^2]} + Y_{s1} \tan \theta_{s1}, \quad (1)$$

where  $\theta_{A1} = \theta_{m1i} - \theta_{m2i}$ , and  $\theta_{A2} = \theta_{m1i} + \theta_{m2i}$ . For a given source resistance  $R_S$  and line impedance  $Z_{mi}$ , it is demanded that  $B_{TI}(\theta_{m1i}, \theta_{m2i}) = 0$  at  $f_0$  to ensure resonance with the selected stub  $(Z_{s1}, \theta_{s1})$ . For simplification,  $B_{TI}$  can be modeled as a shunt resonator around resonant frequency  $f_0$ ,

$$B_{TI} = b_{TI}(f/f_0 - f_0/f),$$
(2)

where *f* denotes the frequency variable, and  $b_{TI}$  is its susceptance slope parameter. This parasitic resonator and the  $\lambda/4$  stepped-impedance resonator (SIR) jointly constitute the overall input resonators  $jB_{1L} = j(B_{TI} + B_{\lambda/4})$ . Eventually, the total susceptance slope parameter of resonator 1 seen from the left-handed side (LHS) can be acquired by finding the differentiation of  $B_{1L}$ .

$$b_{1L} = \frac{f_0}{2} \frac{dB_{TI}}{df} + \frac{f_0}{2} \frac{dB_{\lambda/4}}{df} = b_{TI} + b_{\lambda/4},$$
 (3)

where  $b_{\lambda/4}$  denotes the susceptance slope parameter of the  $\lambda/4$  SIR composed of two sections of transmission lines  $(Z_h, \theta_c)$  and  $(Z_2, \theta_2)$  that can be analytically given as

$$b_{\lambda/4} = Y_2 \sec^2 \theta_2 \frac{\theta_2 (1 + \alpha_Y^2 \tan^2 \theta_1) + \alpha_Y \theta_1 \sec^2 \theta_1}{2(\alpha_Y \tan \theta_1 + \tan \theta_2)^2}.$$
 (4)

with  $\alpha_Y = Y_2/Y_1$ ,  $\theta_1 = \theta_c$ , and  $Y_1 = Y_h$ .

To meet the filter specifications, the external quality factor of the proposed  $\Pi$ -tapped feed must fulfill the following condition

$$\frac{b_{1L}(\theta_{m1i}, \theta_{m2i})}{G_{TI}(\theta_{m1i}, \theta_{m2i})} = Q_{EI}, \quad \text{where} \quad Q_{EI} = \frac{g_0 g_1}{\Delta}.$$
 (5)

Using (5), the electrical lengths  $(\theta_{m1i}, \theta_{m2i})$  can be solved for. Similarly, the electrical lengths  $(\theta_{m1o}, \theta_{m2o})$  of the output feed with predetermined load resistance and line impedance  $Z_{mo}$  can be calculated from  $B_{TO}(\theta_{m1o}, \theta_{m2o}) = 0$  and  $b_{2R}/G_{TO} = Q_{EO}$  seen from the RHS of resonator 2, where  $Q_{EO} = g_2g_3/\Delta$ .



**FIGURE 4.** Input susceptance  $Y_{TI}$  of the proposed  $\Pi$ -tapped feed under  $R_S = 10 \ \Omega$  and open-ended stub  $(Z_{s1}, \theta_{s1}) = (70\Omega, 45^\circ)$ . (a) Real part. (b) Imaginary part.

To validate the design guideline, a BPIMT is designed with arbitrary  $f_0$  and  $\Delta = 7\%$  for a 0.1-dB-ripple Chebyshev response. The associated values of the lowpass prototype are  $[g_0, g_1, g_2, g_3] = [1, 0.8431, 0.6220, 1.3554]$ . Using  $g_0 = 1$ and  $g_1 = 0.8341(Q_{EI} = 12.0443)$ , the input admittances  $Y_{TI}$ versus frequency of the  $\Pi$ -tapped feeds for  $Z_{mi} = 40, 60$ , and 100  $\Omega$  are accordingly calculated and drawn in Fig. 4. Obviously, the admittance  $Y_{TI}$  contributed by the  $\Pi$ -tapped feed behaves like a parallel resonator around  $f_0$  and the equivalent input conductance  $G_{TI}$  varies with different characteristic impedance  $Z_{mi}$ . By choosing the  $\lambda/4$  resonator adjacent to the tapped feed as uniform-impedance ( $Z_1 = Z_2 = 60 \Omega$ ,  $\theta_C = 70^\circ, \theta_2 = 20^\circ$ ), its susceptance slope parameter can be calculated as  $b_{\lambda/4} = 1.31$  cS. With the aid of (5), the resultant



**FIGURE 5.** (a) Susceptance slope parameter  $b_{1L}$  and (b)  $(\theta_{m1i}, \theta_{m2i})$  of the proposed  $\Pi$ -tapped feed incorporating  $\lambda/4$  SIR under  $R_S = 10 \Omega$  and open-ended stub  $(Z_{S1}, \theta_{S1}) = (70 \Omega, 45^{\circ})$ .



**FIGURE 6.** Design graph of  $\theta_{m1i}$  and  $\theta_{m2i}$  using  $Z_{mi}$  and  $R_S$  as parameters with termination open-ended stub  $(Z_{s1}, \theta_{s1}) = (70 \ \Omega, 45^{\circ})$ .

susceptance slope parameter  $b_{1L}$  of resonator 1 seen from the LHS is shown in Fig. 5(a) solved under  $R_S = 10 \Omega$  and openended stub  $(Z_{s1}, \theta_{s1}) = (70 \Omega, 45^\circ)$ . Moreover, the auxiliary chart of  $(\theta_{m1i}, \theta_{m2i})$  with different  $Z_{mi}$  is illustrated in Fig. 5(b).

For convenience, a low-Z ( $R_S$ ) to high-Z ( $R_L$ ) transformation is considered. In Fig. 6, the design graphs are shown for determining the ( $\theta_{m1i}$ ,  $\theta_{m2i}$ ) using both  $Z_{mi}$  and 10  $\Omega \leq R_S \leq 20\Omega$  as parameters with the attached open-ended stub ( $Z_{s1}$ ,  $\theta_{s1}$ ) = (70  $\Omega$ , 45°). For ease of usage, only monotonic solutions of ( $\theta_{m1i}$ ,  $\theta_{m2i}$ ) (as  $R_S$  increases,  $\theta_{m1i}$  increases and  $\theta_{m2i}$  decreases; as  $Z_{mi}$  increases, both  $\theta_{m1i}$  and  $\theta_{m2i}$  decrease) are included. However, non-monotonic solutions can still be acquired based on (5). For instance, referring to Fig. 5(b), the ( $\theta_{m1i}$ ,  $\theta_{m2i}$ ) curve with  $40\Omega \leq Z_{mi} \leq 100\Omega$  under  $R_S = 10\Omega$  shows non-monotonicity. Thus, only the results corresponding to  $Z_{mi} = 40$ , 50  $\Omega$  are exhibited in Fig. 6 to avoid the intersection of constant- $R_S$  gridlines.

In addition, using  $g_2 = 0.6220$  and  $g_3 = 1.3554$  ( $Q_{EO} = 12.0443$ ), the design graphs for determining the electrical lengths ( $\theta_{m1o}$ ,  $\theta_{m2o}$ ) of the output  $\Pi$ -tapped feed using both  $Z_{mo}$  and 20  $\Omega \leq R_L \leq 440 \Omega$  as parameters with selected open-ended stub ( $Z_{s2}$ ,  $\theta_{s2}$ ) = (70 $\Omega$ , 30°) are shown in Fig 7 Note that the design charts shown in Fig. 6 and Fig. 7 can be flexibly utilized in any center frequency  $f_0$ .



**FIGURE 7.** Design graph of  $\theta_{m1o}$  and  $\theta_{m2o}$  using  $Z_{mo}$  and  $R_L$  as parameters with termination open-ended stub  $(Z_{s2}, \theta_{s2}) = (70 \ \Omega, \ 30^{\circ})$ . (a)  $R_L = 20$  to 200  $\Omega$ . (b)  $R_L = 200$  to 440  $\Omega$ .



FIGURE 8. Design model for the proposed type-A bandpass.

#### **III. DESIGN OF TYPE-A BPIMT USING A PCL SECTION**

In addition to the  $\Pi$ -tapped feeds realizing the specified external quality factor, the SE-PCL section constituting the BPIMT provides the required interstage coupling. On the foundation of Sec. II, the design model of the proposed type-A BPIMT shown in Fig. 2 is depicted in Fig. 8. The design approach of the proposed BPIMT will be investigated in this section.

#### A. SHORT-ENDED PARALLEL COUPLED-LINE

The SE-PCL serving as the interstage coupling adopted in Fig. 2 for even-/odd-mode characteristic impedances  $(Z_{0e}, Z_{0o})$  and coupled length  $\theta_c$  can be modeled [26] by an admittance inverter  $J_{12}$  attached to two shunt short-circuited



FIGURE 9. Equivalent-circuit model of the SE-PCL adopted in Fig. 2.

stubs ( $\theta_C$ ,  $Y_h$ ) as shown in Fig. 9. The required  $J_{12}$  value is determined by the two adjacent resonators. The input admittances looking toward the LHS and RHS of inverter  $J_{12}$  are  $jB_{1R}$  and  $jB_{2L}$  associated with resonators 1 and 2, respectively, and they can be readily calculated by network analysis. It is worth mentioning that the two resonators are not identical due to asymmetric  $R_S$  and  $R_L$ , and thus, they possess different susceptance slope parameters observed from the LHS of resonator 1 and from the RHS of resonator 2 given as

$$B_{1R} = -Y_h \cot \theta_C + Y_2 (B_{TI} + Y_2 \tan \theta_2) / (Y_2 - B_{TI} \tan \theta_2)$$
  

$$B_{2L} = -Y_h \cot \theta_C + Y_2 (B_{TO} + Y_2 \tan \theta_2) / (Y_2 - B_{TO} \tan \theta_2)$$
(6)

The susceptance slope parameters  $b_{1R}$  and  $b_{2L}$  at  $f_0$  can be found by differentiating  $B_{1R}$  and  $B_{2L}$  with respect to frequency.

By providing the coupled length  $\theta_C$ , the preferable reference admittance  $Y_h$ , and the coupling coefficient  $k_{12}$ , the  $Y_{0e}$  and  $Y_{0o}$  of the PCL section can be solved from

$$Y_{0e} = Y_h + J_{12}\sin\theta_C \text{ and } Y_{0o} = Y_h - J_{12}\sin\theta_C \quad (7a)$$

with  $J_{12} = Y_d / \sin\theta_C$  and  $Y_h = (Y_{0o} + Y_{0e})/2$ . As a result, the admittance inverter value can be obtained through

$$\frac{J_{12}}{\sqrt{b_{1R}b_{2L}}} = k_{12} = \frac{\Delta}{\sqrt{g_{1g_2}}}, \text{ where } Y_d = \frac{Y_{0o} - Y_{0e}}{2}.$$
 (7b)

According to (7), it is evident that both the source and load resistances  $R_S$  and  $R_L$  will affect the interstage coupling since  $b_{1R}$  and  $b_{2L}$  depend on source and load terminations, respectively. After determining that the source impedance  $R_S = 10 \Omega$ , the coupled length  $\theta_c = 70^\circ$ , the element values of lowpass prototype  $g_2 = 0.8431$ ,  $g_3 = 0.6220$ , and the FBW  $\Delta = 7\%$ , the calculated even-/odd-mode impedances ( $Z_{0e}, Z_{0o}$ ) with  $R_L$  as parameters are drawn in Fig. 10 indicating that the variation of the load resistance alters the even-/odd-mode impedances. Note that for layout convenience, the line characteristic impedances  $Z_{mo}$  of the output  $\Pi$ -tapped feed are chosen as  $60 \Omega$  for  $20 \Omega \leq R_L \leq 200 \Omega$  and  $80 \Omega$  for  $200 \Omega \leq R_L \leq 440 \Omega$ .

### B. COMPLETE BANDPASS IMPEDANCE TRANSFORMER DESIGN

The design procedure is as follows:

1) Specify the source and load impedances  $(R_S, R_L)$ , the filter specifications including  $f_0$ , FBW, and the low-pass prototype response thus giving the relevant  $Q_{EI}$ ,  $Q_{EO}$ , and  $k_{12}$ .



**FIGURE 10.** Design graph for determining  $(Z_{0e}, Z_{0o})$  using  $R_L$  as a parameter with termination  $R_5 = 10 \ \Omega$ , open-ended stubs  $(Z_{51}, \theta_{51}) = (70 \ \Omega, 45^\circ)$  and  $(Z_{52}, \theta_{52}) = (70\Omega, 30^\circ)$ , coupled length  $\theta_C = 70^\circ$ , the reference impedance  $Z_h = 60 \ \Omega$ , and  $Z_2 = 60 \ \Omega$  (the filter is designed for Chebyshev 0.1-dB-ripple response). (a)  $20 \ \Omega \le R_L \le 200 \ \Omega$ . (b)  $200 \ \Omega \le R_L \le 440 \ \Omega$ .

- 2) Determine the impedance values  $Z_1$  and  $Z_2$  of the  $\lambda/4$  SIR and calculate the corresponding susceptance slope parameter  $b_{\lambda/4}$ .
- 3) Select the appropriate characteristic impedances  $Z_{mi}$ and  $Z_{mo}$  for the I/O  $\Pi$ -tapped feeds and pick up the open-circuited stubs  $(Z_{s1}, \theta_{s1})$  and  $(Z_{s2}, \theta_{s2})$ . The electrical lengths  $(\theta_{m1} \text{ and } \theta_{m2})$  can then be calculated based on (5). The auxiliary design graphs for determining the electrical lengths  $\theta_{m1}$  and  $\theta_{m2}$  relevant to the input and output feeds can be drawn to facilitate the design.
- 4) Once the I/O  $\Pi$ -tapped feeds are both available, the susceptance slope parameters  $b_{1R}$  and  $b_{2L}$  required in (7) for obtaining the even-/odd-mode impedances of the PCL section can be calculated by (6). The auxiliary design graphs for determining the PCL impedances  $Z_{0e}$  and  $Z_{0o}$  can be drawn to facilitate the design.
- 5) Finally, convert the electrical design parameters into physical dimensions and optimize the BPIMT using a full-wave EM simulator.

Note that the asymmetric structure makes the high impedance transformation ratio possible and the synthesis approach is applicable for flexible  $r_Z$ . Different from those works in the literature, the proposed approach originated from the inverter-based coupled-resonator filter.

#### TABLE 1. Circuit design parameters.





**FIGURE 11.** Circuit-level simulated (solid line) scattering and calculated parameters from the coupling-matrix analysis (dashed line) of BPIMTs CktA1 and CktA2. (a) 10:200 Chebyshev 0.1-dB-ripple response FBW=7%. (b) 5:475 Butterworth response FBW = 10%.

### **IV. DESIGN AND IMPLEMENTATION OF A TYPE-A BPIMT**

To demonstrate the synthesis feasibility, two sample circuits with the specifications shown in Table 1 are designed. CktA1 is designed with a moderate transforming ratio of  $r_Z = 20 \ \Omega/\Omega$  whereas CktA2 is designed with an extremely high impedance ratio of  $r_Z = 95 \ \Omega/\Omega$ . The circuit-level simulated results using ideal TL components and the calculated results from coupling-matrix analysis are compared in Fig. 17 showing satisfactory agreement in terms of bandwidth, return loss, and passband ripple. The design formulas are proven accurate for achieving a target filtering impedance transformer.

The two type-A BPIMTs will be fabricated and measured in this section. The measurements are carried out by an R&S ZVB20 network analyzer. For measurement purposes, two 15-mm-long 50 Ohm lines are attached to the I/O ports of all circuits where the TRL (through-reflection-line) calibration technique is then adopted to de-embed their effects including the SMA connectors.

#### A. BPIMT CKTA1: $r_Z = 20$

A sample BPIMT (CktA1) with  $R_S = 10 \Omega$  and  $R_L = 200 \Omega$ was designed with  $f_0 = 2.5$  GHz and ripple- $\Delta = 7\%$ 



**FIGURE 12.** (a) Layout  $(w_m = 0.81, L_{m1i} = 8.7, L_{m2i} = 2.3, w_2 = 4.3, L_2 = 0.81, w_{s1} = 0.57, L_{s1} = 9.3, w_{s2} = 0.57, L_{s2} = 6.2, L_{m1o} = 4.9, L_{m2o} = 7.45$  mm) and (b) circuit photograph of the proposed bandpass impedance transformer CktA1 (10:200).



**FIGURE 13.** EM simulated and measured scattering parameters of the 10:200 BPIMT CktA1 with Chebyshev 0.1-dB-ripple response and FBW=7%. (a) Passband  $S_{11}$  and  $S_{21}$ . (b) Zoom-in  $S_{11}$ ,  $S_{22}$ , and  $S_{21}$ . (c) Wideband-view response.

for a Chebyshev 0.1-dB-ripple response. The filter design parameters are  $Q_{EI} = Q_{EO} = 12.044$  and  $k_{12} = 0.0967$ . The  $\lambda/4$  SIR has  $Z_1 = Z_2 = 60 \Omega$ ,  $\theta_c = 70^\circ$ ,  $\theta_2 = 20^\circ$  and its relevant  $b_{\lambda/4} = 1.31$  cS. The two open-circuited stubs attached to the input and output tapped feeds are picked up with electrical lengths 45° and 30°, respectively, for creating TZs at  $2f_0$  and  $3f_0$ . With (3), the calculated susceptance slope parameters are  $(b_{1L}, b_{2R}) = (35.23, 29.4)$  cS. The calculated electrical length  $(\theta_{m1i}, \theta_{m2i})$  of the input tapped feed with  $Z_{mi} = 60 \Omega$  is labeled point P1 in Fig. 6 whereas the  $(\theta_{m1o}, \theta_{m2o})$  of the output tapped feed with  $Z_{MO} = 60 \Omega$ is labeled point P2 in Fig. 7. With (6), the  $(b_{TI}, b_{TO}) =$ (22.14, 16.31) cS and  $(b_{1R}, b_{2L}) = (39.56, 32.95)$  cS leading to the inverter value  $J_{12} = 3.49$  cS. By setting  $Z_{mo} = Z_{mi}$ , point P3 in Fig. 10 gives the PCL information. The design electrical parameters for the schematic of the type-A BPIMT in Fig. 2 are now completely determined.



**FIGURE 14.** (a) Layout  $(w_{mi} = 1.9, L_{m1i} = 9.55, L_{m2i} = 4.1, w_2 = 1.45, L_2 = 5.3, w_{s1} = 1.1, L_{s1} = 11.8, w_{s2} = 1.1, L_{s2} = 8.1, w_{m0} = 0.86, L_{m20} = 15.1$ ) and (b) circuit photograph of the proposed bandpass impedance transformer CktA2 (5:475).

The transformer CktA1 was implemented on a 0.508-mmthick RO4003c substrate ( $\varepsilon_r = 3.55$ , tan $\delta = 0.0027$ ). The layout dimensions of the fabricated BMIMT CktA1 are annotated in Fig. 14. The circuit size excluding the feedlines is  $32.32 \times 10.36 \text{ mm}^2$  (0.2265 × 0.085  $\lambda_0^2$ ). The passband scattering parameters are shown in Fig. 15(a) and the zoomin  $S_{11}$ ,  $S_{22}$ , and  $S_{21}$  are presented in Fig. 15(b). The measured center frequency, minimum insertion loss and 3 dB-FBW are 2.52 GHz, 0.883 dB and 13.26%, respectively. The -10-dB return loss bandwidth is from 2.404 to 2.636 GHz. The wideband frequency response ranging from 1 to 10 GHz is shown in Fig. 15(c). The 20 dB rejection bandwidths at lower and higher sidebands are from dc to 2.074 GHz and from 3.02 to 8.62 GHz. Note that the abrupt spike approximately 8 GHz may result from the inaccuracy of the TRL calibration.

#### *B. BPIMT CKTA2: r*<sub>Z</sub> = 95

The other type-A BPIMT (CktA2) with much higher impedance ratio  $r_Z = 95$  (5:475) is demonstrated. The transformer is designed with  $f_0 = 2.0$  GHz and 3 dB- $\Delta = 10\%$ 



**FIGURE 15.** EM simulated and measured inband scattering parameters of the BPIMT CktA2 (5:475) with Butterworth response FBW=10%. (a) Passband S<sub>11</sub> and S<sub>21</sub>. (b) Zoom-in S<sub>11</sub>, S<sub>22</sub>, and S<sub>21</sub>. (c) Wideband-view response.

for a Butterworth response. The filter design parameters are  $Q_{\rm EI} = Q_{\rm EO} = 14.14$  and  $k_{12} = 0.0707$ . It is worth mentioning that since the filter response is chosen differently now, the deign graphs for finding the  $(\theta_{m1}, \theta_{m2})$  of the input/output  $\Pi$ -tapped feeds and the  $(Z_{0e}, Z_{0o})$  shown in Figs. 6, 7, and 10 can be re-drawn on the derived formulas (5) and (7) if required.

A  $\lambda/4$  SIR identical to CktA1 is also selected here. The calculated susceptance slope parameters are  $(b_{1L}, b_{2R}) = (37.58, 26.92) \text{ cS}$  and  $(b_{1R}, b_{2L}) = (42.34, 30.34) \text{ cS}$  available for calculation of the model parameters. The electrical lengths for the input and output tapped feeds are  $(\theta_{m1i}, \theta_{m2i}) = (52.25^{\circ}, 14.97^{\circ})$  with  $Z_{mi} = 50 \Omega$  and  $(\theta_{m1o}, \theta_{m2o}) = (4.05^{\circ}, 52.6^{\circ})$  with  $Z_{mo} = 80 \Omega$ , respectively. The inverter value  $J_{12}$  is 2.534 cS resulting in  $(Z_{0e}, Z_{0o}) = (70.0033, 52.4982) \Omega$  with  $\theta_C = 70^{\circ}$  and  $Z_h = 60 \Omega$ .

The transformer is implemented on an 0.813-mm-thick RO4003c substrate ( $\varepsilon_r = 3.55$ , tan $\delta = 0.0027$ ). The layout dimensions of the fabricated BMIMT CktA2 are annotated in Fig. 12. The circuit size excluding the feedlines

is  $30.85 \times 14.37 \text{ mm}^2$  (0.203 × 0.095  $\lambda_0^2$ ). The passband scattering parameters are shown in Fig. 13(a) and the zoomin  $S_{11}$ ,  $S_{22}$ , and  $S_{21}$  are presented in Fig. 13(b). The measured center frequency, minimum insertion loss and 3 dB-FBW are 1.974 GHz, 0.9436 dB and 10.033%, respectively. The -10-dB return loss bandwidth is from 1.913 to 2.034 GHz. The wideband frequency response ranging from 1 to 8 GHz is shown in Fig. 13(c). The 20-dB rejection bandwidths at lower and higher sidebands are from dc to 1.67 GHz and from 2.275 to 7.2 GHz. Two transmission zeros, TZ1 and TZ2 contributed by the open-circuited stubs, can be found among the stopband.

## V. DESIGN AND IMPLEMENTATION OF THE TYPE-B BPIMT USING INDUCTIVE COUPLING

The impedance-transformation technique based on the proposed  $\Pi$ -tapped feeds can be applied in different types of coupled-resonator filter topologies. Different from the type-A BPIMT, in this section, the type-B BPIMT utilizing inductive coupling [27] is proposed as shown in Fig. 16(a).



FIGURE 16. Type-B BPIMT with inductive coupling. (a) Schematic. (b) Inverter-based equivalent-circuit model.

#### A. DESIGN APPROACH

The schematic shown in Fig. 16(a) can be converted to the equivalent-circuit model presented in Fig. 16(b). Likewise, the  $\Pi$ -tapped feed can be design based on Sec. II. For the inductive coupling between resonators [28], it can be modeled as an impedance inverter  $K_{12}$ 

$$L_{12} = \frac{Z_1}{\omega_0} \frac{K_{12}/Z_1}{1 - (K_{12}/2)} \quad \text{and} \quad \varphi_{12} = -\frac{1}{2} \tan^{-1} \frac{2X_{12}}{Z_1}.$$
 (8a)

with

$$K_{12} = \sqrt{\frac{\Delta^2 \cdot x_{1R} \cdot x_{2L}}{g_1 g_2}},$$
 (8b)

where  $x_{1R}$  and  $x_{2L}$  are the reactance slope parameters observed from the LHS of resonator 1 and from the RHS of resonator 2, respectively. The reactance slope parameters  $x_{1R}$ and  $x_{2L}$  at  $f_0$  can be found by differentiating  $X_{1R}$  and  $X_{2L}$  with respect to frequency. The reactances  $X_{1R}$  and  $X_{2L}$  are

$$X_{1R} = \frac{(B_{TI} \tan \theta_2 - Y_2) + \alpha_Y \tan \theta_1 (B_{TI} + Y_2 \tan \theta_2)}{\alpha_Y^{-1} (Y_2 - B_{TI} \tan \theta_2) + (B_{TI} + Y_2 \tan \theta_2)}$$
$$X_{2L} = \frac{(B_{TO} \tan \theta_2 - Y_2) + \alpha_Y \tan \theta_1 (B_{TO} + Y_2 \tan \theta_2)}{\alpha_Y^{-1} (Y_2 - B_{TO} \tan \theta_2) + (B_{TO} + Y_2 \tan \theta_2)}.$$
(9)

Note that under the particular UIR condition, the TL section  $\theta_1 + \theta_2$  becomes a uniform  $\lambda/4$  transformer with characteristic admittance  $Y_1(=1/Z_1)$  at  $f_0$  causing

$$X_{1R} \approx B_{TI}/Y_1^2$$
 and  $X_{2L} \approx B_{TO}/Y_1^2$ . (10a)

Based on (10a), the  $x_{1R}$  and  $x_{2L}$  are approximated as

$$x_{1R} \approx b_{TI}/Y_1^2$$
 and  $x_{2L} \approx b_{TO}/Y_1^2$  (10b)

where  $b_{TI}$  and  $b_{TO}$  represent the susceptance slope parameters of the input and output  $\Pi$ -tapped feeds. Through (10), one can convert the calculated  $b_{TI}$  and  $b_{TO}$  acquired from (5) to the  $x_{1R}$  and  $x_{2L}$  required in (8) for this type-B BPMIT as the target FBW is relatively narrow.

For demonstration, a BPIMT with  $f_0 = 2.0$  GHz and  $3 \text{ dB-}\Delta = 10\%$  was designed for a Butterworth response. The filter design parameters are  $Q_{EI} = Q_{EO} = 12.044$ and  $k_{12} = 0.0967$ . The line impedances  $Z_{mi} = 50 \Omega$  and  $Z_{mo} = 80 \Omega$  for the input/output  $\Pi$ -tapped feeds are first determined, and the  $\lambda/4$  SIRs adopted here are  $Z_1 = Z_2 =$ 60  $\Omega$  and  $\theta_1 + \theta_2 = 90^\circ$ . The calculated susceptance slope parameters are  $(b_{\text{TI}}, b_{\text{TO}}) = (24.49, 13.84) \text{ cS}, (b_{1L}, b_{2R}) =$ (37.58, 26.93) cS, and  $(x_{1R}, x_{2L}) = (134.08, 96.35) \Omega$  for evaluating the model parameters. The electrical lengths for the input and output  $\Pi$ -tapped feeds are  $(\theta_{m1i}, \theta_{m2i}) =$  $(52.25^{\circ}, 14.97^{\circ})$  and  $(\theta_{m1o}, \theta_{m2o}) = (0.41^{\circ}, 56.18^{\circ})$ , respectively. The inverter value  $K_{12}$  is 8.038  $\Omega$  resulting in  $L_{12}$  = 0.6513 nH with  $\varphi_{12} = -7.63^{\circ}$ . The circuit-level simulated results using ideal TL components and the calculated results from the coupling-matrix analysis are compared in Fig. 17, showing significant agreement in terms of bandwidth, return loss, and passband ripple.



**FIGURE 17.** Circuit-level simulated (solid line) scattering and calculated parameters from the coupling-matrix analysis (dashed line) of the 5:520 BPIMT CktB with Butterworth response FBW = 10%.

In microwave practice, short-ended stubs are commonly adopted to implement the inductive components. To reduce the effect of process tolerance, a double-loaded short-circuited stub is employed to achieve the required  $K_{12} = 8.03813 \ \Omega$ . The inverter value  $K_{12}$  and electrical



**FIGURE 18.** EM-extracted inverter  $K_{12}$  value ( $w_1 = 1.5$ ,  $w_{ind} = 0.6$ ,  $w_p = 0.9$  mm, Via diameter = 0.5 mm). (a)  $K_{12}$  vs. frequency. (b) Design graphs of  $K_{12} / \varphi_{12}$  vs.  $d_{12} @ f_0 = 2$  GHz.

lengths of the cascading lines corresponding to the inductive coupling can be extracted with the EM simulator [29]. The EM-extracted inverter values vs. frequency are shown in Fig. 18(a). The realistic  $K_{12} / \varphi_{12}$  design graph extracted at 2 GHz vs. the stub length  $l_{in}$  is displayed in Fig. 18(b). With the aid of Fig. 18(b), one can determine the demanded stub length according to the filter specification.

#### **B. IMPLEMENTATION AND MEASUREMENT**

The transformer CktB was fabricated on an 0.813-mm-thick RO4003c substrate ( $\varepsilon_r = 3.55$ , tan $\delta = 0.0027$ ). The layout dimensions of the fabricated BMIMT CktB are annotated in Fig. 19. The circuit size excluding the feedlines is  $31.22 \times 23.5 \text{ mm}^2$  (0.208 × 0.156  $\lambda_0^2$ ). The passband scattering parameters are shown in Fig. 20(a) and the zoom-in  $S_{11}$ ,  $S_{22}$ , and  $S_{21}$  vs. frequency are presented in Fig. 20(b). The measured center frequency, minimum insertion loss and 3 dB-FBW are 1.997 GHz, 1.171 dB and 7.96%, respectively. The -10-dB  $S_{11}$  and  $S_{22}$  bandwidths are 1.96-2.048 and 1.958-2.067 GHz, respectively. The measured bandwidth shrinkage may result from the drilling inaccuracy of the hole position. The wideband frequency response ranging from 1 to 8 GHz is shown in Fig. 20(c). The 20-dB rejection bandwidths at lower and higher sidebands are from dc to 1.771 GHz and from 2.266 to 4.497 GHz. Since the resonators



**FIGURE 19.** (a) Layout ( $w_f = 1.9$ ,  $w_{MI} = 1.9$ ,  $L_{m1i} = 11.63$ ,  $L_{m2i} = 3.49$ ,  $w_{s1} = 1.1$ ,  $L_{s1} = 11.65$ ,  $w_1 = 1.5$ ,  $L_1 + L_2 = 18.55$ ,  $w_{ind} = 0.6$ ,  $l_{ind} = 2.13$ ,  $w_{mo} = 0.83$ ,  $L_{m2o} = 14.45$ ,  $w_{s2} = 1.1$ ,  $L_{s2} = 7.5$ , Unit: mm) and (b) circuit photograph of the proposed bandpass impedance transformer CktB (5:520).

constituting the BPIMT are linked by inductive coupling, the resonance phenomena become more complicated than the edge-coupled type filter. The out-of-band response cannot merely be predicted by the isolated resonator resonances but by the resonances of linked resonators.

Ref	$f_c$ (GHz)	FBW (%)	Ratio $r_Z$ ( $\Omega/\Omega$ )	Specification Designable	
[10]	2.0	77.8% (17 dB RL)	$r_z = 2.2$ (50:110)	FBW (yes) response (yes)	
[12]	2.0	54% (15 dB RL)	$r_z = 4.0$ (50:200)	FBW (no) Response (yes)	
[15]	2.0	13.22 (15 dB RL)	$r_z = 2.0$ (25:50)	FBW (yes) response (yes)	
[17]	1.0	50% (15 dB RL)	$r_z = 2.0$ (25:50)	FBW (yes) response (yes)	
[18]	2.0	9.6% (15 dB RL)	$r_z = 20$ (50:1000)	FBW (yes) response (yes)	
[19]	2.6	8.27% (18 dB RL)	$r_z = 10$ (5:50)	FBW (yes) response (yes)	
This CktA1	2.5	Chebyshev 13% (3 dB-IL)	$r_Z = 20$ (10:200)	FBW (yes) response (yes)	
This CktA2	2.0	Butterworth 10% (3 dB-IL)	$r_Z = 95$ (5:475)	FBW (yes) response (yes)	
This CktB	2.0	Butterworth 10% (3 dB-IL)	$r_z = 104$ (5:520)	FBW (yes) response (yes)	

TABLE 2.	Comparison	with	previous	works.
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\* IL: insertion loss; RL: return loss

#### VI. PERFORMANCE COMPARISON AND DISCUSSION

Table 2 compares the three circuits proposed in this study with filtering impedance transformers in the literature. The proposed BPIMT utilizing  $\Pi$ -tapped feeds originates from the inverter-based coupled-resonator filter and thus can be designed through the external quality factors and coupling



**FIGURE 20.** EM simulated and measured inband scattering parameters  $S_{11}$  and  $S_{21}$  of the 5:520 BPIMT CktB with Butterworth response FBW=10%. (a) Passband  $S_{11}$  and  $S_{21}$ . (b) Zoom-in  $S_{11}$ ,  $S_{22}$ , and  $S_{21}$ . (c) Wideband-view response.

coefficients according to specifications. In this way, as the filtering order goes higher, the design approach can be readily extended without increasing complexity too much. The filter response and FBW can be more flexibly controlled. It is worth mentioning that the proposed BPIMTs achieve an extremely high impedance transforming ratio and a wide range of source and load impedances.

#### **VII. CONCLUSION**

Bandpass impedance transformers featuring extremely high transforming ratio, designable filter response, and simple structure are proposed in this study. The synthesis approaches, detailed design formulas and the auxiliary design graphs for two different BPIMT topologies are well developed and validated by experimental results. Theoretically speaking, the proposed  $\Pi$ -tapped feeds can be extensively applied in most coupled-resonator filters for achieving impedance transformation. Moreover, the synthesis method can be readily extended to BPIMT with higher order (N > 2). Specifically, the proposed BPIMTs achieve an extremely high transforming ratio of 104, which is the highest value reported

to the best of the authors' knowledge. The BPIMT can find applications in RF/microwave front ends.

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