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# Multiple Sclerosis Detection Based on Biorthogonal Wavelet Transform, RBF Kernel Principal Component Analysis, and Logistic Regression

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**ABSTRACT** To detect multiple sclerosis (MS) diseases early, we proposed a novel method on the hardware of magnetic resonance imaging, and on the software of three successful methods: biorthogonal wavelet transform, kernel principal component analysis, and logistic regression. The materials were 676 MR slices containing plaques from 38 MS patients, and 880 MR slices from 34 healthy controls. The statistical analysis showed our method achieved a sensitivity of  $97.12 \pm 0.14\%$ , a specificity of  $98.25 \pm 0.16\%$ , and an accuracy of  $97.76 \pm 0.10\%$ . Our method is superior to five state-of-the-art approaches in MS detection.

**INDEX TERMS** Biorthogonal wavelet transform, kernel principal component analysis, logistic regression, multiple sclerosis, computer vision, machine learning.

## I. INTRODUCTION

Multiple sclerosis (MS) affects human brain and spinal cord by damaging the insulating covers of neural cells [1]. The cause is unclear, thus the underlying mechanism is either immune system destruction [2] or myelin-producing cell failure [3]. Clinically, MS is associated with depression [4], lower urinary tract symptom [5], fatigue [6], muscle weakness [7], etc.

To detect MS early, the neuroradiologists tend to use magnetic resonance imaging (MRI) technique to scan the patients' brains. Nevertheless, the normal-appearing white matter (NAWM) paradox [8], [9] poses a radical challenge, since the lesions within the white matter may appear the same as healthy white matter.

With the rapid development in computer science, the computer vision (CV) [10], [11] has high probabilities to help neuroradiologists to detect MS. CV studies and mimics the human vision, and thus gaining high-level understanding on digital images and videos. It can implement any tasks that a human visual system can do. Artificial intelligence (AI) [12] can ease the process that CV learns to understand the contents in image and video. Therefore, CV is often combined with AI [13] and its variants, such as machine learning [14], bio-inspired mechanism [15], expert system [16], swarm intelligence [17], etc.

Current CV systems on brain diseases capture more exciting attentions from scholars in both research and industrial domains. For example, Murray et al. [18] extracted features

from MS images. They employed a multiscale amplitude-modulation frequency-modulation (abbreviated as MAMFM) method. Finally, support vector machine (SVM) was used. Phillips et al. [19] suggested a novel feature—wavelet entropy (WE)—for abnormal brain detection. To train the classifier, a Hybridization of Biogeography-based optimization and Particle swarm optimization (HBP) was proposed. Siddiqui et al. [20] presented a combined system based on discrete wavelet transform (DWT), principal component analysis (PCA), and least-square support vector machine (LS-SVM). Nayak et al. [21] proposed a novel abnormal MR image detector, based on DWT, probabilistic PCA (PPCA), and random forest (RF). Zhou [22] used stationary wavelet entropy (SWE) to detect MS. They compared three algorithms: decision tree (DT), k-nearest neighbors (kNN), and SVM.

Nevertheless, the accuracy performances of above mentioned references are not satisfying. Besides, their statistical analysis only reported the average result, other than the standard deviation. In this study, we presented a novel MS detection method based on biorthogonal wavelet transform, kernel principal component analysis, and logistic regression. The structure is organized as follows: Section II gives the materials. Section III offers the methodology. Section IV presents the results and discussions. Section V concludes the paper.

## II. MATERIALS

In this study, we obtain 676 MR slices containing plaques from 38 MS patients, and 880 MR slices from 34 healthy controls. The detailed description of those data can be found in reference [22]. The MS patients and healthy controls are scanned by different scanners in different positions. To ease brain slice comparability, we used the histogram stretching (HS) [23] method to increase the dynamic range of all MS and healthy brain images. The HS was performed as follows:

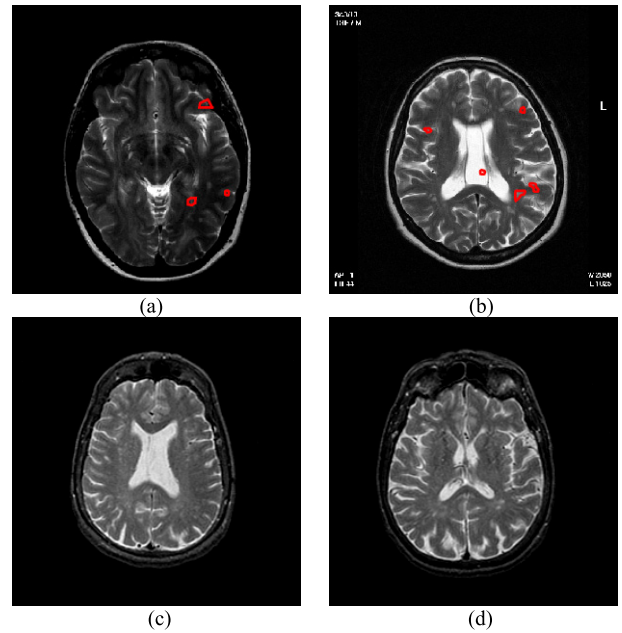
$$b(i, j) = \frac{a(i, j) - a_{\min}}{a_{\max} - a_{\min}} \quad (1)$$

where  $(i, j)$  represents the coordinate of the pixels,  $a$  represents original slice,  $b$  the HS normalized slice. The  $a_{\min}$  and  $a_{\max}$  represent the minimum and maximum intensity values, respectively. Figure 1 shows the samples of our used brain slices.

## III. METHODOLOGY

### A. DISCRETE WAVELET TRANSFORM

In numerical analysis, the discrete wavelet transform (DWT) is an effective way to extract global features from images or videos. It is also used in JPEG 2000—an image compression standard and coding system [24] and the fingerprint identification systems [25]. In academic fields, DWT is applied in various fields, e.g., classification of MR image [26], hearing loss detection [27], pathological brain detection [28], video watermarking [29], abnormal brain detection [30], infant cry



**FIGURE 1.** Sample of brain slices. (a) A MS slice with 3 plaques. (b) A MS slice with 5 plaques. (c) A healthy brain slice. (d) Another healthy brain slice.

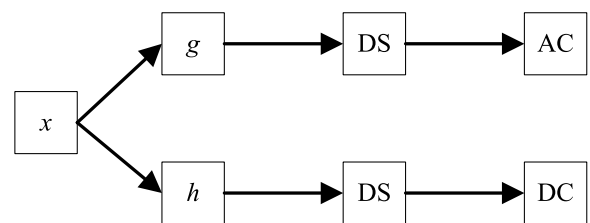
detection [31], dendrite spine detection [32], biometric template generation [33], tea classification [34], etc.

Mathematically, the DWT of a brain image  $x$  is obtained by passing it through a series of filters. The discrete samples of  $x$  are passed through a low-pass filter  $g$  and a high-pass filter  $h$ , resulting the approximation coefficients (AC) and detail coefficients (DC), respectively. The filters output are usually down-sampled by a factor of 2.

$$AC(n) = \sum_{m=-\infty}^{+\infty} x(m)g(2n - m) \quad (2)$$

$$DC(n) = \sum_{m=-\infty}^{+\infty} x(m)h(2n - m) \quad (3)$$

These two filters are known as the quadrature mirror filter. Figure 2 shows the diagram of passing through filters.



**FIGURE 2.** Diagram of passing through filters (DS = down-sampling, AC = approximation coefficient, DC = detail coefficient).

### B. BIORTHOGONAL WAVELET TRANSFORM

There are many wavelet families, such as Haar [35], db [36], and others. In this study, we chose the biorthogonal wavelet. The advantage of orthogonal wavelet is the associated wavelet transform is orthogonal, thus, the inverse wavelet transform

is the adjoint of the wavelet transform. The advantage of biorthogonal wavelet transform (BWT) is it allows more degrees of freedom compared to orthogonal wavelet [37].

In this study, we chose the biorthogonal 4.4 wavelet. Its filters and functions for decomposition are shown in Figure 3 and Figure 4, respectively. The corresponding filters and functions for reconstruction are not presented, since our task only uses decomposition.

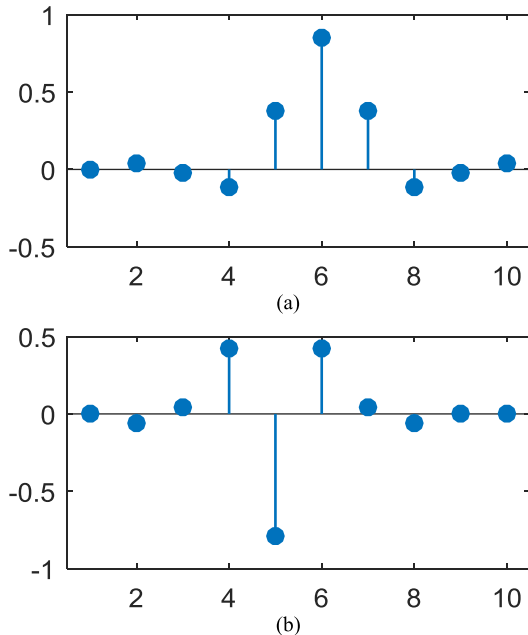


FIGURE 3. Filters of biorthogonal 4.4: (a) low-pass filter  $g$ ; (b) high-pass filter  $h$ .

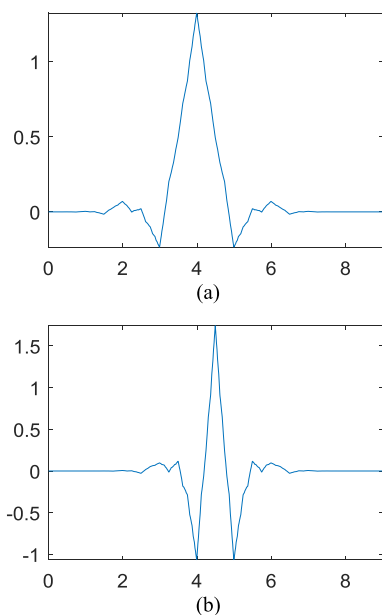


FIGURE 4. Functions of biorthogonal 4.4: (a) scaling function; (b) wavelet function.

Besides BWT, there are many other excellent wavelet transform variants, such as wavelet packet transform [38],

relative wavelet energy [39], wavelet energy [40], scale-discretized wavelet transform [41], stationary wavelet transform [42], spherical wavelet transform [43], exponential wavelet transform [44], dual-tree complex wavelet transform [45], etc. Those advanced wavelet transforms are also expected to give better performance than standard DWT. In the future, we shall test their performances.

### C. PRINCIPAL COMPONENT ANALYSIS

As an effective dimensionality reduction tool, principal component analysis (PCA) can reduce the size of wavelet coefficients from MR brain images [46]. Assume there is a dataset  $C$  with size of  $N$  and dimension of  $d$ , first we calculate the sample mean  $m_j$  of  $j$ -th feature as

$$m_j = \frac{1}{N} \sum_{i=1}^N C(i, j) \quad (4)$$

Next, we calculate the zero-mean dataset  $B$  as

$$B = C - em^T \quad (5)$$

Here  $e$  represents an  $N \times 1$  vector of all ones [47].

Third, the  $d \times d$  covariance matrix  $Z$  is generated

$$Z = \frac{B^*B}{N - 1} \quad (6)$$

Fourth, the covariance matrix  $Z$  has an eigen decomposition expression as

$$Z = XYX^{-1} \quad (7)$$

here  $X$  represents the eigenvector matrix, and  $Y$  represents the eigenvalue matrix, which is also a diagonal matrix[48].

$$Y = \begin{bmatrix} Y(1, 1) & & & \\ & Y(2, 2) & & \\ & & \ddots & \\ & & & Y(d, d) \end{bmatrix} \quad (8)$$

Fifth, we rearrange  $X$  and  $Y$ , so that the eigenvalue is in a decreasing way.

$$Y(1, 1) \geq Y(2, 2) \geq \dots \geq Y(d, d) \quad (9)$$

Sixth, we calculate cumulative variance for each eigenvector by

$$G(k) = \sum_{i=1}^k Y(i, i) \quad (10)$$

Thus, we can form a vector as

$$G = [G(1) \ G(2) \ \dots \ G(d)] \quad (11)$$

Seventh, assume the threshold is  $T$ , and thus we select  $L^*$  that satisfies

$$L^* = \arg \min \left\{ L \mid \frac{G(L)}{G(d)} \geq T \right\} \quad (12)$$

Finally, we output  $L^*$  most important principal components.

**D. KERNEL PCA**

The shortcoming of PCA is it cannot extract non-linear structure information [49]. To solve this problem, scholars have proposed a powerful variant of PCA—kernel PCA (KPCA). The KPCA implements the same as PCA except transforming the dataset  $C$  into a higher-dimensional space [50].

Two different KPCAs were studied. One is the polynomial kernel PCA (PKPCA) defined as

$$k(x, y|PKPCA) = [a(x \times y) + b]^c \tag{13}$$

where  $a, b,$  and  $c$  are kernel parameters

The other is the RBF kernel PCA (RKPCA) [51] defined as

$$k(x, y|RKPCA) = \exp\left(-\frac{\|x - y\|^2}{d^2}\right) \tag{14}$$

where  $d$  represents the scaling factor.

The optimal estimation of hyper parameters  $a, b, c,$  and  $d$  can be obtained by grid search (GS) algorithm. GS is also named as parameter sweep. It is an exhaustive searching method within a manually specified subset of the hyper parameter space.

**E. LOGISTIC REGRESSION**

Traditional regression analysis help the users understand the relationship between a dependent variable and on or more independent variables. Logistic regression is an improved regression model that can handle the situation where dependent variable is categorical [52]. In this study, we predict a bran MR image as either MS or healthy. This prediction output belongs to a binary categorical variable.

For a binary logistic regression, the output is usually encoded as either 0 or 1 [53]. Following common convention, we encode the particular noteworthy output as 1, here the MS patient. We also encode the contrary output as 0, here as the healthy. Table 1 shows the encoding strategy for the output.

**TABLE 1. Output encoding.**

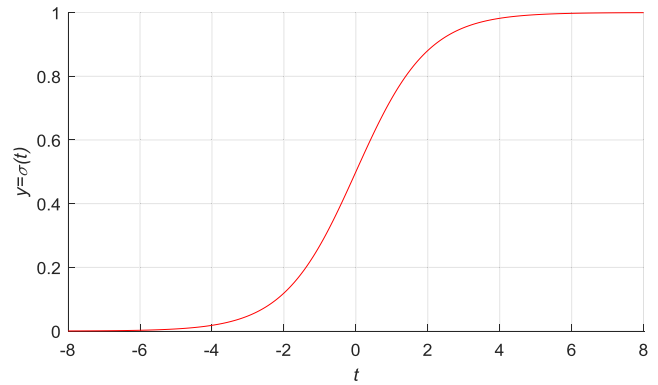
| Value | Meaning         |
|-------|-----------------|
| 1     | MS patient      |
| 0     | Healthy Subject |

Suppose we have  $L$  principal components as  $[x_1, x_2, \dots, x_L]$  as the independent variable, and we have one dependent variable  $y$  either 0 or 1 indicating healthy or MS patient. Then, we can create the binary logistic regression model as to find the optimal vector  $\beta = [\beta_0, \beta_1, \beta_2, \dots, \beta_L]$  that best fits

$$y = \begin{cases} 1 & \beta_0 + \beta_1 x_1 + \beta_2 x_2 + \dots + \beta_L x_L + \varepsilon > 0 \\ 0 & \text{otherwise} \end{cases} \tag{15}$$

here  $\varepsilon$  represents the unobservable error.

To achieve above model, a challenge arise as to smash the input (with values from negative to positive infinity) to the output (with values between 0 and 1). The logistic function



**FIGURE 5. Logistic function.**

$\sigma(t)$  can solve this problem [54].  $\sigma(t)$  is defined below with a curve plot shown in Figure 5.

$$\sigma(t) = \frac{1}{1 + \exp(-t)} \tag{16}$$

In this study,  $t$  can be regarded as a latent variable, which is a linear weighted combination of independent variable  $x$  as

$$t \leftarrow \beta_0 + \beta_1 x_1 + \beta_2 x_2 + \dots + \beta_L x_L \tag{17}$$

Thus, the binary logistic model is:

$$F(x) = \frac{1}{1 + \exp[-(\beta_0 + \beta_1 x_1 + \beta_2 x_2 + \dots + \beta_L x_L)]} \tag{18}$$

where  $F(x)$  represents the probability of dependent variable  $y = 1$ , i.e., corresponding to a MS patient.  $\beta_0$  is the intercept.  $[\beta_1, \beta_2, \dots, \beta_L]$  represents the regression coefficient for  $[x_1, x_2, \dots, x_L]$ .

There are other advanced classifiers besides LR, such as feed forward neural network [55], association rule learning [56], decision tree [57], dynamic Bayesian network [58], nonparallel support vector machine [59], reinforcement learning [60], twin support vector machine [61], extreme learning machine [62], etc. Those classifiers have a radically different mechanism with the LR, but they may also give satisfying performances. In the future, we shall apply them to MS detection.

**F. STATISTICAL ANALYSIS**

Before we step into the experiment, we need to point out the importance of statistical analysis and its relationship to the hyper parameters of  $[a, b, c, d]$ .

We used a ten-fold cross validation (TFCV) as shown in Fig. 6. The whole dataset was segmented into 10 folds (A to J). In every trial, eight folds out of 10 folds were used for training, one fold for validation, and the final fold for test. The purposes of the three sets are listed in Table 2. Note that the classifier needs to be retrained for each trial. To further reduce the randomness, we ran the TFCV ten times, and report the average and the standard deviation in terms of sensitivity, accuracy, and specificity.

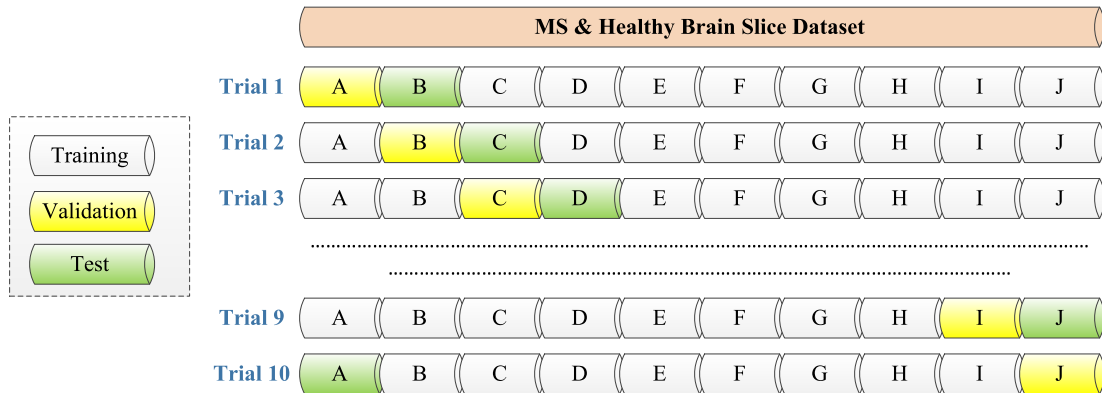


FIGURE 6. Illustration of TFCV.

TABLE 2. Purpose of training, validation and test sets.

| Set        | Purpose                              |
|------------|--------------------------------------|
| Training   | Reduce training error                |
| Validation | Optimize hyperparameters             |
| Test       | Give unbiased performance estimation |

TABLE 3. Comparison of different dimensionality reduction methods (Threshold = 95% of total variance).

| Method | No. of PCs | Ratio |
|--------|------------|-------|
| PCA    | 424        | 0.58% |
| PKPCA  | 405        | 0.55% |
| RKPCA  | 396        | 0.54% |

TABLE 4. Sensitivities over 10 runs.

|      | F1   | F2   | F3   | F4   | F5   | F6   | F7   | F8   | F9   | F10 | Sum            |
|------|------|------|------|------|------|------|------|------|------|-----|----------------|
| R1   | 95.  | 97.  | 100. | 92.  | 100. | 98.  | 95.  | 97.  | 97.  | 97. | 97.04          |
| R2   | 100. | 94.  | 95.  | 94.  | 100. | 98.  | 100. | 92.  | 98.  | 95. | 97.04          |
| R3   | 100. | 98.  | 94.  | 97.  | 100. | 98.  | 95.  | 97.  | 98.  | 94. | 97.34          |
| R4   | 98.  | 94.  | 100. | 100. | 98.  | 100. | 97.  | 92.  | 97.  | 94. | 97.19          |
| R5   | 95.  | 91.  | 98.  | 97.  | 98.  | 97.  | 98.  | 100. | 100. | 97. | 97.34          |
| R6   | 97.  | 97.  | 100. | 89.  | 100. | 100. | 94.  | 97.  | 97.  | 98. | 97.04          |
| R7   | 100. | 97.  | 94.  | 98.  | 98.  | 91.  | 94.  | 100. | 100. | 97. | 97.04          |
| R8   | 94.  | 100. | 98.  | 97.  | 97.  | 97.  | 100. | 94.  | 98.  | 94. | 97.04          |
| R9   | 94.  | 100. | 95.  | 95.  | 100. | 97.  | 95.  | 97.  | 97.  | 97. | 96.89          |
| R10  | 95.  | 100. | 100. | 94.  | 94.  | 100. | 100. | 94.  | 98.  | 94. | 97.19          |
| Ave. |      |      |      |      |      |      |      |      |      |     | 97.12<br>±0.14 |

IV. RESULTS AND DISCUSSIONS

Our experiment was performed on Dell laptop with 3.20 GHz i5-3470 CPU and 4GB RAM. Programs were developed in-house and ran on Windows 10 Operating System.

TABLE 5. Specificities over 10 runs.

|      | F1   | F2   | F3   | F4   | F5   | F6   | F7   | F8   | F9   | F10  | Sum            |
|------|------|------|------|------|------|------|------|------|------|------|----------------|
| R1   | 100. | 100. | 100. | 97.  | 95.  | 95.  | 96.  | 97.  | 100. | 98.  | 98.41          |
| R2   | 98.  | 96.  | 95.  | 98.  | 96.  | 100. | 100. | 100. | 97.  | 97.  | 98.30          |
| R3   | 100. | 97.  | 100. | 97.  | 100. | 98.  | 98.  | 97.  | 93.  | 97.  | 98.18          |
| R4   | 96.  | 98.  | 100. | 96.  | 100. | 100. | 97.  | 97.  | 97.  | 98.  | 98.52          |
| R5   | 95.  | 100. | 96.  | 100. | 95.  | 100. | 96.  | 98.  | 97.  | 98.  | 98.07          |
| R6   | 97.  | 100. | 100. | 97.  | 95.  | 97.  | 96.  | 100. | 96.  | 100. | 98.18          |
| R7   | 96.  | 96.  | 100. | 100. | 96.  | 100. | 98.  | 96.  | 96.  | 100. | 98.41          |
| R8   | 97.  | 100. | 100. | 94.  | 96.  | 100. | 100. | 100. | 97.  | 95.  | 98.52          |
| R9   | 100. | 98.  | 96.  | 98.  | 100. | 96.  | 100. | 97.  | 95.  | 100. | 98.52          |
| R10  | 98.  | 98.  | 98.  | 96.  | 96.  | 100. | 98.  | 96.  | 97.  | 100. | 98.30          |
| Ave. |      |      |      |      |      |      |      |      |      |      | 98.25<br>±0.16 |

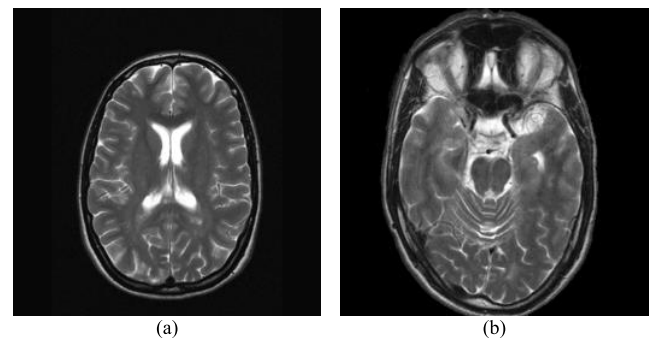
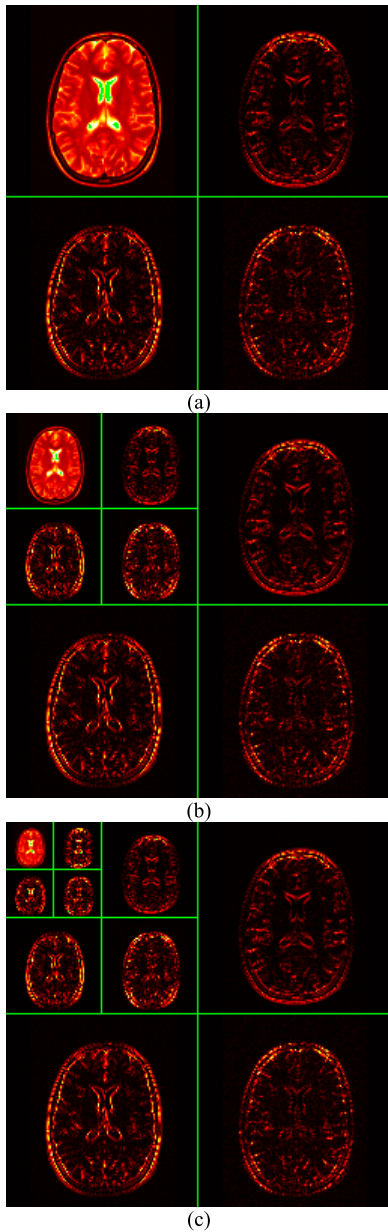


FIGURE 7. Two samples for biorthogonal decomposition. (a) Sample I. (b) Sample II.

A. BIORTHOGONAL DECOMPOSITION

Figure 7 presents two samples. We performed three-level bior 4.4 decomposition over these two sample images. The decompositions results are offered in





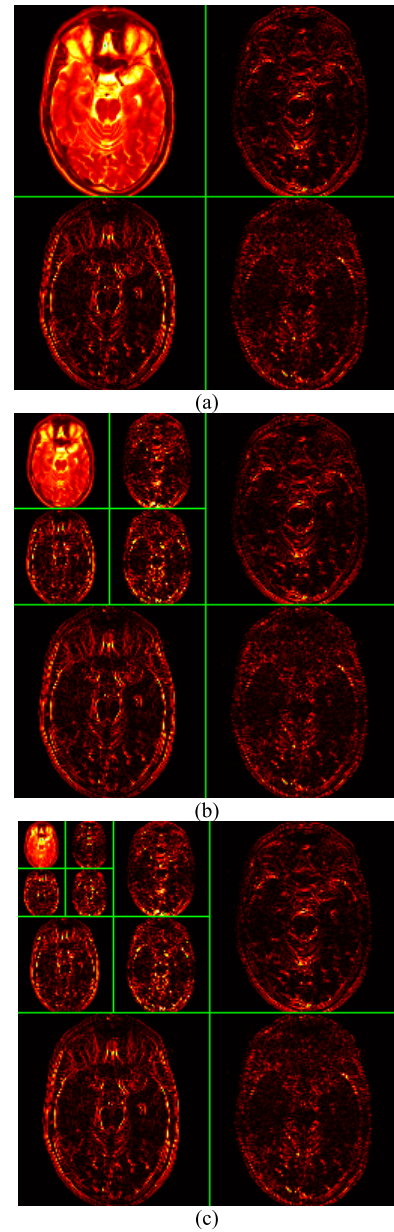
**FIGURE 8.** BWT Decomposition of Sample I (Hot color map was added). (a) 1-level. (b) 2-level. (c) 3-level.

Figure 8 and Figure 9, respectively. For better view of coefficients, we use hot pseudo color map.

Some literature combined entropy with discrete wavelet transform [63], [64]. In this condition, the entropy operation can be regarded as a means to reduce features. Nevertheless, we already used KPCA in this study; thus it is unnecessary for us to perform entropy operations.

**B. PCA VERSUS KPCA**

In this section, we compared PCA with KPCA. The wavelet coefficients of each brain image were realigned as a row vector with length of 73056. This value is a bit more than  $256^2 = 65536$  due to the border and down sampling. Afterwards, the 1556 images will form a matrix with size of  $1556 \times 73056$ .



**FIGURE 9.** BWT Decomposition of Sample II (Hot color map was added). (a) 1-level. (b) 2-level. (c) 3-level.

Using three dimensionality reduction methods (PCA, PKPCA, RKPCA) and setting the threshold as 95%, we plot the cumulated explained variances versus selected PCs in Figure 10. Here we know that PCA selects 424 PCs, PKPCA selects 405 PCs, and RKPCA selects 396 PCs. Dividing them by the total coefficients, we know that PCA selects 0.58% of total coefficients, PKPCA selects 0.55%, and RKPCA selects 0.54%, which are listed in Table 3. Therefore, we find that RKPCA selects the least number of PCs while attaining the same threshold.

**C. STATISTICAL ANALYSIS**

The sensitivities, specificities, and accuracies over all 10 runs are listed below in Table 4, Table 5, and Table 6, respectively.

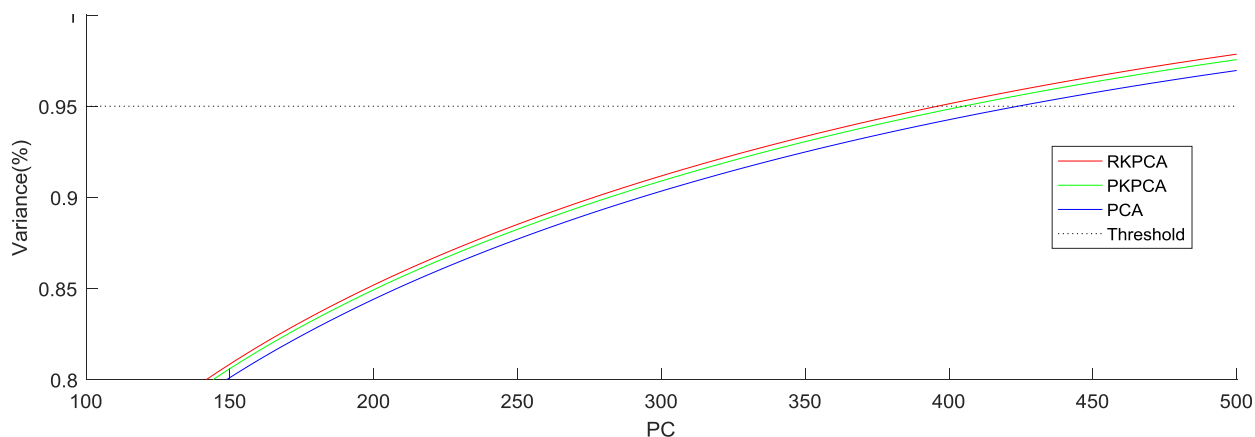


FIGURE 10. Selected PCs by different algorithms.

TABLE 6. Accuracies over 10 runs.

|      | F1   | F2   | F3   | F4  | F5   | F6   | F7   | F8  | F9  | F10 | Sum   |
|------|------|------|------|-----|------|------|------|-----|-----|-----|-------|
| R1   | 98.  | 98.  | 100. | 95. | 97.  | 96.  | 96.  | 97. | 98. | 98. | 97.62 |
|      | 06   | 72   | 00   | 48  | 42   | 79   | 15   | 42  | 72  | 08  |       |
| R2   | 99.  | 95.  | 95.  | 96. | 98.  | 99.  | 100. | 96. | 98. | 96. | 97.69 |
|      | 36   | 51   | 51   | 77  | 06   | 35   | 00   | 79  | 08  | 79  |       |
| R3   | 100. | 98.  | 97.  | 97. | 100. | 98.  | 97.  | 97. | 95. | 96. | 97.75 |
|      | 00   | 08   | 42   | 42  | 00   | 71   | 44   | 44  | 51  | 15  |       |
| R4   | 97.  | 96.  | 100. | 98. | 99.  | 100. | 97.  | 95. | 97. | 96. | 97.94 |
|      | 44   | 79   | 00   | 06  | 35   | 00   | 44   | 48  | 44  | 77  |       |
| R5   | 95.  | 96.  | 97.  | 98. | 96.  | 98.  | 97.  | 99. | 98. | 98. | 97.75 |
|      | 51   | 13   | 44   | 72  | 79   | 72   | 44   | 35  | 71  | 06  |       |
| R6   | 97.  | 98.  | 100. | 94. | 97.  | 98.  | 95.  | 98. | 96. | 99. | 97.62 |
|      | 44   | 72   | 00   | 19  | 42   | 72   | 51   | 72  | 77  | 35  |       |
| R7   | 98.  | 96.  | 97.  | 99. | 97.  | 96.  | 96.  | 98. | 98. | 98. | 97.81 |
|      | 06   | 77   | 44   | 36  | 44   | 13   | 79   | 08  | 08  | 71  |       |
| R8   | 96.  | 100. | 99.  | 95. | 96.  | 98.  | 100. | 97. | 98. | 94. | 97.88 |
|      | 77   | 00   | 35   | 48  | 79   | 72   | 00   | 44  | 08  | 87  |       |
| R9   | 97.  | 99.  | 96.  | 97. | 100. | 96.  | 98.  | 97. | 96. | 98. | 97.75 |
|      | 42   | 36   | 15   | 44  | 00   | 79   | 08   | 42  | 15  | 71  |       |
| R10  | 97.  | 99.  | 99.  | 95. | 95.  | 100. | 99.  | 95. | 98. | 97. | 97.75 |
|      | 44   | 35   | 36   | 48  | 51   | 00   | 35   | 51  | 06  | 44  |       |
| Ave. |      |      |      |     |      |      |      |     |     |     | 97.76 |
|      |      |      |      |     |      |      |      |     |     |     | ±0.10 |

Here F means fold, R means run. We can observe that our proposed method yields a sensitivity of  $97.12 \pm 0.14$ , a specificity of  $98.25 \pm 0.16$ , and an accuracy of  $97.76 \pm 0.10$ .

D. COMPARISON TO STATE-OF-THE-ART METHODS

We submitted a 1556x396 matrix to the classifier of LR. Here 1556 is the number of total image, 396 is the number of PCs. Two Matlab commands “mnrfit” and “mnrvl” were used to accelerate the program developing.

We compared our BWT + RKPCA + LR method with five state-of-the-art approaches: MAMFM + SVM [18], WE + HBP [19], DWT + PCA + LS-SVM [20], DWT + PPCA + RF [21], and SWE + DT [22]. Table 7 presents the comparison results. Note that our method runs 10 times, so we also report the standard deviation. The unit of data in Table 7 is percentage.

TABLE 7. Algorithm comparison.

| Method                  | Sensitivity       | Specificity  | Accuracy          |
|-------------------------|-------------------|--------------|-------------------|
| MAMFM + SVM [18]        | 94.08             | 93.64        | 93.83             |
| WE + HBP [19]           | 96.15             | 97.16        | 96.72             |
| DWT + PCA + LS-SVM [20] | 95.86             | 96.48        | 96.21             |
| DWT + PPCA + RF [21]    | 96.01             | 96.70        | 96.40             |
| SWE + DT [22]           | 96.75             | <b>98.30</b> | 97.62             |
| BWT + RKPCA + LR(Our)   | <b>97.12±0.14</b> | 98.25±0.16   | <b>97.76±0.10</b> |

(Bold means the best)

From the data in Table 7, we see that our BWT + RKPCA + LR method achieves the highest sensitivity and accuracy of all six algorithms. For the specificity, our method achieves an average value of 98.25%, slightly lower than the SWE + DT [22] method of 98.30%. It is worthy to note that sensitivity is more important than specificity, since detecting MS can provide early treatment. We can conclude that our method is superior to other five state-of-the-art approaches.

V. CONCLUSION

In this study, our team presents a novel MS detection method on the basis of BWT, RKPCA, and LR. The experiments results showed that this BWT + RKPCA + LR method was superior to five state-of-the-art methods.

In the future, we shall apply our method to brain CT [65], retinal image [66], low-dose X-ray [67], PET, and SPECT. The structure extraction [68] method will also be tested.

CONFLICT OF INTEREST

We have no conflict of interest to disclose, with regard to the subject matter of this paper.

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