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# Coverage and Rate Analysis for Downlink HetNets Using Modified Reverse Frequency Allocation Scheme

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**ABSTRACT** The deployment of heterogeneous networks (HetNets) inevitably demands the design of interference management techniques to elevate the overall network performance. This paper presents a novel interference mitigation technique known as reverse frequency allocation (RFA), which provides an efficient resource allocation compared with the other state-of-the-art techniques. RFA reverses the transmission direction of interferers, thereby minimizing the cross-tier interference. Eventually, better coverage as well as increased data rates are achieved by providing complementary spectrum to the macro and pico users. In this paper, we present a tractable approach for modeling HetNets under the proposed RFA scheme. Specifically, we employ well known tools from stochastic geometry to derive closed-form expressions for the coverage probability and rate coverage in two-tier cellular network employing RFA and its variants. The modeling is performed using two approaches; first, where the base stations and users are modeled as independent Poisson point processes (PPPs) and second, the interference is approximated using the fluid model. It is shown that the results obtained from the PPP model are accurate for higher values of path loss exponents, while the results from fluid model are useful for smaller values of path loss exponents. The plausibility of model is validated through the Monte-Carlo simulations and the network performance is evaluated in terms of coverage probability, coverage rate, and outage capacity. The results demonstrate that 2-RFA yields outage capacity gains of 13% as compared with the soft fractional frequency reuse scheme, whereas, the performance gains can be further improved by 14% by employing the proposed variants of RFA.

**INDEX TERMS** 5G heterogeneous network, reverse frequency allocation, stochastic geometry, coverage probability, outage capacity.

## I. INTRODUCTION

Addressing the enormous growth of mobile traffic is one of the pivotal challenges for future wireless cellular networks. By observing the current growth trends in the traffic load, it is expected that the mobile data traffic across the globe will exponentially increase over next few years. The recent forecast in [1] shows that the data traffic is expected to increase 1000 folds by the year 2020 and by 10,000 times by 2025. Furthermore, this unprecedented demand for wireless connectivity is increasingly becoming heterogeneous due

to considerable need for connecting machines with other machines paving way for Internet-of-Things. With exponential proliferation of smart phones, augmented reality (AR) applications are gaining huge momentum, possibly rendering AR as killer application for next generation of cellular network. To summarize, the two key requirements which have emerged from various verticals for future wireless networks are low latency and higher throughput. Keeping this in mind, both academia and industry are currently working on developing fifth-generation (5G) wireless networks [2].

5G wireless networks are geared to exploit aggressive spatial reuse of spectrum to realize higher throughput via heterogeneous cellular architecture, i.e., HCNs (heterogeneous cellular networks) [3].

HCNs are efficient as well as cost effective solution for offloading the mobile users from the macro base station to small access points (SAPs). SAPs include operator and/or user deployed pico base stations (PBSs) [4], or femto BSs [5], [6], provisioned with multiple radio access technologies (multi-RAT). The BSs of various tiers included in HCNs vary in their transmit power, density, propagation characteristics (e.g., path loss exponents), deployment modes (e.g., open vs. closed, indoor vs. outdoor) [7] and supported quality of service (QoS) requirements. Therefore, user experience in terms of rate, reliability and coverage is varying as compared to the stand alone macro BS networks. The eminent advantage of SAPs is that they can be seamlessly overlaid in the existing macro cellular wireless networks whereby according to [8], the number of small base stations (SBS) would increase up to 17 million by 2017.

As the number of tiers is increased to improve the performance of the wireless network, the system has to face major technical challenges. For instance, dealing with the aggregate effect of interference from different tiers and from the cells of same tier while evaluating the signal-to-interference plus noise ratio (SINR) and throughput of the mobile users, increased complexity, self organization, back-hauling and handover etc. Hence, this stands as a necessity to consider for a pragmatic solution that not only minimizes these challenges but also provides phenomenal boost in the data rates. Interference can be reduced within the operator deployed macrocells by implementing interference management techniques such as the frequency reuse schemes, sub-carrier allocation, codebook restriction strategy to select the best channel [9], and centralization of the network. However, these techniques can be deployed in co-tier cellular network. For the intercell interference (ICI) management in HetNets, 3GPP Release 10 introduced almost blank subframes (ABS)/ based enhanced inter cell interference coordination (eICIC) which is an efficient way to increase the cell-edge area of users [10]. Reducing the power of the small cells increases the throughput of the victim macro user equipments (MUEs) [11], and efficiently defining the user association criteria also enhances the performance of HetNets [12].

A number of recent literature addressed the main issues of interference, limited resource availability and load balancing thereby, introducing the schemes that mitigate interference in heterogeneous cellular networks [13], improve capacity by using the spectrum resources efficiently [14] and by offloading the traffic towards SAPs [15], [16]. Other solutions include power control mechanism, adjusting the transmissions of both tiers in separate time frames for achieving significant gain in the data rates. To mitigate the impact of interference, we present an efficient frequency allocation scheme in a two tier network that reverses the

transmission direction of both tiers, thereby enhances the data rates of downlink users. The following subsection gives an overview of relevant literature in HetNets.

#### A. RELATED WORK AND MOTIVATION

When the users are allowed to connect to the APs of any tier, they generally connect to high powered macro base stations (MBSs) causing load disparity and under utilization of resources. On the other hand, for load balancing, MBS can offload small fraction of macro users to SAPs, however, this leads to lower SINR. Therefore, during the transmission/reception period of small cells, the time/frequency resources of the macro cells become mute [10], leading to the wastage of time/frequency resources assigned to the subscribers attached to the MBS. Moreover, for load balancing, only a limited number of users can be offloaded to the SAPs and the users connected to the SAPs do not receive optimal SINR. Therefore, it is required to apply some resource allocation algorithm along with innovative interference mitigation schemes to substantially enhance the gains of the network.

In [14], many frequency allocation schemes are discussed to minimize the impact of interference and fair resource partitioning among the users connected to macro cells and femto cells. A comprehensive survey [17], depicts many strategies to deal with the interference scenarios. In [18], buffered fractional frequency reuse (FFR) scheme for the elevation of data rates of cell edge macro user equipments (MUEs) is developed and compared with several other frequency reuse schemes. A detailed analysis of coverage probability for open and closed access modes for FFR schemes is proposed in [19]. Universal blanking pattern is introduced in [20] to provide coordination among base stations of various tiers and reducing interference by using physical resource block allocation. The performance and spectral efficiency of SAPs can be improved by utilizing antennas, selection diversity schemes and beamforming for interference management in uplink as well as in downlink [21]. A variant of shared frequency scheme is proposed in [22] that avoids the prominent source of interference from MBS by dividing the macrocell into several regions. In [23], a cross-polarized complementary frequency allocation (CPCFA) scheme in femto-macro networks is introduced to exploit the diversity in the frequency spectrum by employing the cross-polarization discrimination (XPD) property that supports the independent operations within each of the tier by utilizing different polarizations at the cost of complexity.

Motivated by the results of [22], in this work, we deploy a variant of shared frequency scheme, namely reverse frequency allocation (RFA) in a dense heterogeneous network comprising of two tiers, i.e., picocells and macrocells. We present a framework based on the stochastic geometry that analyzes the coverage of users attached to the pico BSs in a closed subscriber group (CSG). RFA scheme provides significant gains in the data rates of downlink pico user equipments (PUEs) by partitioning the cell into non-overlapping

regions and applying complementary spectrum allocation between the macrocells and picocells, i.e., the direction of radio transmissions of macrocells is reversed and allocated to the picocells that are in the other spatially separated area. Hence, there is a prominent reduction in the number of interfering entities in each region of a macro cell, whereas the detrimental impact of MBS interference is completely avoided.

**B. CONTRIBUTIONS**

The main contributions of this paper are four fold:

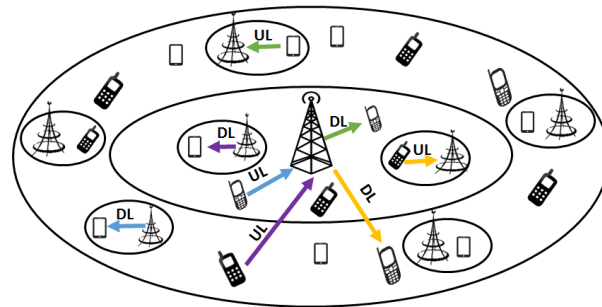
- We provide a detailed description of RFA schemes in terms of bandwidth allocation and interference mitigation. In addition, we devise a hybrid RFA scheme that takes advantage of prominent aspects (higher bandwidth and minimized interference) of existing RFA schemes.
- Utilizing stochastic geometry, we derive the analytical expressions of coverage probability and rate coverage for various RFA schemes. Our analysis assumes that there is no cross-tier interference from other macro cells and prove that the proposed modified RFA scheme is the optimal scheme among other RFA schemes.
- Mathematical modeling is performed using two different approaches; in the first approach, the location of the interferers is modeled as independent PPPs, best suitable for higher values of pathloss exponent. Whereas, in the second approach, the expected value of the cumulative interference is calculated using fluid model.
- Analysis of proposed scheme for multiple cells is involved, however, with the help of simulations, the network performance is evaluated in terms of average outage probability and outage capacity, a quantity that provides favorable throughput fairness. The plausibility of model is also verified through simulations and it has been observed that the proposed modified scheme excels in terms of data rates and enhanced capacity as compared to the baseline RFA and SFR scheme.

**C. ORGANIZATION**

The organization of this paper is as follows. Section II presents the sub-carrier allocation in general RFA setting. Section III provides the mathematical modeling of RFA scheme based on the above mentioned two approaches. Closed-form expressions of coverage probability for modified RFA scheme are derived in Section IV. Section V gives insight of the network performance when RFA scheme is implemented in multi-cellular network. Simulation results and discussion are described in Section VI. The conclusion and future work is provided in Section VII.

**II. SUB-CARRIER ALLOCATION IN RFA SCHEME**

Like other FFR schemes, a conventional 2-RFA scheme [24] divides the coverage area of each macrocell into two regions, i.e., an interior region and an exterior region [25]. However, distinguished attribute in this scheme is the reversal of transmission directions of the two tiers to achieve minimal



**FIGURE 1.** Illustration of 2-RFA in a single cell with two-tier network. (The signaling colors are conversant with the spectrum colors in the Table I).

**TABLE 1.** Frequency partitioning in 2-RFA scheme.

B <sub>1</sub>		B <sub>2</sub>	
Inner UL Picocell	Inner DL Picocell	Outer UL Picocell	Outer DL Picocell
B <sub>1y</sub>	B <sub>1z</sub>	B <sub>2y</sub>	B <sub>2z</sub>
Outer DL Macrocell	Outer UL Macrocell	Inner DL Macrocell	Inner UL Macrocell

interference and maximum gain for the downlink (DL) users. Furthermore, frequency division duplexing (FDD) scheme is considered, where the traffic in this study is assumed to be symmetrical and equal bandwidth,  $b_{ul}$  is allocated for the uplink transmission and downlink  $b_{dl}$  channels, i.e.,  $B = b_{dl} \cup b_{ul}$ , where  $B$  is the available bandwidth. Additionally, there exist no interference between UL and DL traffic of the same tier. Taking advantage of this aspect, we distribute the pico and macro users such that if the pico user equipments (PUEs) connected to the PBSs of inner region of macrocell are at DL, the macro user equipments (MUEs) of outer region utilizing the same frequency band are at UL and vice versa. Therefore, the cross-tier interference is minimized. In a similar manner, the PUEs of outer region while receiving transmission from the tagged PBSs, encounter cross-tier interference from the inner region uplink MUEs. The detailed interference scenario for the users of both tiers is elaborated in Fig. 1 and bandwidth allocation among the users of inner and outer regions connected to PBSs and MBS is shown in Table I, respectively.

Although 2-RFA provides significant gains in terms of coverage probability and throughput values as compared to other FFR schemes [23], the level of interference could be further minimized. Partitioning the macro-cell into further non-overlapping regions of equal area is an ingenious means to attain higher SINR. In this way, the subscribers utilizing the same spectrum, are spaced further apart, thereby the level of interference is reduced. Dividing the cell into multiple  $w$  non-overlapping logical regions, we have  $w = 2^l$ , where  $l \in \mathbb{N}^+$  and  $\mathbb{N}^+ = \{1, 2, \dots\}$ . Hence, the macrocell can be partitioned up to  $w$  non-overlapping regions to attain a  $w$ -RFA scheme. The number of co-channel users, i.e., the users which

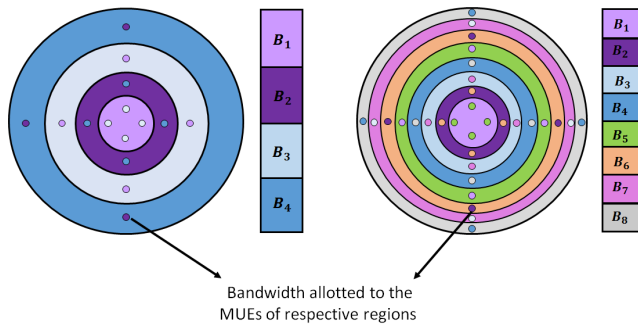


FIGURE 2. Bandwidth allocation in multi region RFA (4-RFA and 8-RFA).

are assigned the same spectrum, is reduced and they are now distributed in the far apart regions within the same cell. Therefore, the probability of interference from the adjacent regions is minimized. For instance, partitioning the macrocell into four regions to devise a 4-RFA scheme, the provided spectrum is now divided into four sub-bands and the PUEs of region  $R_1$  receive co-tier interference from the same region and cross-tier interference from a distant region  $R_3$  as shown in Fig. 2. The increased path loss between the intended user and the interferers eventually provides better SINR. Likewise, the downlink transmission of  $R_2$  PUEs is being interfered by the PBSs of same region and from the uplink MUEs located in  $R_4$ . Similarly,  $R_3$  PUEs receive interference from PBSs situated in  $R_3$  and from MUEs in  $R_1$ . In order to attain better SINR of the downlink users, we can further partition the macrocell into 8 regions, whereby the distance between the interferers is further increased, i.e.,  $R_1$  PUEs now receive cross-tier interference from  $R_5$  UL MUEs,  $R_2$  PUEs from  $R_6$  UL MUEs and so on. The detailed bandwidth allocation among the users of 4-RFA and 8-RFA is given in Fig. 2. The resulting SINR expression of a DL PUE connected to the PBS in any region is expressed as

$$SINR = \frac{P_p h_i |x_i|^{-\beta_2}}{\sum_{q=1, q \neq i}^{\Psi} P_p h_q |x_q|^{-\beta_2} + \sum_{m=1}^{\Omega} P_m h_m |x_m|^{-\beta_1} + \sigma^2}, \tag{1}$$

where  $P_p$  and  $P_m$  are the transmission powers of PBSs and MUEs, respectively and  $h_i \sim \exp(1)$  is independently and identically distributed (i.i.d) exponential fading gain with unit mean. The path loss function is expressed as  $|x_i|^{-\beta_2}$ , where  $x_i$  is the distance between the intended PUE and the serving PBS,  $\beta_2$  is the path loss exponent for the pico tier and  $\beta_1$  for the macro tier. The denominator of (1) represents the interference that PUE experiences from all the DL PBSs  $\Psi$  located in the same region other than the serving PBS and from the UL MUEs  $\Omega$  in other region exploiting same bandwidth spectrum, respectively, while noise power is expressed as  $\sigma^2$ .

Although, a higher region RFA provides less interference, however, as we opt for these RFA schemes, the division of cell causes partitioning of spectrum into orthogonal bands as

well [26]. Hence, the more we partition the cell, a smaller spectrum is available for the users of higher region RFA. While considering this degradation and requirement of downlink users, in terms of substantial rates, partitioning the cell overwhelmingly is not an attractive solution. Keeping the above in view, we devise a hybrid scheme by merging the 2-RFA and 4-RFA schemes such that the benefits of both schemes in terms of higher sum capacity and vulnerability to interference are achieved, respectively. Combination of other RFA schemes can also be assumed, however, it is shown in Section VI that the optimal rates are achieved by deploying a modified version of 4-RFA, which we call as modified 4-RFA or M-4-RFA scheme. In M-4-RFA scheme, the macrocell is divided into four regions similar to conventional 4-RFA scheme, however, frequency sub-carriers are allocated just like 2-RFA, such that PUEs of each region now receive co-tier as well as cross-tier interference from two regions rather than just a single region. For instance, a PUE located in  $R_1$  receives co-tier interference from  $R_1$  downlink PBSs and from PBSs of  $R_3$ , likewise it receives cross-tier interference from uplink MUEs located in  $R_2$  and  $R_4$ , respectively. The benefit of this scheme is that although the amount of interference increases as compared to 4-RFA, however, bandwidth division is small. Consequently, appreciable increase in the data rates is achieved.

### III. MATHEMATICAL MODELING OF 2-RFA SCHEME

In this section, we present analytical expressions for the coverage probabilities of DL PUEs in a heterogeneous two tier cellular network, i.e., pico cells are overlaid with macro cellular network. To calculate the coverage of the networks, it is considered that a conventional hexagonal grid model provides an upper bound on coverage, i.e., the deployment of BSs having deterministic cell boundaries is a widely used approach for simulations but too idealistic for practical scenarios. Therefore, in [27], it is stated that a PPP distribution could be used that helps in the modeling of these networks through stochastic geometry. In such models, the BSs have cell boundaries corresponding to Voronoi tessellations where the BSs locations are modeled by a PPP of finite intensity. Recently, in [28] it is explained that by assuming BS coverage area as Voronoi tessellations, accuracy in the modeling of coverage probability is achieved for higher values of path loss exponent, i.e., 4 or higher, whereas for smaller values of path loss exponent, e.g., 2.5, the performance of model is not matched accurately.

Therefore, to provide the tractable coverage probability expressions for a vast variety of parameters, we perform the modeling of the network using two approaches; in the first approach, the PBSs are spatially modeled as a PPP, and interference is calculated through Laplace transform. Whereas in the second approach, the expected value of interference is calculated using the fluid model [29], where the distribution of users and BSs is assumed to be uniformly random and results are valid even for smaller values of path loss exponent.

**A. COVERAGE PROBABILITY ANALYSIS  
CONSIDERING PPP**

As mentioned earlier, a closed access mode is considered, i.e., each user is connected to the closest BS of a particular tier. For a 2-RFA scheme, we divide the macro cell into 2 regions of equal area. The distribution of PBSs and MUEs in each region is considered as independent PPPs,  $\Phi_j^{(v)}$  of intensity  $\lambda_j^{(v)}$  and  $\Phi_k^{(v)}$  of intensity  $\lambda_k^{(v)}$ , respectively, where  $v$  denotes the regions of macrocell, i.e,  $v \in \{1, 2\}$  for 2-RFA. Each user is served by at most one pico BS with transmit power  $P_p$  and the user can communicate with the tagged BS if the resulting SINR is greater than a pre-defined threshold  $\tau$ . Without loss of generality, it is assumed that the user is at the origin. Hence, the received power at the user from a PBS located at distance  $x_i^{(1)}$  is given as  $P_p h_i^{(1)} ||x_i^{(1)}||^{-\beta_2}$ . As far as interference is concerned, a worst case scenario is assumed in which all the PBSs and MUEs that utilize the same spectrum are transmitting, therefore a user experiences interference from all the interfering entities. The generalized expression of SINR for a downlink pico user located in the inner region  $R_1$  of macro cell connected to its PBS of same region is expressed as

$$SINR_x^{(1)} = \frac{P_p h_i^{(1)} ||x_i^{(1)}||^{-\beta_2}}{I_{pbs} + I_{mue} + \sigma^2}, \quad (2)$$

where  $I_{pbs}$  is the interference from the downlink PBSs located in  $R_1$  and  $I_{mue}$  represents the interference active form all the transmitting uplink MUEs from region  $R_2$ , respectively. Both interfering entities,  $I_{pbs}$  and  $I_{mue}$  are expressed as

$$I_{pbs} = \sum_{\substack{x_j^{(1)} \in \Phi_j^{(1)} \\ x_j^{(1)} \neq x_i^{(1)}}} P_p h_j^{(1)} ||x_j^{(1)}||^{-\beta_2},$$

$$I_{mue} = \sum_{x_k^{(2)} \in \Phi_k^{(2)}} P_m h_k^{(2)} ||x_k^{(2)}||^{-\beta_1}.$$

**1) DISTANCE TO THE CLOSEST PICO BASE STATION**

Since, each user connects with the closest pico base station, no other base station can be closer than  $x_i^{(1)}$ , in other words all the other PBSs are at least at the distance  $\chi$  from the user. For the sake of simplicity, we drop the subscript  $i$  and represent the distance between the serving PBS and PUE as  $x^{(1)}$ . Then probability density function (PDF) of  $x^{(1)}$  can be formulated by utilizing the fact that the null probability, i.e.,

$$\mathbb{P}[x^{(1)} > \chi] = e^{-\lambda_j^{(1)} \pi \chi^2}.$$

Therefore, the cumulative distribution function (CDF) is

$$\mathbb{P}[x^{(1)} \leq \chi] = 1 - e^{-\lambda_j^{(1)} \pi \chi^2}.$$

The PDF then becomes

$$f(x^{(1)}) = \frac{dF(x^{(1)})}{dx^{(1)}} = 2\pi \lambda_j^{(1)} x^{(1)} e^{-\pi \lambda_j^{(1)} x^{(1)2}}.$$

**2) COVERAGE PROBABILITY**

Given the SINR threshold and path loss exponent, the coverage probability is expressed as

$$P_c^{(1)}(\tau) = \int_{x^{(1)} > 0} \mathbb{E}_{I_x^{(1)}} \left[ \mathbb{P}[SINR_x^{(1)} > \tau] \right] f(x^{(1)}) dx^{(1)}, \quad (3)$$

$$= \int_{x^{(1)} > 0} \mathbb{E}_{I_x^{(1)}} \left[ \mathbb{P} \left( h > \tau (P_p)^{-1} x^{(1)\beta_2} (I_x^{(1)} + \sigma^2) \right) \right] \times 2\pi \lambda_j^{(1)} x^{(1)} e^{-\pi \lambda_j^{(1)} x^{(1)2}} dx^{(1)}. \quad (4)$$

The inner expectation in (4) can be further simplified as

$$\mathbb{E}_{I_x^{(1)}} \left[ \mathbb{P} \left( h > \tau (P_p)^{-1} x^{(1)\beta_2} (I_{pbs} + I_{mue} + \sigma^2) \right) \right] = \exp \left( \frac{-\tau \sigma^2}{P_p x^{(1)-\beta_2}} \right) \mathbb{E}_{I_x^{(1)}} \left( e^{-\frac{\tau (I_{pbs} + I_{mue})}{P_p x^{(1)-\beta_2}}} \right). \quad (5)$$

By putting the value of expectation obtained in (5) back into (4), the coverage probability is given as

$$P_c^{(1)}(\tau) = 2\pi \lambda_j^{(1)} \int_{\mathbb{R}^2} \mathcal{L}_{I_{pbs}}(s) \mathcal{L}_{I_{mue}}(s) e^{-\frac{\tau \sigma^2}{P_p x^{(1)-\beta_2}}} \times e^{-\pi \lambda_j^{(1)} x^{(1)2}} x^{(1)} dx^{(1)}, \quad (6)$$

where  $\mathcal{L}_{I_{pbs}}(\cdot)$  and  $\mathcal{L}_{I_{mue}}(\cdot)$  are the Laplace transforms of interference from the DL PBSs and UL MUEs from the respective regions and are given as

$$\mathcal{L}_{I_{pbs}}(s) = \exp \left( -\pi \lambda_j^{(1)} (s P_p)^{2/\beta_2} C_2^{(1)} \right), \quad (7)$$

$$\mathcal{L}_{I_{mue}}(s) = \exp \left( -\pi \lambda_k^{(2)} (s P_m)^{2/\beta_1} C_1^{(2)} \right). \quad (8)$$

The proof for (7) and (8) are given in Appendices A and B, respectively.

*Theorem 1:* The probability of coverage of a DL PUE located at origin in  $R_1$  is given as

$$P_c^{(1)}(\tau) = \pi \lambda_j^{(1)} \int_0^{R_1^2} \exp \left( -\pi v^{(1)} \lambda_j^{(1)} - \pi v^{(1)} \lambda_j^{(1)} \tau^{2/\beta_2} C_2^{(1)} - \pi v^{(1)\beta_2/\beta_1} \lambda_k^{(2)} \left( \frac{\tau P_m}{P_p} \right)^{2/\beta_1} C_1^{(2)} - \left( \frac{\tau \sigma^2}{P_p} v^{(1)\beta_2/2} \right) \right) dv^{(1)}, \quad (9)$$

where  $C_2^{(1)} = \int_{\tau^{-(2/\beta_2)}(R_1/x^{(1)})^2}^{\tau^{-(2/\beta_2)}} \left( \frac{1}{1+(u^{(1)\beta_2/2})} \right) du^{(1)}$  and  $C_1^{(2)} = \int_{\left( \frac{\tau P_m}{P_p x^{(1)-\beta_2}} \right)^{-2/\beta_1} (R_2)^2}^{\left( \frac{\tau P_m}{P_p x^{(1)-\beta_2}} \right)^{-2/\beta_1} (R_1)^2} \left( \frac{1}{1+(w^{(2)\beta_1/2})} \right) dw^{(2)}$ .

*Proof:* The final expression for the coverage probability is obtained by plugging the values of Laplace transforms of interferences from the DL PBSs (7) and from UL MUEs (8) into (6) and simplifying, with a final substitution of  $v^{(1)} = x^{(1)2}$ . Following the same procedure, the coverage

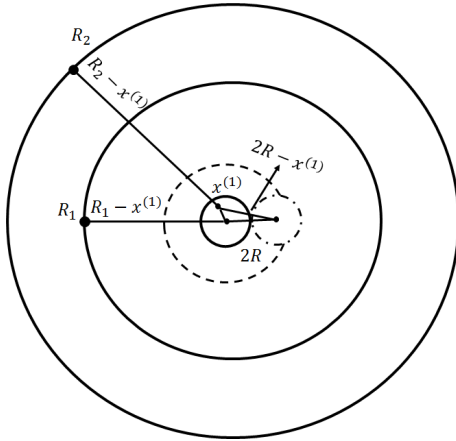


FIGURE 3. Integration limits for cumulative interference computation.

probability of DL PUE located in  $R_2$  can be derived and the final expression is given as

$$P_c^{(2)}(\tau) = \pi \lambda_j^{(2)} \int_0^{R_2^2} \exp\left(-\pi v^{(2)} \lambda_j^{(2)} - \pi v^{(2)} \lambda_j^{(2)} \tau^{2/\beta_2} C_2^{(2)} - \pi v^{(2)\beta_2/\beta_1} \lambda_k^{(1)} \left(\frac{\tau P_m}{P_p}\right)^{2/\beta_1} C_1^{(1)} - \left(\frac{\tau \sigma^2}{P_p} v^{(2)\beta_2/2}\right)\right) dv^{(2)}, \quad (10)$$

where  $C_2^{(2)} = \int_{\tau^{-(2/\beta_2)}(R_2/x^{(2)})^2}^{\tau^{-(2/\beta_2)}(R_1/x^{(2)})^2} \left(\frac{1}{1+(u^{(2)\beta_2/2})}\right) du^{(2)}$  and  $C_1^{(1)} = \left(\frac{\tau P_m}{P_p x^{(2)-\beta_2}}\right)^{-2/\beta_1} (R_1)^2 \int_{\left(\frac{\tau P_m}{P_p x^{(2)-\beta_2}}\right)^{-2/\beta_1} (x^{(1)})^2}^{\left(\frac{1}{1+(w^{(1)\beta_1/2})}\right)} dw^{(1)}$ .

**B. COVERAGE PROBABILITY ANALYSIS USING FLUID MODEL**

The coverage probability modeling for smaller path loss exponent values can be performed using the fluid model [29]. In this approach, we approximate the average value of interference, by replacing the interfering entities by an equivalent continuum of transmitters, assuming that the PBSs and MUEs are uniformly distributed in the network. Hence, network can be characterize by the PUE density  $\rho_{PUE}^{(v)}$ , PBSs density  $\rho_j^{(v)}$ , and MUE density  $\rho_k^{(v)}$ , respectively. The basic concept of this approach is illustrated in Fig. 3, where the network boundary is assumed to be circular having a radius  $R_2$ , i.e, outer region of 2-RFA. The serving PBS is located at the origin, having a circular coverage area of radius  $R$ . The PUE is situated at a distance  $x^{(1)}$  within the coverage area of that PBS. The cumulative interference from both tiers is calculated by dividing the network into rings as explained in the following section.

**1) APPROXIMATE CUMULATIVE INTERFERENCE CALCULATION**

The interference from the PBSs having density  $\rho_j^{(1)}$  to the intended PUE in the elementary surface  $rdrd\theta$  is given as

$\rho_j^{(1)} r dr d\theta$ , whereas from MUEs having density  $\rho_k^{(2)}$  to the PUE is depicted as  $\rho_k^{(2)} r dr d\theta$ . Hence, the contribution of co-tier as well as cross-tier interference is  $P_p h_j^{(1)} r^{-\beta_2} \rho_j^{(1)} r dr d\theta$  and  $P_m h_k^{(2)} r^{-\beta_1} \rho_k^{(2)} r dr d\theta$ , respectively. From Fig. 3, it is evident that the distance between the two neighboring PBSs is  $2R$ , where coverage radius  $R \propto \sqrt{\mathbb{E}[Area]}$ . Therefore, the distance between the PUE to the closest interfering PBS is taken as  $2R - x^{(1)}$ . Extending the same concept, the integration surface for the PBSs is approximated with a ring having an inner radius  $2R - x^{(1)}$  and outer radius  $R_1 - x^{(1)}$ . In the similar way, the interference from MUEs is approximated from  $R_1 - x^{(1)}$  to  $R_2 - x^{(1)}$ . Thus, the interference expression can be given as

$$I(x^{(1)}) = \int_0^{2\pi} \int_{2R-x^{(1)}}^{R_1-x^{(1)}} \rho_j^{(1)} P_p h_j^{(1)} r^{-\beta_2} r dr d\theta + \int_0^{2\pi} \int_{R_1-x^{(1)}}^{R_2-x^{(1)}} \rho_k^{(2)} P_m h_k^{(2)} r^{-\beta_1} r dr d\theta \quad (11)$$

$$= \frac{2\pi \rho_j^{(1)} P_p h_j^{(1)}}{\beta_2 - 2} \left[ (2R - x^{(1)})^{(2-\beta_2)} - (R_1 - x^{(1)})^{(2-\beta_2)} \right] + \frac{2\pi \rho_k^{(2)} P_m h_k^{(2)}}{\beta_1 - 2} \left[ (R_1 - x^{(1)})^{(2-\beta_1)} - (R_2 - x^{(1)})^{(2-\beta_1)} \right], \quad (12)$$

where  $R$  is the radius of serving PBS,  $R_1$  and  $R_2$  are the radii of inner and outer regions of macrocell, respectively. Eventually, the average value of the cumulative interference can be computed as

$$\mathbb{E}[I_x^{(1)}] = \frac{2\pi \rho_j^{(1)} P_p}{\beta_2 - 2} \left[ (2R - x^{(1)})^{(2-\beta_2)} - (R_1 - x^{(1)})^{(2-\beta_2)} \right] + \frac{2\pi \rho_k^{(2)} P_m}{\beta_1 - 2} \left[ (R_1 - x^{(1)})^{(2-\beta_1)} - (R_2 - x^{(1)})^{(2-\beta_1)} \right]. \quad (13)$$

**2) COVERAGE PROBABILITY**

The expression for the coverage probability is achieved by assuming the uniform distribution of interferers, distributed over the circular regions of equal area, where the resulting CDF is given as

$$\mathbb{P}[x^{(1)} \leq \chi] = \frac{\chi^2}{\zeta_f^2} \rho, \quad 0 \leq \chi \leq R$$

where  $\rho$  represents the combined density of the interfering entities in both the regions and  $\zeta_f^2$  is the empirically calculated value actin as a normalizing factor. The value of this factor depends upon the shape of the coverage area of BS [28]. Thus, the PDF is expressed as

$$f(x^{(1)}) = \frac{2x^{(1)}}{\zeta_f^2} \rho, \quad 0 \leq x^{(1)} \leq R.$$

*Theorem 2 (Approximate Coverage Probability Using Fluid Model):* The lower bound for the coverage probability

$P_c^{(1)}(\tau)$  of a randomly chosen DL subscriber connected to PBS located in  $R_1$  is given as

$$P_c^{(1)}(\tau) = \frac{\rho}{\zeta_f^2} \int_0^{R^2} \exp\left(-\tau v^{(1)\beta_2/2} \gamma^{(1)}(\beta, v^{(1)})\right) dv^{(1)}. \quad (14)$$

*Proof:*

$$P_c^{(1)}(\tau) = \mathbb{E}_x^{(1)} \left[ \mathbb{E}_{I_x^{(1)}} \mathbb{P}\left(\text{SINR}_x^{(1)} > \tau\right) \right], \quad (15)$$

$$P_c^{(1)}(\tau) = \frac{\rho}{\zeta_f^2} \int_0^R \mathbb{E}_{I_x^{(1)}} \left[ \mathbb{P}\left(h > \tau P_p^{-1} x^{(1)\beta_2} (\sigma^2 + I_x^{(1)})\right) \right] \times 2x^{(1)} dx^{(1)}. \quad (16)$$

Expected value of inner probability can be further simplified as

$$\begin{aligned} & \mathbb{E}_{I_x^{(1)}} \left[ \mathbb{P}[h > \tau P_p^{-1} x^{(1)\beta_2} (\sigma^2 + I_{pbs} + I_{mue})] \right] \\ &= e^{(-\tau P_p^{-1} x^{(1)\beta_2} \sigma^2)} \mathbb{E}_{I_x^{(1)}} \left[ \exp\left(-P_p^{-1} \tau x^{(1)\beta_2} (I_{pbs} + I_{mue})\right) \right]. \end{aligned} \quad (17)$$

Using Jensen's inequality, we have

$$\mathbb{E}_{I_x^{(1)}} \left[ \exp\left(-\tau P_p^{-1} x^{(1)\beta_2} I_x^{(1)}\right) \right] \geq \exp\left(-\tau P_p^{-1} x^{(1)\beta_2} \mathbb{E}[I_x^{(1)}]\right). \quad (18)$$

By replacing the expected value of interference obtained from (13) in (18), we get

$$\mathbb{E}_{I_x^{(1)}} \left[ \exp\left(-\tau P_p^{-1} x^{(1)\beta_2} I_x^{(1)}\right) \right] \geq \exp\left(-\tau x^{(1)\beta_2} \gamma^{(1)}(\beta, v^{(1)})\right), \quad (19)$$

where

$$\gamma^{(1)}(\beta, v^{(1)}) = \frac{\sigma^2}{P_p} + \frac{2\pi\rho_j^{(1)}}{\beta_2 - 2} \alpha^{(1)} + \frac{2\pi\rho_k^{(2)} P_m}{P_p(\beta_1 - 2)} \mu^{(2)}. \quad (20)$$

In (20),  $\alpha^{(1)} = [(2R - v^{(1)1/2})^{(2-\beta_2)} - (R_1 - v^{(1)1/2})^{(2-\beta_2)}]$  and  $\mu^{(2)} = [(R_1 - v^{(1)1/2})^{(2-\beta_1)} - (R_2 - v^{(1)1/2})^{(2-\beta_1)}]$ , respectively. By substituting  $x^{(1)2} = v^{(1)}$  and by putting the value of  $\exp\left(-\tau x^{(1)\beta_2} \gamma^{(1)}(\beta, v^{(1)})\right)$  into (16), we get the final expression of coverage probability with interferers having uniformly distribution over the respective regions and which completes the proof. ■

Following the similar procedure, the coverage probability of PUE located in  $R_2$  can be derived. The final expression is given as

$$P_c^{(2)}(\tau) = \frac{\rho}{\zeta_f^2} \int_0^{R^2} \exp\left(-\tau v^{(2)\beta_2/2} \gamma^{(2)}(\beta, v^{(2)})\right) dv^{(2)}, \quad (21)$$

where

$$\gamma^{(2)}(\beta, v^{(2)}) = \frac{\sigma^2}{P_p} + \frac{2\pi\rho_k^{(1)} P_m}{P_p(\beta_1 - 2)} \alpha^{(2)} + \frac{2\pi\rho_j^{(2)}}{\beta_2 - 2} \mu^{(1)}, \quad (22)$$

where  $\alpha^{(2)} = [(2R - v^{(2)1/2})^{(2-\beta_1)} - (2R + R_1 - v^{(2)1/2})^{(2-\beta_1)}]$ , and  $\mu^{(1)} = [(R_1 - v^{(2)1/2})^{(2-\beta_2)} - (2R + R_2 - v^{(2)1/2})^{(2-\beta_2)}]$ , respectively.

*Remarks:* Now that we have derived the analytical coverage probability expressions for the 2-RFA, the similar procedure is followed for the higher region RFA schemes. As DL PUEs in any region receive co-tier as well as cross-tier interference only from one region. Therefore, the aforementioned analysis can be extended easily. In the subsequent section, we provide the expressions for M-4-RFA and explain the modification that occurs in the network while implementing this scheme.

#### IV. COVERAGE PROBABILITY ANALYSIS OF M-4-RFA

Division of a macrocell reduces the number of interfering entities that utilize the same spectrum. Thus, the outage probability is minimized, in addition throughput of the DL PUEs also alleviates. Therefore, we opt for a moderate option in which we divide the macrocell into 4 regions. In this scheme, the impact of interference is increased as compared to the corresponding 4 region RFA scheme, however, the users are provided with the higher data rates, as bandwidth division is similar to 2-RFA. The SINR expression for a DL PUE located in  $R_1$  in M-4-RFA is given as

$$\text{SINR}_x^{(1)} = \frac{P_p h_i^{(1)} \|x_i^{(1)}\|^{-\beta_2}}{I_{pbs} + I_{mue} + \sigma^2}, \quad (23)$$

where  $I_{pbs}$  is the interference from the downlink PBSs located in  $R_1$  and  $R_3$ , and  $I_{mue}$  represents the interference arriving from all the transmitting uplink MUEs from region  $R_2$  and  $R_4$ , respectively.  $I_{pbs}$  and  $I_{mue}$  are expressed as

$$\begin{aligned} I_{pbs} &= \sum_{\substack{x_j^{(1)} \in \Phi_j^{(1)} \\ x_j^{(1)} \neq x_i^{(1)}}} P_p h_j^{(1)} \|x_j^{(1)}\|^{-\beta_2} + \sum_{x_l^{(3)} \in \Phi_l^{(3)}} P_p h_l^{(3)} \|x_l^{(3)}\|^{-\beta_2}, \\ I_{mue} &= \sum_{x_k^{(2)} \in \Phi_k^{(2)}} P_m h_k^{(2)} \|x_k^{(2)}\|^{-\beta_1} + \sum_{x_n^{(4)} \in \Phi_n^{(4)}} P_m h_n^{(4)} \|x_n^{(4)}\|^{-\beta_1}, \end{aligned}$$

where  $\Phi_j^{(1)}$  and  $\Phi_l^{(3)}$  represent the independent PPPs of PBSs in  $R_1$  and  $R_3$ , respectively, and  $\Phi_k^{(2)}$ ,  $\Phi_n^{(4)}$  are that of UL MUEs in  $R_2$  and  $R_4$ , respectively.

#### A. COVERAGE PROBABILITY OF M-4-RFA USING PPP

The analytical expression for the coverage probability can be derived using the similar procedure as above, however, for the interference calculation the Laplace transforms now include additional terms. The final expression of PUE located in  $R_1$  can be expressed as

$$\begin{aligned} P_c^{(1)}(\tau) &= \pi \lambda_j^{(1)} \int_0^{R_1^2} \exp\left(-\pi v^{(1)} \lambda_j^{(1)} - \pi v^{(1)} \lambda_j^{(1)} \tau^{2/\beta_2} C_2^{(1)}\right. \\ &\quad \left.- \pi v^{(1)\beta_2/\beta_1} \lambda_k^{(2)} \left(\frac{\tau P_m}{P_p}\right)^{2/\beta_1} C_1^{(2)} - \pi v^{(1)} \lambda_l^{(3)} \tau^{2/\beta_2} C_2^{(3)}\right. \\ &\quad \left.- \pi v^{(1)\beta_2/\beta_1} \lambda_n^{(4)} \left(\frac{\tau P_m}{P_p}\right)^{2/\beta_1} C_1^{(4)} - \left(\frac{\tau \sigma^2}{P_p} v^{(1)\beta_2/2}\right)\right) dv^{(1)}, \end{aligned} \quad (24)$$

where

$$\begin{aligned}
 C_2^{(1)} &= \int_{\tau^{-(2/\beta_2)}}^{\tau^{-(2/\beta_2)}(R_1/x^{(1)})^2} \left( \frac{1}{1 + (u^{(1)\beta_2/2})} \right) du^{(1)}, \\
 C_2^{(3)} &= \int_{\tau^{-(2/\beta_2)}(R_2/x^{(1)})^2}^{\tau^{-(2/\beta_2)}(R_3/x^{(1)})^2} \left( \frac{1}{1 + (u^{(3)\beta_2/2})} \right) du^{(3)}, \\
 C_1^{(2)} &= \int_{\left(\frac{\tau P_{m_x^{(1)\beta_2}}}{P_p}\right)^{-2/\beta_1}}^{\left(\frac{\tau P_{m_x^{(1)\beta_2}}}{P_p}\right)^{-2/\beta_1}} \frac{(R_2)^2}{(R_1)^2} \left( \frac{1}{1 + (w^{(2)\beta_1/2})} \right) dw^{(2)}, \text{ and} \\
 C_1^{(4)} &= \int_{\left(\frac{\tau P_{m_x^{(1)\beta_2}}}{P_p}\right)^{-2/\beta_1}}^{\left(\frac{\tau P_{m_x^{(1)\beta_2}}}{P_p}\right)^{-2/\beta_1}} \frac{(R_4)^2}{(R_3)^2} \left( \frac{1}{1 + (w^{(4)\beta_1/2})} \right) dw^{(4)}.
 \end{aligned}$$

Whereas the coverage probability expressions for the pico users located in  $R_2$ ,  $R_3$ , and  $R_4$  regions are given in Appendix C.

### B. COVERAGE PROBABILITY OF M-4-RFA USING FLUID MODEL

The PBSs and MUEs are uniformly distributed in the four regions of a macrocell. Each PUE in any region receives cross-tier as well as co-tier interference from two regions, thus the PUE has to face co-tier as well as cross-tier interference from four regions. Consequently, following coverage probability expression is obtained

$$P_c^{(1)}(\tau) = \frac{\rho}{\zeta_f^2} \int_0^{R^2} \exp(-\tau v^{(1)\beta_2/2}) \psi^{(1)}(\beta, v^{(1)}) dv^{(1)}, \quad (25)$$

where

$$\begin{aligned}
 \psi^{(1)}(\beta, v^{(1)}) &= \frac{\sigma^2}{P_p} + \frac{2\pi\rho_j^{(1)}}{\beta_2 - 2} \left[ (2R - v^{(1)1/2})^{(2-\beta_2)} - (R_1 - v^{(1)1/2})^{(2-\beta_2)} \right] \\
 &+ \frac{2\pi\rho_k^{(2)}P_m}{P_p(\beta_1 - 2)} \left[ (R_1 - v^{(1)1/2})^{(2-\beta_1)} - (R_2 - v^{(1)1/2})^{(2-\beta_1)} \right] \\
 &+ \frac{2\pi\rho_l^{(3)}}{\beta_2 - 2} \left[ (R_2 - v^{(1)1/2})^{(2-\beta_2)} - (R_3 - v^{(1)1/2})^{(2-\beta_2)} \right] \\
 &+ \frac{2\pi\rho_n^{(4)}P_m}{P_p(\beta_1 - 2)} \left[ (R_3 - v^{(1)1/2})^{(2-\beta_1)} - (R_4 - v^{(1)1/2})^{(2-\beta_1)} \right].
 \end{aligned} \quad (26)$$

Following the similar procedure, the coverage probability of users located in  $R_2$ ,  $R_3$ , and  $R_4$ , respectively, can be derived. The final expressions are given in Appendix D.

### C. COVERAGE RATE ANALYSIS

Generally, the performance of network is evaluated in terms of eminent coverage improvement and enhanced data rates. In the above sections, the analytical closed-form expressions for the coverage probability have been derived, for the users having SINR greater than some threshold. In this section, exact rate distribution expression termed as rate coverage

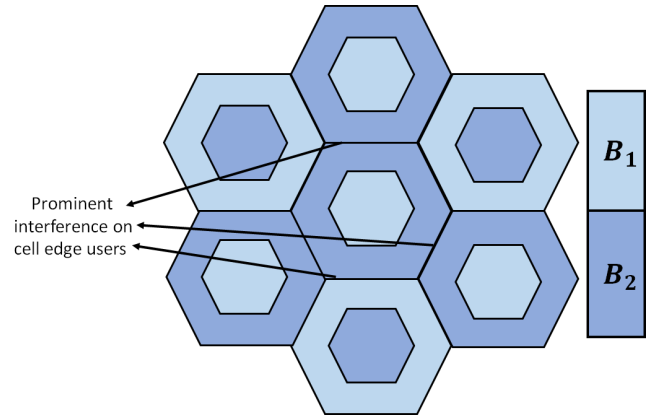


FIGURE 4. 2-RFA in a multi-cell scenario. The cell area is divided into two regions with frequency bands  $B_1$  and  $B_2$ .

probability is provided, by virtue of which the probability that the rate of an intended user is greater than the given threshold can be calculated. The expression for the rate coverage is derived in the following lemma.

*Lemma 1:* Given the SINR coverage probability greater than the threshold  $\tau$ ,  $P_c(\tau)$ , the coverage rate probability is evaluated as  $P(\delta) = P_c(2^{\delta/\Delta B} - 1)$ .

*Proof:* The proof is similar to [15], for  $\delta < \Delta B \log_2(1 + \tau_{max})$ , where  $\delta$  is the rate threshold,  $\Delta B = B/N$ ,  $B$  represents the total system bandwidth and  $N$  depicts the number of sub-bands provided to the users of each RFA scheme, like 2, 4, M-4, and 8-RFA scheme. The final expression directly follows and can be evaluated through a change of variables  $P(\delta) = \mathbb{P}[SINR > 2^{\delta/\Delta B} - 1] = P_c(2^{\delta/\Delta B} - 1)$ .

### V. RFA IN MULTI-CELL NETWORK

Given the SINR of downlink PUEs, we have formulated a framework which allows to analyze the network when the DL PUEs are located in a single macrocell partitioned into regions of equal area and receive interference from the UL MUEs and DL PBSs of the respective regions other than the serving PBS. In this section, we discuss the impact of inter-cell interference on the DL PUEs. While extending the baseline 2-RFA scheme in multi-cell, the distance between the macro as well as the pico users exploiting the same sub-carriers is reduced drastically, causing considerable amount of interference both from co-tier and cross-tier. This can be seen in Fig. 4, as the PUEs of  $R_2$  region in the central cell have to face prominent interference directly from the adjacent regions of neighboring cells, exploiting the same spectrum. Therefore, due to the inevitable intercell interference (ICI) from the neighboring cells, the SINR of cell edge users is affected immensely, making 2-RFA a less appropriate solution, even in multi-cellular network [26].

Partitioning the macro-cells into further non-overlapping regions of equal area reduces not only the intracell but also the intercell interference. The MUEs and PBSs of neighboring cells utilizing same spectrum, are spaced further apart, thereby decreasing the level of interference.



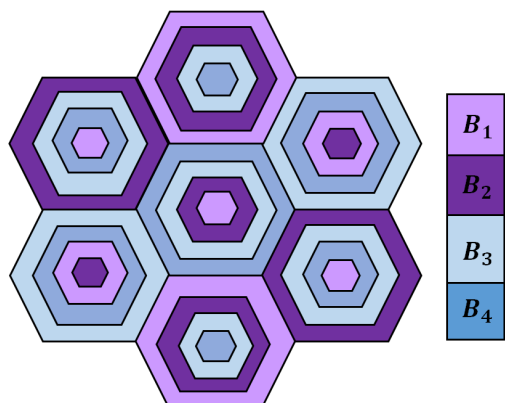


FIGURE 5. 4-RFA in a multi-cell scenario. The cell area is divided into four regions with frequency bands  $B_1$ ,  $B_2$ ,  $B_3$  and  $B_4$ .

When 4-RFA scheme is extended in multi-cell, the interfering cells experience maximum attenuation in their signals, i.e., the distance between the intended PUE and interfering cells is increased, which is evident in Fig. 5. It can be observed from the figure that the cell edge PUEs in  $R_4$  do not receive any co-tier interference from the adjacent regions of neighboring cells but only cross-tier interference from low powered MUEs from two neighboring cells. Thereby, the impact of interference becomes negligible, as a consequence, higher SINR is achieved. By opting the other higher region RFA schemes, for instance, 8-RFA and 16-RFA, the chance that the PUEs receive interference from the adjacent regions of other cells declines further, however, the issue of availability of smaller sub-bands to the users still persists. On the other hand, implementing the M-4-RFA scheme in multicell, the number of interfering entities in the adjacent regions of other cells is reduced. In this way, maximum benefit from the bandwidth can be exploited by making the impact of interference negligible. Therefore, M-4-RFA provides significant gains even when cross-tier interference of multi-cell is considered, the simulation results provide validation in the next section.

### VI. RESULTS & SYSTEM PERFORMANCE

In the previous sections, the analytical expressions for the coverage probability and rate coverage have been derived, whereas the accuracy of these expressions is validated through simulations in this section. To investigate the system performance, two simulation scenarios are considered. In the first case, the location of the PBSs, PUEs and that of MUEs is assumed to be uniformly distributed, whereas the second case follows by modeling the locations of PBSs and MUEs as spatial PPPs.

A two tier network is considered, where the radius of macro cell is assumed 1 km and is divided into two regions of equal area for 2-RFA and four regions of equal area for 4-RFA and M-4-RFA schemes, respectively. The rest of the parameters are shown in Table II. The comparison of three theoretically derived results of 2-RFA, 4-RFA and M-4-RFA, using fluid model with that of Monte-Carlo

TABLE 2. Simulation parameters.

Parameters	Values
System Bandwidth	10 MHz
Macrocell radius	1 km
No. of PBSs	120
No. of PUEs	400
No. of MUEs	120
Thermal noise	-174 dBm/Hz
PBS power	23 dBm
MBS power	46 dBm
Max. MUE power	23 dBm

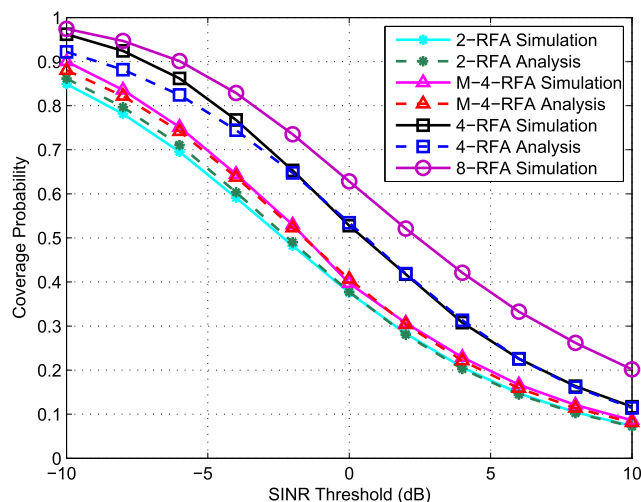


FIGURE 6. Coverage probability comparison of 2, 4, M-4, 8-RFA schemes in a two tier network ( $\beta_1 = 3$ ,  $\beta_2 = 2.5$ , No noise).

simulations along with 8-RFA is depicted in Fig. 6. The path loss exponent for pico cells is taken as 2.5 and that of macro users as 3. It can be noticed that as we divide the macrocell area into higher regions, the coverage probability increases, i.e. 8-RFA provides best coverage as compared to 4-RFA. Similarly 4-RFA outperforms 2-RFA. The figure also shows that M-4-RFA provides better coverage as compared to 2-RFA when the downlink PUE receives the same amount of interference as in 2-RFA, however these entities are now distantly located, due to modified sub-band allocation. In 4-RFA, users of each region get cross-tier interference from only one region, therefore, a better coverage is obtained, however the users are deprived of higher data rates, due to bandwidth division. From the figure, it is also validated that the simulation results agree with the trends generated through the analytical expressions for varying SINR threshold. In Fig. 7, the path loss exponents of pico tier and that of macro tier are assumed as 2.75 and 3.5, respectively. The figure also follows the similar trends in the simulation as well as the numerically computed values as of Fig. 6.

In Figs. 8 and 9, the PBSs are modeled as PPP having intensity  $\lambda = 3.8216 \times 10^{-5}$  BSs/m<sup>2</sup>. The values of path loss

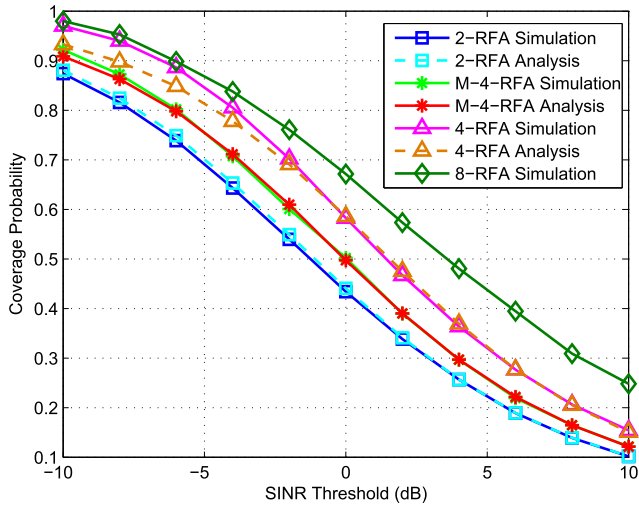


FIGURE 7. Coverage probability comparison of 2, 4, M-4, 8-RFA schemes in a two tier network ( $\beta_1 = 3.5, \beta_2 = 2.75$ , No noise).

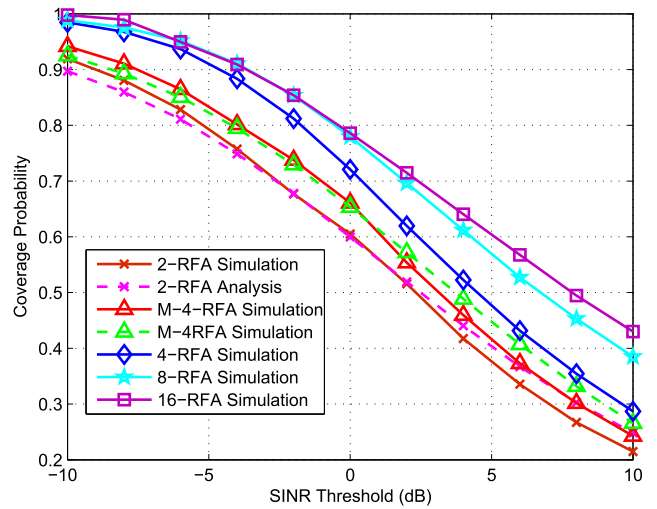


FIGURE 9. Coverage probability comparison of different RFA schemes in a two tier network, ( $\beta_1 = 4.5, \beta_2 = 3.75, \lambda_2 = 3\lambda_1$ , No noise).

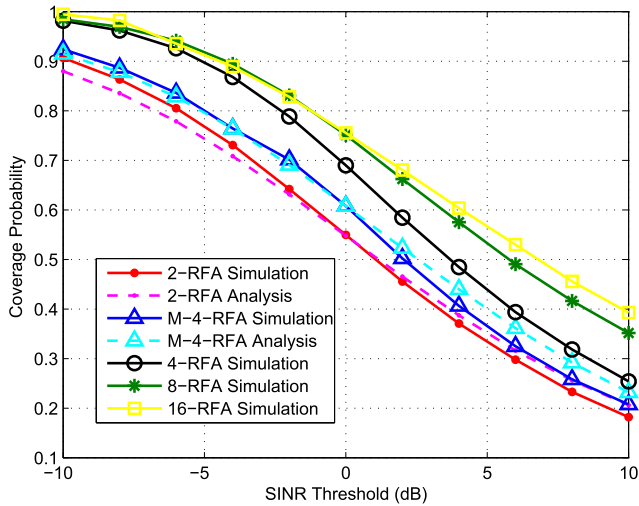


FIGURE 8. Coverage probability comparison of different RFA schemes in a two tier network, ( $\beta_1 = 4, \beta_2 = 3.5, \lambda_2 = 3\lambda_1$ , No noise).

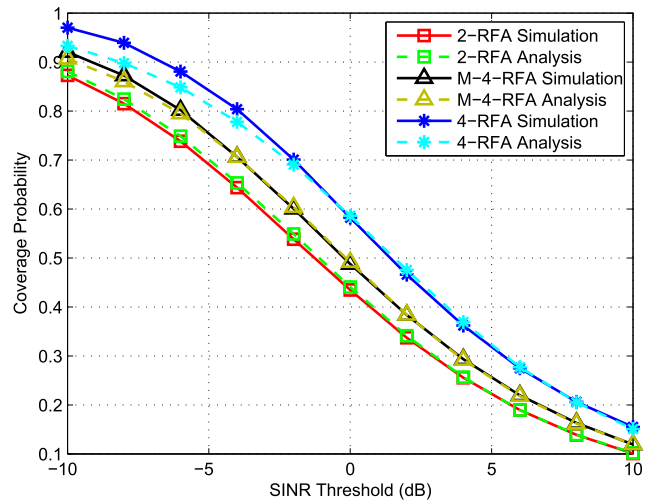


FIGURE 10. Coverage probability comparison of RFA schemes in a two tier network ( $\beta_1 = 2.75, \beta_2 = 3.5$ , noise thermal density =  $-174$  dBm/Hz).

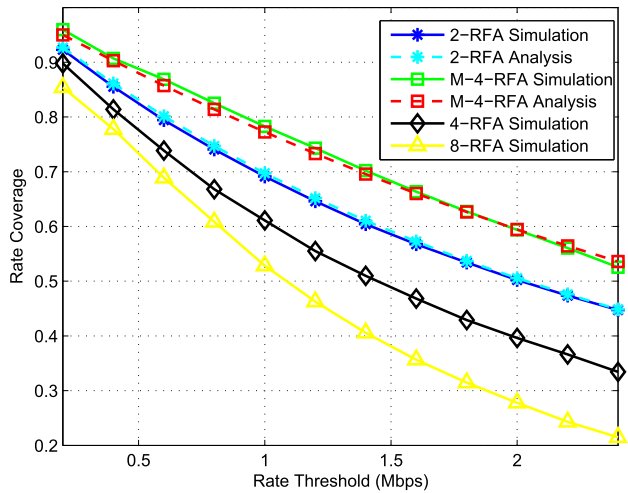
exponents for the pico cells and macrocell are 3.5 and 4 for Fig. 8, whereas 3.75 and 4.5 for Fig. 9, respectively. Firstly, the simulation results are quite close to analytical ones. Another fact that can be observed, it is not useful to partition the macrocell into higher regions because after dividing the macrocell into more than 8 regions, saturation occurs and no significant improvement in coverage probability is achieved.

Next the impact of thermal noise on the achievable coverage probability is investigated, the remaining simulation environment remains the same and thermal noise density is taken as  $-174$  dBm/Hz. The result is provided in Fig. 10, which verifies the fact that even after including noise the intended downlink users follow the same coverage trend when only interference is considered. For instance, at the SINR threshold value of 8 dB, the coverage probability of users implementing 2-RFA scheme is affected by 0.01% and that of M-4-RFA by 0.008% with the addition of noise. Hence, this result supports

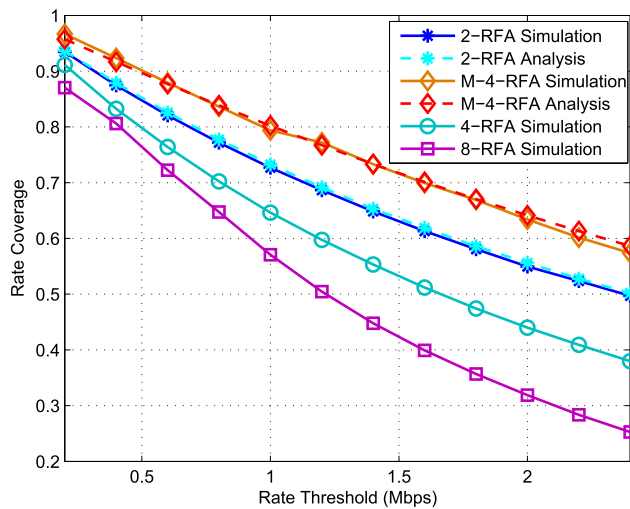
the claim that in the presence of interference, noise is not an influential factor and thus can be ignored.

The graphs in Figs. 11 and 12, show rate coverage probabilities,  $P(\delta)$ , as a function of the rate threshold  $\delta$ . We can observe that the M-4-RFA shows higher rates as opposed to the 2, 4 and 8-RFA, which is expected given the reduced level of interference and greater bandwidth allotted to users. We can also see that the simulation results follow the similar trend generated using Lemma 1.

After investigating the impact of coverage and rate coverage probability considering the cross-tier interference from single macrocell, now we get some insights of multi-cellular network which exploits various RFA techniques and conventional SFR scheme, in order to get improved coverage and elevated data rates. Fig. 13 depicts the outage probability of 2-RFA, 4-RFA, M-4-RFA, 8-RFA, 16-RFA and SFR, in



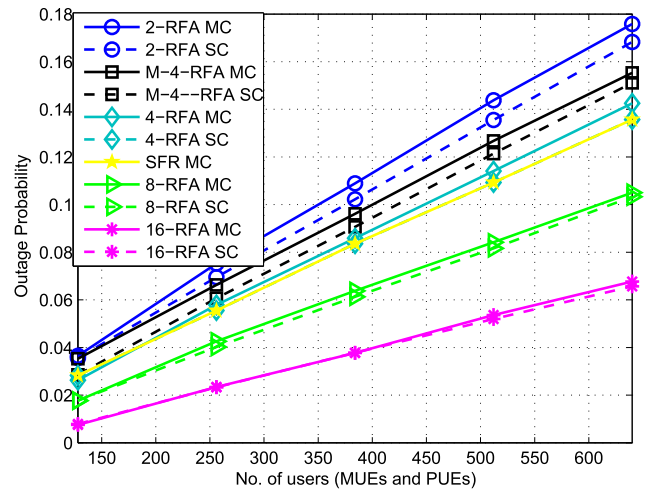
**FIGURE 11.** Rate coverage comparison between RFA schemes in a two tier network. (The operational system bandwidth is assumed 10 MHz,  $\beta_1 = 3.5$ ,  $\beta_2 = 2.75$ ).



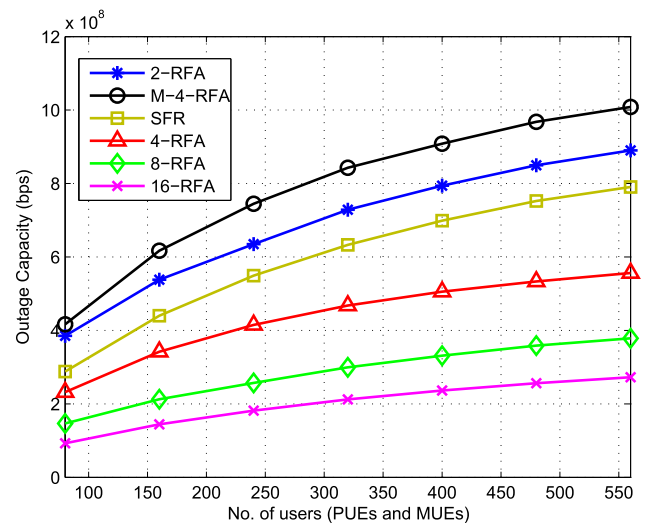
**FIGURE 12.** Rate coverage comparison between RFA schemes in a two tier network. (The operational system bandwidth is assumed 10 MHz,  $\beta_1 = 4$ ,  $\beta_2 = 3$ ).

single cell (SC) and multi-cell (MC) scenarios where the results are generated through Monte-Carlo simulations when the radius of macrocells is assumed as 2000 m, and path loss exponents for the small cells and macrocells are 2.5 and 3, respectively. From this figure, it can be observed that the intercell interference in 2-RFA is much greater than the rest of the RFA schemes and SRF scheme. The hybrid M-4-RFA scheme has a slightly greater interference than the regular 4-RFA scheme due to increased interfering cells. However, even with the elevated interference, the users now can get better data rates. Dividing the macrocell into higher regions reduces the gap between outage probability of SC and MC, because of increased separation among the users.

Finally, in Fig. 14, we depict the outage capacity, which is defined as the maximum constant rate that is maintained for the success probability. The 2-RFA scheme provides channel fairness, as a consequence, the cell edge users do not achieve



**FIGURE 13.** Outage probability of various RFA schemes in single and multi-cell scenarios ( $\tau = 0.4$ ,  $\beta_1 = 3$ ,  $\beta_2 = 2.5$ ).



**FIGURE 14.** Outage capacity of downlink PUEs in multi-cell with increasing user density ( $\beta_1 = 3$ ,  $\beta_2 = 2.5$ ,  $B = 10\text{MHz}$ ).

favorable data rates, whereas M-4-RFA is a scheme that provides fairness to all the users, as the intended PUEs have higher SINR in addition to better data rates. Eventually, when the performance is evaluated in terms of outage capacity, which depicts the sum rate of the users when they are in coverage instead of ergodic rate, it can be observed that the M-4-RFA provides higher outage capacity as compared to baseline schemes, which approves that even at higher user density, hybrid RFA scheme outperforms all the remaining RFA schemes.

### VII. CONCLUSION

In this paper, we analyzed a frequency allocation technique that reduces the impact of interference by assigning complementary sub-bands to different regions of a macrocell. The performance of different RFA schemes has been compared, while we also devised a hybrid M-4-RFA scheme that

combines the prominent aspects of various RFA schemes. Consequently, significant gains in terms of coverage and throughput are achieved. Approximated closed-form expressions for the coverage probability and rate coverage are derived using two approaches. The performance of the network is evaluated by varying sets of parameters, which verifies the fact that despite of slightly increased complexity as compared to baseline 2-RFA and SFR scheme, the proposed M-4-RFA scheme provides prominent performance gain. As a future work, the analytical modeling can be extended to the multi cellular network, where the impact of sectoring, addition of antennas and power allocation schemes can also be studied.

### APPENDIX A

The Laplace transform definition yields

$$\begin{aligned} \mathcal{L}_{I_{pbs}}(s) &= \mathbb{E} \left[ e^{-sI_{pbs}} \right], \\ &= \mathbb{E} \left[ \exp \left( -s \sum_{x_j^{(1)} \in \Phi_j^{(1)}/x^{(1)}} P_p h_j^{(1)} \|x_j^{(1)}\|^{-\beta_2} \right) \right], \end{aligned} \quad (27)$$

$$= \mathbb{E} \left[ \prod_{x_j^{(1)} \in \Phi_j^{(1)}/x^{(1)}} \exp \left( -s P_p h_j^{(1)} \|x_j^{(1)}\|^{-\beta_2} \right) \right], \quad (28)$$

$$= \mathbb{E}_{\Phi_j^{(1)}} \left[ \prod_{x_j^{(1)} \in \Phi_j^{(1)}/x^{(1)}} \frac{1}{1 + s P_p \|x_j^{(1)}\|^{-\beta_2}} \right]. \quad (29)$$

The channel gains are Rayleigh fading and are independent of PPP. The sum over PPP leads to the product form in (28) and the moment generating function of an exponential random variable yields (29). By applying the probability generation functional (PGFL) of PPP we obtain (30). Transformation of Cartesian to polar coordinates  $x_j^{(1)} = (r, \theta)$ , gives

$$\mathcal{L}_{I_{pbs}}(s) = \exp \left( \lambda_j^{(1)} \int_{\mathbb{R}^2/x^{(1)}} \left( 1 - \frac{1}{1 + s P_p \|x^{(1)}\|^{-\beta_2}} \right) dx^{(1)} \right), \quad (30)$$

$$= \exp \left( -2\pi \lambda_j^{(1)} \int_{x^{(1)}}^{R_1} \left( 1 - \frac{1}{1 + s P_p r^{-\beta_2}} \right) r dr \right), \quad (31)$$

where  $R_1$  is the radius of region 1 of macrocell. Thus, the interference from all the PBSs present in this region other than the serving BS at distance  $x^{(1)}$  is calculated by implementing the change of variables  $u^{(1)} = \tau^{-2/\beta_2} (\frac{r}{x^{(1)}})^2$ . The Laplace transform is given by

$$\mathcal{L}_{I_{pbs}}(s) = \exp \left( -\pi \lambda_j^{(1)} (s P_p)^{2/\beta_2} C_2^{(1)} \right), \quad (32)$$

where  $C_2^{(1)} = \int_{\tau^{-2/\beta_2} (R_1/x^{(1)})^2}^{\tau^{-2/\beta_2}} \left( \frac{1}{1+(u^{(1)})^{\beta_2/2}} \right) du^{(1)}$ .

### APPENDIX B

The Laplace transform of cumulative interference from the MUEs located in  $R_2$  is given as

$$\begin{aligned} \mathcal{L}_{I_{mue}^{(2)}}(s) &= \mathbb{E} \left[ e^{-sI_{mue}^{(2)}} \right], \\ &= \mathbb{E} \left[ \exp \left( -s \sum_{x_k^{(2)} \in \Phi_k^{(2)}} P_m h_k^{(2)} \|x_k^{(2)}\|^{-\beta_1} \right) \right], \end{aligned} \quad (33)$$

$$= \mathbb{E} \left[ \prod_{x_k^{(2)} \in \Phi_k^{(2)}} \exp \left( -s P_m h_k^{(2)} \|x_k^{(2)}\|^{-\beta_1} \right) \right], \quad (34)$$

$$= \mathbb{E}_{\Phi_k^{(2)}} \left[ \prod_{x_k^{(2)} \in \Phi_k^{(2)}} \frac{1}{1 + s P_m \|x_k^{(2)}\|^{-\beta_1}} \right], \quad (35)$$

$$= \exp \left( \lambda_k^{(2)} \int_{\mathbb{R}^2} \left( 1 - \frac{1}{1 + s P_m \|x^{(2)}\|^{-\beta_1}} \right) dx^{(2)} \right), \quad (36)$$

$$= \exp \left( -2\pi \lambda_k^{(2)} \int_{R_1}^{R_2} \left( 1 - \frac{1}{1 + s P_m r^{-\beta_1}} \right) r dr \right), \quad (37)$$

where the integration limit from  $R_1$  to  $R_2$ , defines the annular region of macrocell. Following the same procedure as in Appendix A and implementing the change of variables  $w^{(2)} = (\frac{\tau P_m x^{(1)\beta_2}}{P_p})^{-2/\beta_1} (r)^2$ , the Laplace transform can be further simplified as

$$\mathcal{L}_{I_{mue}^{(2)}}(s) = \exp \left( -\pi \lambda_k^{(2)} (s P_m)^{2/\beta_1} C_1^{(2)} \right), \quad (38)$$

where  $C_1^{(2)} = \int_{(\frac{\tau P_m x^{(1)\beta_2}}{P_p})^{-2/\beta_1} (R_1)^2}^{(\frac{\tau P_m x^{(1)\beta_2}}{P_p})^{-2/\beta_1} (R_2)^2} \left( \frac{1}{1+(w^{(2)\beta_1/2})} \right) dw^{(2)}$ .

### APPENDIX C

The impact of cumulative co-tier as well as cross-tier interference from all the four regions is obtained by deriving the Laplace transforms of interference from the DL and UL transmitters. By following the above mentioned procedure, the coverage probability of PUE located in  $R_2$  is given as

$$\begin{aligned} P_c^{(2)}(\tau) &= \pi \lambda_j^{(2)} \int_0^{R_2^2} \exp \left( -\pi v^{(2)} \lambda_j^{(2)} - \pi v^{(2)} \lambda_j^{(2)} \tau^{2/\beta_2} C_2^{(2)} \right. \\ &\quad \left. - \pi v^{(2)\beta_2/\beta_1} \lambda_k^{(1)} \left( \frac{P_m \tau}{P_p} \right)^{2/\beta_1} C_1^{(1)} - \pi v^{(2)} \lambda_l^{(4)} \tau^{2/\beta_2} C_2^{(4)} \right. \\ &\quad \left. - \pi v^{(2)\beta_2/\beta_1} \lambda_n^{(3)} \left( \frac{P_m \tau}{P_p} \right)^{2/\beta_1} C_1^{(3)} - \left( \frac{\tau \sigma^2}{P_p} v^{(2)\beta_2/2} \right) \right) dv^{(2)}. \end{aligned} \quad (39)$$

When a PUE is in  $R_3$  region, it receives cross-tier interference from  $R_2$  and  $R_4$ , respectively, thus the coverage probability

expression becomes

$$\begin{aligned}
P_c^{(3)}(\tau) &= \pi \lambda_j^{(3)} \int_0^{R_3^2} \exp\left(-\pi v^{(3)} \lambda_j^{(3)} - \pi v^{(3)} \lambda_j^{(3)} \tau^{2/\beta_2} C_2^{(3)}\right. \\
&\quad \left.- \pi v^{(3)\beta_2/\beta_1} \lambda_k^{(4)} \left(\frac{P_m \tau}{P_p}\right)^{2/\beta_1} C_1^{(2)} - \pi v^{(3)} \lambda_l^{(1)} \tau^{2/\beta_2} C_2^{(1)}\right. \\
&\quad \left.- \pi v^{(3)\beta_2/\beta_1} \lambda_n^{(2)} \left(\frac{P_m \tau}{P_p}\right)^{2/\beta_1} C_1^{(4)} - \left(\frac{\tau \sigma^2}{P_p} v^{(3)\beta_2/2}\right)\right) dv^{(3)}. \quad (40)
\end{aligned}$$

Similarly, when the PUE is in  $R_4$  region, it receives cross-tier interference from  $R_1$  and  $R_3$ , respectively. The coverage probability is expressed as

$$\begin{aligned}
P_c^{(4)}(\tau) &= \pi \lambda_j^{(4)} \int_0^{R_4^2} \exp\left(-\pi v^{(4)} \lambda_j^{(4)} - \pi v^{(4)} \lambda_j^{(4)} \tau^{2/\beta_2} C_2^{(4)}\right. \\
&\quad \left.- \pi v^{(4)\beta_2/\beta_1} \lambda_k^{(3)} \left(\frac{P_m \tau}{P_p}\right)^{2/\beta_1} C_1^{(1)} - \pi v^{(4)} \lambda_l^{(2)} \tau^{2/\beta_2} C_2^{(2)}\right. \\
&\quad \left.- \pi v^{(4)\beta_2/\beta_1} \lambda_n^{(1)} \left(\frac{P_m \tau}{P_p}\right)^{2/\beta_1} C_1^{(3)} - \left(\frac{\tau \sigma^2}{P_p} v^{(4)\beta_2/2}\right)\right) dv^{(4)}. \quad (41)
\end{aligned}$$

## APPENDIX D

When the pico user is located in  $R_2$  region, the uniformly distributed PBSs other than the serving PBS in that region act as interferers, along with the PBSs in  $R_4$  region. Therefore, by evaluating the expected value of interference as in (26). The PUE that is located in  $R_2$  region has coverage probability

$$P_c^{(2)}(\tau) = \frac{\rho}{\zeta_f^2} \int_0^{R^2} \exp\left(-\tau v^{(2)\beta_2/2} \psi^{(2)}(\beta, v^{(2)})\right) dv^{(2)}. \quad (42)$$

Similarly, when a PUE is in  $R_3$ , the lower bound of coverage probability is expressed as

$$P_c^{(3)}(\tau) = \frac{\rho}{\zeta_f^2} \int_0^{R^2} \exp\left(-\tau v^{(3)\beta_2/2} \psi^{(3)}(\beta, v^{(3)})\right) dv^{(3)}. \quad (43)$$

Finally, coverage probability of a PUE that is located in  $R_4$  is given as

$$P_c^{(4)}(\tau) = \frac{\rho}{\zeta_f^2} \int_0^{R^2} \exp\left(-\tau v^{(4)\beta_2/2} \psi^{(4)}(\beta, v^{(4)})\right) dv^{(4)}, \quad (44)$$

where  $\psi^{(2)}(\beta, v^{(2)})$ ,  $\psi^{(3)}(\beta, v^{(3)})$  and  $\psi^{(4)}(\beta, v^{(4)})$ , can be obtained by computing the integration limits for cumulative interference similar to (13) and (26).

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