

## RESEARCH ARTICLE

# Mechanism and Analytical Model for Switching Transient Process in SiC 3L-ANPC Converter

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**ABSTRACT** Silicon carbide three-level active neutral point clamped converters (SiC 3L-ANPC) have emerged as promising solutions for medium-voltage high-capacity applications. However, compared to traditional two-level converters, they exhibit a relatively higher presence of stray parameters. The combined impact of high  $dv/dt$ ,  $di/dt$  and multiple stray parameters during the switching transient process can lead to non-ideal behaviors, including voltage and current overshoots, along with oscillations. These issues contribute to increased switching losses and limitations in power handling. Therefore, a thorough evaluation of the switching transient process becomes imperative to ensure the proper design and protection of 3L-ANPC converters. An analytical model is proposed in this article that accurately characterizes the switching transient process of SiC 3L-ANPC converters. The model is developed based on a comprehensive analysis of the switching transient mechanism. By focusing on specific pivotal moments within the transient process, the model significantly reduces computational time. Moreover, these distinct moments carry explicit physical significance and possess universal applicability. Experimental results validate the effectiveness of the proposed model, showcasing a maximum calculation error of less than 6% for transient overshoots. The insights presented in this article provide guidance for designing circuit parameters in SiC 3L-ANPC converters, aiding in the mitigation of overvoltage issues.

**INDEX TERMS** SiC MOSFET, switching transient, 3L-ANPC, analytical model, parasitic parameters.

## I. INTRODUCTION

In the rapidly advancing realm of power electronics, the silicon carbide (SiC) power devices have revolutionized converter design by offering high switching speeds and minimized switching losses [1], [2]. Concurrently, the three-level active neutral point clamped (3L-ANPC) converter has garnered significant attention owing to its compelling attributes, including low device voltage requirements, superior output power quality, and minimal electromagnetic interference [3], [4], [5]. The SiC 3L-ANPC power converter embodies a dual advantage paradigm. Consequently, it has emerged as a focal point in international research endeavors [6], [7] and stands as a highly competitive solution within the global aviation

sector for medium-voltage, large-capacity, high-performance power converters [8], [9].

However, within the high-speed switching transient process of SiC devices, non-ideal behaviors such as voltage/current overshoots and oscillations have emerged as significant impediments, impeding the enhancement of converter performance. This challenge is particularly prominent in the context of 3L-ANPC converter, where the transient commutation circuit presents notably greater intricacy than that of a two-level circuit. Multiple commutation circuits exhibit coupling, each involving numerous switches, connecting lines, and parasitic parameters, intensifying the severity of switching transient non-ideal behaviors [10]. In contrast to Si IGBT, SiC MOSFET demonstrates distinct characteristics including reduced reverse transfer capacitance and larger output capacitance, leading to elevated  $dv/dt$  and  $di/dt$  and

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exacerbated voltage and current overshoots. These factors contribute to intricate interactions between the switching transient and the parasitic parameters within both the device and circuit, resulting in diverse electromagnetic transient process behaviors. Therefore, it becomes indispensable to understand the processes and the mechanisms of switching transients in SiC 3L-ANPC converters for further elevating the application potential of SiC power devices and facilitating the efficient, high-quality, and highly reliable utilization. Subsequently, efforts should be directed towards managing the short time-scale switching transient behaviors and regulating them within controllable states.

Extensive analysis and research have been dedicated to exploring the switching transient process of the SiC MOSFETs, leading to significant advancements. The majority of research on switching transients has primarily centered around discrete devices [11], [12], [13], [14], switch-diode combination circuits [15], [16], [17], switch-switch combination circuits [18], [19], [20], [21], or two-level converters [22]. However, different articles propose varying hypotheses concerning the current rise and voltage drop stages in SiC MOSFETs. For instance, in [15], the proposition is that during SiC MOSFET turn-on, current increases precede voltage decrease. This perspective suggests that the drain-source voltage remains relatively stable until the current reaches the load current threshold. Conversely, [20] contends that the current rise and voltage drop occur simultaneously and should not be treated as distinct events. Such contrasting viewpoints in assumptions can yield disparate outcomes when modeling switch transients. Furthermore, the intricate topology of the 3L-ANPC circuit exacerbates the divergence between these results.

Several studies have explored the switching transient behavior of SiC 3L-ANPC converters [10], [23], [24], [25]. In [23], an analysis of the commutation circuits of 3L-ANPC converters is conducted, delving into the on and off characteristics of power devices in different commutation circuits. However, the conclusion is derived from double-pulse experiments, lacking the establishment of a corresponding mathematical model and exhibiting a relatively weak theoretical foundation. Reference [24] presents an analytical model for the drain-source overvoltage of SiC MOSFETs in 3L-ANPC converters. Nevertheless, this analytical model is presented in matrix form, making it less intuitive in reflecting the influence of diverse parasitic parameters on voltage overshoot. Both [10] and [25] propose control methods to mitigate the switching transient non-ideal behavior of SiC 3L-ANPC converters, yet there is an absence of analysis on the mechanism behind this non-ideal behavior. Currently, for SiC 3L-ANPC converters, there exists a dearth of a comprehensive analytical model that elucidates the coupling effects between different circuits and establishes the relationship between SiC MOSFET overvoltage, overcurrent, and parasitic parameters.

The predominant approach in current research involves circuit simulation or numerical models. However, these method

lacks intuitive depiction of the coupling between transient voltage/current overshoot and system elements, limiting its applicability in engineering practices. Moreover, short-time scale system-level simulations encounter challenges such as prolonged simulation durations and frequent convergence issues. Hence, it is crucial to investigate the quantitative relationship between the switching transient process and system elements in SiC 3L-ANPC converters. This entails establishing an analytical model of the switching transients and achieving a quantitative evaluation of voltage/current overshoots by directly substituting parameters.

In response to these challenges, this article presents an analytical model aimed at understanding the switching transient process within SiC 3L-ANPC converters, derived from an in-depth comprehension of commutation mechanisms. The proposed model employs a piecewise linearization approach, effectively segmenting the SiC MOSFETs' switch transient process into distinct stages based on the external circuit status. By calculating specific circuit states at certain times, this model accurately forecasts the entire switch transient process, markedly improving computational efficiency. Experimental validation demonstrates the model's efficacy in precisely predicting the switching transient process of the configured SiC 3L-ANPC setup, with a maximum calculation error of less than 6% for transient overshoots. Compared to circuit simulation methods, this proposed model offers a clearer depiction of coupling relationships and significantly enhances calculation speed. This enhancement establishes a robust scientific foundation for subsequent investigations into non-ideal transient behavior of switches and facilitates optimization in design practices.

The rest of this paper is organized as follows. In section II, the commutation mechanism of 3L-ANPC and the generation mechanism of non-ideal behaviors in switching transients are discussed. Then, the analytical model for the switching transient process of SiC 3L-ANPC converters is presented in section III. Analytical and experimental results are given in section IV. Guidance for the design of circuit parameters in SiC 3L-ANPC converters is also offered to facilitate the mitigation of overvoltage issues. Eventually, section V includes the conclusion of this paper.

## II. MODULATION STRATEGY AND NON-IDEAL BEHAVIORS OF SIC 3L-ANPC CONVERTER

Fig. 1 illustrates the schematic diagram of the three-phase 3L-ANPC circuit, where  $S_{Xn}$  ( $X \in (A, B, C)$  and  $n \in (1, 2, \dots, 6)$ ) represents a SiC MOSFET in Kelvin package. Specifically,  $S_{X1}$  and  $S_{X2}$  form the upper bridge arm, while  $S_{X3}$  and  $S_{X4}$  constitute the lower bridge arm, and  $S_{X5}$  and  $S_{X6}$  compose the output bridge arm.  $C_{bank\_1}$  and  $C_{bank\_2}$  represent the bus capacitors, respectively.  $L_{stray\_1}$  and  $L_{stray\_2}$  denote the positive and negative DC bus parasitic inductances, including the parasitic inductance of the neutral line. Furthermore,  $R_{load}$  and  $L_{load}$  represent the load resistance and inductance parameters, respectively. The blue box in the lower left corner indicates the equivalent circuit diagram of

TABLE 1. Typical modulation schemes and switching modes for 3L-ANPC converters.

Modulation Scheme	Output positive voltage (P state)	Output zero voltage (0 state)	Output negative voltage (N state)	Features
Opposite-side Clamping Method	$S_1, S_3, S_5$ are turned on	$S_1, S_3, S_6$ are turned on ( $0^+$ state, used when outputting positive voltage) $S_2, S_4, S_5$ are turned on ( $0^-$ state, used when outputting negative voltage)	$S_2, S_4, S_6$ are turned on	$S_5$ - $S_6$ is a high-frequency switch pair in full cycle complementary with severe uneven heating
Same-side Clamping Method	$S_1, S_3, S_5$ are turned on	$S_2, S_3, S_5$ conducted ( $0^+$ state, used when outputting positive voltage) $S_2, S_3, S_6$ are turned on ( $0^-$ state, used when outputting negative voltage)	$S_2, S_4, S_6$ are turned on	$S_1$ - $S_2$ and $S_4$ - $S_3$ are complementary high-frequency switching pairs in the positive and negative halves, respectively
Full-path Clamping Method	$S_1, S_3, S_5$ are turned on	$S_1, S_3, S_5, S_6$ are turned on	$S_2, S_4, S_6$ are turned on	$S_1$ - $S_2$ - $S_5$ - $S_6$ and $S_4$ - $S_3$ - $S_5$ - $S_6$ are complementary high-frequency switching pairs in the positive and negative halves, respectively, with high switching loss

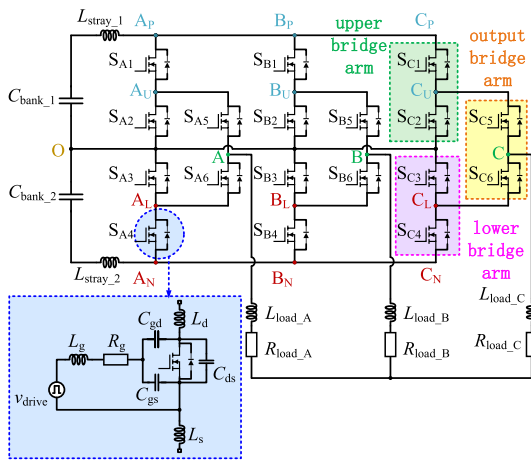


FIGURE 1. Schematic diagram of a three-phase 3L-ANPC converter.

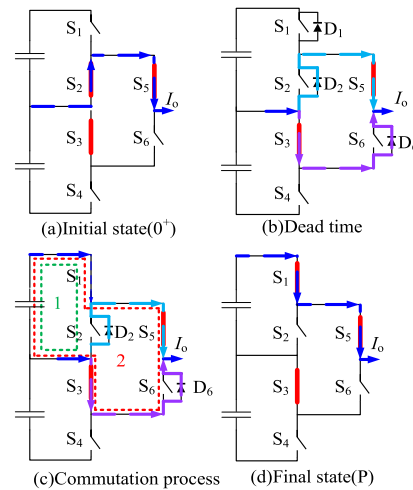


FIGURE 2. Schematic diagram of the commutation from  $0^+$  state to P state by the same-side clamping method.

the SiC MOSFET, taking into account the primary parasitic parameters. This equivalent circuit includes  $R_g$ , which represents the total gate drive resistance, and  $C_{gd}$ ,  $C_{gs}$ , and  $C_{ds}$ , which represent the junction capacitances. Additionally,  $L_d$ ,  $L_s$ , and  $L_g$  correspond to the drain, source, and gate parasitic inductances, respectively. These parasitic inductances incorporate the device lead inductance and external line parasitic inductance.

The 3L-ANPC converter can produce three output levels—positive (P), negative (N), and zero (0)—using four current branches and employing multiple methods for zero level operation [26], [27]. Considering the variations in zero level current paths, three prevalent modulation strategies are commonly employed in 3L-ANPC converters: the opposite-side clamping method, the same-side clamping method, and the full-path clamping method [26], as delineated in Table 1. Notably, in the switching process from the  $0^+$  state to the P state using the opposite-side clamping method,  $S_2$  remains inactive. The load current switches from  $S_3$ - $S_6$  to  $S_1$ - $S_5$ , involving only one commutation loop. Conversely, both the

same-side and full-path clamping methods encompass two simultaneous commutation loops for the same switching transient process. For instance, considering the same-side clamping method illustrated in Fig. 2, the conducting switch is depicted by the red short wire for clarity.

Initially,  $S_2, S_3,$  and  $S_5$  are turned on, while the remaining switches are turned off, directing the load current  $I_0$  through  $S_2$  and  $S_5$ . Assuming that the SiC MOSFET’s on-state resistance is lower than the body diode resistance, the shunt between the body diode of  $S_6$  and  $S_3$  is deemed negligible. The sequential transition from the  $0^+$  state to the P state unfolds in two steps: first,  $S_2$  deactivates, followed by a dead time, after which  $S_1$  activates. When  $S_2$  switches off, the load current divides into two paths:  $D_2$ - $S_5$  and  $S_3$ - $D_6$ , each carrying approximately  $I_0/2$ , as depicted in Fig. 2(b).  $S_1$  activation triggers commutation processes—short loop commutation from  $D_2$  to  $S_1$  and long loop commutation from  $S_3$ - $D_6$  to  $S_1$ - $S_5$ —occurring concurrently, as depicted in Fig. 2(c). These commutation processes are interconnected through variations

**TABLE 2.** Physical meaning of the segmentation points in  $S_{A1}$  turn-on process.

Segmentation Points	Physical Meaning
$t_0$	The gate drive voltage $v_{\text{drive}}$ abruptly changes from $V_L$ to $V_H$
$t_1$	The gate source voltage $v_{\text{gs}, A1}$ reaches the threshold voltage $V_{\text{th}}$
$t_2$	The short commutation loop completes the commutation, i.e. $i_{d, A2}$ reaches 0
$t_3$	The long commutation loop completes the commutation, i.e. $i_{d, A6}$ reaches 0
$t_4$	$v_{\text{ds}, A6}$ beyond $v_{\text{ds}, A2}$
$t_5$	$i_{d, A6}$ reaches 0
$t_6$	$i_{d, A2}$ reaches 0

in  $S_1$  voltage and current, introducing complexity into the 3L-ANPC converter's commutation involving five devices in the bridge arm. This complexity starkly contrasts with the commutation transient of the two-level converter.

When the converter's output current  $I_o > 0$ , the transition from the  $0^+$  state to the P state involves the cutoff of  $D_2$  and  $D_6$ . Consequently,  $S_2$  and  $S_6$  can act as SiC MOSFET output capacitors, causing terminal voltage overshoots and oscillations due to capacitor charge and discharge effects. These charging and discharging currents influence the  $S_1$  branch, resulting in corresponding overshoots and oscillations in its current. Conversely, during the transition from the P state to the  $0^+$  state,  $S_1$  simulates an output capacitor, causing voltage overshoots in  $S_1$  and current overshoots in the  $S_2$  and  $S_6$  branches. When the DC power supply transfers energy to the load via the inverter during the transition from the  $0^+$  state to the P state, the resulting switching transient experiences more pronounced voltage and current overshoots compared to the transition from the P state to the  $0^+$  state. These effects are mirrored during transitions between the N state and  $0^-$  state.

The previously stated conclusion presumes a positive output voltage with the load current exiting the converter. However, in cases involving inductive or capacitive loads, there can be a phase shift between the current and voltage waveforms. This phase difference can alter the occurrence of non-ideal behavior during the switching transient if the output voltage opposes the direction of the load current. For example, consider Fig. 2, where if the load current  $I_o$  flows from the load back into the converter during the  $0^+$  state, the freewheeling stage after  $S_2$  deactivation routes  $I_o$  through the parasitic diode  $D_1$  rather than  $D_2$ . Consequently, transient non-ideal behavior is observed in the voltages of  $S_2$  and  $S_6$ , as well as the current in  $S_1$ . Subsequently, during the  $S_1$  activation process, the commutation occurs solely within  $S_1$ , specifically between the body diode and the MOSFET channel, thereby minimizing evident non-ideal behavior.

### III. ANALYTICAL MODEL FOR SWITCHING TRANSIENT PROCESS IN SiC 3L-ANPC CONVERTER

The analytical model proposed for the SiC 3L-ANPC converter's switching transient process relies on a piecewise

linear model [15]. The methodology involves several key steps: Initially, a thorough understanding of the switching mechanism allows for a logical segmentation of the transient process, enabling approximations of linear changes in voltage and current within defined stages. This segmentation ensures that each transition point holds distinct physical significance. Equivalent transient commutation circuits are formulated for these stages, utilizing Kirchhoff's law to establish a system of differential equations. The subsequent step leverages the linear assumption by substituting  $dv$ ,  $di$ , and  $dt$  with  $\Delta v$ ,  $\Delta i$ , and  $\Delta t$  within each stage. This substitution leads to difference equations, simplifying the definition of the duration  $\Delta t$  for every stage. Solving each stage involves incorporating  $\Delta t$  back into the difference equations, facilitating the derivation of analytical formulas for the final voltage and current values within each stage. Additionally, maintaining the linear assumption enables the derivation of analytical formulas for the voltage and current at specific moments within these stages.

To mitigate errors caused by oversimplification of the nonlinear junction capacitances and transconductance of SiC MOSFETs, this article adopts the junction capacitances and transconductance models proposed in [20]:

$$C_{\text{xss}}(v_{\text{ds}}) = \frac{C_{0\text{xss}} - C_{\text{hxss}}}{1 + (v_{\text{ds}}/V_b)^r} + C_{\text{hxss}}, \quad x = o, i, r \quad (1)$$

$$g_{\text{fs}}(i_{\text{d}}) = k_1 k_2 \left(\frac{i_{\text{d}}}{k_1}\right)^{1-1/k_2} \quad (2)$$

where  $C_{\text{hxss}}$  and  $C_{0\text{xss}}$  represent the capacitance values at high and zero voltages, respectively, and  $V_b$ ,  $r$ ,  $k_1$ , and  $k_2$  need to be fitted based on the device datasheet [28]. The nonlinear capacitance and transconductance values are calculated as the average of integrals within each stage, allowing for a better representation of the dynamic characteristics during the switching transient process in the SiC 3L-ANPC converter.

#### A. TURN-ON MODEL

This section provides a clear focus on deriving the turn-on model, specifically using the turn-on process of  $S_{A1}$  as a detailed example. The schematic diagram displaying voltage and current waveforms is shown in Fig. 3. Traditional studies on SiC MOSFET turn-on processes often segment it

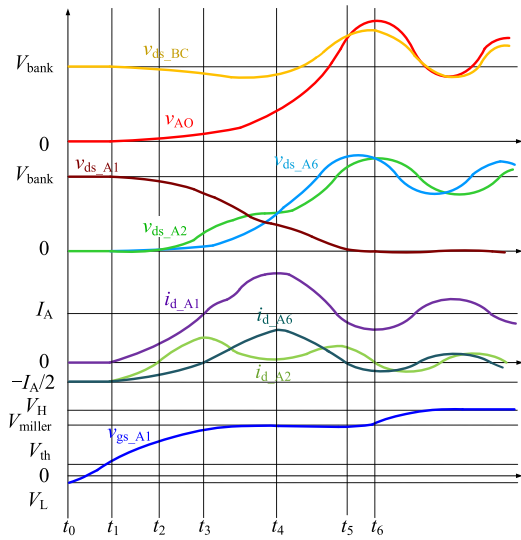


FIGURE 3. Schematic diagram of voltage and current waveforms during the turn-on process of SA1.

into delay, current rise, and voltage drop stages, primarily centered on device behavior. However, within the 3L-ANPC converter, solely relying on SA1’s behavior for stage division is inadequate due to concurrent changes in SA2 and SA6 transitioning from freewheeling to cutoff. Therefore, the proposed analytical model in this article delineates stages based on equivalent circuit changes, considering the overall circuit behavior. The transient process is segmented into 5 stages, with stage 4 further subdivided into 3 sub-stages to refine the segmented linear model. Each segmentation point is defined with explicit physical significance, outlined comprehensively in Table 2.

At  $t_0$ , phase A is in the state depicted in Fig. 2(b), where the load current  $I_A$  is flowing through the branches DA2-SA5 and SA3-DA6. The drain-source voltage  $v_{ds\_A2}(t_0)$  and  $v_{ds\_A6}(t_0)$  can be approximated as the negative value of the renewal diode voltage drop, denoted as  $-V_{DB}$ , and  $v_{ds\_A1}(t_0)$  can be calculated as the difference between the upper bus voltage  $V_{bank}$  and  $v_{ds\_A2}(t_0)$ , i.e.,  $V_{bank} + V_{DB}$ . Each stage’s modeling approach will be described in detail, considering the simplified transient circuit.

**Stage 1** ( $t_0 - t_1$ ): This is the turn-on delay stage. At  $t_0$ , the gate drive voltage of SA1,  $v_{drive}$ , transitions from  $V_L$  to  $V_H$ . Consequently, the gate-source voltage  $v_{gs\_A1}$  starts to increase exponentially from  $V_L$  to the threshold voltage  $V_{th}$ , reaching this threshold at  $t_1$ . In practical engineering, the parasitic inductance  $L_g$  of the gate loop is typically designed to be small, and the rate of change of current  $i_{g\_A1}$  is not significant. Therefore, the impact of  $L_g$  on the switching transient voltage and current can be considered negligible. The transient equivalent circuit of the SA1 gate loop during this stage is illustrated in Fig. 4, where  $C_{iss\_A1}$  represents the input capacitor of SA1.

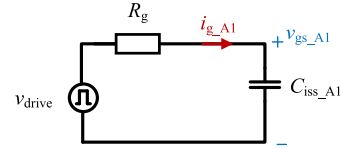


FIGURE 4. Transient equivalent circuit of 3L-ANPC in SA1 turn-on process: Stage 1.

The kinetic model of this stage is shown in (3) and (4):

$$v_{drive} = R_g i_{g\_A1} + v_{gs\_A1} \quad (3)$$

$$i_{g\_A1} = C_{iss\_A1} \frac{dv_{gs\_A1}}{dt} \quad (4)$$

The duration of this stage is solved by combining (3) and (4):

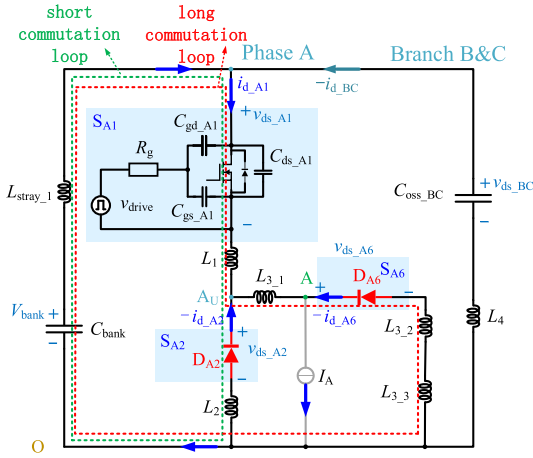
$$t_1 - t_0 = R_g C_{iss\_A1} \ln\left(\frac{V_H - V_L}{V_H - V_{th}}\right) \quad (5)$$

During the turn-on delay stage, the voltage and current on the power circuit maintain the same values as at time  $t_0$ . This means that there is no significant voltage or current variation on the power circuit.

**Stage 2** ( $t_1 - t_2$ ): During this stage, the conductive channel width of SA1 begins to increase, causing a drop in  $v_{ds\_A1}$ . The short commutation loop formed by SA1 and DA2 is synchronized with the long commutation loop formed by SA1, SA5, DA6, and SA3. Assuming that  $I_A$  is equally shared between the two commutation loops at  $t_1$ , and if the parasitic inductance of the long commutation loop is  $m$  times that of the short loop, the commutation rate of the former will be approximately  $1/m$  of that of the latter. At  $t_2$ , the current in the short commutation loop ( $i_{d\_A2}$ ) is fully commuted, while approximately  $1/m$  of the current in long commutation loop ( $i_{d\_A6}$ ) is commuted.

The transient equivalent circuit for this stage is shown in Fig. 5, which includes  $L_1$  and  $L_2$  as the total parasitic inductance of the drain and source of SA1 and SA2, respectively.  $L_{3\_1}$ ,  $L_{3\_2}$ , and  $L_{3\_3}$  represent the total parasitic inductance of the drain and source of SA5, SA6, and SA3, respectively.  $L_4$  represents the parallel equivalent parasitic inductance of the upper half bridge arm of phases B and C.  $L_3$  is defined as the sum of  $L_{3\_1}$ ,  $L_{3\_2}$ , and  $L_{3\_3}$ . The direction of the current flowing into the drain of the SiC MOSFET is defined as the positive direction of the branch current.

The junction capacitances and parasitic inductances in the two commutation loops for phase A are mainly considered in Fig. 5, while ignoring the effect of the on-state resistances of SA3 and SA5. During the turn-on transient of SA1, the inductive voltage on the upper bus inductor  $L_{stray\_1}$  will impact the terminal voltage of the upper bridge arm of phases B and C due to the rapid change of  $i_{d\_A1}$ , and then excite oscillation currents for charging and discharging of their junction capacitors. The majority of the oscillation currents in phases B and C flow directly back to the bus capacitor through the neutral point, having less impact on the lower half bridge arm and the output bridge arm. So only two switches of phases B and C are considered in Fig. 5, respectively.



**FIGURE 5.** Transient equivalent circuit of 3L-ANPC in  $S_{A1}$  turn-on process: Stage 2.

Furthermore, regardless of whether phases B and C are in the P, N,  $0^+$ , or  $0^-$  states, only one SiC MOSFET will be turned on in the upper bridge arm of both phases, while the other one behaves as an output capacitor. In this article, the parallel branches of the upper bridge arms of phases B and C are equivalently represented by a new branch “B&C”, where  $C_{oss\_BC}$  represents the equivalent capacitance of the upper bridge arm branches of phases B and C, approximately twice the output capacitor of SiC MOSFET. The current  $i_{d\_BC}$  represents the total transient current flowing through the upper bridge arms of phases B and C.

The gate current of  $S_{A1}$ ,  $i_{g\_A1}$ , can be expressed by (6) and (7):

$$i_{g\_A1} = \frac{V_H - V_{gs\_A1}}{R_g} \quad (6)$$

$$i_{g\_A1} = C_{iss\_A1} \frac{dv_{gs\_A1}}{dt} - C_{gd} \frac{dv_{ds\_A1}}{dt} \quad (7)$$

The combination of (6) and (7) results in (8):

$$V_H - v_{gs\_A1} = R_g C_{iss\_A1} \frac{dv_{gs\_A1}}{dt} - R_g C_{gd} \frac{dv_{ds\_A1}}{dt} \quad (8)$$

For the short commutation loop, there is:

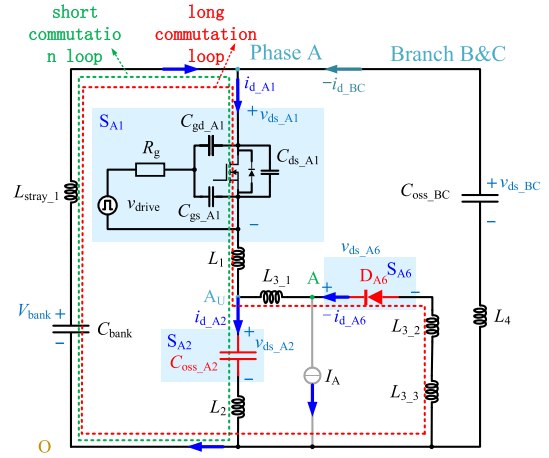
$$V_{bank} = v_{ds\_A1} + (L_1 + L_{stray\_1}) \frac{di_{d\_A1}}{dt} + v_{ds\_A2} + L_2 \frac{di_{d\_A2}}{dt} + L_{stray\_1} \frac{di_{d\_BC}}{dt} \quad (9)$$

For the long commutation loop, there is:

$$V_{bank} = v_{ds\_A1} + (L_1 + L_{stray\_1}) \frac{di_{d\_A1}}{dt} + v_{ds\_A6} + L_3 \frac{di_{d\_A6}}{dt} + L_{stray\_1} \frac{di_{d\_BC}}{dt} \quad (10)$$

For the “B&C” brunch, there are:

$$V_{bank} = v_{ds\_BC} + L_{stray\_1} \frac{di_{d\_A1}}{dt} + (L_4 + L_{stray\_1}) \frac{di_{d\_BC}}{dt} \quad (11)$$



**FIGURE 6.** Transient equivalent circuit of 3L-ANPC in  $S_{A1}$  turn-on process: Stage 3.

$$i_{d\_BC} = C_{oss\_BC} \frac{dv_{ds\_BC}}{dt} \quad (12)$$

For  $S_{A1}$ , there is:

$$v_{gs\_A1}(t_2) = \frac{i_{d\_A1}(t_2) - i_{d\_A1}(t_1)}{g_{fs}} + v_{gs\_A1}(t_1) \quad (13)$$

The quadratic equation with respect to the parameter  $(t_2 - t_1)$  is obtained by combining (8)-(13) and replacing all the differential terms with difference terms (e.g.  $dv_{ds\_A1}$  is replaced by  $v_{ds\_A1}(t_2) - v_{ds\_A1}(t_1)$ ):

$$A_1(t_2 - t_1)^2 + B_1(t_2 - t_1) + C_2 = 0 \quad (14)$$

The solution of (14) provides the duration of stage 2, where the specific parameter values are listed in Table 6 in the Appendix. By substituting the time duration back into (8)-(13), the values of voltage and current at  $t_2$  can be determined. Then, based on the assumption of linearity, the voltage and current at any moment between  $t_1$  and  $t_2$  can be calculated. For example, the analytical formulas of  $i_{d\_A1}$  and  $v_{ds\_A1}$  are as shown in (15) and (16).

$$i_{d\_A1}(t) = \frac{A_1(m+1)I_A}{(-B_1 + \sqrt{B_1^2 - 4A_1C_1})m} (t - t_1) \quad (15)$$

$$v_{ds\_A1}(t) = -\frac{4A_1^2((m+1)(L_1 + L_{stray}) + mL_2)I_A}{(-B_1 + \sqrt{B_1^2 - 4A_1C_1})^2m} (t - t_1) + V_{bank} + V_{DB} \quad (16)$$

**Stage 3** ( $t_2 - t_3$ ): At  $t_2$ ,  $i_{d\_A2}$  reaches 0, and subsequently,  $S_{A2}$  is represented in the transient equivalent circuit as the MOSFET output capacitor  $C_{oss\_A2}$ . As  $C_{oss\_A2}$  charges, the voltage  $v_{ds\_A2}$  gradually increases. Meanwhile,  $D_{A6}$  continues to conduct until  $t_3$ . Fig. 6 illustrates the transient equivalent circuit for this stage.

For  $S_{A1}$ , there is:

$$v_{gs\_A1}(t_3) = \frac{i_{d\_A1}(t_3) - i_{d\_A1}(t_2)}{g_{fs}} + v_{gs\_A1}(t_2) \quad (17)$$

For  $S_{A2}$ , there is:

$$i_{d\_A2} = C_{oss\_A2} \frac{dv_{ds\_A2}}{dt} \quad (18)$$

By combining equations (8)-(12), (17) and (18), and replacing all the differential terms in the equation with difference terms, a quadratic equation with respect to the parameter ( $t_3-t_2$ ) can be derived as follows:

$$A_2(t_3 - t_2)^4 + B_2(t_3 - t_2)^3 + C_2(t_3 - t_2)^2 + D_2(t_3 - t_2) + E_2 = 0 \quad (19)$$

The non-negative real number solution of this equation represents the duration stage 3. The calculation of voltage and current at any moment between  $t_2$  and  $t_3$  follows a similar procedure as the previous stage and does not need to be repeated. The specific parameter values in (19) can be found in Table 6 in the Appendix.

**Stage 4** ( $t_3 - t_6$ ): The transient equivalent circuit for this stage is illustrated in Fig. 7. At  $t_3$ ,  $D_{A6}$  stops freewheeling, and then it can be represented as an output capacitor  $C_{oss\_A6}$ .  $v_{gs\_A1}$  enters Miller platform, while  $v_{ds\_A1}$  continues to decrease, and  $i_{d\_A1}$  exhibits an initial overshoot before entering into oscillation at  $t_4$ . At  $t_3$ ,  $C_{oss\_A2}$  has been charging for some time, while  $C_{oss\_A6}$  has just started charging, resulting in a charge imbalance between them. Since the  $C_{oss\_A2}$  branch and the  $C_{oss\_A6}$  branch are connected in parallel, this charge imbalance leads to mutual charging and discharging behavior, resulting in higher frequency oscillations of  $i_{d\_A2}$  and  $i_{d\_A6}$ . The coupling effect of  $C_{oss\_A2}$  and  $C_{oss\_A6}$  is the most significant difference in switch transient behavior between the 3L-ANPC circuit and the two-level circuit.

In this stage, the behavior of each voltage and current becomes more complex. To enhance the accuracy of the segmented linear model, this stage is further divided into three sub-stages.

**Sub-stage 4.1** ( $t_3 - t_4$ ): The terminal voltage of capacitor  $C_{oss\_A6}$  is approximately zero at  $t_3$ , which gives it a high charge absorption capacity. It not only absorbs charge from the bus capacitor  $C_{bank}$  but also absorbs charge from capacitor  $C_{oss\_A2}$ . As a result, the current  $i_{d\_A2}$  decreases while  $i_{d\_A6}$  increases. As the voltage difference between  $v_{ds\_A2}$  and  $v_{ds\_A6}$  decreases, the rate at which  $C_{oss\_A6}$  absorbs charge from  $C_{oss\_A2}$  slows down. At  $t_4$ ,  $v_{ds\_A2} = v_{ds\_A6}$ , and the charge absorption between them temporarily stops. At this point, the rate of change of currents  $i_{d\_A2}$  and  $i_{d\_A6}$  can be approximated as zero.

**Sub-stage 4.2** ( $t_4 - t_5$ ): Although  $v_{ds\_A2} = v_{ds\_A6}$  at  $t_4$ ,  $i_{d\_A2}$  and  $i_{d\_A6}$  are not equal, indicating that  $C_{oss\_A2}$  and  $C_{oss\_A6}$  are not charging at the same rate. As a result, there is a voltage difference between  $v_{ds\_A2}$  and  $v_{ds\_A6}$  again. This time,  $C_{oss\_A2}$  absorbs charge from  $C_{oss\_A6}$ , leading to an increase in  $i_{d\_A2}$  and a decrease in  $i_{d\_A6}$ . Eventually,  $i_{d\_A6}$  drops to 0 at  $t_5$ , while  $v_{ds\_A6}$  reaches its peak. At  $t_5$ ,  $S_{A1}$  is nearly fully turned on, and as an approximation,  $v_{ds\_A1}$  drops to  $V_{miller} - V_{th}$ .

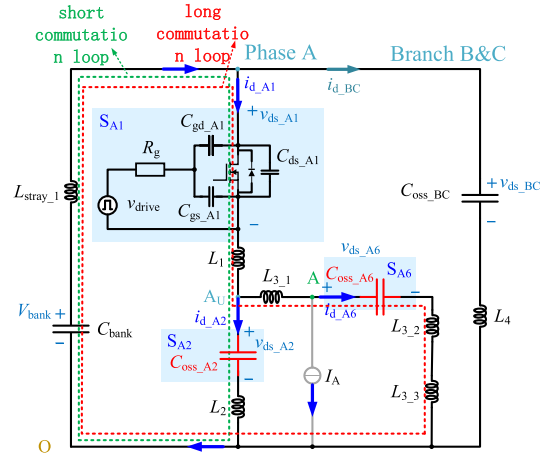


FIGURE 7. Transient equivalent circuit of 3L-ANPC in  $S_{A1}$  turn-on process: Stage 4.

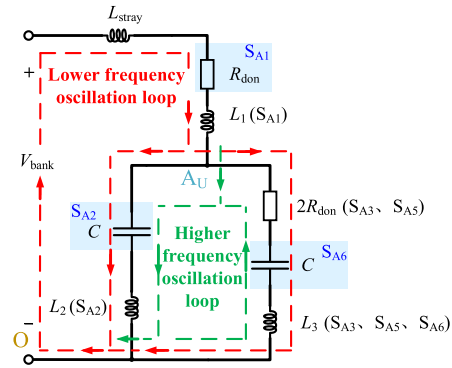


FIGURE 8. Transient equivalent circuit of 3L-ANPC in  $S_{A1}$  turn-on process: Stage 5.

**Sub-stage 4.3** ( $t_5 - t_6$ ): At  $t_6$ ,  $i_{d\_A2}$  drops to 0 and  $v_{ds\_A2}$  reaches its peak. In this article,  $S_{A1}$  is considered fully turned on at  $t_6$ , and  $v_{ds\_A1}$  drops to  $I_A \times R_{don}$ , where  $R_{don}$  represents the on-state resistance of the SiC MOSFET and  $I_A$  is the output current of phase A. Although  $v_{ds\_A6}$  starts to decay and oscillate from  $t_5$ , this article still assumes linearity for  $v_{ds\_A6}$  in this sub-stage to simplify the equation-solving process.

Within the three sub-stages of stage 4, for  $S_{A1}$ , there are:

$$v_{gs\_A1}(t_{k+1}) = \frac{i_{d\_A1}(t_{k+1}) - i_{d\_A1}(t_k)}{g_{fs}} + v_{gs\_A1}(t_k) \quad (k = 3, 4, 5) \quad (20)$$

For  $S_{A6}$ , there is:

$$i_{d\_A6} = C_{oss\_A6} \frac{dv_{ds\_A6}}{dt} \quad (21)$$

Combining (8)-(12), (18), (20), and (21), and replacing all the differential terms in the equation with difference terms, the quadratic equations with respect to the parameters ( $t_4-t_3$ ), ( $t_5-t_4$ ), and ( $t_6-t_5$ ) are obtained:

$$A_k(t_{k+1} - t_k)^4 + B_k(t_{k+1} - t_k)^3 + C_k(t_{k+1} - t_k)^2$$

$$+ D_k(t_{k+1} - t_k) + E_k = 0 (k = 3, 4, 5) \quad (22)$$

The non-negative real number solutions of the equation correspond to the durations of the respective sub-stages. The calculation of voltage and current at any moment between  $t_3$  and  $t_6$  follows a similar procedure as the previous phase and will not be reiterated. The specific parameter values in (22) can be found in Table 6 in the Appendix.

**Stage 5** (after  $t_6$ ): This is the oscillation stage of turn-on process. After  $t_6$ , the gate voltage  $v_{gs\_A1}$  of  $S_{A1}$  continues to exponentially increase to  $V_H$ . The voltages  $v_{ds\_A2}$ ,  $v_{ds\_A6}$ ,  $v_{AO}$ , and  $v_{ds\_BC}$  start to decay and exhibit oscillations.

In order to analyze the oscillation frequency in the complex topology of the 3L-ANPC, this article simplifies the analysis by ignoring the energy exchange between phases. Instead, the focus is placed on the energy exchange between the junction capacitances and the parasitic inductances within each phase. The transient equivalent circuit for the oscillation stage is shown in Fig. 8, where  $C_{oss\_A2} \approx C_{oss\_A6} \approx C$ .

The equivalent impedance of the circuit in Fig. 8 can be represented as:

$$Z_{eq} = \frac{1}{2j\omega C} + j\omega(L_1 + L_{stray\_1} + \frac{L_2 + L_3 - 2\omega^2 L_2 L_3 C}{4 - 2\omega^2(L_2 + L_3)C}) \quad (23)$$

According to (23), a total of four solutions of the resonant frequency can be obtained, of which two negative ones are invalid, and two positive ones are the actual resonant frequency, in (24) and (25), as shown at the bottom of the next page.

Among these frequencies,  $f_1$  is the lower oscillation frequency, resulting from the combination of inductance and capacitance components in the red loop in Fig. 8. The variation direction of each branch current under  $f_1$  is the same. On the other hand,  $f_2$  is a higher oscillation frequency, mainly occurring in the green loop of Fig. 8, with  $S_{A2}$  and  $S_{A6}$  experiencing opposite changes. In Fig. 8, the output voltage  $v_{AO}$  can be approximated as the voltage between point  $A_U$  and point  $O$ , and its oscillation peaks and valleys are primarily determined by  $f_1$ . Part of the higher frequency oscillation current will “leak” into the lower frequency oscillation loop, causing the waveform of  $v_{AO}$  to appear as a non-standard attenuation sine wave. However, the higher frequency vibration amplitude of  $v_{AO}$  is relatively low. Therefore, the output voltage analytical model proposed in this article mainly focuses on considering oscillations with  $f_1$  as the resonant frequency. This choice minimizes the computational complexity of the model while capturing the main oscillation trend effectively.

The equivalent resistance of the circuit in Fig. 8 can be determined as follows:

$$R_{eq} = 2R_{don} \frac{|Z_{2//6}|^2}{|Z_6|^2} + R_{don} \quad (26)$$

where  $Z_6$  represents the total impedance of the  $S_{A6}$  branch, and  $Z_{2//6}$  represents the impedance of the parallel branch consisting of  $S_{A2}$  and  $S_{A6}$ .

Therefore, the expression for  $v_{AO}$  can be obtained as follows:

$$v_{AO} = V_{bank} + (v_{AO(t_6)} - V_{bank})e^{-\frac{R_{eq}}{2L_{eq}}(t-t_6)} \cos(2\pi f_1(t - t_6)) \quad (27)$$

where  $L_{eq}$  refers to the equivalent inductance in (23).

Similarly, the analytical expressions for  $v_{ds\_A2}$ ,  $v_{ds\_A6}$  and  $v_{ds\_BC}$  can be derived using similar methods.

## B. TURN-OFF MODEL

In contrast to the turn-on process, the turn-off process of the 3L-ANPC does not involve a state change of the switching device from the current-continuing diode to the output capacitor. As a result, the number of stages in the turn-off process is relatively small. Fig. 9 illustrates the schematic waveforms of each voltage and current during the turn-off process, using the example of  $S_{A1}$  turn-off.

At  $t_0'$ , phase A is in the P state, and  $I_A$  flows to the load through  $S_{A1}$ - $S_{A5}$ .  $v_{ds\_A1}(t_0')$  is equal to  $R_{don} \times I_A$ , and  $v_{ds\_A2}(t_0')$  and  $v_{ds\_A6}(t_0')$  are equal to the upper bus voltage  $V_{bank}$ . In this article, the turn-off transient process of 3L-ANPC is divided into three stages and the segmentation points are shown in Table 3, all of which also have clear physical meaning.

**Stage 1 ( $t_0' - t_1'$ ):** This is the turn-off delay stage. At  $t_0'$ , the gate drive voltage of  $S_{A1}$   $v_{drive}$  transitions from  $V_H$  to  $V_L$ . Simultaneously, the gate-source voltage  $v_{gs\_A1}$  exponentially decreases from  $V_H$  and reaches the Miller voltage  $V_{miller}$  at  $t_1'$ . During this stage, all other voltages and branch currents on the power side remain unchanged. Therefore, the turn-off delay process can still be described by (3) and (4).

The time duration of this stage is solved by combining (3) and (4), as shown in (28):

$$t_1' - t_0' = R_g C_{iss\_A1} \ln\left(\frac{V_H - V_L}{V_{miller} - V_L}\right) \quad (28)$$

**Stage 2 ( $t_1' - t_2'$ ):** During this stage,  $S_{A1}$  experiences a voltage rise, following the same transient equivalent circuit as shown in Fig. 7. In the drive loop,  $v_{gs\_A1}$  decreases approximately linearly from  $V_{miller}$  to  $V_{th}$ . In the power loop,  $v_{ds\_A2}$  and  $v_{ds\_A6}$  decrease from the upper bus voltage  $V_{bank}$  to approximately 0, while  $v_{ds\_A1}$  increases from  $R_{don} \times I_A$  to its peak value, and  $i_{d\_A1}$  decreases from  $I_A$  to 0. Throughout this stage,  $v_{ds\_A2}$  and  $v_{ds\_A6}$  exhibit significant variations, while the influence of parasitic inductors  $L_2$  and  $L_3$  on the transient behavior is relatively small. Therefore, this article assumes that the currents  $i_{d\_A2}$  and  $i_{d\_A6}$  are equal until  $t_2'$ .

The quadratic equation with respect to the parameter ( $t_2' - t_1'$ ) can be derived by combining (8)-(12), along with (18) and (21), and replacing all the differential terms with their corresponding difference terms:

$$A'_1(t_2' - t_1')^2 + B'_1(t_2' - t_1') + C'_2 = 0 \quad (29)$$

The solution of (29) provides the duration of this stage. Similarly to the turn-on process, this duration is then used



TABLE 3. Physical meaning of the segmentation points in  $S_{A1}$  turn-off process.

Segmentation Points	Physical Meaning
$t_0'$	The gate drive voltage $v_{drive}$ abruptly changes from $V_H$ to $V_L$
$t_1'$	The gate source voltage $v_{gs\_A1}$ reaches the Miller voltage $V_{miller}$
$t_2'$	$i_{d\_A1}$ reaches 0

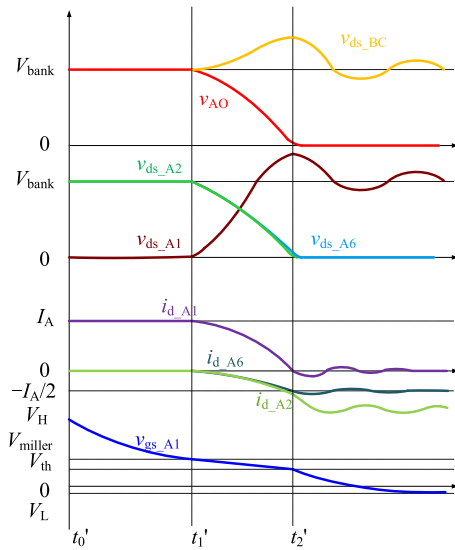


FIGURE 9. Schematic diagram of voltage and current waveforms during the turn-off process of  $S_{A1}$ .

to substitute back into the difference form of the equations, allowing for the determination of the voltages and currents at  $t_2'$ . By assuming linearity, the voltage and current at any moment within this stage can be calculated. The specific parameters in (29) are taken as follows:

$$\begin{cases} A'_1 = (V_L - \frac{V_{miller} + V_{th}}{2}) \\ B'_1 = R_g(C_{gd}V_{bank} - C_{iss\_A1}(V_{th} - V_{miller})) \\ C'_1 = R_g(2L_1 + 2L_{stray} + L_2)C_{gd}I_A \end{cases} \quad (30)$$

**Stage 3 (after  $t_2'$ ):** This is the oscillation stage of turn-off process. The transient equivalent circuit is shown in Fig. 10. In the power loop,  $v_{ds\_A1}$  experiences a significant overshoot and oscillation. On the other hand,  $v_{ds\_A2}$  and  $v_{ds\_A6}$  reach the diode on-state voltages  $-V_{DB}$  after  $t_2'$ , resulting in smaller

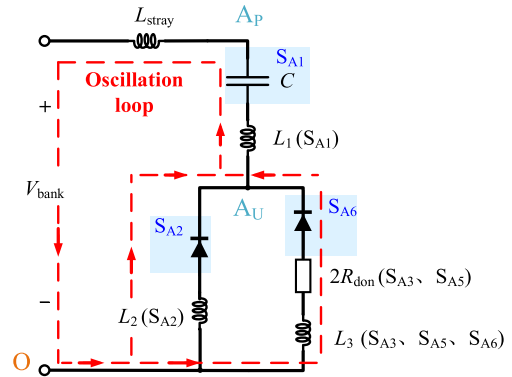


FIGURE 10. Transient equivalent circuit of 3L-ANPC in  $S_{A1}$  turn-off process: Stage 3.

and negligible voltage oscillations. In the drive loop,  $v_{gs\_A1}$  exponentially decreases from  $V_{th}$  to  $V_L$ .

By neglecting the resistance term in Fig. 10, the resonant frequency is determined as follows:

$$f' = \frac{1}{2\pi\sqrt{(L_1 + L_{stray} + \frac{L_2L_3}{L_2+L_3})C}} \quad (31)$$

Then the equivalent resistance is calculated as:

$$R'_{eq} = (2R_{don} + R_{DB})\frac{|Z_{2//6}|^2}{|Z_6|^2} + R_{DB}\frac{|Z_{2//6}|^2}{|Z_2|^2} \quad (32)$$

where  $Z_2$  represents the total impedance of the  $S_{A2}$  branch, and  $R_{DB}$  represents the diode forward conduction resistance.

Hence, the analytical expression for  $v_{ds\_A1}$  can be given as:

$$v_{ds\_A1} = V_{bank} + (v_{ds\_A1}(t_2') - V_{bank})e^{-\frac{R'_{eq}}{2L_{eq}}(t-t_2')} \times \cos(2\pi f'(t-t_2')) \quad (33)$$

Similarly, the analytical expression for  $v_{ds\_BC}$  can be approximated.

$$f_1 = \frac{1}{2\pi}\sqrt{\frac{2(L_1 + L_{stray}) + (L_2 + L_3) - \sqrt{2^2(L_1 + L_{stray})^2 + (L_2 - L_3)^2}}{2C((L_1 + L_{stray})(L_2 + L_3) + L_2L_3)}} \quad (34)$$

$$f_2 = \frac{1}{2\pi}\sqrt{\frac{2(L_1 + L_{stray}) + (L_2 + L_3) + \sqrt{2^2(L_1 + L_{stray})^2 + (L_2 - L_3)^2}}{2C((L_1 + L_{stray})(L_2 + L_3) + L_2L_3)}} \quad (35)$$

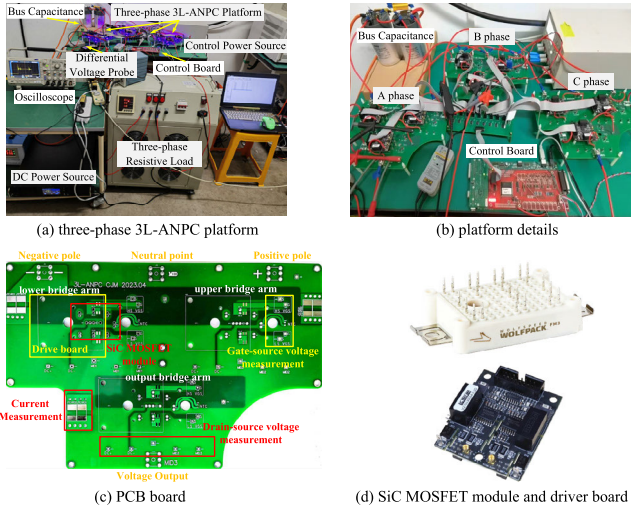


FIGURE 11. Experimental platform of 3L-ANPC converter.

TABLE 4. Circuit parameters.

Parameters	Value	Parameters	Value
$L_{stray}$ /nH	117.5552	$C_{iss}$ /nF	6.6
$L_1$ /nH	15.0279	$C_{oss}$ /nF	0.29~7
$L_2$ /nH	30.9861	$C_{rss}$ /nF	0.019~2.5
$L_3$ /nH	111.1774	$R_g$ / $\Omega$	2
$L_4$ /nH	143.3677	$g_{fs}$ /S	0~10

It should be noted that the analytical model proposed in this article may require slight adjustments based on the actual application scenarios. When the load current or the relationship between  $L_2$  and  $L_3$  changes, the sequence of events may differ slightly from the schematic diagram in Fig. 3. For example,  $v_{ds\_A2}$  may peak after the zero-crossing point of  $i_{d\_A6}$ , resulting in changes in the sequence of  $t_5$  and  $t_6$  in Fig. 3. However, in such cases, the segmentation points of stages can be appropriately adjusted, resulting in a substantial reduction in the calculation error.

#### IV. EXPERIMENTAL VERIFICATION

The three-phase 3L-ANPC platform is designed for experimental verification, as shown in Fig. 11. The SiC MOSFETs CAB016M12FM3 rated at 1200V, 78A from Wolfspeed are used. The parasitic parameters in the circuit are extracted by ANSYS Q3D, as shown in Table 4.

Experiments are carried out under the conditions of  $R_g = 12\Omega$  and  $R_g = 3\Omega$  respectively. The experimental and the analytical results under different operational conditions are compared in Fig. 12 to Fig. 15, when the bus voltage  $2V_{bank} = 700V$  and the load current  $I_A = 10A$ .

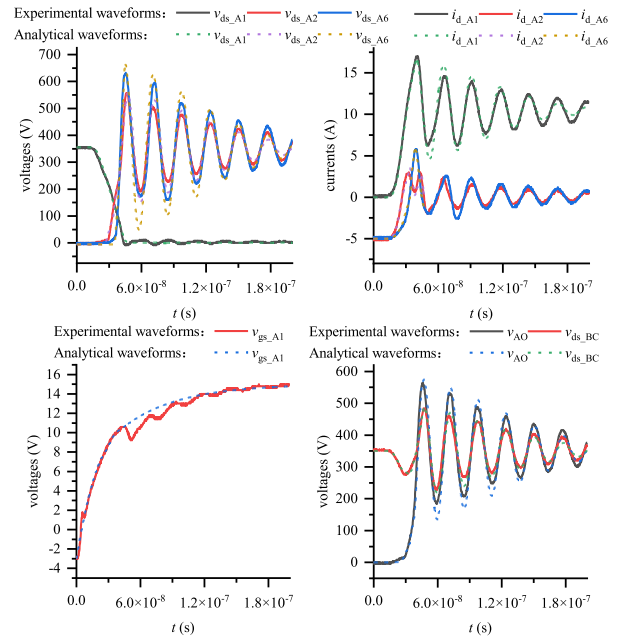


FIGURE 12. Experimental and analytical results in  $S_{A1}$  turn-on process under  $R_g = 12\Omega$ .

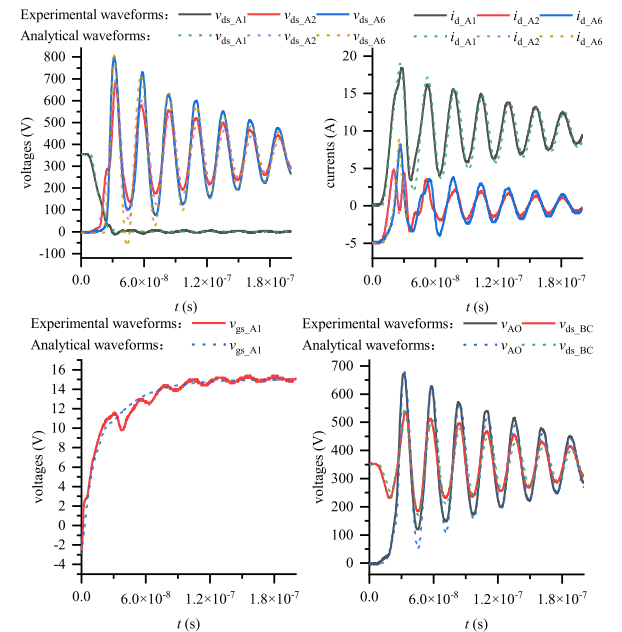


FIGURE 13. Experimental and analytical results in  $S_{A1}$  turn-on process under  $R_g = 3\Omega$ .

Fig. 13 and Fig. 14 present the experimental and analytical waveforms for the  $S_{A1}$  turn-on process, while Fig. 15 and Fig. 16 illustrate the waveforms for the  $S_{A1}$  turn-off process. The assessed voltages and currents encompass  $v_{ds\_A1}$ ,  $v_{ds\_A2}$ ,  $v_{ds\_A6}$ ,  $i_{d\_A1}$ ,  $i_{d\_A2}$ ,  $i_{d\_A6}$ ,  $v_{gs\_A1}$ ,  $v_{AO}$ , and  $v_{ds\_BC}$ , among others. Table 5 provides the calculation errors for each peak, demonstrating that the maximum error is below 6%. The results indicate an agreement between the proposed

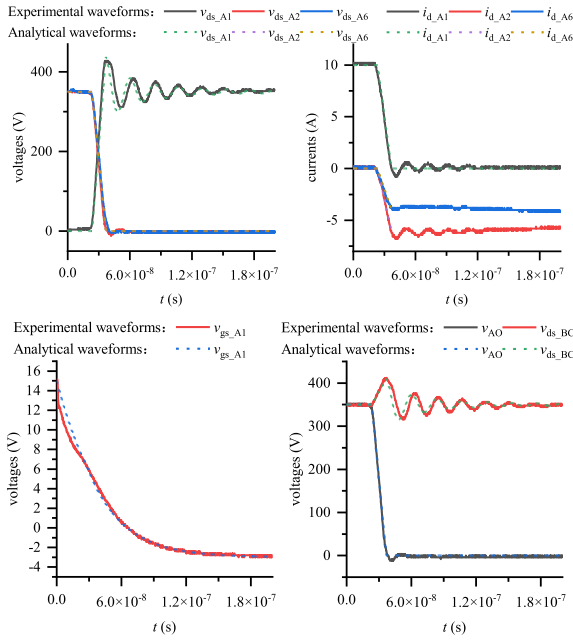


FIGURE 14. Experimental and analytical results in  $S_{A1}$  turn-off process under  $R_g = 12\Omega$ .

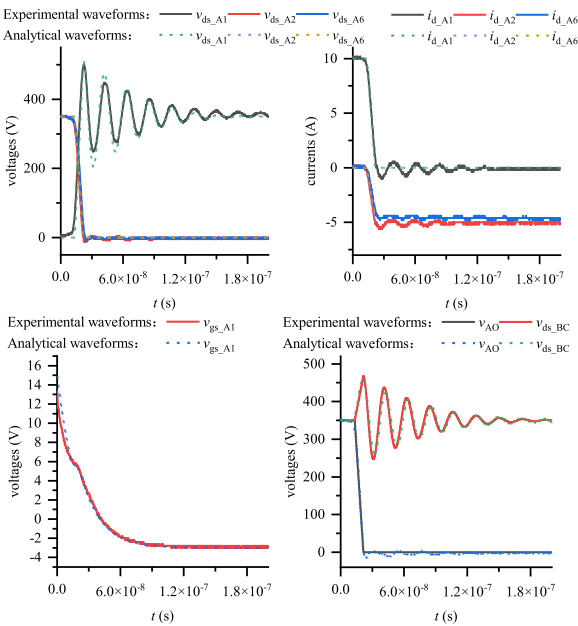


FIGURE 15. Experimental and analytical results in  $S_{A1}$  turn-off process under  $R_g = 3\Omega$ .

analytical model and the experimental findings, affirming the correctness and validity of the proposed model in capturing the switching transient process of the 3L-ANPC. The proposed analytical model offers several significant advantages, including fast calculation speed, intuitive coupling relationships, and easy applicability. For example, when using Pspice for circuit simulation, simulating a fundamental cycle of an aviation 400Hz AC power supply takes approxi-

TABLE 5. Calculation errors.

Parameters	Overshoot Multiplier		Error		
	$R_g = 3\Omega$	$R_g = 12\Omega$	$R_g = 3\Omega$	$R_g = 12\Omega$	
$S_{A1}$ turn-on process	$v_{ds\_A2}/V$	1.897	1.588	2.02%	1.44%
	$v_{ds\_A6}/V$	2.280	1.797	5.22%	4.78%
	$v_{AO}/V$	1.908	1.608	3.23%	1.58%
	$v_{ds\_BC}/V$	1.508	1.374	1.21%	2.11%
$S_{A1}$ turn-off process	$i_{d\_A1}/A$	1.820	1.680	3.33%	3.53%
	$v_{ds\_A1}/V$	1.405	1.211	2.45%	1.87%
	$v_{ds\_BC}/V$	1.322	1.177	4.47%	1.98%

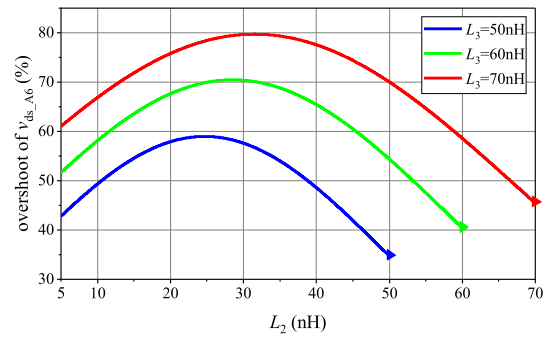


FIGURE 16. Experimental and analytical results in  $S_{A1}$  turn-off process under  $R_g = 3\Omega$ .

mately 28 minutes, with an average of 29 seconds for each switching cycle ( $f_{sw} = 25kHz$ ). On the other hand, the proposed analytical model achieves a computation time of only 0.02 seconds per switching cycle. This represents a substantial improvement in computational efficiency, being approximately 1500 times faster than the circuit simulation.

Furthermore, the experimental results reveal insights regarding the voltage stress and output voltage distortion during the turn-on and turn-off transient processes in the 3L-ANPC converter. Firstly, it is observed that the turn-on transient process causes higher device voltage stress and more severe output voltage distortion compared to the turn-off transient process under the same driving resistance. Additionally, it is found that the voltage stress on the output bridge arm devices is greater than that on the upper and lower bridge arm devices. This is attributed to the fact that the output bridge arm devices are situated in the long commutation loop, where the parasitic inductance is significantly higher. As a result, the impact on the output bridge arm devices is more pronounced.

Significantly, the voltage stress experienced by the output bridge arm device in the 3L-ANPC converter is influenced not only by the parasitic inductance of the long commutation loop but also by the parasitic inductance of the short com-

TABLE 6. Equation coefficients for each stage in turn-on process.

Stage	Equation coefficients
Stage 2	$A_1 = 2g_{fs}V_H - 2g_{fs}V_{gs\_A1(t1)} - I_{d\_A1(t2)}$ (A1)
	$B_1 = -2R_g C_{iss\_A1} i_{d\_A1(t2)}$ (A2)
	$C_1 = -4g_{fs}R_g C_{gd}((L_1 + L_{stray\_1})I_{d\_A1(t2)} + L_2(I_{d\_A2(t2)} - I_{d\_A2(t1)}))$ (A3)
Stage 3	$A_2 = 2g_{fs}V_H - 2g_{fs}V_{gs\_A1(t2)} - I_{d\_A6(t3)}$ (A4)
	$B_2 = -2R_g C_{iss\_A1}(I_{d\_A6(t3)} + I_A - I_{d\_A1(t2)}) - 2g_{fs}R_g C_{gd}(2V_{ds\_A1(t2)} - 2V_{bank} + V_{ds\_A6(t3)} + V_{ds\_A6(t2)})$ (A5)
	$C_2 = 4(2g_{fs}V_H - 2g_{fs}V_{gs\_A1(t2)} - I_A + I_{d\_A1(t2)})L_2 C_{oss\_A2} + 4L_3 C_{oss\_A2} I_{d\_A6(t2)}$ (A6)
	$-4g_{fs}R_g C_{gd}((L_1 + L_{stray\_1})(I_A - I_{d\_A1(t2)}) - L_3 I_{d\_A6(t2)})$ (A6)
	$D_2 = -8R_g C_{iss\_A1} C_{oss\_A2}(L_2(I_A - I_{d\_A1(t2)}) - L_3 I_{d\_A6(t2)})$ (A7)
	$-8g_{fs}R_g L_2 C_{gd} C_{oss\_A2}(2V_{ds\_A1(t2)} - 2V_{bank} + V_{ds\_A6(t3)} + V_{ds\_A6(t2)})$ (A7)
Stage 4	$E_2 = -16g_{fs}R_g C_{gd} C_{oss\_A2}(L_2(L_1 + L_{stray\_1})(I_A - I_{d\_A1(t2)}) - L_3(L_1 + L_{stray\_1} + L_2)I_{d\_A6(t2)})$ (A8)
	$A_3 = -(g_{fs}R_g C_{gd} + C_{oss\_A2} + C_{oss\_A6})(V_{ds\_A6(t3)} - V_{ds\_A2(t3)})$ (A9)
	$B_3 = 4(g_{fs}V_H - g_{fs}V_{gs\_A1(t3)} + I_{d\_A2(t3)})(L_2 C_{oss\_A2} - L_3 C_{oss\_A6}) - 2R_g C_{iss\_A1}(C_{oss\_A2} + C_{oss\_A6})(V_{ds\_A6(t3)} - V_{ds\_A2(t3)}) - 4(g_{fs}R_g C_{gd} + C_{oss\_A2} + C_{oss\_A6})L_2 I_{d\_A2(t3)}$ (A10)
	$C_3 = 4(C_{oss\_A2}V_{ds\_A2(t3)} + C_{oss\_A6}V_{ds\_A6(t3)})(L_2 C_{oss\_A2} - L_3 C_{oss\_A6}) - 4g_{fs}R_g C_{gd}(2V_{ds\_A1(t3)} - 2V_{bank} + V_{ds\_A6(t3)})(L_2 C_{oss\_A2} - L_3 C_{oss\_A6}) - 8R_g C_{iss\_A1}(C_{oss\_A2} + C_{oss\_A6})L_2 I_{d\_A2(t3)} + 8R_g C_{iss\_A1} I_{d\_A2(t3)}(L_2 C_{oss\_A2} - L_3 C_{oss\_A6})$ (A11)
	$-4g_{fs}R_g C_{gd}((L_1 + L_{stray\_1})(C_{oss\_A2} + C_{oss\_A6}) + L_3 C_{oss\_A6})(V_{ds\_A6(t3)} - V_{ds\_A2(t3)}) - 4(g_{fs}R_g C_{gd} + C_{oss\_A2} + C_{oss\_A6})(L_2 C_{oss\_A2} V_{ds\_A2(t3)} - L_3 C_{oss\_A6} V_{ds\_A6(t3)})$ (A11)
	$D_3 = -8R_g C_{iss\_A1}(C_{oss\_A2} + C_{oss\_A6})(L_2 C_{oss\_A2} V_{ds\_A2(t3)} - L_3 C_{oss\_A6} V_{ds\_A6(t3)}) + 8R_g C_{iss\_A1}(C_{oss\_A2} V_{ds\_A2(t3)} + C_{oss\_A6} V_{ds\_A6(t3)})(L_2 C_{oss\_A2} - L_3 C_{oss\_A6}) + 16g_{fs}R_g C_{gd}((L_1 + L_{stray\_1})I_{d\_A2(t3)} + L_3 I_{d\_A6(t3)})(L_2 C_{oss\_A2} - L_3 C_{oss\_A6}) - 16g_{fs}R_g C_{gd}((L_1 + L_{stray\_1})(C_{oss\_A2} + C_{oss\_A6}) + L_3 C_{oss\_A6})L_2 I_{d\_A2(t3)}$ (A12)
	$E_3 = 16g_{fs}R_g C_{gd}(L_1 + L_{stray\_1})(C_{oss\_A2} V_{ds\_A2(t3)} + C_{oss\_A6} V_{ds\_A6(t3)})(L_2 C_{oss\_A2} - L_3 C_{oss\_A6}) + 16g_{fs}R_g L_3 C_{gd} C_{oss\_A6} V_{ds\_A6(t3)}(L_2 C_{oss\_A2} - L_3 C_{oss\_A6}) - 16g_{fs}R_g C_{gd}((L_1 + L_{stray\_1})(C_{oss\_A2} + C_{oss\_A6}) + L_3 C_{oss\_A6})(L_2 C_{oss\_A2} V_{ds\_A2(t3)} - L_3 C_{oss\_A6} V_{ds\_A6(t3)})$ (A13)
	$A_4 = (2g_{fs}V_H - 2g_{fs}V_{gs\_A1(t4)} - I_A + I_{d\_A1(t4)})C_{oss\_A6} - g_{fs}R_g C_{gd} I_{d\_A6(t4)} - (C_{oss\_A2} I_{d\_A6(t4)} - C_{oss\_A6} I_{d\_A2(t4)})$ (A14)
	$B_4 = -2R_g C_{iss\_A1}(C_{oss\_A2} I_{d\_A6(t4)} - C_{oss\_A6}(I_{d\_A6(t4)} + 2I_{d\_A2(t4)})) - 4g_{fs}R_g C_{gd} C_{oss\_A6}(V_{ds\_A1(t4)} - V_{bank} + V_{ds\_A6(t4)})$ (A15)
	$C_4 = 4(2g_{fs}V_H - 2g_{fs}V_{gs\_A1(t4)} - I_A + I_{d\_A1(t4)})L_2 C_{oss\_A2} C_{oss\_A6} - 4C_{oss\_A2} C_{oss\_A6}(L_2 I_{d\_A2(t4)} - L_3 I_{d\_A6(t4)}) - 4g_{fs}R_g C_{gd} C_{oss\_A6}((L_1 + L_{stray\_1})(I_A - I_{d\_A1(t4)}) - L_3 I_{d\_A6(t4)}) - 4g_{fs}R_g L_2 C_{gd} C_{oss\_A2} I_{d\_A6(t4)} - 4g_{fs}R_g(L_1 + L_{stray\_1})C_{gd}(C_{oss\_A2} I_{d\_A6(t4)} - C_{oss\_A6} I_{d\_A2(t4)})$ (A16)
$D_4 = 8R_g(L_2 + L_3)C_{iss\_A1} C_{oss\_A2} C_{oss\_A6} I_{d\_A6(t4)} - 16g_{fs}R_g L_2 C_{gd} C_{oss\_A2} C_{oss\_A6}(V_{ds\_A1(t4)} - V_{bank} + V_{ds\_A6(t4)})$ (A17)	
$E_4 = -16g_{fs}R_g L_2 C_{gd} C_{oss\_A2} C_{oss\_A6}((L_1 + L_{stray\_1})(I_A - I_{d\_A1(t4)}) - L_3 I_{d\_A6(t4)}) - L_3 I_{d\_A6(t4)} - 16g_{fs}R_g(L_1 + L_{stray\_1})C_{gd} C_{oss\_A2} C_{oss\_A6}(L_2 I_{d\_A2(t4)} - L_3 I_{d\_A6(t4)})$ (A18)	
Stage 5	$A_5 = i_{d\_A2(t5)}$ (A19)
	$B_5 = C_{oss\_A2}(2V_{ds\_A1(t5)} - 4V_{bank} + 4V_{ds\_A2(t5)} + 2V_{ds\_A1(t5)})$ (A20)
	$C_5 = -4(L_1 + L_{stray\_1} + L_2)C_{oss\_A2} I_{d\_A2(t5)} + 4(L_1 + L_{stray\_1} + L_3)C_{oss\_A6} I_{d\_A2(t5)}$ (A21)
	$D_5 = 8L_3 C_{oss\_A2} C_{oss\_A6}(V_{ds\_A1(t5)} - 2V_{bank} + 2V_{ds\_A2(t5)} + V_{ds\_A1(t5)}) + 16(L_1 + L_{stray\_1} + L_3)C_{oss\_A2} C_{oss\_A6}(V_{ds\_A2(t5)} - V_{ds\_A6(t5)})$ (A22)
	$E_5 = -16(L_1 L_3 + L_{stray\_1} L_3 + L_1 L_2 + L_{stray\_1} L_2 + L_2 L_3)C_{oss\_A2} C_{oss\_A6} I_{d\_A2(t5)}$ (A23)

mutation loop. Fig. 15 illustrates the relationship between the overshoot percentage of  $v_{ds\_A6}$  (with respect to  $V_{bank}$ ) and the values of  $L_2$  and  $L_3$ . It can be observed that the overshoot of  $v_{ds\_A6}$  is affected by the values of  $L_2$  and exhibits a non-monotonic behavior. Specifically, as  $L_2$  increases, the overshoot of  $v_{ds\_A6}$  initially increases, reaches a maximum value when  $L_2$  is approximately equal to  $L_3/2$ , and then decreases. The minimum voltage overshoot occurs when  $L_2$  is equal to  $L_3$ . Considering the typical design objective of limiting parasitic inductance in a circuit, this article disregards the case where  $L_2$  exceeds  $L_3$ . The findings in Fig. 15 emphasize that the design of the 3L-ANPC converter should not only focus on restricting the parasitic inductance of the commutation loops but also aim to ensure that the values of  $L_2$  and  $L_3$  deviate significantly from the  $L_2 = L_3/2$  relationship. By deviating from this relationship, the voltage overshoot and related stress on the output bridge arm device can be effectively minimized, promoting the reliable operation of the 3L-ANPC converter.

## V. CONCLUSION

In this paper, the switching mechanism of 3L-ANPC converter is investigated. The focus is on analyzing the non-ideal behaviors during switching transients and understanding their generation mechanisms. An analytical model for the switching transient process in SiC 3L-ANPC converter is developed. Based on the theoretical analysis, simulation, and experimental study, the following conclusions have been drawn:

- 1) In the same-side and full-path clamping method employed in the 3L-ANPC converter, both long and short commutation loops are present which introduce additional complexities to the switching transient behavior of the converter. During the switching transient, electromagnetic energy is exchanged not only between the parasitic inductances and junction capacitances within the individual commutation loop but also between the junction capacitances in both commutation loops. This energy transfer between the different elements results in intricate dynamics of voltage and current waveforms across multiple switching devices.
- 2) When comparing the turn-on process with the turn-off process in the 3L-ANPC converter, it is observed that the former results in more severe voltage stress. Furthermore, in the 3L-ANPC topology, the output bridge arm devices experience greater voltage stress compared to the upper and lower bridge arm devices. This is mainly due to their location in the long commutation loop, which exhibits higher parasitic inductance. It is important to note that the voltage stress experienced by the devices in both commutation loops is influenced not only by the parasitic parameters of their respective commutation loops but also by the parasitic parameters of the other commutation loop. This introduces a non-monotonic relationship between the voltage stress and the parasitic parameters. In particular, when the

parasitic inductance of the short commutation loop, represented by  $L_2$ , is approximately equal to half of the parasitic inductance of the long commutation loop, represented by  $L_3$ , it has the greatest influence on the voltage stress of the output bridge arm devices. Therefore, in the design process, it is crucial to deviate from this relationship as much as possible to mitigate the voltage stress on the output bridge arm devices.

- 3) The analytical model proposed in this paper for the switching transient process of SiC 3L-ANPC converters exhibits high accuracy, with a maximum error in peak calculation of less than 6%. In comparison to circuit simulation methods and numerical iterative calculations, the modeling approach presented in this paper offers several advantages. Firstly, it provides clearer and more intuitive coupling relationships between variables, allowing for a better understanding of the system dynamics during switching transients. Additionally, the calculation speed of the proposed model is significantly faster, enabling quick evaluation and analysis of system performance. The analytical model serves as a tool for conducting quantitative assessments of the impact of non-ideal behavior during switching transients on overall system performance. It also facilitates research on methods to suppress such non-ideal behavior, system optimization design, verification of design schemes, determination of safe operating points, and adjustment of protection thresholds. By using the model, design and application processes can be made more informed, reducing the potential for blind design decisions and enhancing the overall efficiency and reliability of the system.

## APPENDIX

See Table 6.

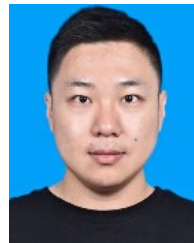
## REFERENCES

- [1] K. Tachiki, T. Ono, T. Kobayashi, and T. Kimoto, "Short-channel effects in SiC MOSFETs based on analyses of saturation drain current," *IEEE Trans. Electron Devices*, vol. 68, no. 3, pp. 1382–1384, Mar. 2021.
- [2] X. Deng, X. Xu, X. Li, X. Li, Y. Wen, and W. Chen, "A novel SiC MOSFET embedding low barrier diode with enhanced third quadrant and switching performance," *IEEE Electron Device Lett.*, vol. 41, no. 10, pp. 1472–1475, Oct. 2020.
- [3] Z. Shen, M. Chen, H. Wang, X. Wang, and F. Blaabjerg, "EMI filter robustness in three-level active neutral-point-clamped inverter," *IEEE Trans. Power Electron.*, vol. 37, no. 4, pp. 4641–4657, Apr. 2022.
- [4] D. Andler, R. Álvarez, S. Bernet, and J. Rodríguez, "Switching loss analysis of 4.5-kV–5.5-kA IGBTs within a 3L-ANPC phase leg prototype," *IEEE Trans. Ind. Appl.*, vol. 50, no. 1, pp. 584–592, Jan. 2014.
- [5] J. Wang, X. Liu, Q. Peng, Y. Xun, S. Yu, N. Jiang, W. Wang, and F. Hou, "Co-reduction of common mode noise and loop current of three-level active neutral point clamped inverters," *IEEE J. Emerg. Sel. Topics Power Electron.*, vol. 9, no. 1, pp. 1088–1103, Feb. 2021.
- [6] H. Liu and T. Zhao, "Optimal gate driving strategy for Si/SiC hybrid switch-based 3L-ANPC inverter with improved output capacity," in *Proc. IEEE Appl. Power Electron. Conf. Exposit. (APEC)*, Phoenix, AZ, USA, Jun. 2021, pp. 741–746.
- [7] Y. Jiao and F. C. Lee, "New modulation scheme for three-level active neutral-point-clamped converter with loss and stress reduction," *IEEE Trans. Ind. Electron.*, vol. 62, no. 9, pp. 5468–5479, Sep. 2015.

- [8] D. Pan, D. Zhang, J. He, C. Immer, and M. E. Dame, "Control of MW-scale high-frequency 'SiC+Si' multilevel ANPC inverter in pump-back test for aircraft hybrid-electric propulsion applications," *IEEE J. Emerg. Sel. Topics Power Electron.*, vol. 9, no. 1, pp. 1002–1012, Feb. 2021.
- [9] F. Diao, X. Du, Z. Ma, Y. Wu, F. Guo, Y. Li, Z. Zhao, and Y. Zhao, "A megawatt-scale Si/SiC hybrid multilevel inverter for electric aircraft propulsion applications," *IEEE J. Emerg. Sel. Topics Power Electron.*, vol. 11, no. 4, pp. 4095–4107, Apr. 2023.
- [10] H. Gui, Z. Zhang, R. Chen, R. Ren, J. Niu, B. Liu, H. Li, Z. Dong, F. Wang, L. M. Tolbert, B. J. Blalock, D. J. Costinett, and B. B. Choi, "A simple control to reduce device over-voltage caused by non-active switch loop in three-level ANPC converters," in *Proc. IEEE Appl. Power Electron. Conf. Exposit. (APEC)*, Anaheim, CA, USA, Mar. 2019, pp. 1337–1343.
- [11] A. Lachichi and P. Mawby, "Modeling of bipolar degradations in 4H-SiC power MOSFET devices by a 3C-SiC inclusive layer consideration in the drift region," *IEEE Trans. Power Electron.*, vol. 37, no. 3, pp. 2959–2969, Mar. 2022.
- [12] S. Hu, M. Wang, Z. Liang, and X. He, "A frequency-based stray parameter extraction method based on oscillation in SiC MOSFET dynamics," *IEEE Trans. Power Electron.*, vol. 36, no. 6, pp. 6153–6157, Jun. 2021.
- [13] V. Talesara, D. Xing, X. Fang, L. Fu, Y. Shao, J. Wang, and W. Lu, "Dynamic switching of SiC power MOSFETs based on analytical subcircuit model," *IEEE Trans. Power Electron.*, vol. 35, no. 9, pp. 9680–9689, Sep. 2020.
- [14] H. Gui, Z. Zhang, R. Chen, J. Niu, L. M. Tolbert, F. Wang, D. Costinett, B. J. Blalock, and B. B. Choi, "Gate drive technology evaluation and development to maximize switching speed of SiC discrete devices and power modules in hard switching applications," *IEEE J. Emerg. Sel. Topics Power Electron.*, vol. 8, no. 4, pp. 4160–4172, Dec. 2020.
- [15] X. Wang, Z. Zhao, K. Li, Y. Zhu, and K. Chen, "Analytical methodology for loss calculation of SiC MOSFETs," *IEEE J. Emerg. Sel. Topics Power Electron.*, vol. 7, no. 1, pp. 71–83, Mar. 2019.
- [16] Y. Wu, S. Yin, H. Li, and W. Ma, "Impact of RC snubber on switching oscillation damping of SiC MOSFET with analytical model," *IEEE J. Emerg. Sel. Topics Power Electron.*, vol. 8, no. 1, pp. 163–178, Mar. 2020.
- [17] Z. Chen, Y. Yao, D. Boroyevich, K. D. T. Ngo, P. Mattavelli, and K. Rajashekar, "A 1200-V, 60-A SiC MOSFET multichip phase-leg module for high-temperature, high-frequency applications," *IEEE Trans. Power Electron.*, vol. 29, no. 5, pp. 2307–2320, May 2014.
- [18] Y. Chen, C. Li, and Z. Lu, "Modeling study of SiC MOSFET crosstalk voltage in half-bridge structure," *Proc. CSEE*, vol. 40, no. 6, pp. 1775–1786, Mar. 2020.
- [19] N. Fritz, G. Engelmann, A. Stippich, C. Lüdecke, D. A. Philipps, and R. W. D. Doncker, "Toward an in-depth understanding of the commutation processes in a SiC MOSFET switching cell including parasitic elements," *IEEE Trans. Ind. Appl.*, vol. 56, no. 4, pp. 4089–4101, Jul. 2020.
- [20] J. Sun, L. Yuan, R. Duan, Z. Lu, and Z. Zhao, "A semiphenomenological analytical model for switching transient process of SiC MOSFET module," *IEEE J. Emerg. Sel. Topics Power Electron.*, vol. 9, no. 2, pp. 2258–2270, Apr. 2021.
- [21] L. Wang, H. Ma, and K. Yuan, "Modeling and influencing factor analysis of SiC MOSFET half-bridge circuit switching transient overcurrent and overvoltage," *Trans. China Electrotechnical Soc.*, vol. 35, no. 17, pp. 3652–3665, Sep. 2020.
- [22] W. Perdikakis, M. J. Scott, K. J. Yost, C. Kitzmiller, B. Hall, and K. A. Sheets, "Comparison of Si and SiC EMI and efficiency in a two-level aerospace motor drive application," *IEEE Trans. Transport. Electrific.*, vol. 6, no. 4, pp. 1401–1411, Dec. 2020.
- [23] Y. Jiao, S. Lu, and F. C. Lee, "Switching performance optimization of a high power high frequency three-level active neutral point clamped phase leg," *IEEE Trans. Power Electron.*, vol. 29, no. 7, pp. 3255–3266, Jul. 2014.
- [24] H. Gui, R. Chen, R. Ren, J. Niu, F. Wang, L. M. Tolbert, D. J. Costinett, B. J. Blalock, and B. B. Choi, "Modeling of multi-loops related device turn-on overvoltage in 3L-ANPC converters," in *Proc. 20th Workshop Control Model. for Power Electron. (COMPEL)*, Toronto, ON, Canada, Jun. 2019, pp. 1–6.
- [25] B. Liu, R. Ren, E. A. Jones, H. Gui, Z. Zhang, R. Chen, F. Wang, and D. Costinett, "Effects of junction capacitances and commutation loops associated with line-frequency devices in three-level AC/DC converters," *IEEE Trans. Power Electron.*, vol. 34, no. 7, pp. 6155–6170, Jul. 2019.
- [26] D. Pan, M. Chen, X. Wang, H. Wang, F. Blaabjerg, and W. Wang, "EMI modeling of three-level active neutral-point-clamped SiC inverter under different modulation schemes," in *Proc. 10th Int. Conf. Power Electron. ECCE Asia (ICPE - ECCE Asia)*, May 2019, pp. 1–6.
- [27] D. Zhang, J. He, and D. Pan, "A megawatt-scale medium-voltage high efficiency high power density," in *Proc. IEEE Energy Convers. Congr. Expo. (ECCE)*, Portland, OR, USA, 2018, pp. 806–813.
- [28] CAB016M12FM3. Pdf. Accessed: Apr. 2022. [Online]. Available: <https://assets.wolfspeed.com/uploads/2021/05/CAB016M12FM3.pdf>



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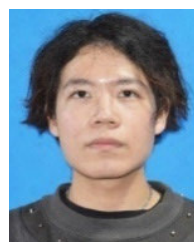
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