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## **APPLIED RESEARCH**

# Reactive Power Controller for Single Phase Dual Active Bridge DC–DC Converters

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**ABSTRACT** In this study, we have proposed a triple-phase shift power-level controller (TPSPC) that achieves zero reactive power generation by fundamental components in a single-phase dual active bridge (DAB) DC-DC converter. The proposed power controller efficiently controls the active and reactive powers independently. The TPSPC regulates the phase shifts between the two H-bridges and inner phase shifts within each bridge to effectively eliminate the reactive power of the fundamental components in the converter. This elimination significantly decreases the inductor current across all load conditions without requiring a multiple mode analysis for the different operational states or any overly complex control functions. Unlike dual-phase shift power-level controllers, the TPSPC uniquely manages each phase shift independently, reducing the inductor current and significantly enhancing the performance. The versatile TPSPC methodology demonstrated in this study is promising for various DAB applications, such as aerospace systems, hybrid electric vehicle charging systems, and the asynchronous interconnection of micro-grids.

**INDEX TERMS** Dual active bridge converter, power-level controller, triple-phase shift.

#### **I. INTRODUCTION**

<span id="page-0-1"></span>The power flow in a dual active bridge (DAB) converter is primarily controlled by varying the phase difference between the voltages of the two H-bridges. The single-phase shift (SPS) modulation is a widely utilized control approach [\[1\]](#page-8-0) in which the direction and magnitude of active power are managed by manipulating the phase difference between two H-bridges. However, this method can result in a high circulating current, primarily when the voltages on the primary and secondary sides are unequal. Several strategies [\[2\],](#page-8-1) [\[3\],](#page-8-2) [\[4\],](#page-8-3) [\[5\],](#page-8-4) [\[6\],](#page-8-5) [\[7\],](#page-8-6) [\[8\]](#page-8-7) to overcome this drawback have been proposed in previous studies; inner phase shifts were added to the SPS method to minimize circulating current or reduce reactive power. Reactive power elimination was initially introduced in [\[9\]; su](#page-8-8)bsequently, a reactive power regulation technique based on a triple-phase shift was proposed in [\[10\],](#page-8-9) [\[11\], a](#page-8-10)nd [\[12\]](#page-8-11) to minimize the circulating current. However, in these methods [\[2\],](#page-8-1) [\[3\],](#page-8-2) [\[4\],](#page-8-3) [\[5\],](#page-8-4) [\[6\],](#page-8-5) [\[7\],](#page-8-6) [\[8\],](#page-8-7) [\[9\],](#page-8-8) [\[10\],](#page-8-9) [\[11\],](#page-8-10) [\[12\], t](#page-8-11)he reactive power was not directly controlled to reduce the inductor current. Instead, these approaches

<span id="page-0-4"></span><span id="page-0-3"></span><span id="page-0-2"></span>The associate editor coordinating the [rev](https://orcid.org/0000-0001-8407-3167)iew of this manuscript and approving it for publication was Zhe Zhang<sup>1</sup>.

<span id="page-0-10"></span><span id="page-0-9"></span><span id="page-0-8"></span><span id="page-0-7"></span><span id="page-0-6"></span><span id="page-0-5"></span><span id="page-0-0"></span>involved meticulous phase-shift signal selection through predefined mode transitions, complex switching table schemes, and gain selections. To address the intricacies associated with mode switching, modulation schemes based on the frequency domain [\[13\],](#page-8-12) [\[14\],](#page-8-13) [\[15\]](#page-8-14) have been introduced to minimize the reactive power. Efforts to minimize or eliminate the reactive power in DAB converters have led to several innovative methods. A variable inductance structure for DAB converters is introduced  $[16]$  to reduce reactive power by adjusting the inductor value and applying phase shift modulation. In [\[17\],](#page-8-16) an artificial intelligence (AI) based scheme utilizing the advanced deep reinforcement learning algorithm minimizes the reactive power in DAB converters. The AI agent optimizes real-time control to achieve the low circulating power between the H-bridges. An unconventional approach in [\[18\]](#page-8-17) employs a sinusoidal pulse width-phase shift modulation scheme with Lagrange's Multiplier Method to reduce reac-tive power and current stress in DAB converters. In [\[19\],](#page-8-18) a proportional-value modulation technique is proposed for the bidirectional reactive current elimination in DAB converters. A frequency-modulated scheme is introduced [\[20\], i](#page-8-19)ncorporating a variable-frequency control algorithm to linearize the nonlinear phase shift angle function to minimize the reactive

power flow. However, these methods indirectly manage reactive power to minimize inductor current and do not eliminate reactive power completely.

<span id="page-1-4"></span>A frequency-domain-based dual-phase shift power-level controller (DPSPC) [\[21\]](#page-9-0) was presented, which offered the ability to directly and independently regulate the active and reactive powers. This approach significantly decreased the inductor current compared with the SPS and dual-phase shift [\[3\]](#page-8-2) methods. However, the DPSPC relied on only two phase shifts as control variables, and the inner phase shift of the secondary H-bridge remained unaltered. This constraint curtailed the potential to optimize the maximum power flow and efficiency under light load conditions.

Therefore, in this study, we introduced a triple-phase shift power-level controller (TPSPC) that eliminates the reactive power of fundamental components irrespective of the connected load. The TPSPC accurately follows the specified power command to regulate the output voltage at each sampling point without requiring multi-mode analysis for different operational states or any overly complex control functions. Notably, the proposed TPSPC methodology significantly reduces the root mean square (rms) inductor current, thereby achieving reductions of up to 51% and 31% compared with the SPS and DPSPC modulation schemes, respectively.

#### **II. MODELING OF SINGLE-PHASE DUAL ACTIVE BRIDGE CONVERTER**

The schematic in Fig. [1](#page-1-0) depicts the circuit configuration of a single-phase DAB converter. The active power flows from the primary to the secondary-side H-bridge inverter through a high-frequency transformer. The voltages of the primary and secondary windings of the transformer are denoted as  $v_{pr}(t)$ and  $v_{sr}(t)$ , respectively.  $V_{in}$  and  $V_{out}$  represent the input and output voltages of the DAB converter, respectively. *L<sup>t</sup>* and  $R_t$  represent the leakage inductance and parasitic resistance of the transformer windings, respectively. The fundamental components of the voltages of the primary and secondary sides, along with the phase shifts between the bridges during one switching cycle in the steady state, are shown in Fig. [2.](#page-1-1) The inner phase shifts of the two inverters are denoted as  $d_1$ and  $d_2$ , respectively, and  $d_3$  represents the phase shift between the voltages of the primary and secondary windings of the transformer. The power flow in the converter is regulated by varying the phase shift  $d_3$  or amplitude of the fundamental component of the two H-bridge inverter voltages with  $d_1$  and *d*<sub>2</sub>, where  $0 \le d_1 \le 1$ ,  $0 \le d_2 \le 1$ , and  $-1 \le d_3 \le 1$ .

The primary and secondary voltages across the transformer windings are mathematically expressed as [\[22\]:](#page-9-1)

$$
v_{pr}(t) = \sum_{n=1,3,5..}^{\infty} \frac{4V_{in}}{n\pi} \cos\left(n\pi \frac{d_1}{2}\right) \sin(n\omega_s t),
$$
 (1a)  

$$
v_{sr}(t) = \sum_{n=1,3,5..}^{\infty} \frac{4V_{out}}{n\pi} \cos\left(n\pi \frac{d_2}{2}\right) \sin(n\omega_s t - n\varphi),
$$
 (1b)

<span id="page-1-0"></span>

**FIGURE 1.** Dual active bridge converter.

<span id="page-1-1"></span>

**FIGURE 2.** Fundamental component analysis.

$$
\varphi = \left(d_3 + \frac{d_2 - d_1}{2}\right)\pi,\tag{1c}
$$

where  $\omega_s$  and  $\varphi$  represent the angular frequency and phase shift of individual fundamental components, respectively.

The AC equivalent circuit of the DAB converter considering only the fundamental components is illustrated in Fig. [3.](#page-1-2)

<span id="page-1-2"></span>

**FIGURE 3.** AC equivalent circuit diagram.

<span id="page-1-5"></span><span id="page-1-3"></span>The fundamental component of current through the inductor is denoted as  $i(t)$ . Since both inverters operate at the same switching frequency, the inductor current and transformer's winding voltages can be seen as rotating vectors  $i$ ,  $v_p$ , and  $v_s$ all rotating at the identical angular speed of  $\omega_s$ . The vector diagram illustrating their relationship is depicted in Fig. [4.](#page-2-0)

The projection of voltages and current in the *dq* rotating reference frame are employed throughout the entire analysis and power controller design in this paper. The primary and secondary voltages  $v_{pdq}(t)$  and  $v_{sdq}(t)$  in the *dq* rotating ref-

<span id="page-2-0"></span>

**FIGURE 4.** Vector Diagram.

erence frame can be given as:

<span id="page-2-3"></span>
$$
\begin{bmatrix} v_{pd}(t) \\ v_{pq}(t) \end{bmatrix} = \frac{4v_{in}(t)}{\pi} \cos\left(\pi \frac{d_1}{2}\right) \begin{bmatrix} \sin\pi d_3 \\ \cos\pi d_3 \end{bmatrix},\tag{2a}
$$

$$
\begin{bmatrix} v_{sd}(t) \\ v_{sq}(t) \end{bmatrix} = \frac{4v_{out}(t)}{\pi} \cos\left(\pi \frac{d_2}{2}\right) \begin{bmatrix} \sin\left(\pi \frac{d_2 - d_1}{2}\right) \\ \cos\left(\pi \frac{d_2 - d_1}{2}\right) \end{bmatrix}, (2b)
$$

where  $v_{in}(t)$  and  $v_{out}(t)$  represent the input voltage of the primary H-bridge inverter and the output voltage of the secondary H-bridge inverter, respectively.

The inductor current in the *dq* rotating reference frame  $i_{Ld}(t)$  and  $i_{Lq}(t)$  can be determined as:

$$
\begin{bmatrix}\ni_{Ld}(t) \\
i_{Lq}(t)\n\end{bmatrix} = \frac{1}{\sqrt{R_t^2 + \omega_s^2 L_t^2}} \begin{bmatrix}\nv_{pq}(t) - v_{sq}(t) \\
v_{sd}(t) - v_{pd}(t)\n\end{bmatrix}.
$$
 (3)

#### **III. TRIPLE-PHASE SHIFT POWER-LEVEL CONTROLLER DESIGN**

A *dq* rotating reference frame is adopted in this study to analyze the converter's instantaneous power. We assumed an imaginary axis orthogonal to the real axis with the same angular frequency. The voltage equations in the *dq* rotating reference frame are mathematically expressed as follows:

$$
\frac{di_{Ld}(t)}{dt} = \frac{1}{L_t} v_{pd}(t) - \frac{1}{L_t} v_{sd}(t) - \frac{R_t}{L_t} i_{Ld}(t) - \omega_s i_{Lq}(t). \tag{4a}
$$

$$
-\frac{di_{Lq}(t)}{dt} = \frac{1}{L_t}v_{pq}(t) - \frac{1}{L_t}v_{sq}(t) - \frac{R_t}{L_t}i_{Lq}(t) + \omega_s i_{Ld}(t).
$$
 (4b)

The instantaneous active and reactive powers supplied from the source through the fundamental components can be mathematically expressed as follows:

<span id="page-2-2"></span>
$$
p(t) = \frac{1}{2} \left( v_{pd}(t) i_{Ld}(t) + v_{pq}(t) i_{Lq}(t) \right).
$$
 (5a)

<span id="page-2-4"></span>
$$
q(t) = \frac{1}{2} \left( v_{pq}(t) i_{Ld}(t) - v_{pd}(t) i_{Lq}(t) \right).
$$
 (5b)

A unique voltage command was obtained in the *dq* rotating reference frame for each sampling time by combining  $(1)$ ,  $(4)$ and  $(5)$ , as follows:

 $v_{pd}^*(k)$ 

$$
=2\left(\frac{i_{Ld}(k)}{i_{Ld}^2(k)+i_{Lq}^2(k)}\right)\left(\begin{array}{c}p^*(k)+\frac{R_tT_s}{L_t}p(k)-\omega_sT_sq(k)\\-\frac{T_s}{2L_t}\left(\begin{array}{c}v_{pd}^2(k)+v_{pq}^2(k)\\-v_{pd}(k)v_{sd}(k)\end{array}\right)\\-2\left(\frac{i_{Lq}(k)}{i_{Lq}^2(k)+i_{Ld}^2(k)}\right)\left(\begin{array}{c}q^*(k)+\frac{R_tT_s}{L_t}q(k)+\omega_sT_sp(k)\\-v_{pq}(k)v_{sq}(k)\end{array}\right)\right)\n\tag{6a}
$$
\n
$$
v_{pq}^*(k)
$$
\n
$$
v_{pq}^*(k)
$$
\n
$$
=2\left(\frac{i_{Lq}(k)}{i_{Ld}^2(k)+i_{Lq}^2(k)}\right)\left(\begin{array}{c}p^*(k)+\frac{R_tT_s}{L_t}p(k)+\omega_sT_sq(k)\\-v_{pq}(k)v_{sd}(k)\end{array}\right)\right),
$$
\n
$$
v_{pq}^*(k)
$$
\n
$$
=2\left(\frac{i_{Lq}(k)}{i_{Ld}^2(k)+i_{Lq}^2(k)}\right)\left(\begin{array}{c}p^*(k)+\frac{R_tT_s}{L_t}p(k)-\omega_sT_sq(k)\\-v_{pq}(k)v_{sd}(k)\\-v_{pq}(k)v_{sd}(k)\end{array}\right)\right)
$$
\n
$$
+2\left(\frac{i_{Ld}(k)}{i_{Lq}^2(k)+i_{Ld}^2(k)}\right)\left(\begin{array}{c}\frac{T_s}{2L_t}\left(\begin{array}{c}v_{pd}(k)+\omega_sT_sp(k)\\-v_{pq}(k)v_{sd}(k)\end{array}\right)\\-\frac{T_s}{2L_t}\left(\begin{array}{c}v_{pd}(k)v_{sd}(k)\\-v_{pq}(k)v_{sd}(k)\end{array}\right)\end{array}\right),
$$

(6b)

where  $T_s$  and the superscript "\*" represent the pulse-width modulation period and corresponding command variables, respectively.

The instantaneous phase angle  $\theta$  of the fundamental component is mainly estimated by the arctangent function method or the synchronous frame method. The synchronous frame method is widely recognized in power electronics for better performance [\[23\]](#page-9-2) and is chosen for angle estimation in this paper. The primary side voltage in  $v_{p\alpha\beta}$  in a stationary reference frame can be easily obtained from the Fourier series representation of voltage from [\(1\)](#page-1-3) as:

<span id="page-2-5"></span>
$$
v_{p\alpha}(t) = \frac{4V_{in}}{\pi} \cos\left(\pi \frac{d_1}{2}\right) \sin\left(\omega_s t + \delta\right). \tag{7a}
$$

$$
v_{p\beta}(t) = \frac{4V_{in}}{\pi} \cos\left(\pi \frac{d_1}{2}\right) \cos\left(\omega_s t + \delta\right). \tag{7b}
$$

<span id="page-2-1"></span>The angle  $\delta$  signifies the phase shift between the voltages of the primary and secondary windings of the transformer. This phase shift can be achieved by either lagging the secondary side voltage or leading the primary side voltage. In this study, the primary side voltage is adjusted to lead, signifying that under typical operating conditions  $\delta$  equals  $d_3$ .

Applying the Park transformation to the voltage signals *vp*<sup>α</sup> and  $v_{p\beta}$ , the voltage components  $\hat{v}_{pd}(t)$  and  $\hat{v}_{pq}(t)$  in the *dq* rotating reference frame can be expressed as:

$$
\begin{bmatrix} \hat{v}_{pd}(t) \\ \hat{v}_{pq}(t) \end{bmatrix} = \begin{bmatrix} \cos(\hat{\theta}) & \sin(\hat{\theta}) \\ -\sin(\hat{\theta}) & \cos(\hat{\theta}) \end{bmatrix} \begin{bmatrix} v_{p\alpha}(t) \\ v_{p\beta}(t) \end{bmatrix},
$$
 (8)

where  $\hat{\theta}$  is the estimated phase angle.

The value of  $v_{pd}$  can be computed using [\(2\).](#page-2-3) The difference between  $v_{pd}$  and  $v^{\wedge}_{pd}$  is employed within the control Proportional-Integral (PI) loop to extract the frequency and phase angle, as illustrated in Fig. [6.](#page-3-0) The estimated frequency can be obtained as:

$$
\hat{\omega}_s(t) = K_p \cdot e(t) + K_i \int e(t)dt + \omega_s(t), \tag{9}
$$

where  $e(t) = v_{pd}(t) - \hat{v}_{pd}(t)$ , and  $K_p$  and  $K_i$  are the gains of the PI controller.

<span id="page-3-1"></span>

**FIGURE 5.** Voltage vector solutions for active and reactive power commands at three different sampling points in dq voltage plane.

<span id="page-3-0"></span>

**FIGURE 6.** Synchronous frame-based angle estimation.

Subsequently, the estimated phase angle can be obtained as:

$$
\hat{\theta}(t) = \int \hat{\omega}_s(t)dt + \hat{\omega}_s(0). \tag{10}
$$

When the error denoted as  $'e(t)$ ' converges to zero, the phase angle difference  $\theta(t) - \hat{\theta}(t)$  will also approach zero. This implies that the actual angle and the estimated angle become identical.

Consequently,  $\theta(t) = \hat{\theta}(t)$ .

The imaginary stationary voltage is always orthogonal to the real axis voltage. Furthermore, the frequency of the fundamental component remains constant under usual operating circumstances and the gains can be easily calculated by ensuring system stability.

The graphical representation delineates the voltage commands at three distinct sampling points during the transient period is depicted in Fig. [5.](#page-3-1) These voltage commands are computed from the intersection of the active and reactive powers in the *dq* voltage plane. The circle defines the physical limit of the DC-link voltage of the converter. The overall control block diagram of the TPSPC is shown in Fig. [7.](#page-3-2)

A Proportional-Integral controller generates an active power command that regulates the output voltage to follow the reference voltage (*Vref* ). Meanwhile, the reactive power generator provides a reactive power command to minimize the inductor current.

<span id="page-3-2"></span>

**FIGURE 7.** Overall control block diagram.

The voltage command  $v_{\text{pdq}}^*$  in [\(6\)](#page-2-4) is converted into a stationary reference frame voltage vector with amplitude *V<sup>m</sup>* and a phase shift  $\psi$  for the required active and reactive power commands.

Consequently, the phase shifts,  $d_1$  and  $d_3$ , for the next sample are obtained as follows:

$$
d_1(k+1) = \frac{2}{\pi} \cos^{-1} \left( \frac{\pi}{4} \cdot \frac{V_m}{V_{in}} \right), \quad (11a)
$$

$$
d_3(k+1) = \frac{\psi}{\pi},\tag{11b}
$$

where  $d_1$  and  $d_3$  are the manipulated inputs of the proposed controller, which effectively controls the active and reactive power independently. This approach eliminates the need for multiple modes of analysis for different operational states and overly complex control functions.

#### **IV. REACTIVE POWER CONTROLLER**

The total active power can be expressed as the sum of fundamental odd frequency components as [\[13\]:](#page-8-12)

$$
P_T = \sum_{n=1,3,5..}^{\infty} P_n
$$
  
= 
$$
\sum_{n=1,3,5..}^{\infty} \frac{8V_{in}V_{out}}{n^3 \pi^2 \omega_s L_t}
$$
  

$$
\left(\cos\left(n\pi \frac{d_1}{2}\right)\cos\left(n\pi \frac{d_2}{2}\right)\sin(n\varphi)\right).
$$
 (12)

The curves to represent different active power components and the total active power are shown in Fig. [8.](#page-4-0) All active power components are normalized using  $P_N = V_{in*}V_{out}/(8*f_{s*}L_t)$ , where  $f_s$  is the switching frequency.

It can be observed that the curve representing the total power achieved by the traditional piecewise linear method which attains a maximum value of 1. Additionally, among all components  $(P_1, P_3, \text{ and } P_5)$ , the fundamental component of active power  $(P_1)$  stands out with the highest amplitude, closely resembling the overall power obtained through the traditional piecewise linear method  $(P_T)$ .

<span id="page-4-0"></span>

**FIGURE 8.** Active power curves of different frequencies component.

The details of the fundamental active and reactive powers are provided in [\[13\]:](#page-8-12)

<span id="page-4-1"></span>
$$
p(t) = \frac{v_1(t) v_2(t) \sin(\varphi)}{\omega_s L_t},
$$
\n(13a)

$$
q(t) = \frac{v_1(t) (v_1(t) - v_2(t) \cos(\varphi))}{\omega_s L_t},
$$
 (13b)

where  $v_1(t) = \frac{4V_{in}}{\sqrt{2\pi}}$  $\frac{V_{in}}{Z_{\pi}}$  cos  $\left(\pi \frac{d_1}{2}\right)$  and  $v_2$  (*t*) =  $\frac{4V_{out}}{\sqrt{2}\pi}$  $\frac{V_{out}}{2\pi}$  cos  $\left(\pi \frac{d_2}{2}\right)$ . The active and reactive components of the inductor current are expressed as follows [\[24\]:](#page-9-3)

<span id="page-4-9"></span><span id="page-4-2"></span>
$$
i_{L\,active}(t) = \frac{v_2(t)\sin(\varphi)}{\omega_s L_t}.
$$
\n(14a)

$$
i_{L\text{ reactive}}(t) = \frac{v_1(t) - v_2(t)\cos(\varphi)}{\omega_s L_t}.
$$
 (14b)

The inductor rms current in discrete time can be obtained from [\(13\)](#page-4-1) and [\(14\)](#page-4-2) as:

$$
i_L(k) = \frac{1}{\omega_s L_t} \sqrt[4]{\begin{pmatrix} v_2^4(k) + 4\omega_s L_t \cdot v_2^2(k) \cdot q(k) \\ -4\omega_s^2 L_t^2 \cdot p^2(k) \end{pmatrix}}.
$$
 (15)

From  $(15)$ , the rms current of the inductor can be effectively controlled by appropriately manipulating  $v_2(k)$  and  $q(k)$  under varying active power requirements. The condition for the minimum value of the inductor current is obtained by taking the partial derivative of  $(15)$  with respect to  $v_2(k)$  and *q*(*k*):

$$
q(k) = 0 \text{ and } v_2(k) = \sqrt{2\omega_s L_t \cdot p(k)}.
$$
 (16)

Consequently, the inner phase shift  $d_2$  is obtained from [\(16\)](#page-4-4) as follows:

$$
d_2(k) = \frac{2}{\pi} \cos^{-1} \left( \sqrt{\frac{\omega_s L_t \cdot p(k)}{4V_{out}^2}} \right).
$$
 (17)

However, in the DPSPC scheme, the inner phase shift of the secondary H-bridge  $d_2$  remained fixed across all load conditions, limiting its potential to achieve higher power flow and efficiency. Conversely, the proposed TPSPC method actively adjusts  $d_2$  based on the active power requirements, as shown in Fig. [9.](#page-4-5)

<span id="page-4-5"></span>

**FIGURE 9.** Inner phase shift  $d_2$  over all load conditions.

The reactive power curves for different load conditions are shown in Fig. [10.](#page-5-0) The symbol '•' denotes instances of zero reactive power at a particular active power demand. The red vertical dashed lines denote the physical constraints on the primary H-bridge voltage. When the voltage required to achieve zero reactive power exceeds the physical limit, the reactive power command is obtained from  $(13)$  and  $(16)$  as follows:

<span id="page-4-7"></span><span id="page-4-6"></span>
$$
q(k) = \frac{v^2(k)}{\omega_s L_t} - \sqrt{\frac{2v^2(k) \cdot p(k)}{\omega_s L_t} - p^2(k)},
$$
 (18)

<span id="page-4-3"></span>where  $v(k)$  is defined as:

$$
v(k) = \frac{1}{2}\sqrt{1 + 4\omega_s^2 L_t^2 \cdot p^2(k)}, \left(0 \le v(k) \le \frac{4V_{in}}{\sqrt{2}\pi}\right). \quad (19)
$$

The necessary maximum leakage inductance  $(L_{max})$  to achieve a zero reactive power of the fundamental components at a given rated power (*Prated* ) can be obtained as follows:

<span id="page-4-8"></span>
$$
L_{max} = \frac{v^2}{\omega_s \cdot P_{rated}}, \quad \text{where } v = \frac{4V_{in}}{\sqrt{2\pi}}.
$$
 (20)

<span id="page-4-4"></span>The reactive power command is obtained by utilizing [\(18\)](#page-4-6) and [\(19\),](#page-4-7) as shown in Fig. [11.](#page-5-1) Suppose the active power

demand is within the physical limit of the primary-side voltage, then [\(18\)](#page-4-6) results in a reactive power command of zero. On the contrary, suppose the active power demand exceeds the physical limit of the input voltage; then, the same equation results in a reactive power command based on the input voltage of the converter.

<span id="page-5-0"></span>

**FIGURE 10.** Reactive power curves with loads.

<span id="page-5-1"></span>

**FIGURE 11.** Block diagram to generate the reactive power command.

#### **V. LOSS ESTIMATION**

The main power losses in a DAB converter can be classified as switching and conduction losses.

#### A. SWITCHING LOSS CALCULATIONS

The switching losses in semiconductor devices are due to continuous switching (ON and OFF) transitions during which a device is simultaneously exposed to high voltage and current. The switching losses (*PSW*\_*on* and *PSW*\_*off* ) in MOSFETs can be determined by:

$$
P_{SW\_on} = \frac{1}{2}V_{DS} \cdot I_{DS} \cdot T_{ON} \cdot f_s, \qquad (21a)
$$

$$
P_{SW\_off} = \frac{1}{2} V_{DS} \cdot I_{DS} \cdot T_{OFF} \cdot f_s, \qquad (21b)
$$

where *VDS* and *IDS* denote the voltage and current at the instant of switching, *f<sup>s</sup>* represents switching frequency, and *TON* and *TOFF* signify the time intervals during the ON and OFF switching events, respectively. It computes the power loss in a single switch during the turn ON and turn OFF switching transition. The cumulative losses for one H-bridge can be determined by multiplying it by 4.

#### B. CONDUCTION LOSS CALCULATIONS

Conduction losses are determined by the root mean square (rms) current  $(I_{Sp}$  rms and  $I_{Ss}$  rms) flowing through the primary and secondary inverters' switches. The rms switch current for primary and secondary side H-bridge inverters can be derived from the inductor's rms current  $(i_L)$  as  $[25]$ :

<span id="page-5-2"></span>
$$
Is_p = \frac{i_L}{\sqrt{2}} \text{ and } Is_s = n \cdot \frac{i_L}{\sqrt{2}},
$$
 (22)

where *n* is the transformer turn ratio.

Usually, high-frequency skin and proximity effects are ignored for power semiconductor devices. Consequently, the switch resistance for the chosen MOSFET(G3R75MT12D) is taken from datasheet values, where *RDS*(*on*) is specified as  $75 \text{ mA}$ . Since there are 4 switches in each H-bridge inverter, the conduction losses can be calculated as follows:

$$
P_{P,cond} = 4R_{DS,on} \cdot (Is_p)^2, \qquad (23a)
$$

$$
P_{S,cond} = 4R_{DS(on)} \cdot (Is_s)^2, \qquad (23b)
$$

where *PP*,*cond* and *PS*,*cond* are the conduction losses of the primary and secondary side H-bridge inverters.

The analysis above clearly indicates that conduction and switching losses exhibit a direct proportionality to the inductor rms current. A reduction in inductor current leads to decreased losses, subsequently contributing to an improvement in overall efficiency.

#### **VI. TEST RESULTS**

The leakage inductance was selected from [\(20\)](#page-4-8) for a 1.5 kW DAB converter, and the performances of the proposed law, SPS, and DPSPC modulation methods were tested on the converter with identical parameters.

#### A. SIMULATION RESULTS

<span id="page-5-3"></span>The DAB converter parameters were computed to satisfy the requirements of an electric vehicle (EV) charging station. Notably, the charging voltage varies for different levels of EV charging systems [\[26\],](#page-9-5) [\[27\]. T](#page-9-6)he charging voltage at a Level-1 charging station ranges between 200-400 V, whereas the mean value of the rectified voltage from a 120 V AC input is approximately 108 V.

The proposed power-level controller was validated using the Matlab Simulink 2022b software. The main parameters of the 1.5 kW EV charging system are as follows:  $R_t = 50$  m $\Omega$ ,  $L_t$  = 33.3  $\mu$ H, switching frequency  $f_s$  = 30 kHz, transformer turn ratio = 1:1, input voltage  $V_{in}$  = 108 V, and output voltage  $V_{out} = 250$  V.

To comprehensively analyze the effect of the TPSPC method, a test is performed at 0.6pu load for comparison with the SPS and DPSPC methods; the results are shown in Fig. [12.](#page-6-0) The obtained waveforms revealed that the inductor current and reactive power for the proposed method are the lowest among the three techniques, despite having an exact active power requirement. The results demonstrate the effectiveness of the TPSPC in minimizing inductor rms current and reactive

power, thus enhancing the overall performance of the converter.

<span id="page-6-0"></span>

**FIGURE 12.** Inductor current and reactive power at 0.6pu load.

The time domain profiles of  $V_{out}$ ,  $p^*$ ,  $p$ ,  $q^*$ ,  $q$ ,  $v_{pdq}^*$ , and *vpdq* arranged sequentially from top to bottom are shown in Fig. [13.](#page-6-1) At first, the converter operated at 0.2pu of the rated load at an output voltage of 250V. At t=50 ms, the connected load increased to full capacity. The TPSPC efficiently maintained the output voltage while concurrently regulating the active and reactive powers.

The inductor rms current across different load conditions is shown in Fig. [14.](#page-6-2) Notably, reductions of up to 51% and 31% were observed in comparison with the conventional SPS and DPSPC control methods, respectively. Efficiency calculations were performed for various loads to assess the efficacy of the TPSPC modulation scheme, as examined in [\[28\].](#page-9-7) As shown in Fig. [15,](#page-6-3) the TPSPC method outperformed the SPS and DPSPC methods, achieving a better performance.

#### B. EXPERIMENTAL RESULTS

A scaled-down laboratory prototype of the DAB converter was built by utilizing TMS320F28335 as the primary controller to demonstrate the effectiveness of the proposed control approach. The experimental setup, including the prototype DAB converter, DC power supplies, DC electronic load, differential probes, a sensor module, and a control board, is shown in Fig. [16.](#page-7-0)

The prototype input and output voltages were 108 V and 250 V, respectively. To minimize the switching losses, a silicon carbide MOSFET (G3R75MT12D) was utilized for the power switches, and the dead time between the switches was fixed at 150 ns for modulation. The inductor size was calculated using [\(20\)](#page-4-8) at a rated power of 350 W.

Table [1](#page-7-1) lists the primary electrical parameters of the experimental setup.

<span id="page-6-1"></span>

<span id="page-6-2"></span>**FIGURE 13.** Results of the TPSPC at 0.2pu and full load.



<span id="page-6-4"></span><span id="page-6-3"></span>**FIGURE 14.** Inductor rms current at different loads.



**FIGURE 15.** Efficiency curves at different loads.

Conventional voltage closed-loop control-based SPS and DPSPC controls were chosen for the comparative experiments to demonstrate the effectiveness of the proposed

<span id="page-7-0"></span>

**FIGURE 16.** Experimental Setup.

<span id="page-7-1"></span>**TABLE 1.** Electrical parameters of the experiment platform.

| <b>Electrical Parameters</b>          | Value   | Unit |
|---------------------------------------|---------|------|
| Rated Power                           | 350     | W    |
| Input/Output Voltage $V_{in}/V_{out}$ | 108/250 | V    |
| Switching Frequency $f_s$             | 30      | kHz  |
| Inductance $L_t$                      | 130     | μH   |
| Capacitance                           | 235     | μF   |
| Dead Time                             | 150     | ns   |

<span id="page-7-2"></span>

<span id="page-7-3"></span>

**FIGURE 18.** Inductor rms current at different loads.

approach more intuitively. The experimental waveform of the inductor current at a steady state for SPS, DPS, and the proposed approach at 0.6pu of the load is illustrated in Fig[.17.](#page-7-2) The current through the inductor was lower at different load

<span id="page-7-4"></span>

**FIGURE 19.** Efficiency curves at different loads.

<span id="page-7-5"></span>

**FIGURE 20.** Control performance of the proposed controller.

levels compared with that of the SPS and DPSPC modulation methods, as shown in Fig. [18.](#page-7-3) To determine the power losses  $(P_d)$  at different operating conditions, the Digital DC Power Supply (Xantrex XDC 300-20) is used to obtain the input voltage and current, facilitating the calculation of input power (*Pin*). The output power (*Pout*) is determined by measuring the output voltage using a differential probe (Teledyne Lecroy HVD3102) with a digital oscilloscope (Lecroy LT374M). The load resistance value is obtained from the DC electronics load (Sorensen SLH-300-12-1200). The losses are subsequently computed using  $P_d = P_{in} - P_{out}$ , and the efficiency

is calculated accordingly. The measurement results closely align with the estimated values. The efficiency under various load conditions is illustrated in Fig. [19.](#page-7-4) The TPSPC method outperforms both SPS and DPSPC methods which demonstrates a better performance.

The control performance of the proposed method on the output voltage regulation for load variation from 0.2pu to full load is shown in Fig. [20.](#page-7-5) On the top, the waveforms of the primary and secondary side transformer winding voltage are displayed along with the zoomed-in waveforms of the inductor current at 0.2pu and 1.0pu loads.

Initially, the converter supplied a load of 70 W at 250 V from a 108 V source. Subsequently, the load suddenly changed to 350 W, whereas the input voltage remained unchanged. The fundamental active and reactive power signals shown in the figure were obtained using the two digital-to-analog channels of the control board. The proposed controller regulated the fundamental active and reactive powers while maintaining the output voltage and minimized the inductor current with a change in the load condition.

#### **VII. CONCLUSION**

This study introduced a triple-phase shift power-level controller that could independently control active and reactive powers in single-phase dual active bridge DC-DC converters. The proposed controller was developed by employing the fundamental components of current and voltages of the converter in a *dq* rotating reference frame. Phase shifts *d*<sub>1</sub> and *d*<sup>3</sup> were calculated from the voltage command vector, which was determined by calculating the intersection of the active and reactive powers in the *dq* voltage plane. To achieve zero reactive power across all load conditions, an empirical formula was presented to calculate the necessary maximum leakage inductance. The phase shift  $d_2$  was actively manipulated to ensure zero reactive power according to the active power demand. The proposed controller provided control partitioning for active and reactive powers in the converter and achieved better efficiency and a lower inductor current across all load conditions.

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