

Received February 7, 2017, accepted March 7, 2017, date of publication March 13, 2017, date of current version May 17, 2017.

Digital Object Identifier 10.1109/ACCESS.2017.2681697

# Output Predictor-Based Active Disturbance Rejection Control for a Wind Energy Conversion System With PMSG

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This work was supported in part by the National Natural Science Foundation of China under Grant 51405428, in part by the Natural Science Foundation of Jiangsu Province under Grant BK20140490, in part by the Open Project Program of Ministry of Education Key Laboratory of Measurement and Control of CSE, under Grant MCCSE2015A01 and Grant MCCSE2016A01, and in part by a Project Funded by the Priority Academic Program Development of Jiangsu Higher Education Institutions.

**ABSTRACT** Considering the internal and external disturbances in wind energy conversion systems, a predictive active disturbance rejection control (PADRC) strategy for a direct-driven permanent magnet synchronous generator (PMSG)-based wind energy conversion system, is proposed to maximize the wind power extraction in this paper. First, the proposed PADRC method can successfully deal with the effects of the uncertainties in the internal dynamics, modeling error, external forces and the variety of wind speeds, since it inherits the merits of active disturbance rejection control (ADRC). Second, the introduction of Smith Predictor can overcome the time delay in wind turbine system to guarantee the maximum power tracking performance for different wind speeds. Finally, simulation studies are conducted to evaluate power tracking performances of the proposed control strategy. It is shown that the proposed PADRC strategy exhibits significant improvements in both maximum power tracking performance and anti-disturbance ability compared with the traditional ADRC approach.

**INDEX TERMS** Permanent magnet synchronous generator, wind energy conversion system, active disturbance rejection controller, smith Predictor, maximum power tracking.

## I. INTRODUCTION

Global warming and harmful effect of fossil fuel emissions on the climate and environment have boosted worldwide interests in the renewable energy resources [1], [2]. Among them, wind energy as a new pollution-free and inexhaustible resource is extensively developed in recent decades due to the probable depletion, high costs, and negative environmental impacts of conventional energy sources. Among currently available wind energy conversion systems (WECSs), there are mainly two kinds of operation mode of generator, i.e., the fixed speed mode, and the variable speed mode. The variable speed wind turbines are preferable to fixed speed ones, since the variable speed wind turbines have simpler structure with more stability, lower mechanical stress, smaller aerodynamic noise. Moreover, the variable speed wind turbines can capture the maximum power over a wide range of wind speed by adjusting the generator's speed to be its optimal one. The direct-driven PMSG has been widely applied in WECSs owing to its competitive advantages, such as gearless

construction, high power density, little noise, high efficiency, good reliability, easy maintenance [3]. In addition, the direct-driven PMSG can possibly be operated at low speeds but still achieve high torques. It is well-known that the main control purpose for the wind turbine in the low speed region is the power efficiency maximization. Thus, in order to achieve optimum wind energy extraction from the wind turbine below the rated wind speed, the wind turbine generator should be operated in variable-speed mode. To achieve this goal, the tip speed ratio should be maintained at its optimum value despite variation of wind speed. Due to stochastic characteristics of natural wind, along with the aerodynamic characteristics of a wind turbine, the WECS are essential non-linear systems [4], [5]. In addition, the performance of WECS is interrupted by lumped disturbances, including internal disturbances, i.e., parameter variations, control couplings, modeling errors and nonlinear dynamics of the plant, and external disturbances which mainly come from wind gusting, torsional vibration, wind stream dissymmetry, etc [6], [7]. The lumped

disturbances cause the parameter variations, large power fluctuations and unavoidable vibrations with detrimental effects to wind turbines. So the anti-disturbance ability of wind turbine is a significant task to capture the optimal power in real time.

Over the past few decades, numerous feedback control strategies have been exploited to improve the efficiency and power quality of wind turbine equipped with PMSG [8]–[11]. Although these conventional feedback based maximum power point tracking methods can finally suppress them through feedback regulation in a relatively slow way, they usually cannot react directly and fast enough to reject the lumped disturbances. Moreover, wind turbines are expected to work effectively under wide range of wind speeds. Therefore, the control designs for wind energy conversion systems become more significant. Since the sliding mode control (SMC) shows a good robustness for anti-disturbances, it is widely used in WECS. To deal with the problem of controlling power generation in variable speed wind turbines, a high-order sliding-mode control strategy is proposed to maximize the generated power from wind turbine in [12]. The proposed strategy presents excellent dynamic performance robust against parametric uncertainties and lumped disturbances. Commonly, the SMC faces an unavoidable application problem which is known as chattering. This can degrade the tracking performance when the WECS encounters severe disturbances. Hence, we should rationally design the control algorithm for maximum power tracking of the WECS, with the aim of obtaining robustness of the whole closed-loop system. Unfortunately, the accurate model of WECS is difficult to obtain and lumped disturbances cannot be directly measured or require costly sensors, which bring many challenges to control algorithm design.

The active disturbance rejection controller (ADRC) is a novel robust control method to attenuate internal and external disturbances. A nonlinear ADRC method is originally proposed by Han in 1995 [13], and then fully articulated in 2009 after more than ten years' developments [14]. Compared with the model-based control methods, the ADRC can be designed without the detailed mathematical model. The essence of ADRC is that both the internal uncertainties and external disturbances, i.e., lumped disturbances, can be estimated by an extended state observer (ESO), then the effect of lumped disturbances can also be compensated by the feed-forward channel with the estimated value. On the basis of nonlinear ADRC proposed by Han, a structure of linear ADRC (LADRC) with the advantages of nonlinear ADRC, is proposed by Gao for the practical industrial applications [15]. The LADRC simplifies the controller design and reduces the difficulty in tuning, analysis and implementation. Due to these promising features, the LADRC, as a new control design framework, has become increasingly popular and been widely investigated in recent years. Nowadays, the LADRC has been widely applied to various industrial areas, such as motor system [16], robotic system [17], maglev system [18], structural vibration [19], energy conversion

systems [20], tower cranes [21], and non-minimum phase system [22]. However, the employment of ADRC into PMSG-based wind energy conversion system is rather new.

Compared with the conventional strategies in WECSs, the LADRC has some advantages, such as little requirement of information about the plant dynamics, simple structure, excellent ability of disturbance rejection. But LADRC also has some limitations for WECS, especially in certain situations with high inertia, strong nonlinearity, rapid parameters perturbations, and large random external disturbances. Under such circumstances, ESOs may not estimate lumped disturbance accurately. In order to solve the problem of severe lumped disturbances in PMSG based WECS, the authors proposed a model-based ADRC method with the available model information into an ESO to efficiently compensate the lumped disturbances [2].

Besides these severe disturbances, the time delay is also a major issue of control system design for the excellent performance of WECSs with LADRC method. The time delay of WECS may arise from many terms, including computational delay, the finite response time of the inner current loop and sensor, the mechanical coupling, and the transmission characteristics [23]. The time delay will give rise to current waveforms distortion, voltage losses and torque pulsation torque pulsation. Thus, the time delay in WECS also poses a serious challenge. Considering the characteristics of WECS, this paper aims to deal with the critical issue in WECS based on direct-driven (PMSG): the attenuation of the effects of disturbances and the time delay, with the aim of extracting maximum power from the wind turbine below the rated speed. In this paper, ADRC is a proposed control solution to the PMSG-based WECS. Since the Smith Predictor is a specifically method to solve the problem of time delay in control systems, a novel predictive ADRC (PADRC) based on Smith Predictor is introduced to the variable speed wind turbines to deal with the challenges of lumped disturbances and the time delay in WECS.

The rest of this paper is organized as follows. The dynamics of PMSG based wind turbine are described in **Section II**. The control scheme of the proposed PADRC for PMSG is illustrated in **Section III**. Simulation researches with several kinds of wind types are carried out to verify the superiority of the proposed PADRC method in **Section IV**. The conclusions are given in the last.

## II. WIND TURBINE SYSTEM DESCRIPTION

### A. WIND TURBINE MODELING

The mechanical power  $P_m$  extracted by a variable speed wind turbine from the natural wind is expressed as follows [24]:

$$P_m = \frac{1}{2} \rho \pi R^2 C_P(\lambda, \beta) v^3, \quad (1)$$

The mechanical torque of the wind turbine can be described as,

$$T_m = 0.5 \rho \pi C_P(\lambda, \beta) R^3 v^2 / \lambda, \quad (2)$$

where  $\rho$ ,  $R$ ,  $v$  and  $\lambda$  are the air density, the blade radius, wind speed and tip-speed ratio, respectively. The parameter  $C_p$  denotes the power coefficient of wind turbine, which depends on the blades' aerodynamic design and operating conditions. It is a nonlinear function of the blade pitch angle  $\beta$  and the tip-speed ratio  $\lambda$ , which is given by (3), as indicated in [24]:

$$\lambda = \frac{\omega R}{v}, \quad (3)$$

where  $\omega$  is the angular velocity of rotor (rad/s). The parameter  $C_p(\lambda, \beta)$  can be expressed by the following equation [24],

$$C_p(\lambda, \beta) = 0.22 \left( \frac{116}{\lambda_i} - 0.4\beta - 5 \right) e^{-\frac{12.5}{\lambda_i}} + 0.0068\lambda, \quad (4)$$

where  $\frac{1}{\lambda_i} = \frac{1}{\lambda + 0.08\beta} - \frac{0.035}{\beta^3 + 1}$ .

The typical curves of  $C_p$  versus  $\lambda$  is obtained in [2]. According to Eq. (1), for a given value of wind speed  $v$ , the maximum power extraction is achieved when  $C_p$  takes its maximum value. Therefore, the power coefficient  $C_p$  for each  $\beta$  can reach a maximum value at the optimum tip-speed ratio  $\lambda_{opt}$ . The maximum power coefficient  $C_{pmax}$  ( $C_p = 0.48$ ) can be achieved when  $\beta = 0$  and  $\lambda = 8$ . And from Eq.(3), it can be obtained that the output power is the maximum at the optimum speed  $\omega_{opt}$  for a certain  $v$ , which corresponds to the optimum tip speed ratio  $\lambda_{opt}$ . Therefore, the wind turbine should be always operated at  $\lambda_{opt}$  to extract maximum power at variable wind speed when the wind speeds are below the rated speed of wind turbine. The speed of wind turbine should be equal to the optimum speed  $\omega_{opt}$  to achieve the optimum power extraction.

### B. PMSG MODELING

According to the theory of the space vector, the stator voltage equations for PMSG can be represented in the rotating  $d$ - $q$  reference frame as follows [24], [25],

$$\begin{cases} u_d = L_d \frac{di_d}{dt} + R_s i_d - L_q n \omega i_q \\ u_q = L_q \frac{di_q}{dt} + R_s i_q + L_d n \omega i_d + n \omega \psi_f \end{cases} \quad (5)$$

where  $u_d$ ,  $u_q$  and  $i_d$ ,  $i_q$  are the stator voltages and currents in the direct and quadrature axis of rotor, respectively. The parameters  $R_s$ ,  $\psi_f$  and  $n$  are the resistance of stator windings, the magnet flux and the pair of poles, respectively. The parameters  $L_d$ ,  $L_q$  are the  $d$ - $q$  inductances of the stator windings, here  $L_q = L_d = L$ . The electromagnetic torque  $T_e$  of PMSG can be given as Eq.(6):

$$T_e = \frac{3}{2} n \psi_f i_q. \quad (6)$$

The rotor dynamics of wind turbine can be described as follows:

$$J \frac{d\omega}{dt} = T_m - B_v \omega - T_e, \quad (7)$$

where  $J$  ( $\text{kg} \cdot \text{m}^2$ ) represents the total inertia,  $B_v$  ( $\text{kg} \cdot \text{m}^2/\text{s}$ ) is the viscous friction coefficient, and  $T_m$  ( $\text{N} \cdot \text{m}$ ) denotes the drive torque.

## III. CONTROL DESIGN

### A. ADRC BASED ON SMITH PREDICTOR

Note that the ESO can deal with the uncertainties of the system. In order to achieve superior performance, the ADRC concept is introduced to design the controller for lumped disturbances. With the dynamic compensation of the estimation information, the speed loot for system (7) is reduced to a double integrator. Consider the following system dynamics.

$$J \dot{\omega} = F + g(\omega, t) + w \quad (8)$$

where  $F$  is the control variable,  $w$  is the external disturbances,  $t$  is the time and  $g(\omega, t)$  is a time-varying function of angular velocity. So the original system (8) is reformulated as,

$$\dot{\omega} = b_0 u + f(\omega, w, t) \quad (9)$$

where  $b_0$  is the parameter related to system model,  $f(\omega, w, t)$  is the lumped disturbances, which includes not only the external disturbances but also the unknown internal dynamics. Then the state vector of the systems can be defined as  $x = [x_1 \ x_2]^T = [\omega \ f]^T$ , which has two components. Note that for a first-order system the state vector is normally defined as  $x = [\omega]$  with one state variable. The variable  $x_2 = f$ , representing the lumped disturbances, is an extended state variable of the first-order system.

The state space representation of Eq. (9) is defined as:

$$\begin{cases} \dot{x} = Ax + b_0 Bu + Ef \\ y = Cx \end{cases} \quad (10)$$

where  $A = \begin{bmatrix} 0 & 1 \\ 0 & 0 \end{bmatrix}$ ,  $B = \begin{bmatrix} 1 \\ 0 \end{bmatrix}$ ,  $E = \begin{bmatrix} 0 \\ 1 \end{bmatrix}$ , and  $C = [1 \ 0]$ .

An extended state space form of Eq. (10) is designed as:

$$\dot{\hat{x}} = A\hat{x} + bBu + L(x_1 - \hat{x}_1) \quad (11)$$

where  $\hat{x} = [\hat{x}_1 \ \hat{x}_2]^T$  are the observer vector of the state vector  $x$ , and  $b$  represents the estimation of  $b_0$ . The vector  $L = [l_1 \ l_2]^T$  is the observer gain vector. Therefore, the ADRC of Eq.(11) can be expressed as follows for this SISO system.

$$u = k_1(y^* - \hat{x}_1) - \hat{x}_2/b \quad (12)$$

where  $y^*$  and  $k_1$  are the expected output value and controller gain of feedback channel, respectively. Combining the above Eq.(10), the state variable  $\hat{x}_1$  is an estimate of the output  $y$ .

Unfortunately, the ADRC controller with the structure (12) cannot directly handle the system time delay. It is well-known that Smith Predictor is an effective strategy to deal with the effect of time delays. The idea of incorporating the Smith Predictor technique, as shown in Fig. 1, is to have the controller act on the system without the delayed part. The tracking performance of the input wind speeds is significantly improved, since the proposed ADRC based on Smith Predictor method can provide a faster reaction to the changes in the system. According to the substance of the Smith Predictor method and the characteristics of the system, in order to solve the problems of lumped disturbances and time delay,

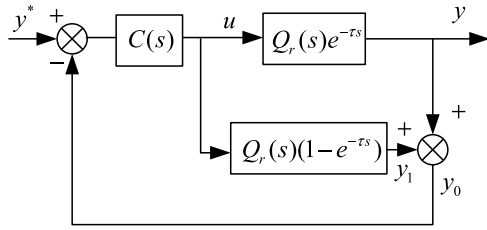


FIGURE 1. Classical structure of smith predictor.

simultaneously, the transfer function of whole system can be shown as Eq. (13),

$$Q(s) = Q_r(s)e^{-\tau s}, \quad (13)$$

where  $Q(s)$  and  $Q_r(s)$  describe the transfer function form of plant with time delay and the normal model, respectively. The parameter  $\tau$  is the time delay coefficient.

From Fig. 1, we can obtain that  $y = Q_r(s)e^{-\tau s}u$  and  $y_1 = Q_r(s)(1 - e^{-\tau s})u$ , respectively. Thus, it can be seen that the auxiliary output variable  $y_0$  is introduced to offset the effect of the delay loop, which is represents as:

$$y_0 = y + y_1 = Q_r(s)e^{-\tau s}u + Q_r(s)(1 - e^{-\tau s})u = Q_r(s)u \quad (14)$$

According to Eq. (14), the transfers function between  $u$  and  $y_0$  does not contain time delay loop. When time delay  $\tau$  is a small constant, Eq. (14) can be further rewritten as:

$$\begin{aligned} y_0 &= Q_r(s)u = Q_r(s)e^{-\tau s}\left(\frac{1}{e^{-\tau s}}\right)u \\ &= e^{\tau s}Q_r(s)e^{-\tau s}u \approx (1 + \tau s)y = y + \tau sy = y + \tau \dot{y} \end{aligned} \quad (15)$$

The last term of Eq. (15) indicates that the auxiliary output  $y_0$  can be obtained from the system output  $y$  and its differential  $\dot{y}$ . So the significant part in the controller design is to get an effective differentiation of  $y$  with the property of strong against noise.

In conventional PID implementation, the differentiation of output  $y$  is obtained approximately as:

$$\frac{s}{\tau s + 1}y = \frac{1}{\tau}\left(1 - \frac{1}{\tau s + 1}\right)y \quad (16)$$

Eq.(16) can also be rewritten in the following time domain,

$$\dot{y}(t) \approx \frac{1}{\tau}(y(t) - y(t - \tau)) \quad (17)$$

It indicates that if  $y(t)$  contains noise  $n(t)$ , from Eq. (17). The noise  $n(t)$  will be amplified by the factor of  $1/\tau$  in  $\dot{y}(t)$ . Therefore, this kind of approximation is quite sensitive to the noise. To solve this problem, the following approximation equation is employed in this paper.

$$\dot{y}(t) \approx \frac{y(t - t_1) - y(t - t_2)}{t_2 - t_1}, \quad t_2 > t_1 > 0, \quad (18)$$

And the delay signal  $y(t - t_1)$  can be obtained via first-order inertial part  $1/(t_1s + 1)$ . So the transfer function of

the approximate differential equation can be described as follows,

$$g_d(s) = \frac{s}{t_1 t_2 s^2 + (t_1 + t_2)s + 1}. \quad (19)$$

Thus, the control law of PADRC can be constructed in following Eq. (20),

$$\begin{cases} \dot{z}_1 = z_2 - 2p(z_1 - y_0) + b_0 u \\ \dot{z}_2 = -p^2(z_1 - y_0) \\ y_0 = y + \tau \dot{y} \end{cases} \quad (20)$$

where  $z_1$  is the estimate of auxiliary output  $y_0$ ,  $z_2$  is the estimate of lumped disturbances of the system,  $b_0$  is an estimate of  $b$ , and  $p$  is the observer bandwidth of ESO. Generally, the larger the observer bandwidth  $p$  is, the more accurate the estimation will be. However, a large observer bandwidth will increase noise sensitivity. Therefore, an appropriate observer bandwidth should be selected as a compromise between the tracking performance and the noise tolerance.

It can be seen from Eq. (20) that the auxiliary variable  $y_0$  can be obtained from the actual output of the system  $y$  and its derivative  $\dot{y}$ . So the proposed PADRC based on the Smith Predictor method can be described as the following remark.

*Remark:* First, the auxiliary variable  $y_0$  can be estimated through the ESO strategy using the actual output of the system  $y$  and its derivative  $\dot{y}$  based on Eq. (17). Then, the new form of the PADRC strategy can be designed based on the auxiliary output variable  $y_0$  to solve the time delay of wind turbine system. Thus, the novel control law of the ADRC method for wind energy conversion system can be given as Eq. (21),

$$u = k_p(y^* - z_1) - z_2/b_0 \quad (21)$$

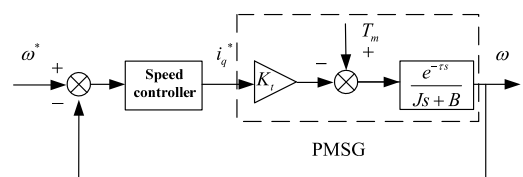


FIGURE 2. Structure of speed control for PMSG with time delay.

### B. THE PROPOSED PADRC DESIGN FOR PMSG

A system configuration of a vector-controlled PMSG drive with time delay is shown in Fig. 2. where  $K_r = (3/2)n\psi_f$ . The time delay coefficient  $\tau$  may arise from computational delay, the finite response time of the inner current loop and sensor, and other significant delay depends on the mechanical coupling and the transmission characteristics. The parameter  $\omega^*$  is the desired speed output from the wind turbine blade.

According to Eq. (7), the speed output of PMSG can be obtained as follows,

$$\dot{\omega} = \frac{T_m}{J} - \frac{B}{J}\omega + b_0 i_q = f + b_0 i_q \quad (22)$$

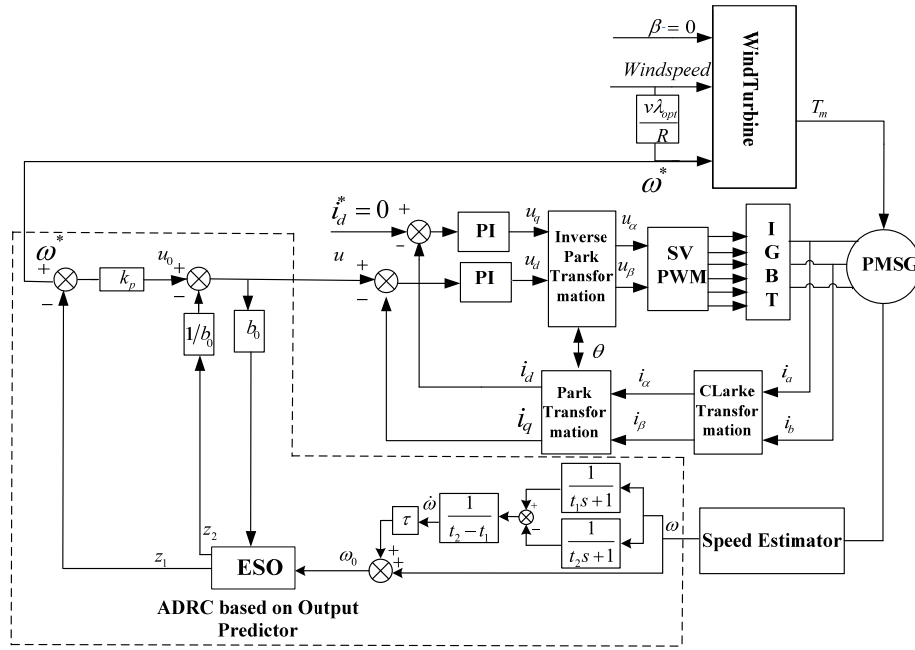


FIGURE 3. The scheme of the proposed PADRC for wind turbine based on PMSG.

TABLE 1. Specification of the PMSG based wind turbine.

PMSG parameters		Wind Turbine parameters	
Rotor inertial (kg·m <sup>2</sup> )	2×10 <sup>-3</sup>	Air density(kg/m <sup>3</sup> )	1.25
Permanent magnetic flux (Wb)	0.175	Optimum tip speed ratio	8
Stator inductance L(H)	8.5×10 <sup>-3</sup>	Basic wind speed(m/s)	6
Pole pairs	4	Turbine blade radius(m)	1.5
Stator resistance(Ω)	2.875	Maximum power coefficient	0.48
Viscous coefficient(N·ms/rad)	8.29×10 <sup>-5</sup>	Ttime delay(ms)	30
Rated Power (kW)	7.5	Rated wind speed (m/s)	37.5
Rated voltage (V)	380	Rated speed (rpm)	1500

where  $b_0 = -K_t/J$ . The function  $f = (T_m/J) - (B/J)\omega$  represents the lumped disturbances, including the friction, the unknown internal dynamics, the external disturbances, the tracking error of the current loop  $i_q$ , and the modeling error. Assuming that  $f$  is globally differentiable, the speed control loop of PMSG is reduced to a first-order system.

Then, the augmented state space form of the dynamic system can be obtained as follows,

$$\begin{cases} \dot{x}_1 = x_2 + bi_q \\ \dot{x}_2 = h \end{cases} \quad (23)$$

where the parameter  $h = df/dt = \dot{f}$  represents the differential of lumped disturbances. And the corresponding ESO of the speed control system for PMSG is designed as follows,

$$\begin{cases} \dot{z}_1 = z_2 - l_1(z_1 - \omega_0) + b_0u \\ \dot{z}_2 = -l_2(z_1 - \omega_0) \end{cases} \quad (24)$$

where  $z_1$  is the estimation of speed output. The parameter  $z_2$  is the estimation of unknown lumped disturbance  $f_i$ . And  $\omega_0 = \omega + \tau\dot{\omega}$  is the auxiliary speed output. The parameters

$l_1$  and  $l_2$  are the observer gains for different state variables. The observer gains are chosen such that the characteristic polynomial  $s^2 + l_1s + l_2$  is Hurwitz. Similar as [19], the ESO of the speed control loop can be chosen as,

$$\begin{cases} \dot{z}_1 = z_2 - 2p(z_1 - \omega_0) + b_0u \\ \dot{z}_2 = -p^2(z_1 - \omega_0) \\ \omega_0 = \omega + \tau\dot{\omega} \\ u = k_p(\omega_o^* - z_1) - z_2/b_0 \end{cases} \quad (25)$$

The observer bandwidth  $p$  should be well designed, so the outputs of ESO  $z_1$  and  $z_2$  can track  $\omega_0$  and  $f$ , respectively. By ignoring the effect of  $f$  using  $z_2$ , the scheme of the proposed PADRC for PMSG is shown in Fig.3.

#### IV. RESULTS AND ANALYSIS

To demonstrate the tracking performance of proposed PADRC strategy, comparative simulation studies with traditional ADRC are carried out in this section.

The parameters of PMSG-based WECS without connecting to the grid are shown in Table 1. A nomenclature summarizing all the symbols throughout this brief is furnished

TABLE 2. Nomenclature.

Symbol	Description [unit]	Symbol	Description [unit]
$A$	System Matrix of Eq.(10)	$T_m$	Mechanical torque of the wind turbine[N·m]
$B$	Input Matrix of Eq.(10)	$u$	Control variable
$B_v$	viscous friction coefficient[ $\text{kg}\cdot\text{m}^2/\text{s}$ ]	$u_d, u_q$	Stator voltage in the $d$ - $q$ axis[V]
$C$	Output Matrix of Eq.(10)	$V_b$	Base wind speed [m/s]
$C_p$	Power coefficient of wind turbine	$V_g$	Gust wind speed [m/s]
$F$	Turbulence scale	$V_n$	Noise wind speed [m/s]
$K_N$	Surface drag coefficient	$V_N$	natural wind speed [m/s]
$i_d, i_q$	Stator current in the $d$ - $q$ axis[A]	$V_r$	Ramp wind speed [m/s]
$J$	total inertia [ $\text{kg}\cdot\text{m}^2$ ]	$v$	Wind speed [m/s]
$L$	Observer gain vector	$\hat{x}$	Observer vector of $x$
$L_d, L_q$	$d$ - $q$ inductances of the state windings [H]	$x$	The state vector
$n$	Pair of poles	$y^*$	Expected output
$p$	Observer bandwidth of ESO	$y_0$	Auxiliary output in Eq.(20)
$P_m$	Mechanical power from wind [W]	$y$	Actual output
$Q(s)$	Transfer function with time delay	$z$	Observer vector of PMSG
$Q_r(s)$	Transfer function of the normal model	$\psi_f$	Magnet flux [Wb]
$R$	Blade radius [m]	$\lambda$	Tip-speed ratio
$R_s$	Resistance of stator windings [ $\Omega$ ]	$\rho$	Air density [ $\text{kg}/\text{m}^3$ ]
$S_v$	Spectral density function	$\omega$	Angular velocity of rotor [rad/s]
$T_e$	electromagnetic torque [N·m]	$\beta$	Blade pitch angle[ $^\circ$ ]

in Table 2. For fair comparisons, firstly, the control inputs of the two algorithms have the same saturation limit; secondly, each algorithm achieves good tracking performance by carefully tuning the parameters of controller. According to the principle of separation, it is very easy to obtain the parameters of feedback part ( $k_p$ ) and the observer bandwidth of the ESO ( $p$ ) via the Try and Error method. The parameters are  $K_p = 30, b = 209, p = 96$  for traditional ADRC and are  $K_p = 10, b = 209, p = 300$  for the proposed PADRC, respectively. The two control methods can both achieve excellent tracking performances.

A. THE WIND SPEED MODEL

As is discussed above, wind is the significant factor to the performance of WECS. The variations of wind speeds have the great influence on the system performance of power generator. Thus, relevant wind model, corresponding to the real wind, should be established to discuss the dynamic performance of WECS. Similar to [2], [26], [27], the wind is constructed by the linear combination of base wind, ramp wind, gust wind and noise wind in this paper. So, the wind model is defined as following Eq. (26),

$$V_N = V_b + V_g + V_r + V_n, \tag{26}$$

where  $V_b$  is the base wind speed,  $V_g$  is the gust wind speed,  $V_r$  is the ramp wind speed,  $V_n$  is the noise wind speed. And the profile of the wind speed is given in Fig.4.

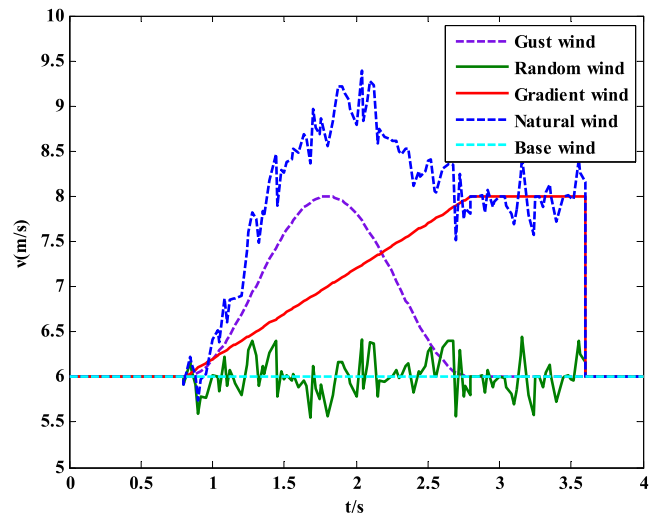


FIGURE 4. The profiles of different winds.

B. SIMULATION RESULTS AND ANALYSIS

1) CASE 1: THE BASE WIND SIMULATION

The base wind always exists in the wind energy conversion systems. Generally, the speed of base wind without change over time, can be regarded as a constant. The base wind speed is usually used to study the power of grid available from PMSG, due to the fact that it reflects the changes of mean wind speed in wind farm. The base wind-speed

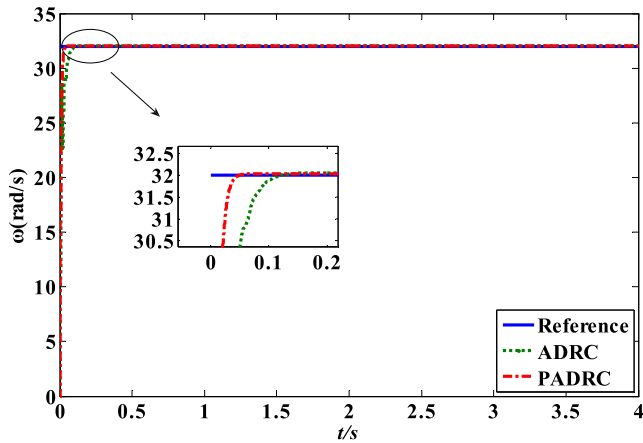


FIGURE 5. The base wind speed tracking.

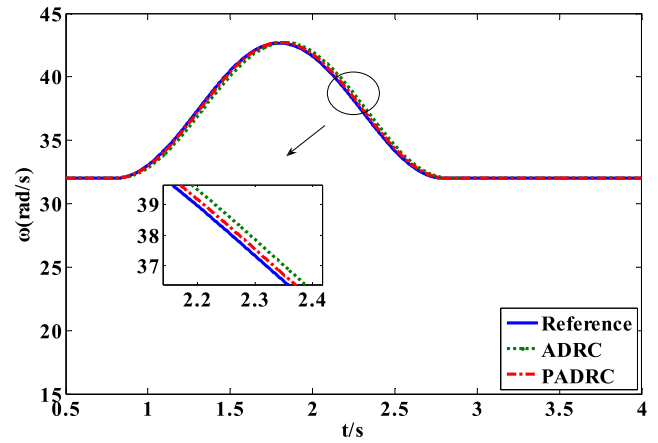


FIGURE 7. The gust wind speed tracking.

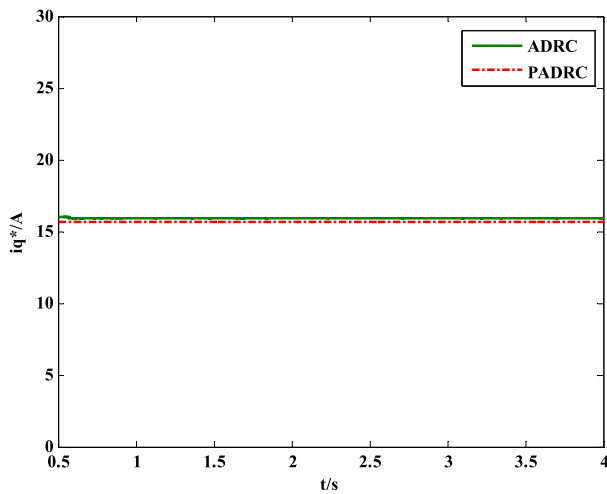


FIGURE 6. The control effects of different ADRC strategies for the base wind.

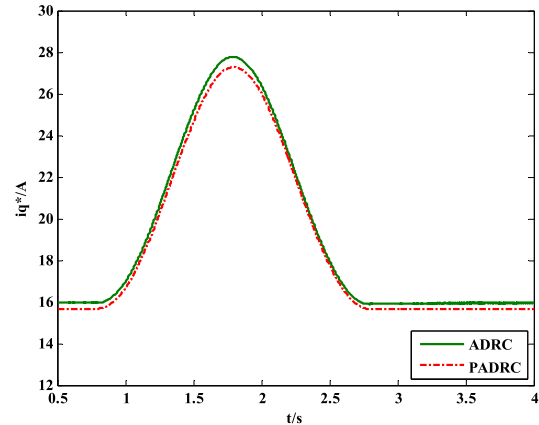


FIGURE 8. The control effects of different ADRC strategies for the gust wind.

component can be expressed by the following Eq. (27).

$$V_b = K_b, \tag{27}$$

where  $K_b$  is a constant, and the base wind speed is 6m/s.

The simulation results of speed tracking performance and the control effects of different ADRC strategies for the base wind are shown in Figs. 5 and 6.

### 2) CASE 2: THE GUST WIND SIMULATION

In order to describe the characteristic of a sudden change in wind speed, the gust wind is introduced to model the wind speed. The gust is widely used in the research of WECS, since it can provide a theoretical basis for the study of the dynamic analysis of wind energy conversion system, and the impact of PMSG on the grid voltage fluctuation. The gust specific mathematical relationship can be described as follows,

$$V_g = \begin{cases} 0, & t < t_{1g} \\ v_{\cos}, & t_{1g} < t < t_{1g} + T_g \\ 0, & t > t_{1g} + T_g, \end{cases} \tag{28}$$

where  $v_{\cos} = \frac{G_{\max}}{2} [1 - \cos 2\pi((t/T_g) - (t_{1g}/T_g))]$ , and  $V_g, v_{\cos}$  represent the gust speed. The parameter  $t_{1g}$  is the gust starting time,  $T_g$  is the gust period, and  $G_{\max}$  is the maximum value of the gust. In this case study, the gust begins at 0.8s, terminates at 2.8s, where the period is 2s, and the gust's maximum speed is 8m/s. The comparison curves of the speed tracking performances and controller outputs for the gust wind are shown in Figs. 7 and 8.

### 3) CASE 3: THE RAMP WIND SIMULATION

To describe the characteristics of a slow change in wind speed, a ramp wind is employed for the model of wind speed. In this paper, the ramp wind can be described as follows.

$$V_r = \begin{cases} 0, & t < t_{1r} \\ v_{ramp}, & t_{1r} < t < t_{2r} \\ 0, & t > t_{2r}, \end{cases} \tag{29}$$

where  $v_{ramp} = R_{\max}(1 - \frac{t-t_{2r}}{t_{1r}-t_{2r}})$ , and  $V_r, v_{ramp}$  represent the wind speed at different times. The parameters  $t_{1r}, t_{2r}$  are the starting time and terminal time respectively. The parameter  $R_{\max}$  is the maximum of ramp wind. In this example, the ramp begins at 0.8s, and terminates at 3.6s. The maximum speed of ramp is 8m/s. The comparison simulation results of the speed

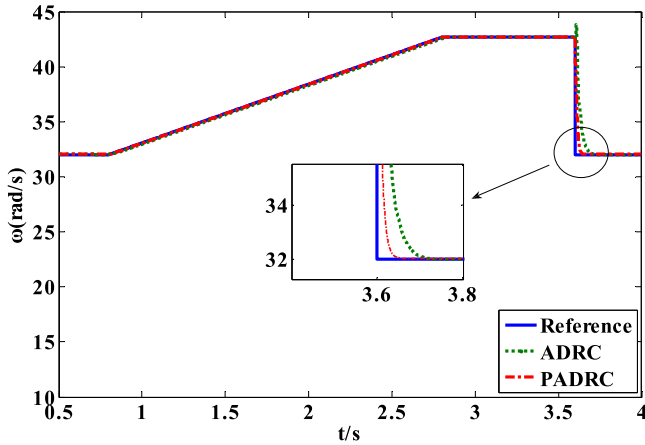


FIGURE 9. The ramp wind speed tracking.

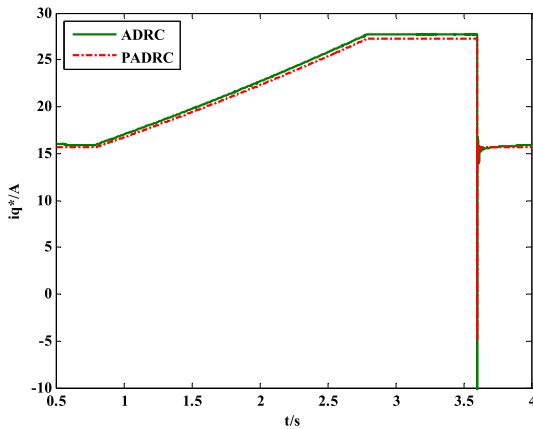


FIGURE 10. The control effects of different ADRC strategies for the ramp wind.

tracking performance and the controller output for the ramp wind are shown in Figs. 9 and 10.

4) CASE 4: THE RANDOM (STOCHASTIC) WIND SIMULATION

This kind of winds are featured with stochastic random in the relative height. The random wind is introduced in this case. The random wind speed component can be expressed by the following Eq. (30) in this paper.

$$V_N = 2 \sum_{i=1}^N \sqrt{S_V(\omega_i)\Delta\omega} \cos(\omega_i + \varphi_i), \quad (30)$$

where  $\omega_i = (1 - 1/2)\Delta\omega$  is a random variable with uniform probability density on the interval  $(0, 2\pi)$  and  $\Delta\omega = (0.5 - 2.0)$  rad/s. The parameter  $\varphi_i$  is also a random variable with uniform probability density on the interval  $(0 \sim 2\pi)$ , and the spectral density function  $S_V(\omega_i)$  with respect of  $\omega_i$  can be defined as the following Eq. (31),

$$S_V(\omega_i) = \frac{2K_N F^2 |\omega_i|}{\pi^2 [1 + (F\omega_i/\bar{v}\pi)^2]^{4/3}}, \quad (31)$$

where  $K_N$  is the surface drag coefficient,  $F$  is the turbulence scale, and  $\bar{v}$  is the mean wind speed. In this paper, it is assumed  $N = 50$ ,  $F = 2000$ ,  $K_N = 0.004$ .

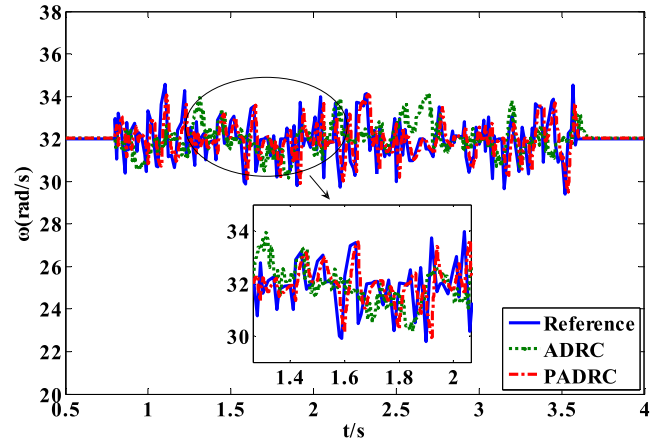


FIGURE 11. The random wind speed tracking.

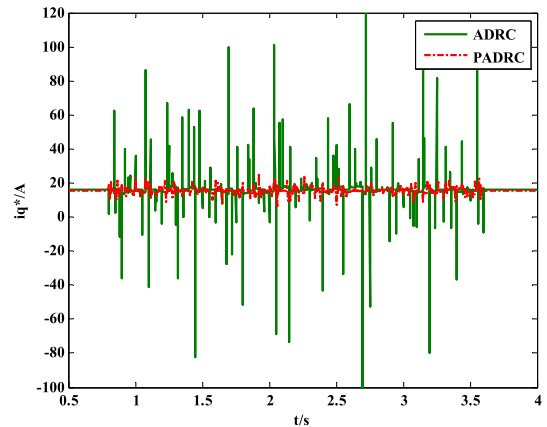


FIGURE 12. The control effects of different ADRC strategies for the random wind.

Figs. 11 and 12 describe the simulation results of the speed tracking performance and the controller output response comparison curves in the random wind. The random wind begins at 0.8s, and terminates at 3.6s in this case.

5) CASE 5: THE NATURAL WIND SIMULATION

It is well known that the natural wind is the main energy source of wind turbine, and is featured with strong mutation and randomness. Since the natural wind consists of the above four kinds of wind, it can be defined by the following Eq. (32),

$$V_N = V_b + V_g + V_{ramp} + V_n \quad (32)$$

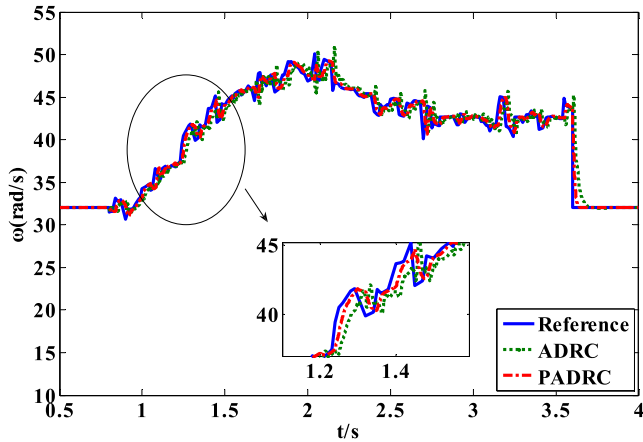
Figs. 13 and 14 show the simulation results of speed tracking performance and control output response comparison curves in the natural wind.

The integral of absolute error (IAE) performance index is employed here to estimate the control performance of tracking performance with five wind types. Values of the performance index in five cases are list in Table 3. Since the sampling frequency is 1kHz in this control system, there are 4000 data samples for each case. It can be observed that the IAE of the five wind types under the proposed PADRC scheme are much smaller than that under the traditional ADRC scheme.

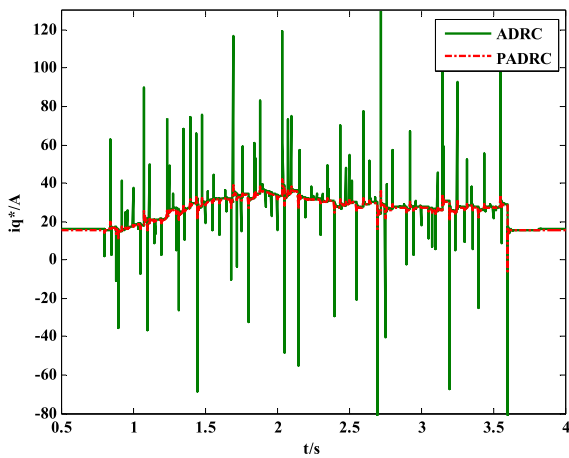


**TABLE 3.** The integral of absolute error (IAE) index for different control methods with five wind types.

IAE	Base wind		Gust wind		Ramp wind		Random wind		Natural wind	
	ADRC	PADRC	ADRC	PADRC	ADRC	PADRC	ADRC	PADRC	ADRC	PADRC
	102.1	89.2	150.3	100.7	273	162.3	620.5	261.9	828.3	323.7



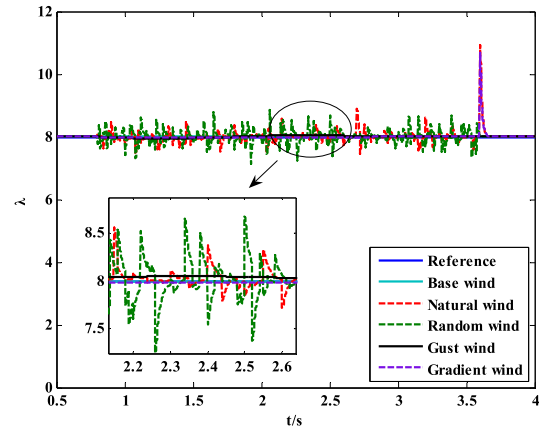
**FIGURE 13.** The natural wind speed tracking.



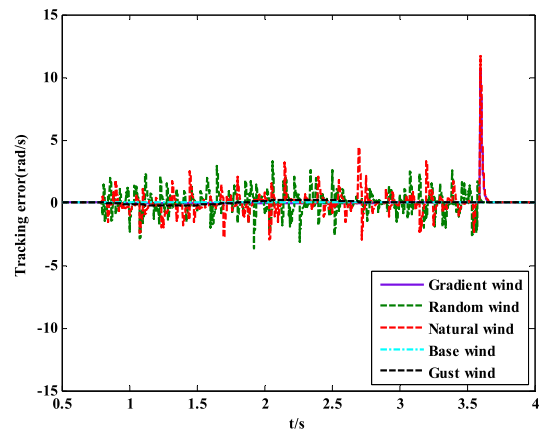
**FIGURE 14.** The control effects of different ADRC strategies for the natural wind.

It can be observed from Figs. 5, 7 and 9 that the simulation results of wind speed show very similar tracking performances between the traditional ADRC and PADRC, when the wind speed keeps constant or changes in a small scale. And from Figs. 6, 8 and 10, we can see that the control signals are nearly the same in steady-state. Since the output rotor speed and the system disturbances change relatively little in the first three cases, the time delay has little effect on the system tracking performance. And the ESO itself can estimate the disturbances and compensate them through the feedback channel.

However, as shown in Figs.11 and 13, the output rotor speed of PADRC system tracks the reference trajectory better than that of the traditional ADRC system, when the wind changes rapidly. And from Figs. 12 and 14, we can see that the absolute values of control signals of PADRC system are much smaller than that of the traditional ADRC



**FIGURE 15.** The tip-speed ratio.



**FIGURE 16.** The tracking error in different wind types.

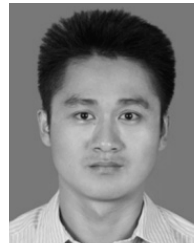
system in steady-state. In this paper, the tracking error and the tip-speed ratio of PADRC system are plotted in Figs. 15 and 16, respectively. As shown in Figs.15 and 16, the tip-speed ratio remains near the optimum value  $\lambda_{opt} = 8$ , and the tracking error is near zero, which shows good tracking performance. The system disturbances increase sharply with wind speed changing in a large scale. The ESO itself can't deal with the rapid disturbances and the effect from time delay thoroughly with the traditional ADRC, due to the existence of time delay and the disturbances. In contrast, the PADRC can well compensate the time delay and deal with disturbances, since it introduces the Smith Predictor to eliminating the effect of time delay. So the proposed PADRC show a better speed tracking performance and smaller control variable in such situations. According to these simulation results, it can be concluded that the PADRC possesses a better dynamic performance than the traditional ADRC strategy.

## V. CONCLUSION

A direct-driven PMSG variable speed WECS, as a nonlinear uncertain dynamic system, is analyzed in this paper. The ADRC strategy, which can deal with uncertainties and large scale variations under different operating conditions, is introduced to realize the maximum output power of the generator for different kinds of wind. The time delay existing in the WECS, caused by computational delay, the finite response time of the inner current loop and sensor, mechanical coupling and the transmission characteristics, can significantly degrade the maximum power point tracking performance of the WECS. To this end, a PADRC based on the Smith Predictor is further proposed to improve the control performance. Finally, the proposed PADRC is successfully validated by simulation studies. Simulation results demonstrate that the proposed control strategy can effectively deal with time delays and exhibit strong robustness against lumped disturbances.

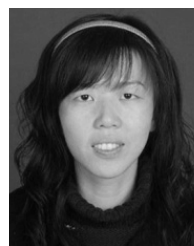
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