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PTA: An Efficient System for Transaction Database Anonymization

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ABSTRACT Several approaches have been proposed to anonymize relational databases using the criterion of *k*-anonymity, to avoid the disclosure of sensitive information by re-identification attacks. A relational database is said to meet the criterion of *k*-anonymity if each record is identical to at least (*k* − 1) other records in terms of quasi-identifier attribute values. To anonymize a transactional database and satisfy the constraint of *k*-anonymity, each item must successively be considered as a quasi-identifier attribute. But this process greatly increases dimensionality, and thus also the computational complexity of anonymization, and information loss. In this paper, a novel efficient anonymization system called PTA is proposed to not only anonymize transactional data with a small information loss but also to reduce the computational complexity of the anonymization process. The PTA system consists of three modules, which are the Pre-processing module, the TSP module, and the Anonymity model, to anonymize transactional data and guarantees that at least *k*-anonymity is achieved: a pre-processing module, a traveling salesman problem module, and an anonymization module. Extensive experiments have been carried to compare the efficiency of the designed approach with the state-of-the-art anonymization algorithms in terms of scalability, runtime, and information loss. Results indicate that the proposed PTA system outperforms the compared algorithms in all respects.

INDEX TERMS Anonymity, TSP, divide-and-conquer, Gray sort, privacy preserving data mining.

I. INTRODUCTION

In recent years, transactional databases have attracted a lot of interest from researchers due to their many real-life applications. Several techniques related to data mining [1], [2], recommender systems [3], [4], and web search personalization [5], [6] have been developed to store, search, access, and analyze information stored in transactional databases. Since transactional data is collected about all aspects of daily life, it may contain sensitive personal information such as information about one's sexual orientation, religion, medical condition, and social insurance number. Hence, if attackers access private information stored in transactional databases, sensitive or confidential information may be leaked, which may lead to serious security threats such as identity theft. Moreover, even if a database is anonymized (e.g. by removing names), sensitive information may still be inferred from non-sensitive information if that information is significantly different for various persons.

In recent decades, developing anonymization methods that satisfy the criteria of *k*-anonymity [7] and *l*-diversity [8] has become an important research topic, to ensure the preservation of privacy when publishing data. The main goal of *k*-anonymity is to prevent re-identification attacks on a relational database, that is to ensure that information stored in an anonymized database cannot be used to re-identify individuals based on their non-sensitive attribute values. A relational database is said to meet the criteria of *k*-anonymity if each record is identical to at least $(k - 1)$ other records in terms of quasi-identifier attribute values. Most of the anonymization techniques for attaining *k*-anonymity first generate equivalence classes of *k* records using Domain Generalization Hierarchies of quasi-identifier attributes such as sex, birth date, and zip code [9]–[11]. Records in each equivalence class are then modified, so that all records share the same quasiidentifier attribute values. Since an equivalence class contains *k* indistinguishable records, the probability that an attacker successfully identify a person is no more than 1/*k* when using *k*-anonymity [12]–[14].

Numerous algorithms have been designed to anonymize transactional data [15]–[18]. However, they are mainly

including some based on the concepts of generaliza-

designed to reduce information loss caused by anonymization. Hence, these approaches remains in some cases vulnerable to re-identification attacks. In this paper, we aim at not only preventing the disclosure of sensitive information in transactional data but also to reduce information loss and the time required to anonymize high dimensional transactional databases. An anonymization system named PTA is proposed, which consists of three modules named the **P**re-processing module, the **T**SP module, and the **A**nonymity module. The proposed system guarantees *k*-anonymity for transactional data. The major contributions of this paper are summarized as follows.

- 1) The challenges raised by the anonymization of highdimensional transactional data are addressed in the developed system by using a divide-and-conquer approach that partition transactions into several segments based on the Hamming distance. Each segment is then individually processed by a designed algorithm named PrimTSP to find the shortest cyclical path that reduces the information loss resulting from anonymization. Because the data is partitioned into segments that are processed independently, the cost of finding the shortest path is considerably reduced.
- 2) The PrimTSP algorithm is proposed to find a shortest cyclical path as a local approximate solution to the Traveling Salesman Problem (TSP). This algorithm is applied to find the most similar consecutive transactions in the database. Furthermore, transactions are sorted by the Gray order to minimize information loss in each segment.
- 3) A new mapping and majority-voting process is developed to find the most similar transactions in each segment. Those are then assigned to the same group based on a symmetric mapping approach. A majority-voting approach is then employed to find the center of each group. Then, groups having the least information loss are selected as equivalence classes and all transactions in each equivalence class are replaced by its center point. Based on the above ideas, the proposed system minimizes information loss.

II. RELATED WORK

Anonymizing data before publication is crucial, otherwise information may be used to identify individuals, and as a result critical personal information may be revealed. Numerous algorithms have been proposed to anonymize databases [19]–[23], to prevent re-identification attacks. A popular criterion for anonymization is *k*-anonymity [7], [9], [11], which states that each record or transaction in a database must be identical to at least $(k - 1)$ other records, where k is a parameter set by the user. In general, techniques for attaining *k*-anonymity construct equivalence classes according to Domain Generalization Hierarchies of quasi-identifier attributes such as sex, birth date, and zip code. Many techniques have been designed to anonymize database and reach *k*-anonymity,

tion [7], [9], [14], suppression [24], [25], clustering [10], [26] and perturbation [11], [16].

Xu *et al.* [14] proposed a generalization-based algorithm to anonymize relational databases using a recoding approach. This approach calculates the utility of each attribute and considers differences between items. Kisilevich *et al.* [24] proposed a new *k*-anonymity method that relies on classification trees and suppression to attain anonymity. This approach suppresses an attribute value in a record if it is highly correlated with the values of sensitive attributes, to ensure anonymity. An advantage of this approach is that the user does not need to provide domain hierarchy trees for the generalization process. Abul *et al.* [26] proposed a novel *k*-anonymity approach based on the concept of co-localization to anonymize databases of moving objects. This approach perturbs the trajectories of moving objects both in terms of space and time to meet the anonymity goal set by the user.

So far, *k*-anonymity techniques have been designed for various types of data. Poulis *et al.* [27] considered the anonymization of Relational-transactiondatasets (RT-datasets), where each record contains both relational attributes and transaction items. Two frameworks were proposed to preserve privacy while minimizing information loss in RT-datasets. Doka *et al.* [28] formulated the problem of maximal-utility *k*-anonymity as a network flow problem to achieve the full potential of heterogeneity and gain higher utility while providing the same privacy guarantee for syntactic data. Wang et al. [29] proposed a novel utility measurement based on graph models. A general *k*-anonymity framework was also designed, which can be used with various utility measures to achieve *k*-anonymity with a small utility loss, for social networks. Furthermore, Chettri and Borah [30] proposed a method called Microaggregation based Classification Tree (MiCT) to achieve *k*-anonymity using the methods of generalization and suppression, for privacy preserving classification of data.

Most approaches for attaining *k*-anonymity are designed for relational data, and hence cannot be directly applied to transactional data. The reason is that if all items (attributes) are considered as quasi-identifiers (QIDs), the problem of anonymization has a very high dimensionality and solving such problem is very expensive. Moreover, if a transactional database is too sparse, the information loss as a result of anonymization will be very high since each transaction is highly different from each other in a sparse database [17]. Xu *et al.* [31] introduced a novel concept to ensure the privacy of transactional data named (*h*, *k*, *p*)-coherence, and designed a greedy algorithm to achieve anonymity while preserving as much sensitive information as possible. Ghinita *et al.* [32] considered the correlation between purchased products to preserve privacy, such that non-sensitive items cannot be used to infer sensitive information. This approach solves the problem of the high dimensionality of

transactional data for anonymization. Wang *et al.* [17] presented a sensitive *k*-anonymity approach to anonymize sensitive attributes, by ensuring that each transaction is identical to at least $(k - 1)$ other transactions. Although this approach provides anonymity for transactional data, it still produces a high information loss since highly similar transactions are replaced by the center point of each equivalence class. Xue *et al.* [18] proposed an algorithm to transform each set-valued record into a bitmap for generalizing the QIDs in a non-reciprocal recoding way. This method successfully reduces information loss but increases the risk of privacy disclosure since the original data may not be wellanonymized and hence sensitive information may still be revealed. Besides, this approach uses a genetic algorithm to find the set of transactions to anonymize, which can lead to long execution times and has a high complexity. Hsu and Tsai [33] proposed the *k*-anonymity of multipattern (KAMP) problem to protect data from re-identification using an hybrid approach, which aims at satisfying the *k*-anonymity of individual patterns. Although this approach uses a perturbation technique to hide sensitive information, there remains a risk that individuals may be re-identified.

III. PRELIMINARIES AND PROBLEM STATEMENT

A set-valued dataset (a transactional database) is a set of transactions denoted as $D = \{T_1, T_2, \ldots, T_n\}$, where *n* is the number of transactions. Let $I = \{I_1, I_2, \ldots, I_d\}$ be the set of all items occurring in the dataset, where $d = |I|$ is the number of distinct items. Furthermore, let there be a set of sensitive items *SI* denoted as $SI = \{s_1, s_2, \ldots, s_m\}$ such that *SI* \subseteq *I*. Let the non-sensitive items in *I* be called the quasiidentifier items, defined as the set $QID = I - SI$, containing $m - d$ items.

TABLE 1. A transactional database.

The set-valued database that will be used to illustrate definitions in this paper is shown in Table 1, where each transaction represents a person. This database contains non-sensitive items (*QID*), as well as sensitive items (*SI*). If this database is made public or if it is accessed by malicious persons, an important privacy risk is that sensitive information about users may be discovered even if only part of the database is accessed. For example, if a person named Alex knows that his colleague Bob has the symptoms *a*, *b*, and *c*, he can deduce that Bob is the person represented by transaction T_4 , and thus infer the sensitive information that Bob has cancer.

To prevent the re-identification of transactions in a database *D*, as in the above example, the database *D* must be

transformed into a new anonymized database D' that meets the constraint of *k*-anonymity. This later constraint states that each transaction must be identical to at least $(k - 1)$ other transactions. The operations of addition (item generalization) and deletion (item suppression) can be used to achieve this purpose. For example, in Table 1, transactions T_2 , T_3 , and T_4 could be assigned to the same equivalence class and then each of those transactions could be replaced by a transaction (*b*, *c*). Similarly, T_1 , T_5 , and T_6 could be assigned to a same equivalence class and then those transactions could be replaced by the transaction (a, b, d) . The database resulting from this transformation is shown in Table 2.

TABLE 2. A database satisfying 3-anonymity.

The database of Table 2 satisfies the criterion of 3-anonymity since each transaction is identical to at least $(k-1) (= 2)$ transactions.

Definition 1 (k-Anonymity of Transactional Data): A transactional database *D'* satisfies the constraint of *k*-anonymity if every transaction $T_j \in D'$ is identical to at least $(k - 1)$ other transactions in D' . Thus, the probability that a transaction is re-identified is not greater than 1/*k*.

To obtain an anonymized database satisfying the criterion of *k*-anonymity, an anonymization algorithm modifies transactions containing sensitive information so that each transaction becomes identical to at least $k - 1$ other transactions. Hence, the anonymization process introduces differences in the database, which can be considered as the information loss caused by the anonymization process.

Definition 2 (Information Loss, IL): The information loss, denoted as *IL*, is defined as the number of item differences between an anonymized database D' and the corresponding original database *D*. An item difference is an item that has been added, replaced or removed from a transaction.

For example, the *IL* of Table 2 with respect to Table 1 is 4 because there are four item differences between the two databases.

Problem Statement: Let there be a transactional database *D*, where each transaction T_j consists of items that are either non-sensitive items (*QIDs*) or sensitive items (*SI*). The goal of attaining *k*-anonymity is to obtain an anonymized transactional database where 1) transactions containing sensitive information are identical to at least $k - 1$ other transactions, and; 2) the difference between the original database *D* and the anonymized database D' is as small as possible. The parameter *k* is called the anonymity degree, and its value is chosen by the user.

FIGURE 1. Flowchart of the PTA system.

IV. THE PROPOSED PTA ANONYMIZATION SYSTEM

To achieve the goal of *k*-anonymity for transactional data while minimizing information loss, we propose a system called PTA. This system has three modules, which it applies one after the other, to anonymize a database.

The first module is the **pre-processing module**. It treats all items in transactions as quasi-identifier attributes and encodes transactions as bitmaps. Then, it sorts the transactions using the Gray order to ensure that the most similar transactions appear consecutively in the database. This sorting order is used to facilitate the minimization of information loss, thereafter. A divide-and-conquer approach is then applied to group the sorted transactions into several segments. This step is done to reduce the execution time of the second module.

The second module is the **TSP module**. It applies a Traveling Salesman Problem (TSP) solving approach to each segment to find a cyclical loop between transactions (a local approximate solution). This process is applied to reduce the information loss in each segment.

The third module, named the **anonymization module** is applied after the second module. It groups similar transactions according to their similarity into groups. Then, a center point is calculated for each group using a mapping and majority-voting approach. The information loss that would be obtained by replacing all transactions by the center point in each group is then calculated. The group having the least information loss is then considered as an equivalence class. All transactions in that equivalence class are then replaced by its center point. The transactions in the equivalence class thus become identical and a minimal amount of information is lost. This process is repeated to create additional equivalence classes. Then, each transaction that has not been assigned to an equivalence class is then assigned to the most similar equivalence class in terms of the Hamming distance. This process increases anonymity for the database since the constraint of *k*-anonymity only requires that each transaction in an equivalence class is similar to at least $(k - 1)$ identical transactions. The flowchart of the designed PTA anonymization system is illustrated in Fig. 1.

A. THE PRE-PROCESSING MODULE

This module treats all items in a transactional database as QIDs and then encodes the database as bitmaps, where each transaction is a bitmap and each item is encoded using the Gray code [34]. Table 3 shows an example of how the decimal numbers from 0 to 7 are coded with the standard binary representation and with the Gray code.

TABLE 3. A gray coding example.

Then, the bitmaps (transactions) are sorted by Gray code. The result is that similar transactions will appear consecutively, which is desirable to be able to minimize information loss. Note that this Gray sort is only used in the pre-processing phase since consecutive transactions may still be very different according to the Hamming distance measure, even after this sort.

To solve this limitation of the Gray sort for anonymizing transactional data, a divide-and-conquer mechanism is then used to partition the transactions into several segments. The number of segments can be set by the user according to his preferences. Then, for each segment, the TSP module will find the shortest cyclical loop, as it will be described in the next section. The result will be then used by the anonymization module. The divide-and-conquer mechanism is used to reduce the time complexity of the tasks performed by the TSP module. The complexity of the operations performed by the TSP module with or without the divide-and-conquer mechanism is analyzed below.

Complexity Analysis: Assume that the original database *D* contains *n* transactions and that the database is

divided into *m* segments. Thus, the size of each segment is *n*/*m*. For each segment, *n*/*m* cyclical loops are generated by the TSP module. The time complexity for finding each loop is $O((n/m)^2)$. Hence, the time complexity for processing each segment is $O((n/m)^3)$, and the time complexity for processing the whole original database is $O(m \times (n/m)^3) = O(n^3/m^2)$. If the divide-and-conquer mechanism is not used, the time complexity for processing the whole original database is $O(n^3)$. Therefore, when $m \geq 2$, the divide-and-conquer mechanism can reduce the time complexity and increase the efficiency of the designed approach.

Definition 3: Assume that the original database is denoted as *D*, and that the database encoded as bitmaps and sorted by the Gray order is denoted as *sortD*.

Definition 4: The proposed anonymization process assumes that *sortD* is divided into *m* segments, each denoted as *seg*_l, where *m* is set by the user, and $1 \le l \le m$.

Besides the above operations, the pre-processing module also builds an adjacency matrix of transactions for each segment. This matrix is built using the Hamming distance as measure of the similarity between transactions in each segment. The Hamming distance is defined as:

$$
hd(TiQID, TjQID) = TiQID \oplus TjQID,
$$
 (1)

where ''⊕'' denotes the XOR operator, and *TiQID*, *TjQID* respectively denotes the QID part of *Tⁱ* and *T^j* .

The adjacency matrix of each segment is used by the TSP module for finding the shortest cyclical path to minimize information loss in a segment.

B. THE TSP MODULE

This module applies an approximate algorithm for the TSP problem to find a shortest path between transactions in each segment *seg_l* $(1 \leq l \leq m)$. This allows to minimize information loss in each segment since the distance between consecutive transactions (nodes) is minimized. The pseudocode of the designed algorithm is shown in Algorithm 1.

Definition 5: For a segment *seg^l* , let the adjacency matrix based on the Hamming distance be denoted as G_{seg} ^{(V, E)}, where *V* is the set of transactions in *seg^l* . Furthermore, let the notation $hd(v_i, v_j)$ represents the length of the edge $(v_i \rightarrow v_j) \in E$ between two transactions v_i and v_j according to the Hamming distance.

The designed PrimTSP algorithm (Algorithm 1) takes as input a set of segments, and outputs an optimized cyclical loop for each segment. The algorithm processes each segment individually to find its shortest path using local optimization to minimize information loss (Lines 4 to 27). Each transaction is represented as a vector (node) in G_{seg} [[] V , *E*) and the Hamming distance between vectors is considered as the information loss. For each row in G_{seg} (*V*, *E*), the first transaction of the row is both set to the start (line 8) and destination (Line 9) nodes to find its shortest cyclical loop using a TSP approach (Lines 12 to 24). Thus, an optimized cyclical path that minimizes information loss for each row (transaction) is calculated. The nodes having the least

Algorithm 1 PrimTSP

Hamming distance to either the start node or destination node are then found and will be considered as the next nodes in this path (Lines 15 to 24). This process is then repeated until all nodes (transactions) have been visited. When the algorithm terminates, an optimized cyclical path has been found for each segment, to minimize information loss. The set of loops found for all segments can be considered as a global solution that minimizes information loss (Lines 28 to 29).

C. THE ANONYMIZATION MODULE

In prior work, *k*-anonymity [17] has been achieved by finding the center point of each group (segment) and then replacing

each group member (transaction) by that center point. However, performing this in the context of this paper is not a trivial task since information loss must be taken into account, and the choice of center points directly influences information loss.

The proposed solution to this problem is the following. By applying the TSP module, an optimized shortest path is obtained for each segment, which minimizes information loss. Each vector (node) in the shortest path is then mapped to several groups using a symmetric mapping approach, which consists of mapping consecutive transactions to the same group for anonymization. A majority-voting approach is then used to find the center point of each group to perform anonymization. After that, the sum of the Hamming distances between all vectors of each group to its center point is calculated to obtain the group total information loss. The detailed procedure for mapping and majority-voting is described in Algorithm 2.

Definition 6 (Group): The structure of each group G_i in a segment is described with three fields: 1).**tidlist:** the IDs of transactions contained in *Gⁱ* ; 2).**data:** the center point of the group; 3).**IL:** the information loss of *Gⁱ* .

In Algorithm 2, the range of the processed vectors (transactions) in a shortest path is used to find the most similar transactions and group them together based on the predefined anonymity degree *k* (Lines 2 to 15). Consecutive transactions in a shortest path are then selected and mapped together as a group. This symmetric mapping procedure ensures that the grouped transactions produce a minimal loss of information. A majority-voting procedure is then applied (Lines 17 to 23) to find the center point of the mapped group and calculate its total information loss (Lines 24 to 25). The result is a set of groups for each segment and a center point for each group.

After the mapping and majority-voting procedure has been applied, the mapped group with the least information loss is then used to create an equivalence class. The transactions in that equivalence class are then replaced by its center point. The other groups are then processed in ascending order of information loss to create additional equivalence classes. This equivalence class building process ensures that each transaction in an equivalence class is identical to at least (*k*−1) other transactions.

Then, each transaction that has not been assigned to any equivalence class is compared with the center points of all equivalence classes. The transaction is then replaced by the center point providing the least information loss. This process increases the anonymity degree of that equivalence class to $(k + m)$, where $m \lt k$) is the number of unassigned transactions that have been added to that class. The pseudo-code of the anonymization algorithm is given in Algorithm 3.

The mapped groups are first discovered (Line 3) and then they are used to find the equivalence classes to perform anonymization. The groups are processed by ascending order of information loss. A group is then chosen to form an equivalence class if no transactions in this group are members of other groups according to the intersection operation

(Lines 6 to 12). Thereafter, each transaction that has not yet been assigned to any equivalence class is assigned to the equivalence class having the most similar center point (Lines 13 to 15). This forward procedure ensures that each transaction in the anonymized database satisfies *k*-anonymity and cannot be re-identified. Each transaction in an equivalence class is then replaced by its center point (Lines 16 to 19) and the information loss is calculated (Line 20). It is thus guaranteed that at least *k*-anonymity is achieved.

V. AN ILLUSTRATED EXAMPLE

An example is provided to illustrate how the designed algorithm is applied, step by step. In this example, suppose that the anonymity degree k is set to 3 and that the number of segments is initially set to 2 (these parameters can be adjusted by the users according to their preferences). Consider the

Algorithm 3 Anonymization

FIGURE 2. Illustration of the transformation and sorting processes.

database depicted in Fig. 2(a), containing thirteen transactions. This database is first transformed into quasi-identifiers and each attribute is represented by a binary value. The resulting database is shown in Fig. 2(b). Then, transformed transactions are sorted by the Gray order. The resulting sorted database is shown in Fig. 2(c).

The divide-and-conquer mechanism is then applied to the sorted database to divide it into segments. The resulting segments are shown in Fig. 3. Segmentation is performed so

Segment TID		QID				SI			TID	QID					SI	
		\boldsymbol{A}	\boldsymbol{B}	C	D	E			Segment		A	B	C	D	E	
seg ₁	T_8	0	0	θ			S_6			$T_{\rm s}$			0		0	\mathbf{S}_2
	T_{3}	0	Ω			J	S,	seg ₂	T_{2}				$\mathbf{0}$	θ	S_2	
	T_{13}	θ				$\overline{0}$	S_{τ}		T.		θ		θ	θ	S_{5}	
	T,	0		θ		$\mathbf 0$	S_1		T_{12}		θ		$\mathbf{0}$		S_5	
	T_{10}	θ		θ		θ	S_2			T ₄		Ω				S_3
	$\rm T_{II}$	0		θ		θ	S_1		T_q		θ	θ	θ		S_7	
	T_6	0		$\mathbf{0}$			S_4									

FIGURE 3. The two segments created from the sorted database.

that each segment can then be independently processed for anonymization. In this section, the first segment is considered to illustrate the anonymization process.

For the first segment, the adjacency matrix based on the Hamming distance (*seg*1) is built. It is depicted in Fig. 4.

T_6
$\overline{2}$
$\overline{2}$
∞

FIGURE 4. The Hamming distance matrix of segment 1.

Each transaction in the first segment is then processed to find its shortest cyclical path using the PrimTSP algorithm. This latter first sets the start and destination nodes of the cyclical loop to transaction T_8 . Recall that the distance between two nodes is considered as the information loss for the purpose of anonymization. In Fig. 4, it can be found that T_3 and T_6 have the least information loss with respect to T_8 since $hd(T_8, T_3) = 1$ and $hd(T_8, T_6) = 1$. Transaction T_3 is first considered as the node preceding the start node T_8 , and hence the start node is set to T_3 . The node that is the closest to the start node is T_{13} . T_6 is still the closest node to the destination node T_8 and $hd(T_8, T_6) = 1 < hd(T_3, T_{13}) = 2$. Thus, T_6 is considered as the node succeeding the destination node T_8 . The destination node is then changed to T_6 . This process is repeated for the other unvisited nodes. When that process ends, the shortest cyclical loop of T_8 has been obtained. This loop is shown in Fig. 5, where numbers above arrows indicate the order used for selecting nodes.

$$
T_{s} \xrightarrow{\textcircled{1}} T_{s} \xrightarrow{\textcircled{2}} T_{1} \xleftarrow{\textcircled{3}} T_{1} \xleftarrow{\textcircled{5}} T_{10} \xleftarrow{\textcircled{4}} T_{1} \xleftarrow{\textcircled{3}} T_{s} \xleftarrow{\textcircled{2}} T_{s}
$$

FIGURE 5. The cyclical loop of transaction τ_8 in the first segment.

The total loss of information for a loop is calculated as the sum of the distances between all nodes in the loop. In this example, the distances between nodes are calculated as $hd(T_8, T_3) = 1$; $hd(T_3, T_{13}) = 2$; $hd(T_{13}, T_{11}) = 1$; $hd(T_{11}, T_{10}) = 0$; $hd(T_{10}, T_1) = 0$; $hd(T_1, T_6) = 1$; $hd(T_6, T_8) = 1$. Hence, the total information loss for this loop is $1 + 2 + 1 + 0 + 0 + 1 + 1 (= 6)$. Each other segment is processed in the same way to find its shortest cyclical path and calculate its information loss. After that, the algorithm finds the cyclical path having the least information loss according to the matrix. This path will then be used by the mapping and majority-voting procedure. In the first segment, the shortest cyclical path is $(T_8, T_6, T_1, T_{10}, T_{11}, T_{13}, T_3)$.

FIGURE 6. The mapped groups, their center points, and their information losses.

After that, transactions in the cyclical path are mapped to several groups. The center point and information loss of each group is calculated. The process of majority-voting is illustrated in Fig. 6(b) for the three transactions 01011, 01010, and 00011. The majority-voting procedure selects the most frequent binary value for each position (attribute). For example, there are two 1 and one 0 in the second position in Fig. 6(b). Thus, the value 1 is the majority and is chosen for the second position. In this example, 0, 1, 0, 1 and 1 are respectively the most frequent values for each of the five positions. Thus, the result of the majority-voting procedure for 01011, 01010 and 00011 is 01011. The result of the mapping and majority-voting procedure for the running example is shown in Fig. $6(a)$.

Then, groups are processed one-by-one by ascending order of information loss. In this example, the group *g*¹⁰ is first processed since its information loss is 0. It is used to create the first equivalence class C_1 . The groups g_1 and g_{11} are then processed. But it is found that there is some overlap as transactions T_1 and T_{10} are in g_1 , and transactions T_{10} and T_{11} are in g_{11} . Thus, these groups are not used to create equivalence classes. Then, the other groups are considered to find a group that has no transaction overlap with other groups. In this example, the group *g*⁸ meet this criterion and is thus selected to create the second equivalence class *C*2. Thus, two equivalence classes are obtained, that is $C_1 = \{T_1,$ T_{10} , T_{11} } and $C_2 = \{T_3, T_8, T_6\}$. However, in segment 1, there is still a transaction (T_{13}) that has not been assigned to any equivalence class. Thus, T_{13} is compared with the center point of each equivalence class and it is assigned to the equivalence class having the most similar center point (that would produce the smallest information loss). Hence, *T*¹³ is assigned to class C_1 . In each equivalence class, transactions

are then replaced by the data contained in the center point. As a result, transactions in each equivalence class become identical. The result for segment 1 is shown in Fig. 7.

				TID	QID	Data	SI
				T_1	B, D	01010	S_1
Class	Tids	Data	IL	T_3	D, E	00011	S_3
C_1	$T_1, T_{10}, T_{11}, T_{13} \mid 01010 \mid$			T_6	D, E	00011	S_4
				T_8	D, E	00011	S_6
C ₂	T_3, T_8, T_6	00011	$\overline{2}$	T_{10}	B, D	01010	S_2
				T_{11}	B, D	01010	S_1
				T_{13}	B, D	01010	S_7

FIGURE 7. The anonymized database (segment 1).

Segment 2 is then processed in the same way. Anonymity is achieved, and in particular for the transactions ${T_1, T_{10}, T_{11}, T_{13}}$, 4-anonymity is obtained.

VI. EXPERIMENTAL EVALUATION

To verify the effectiveness and efficiency of the proposed PTA system, substantial experiments have been conducted on five real-world datasets, namely chess [35], mushroom [35], pumsb [35], connect [35], and accidents [35], and a synthetic dataset named T10I4D100K [36], which was generated using the IBM Quest Synthetic Data Generator. All the algorithms were implemented in Java and experiments were carried out on a personal computer equipped with an Intel Core i3-4160 dual-core processor and 4 GB of RAM, running the 32-bit Microsoft Windows 7 operating system. Parameters and characteristics of the datasets are shown in [35].

The experiments compare the designed approach with the state-of-the-art Gray-TSP algorithm [18] and GSC algorithm [17]. The three algorithms are compared in terms of information loss and runtime for various number of segments *Segs* and various *k* values.

A. EVALUATION OF THE DIVIDE-AND-CONQUER **MECHANISM**

This section assesses the efficiency of the divide-andconquer mechanism, proposed to reduce the runtime of the anonymization process. Results for different *k* values and number of segments are shown in Fig. 8.

In this figure, it can be observed that the number of segments greatly influences the runtime of the proposed algorithm for all *k* values. When the number of segments is increased, the runtime decreases. The reason is that the divide-and-conquer mechanism divides the data into smaller segments that can be anonymized independently. For example, in Fig. 8(c), the runtime is about 600 seconds for 10 segments, and it decreases to 300 seconds when the number of segments is increased to 15. It can also be observed in Fig. 8(f) that the runtime for 50 segments is about 330 seconds, and that it decreases to 80 seconds when the number of segments is raised to 100. Thus, the designed divide-and-conquer mechanism can considerably increase the performance of the proposed anonymization approach.

FIGURE 8. Runtimes for various number of segments and k values. (a) Chess. (b) Mashroom. (c) Pumsb. (d) Connect. (e) Accidents. (f) T10l4D100K.

FIGURE 9. Information loss for various number of segments. (a) Chess. (b) Mashroom. (c) Pumsb. (d) Connect. (e) Accidents. (f) T10l4D100K.

In addition, it can be observed that runtime is not influenced by the value of *k*. The reason is that the time spent by the anonymization module is small compared to the time required for finding a cyclical loop for each segment. However, increasing *k* influences the anonymity degree and the information loss. The results about information loss for various number of segments are shown in Fig. 9, where information loss is expressed as a ratio (the amount of information that has been lost divided by the total amount of information).

In Fig. 9, it can be observed that the number of segments has little influence on information loss. When the number of segments is increased, information loss remains more or less the same. The reason is that the divide-andconquer approach is only used to partition the transactions for the later anonymization process. It is designed to speed up anonymization by dividing the data into segments that can then be anonymized independently. The ratio of information loss rapidly increases when *k* is increased. This is reasonable since when *k* is increased, there are more transactions in each segment or equivalence class, and all transactions in an equivalence class become identical to attain *k* anonymity. Thus, the ratio of information loss increases.

FIGURE 10. Information loss for a fixed k and various number of segments. (a) Chess (k: 15). (b) Mashroom (k: 15). (c) Pumsb (k: 15). (d) Connect (k: 15). (e) Accidents (k: 15). (f) T10l4D100K (k: 15).

FIGURE 11. Information loss for a fixed number of segments and various values of k. (a) Chess (Segs: 60). (b) Mashroom (Segs: 150). (c) Pumsb (Segs: 800). (d) Connect (Segs: 1250). (e) Accidents (Segs: 6000). (f) T10l4D100K (Segs: 1000).

B. INFORMATION LOSS

This section compares the information loss of the proposed PTA system with the state-of-the-art Gray-TSP and GSC algorithms. The parameter k is set to 15, as it is the median value used in previous experiments, and the number of segments is varied. Results are shown in Fig. 10.

In Fig. 10, it can be observed that the designed PTA system performs well on the six datasets. The state-of-the-art GSC algorithm does not apply a divide-and-conquer mechanism for anonymization. Thus, the information loss remains the same when the number of segments is varied. The ratio of

information loss for the proposed PTA system and Gray-TSP algorithm generally decreases when the number of segments is increased. The reason is that when transactions are divided into several segments, transactions in each segment are highly similar. Thus, fewer transformations are needed to modify the transactions in each segment or equivalence class to obtain *k*-anonymity. For example, the information loss for the designed algorithm in Fig. 10(b) and 100 segments is 19.5%, while Gray-TSP obtains about 28%. When the number of segments is increased to 200, the information loss of the proposed PTA system is 19% and the information loss of

FIGURE 12. Runtimes for a fixed k value and various number of segments. (a) Chess (k: 15). (b) Mashroom (k: 15). (c) Pumsb (k: 15). (d) Connect (k: 15). (e) Accidents (k: 15). (f) T10l4D100K (k: 15).

FIGURE 13. Runtimes for a fixed number of segments and various k values. (a) Chess (Segs: 60). (b) Mashroom (Segs: 150). (c) Pumsb (Segs: 800). (d) Connect (Segs: 1250). (e) Accidents (Segs: 6000). (f) T10l4D100K (Segs: 1000).

Gray-TSP decreases to 23%. The GSC algorithm has clearly the worst performance among the three compared algorithms, as it can be observed in Fig. $10(c)$, Fig. $10(e)$, and Fig. $10(f)$. Overall, the proposed PTA system reduces the loss of information for anonymizing datasets. A second experiment was performed to compare information loss for a fixed number of segments, while varying the parameter *k*. Results for the six datasets are shown in Fig. 11. In this experiment, the number of segments used for the six datasets was respectively set to 60, 150, 800, 1,250, 6,000, and 1,000 (the median numbers of segments used in Fig. 10).

It can be observed in Fig. 11 that the proposed PTA system globally has better results than the other two algorithms when *k* is varied. As *k* is increased, the ratio of information loss decreases. This is reasonable since when *k* is increased, more transactions need to be anonymized and transformed into identical transactions for each segment/equivalence class. It can also be seen that the proposed PTA system outperforms the other two algorithms, and that the GSC algorithm generally has the worse performance, such as in Fig. 10(c), Fig. 10(e), and Fig. 10(f). Overall, the value of *k* influences the ratio of information loss, while the number of segments does not have a strong influence on information loss.

C. RUNTIME

In this section, the runtimes of the three algorithms are first compared for a fixed value of *k*, while varying the number of segments, on the same datasets. Results are shown in Fig. 12.

It can be observed in Fig. 12 that the GSC algorithm performs well on all datasets except on the accidents dataset (results shown in Fig. 12(f)). Although the GSC algorithm is sometimes faster than the proposed PTA system, their runtimes are very similar, when the number of segments is varied. The proposed PTA system and the GSC algorithms are both about one to two orders magnitude faster than the Gray-TSP algorithm. For example, in Fig. 12(a), the proposed PTA system requires nearly 10^{-2} seconds while Gray-TSP spends more than $10¹$ seconds for anonymization. The reason is that the Gray-TSP algorithm utilizes a genetic algorithm to calculate the shortest TSP path to anonymize transactions, and the evolutionary process requires a huge amount of time. Results in terms of runtime for a fixed number of segments and various *k* values are shown in Fig. 13.

In general, the proposed PTA system outperforms the Gray-TSP algorithm. But for the chess, mushroom, and pumsb datasets, the proposed PTA system has nearly the same runtime as the GSC algorithm. However, the runtime difference between these algorithms is not huge and the information loss of the GSC algorithm is much greater than the designed system, as it can be observed in Fig. 10. For example, in Fig. 13(b), the runtimes of GSC and the designed system are both less than 10^{-1} seconds, while Gray-TSP exceeds $10¹$ seconds. Besides, the proposed PTA system and the GSC algorithm are one or two orders magnitude faster than the Gray-TSP algorithm, when *k* is varied. When *k* is increased, the runtimes of Gray-TSP and GSC are steady while the runtime of the proposed PTA system is slightly influenced by the value of *k*. In summary, the proposed PTA system can thus achieve better performance than the other two algorithms and the divide-and-conquer mechanism can efficiently reduce the runtime for attaining anonymity.

VII. CONCLUSION

Numerous algorithms have been designed to anonymize relational data. But it is also a critical issue to prevent the disclosure of sensitive information in transactional data. Algorithms that have been proposed for anonymizing transactional data typically produce a high information loss. In this paper, we have presented a novel anonymization system called PTA, which consists of three modules. It anonymized transactional data with a small information loss and it is also very fast compared to the state-of-the-art algorithms for anonymizing transactional data. Substantial experiments have been carried to compare the performance of the designed system to the state-of-the-art algorithms for anonymizing transactional data in terms of runtime and information loss.

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